

Conventional neutrino oscillations

- Conventional approach to neutrino oscillations relies on a number of assumptions:

- Flavor state is a superposition of mass states with identical energies:

$$|\nu_\alpha\rangle = \sum_{i=1}^3 V_{\alpha i}^* |\nu_i(p)\rangle$$

- Production and detection processes occur coherently.
- Mass states travel at speed of light.
- This leads to the extensively experimentally studied oscillation probability

$$P_{\alpha\beta}(L) = \sum_{i,k=1}^3 V_{\alpha i}^* V_{\beta i} V_{\beta k}^* V_{\alpha k} \exp\left(-2\pi i \frac{L}{L_{ik}^{\text{osc}}}\right), \quad L_{ik}^{\text{osc}} = \frac{4\pi E}{\Delta m_{ik}^2}$$

- There are internal inconsistencies within this approach:
 - Distance L can't be defined with delocalized states.
 - The coherence of production and detection should be proven.
 - Equal energy assumption is not Lorentz-invariant.

Neutrino oscillation with wave packets

- The issues above can be addressed when one considers neutrino flavor state as coherent superposition of mass states with different momenta:

$$|\nu_i(k)\rangle \rightarrow \int \frac{dk}{2\pi} f(k, p, \sigma^2) |\nu_i(k)\rangle$$

- Assuming form factor is Gaussian the oscillation probability reads:

$$P_{\alpha\beta}(L) = \sum_{k,j=1}^3 \frac{V_{k\beta} V_{\alpha k}^* V_{j\alpha} V_{\beta j}^*}{\sqrt{1+(L/L_{kj}^d)^2}} \exp\left[-\frac{(L/L_{kj}^{\text{coh}})^2}{1+(L/L_{kj}^d)^2} - D_{kj}^2\right] e^{-i(\varphi_{kj} + \varphi_{kj}^d)}$$

$$\varphi_{kj}^d = -\frac{L/L_{kj}^d}{1+(L/L_{kj}^d)^2} \left(\frac{L}{L_{kj}^{\text{coh}}}\right)^2 + \frac{1}{2} \arctan \frac{L}{L_{kj}^d}, \quad \varphi_{kl} = 2\pi \frac{L}{L_{kl}^{\text{osc}}}$$

- $\sigma_{\text{rel}} = \sigma_p/p$ is the relative momentum dispersion of wave packet. σ_p is the intrinsic momentum dispersion of wave packet. It depends on the kinematics of production and detection processes. In this work $\sigma_p = \text{const}$ is assumed.
- $L^{\text{coh}} = \frac{L_{kj}^{\text{osc}}}{\sqrt{2\pi}\sigma_{\text{rel}}}$ is **coherence length**. At this distance separation of wave packets due to different group velocities suppresses interference between mass states.
- $L_{kj}^d = \frac{L_{kj}^{\text{coh}}}{2\sqrt{2}\sigma_{\text{rel}}}$ is **dispersion length** of wave packet. At this distance coherence between mass states is partially restored due to spacial broadening of wave packet.
- $D_{kj}^2 = \frac{1}{2} \left(\frac{\Delta m_{kj}^2}{4p^2\sigma_{\text{rel}}}\right)^2$ suppresses the coherence of mass states due to spacial localization of production and detection regions.

What do we know about σ_p ?

- No first principle QFT calculations.
- Only phenomenological estimates such as:
 - $\sigma_p \sim 1 \text{ MeV}$, $\sigma_x \sim 10^{-11} \text{ cm}$ — uranium atom size;
 - $\sigma_p \sim 1 - 10 \text{ keV}$, $\sigma_x \sim 10^{-8} - 10^{-7} \text{ cm}$ — atomic scale;
 - $\sigma_p \sim 0.1 \text{ eV}$, $\sigma_x \sim 10^{-4} \text{ cm}$ — pressure broadening.
- Lack of experimental studies.

Reference

- Study of the wave packet treatment of neutrino oscillation at Daya Bay, Eur.Phys.J. C77 (2017), 606

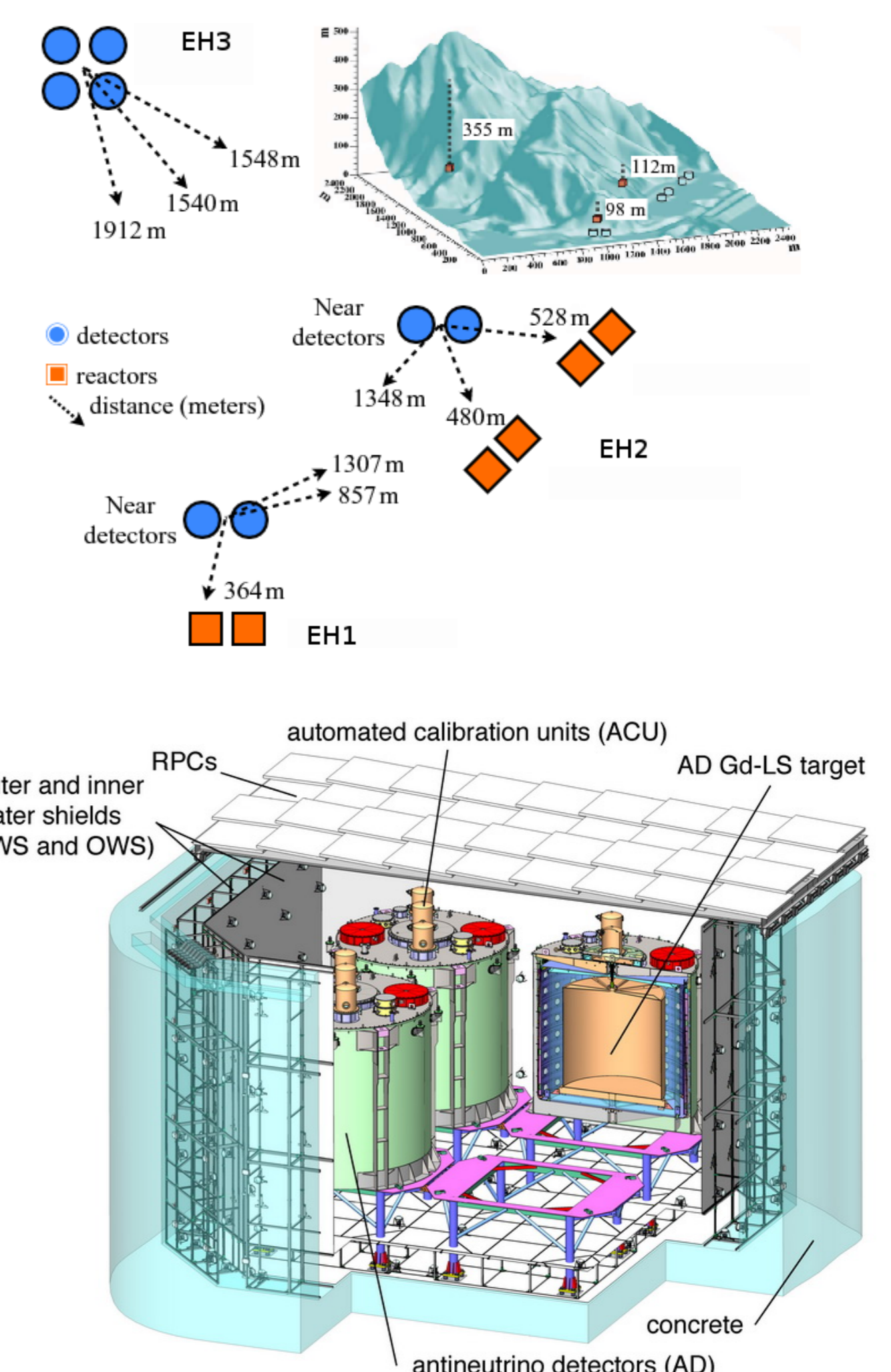


Daya Bay setup

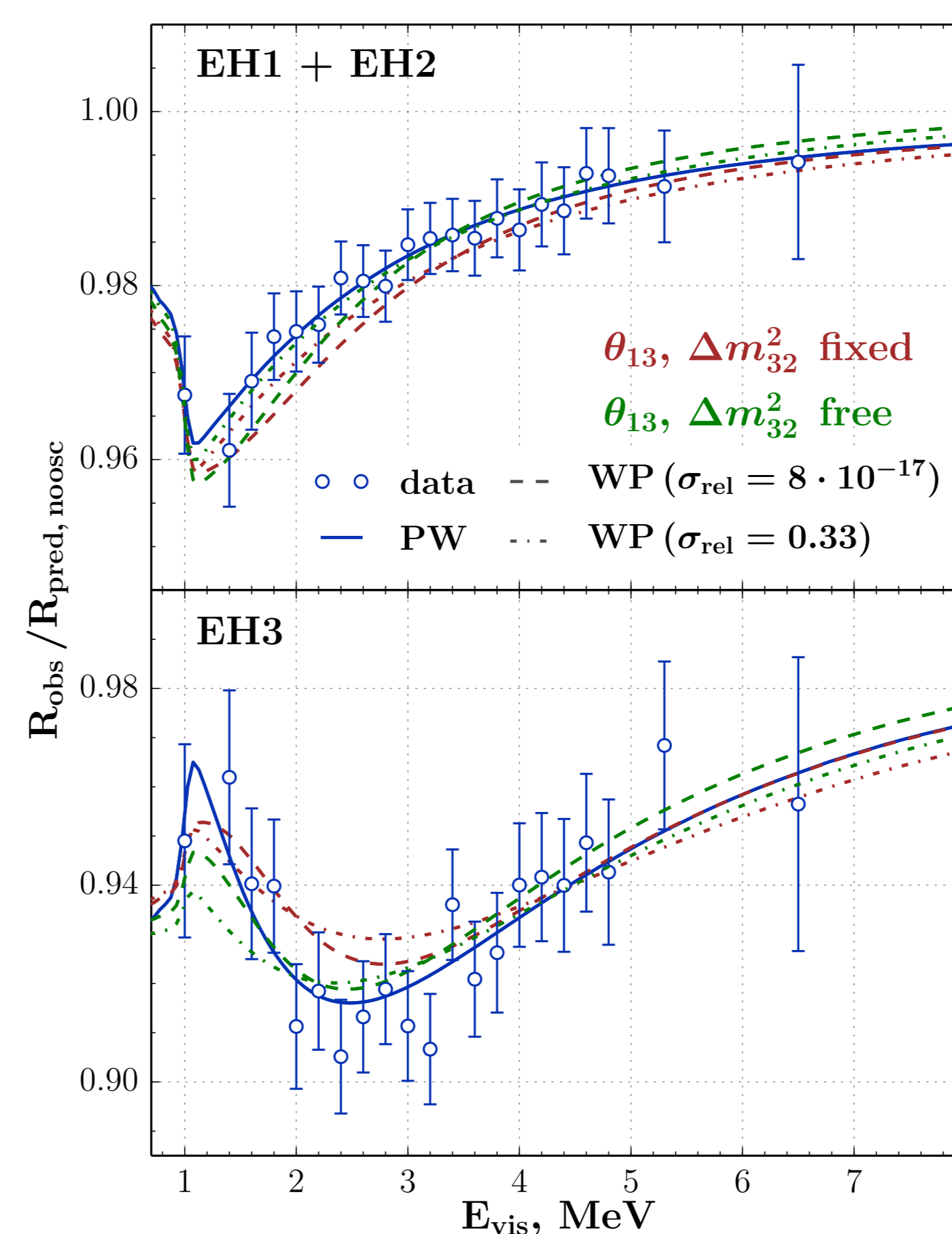
- 8 detectors each with 20 tons of Gd-doped liquid scintillator.
- 6 nuclear reactors each with 2.9 GW of thermal power.
- $\bar{\nu}_e$ detection through IBD
 $\bar{\nu}_e + p \rightarrow e^+ + n$
- Use coincidence of prompt and delayed signals in time to select $\bar{\nu}_e$ events.
- $\bar{\nu}_e$ sample based on 621 days:

	EH1	EH2	EH3
Events	613813	477144	150255

- Energy resolution $\sim 8\%$ at 1 MeV.



Statistical method



Test statistic is defined as:

$$\chi^2 = (\mathbf{d} - \mathbf{t}(\boldsymbol{\eta}))^T \mathbf{V}^{-1} (\mathbf{d} - \mathbf{t}(\boldsymbol{\eta}))$$

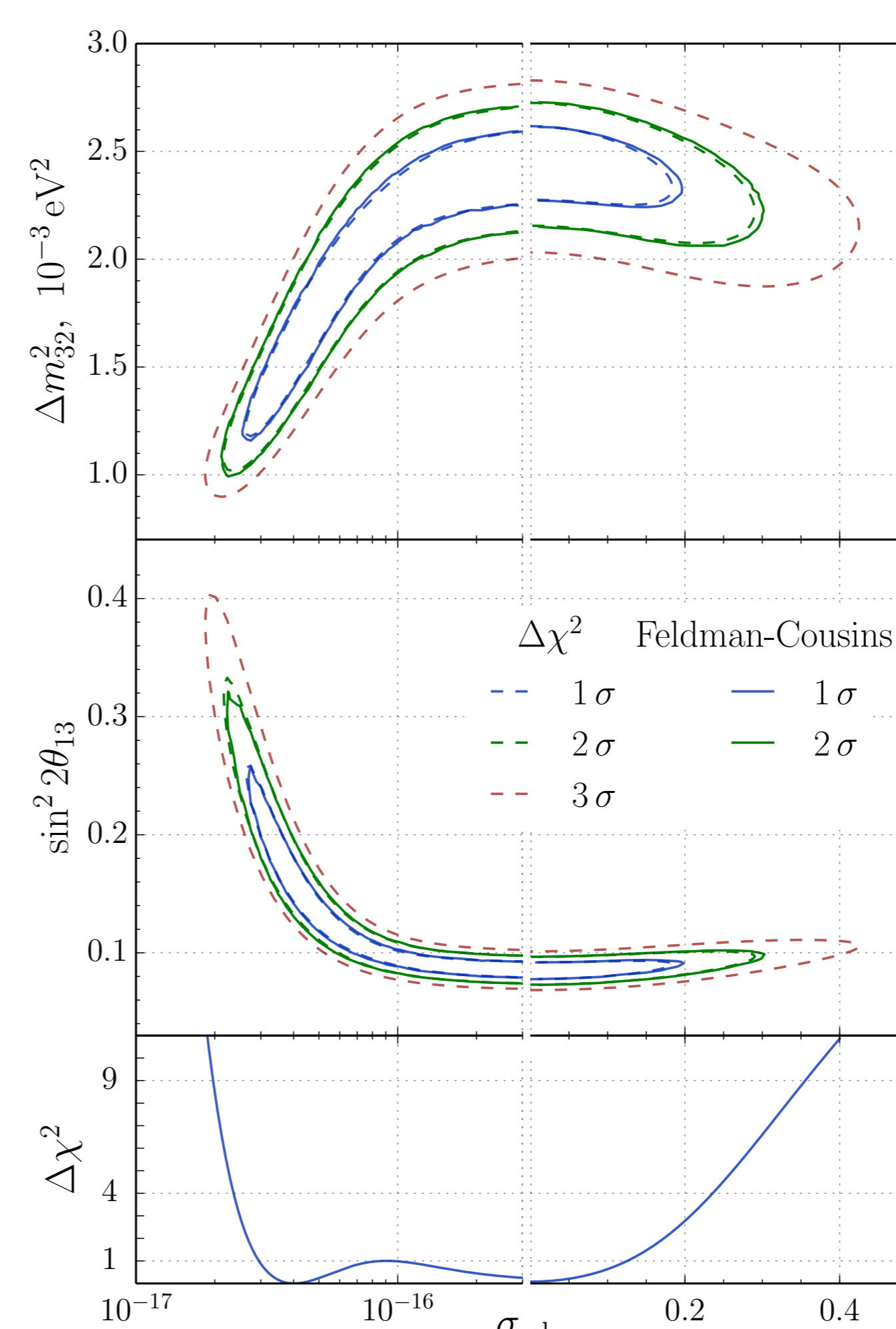
- Free parameters:

- σ_{rel}
- $\sin^2 2\theta_{13}$
- Δm_{32}^2
- Flux normalization N

- Systematical uncertainties are propagated via covariance matrix \mathbf{V} .

- Confidence levels are constructed via **fixed-level $\Delta\chi^2$** and **Feldman-Cousins** methods.

Results and Discussion



- There are 3 distinct regions on σ_{rel} :

- $\sigma_{\text{rel}} < 10^{-16}$ – oscillations are suppressed by D^2 .
- $10^{-16} < \sigma_{\text{rel}} < 0.1$ – no impact on oscillations.
- $\sigma_{\text{rel}} > 0.1$ – loss of coherence due to spacial separation L^{coh} and dispersion L^d .

- Allowed region for σ_{rel} at 95% C.L.:

$$2.38 \cdot 10^{-17} < \sigma_{\text{rel}} < 0.232$$

- The lower limit can be improved with constraints from reactor cores and detector dimensions. Combined limits are:

$$10^{-11} \text{ cm} \lesssim \sigma_x \lesssim 2 \text{ m}$$

- The upper limit on σ_{rel} is

$$\sigma_{\text{rel}} < 0.2 \text{ at } 95\% \text{ C.L.}$$

Conclusion

- First experimental limits on σ_{rel} are obtained.
- Insignificance of decoherence effect ensures unbiased measurement of oscillation parameters using the standard approach in Daya Bay.