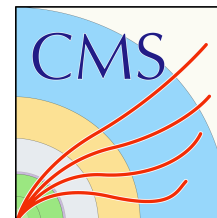


# W mass and transverse momentum measurements at the LHC

Samuel Webb

on behalf of the ATLAS and CMS Collaborations



Johannes Gutenberg University Mainz

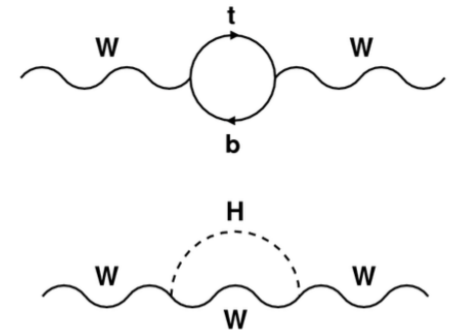
[samuel.webb@cern.ch](mailto:samuel.webb@cern.ch)

- Introduction to W mass measurements at the LHC
  - Focus on **ATLAS 7 TeV result**
    - issues affecting **hadronic recoil resolution**
      - for transverse mass template fits
    - and affecting **lepton  $p_T$  modelling**
      - theoretical model for W  $p_T$  spectrum
- How future experimental uncertainty could be reduced
  - Measuring W  $p_T$  in low pile-up environment
- Summary

# W mass introduction

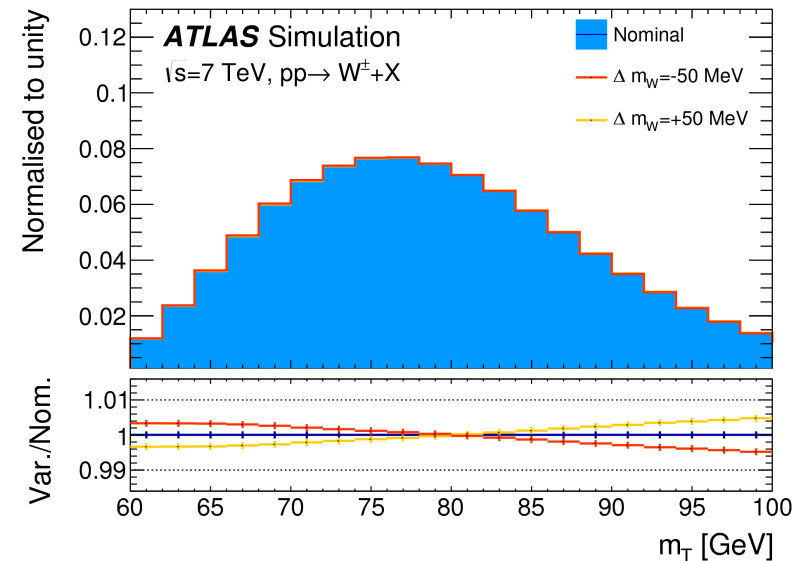
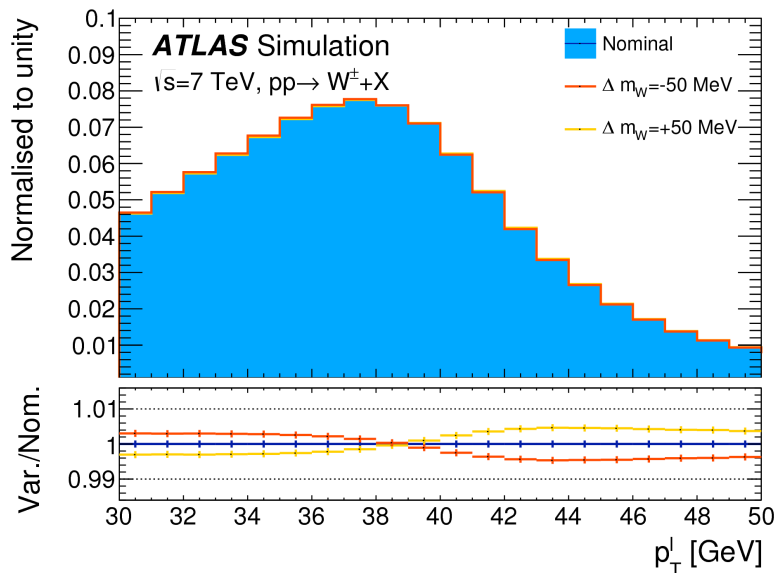
- Theoretical uncertainty on W boson mass smaller than world average experimental
  - 8 MeV compared to 15 MeV
  - potential to constrain new physics
  - improve understanding of PDFs and higher order corrections

$$m_W^2 \left( 1 - \frac{m_W^2}{m_Z^2} \right) = \frac{\pi \alpha}{\sqrt{2} G_\mu} (1 + \Delta r)$$



- Measurements at LHC strongly affected by uncertainties on strange and charm quark PDF
  - 25% of W's induced by charm and strange - 5% at Tevatron
- However larger statistics at LHC
  - allows a more precise detector calibration

- Currently one published measurement of the W boson mass at the LHC
  - ATLAS @ 7 TeV - *Eur. Phys. J. C 78 (2018) 110*
- Template fit method in two kinematic variables
  - $p_T$  of decay lepton (e or  $\mu$ ), W transverse mass



- Also separated by  $W^+$ ,  $W^-$ , and bins of lepton  $\eta$
- 28 categories total

- A large number of systematic sources to consider, each with many sub-contributions
  - Statistical uncertainties
  - Experimental calibration
    - Muon calibration
    - Electron calibration
    - Recoil calibration
  - Electroweak and multi jet background modelling
  - Physics modelling uncertainties
    - fixed order prediction
    - higher order EW corrections
    - PDF modelling

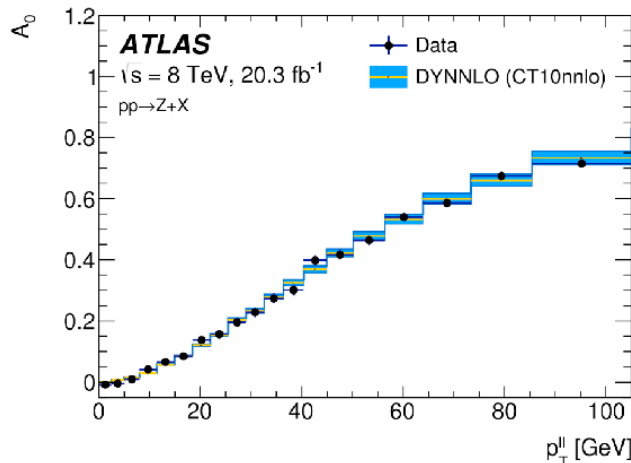
**All of these have to be carefully controlled to get a precise measurement**

- Model used for fitting obtained by re-weighting NLO MC prediction from Powhcg+Pythia to an improved higher order prediction

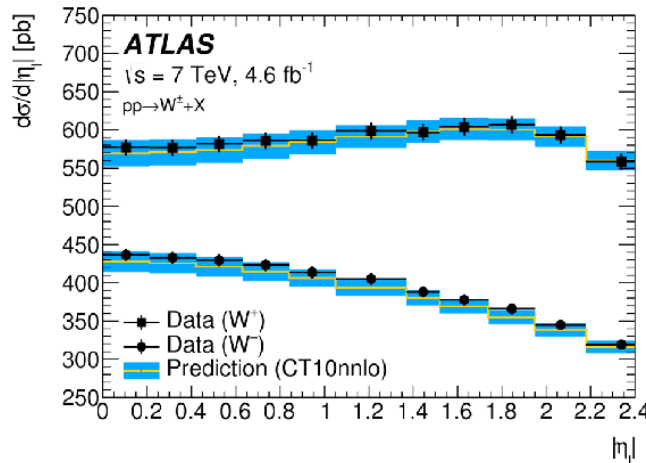
**factorisation of cross section:**



- NNLO predictions** cross-checked with published results



**$A_0$  coefficient**

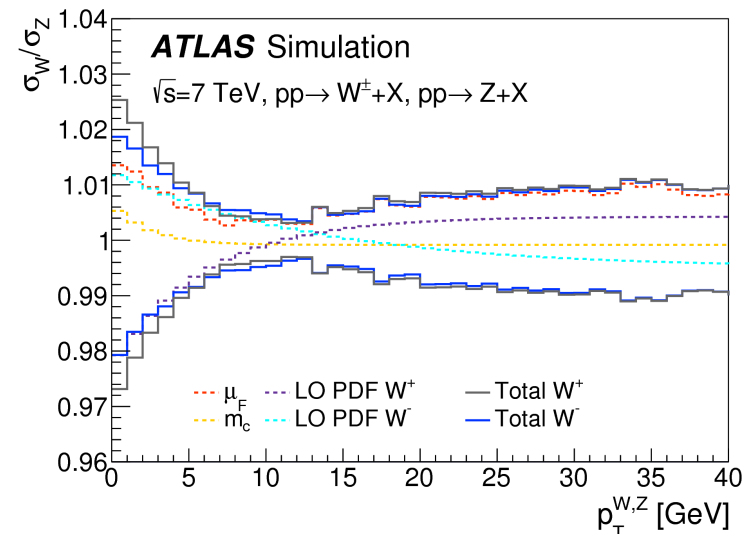
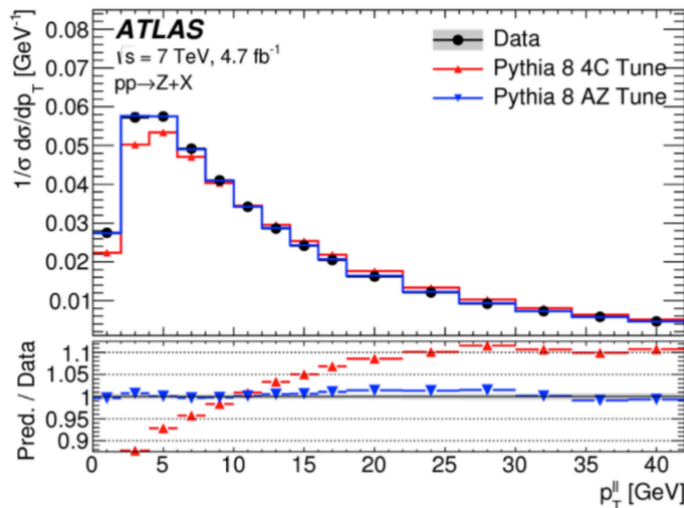


**lepton pseudorapidity (W decays)**

large uncertainty  
from PDF  
modelling for  
fixed order  
prediction  
**~8 MeV**

factorisation of  
cross section:

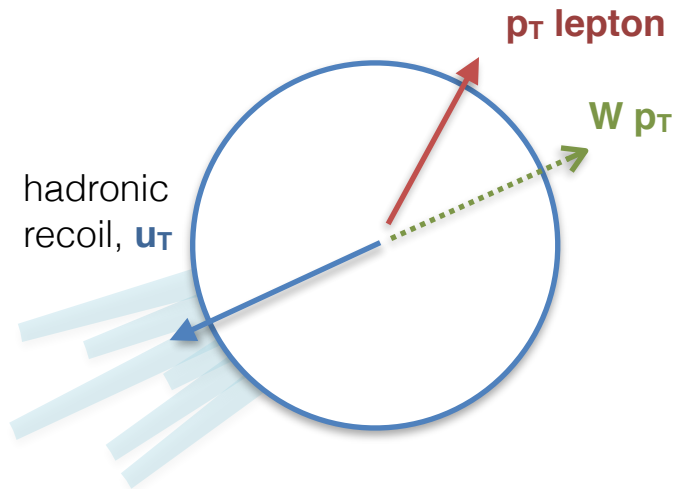
- Tune Pythia8  $p_T$  distribution using Z boson  **$p_T$  measurement** at 7 TeV
- Use Pythia8 to evaluate theory uncertainties on ratio  $W\ p_T / Z\ p_T$  (large  **$\sim 6$  MeV**)



- Transverse mass fit

$$m_T = \sqrt{2p_T^\ell p_T^{\text{miss}}(1 - \cos \Delta\phi)}$$

- depends on calibration of the hadronic recoil,  $\vec{u}_T$   $\vec{p}_T^{\text{miss}} = -(\vec{p}_T^\ell + \vec{u}_T)$



**The recoil is reconstructed from the vector sum of the transverse energy of all clusters reconstructed in the calorimeters**

- Three calibrations steps
  - correct pile-up profile in MC to match data
  - correct for residual differences in transverse energy sum distributions
  - Scale and resolution corrections from  $Z \rightarrow \mu\mu$  sample



- Transverse mass fit

$$m_T = \sqrt{2p_T^\ell p_T^{\text{miss}}(1 - \cos \Delta\phi)}$$

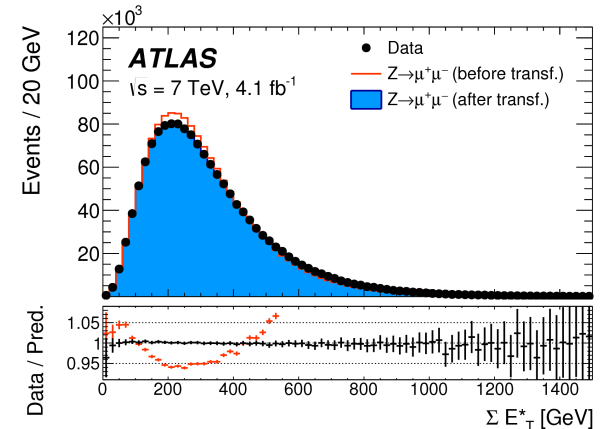
- Resolution of the hadronic recoil a limiting factor for  $m_T$  measurement - 13 MeV (total 25 MeV) -

$m_W$ [MeV]	Stat. Unc.	Muon Unc.	Elec. Unc.	<b>Recoil Unc.</b>	Bkg. Unc.	QCD Unc.	EW Unc.	PDF Unc.	Total Unc.
80375.7	9.6	7.8	5.5	13.0	8.3	9.6	3.4	10.2	25.1

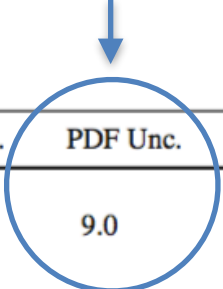


Combined W mass measurement, using transverse mass fit

- Mainly due to **transverse energy sum re-weighting** and transfer of calibration from Z events
- **pile-up** large contributing factor



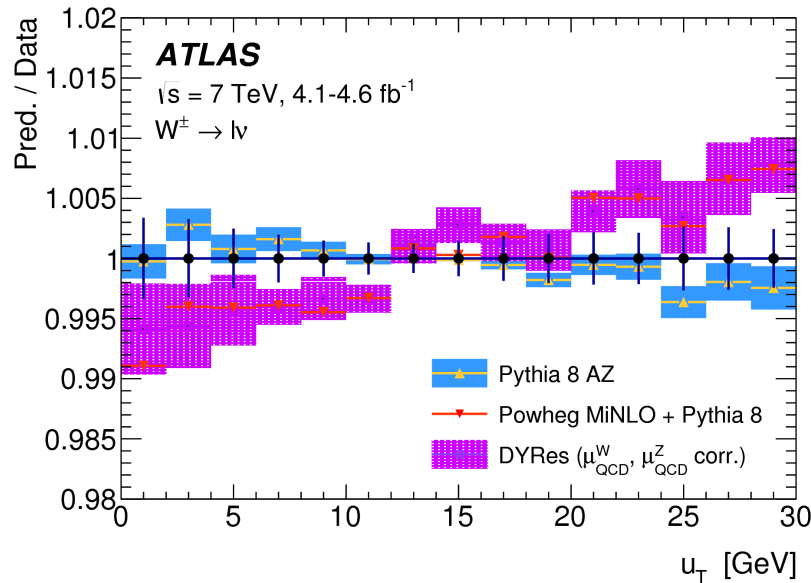
- Lepton  $p_T$  fit
  - Effect of the recoil calibration much smaller with respect to transverse mass fit
  - however strongly affected by modelling of  $W$   $p_T$  in the prediction



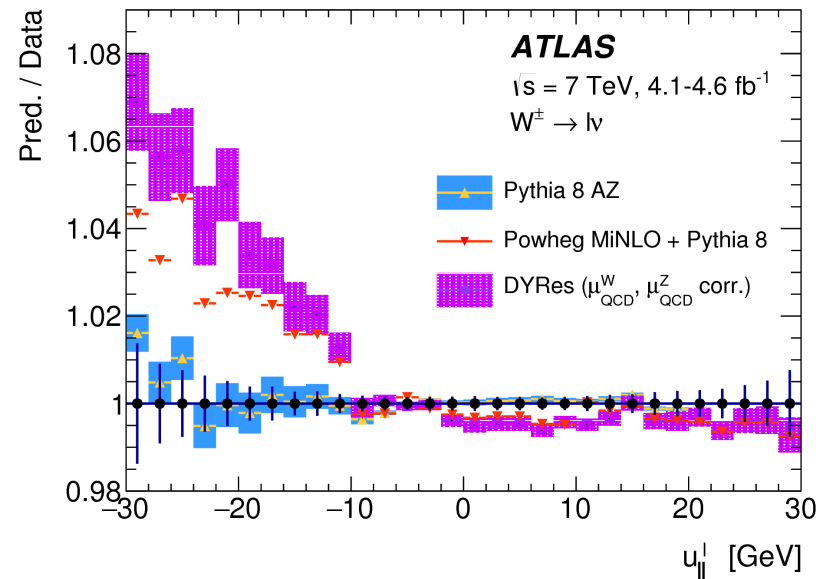
$m_W$ [MeV]	Stat. Unc.	Muon Unc.	Elec. Unc.	Recoil Unc.	Bckg. Unc.	QCD Unc.	EW Unc.	PDF Unc.	Total Unc.
80369.4	7.2	6.3	6.7	2.5	4.6	8.3	5.7	9.0	18.7

- PDF uncertainty anti-correlated between  $W^+$   $W^-$ 
  - reduced in combination

- Many tests of the  $p_T$  modelling show Pythia8 provides a good description (within the large uncertainties)

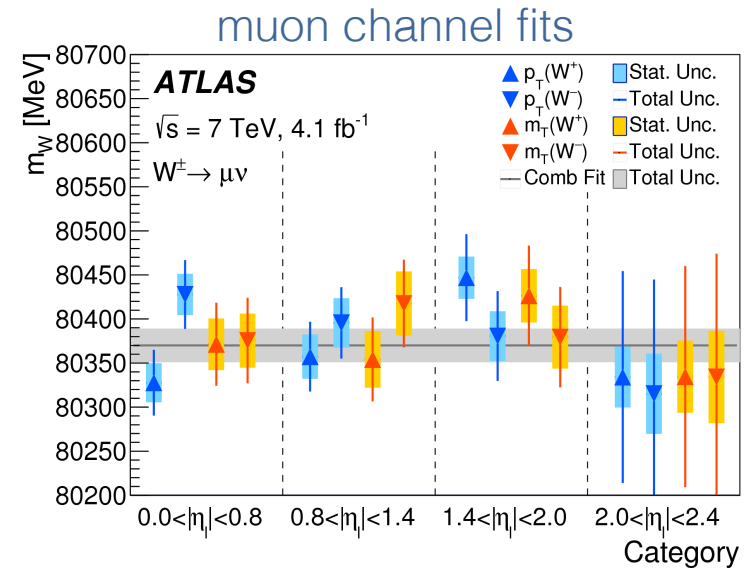
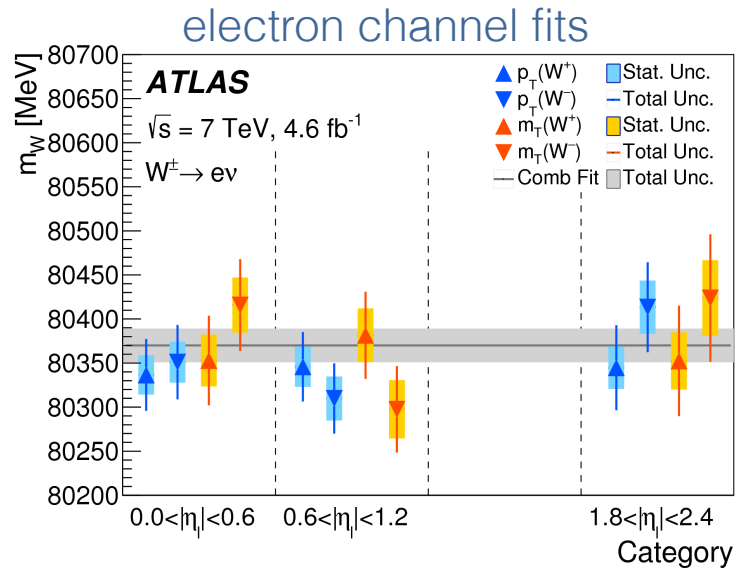


Component of hadronic recoil  
transverse to lepton direction

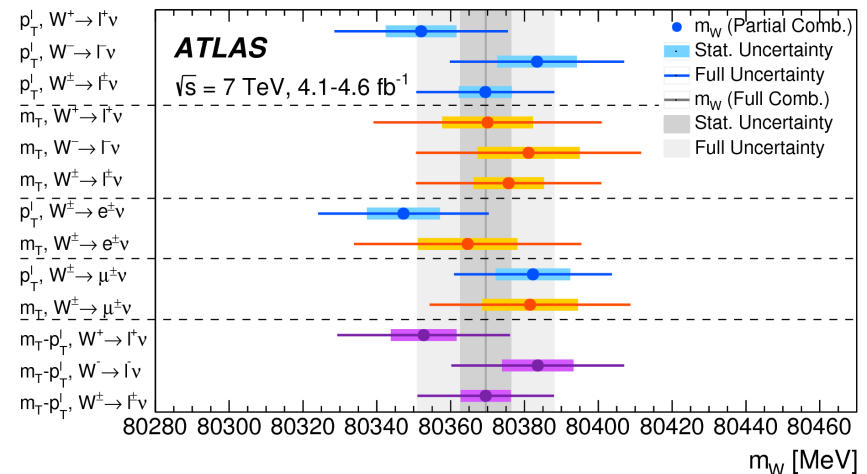


Component of hadronic recoil  
parallel to lepton direction

- NNLO+NNLL predictions do not describe data
  - due to incomplete heavy flavour treatment?



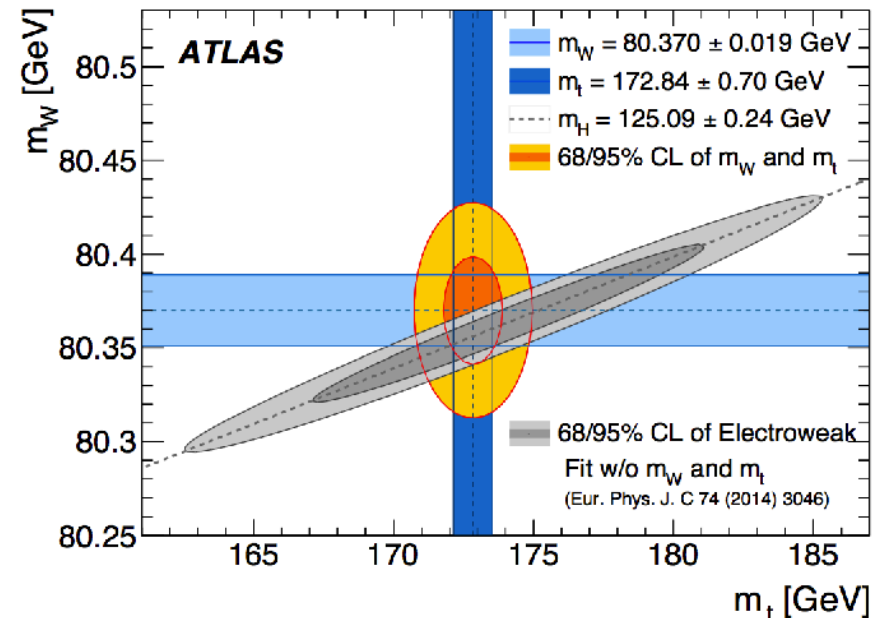
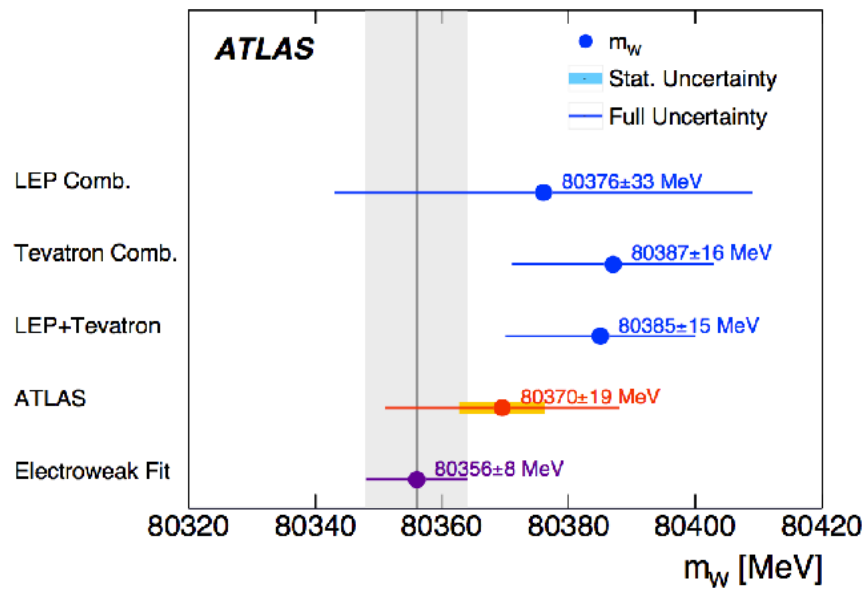
- Measurements consistent
  - in each category
  - in combinations of categories



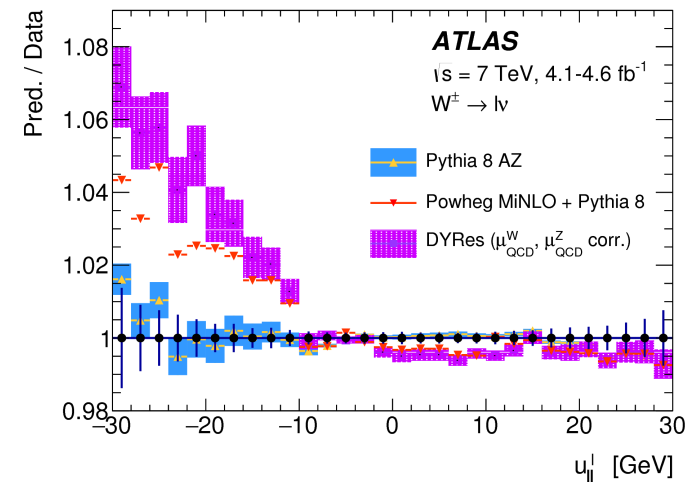
$$m_W = 80369.5 \pm 6.8(\text{stat.}) \pm 10.6(\text{exp. syst.}) \pm 13.6(\text{mod. syst.}) \text{ MeV}$$

$$= 80369.5 \pm 18.5 \text{ MeV},$$

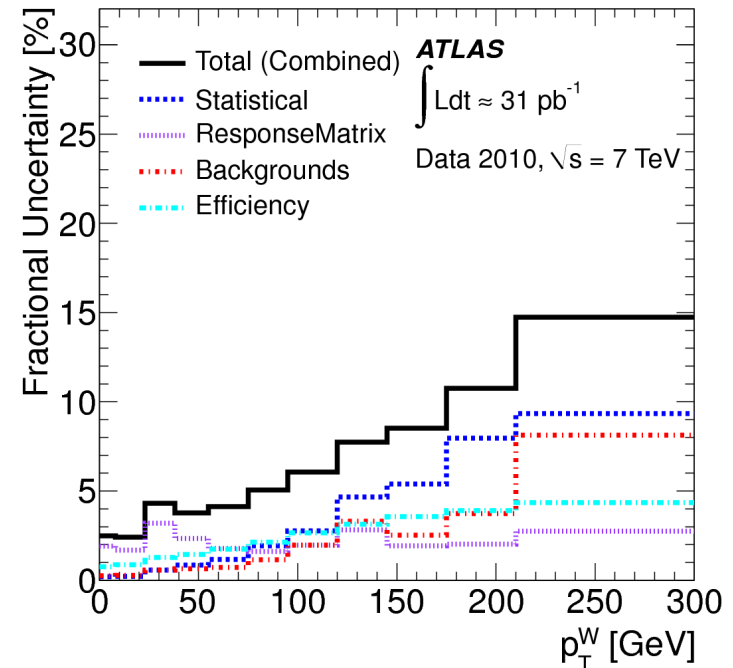
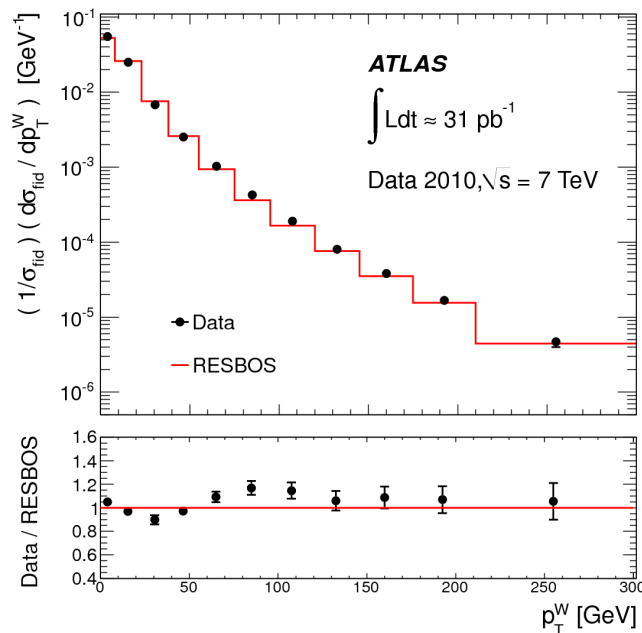
- Final result consistent with theory and previous measurements
  - Uncertainty, 18.5 MeV, dominated by physics modelling uncertainties



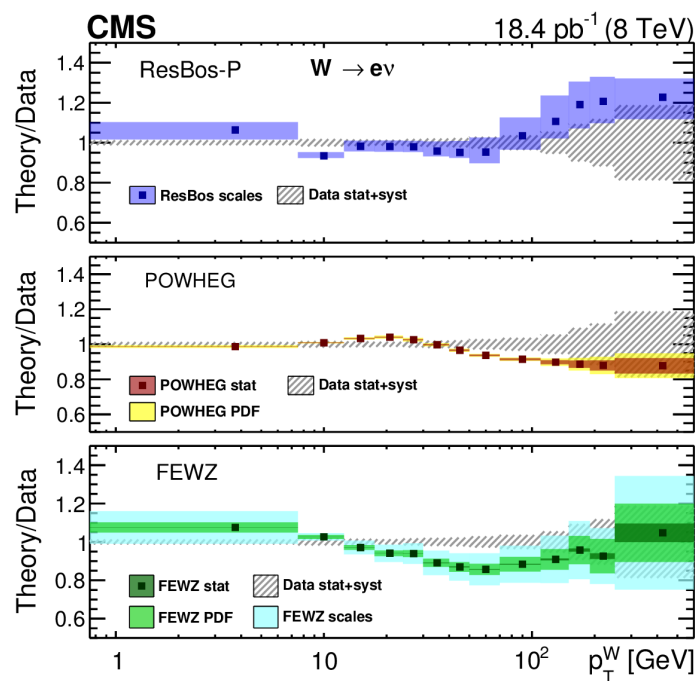
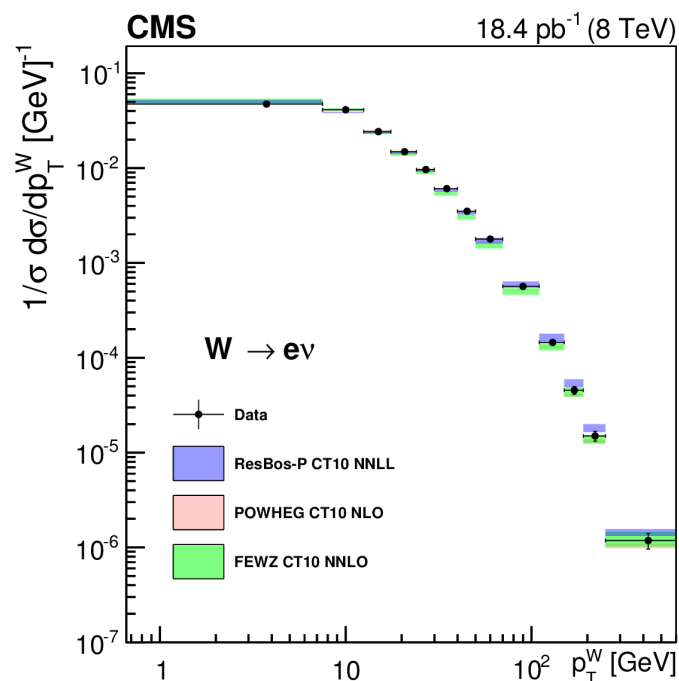
- One of the dominant uncertainties in ATLAS measurement arises from  $W$   $p_T$  modelling
  - tune Pythia8 to  $Z$   $p_T$  distribution
  - evaluate uncertainties related to the difference between  $W$  and  $Z$  transverse momentum distributions
- 1) Improve theoretical modelling of  $W$   $p_T$  and ratio between  $W$   $p_T$  and  $Z$   $p_T$ 
  - (experimental uncertainty on  $Z$   $p_T$  small)
- 2) Directly measure  $W$   $p_T$  distribution in data
  - removes the need for a transfer from  $Z$



- ATLAS 7 TeV W  $p_T$  measurement from 2010 (low pile-up,  $\mu=2$ )
  - combined electron + muon channels
  - uncertainty dominated by low statistics at high  $p_T$  (31 pb $^{-1}$ )
    - low statistics also affects efficiency and calibration sample size
    - for example for the data-driven hadronic recoil calibration



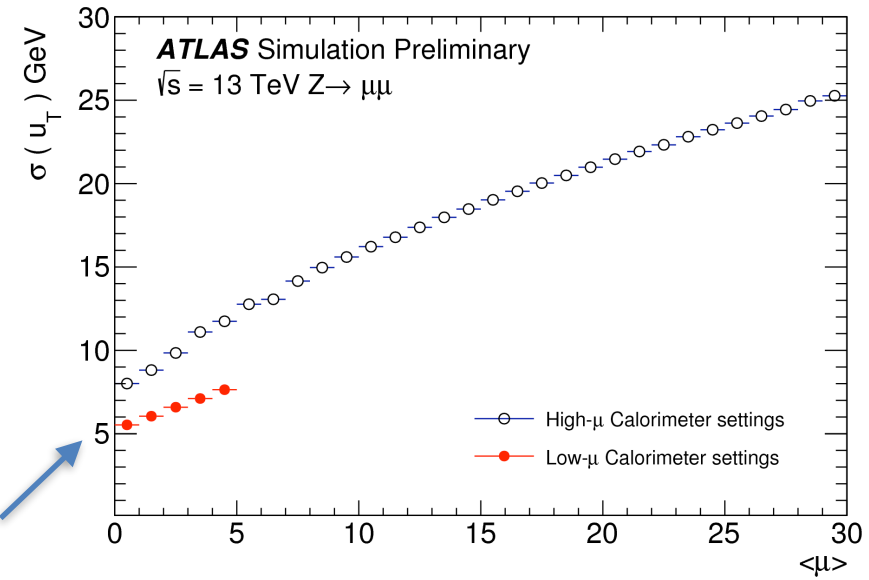
- More recent CMS 8 TeV W  $p_T$  measurement (also low pile-up,  $\mu=4$ )
  - combined electron + muon channels
  - uncertainty again dominated by low statistics at high  $p_T$  (18.4 pb $^{-1}$ )
    - as well as modelling of background from multi-jet processes





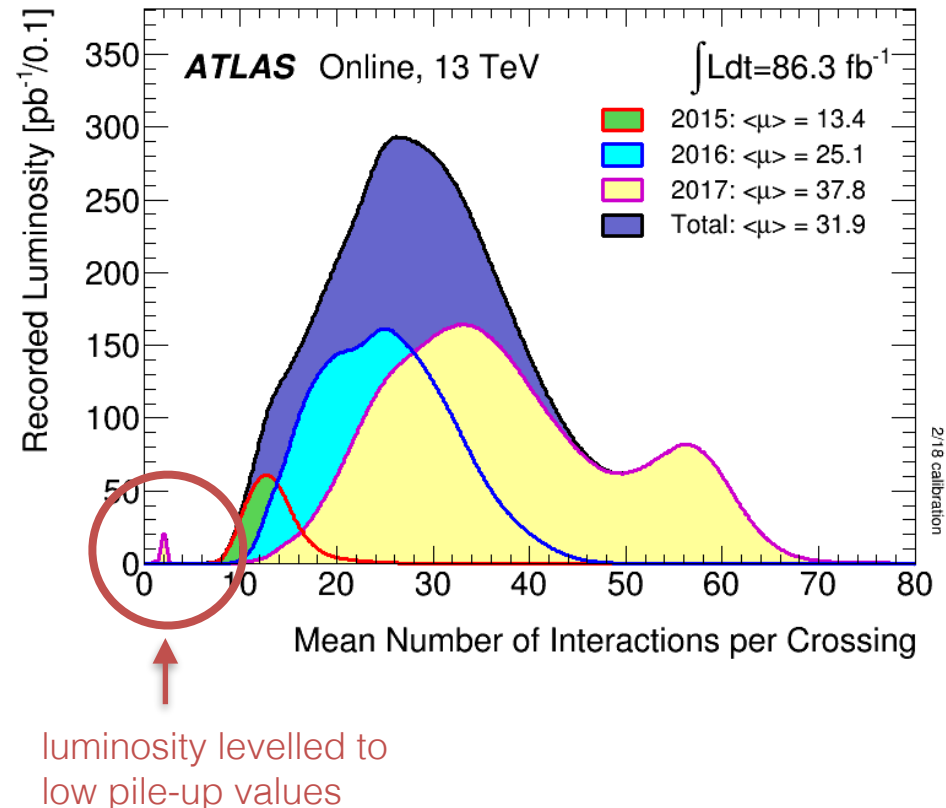
- To reduce uncertainty from  $p_T$  modelling by  $\sim$ factor of two
  - need measurements of  $W p_T$  in bin sizes of 5 GeV or less (for  $W p_T < 30$  GeV)
  - only possible if recoil resolution is comparable or better than 5 GeV

**low pile-up run required**



- In November 2017, ATLAS+CMS collected  $\sim 280$  pb $^{-1}$  of low-pile-up data at  $\sqrt{s} = 5$  TeV, and  $\sim 160$  pb $^{-1}$  at  $\sqrt{s} = 13$  TeV in each case with  $\langle\mu\rangle$  of  $\sim 2$ .
  - Many times more data than previous measurements

- The better recoil resolution may also allow for a W mass measurement in which the **transverse mass fit has a larger contribution to the final value**
  - complementary to previous measurement at 7 TeV
- W  $p_T$  measurements at 5 TeV and 13 TeV could probe how the **importance of heavy quark initiated processes** increases with centre of mass energy



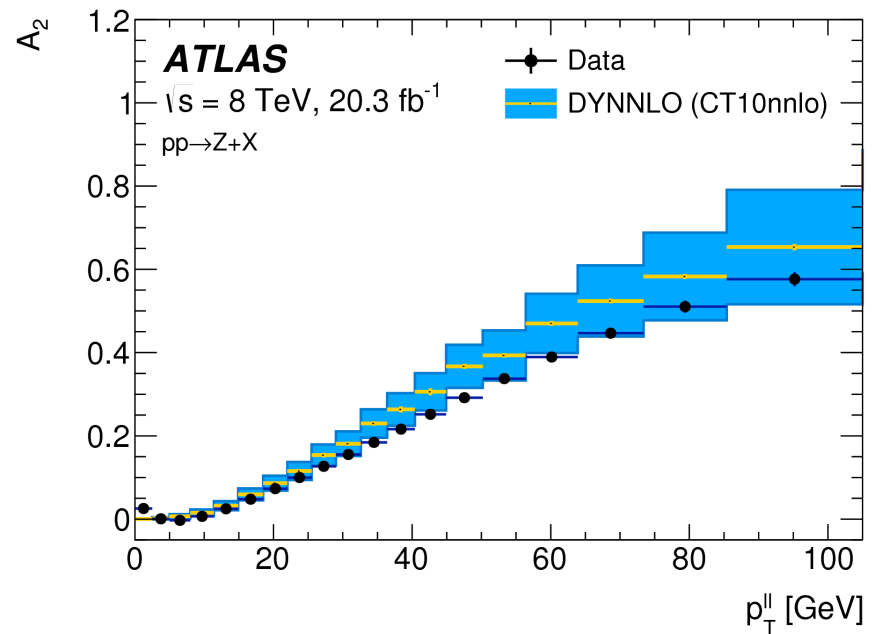
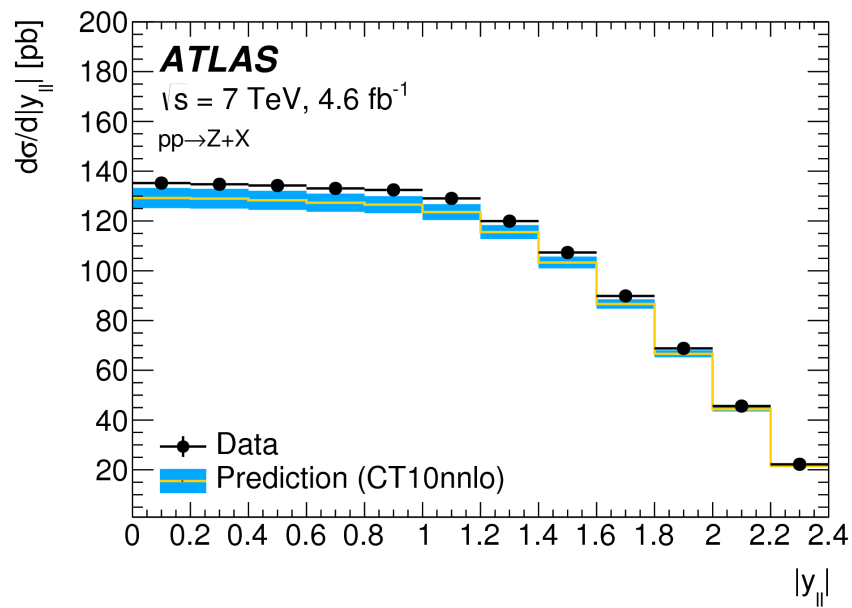
- ATLAS W mass measurement at 7 TeV reached experimental uncertainty of 18.5 MeV
  - theoretical uncertainty 8 MeV - still room to improve measurement
  - dominant uncertainties on the measurement from
    - imperfect knowledge of PDFs in fixed order prediction
    - theoretical description of  $W p_T / Z p_T$  ratio
- Uncertainties could be reduced with a direct measurement of  $W p_T$ 
  - bin sizes  $< 5$  GeV required
  - previous measurements suffered from low data statistics
  - 280 pb<sup>-1</sup> of low-pile-up data at  $\sqrt{s} = 5$  TeV, and 160 pb<sup>-1</sup> at  $\sqrt{s} = 13$  TeV now available



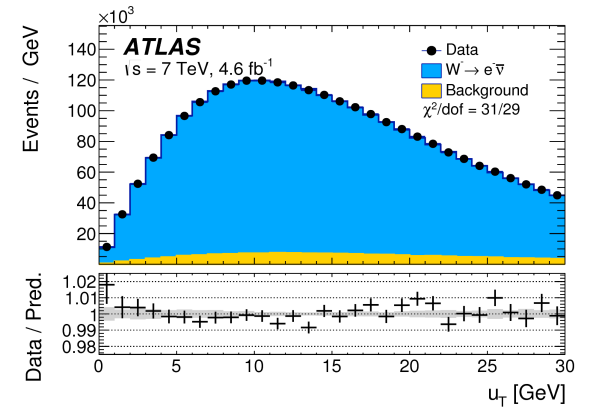
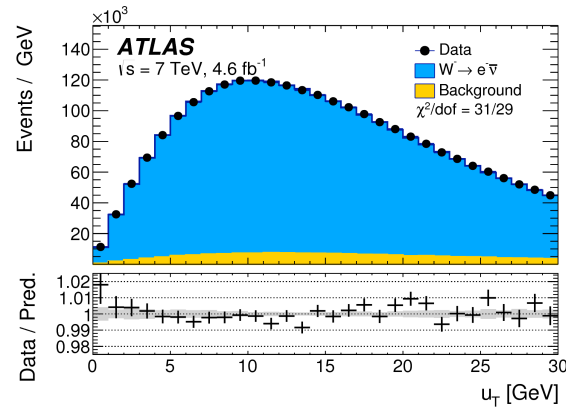
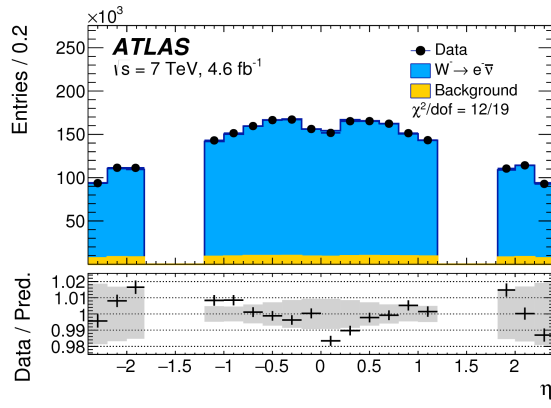
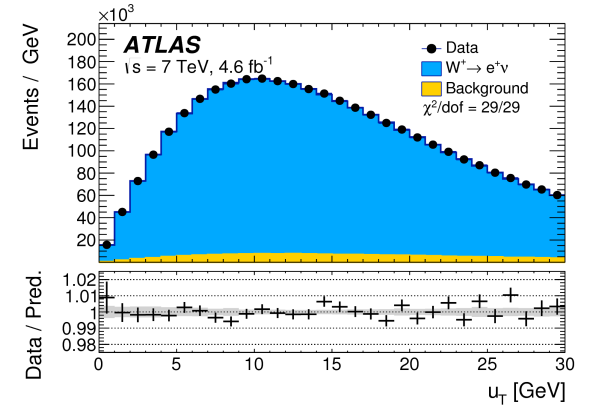
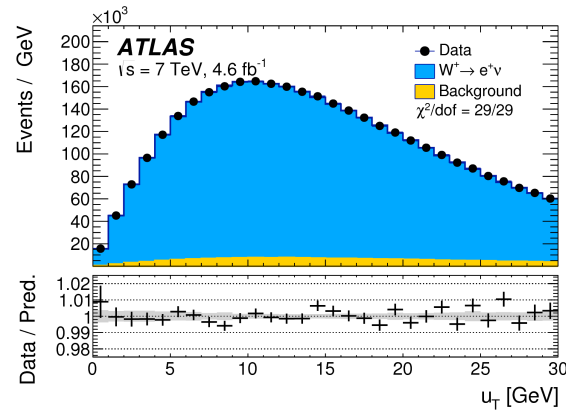
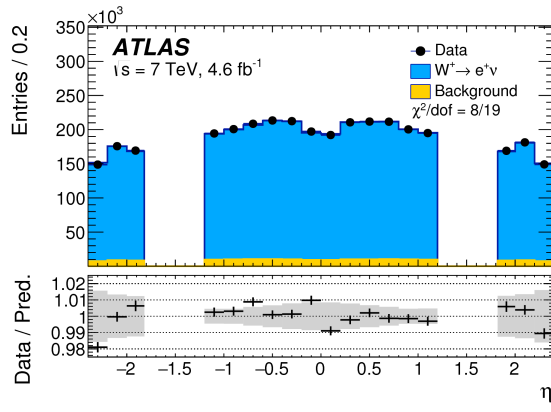
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Additional Material

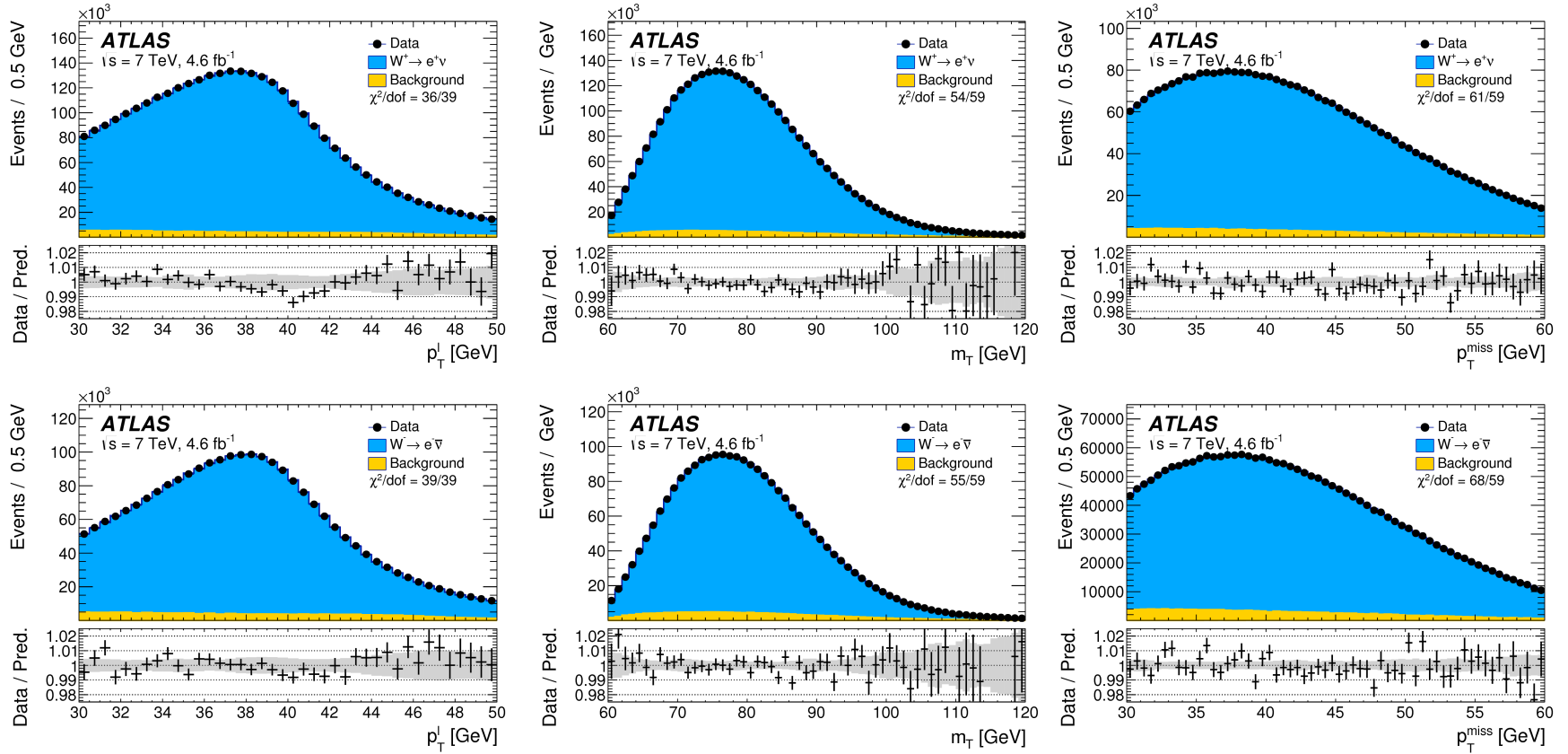
# DYNNLO predictions



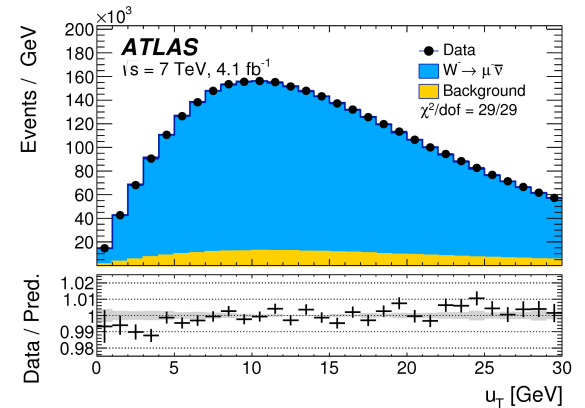
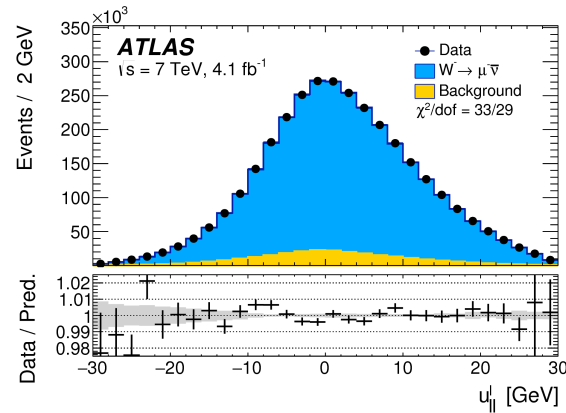
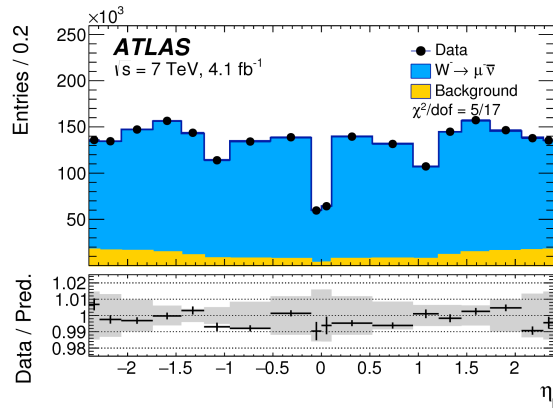
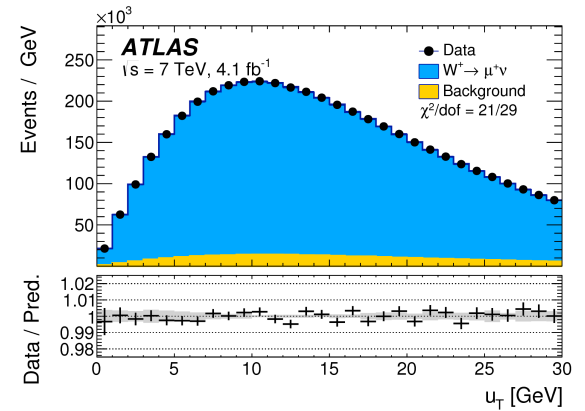
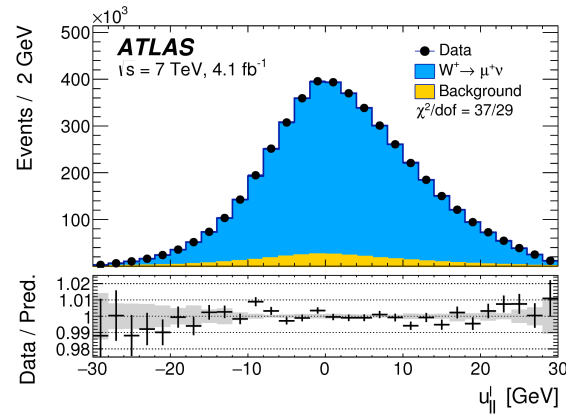
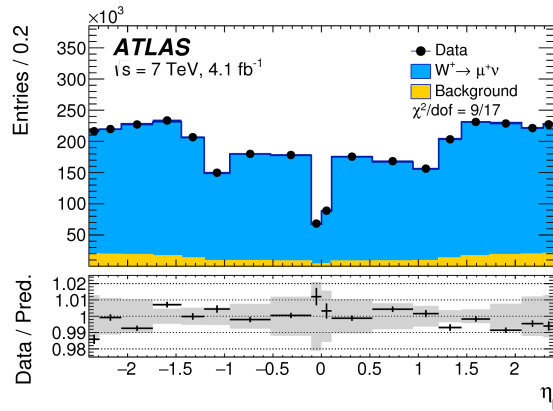
# Control distributions electron channel



# Control distributions electron channel

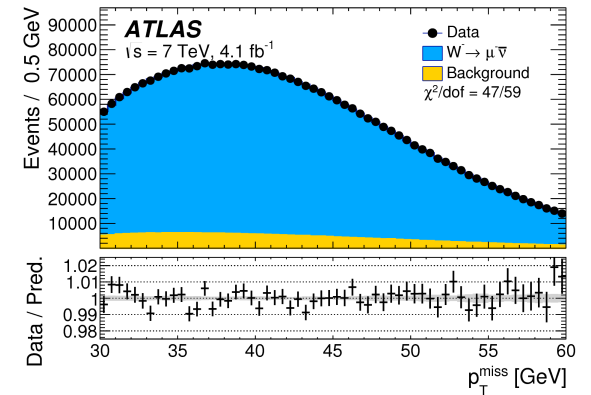
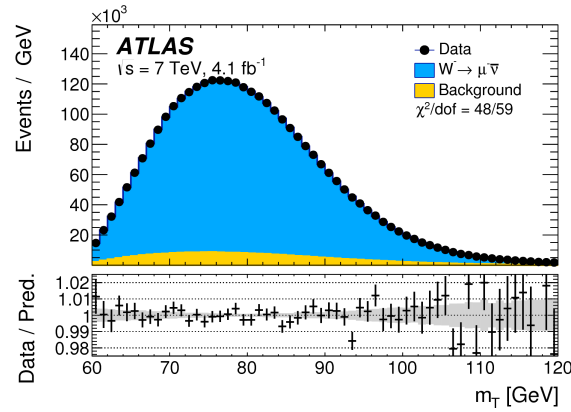
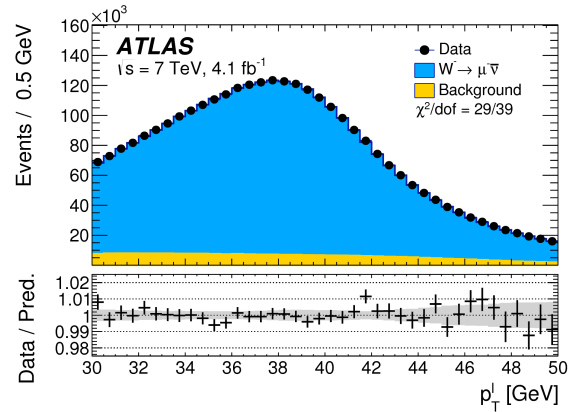
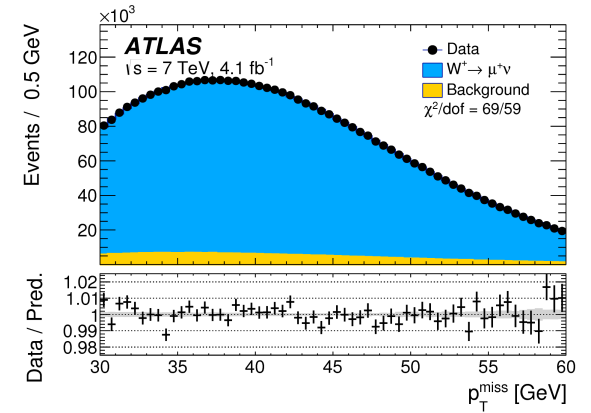
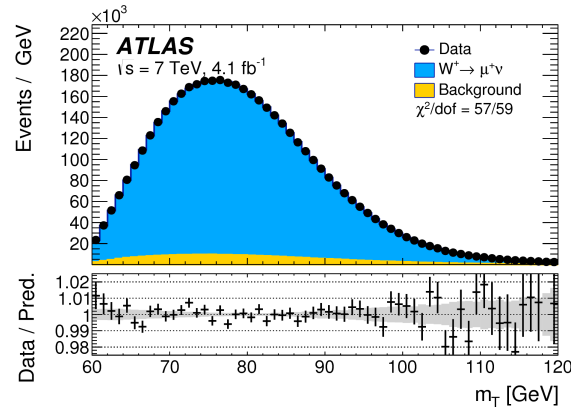
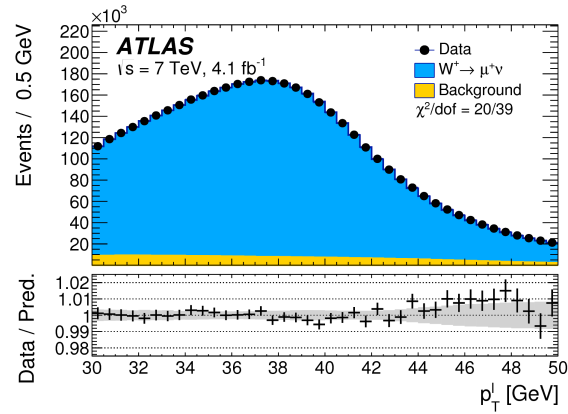


# Control distributions muon channel





# Control distributions muon channel



# Uncertainties due to QCD modelling

$W$ -boson charge Kinematic distribution	$W^+$		$W^-$		Combined	
	$p_T^\ell$	$m_T$	$p_T^\ell$	$m_T$	$p_T^\ell$	$m_T$
$\delta m_W$ [MeV]						
Fixed-order PDF uncertainty	13.1	14.9	12.0	14.2	8.0	8.7
AZ tune	3.0	3.4	3.0	3.4	3.0	3.4
Charm-quark mass	1.2	1.5	1.2	1.5	1.2	1.5
Parton shower $\mu_F$ with heavy-flavour decorrelation	5.0	6.9	5.0	6.9	5.0	6.9
Parton shower PDF uncertainty	3.6	4.0	2.6	2.4	1.0	1.6
Angular coefficients	5.8	5.3	5.8	5.3	5.8	5.3
Total	15.9	18.1	14.8	17.2	11.6	12.9

# Uncertainties due to muon calibration

$ \eta_\ell $ range	[0.0, 0.8]		[0.8, 1.4]		[1.4, 2.0]		[2.0, 2.4]		Combined	
Kinematic distribution	$p_T^\ell$	$m_T$	$p_T^\ell$	$m_T$	$p_T^\ell$	$m_T$	$p_T^\ell$	$m_T$	$p_T^\ell$	$m_T$
$\delta m_W$ [MeV]										
Momentum scale	8.9	9.3	14.2	15.6	27.4	29.2	111.0	115.4	8.4	8.8
Momentum resolution	1.8	2.0	1.9	1.7	1.5	2.2	3.4	3.8	1.0	1.2
Sagitta bias	0.7	0.8	1.7	1.7	3.1	3.1	4.5	4.3	0.6	0.6
Reconstruction and isolation efficiencies	4.0	3.6	5.1	3.7	4.7	3.5	6.4	5.5	2.7	2.2
Trigger efficiency	5.6	5.0	7.1	5.0	11.8	9.1	12.1	9.9	4.1	3.2
Total	11.4	11.4	16.9	17.0	30.4	31.0	112.0	116.1	9.8	9.7

# Uncertainties due to electron calibration

$ \eta_\ell $ range	[0.0, 0.6]		[0.6, 1.2]		[1.82, 2.4]		Combined	
Kinematic distribution	$p_T^\ell$	$m_T$	$p_T^\ell$	$m_T$	$p_T^\ell$	$m_T$	$p_T^\ell$	$m_T$
$\delta m_W$ [MeV]								
Energy scale	10.4	10.3	10.8	10.1	16.1	17.1	8.1	8.0
Energy resolution	5.0	6.0	7.3	6.7	10.4	15.5	3.5	5.5
Energy linearity	2.2	4.2	5.8	8.9	8.6	10.6	3.4	5.5
Energy tails	2.3	3.3	2.3	3.3	2.3	3.3	2.3	3.3
Reconstruction efficiency	10.5	8.8	9.9	7.8	14.5	11.0	7.2	6.0
Identification efficiency	10.4	7.7	11.7	8.8	16.7	12.1	7.3	5.6
Trigger and isolation efficiencies	0.2	0.5	0.3	0.5	2.0	2.2	0.8	0.9
Charge mismeasurement	0.2	0.2	0.2	0.2	1.5	1.5	0.1	0.1
Total	19.0	17.5	21.1	19.4	30.7	30.5	14.2	14.3

# Uncertainties due to recoil corrections

$W$ -boson charge Kinematic distribution	$W^+$		$W^-$		Combined	
	$p_T^\ell$	$m_T$	$p_T^\ell$	$m_T$	$p_T^\ell$	$m_T$
$\delta m_W$ [MeV]						
$\langle \mu \rangle$ scale factor	0.2	1.0	0.2	1.0	0.2	1.0
$\Sigma E_T^*$ correction	0.9	12.2	1.1	10.2	1.0	11.2
Residual corrections (statistics)	2.0	2.7	2.0	2.7	2.0	2.7
Residual corrections (interpolation)	1.4	3.1	1.4	3.1	1.4	3.1
Residual corrections ( $Z \rightarrow W$ extrapolation)	0.2	5.8	0.2	4.3	0.2	5.1
Total	2.6	14.2	2.7	11.8	2.6	13.0

# Number of selected W bosons

$ \eta_\ell $ range	0–0.8	0.8–1.4	1.4–2.0	2.0–2.4	Inclusive
$W^+ \rightarrow \mu^+ \nu$	1 283 332	1 063 131	1 377 773	885 582	4 609 818
$W^- \rightarrow \mu^- \bar{\nu}$	1 001 592	769 876	916 163	547 329	3 234 960
$ \eta_\ell $ range	0–0.6	0.6–1.2		1.8–2.4	Inclusive
$W^+ \rightarrow e^+ \nu$	1 233 960	1 207 136		956 620	3 397 716
$W^- \rightarrow e^- \bar{\nu}$	969 170	908 327		610 028	2 487 525