PIER Graduate Week 2017

Nano-Optics of low dimensional semiconductor structures

Lecture 1: Quantum Optics with Quantum Dots

Martin Kroner

Quantum Photonics Group, ETH Zürich, Switzerland



Explore the nano world with optical means.

Microscopy?

Limited by diffraction limit to the wavelength. \rightarrow Not really "nano"





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Microscopy beyond the diffraction limit:

- Electron microscopy, AFM, ...
- Near field optics
- Super resolution microscopy

- ...



Explore the nano world with optical means

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Microscopy beyond the diffraction limit:

- Electron microscopy, AFM, ...
- Near field optics
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- ...

Observe the structure of nanoscale objects

Why nano?

The physical properties of nano scale structures are governed by **quantum mechanics.**

We do not need to "see" the nano structure to explore its physical properites.

I.e. Quantum size effect.





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Optically create, manipulate and probe quantum, states of light and matter:

- Explore and test quantum mechanics.
- Study interactions of light and matter.
- Observe new states of matter and explore their properties.



Natural quantum system

But: Difficult to control and to couple

Nano technology:

Construct a quantum system with atom-like properties in a solid state environment: Quantum Dot

Requirement: Energy level spacing larger than $k_{\rm B} T$

www.kutl.kyushu-u.ac.jp



Harmonic approximation:

Energy level separation $\Delta E = \hbar \omega$

s-state Electron wave function

$$\psi(r) = rac{1}{\sqrt{\pi}l_{ ext{e}}} \exp\left(-rac{r^2}{2l_{ ext{e}}^2}
ight)$$

With the effective length

$$l_{
m e} = \sqrt{rac{\hbar}{m^{\star}\omega}}$$

I.e.: In GaAs:
$$m^{\star}=0.07m_{
m e}$$

- $l_{\rm e} = 10 {\rm nm} \rightarrow T \le 126 {\rm K}$
- $l_{\rm e} = 100 {\rm nm} \rightarrow T \leq 1.2 {\rm K}$

In reality temperatures must be smaller by approximately a factor of 10.

R. J. Warburton, PRB 58, 16221 (1998)

Optically Active Quantum Dots – From Atoms to Bands



Optically Active Quantum Dots – From Bands to Discrete States



Quantized states for electrons due to nano structuring



$$W_{\mathrm{i}
ightarrow\mathrm{f}}=rac{\pi}{2\hbar}\left|\langle i|H_{\mathrm{int}}|f
angle
ight|^{2}\delta(E_{\mathrm{f}}-E_{\mathrm{i}}-\hbar\omega)$$

Dipole interaction Hamiltonian:

$$H_{\rm int} \sim \epsilon \mathbf{p}$$
 ϵ = Polarization

Wave function:

$$|arphi
angle = |{
m Env}
angle |{
m Bloch}
angle |{
m Spin}
angle$$

Only Bloch part of the wave function changes.



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angle$$

Only Bloch part of the wave function changes.

i.e:
$$egin{aligned} |arphi_{
m e}
angle &= |1/2,+1,2
angle &= |s
angle|\uparrow
angle \ |arphi_{
m ehh}
angle &= |3/2,+3/2
angle &= -rac{1}{\sqrt{2}}\left(|x
angle+{
m i}|y
angle
ight)|\uparrow
angle \end{aligned}$$

Matrix elements of dipole operator:

$$\langle x|p_x|s
angle = \langle y|p_y|s
angle = \langle z|p_z|s
angle = \mathrm{i} p_z$$

$$\implies \left| \langle x + \mathrm{i} y | \frac{p_x - \mathrm{i} p_y}{\sqrt{2}} | s \rangle \right|^2 = p^2$$

Only non zero matrix element for circular polarized light

Self-Assembled Quantum Dots - Crystal structure





Stranski-Krastanov growth

Smaller lattice larger gap GaAs, Si, GaInP

- • Larger lattice constant
- smaller band gap e.g. InAs, InP, Ge

K. Eberl et. al. Physica E 9 (2001) 164 -174

Self-Assembled Quantum Dots - Crystal structure



Self-assembled growth → Size and In distribution varies over QD ensemble







R. J. Warburton, PRB 58, 16221 (1998)



Self-Assembled Quantum Dots - Photoluminescence

- Non resonant excitation (i.e. λ_{exc} =850nm).
- Relaxation of electron and holes into the QD.
- Recombination of electrons and holes:
- \implies Photo emission.

Spectral laser filtering.



Quantization energy: $\hbar\omega_e + \hbar\omega_h \approx 30 \text{meV}$



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Size distribution over QD

ensemble.

→ Inhomogeneous broadening 10-20 meV.

 \implies Single QD spectroscopy.

Non resonant excitation:

charge fluctuations incoherent spectroscopy





Self-Assembled Quantum Dots – Cryogenic Microscopy







Diffraction Limited Microscopy



Extraction of photons:

Acceptance angle of objective: $NA = nsin(\theta) = 0.68$ $\theta = 43^{\circ}$

QD embedded in high refractive index GaAs:

$$n_{\rm GaAs} = 3.4$$

Angle of total internal reflection:

$$lpha_{
m tot} = 17^{\circ}$$

 $lpha_{
m max} = 11^{\circ}$



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Extraction of photons with SIL:

$$\mathrm{NA} = n\mathrm{sin}(heta) = 1.5$$
 $lpha_\mathrm{max} = 26^{\circ}$

Light extracted from the sample passes perpendicular through the surface of the SIL



Increase NA of the objective with solid immersion lens

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Enhance extraction efficiency by adding mirror behind QD



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Enhance extraction efficiency by adding mirror behind QD

Enhance light matter coupling by embedding the QD into a cavity



With optimal coupling the collection efficiency can reach more than 10%

High Photon Extraction Efficiency from QDs



Collection efficiency >90% A. Dousse, APL (2009).



Collection efficiency 21% A. Kaganskiy, ArXiv 1708.03512 (2017).



Collection efficiency of 72%. J. Claudon, et al., Nature Photonics (2010).



D. Cadeddu et al., Appl. Phys. Lett. 108, 011112 (2016).



Scattering response of the QD (weak excitation):

$$\mathbf{e}_{s} = \mathbf{E}_{L} \sigma \frac{\delta \gamma + i \gamma^{2}}{\delta^{2} + \gamma^{2}}$$

Scattering cross section σ Laser detuning δ Radiative damping rate $\gamma = \frac{\Gamma}{2}$



 $\mathbf{e}_{\mathrm{s}} = \mathbf{e}_{\mathrm{coh}} + \mathbf{e}_{\mathrm{incoh}}$

Coherently scattered light can interfere with laser light:

$$\Delta T = |\mathbf{E}_{\mathrm{L}}|^{2} + 2\mathbf{e}_{\mathrm{coh}}\mathbf{E}_{\mathrm{L}} + |\mathbf{e}_{\mathrm{coh}}|^{2}$$

Transmission contrast:

$$\frac{\Delta T}{T} \approx 2 \mathbf{e}_{\mathrm{coh}} \mathbf{E}_{\mathrm{L}} \sim \sigma \frac{\gamma^2}{\delta^2 + \gamma^2}$$





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Self-Assembled Quantum Dots - Charge tunable Quantum Dots



Self-Assembled Quantum Dots - Charge tunable Quantum Dots



Charge of QD changes exciton energy \implies map out charge state by PL.



Typical Coulomb energies:

 $E^{ee} = 23meV$ $E^{eh} = 29meV$

Typical ionization energy:

 $E_{\rm C} = 134 {\rm m}e{\rm V}$

Length of X¹⁻ Plateau:

- RF \implies charging energy,
- PL \implies quantization energy.

(Remember: Coulomb diamonds in transport spectroscopy)

Charge of QD changes exciton energy \implies map out charge state by PL.





QD as a Single Photon Emitter





S. Strauff, et al., Nat. Phot. 27, 704 (2007)

Vision:

Quantum information and communication

Requires:

- Quantum nodes (Qubits)
- Quantum channels:
 - Quantum state transfer
 - Entanglement distribution



Quantum dots as toy model to explore these tasks

Node: Quantum dot Qubit: Electron (or hole) spin in a QD Quantum channel: Photon

H. J. Kimble, Nature 453, 1023-1030 (2008).

Single electron in a QD:

- Degenerate spin states
- Fast spin decay and decoherence



Single electron in a QD:

- Degenerate spin states
- Fast spin decay and decoherence
- ➡ Apply external magnetic field (i.e. in the QD plane)
- \implies All optical transitions allowed



Represent electron spin state on Bloch sphere Single electron in a QD:

- Degenerate spin states
- Fast spin decay and decoherence
- Apply external magnetic field (i.e. in the QD plane)
- All optical transitions allowed
- Eigenstates split by Zeeman energy



Represent electron spin state on Bloch sphere



Spin initialization and measurement by resonant pumping.



X. Xu PRL 99, 097401, (2007).

Send short, detuned, circular polarized laser pulse.



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In z-basis: Laser leads to ac-Stark shift.





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In z-basis: Laser leads to ac-Stark shift. ➡→ Effective magnetic field in zdirection.

 \implies Spin rotation around x-axis.







Send short, detuned, circular polarized laser pulse.

In z-basis: Laser leads to ac-Stark shift. Effective magnetic field in zdirection.

 \implies Spin rotation around x-axis.

Rotation angle depends on pulse shape. (i.e. pulse power, pulse duration)







Larmor frequency: $\omega = g \mu_{
m B} B / \hbar$

Rabi oscillations and Larmor precession:

 \implies Complete coherent control

D. Press Nature Phot. 4, 367, (2010).

- \implies Spin photon entanglement
- Initialize into state $|\downarrow\rangle_x$



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- Resonant laser pulse creates population of state $|\uparrow\downarrow\uparrow\rangle_x$

 \implies Decay with equal probability into $|\uparrow\rangle_x$ or $|\downarrow\rangle_x$ By emitting either a "red" or "blue" photon.

Spin photon entangled state:



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Spin photon entangled state:

- Measure photon and spin state



W.B. Gao Nature 491, 426, (2012).

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Spin photon entangled state:

$$|\Psi
angle = \frac{1}{\sqrt{2}} \left(|\downarrow
angle_x |\omega_{
m red}, H
angle + {
m i}|\uparrow
angle_x |\omega_{
m blue}, V
angle
ight) | |\uparrow\downarrow\Downarrow
angle_x -$$

- Measure photon and spin state

Low detection probability of the photon ($\sim 0.1\%$) \implies Heralded spin photon entanglement





W.B. Gao Nature **491**, 426, (2012).





W.B. Gao Nature 491, 426, (2012).

Spin-Spin Entanglement

Entanglement of two distant (hole) spins:

Two identical QDs each holding one hole.

 \implies Generate an entangled photon-hole pair in each QD

 \implies Entangle the two photons

 \implies Entanglement of the two hole spins.



Spin-Spin Entanglement



Measure classical correlations between the two hole spins:

1: Spin initialization

- 2: Entanglement generation
- 3: Spin measurement in QD1
- 4: Spin measurement in QD2

(in the x-basis)

Measure quantum correlations between the two hole spins:

1: Spin initialization 2: Entanglement generation 3: Phase shift on spin in QD 1 4: Spin measurement in QD1 and QD2 (in the x-basis)



Pulse duration (a.u.)