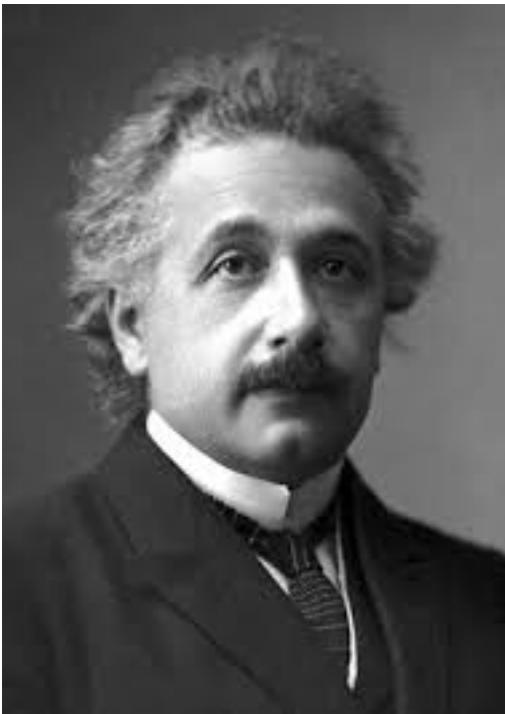


# Natural SUSY from the string theory landscape



Howard Baer  
University of Oklahoma

Planck meeting, Bonn  
May 22, 2018

“Everything should be  
made as simple as  
possible, but not  
simpler”

A. Einstein

“The appearance of fine-tuning  
in a scientific theory is like a  
cry of distress from nature,  
complaining that something  
needs to be better explained”



S. Weinberg

# Following Einstein: be as simple as possible, not simpler

- weak scale effective theory=SM (including Higgs)
- mass instability of fundamental Higgs field duly noted as we proceed beyond the weak scale

# Following Weinberg: must be natural to be plausible

- invoke SUSY: SM-> MSSM
- solves Big Hierarchy problem
- softly broken as expected from SUGRA
- might expect  $m(h) \rightarrow$  LHC scale (multi-TeV)
- require no Little Hierarchy as well

First: avoid unambiguous fine-tunings arising at the weak scale

Scalar potential minimization conditions relate

$m(W, Z, h) \sim 100$  GeV to SUSY Lagrangian

No large uncorrelated cancellations in  $m(Z)$  or  $m(h)$

$$\frac{m_Z^2}{2} = \frac{m_{H_d}^2 + \Sigma_d^d - (m_{H_u}^2 + \Sigma_u^u) \tan^2 \beta}{\tan^2 \beta - 1} - \mu^2 \sim -m_{H_u}^2 - \Sigma_u^u - \mu^2$$

$$\Delta_{EW} \equiv \max_i |C_i| / (m_Z^2/2) \quad \text{with} \quad C_{H_u} = -m_{H_u}^2 \tan^2 \beta / (\tan^2 \beta - 1) \quad \text{etc.}$$

simple, direct, unambiguous interpretation:

- $|\mu| \sim m_Z \sim 100 - 200$  GeV (Chan, Chatto..., Nath; HB, Barger, Huang)
- $m_{H_u}^2$  should be driven to small negative values such that  $-m_{H_u}^2 \sim 100 - 200$  GeV at the weak scale and
- that the radiative corrections are not too large:  $\Sigma_u^u \lesssim 100 - 200$  GeV

CETUP\*-12/002, FTPI-MINN-12/22, UMN-TH-3109/12, UH-511-1195-12

Radiative natural SUSY with a 125 GeV Higgs boson

Howard Baer,<sup>1</sup> Vernon Barger, Peisi Huang,<sup>2</sup> Azar Mustafayev,<sup>3</sup> and Xerxes Tata<sup>4</sup>

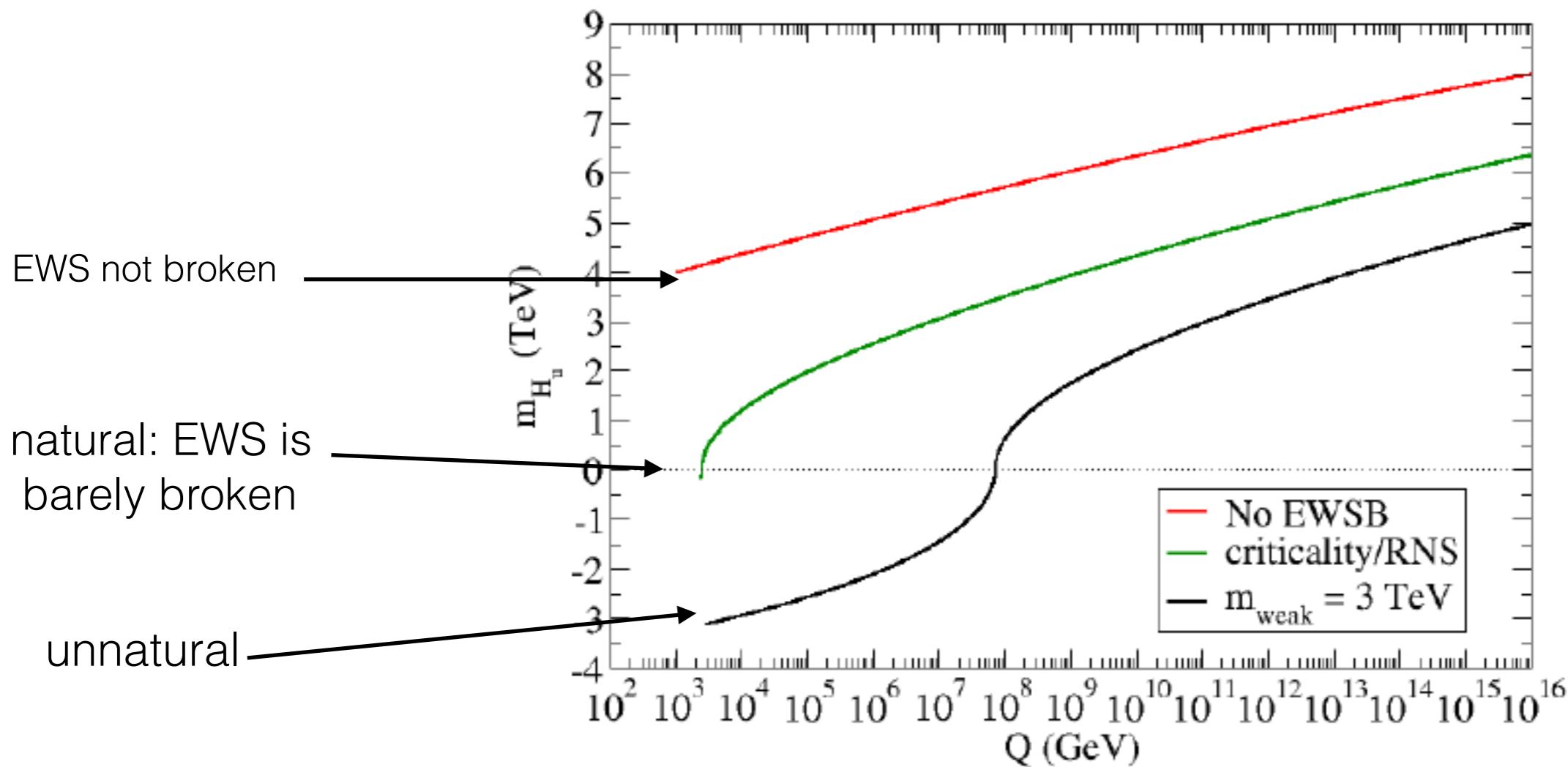
PRL109 (2012) 161802

<sup>1</sup>Dept. of Physics and Astronomy, University of Oklahoma, Norman, OK, 73019, USA

<sup>2</sup>Dept. of Physics, University of Wisconsin, Madison, WI 53706, USA

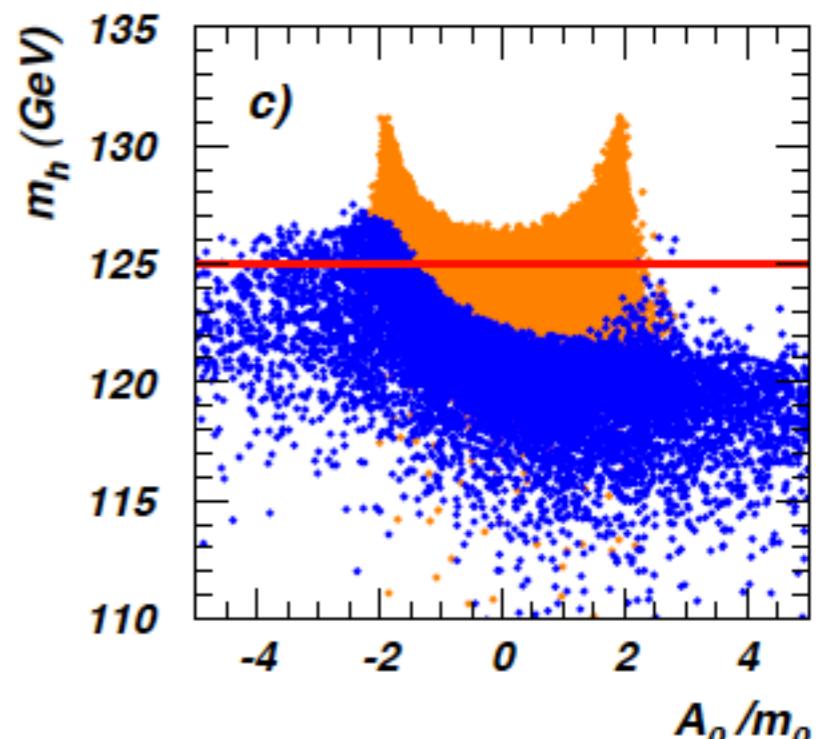
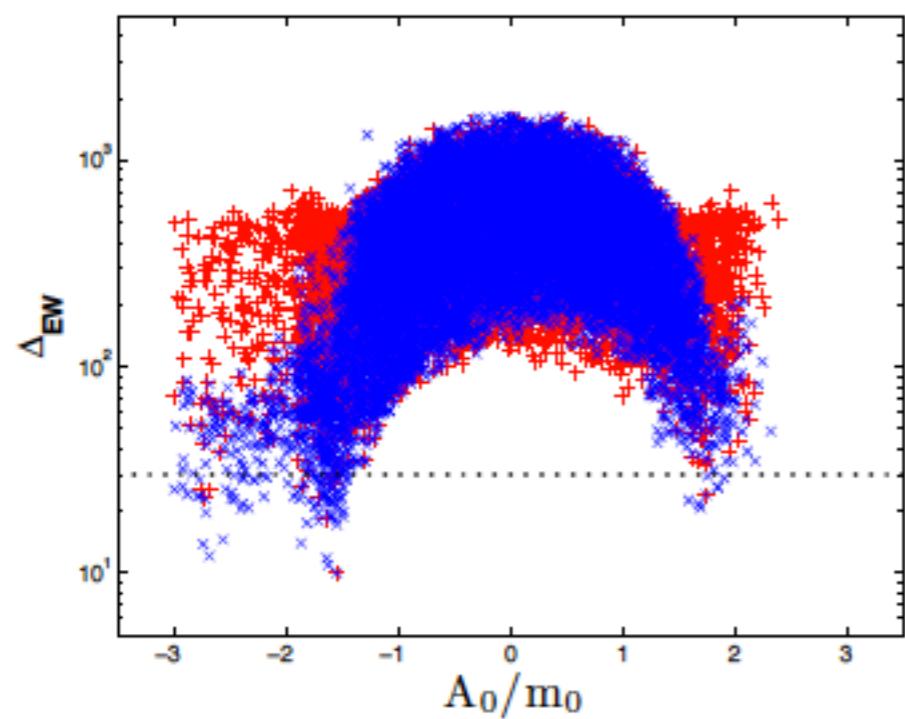
<sup>3</sup>W. L. Fine Institute for Theoretical Physics, University of Minnesota, Minneapolis, MN 55455, USA

radiative corrections drive  $m_{H_u}^2$  from unnatural GUT scale values to naturalness at weak scale:  
radiatively-driven naturalness



Evolution of the soft SUSY breaking mass squared term  $\text{sign}(m_{H_u}^2)\sqrt{|m_{H_u}^2|}$  vs.  $Q$

Large value of  $A_t$  reduces  $\Sigma_u^u(\tilde{t}_{1,2})$  contributions to  $\Delta_{EW}$  while uplifting  $m_h$  to  $\sim 125$  GeV



$$\Sigma_u^u(\tilde{t}_{1,2}) = \frac{3}{16\pi^2} F(m_{\tilde{t}_{1,2}}^2) \left[ f_t^2 - g_Z^2 \mp \frac{f_t^2 A_t^2 - 8g_Z^2 (\frac{1}{4} - \frac{2}{3}x_W) \Delta_t}{m_{\tilde{t}_2}^2 - m_{\tilde{t}_1}^2} \right]$$

$$\Delta_t = (m_{\tilde{t}_L}^2 - m_{\tilde{t}_R}^2)/2 + M_Z^2 \cos 2\beta (\frac{1}{4} - \frac{2}{3}x_W)$$

$$F(m^2) = m^2 \left( \log \frac{m^2}{Q^2} - 1 \right) \quad Q^2 = m_{\tilde{t}_1} m_{\tilde{t}_2}$$

# Is that all there is to EW naturalness in SUSY?

- What about UV fine-tuning measures?
- What about BG/KN etc. bounds  $m(C1) < 100$  GeV,  $m(g_{lno}) < 400$  GeV,  $m(t_1, t_2, b_1) < 500$  GeV?

UV fine-tuning depends on what you take as fundamental soft terms

$$m_h^2 = \mu^2 + m_{H_u}^2(\text{weak}) + (\text{mixings} < m_Z^2) + (\text{rad.corr.} < m_Z^2)$$

expand  $m_{H_u}^2$  in terms of GUT scale soft param's using quasi-analytic solutions to RGEs for  $\tan \beta = 10$

$$\begin{aligned} m_h^2 &\simeq 1.09\mu^2(\Lambda) + m_{H_u}^2(\Lambda) + \delta m_{H_u}^2 \\ &\simeq 1.09\mu^2 + m_{H_u}^2 - 1.92M_3^2 - 0.16M_3M_2 - 0.024M_1M_3 + 0.21M_2^2 \\ &\quad - 0.005M_2M_1 + 0.006M_1^2 + 0.33M_3A_t + 0.08M_2A_t \\ &\quad + 0.013M_1A_t - 0.11A_t^2 - 0.002M_3A_b \\ &\quad - 0.36m_{H_u}^2 + 0.027m_{H_d}^2 \\ &\quad - 0.37m_{Q_3}^2 - 0.29m_{U_3}^2 - 0.025m_{D_3}^2 + 0.026m_{L_3}^2 - 0.027m_{E_3}^2 \\ &\quad - 0.026m_{Q_2}^2 + 0.06m_{U_2}^2 - 0.026m_{D_2}^2 + 0.026m_{L_2}^2 - 0.027m_{E_2}^2 \\ &\quad - 0.026m_{Q_1}^2 + 0.06m_{U_1}^2 - 0.026m_{D_1}^2 + 0.026m_{L_1}^2 - 0.027m_{E_1}^2 \end{aligned}$$

if all high scale soft terms independent then

$$\text{e.g. } 0.37m_{Q_3}^2 < 10m_h^2 \Rightarrow m_{Q_3} < 650 \text{ GeV}$$

If we work within CMSSM,  
get very different answer:

$$\begin{aligned} m_h^2 \simeq & 1.09\mu^2 - 1.893m_{1/2}^2 + 0.421m_{1/2}A_0 - 0.11A_0^2 \\ & - 0.019m_0(3)^2 + 0.006m_0(2)^2 + 0.006m_0(1)^2 \end{aligned}$$

$$0.019m_0(3)^2 < 10m_h^2 \Rightarrow m_0(3) < \sim 3 \text{ TeV}$$

correlations between parameters  
can lead to large cancellations!

If we work in complete model where hidden sector is specified and all soft terms computed in terms of  $m(3/2)$ -  
(as usual in SUGRA models)

$$m_h^2 \simeq 1.09\mu^2 + a \cdot m_{3/2}^2 \simeq \mu^2(\text{weak}) + m_{H_u}^2(\text{weak})$$

model is natural for  $m(3/2)$  large if  $a$  is small

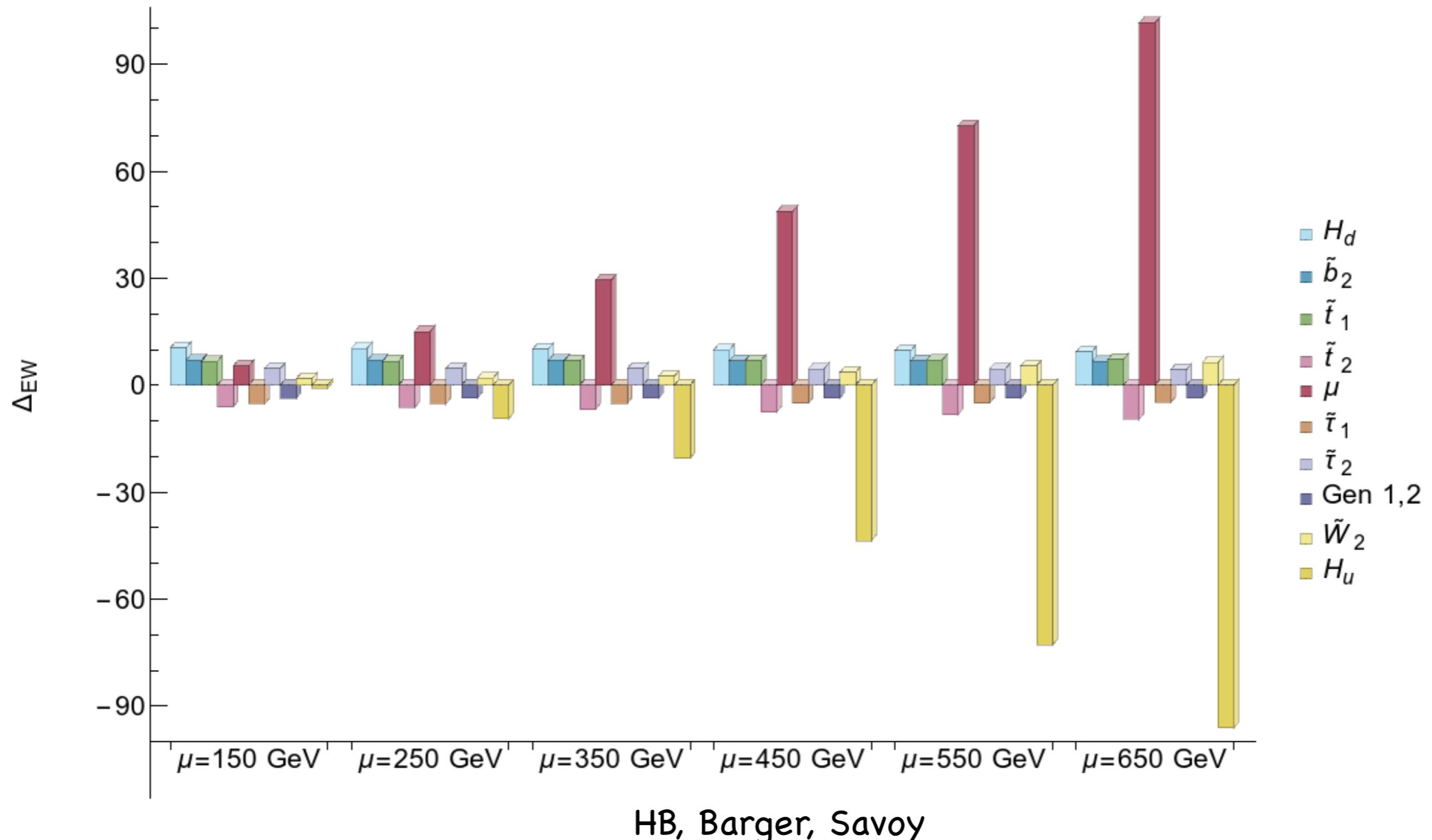
$a \cdot m_{3/2}^2 \simeq m_{H_u}^2$  so  $a$  small  
 $\Rightarrow m_{H_u}^2$  driven small at weak scale: *same as for  $\Delta_{EW}$ !*

$\Delta_{EW}$  is appropriate fine-tuning measure for either IR or *correlated* UV parameters!

# On SUSY parameters

- parameters are introduced by theorists to parametrize our ignorance of SUSY breaking
- in any more fundamental theory, soft terms are calculated in terms of single soft breaking parameter
- e.g.  $m_{3/2}$  in SUGRA or AMSB,  $\Lambda$  in GMSB
- we think  $\Delta_{EW}$  is a better measure of **whether nature is fine-tuned**, rather than our effective theories with artificially-introduced parameters

# How much is too much fine-tuning?



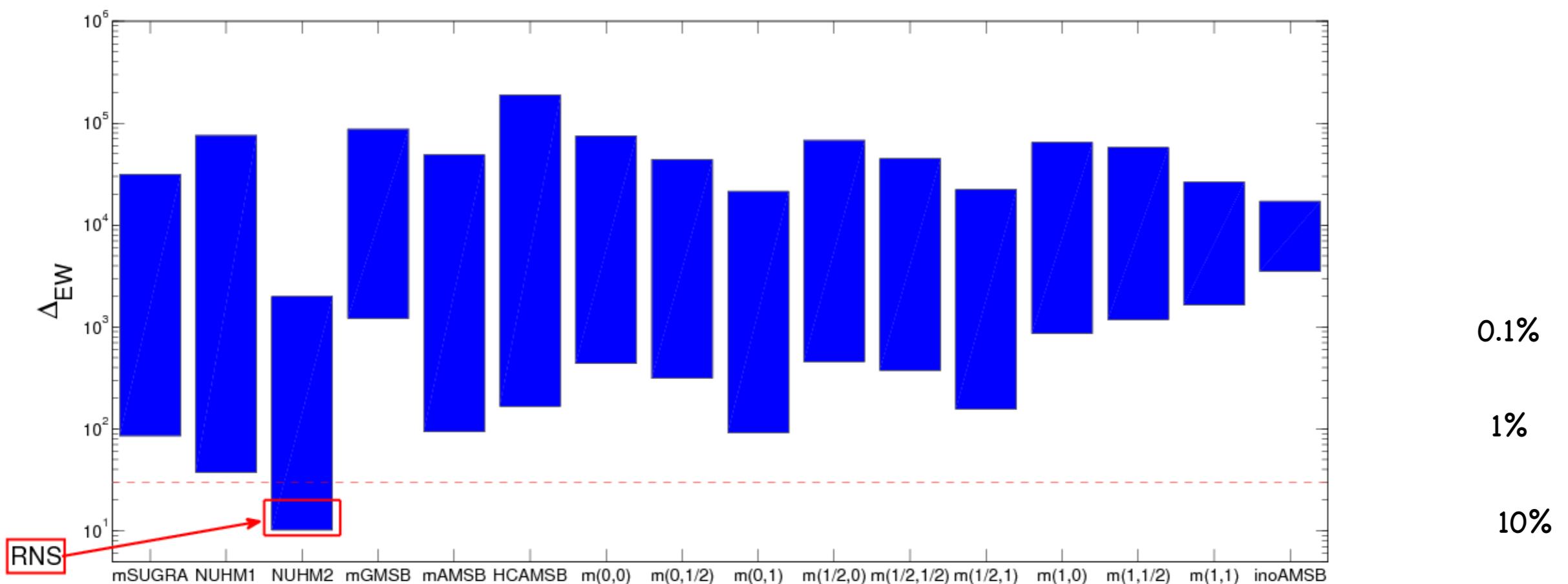
Visually, large fine-tuning has already developed by  $\mu \sim 350$  or  $\Delta_{EW} \sim 30$

Nature is natural  $\Rightarrow \Delta_{EW} < 20 - 30$  (take 30 as conservative)

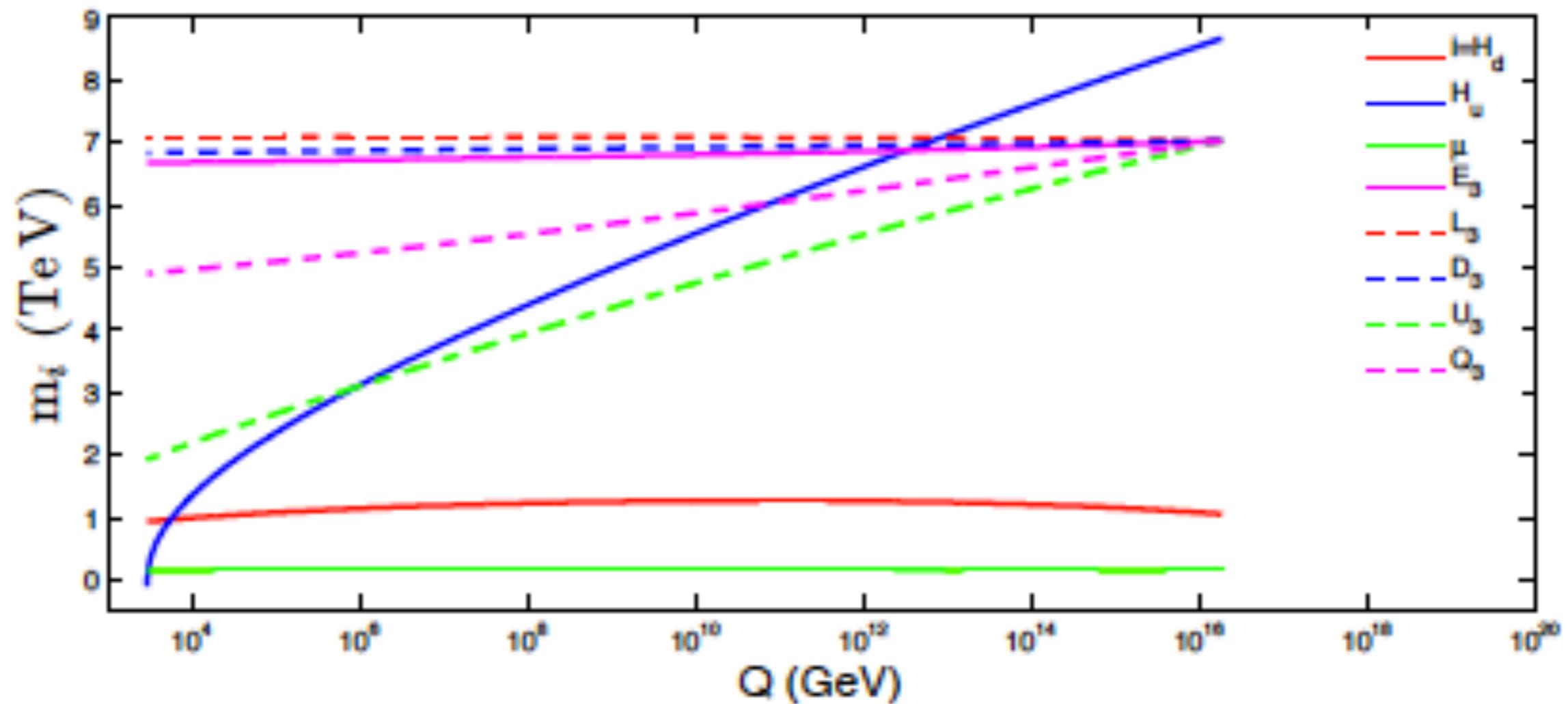
$\Delta_{EW}$  is highly selective:  
 most constrained models are ruled out  
 except NUHM2 and natural generalized AMSB and mirage mediation

D. Matalliotakis and H. P. Nilles, Nucl. Phys. B **435** (1995) 115; M. Olechowski and S. Pokorski, Phys. Lett. B **344** (1995) 201; P. Nath and R. L. Arnowitt, Phys. Rev. D **56** (1997) 2820; J. Ellis, K. Olive and Y. Santoso, Phys. Lett. B **539** (2002) 107; J. Ellis, T. Falk, K. Olive and Y. Santoso, Nucl. Phys. B **652** (2003) 259; H. Baer, A. Mustafayev, S. Profumo, A. Belyaev and X. Tata, JHEP **0507** (2005) 065.

scan over p-space with  $m(h)=125.5\pm 2.5$  GeV:



Applied properly, all three measures agree:  
naturalness is unambiguous and highly predictive!



Radiatively-driven natural SUSY, or RNS:

(typically need  $m_{Hu} \sim 25\text{-}50\%$  higher than  $m_0$ )

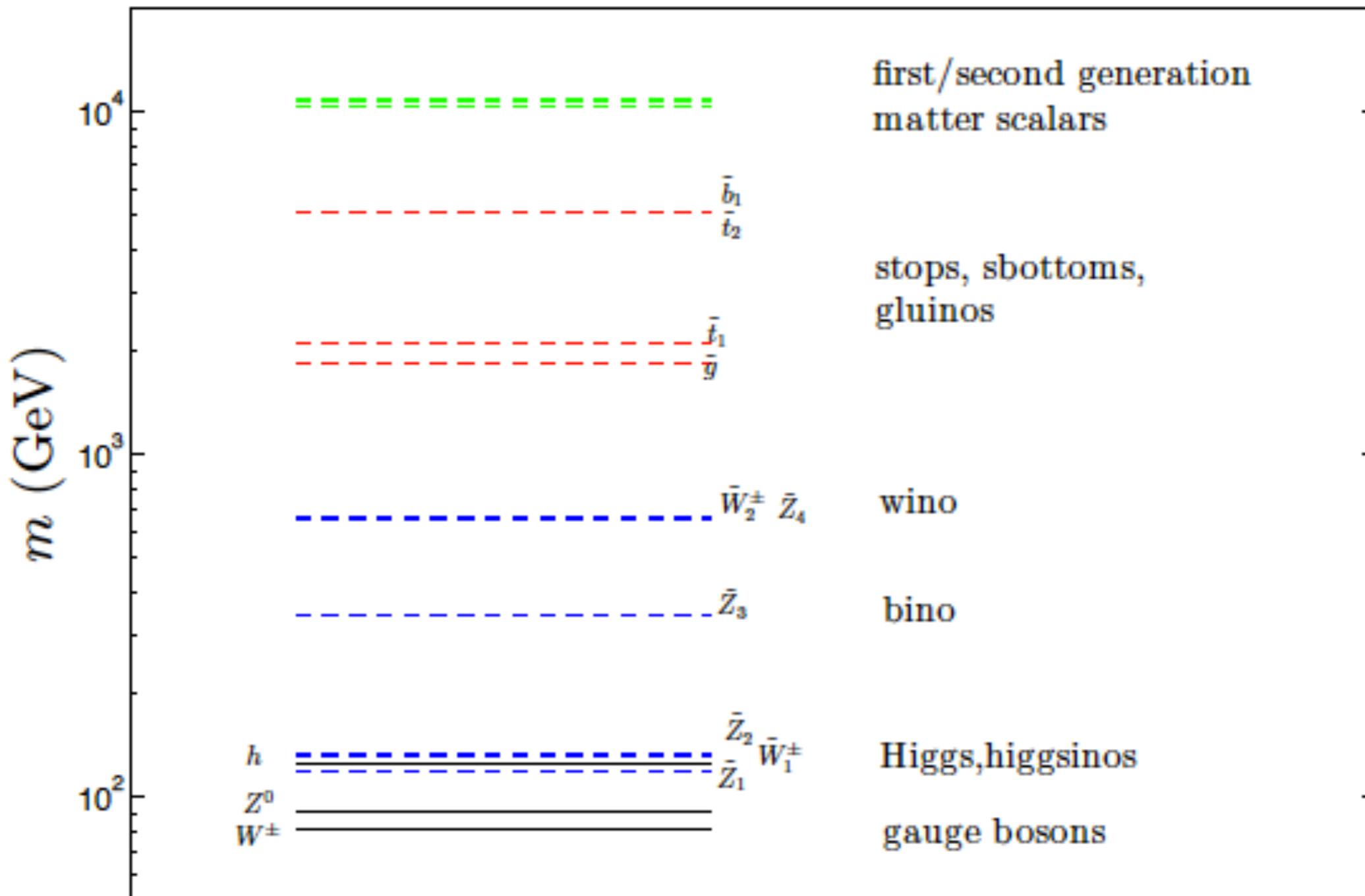
H. Baer, V. Barger, P. Huang, A. Mustafayev and X. Tata, *Phys. Rev. Lett.* **109** (2012) 161802.

H. Baer, V. Barger, P. Huang, D. Mickelson, A. Mustafayev and X. Tata, *Phys. Rev. D* **87** (2013) 115028 [[arXiv:1212.2655 \[hep-ph\]](https://arxiv.org/abs/1212.2655)].

<b>bounds from naturalness (3%)</b>	<b>BG/DG</b>	<b>Delta_EW</b>
<b>mu</b>	350 GeV	0.35 TeV
<b>gluino</b>	400-600 GeV	5-6 TeV
<b>t1</b>	450 GeV	3 TeV
<b>sq/sl</b>	550-700 GeV	10-30 TeV

$h(125)$  and LHC limits are perfectly compatible  
with 3-10% naturalness: **no crisis!**

## Typical spectrum for low $\Delta_{EW}$ models



There is a Little Hierarchy, but it is **no problem**

$$\mu \ll m_{3/2}$$

First order question:

why is the weak scale  $m(W,Z,h) \sim 100$  GeV?

Because  $m_{\mu}(\text{weak})$ ,  $m_{H_u}(\text{weak}) \sim 100-200$  GeV  
and top squarks  $\sim$  few TeV but highly mixed

Second order questions:

1. Why might  $m_{\mu} \ll m(\text{soft})$
2. Why might soft terms be at multi-TeV scale but with  $m(H_u)$  driven radiatively to  $m_{H_u}^2(\text{weak}) \sim -(100-200 \text{ GeV})^2$ ?

SUSY mu problem: mu term is SUSY, not SUSY breaking:  
expect  $\mu \sim M_{\text{Pl}}$  but phenomenology requires  $\mu \sim m(Z)$

- NMSSM:  $\mu \sim m(3/2)$ ; but beware singlets!
- Giudice-Masiero:  $\mu$  forbidden by some symmetry:  
generate via Higgs coupling to hidden sector
- **Kim-Nilles**: invoke SUSY version of DFSZ axion  
solution to strong CP:  $W \ni \lambda_\mu S^2 H_u H_d / m_P$

KN: PQ symmetry forbids mu term,  
but then it is generated via PQ breaking

$$\mu \sim \lambda_\mu f_a^2 / m_P$$

Little Hierarchy due to mismatch between  
PQ breaking and SUSY breaking scales?

$$m_{3/2} \sim m_{hid}^2 / M_P$$
$$f_a \ll m_{hid}$$

Higgs mass tells us where  
to look for axion!

$$m_a \sim 6.2 \mu\text{eV} \left( \frac{10^{12} \text{ GeV}}{f_a} \right)$$

# Little Hierarchy from radiative PQ breaking? exhibited within context of MSY/CCK model

Murayama, Suzuki, Yanagida (1992);  
 Gherghetta, Kane (1995)  
 Choi, Chun, Kim (1996)

Bae, HB, Serce, PRD91 (2015) 015003

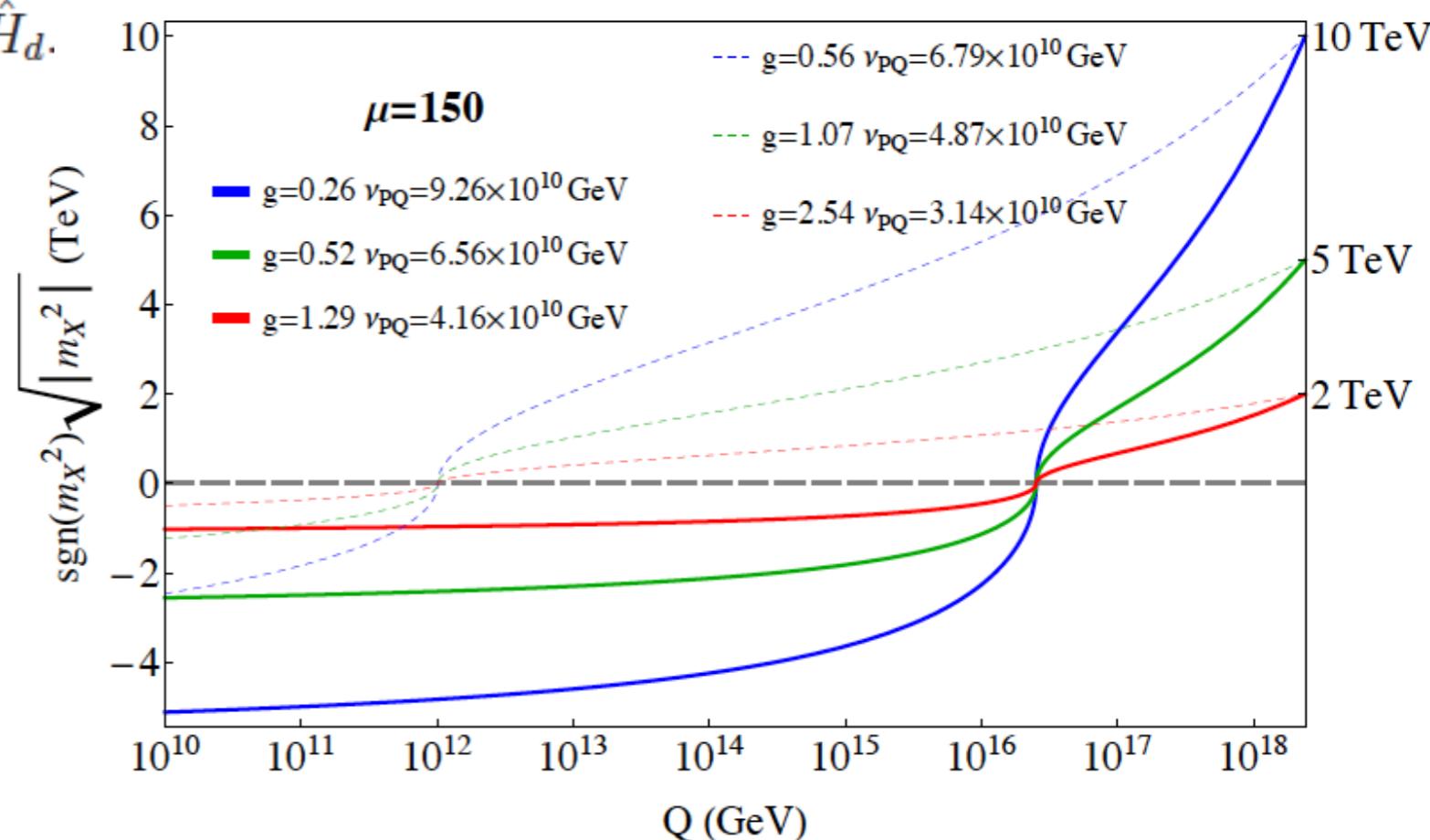
## augment MSSM with PQ charges/fields:

$$\hat{f}' = \frac{1}{2} h_{ij} \hat{X} \hat{N}_i^c \hat{N}_j^c + \frac{f}{M_P} \hat{X}^3 \hat{Y} + \frac{g}{M_P} \hat{X} \hat{Y} \hat{H}_u \hat{H}_d.$$

SUSY breaking triggers  
 PQ breaking:  
 generate fa and MN

$$M_{N_i^c} = v_X h_i|_{Q=v_X}$$

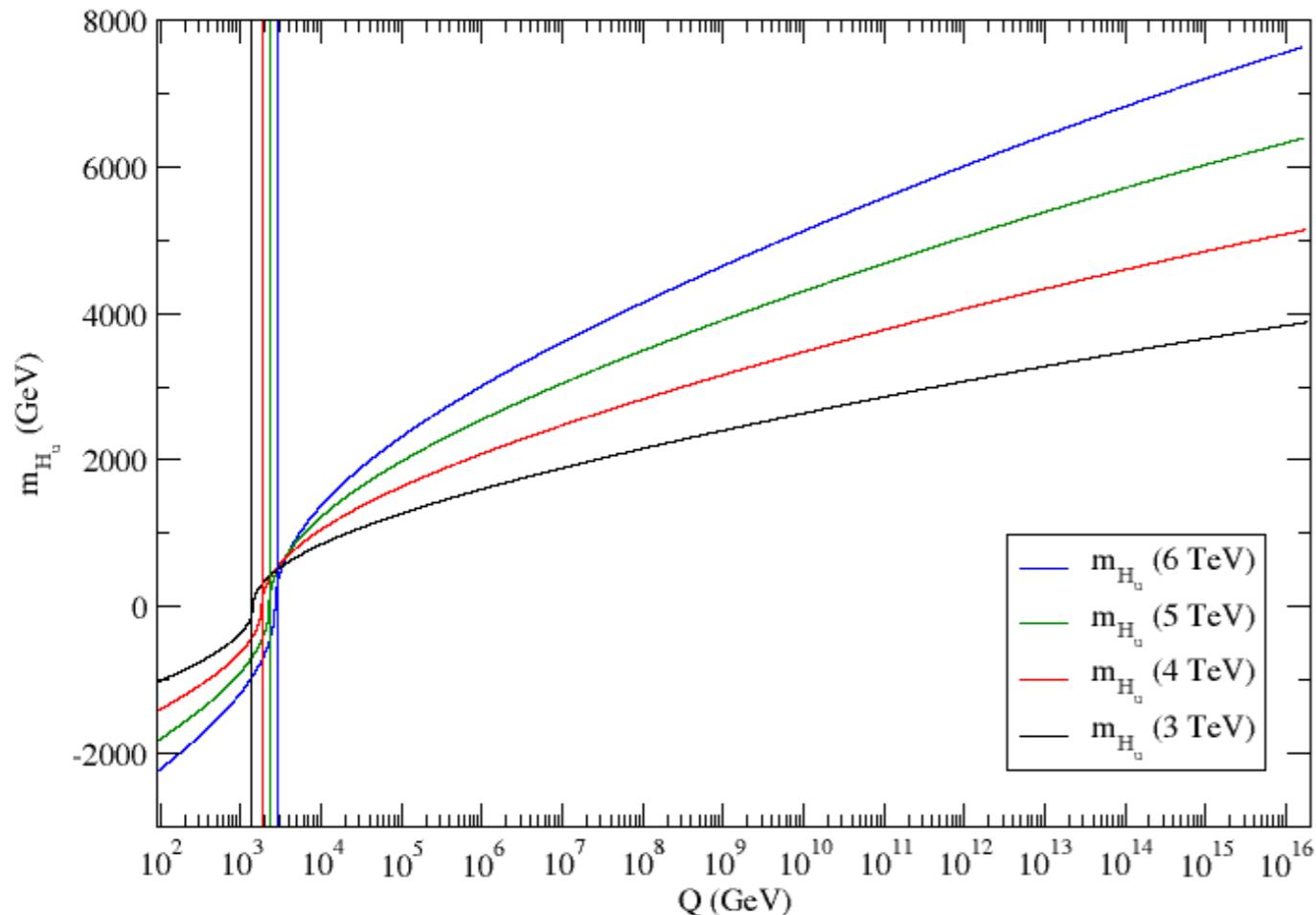
$$\mu = g \frac{v_X v_Y}{M_P} .$$



Large  $m_{3/2}$  generates small  $\mu \sim 100 - 200$  GeV!

# Why might $m_{Hu}$ have the value needed to give naturalness at weak scale?

1. For right correlations amongst soft terms, get “generalized focus point”



e.g.

For  $\mu = 150$  GeV,  $\tan \beta = 10$  and

$$\begin{aligned} m_0^2 &= m_{3/2}^2 \\ A_0 &= -1.6m_{3/2} \\ m_{1/2} &= m_{3/2}/5 \\ m_{H_d}^2 &= m_{3/2}^2/2. \end{aligned}$$

$$m_{Hu}^2(GUT) = 1.8m_{3/2}^2 - (212.52 \text{ GeV})^2.$$

$m_{Hu}^2(\text{weak}) \sim a \cdot m_{3/2}^2$  with correlated soft terms such that  $a$  is small: generalized focus point behavior

# Statistical analysis of SUSY breaking scale in II-B string theory landscape of vacua:

F. Denef & M. Douglas

(for summary, see e.g. hep-th/0405279)

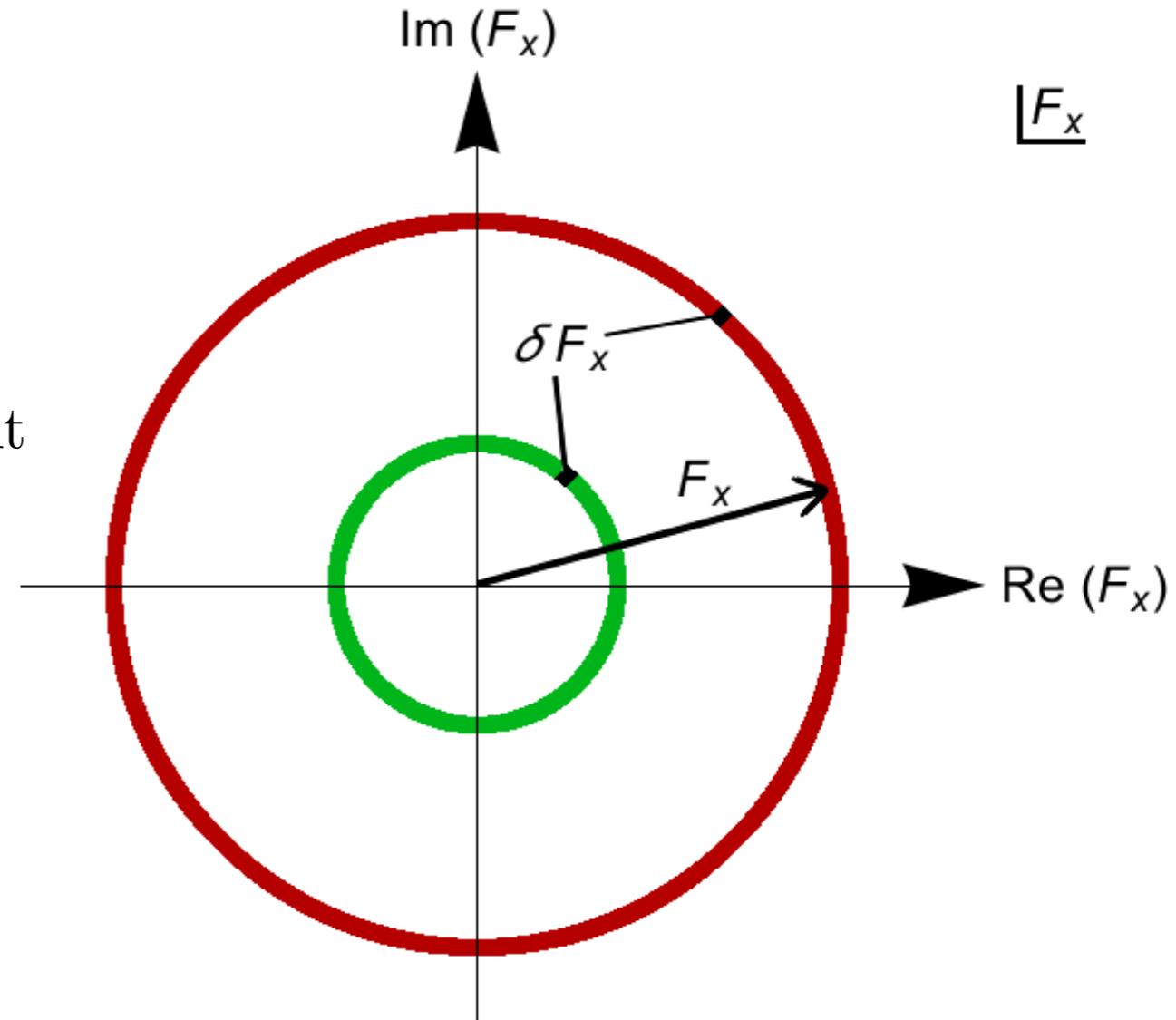
## some reasonable assumptions

- string theory landscape contains vast ensemble of  $N=1$ ,  $d=4$  SUGRA EFTs at high scales
- the EFTs contain the SM as weak scale EFT
- the EFTs contain visible sector +potentially large hidden sector
- visible sector contains MSSM plus extra gauge singlets (e.g. a PQ sector, RN neutrinos,...)
- SUGRA is broken spontaneously via superHiggs mechanism via either F- or D- terms or in general a combination

# Why do soft terms take on values needed for natural (barely-broken) EWSB?

## 2. string theory landscape?

- assume model like MSY/CCK where  $\mu \sim 100$  GeV
- then  $m(\text{weak})^2 \sim |m_{H_u}^2|$
- If all values of SUSY breaking field  $\langle F_X \rangle$  equally likely, then mild (linear) statistical draw towards large soft terms
- This is balanced by anthropic requirement of weak scale  $m_{\text{weak}} \sim 100$  GEV



*Anthropic selection of  $m_{\text{weak}} \sim 100$  GeV:*

If  $m_W$  too large, then weak interactions  $\sim (1/m_W^4)$  too weak  
weak decays, fusion reactions suppressed  
elements not as we know them

$m(\text{weak}) < \sim 400$  GeV (Agrawal et al.)

V. Agrawal, S. M. Barr, J. F. Donoghue and D. Seckel, Phys. Rev. D 57 (1998) 5480;  
V. Agrawal, S. M. Barr, J. F. Donoghue and D. Seckel, Phys. Rev. Lett. 80 (1998) 1822.

Scalar potential is given by usual SUGRA form:

$$\begin{aligned} V &= e^{K/m_P^2} \left( g^{i\bar{j}} D_i W D_{\bar{j}} W^* - \frac{3}{m_P^2} |W|^2 \right) + \frac{1}{2} \sum_{\alpha} D_{\alpha}^2 \\ &= e^{K/m_P^2} \left( \sum_i |F_i|^2 - 3 \frac{|W|^2}{m_P^2} \right) + \frac{1}{2} \sum_{\alpha} D_{\alpha}^2 \end{aligned}$$

- $W$  = holomorphic superpotential
- $K$  = real Kähler function
- $F_i = D_i W = DW/D\phi^i \equiv \partial W/\partial\phi^i + (1/m_P^2)(\partial K/\partial\phi^i)W$  are  $F$ -terms
- $D_{\alpha} \sim \sum \phi^{\dagger} g t_{\alpha} \phi$  are  $D$ -terms
- $\phi^i$  are chiral superfields

**minimize**  $V$ :

- $\partial V/\partial\phi^i = 0$
- $\partial^2 V/\partial\phi^i\partial\phi^j > 0$
- $\Lambda_{cc} = m_{hidden}^4 - 3e^{K/m_P^2}|W|^2/m_P^2$  with
- $m_{hidden}^4 = \sum_i |F_i|^2 + \frac{1}{2} \sum_{\alpha} D_{\alpha}^2$  is hidden sector mass scale

gravitino mass  $m_{3/2} = e^{K/2m_P^2} m_P \sim m_{hidden}^2/m_P$  with  $m_{hidden} \sim 10^{12}$  GeV

# Denef&Douglas: statistics of SUSY breaking in landscape

DD observation:  $W_0$  distributed uniformly as complex variable allows dynamical neutralization of  $\Lambda$  while not influencing SUSY breaking

Then, number of flux vacua containing spontaneously broken SUGRA with SUSY breaking scale  $m_{hidden}^2$  is:

$$dN_{vac}[m_{hidden}^2, m_{weak}, \Lambda] = f_{SUSY}(m_{hidden}^2) \cdot f_{EWFT} \cdot f_{cc} dm_{hidden}^2$$

- $f_{cc} \sim \Lambda/m^4$  where DD maintain  $m \sim m_{string}$  and not  $m_{hidden}$
- $f_{SUSY}(m_{hidden}^2) \sim (m_{hidden}^2)^{2n_F+n_D-1}$  for uniformly distributed values of  $F$  and  $D$  breaking fields
- $f_{EWFT} \sim m_{weak}^2/m_{soft}^2$  (?) where  $m_{soft} \sim m_{3/2} \sim m_{hidden}^2/m_P$

$$n = 2n_F + n_D - 1$$

$$f_{SUSY} \sim m_{soft}^n$$

landscape favors high scale SUSY breaking  
tempered by f(EWFT) anthropic penalty!

$n_F$	$n_D$	$n$
0	1	0
1	0	1
0	2	1
1	1	2
0	3	2
2	0	3
2	1	4

What about DD/AD anthropic penalty  $f_{EWFT} \sim m_{weak}^2/m_{soft}^2$ ?

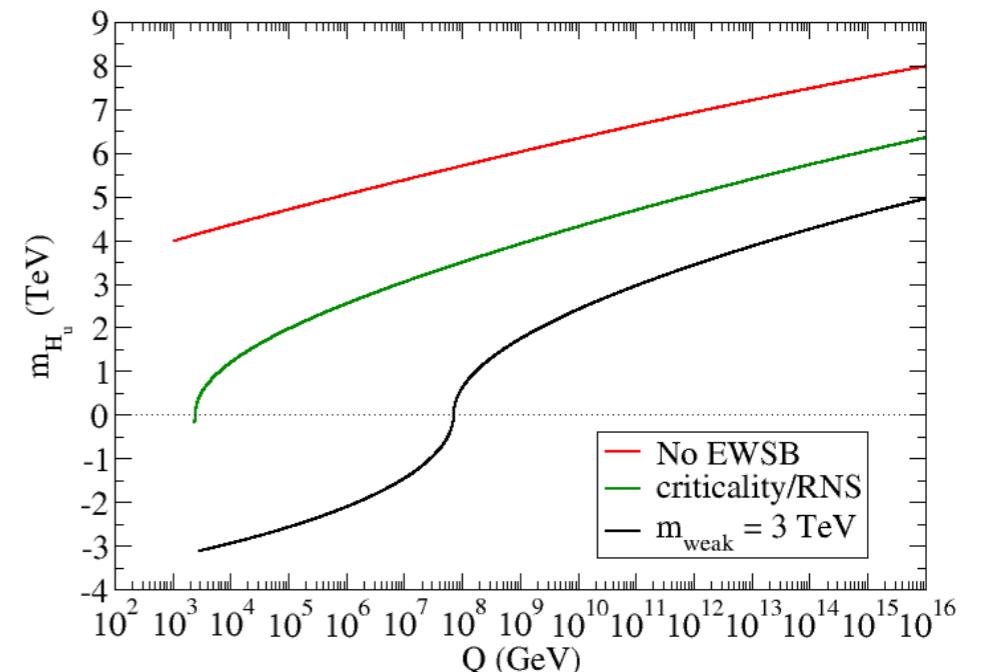
This fails in a variety of *practical* cases:

- $A$ -terms get large:  $\Rightarrow CCB$  minima
- $m_{H_u}^2$  too large: fail to break EW symmetry

Must require proper EWSB!

Even if EWS properly broken, then

- large  $A_t$  reduces EWFT in the  $\Sigma_u^u(\tilde{t}_{1,2})$
- large  $m_{H_u}^2(m_{GUT})$  needed to radiatively drive  $m_{H_u}^2$  to natural value at weak scale



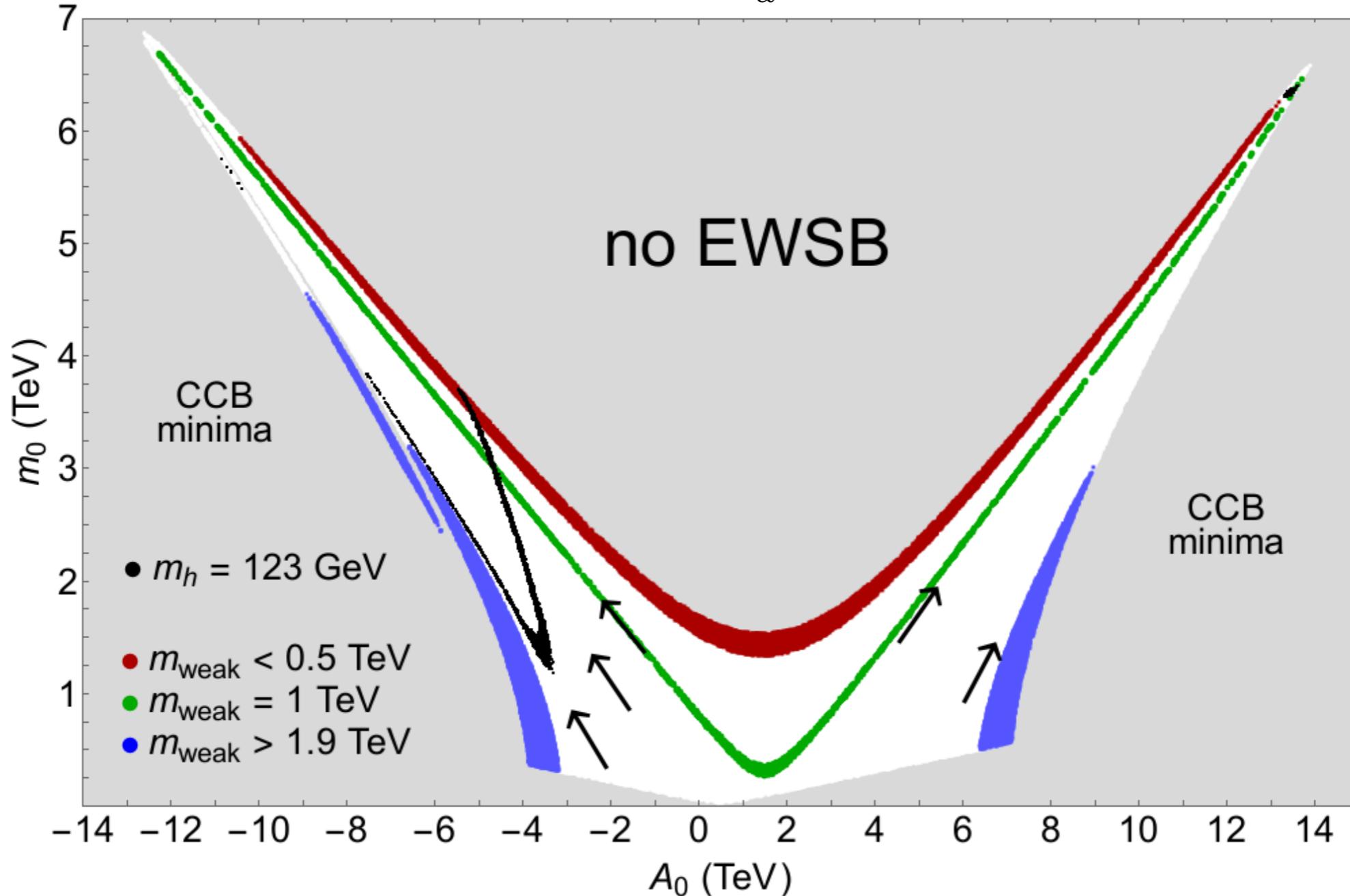
Better proposal:  $f_{EWFT} \Rightarrow \Theta(30 - \Delta_{EW})$

keeps calculated weak scale within factor  $\sim 4$  of measured weak scale  
 $m_{weak} \equiv m_{W,Z,h} \sim 100$  GeV

Assume  $\mu \sim 100 - 200$  GeV via e.g. rad PW breaking: then  $m_Z$  variable and may be large depending on soft terms  $m_{H_{u,d}}^2$  and  $\Sigma_{u,d}^{u,d}(i)$

$$\frac{m_Z^2}{2} = \frac{m_{H_d}^2 + \Sigma_d^d - (m_{H_u}^2 + \Sigma_u^u) \tan^2 \beta}{\tan^2 \beta - 1} - \mu^2$$

$$m_{H_u} = 1.3m_0$$



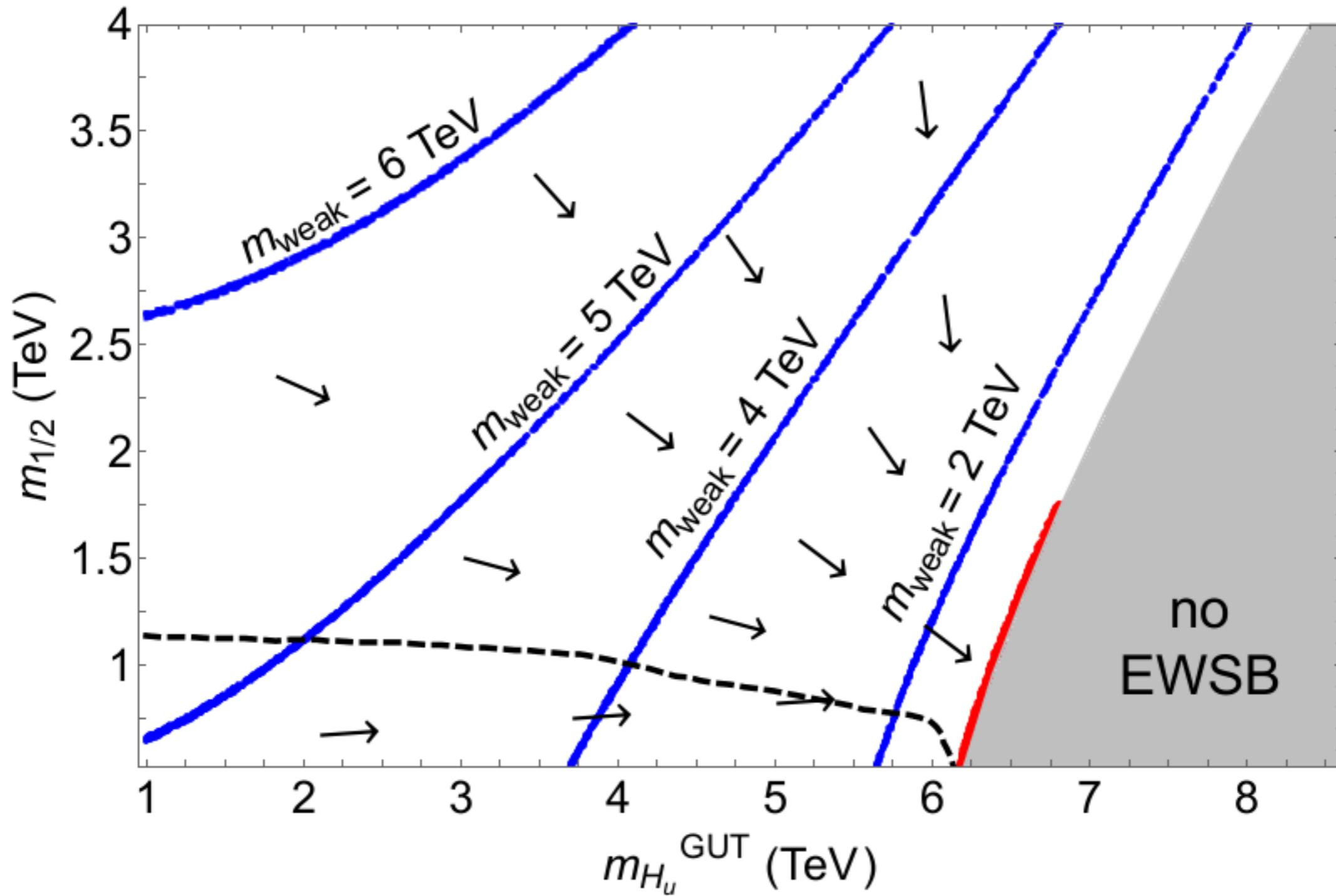
statistical draw to large soft terms balanced by  
anthropic draw toward red ( $m(\text{weak}) \sim 100 \text{ GeV}$ ):  
then  $m(\text{Higgs}) \sim 125 \text{ GeV}$  and natural SUSY spectrum!

Denef, Douglas, JHEP0405 (2004) 072

Giudice, Rattazzi, NPB757 (2006) 19;

HB, Barger, Savoy, Serce, PLB758 (2016) 113

$$m_0 = 5 \text{ TeV}$$



statistical/anthropic draw toward FP-like region

For practical calculations, adopt NUHM3 SUGRA model:

- $m_0(1, 2) = \text{gen}(1, 2)$  common soft mass
- $m_0(3) = \text{gen}(3)$  common soft mass
- $m_{H_u}^2$  up-Higgs soft mass
- $m_{H_d}^2$  down-Higgs soft mass
- $m_{1/2}$  unified gaugino mass
- $A_0$  unified trilinear soft term
- $\tan \beta$

Trade  $m_{H_u}^2, m_{H_d}^2 \Leftrightarrow \mu, m_A$

$m_0(1, 2), m_0(3), m_{1/2}, A_0, \tan \beta, \mu, m_A$  (NUHM3)

Recent work: place on more quantitative footing:  
scan soft SUSY breaking parameters as  $m(\text{soft})^n$   
along with  $f(\text{EWFT})$  penalty

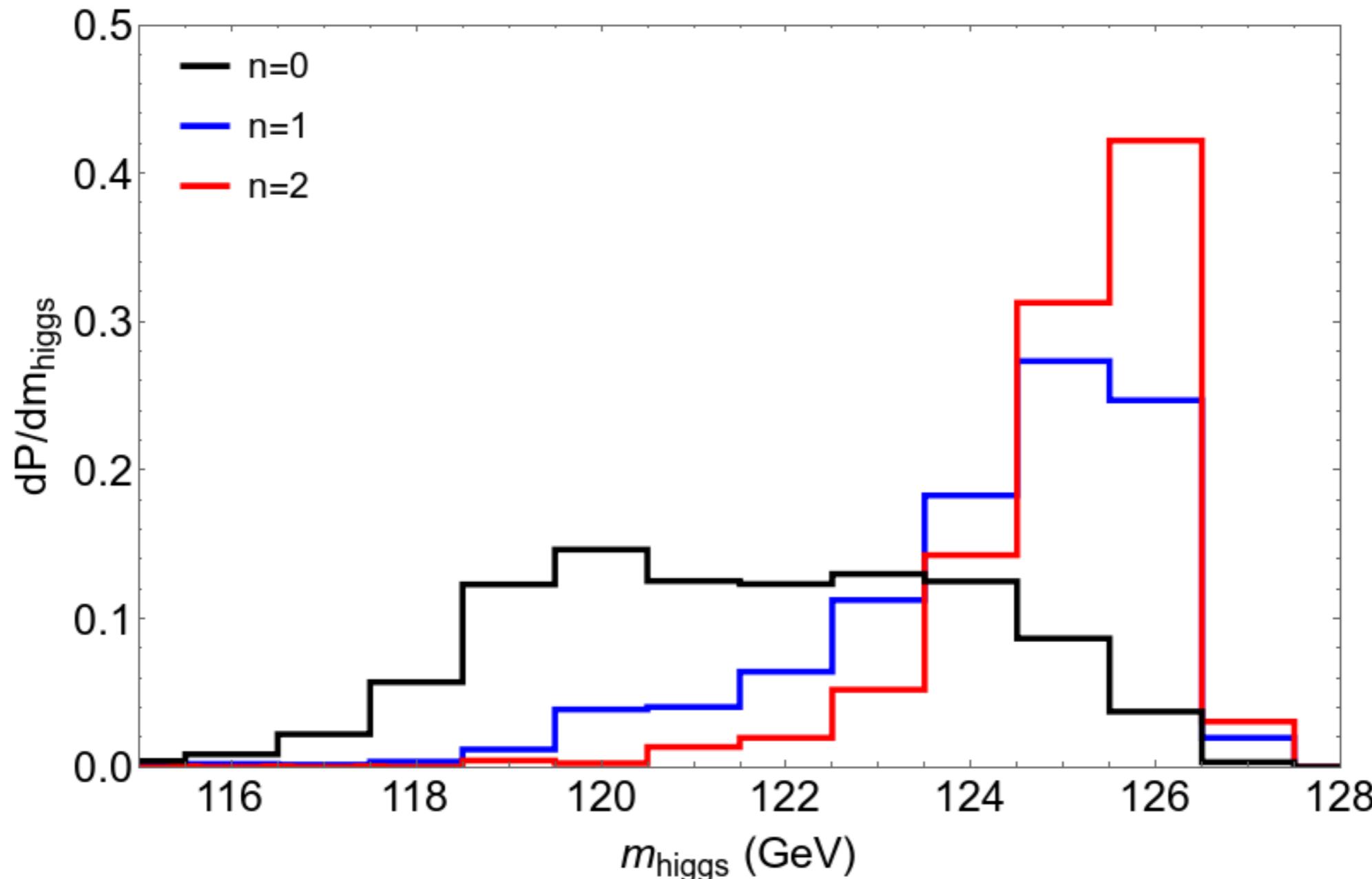
We scan according to  $m_{\text{soft}}^n$  over:

- $m_0(1, 2) : 0.1 - 40 \text{ TeV},$
- $m_0(3) : 0.1 - 20 \text{ TeV},$
- $m_{1/2} : 0.5 - 10 \text{ TeV},$
- $A_0 : 0 - -60 \text{ TeV},$
- $m_A : 0.3 - 10 \text{ TeV},$   
 $\tan \beta : 3 - 60 \quad (\text{flat})$

$\mu = 150 \text{ GeV}$  (fixed)

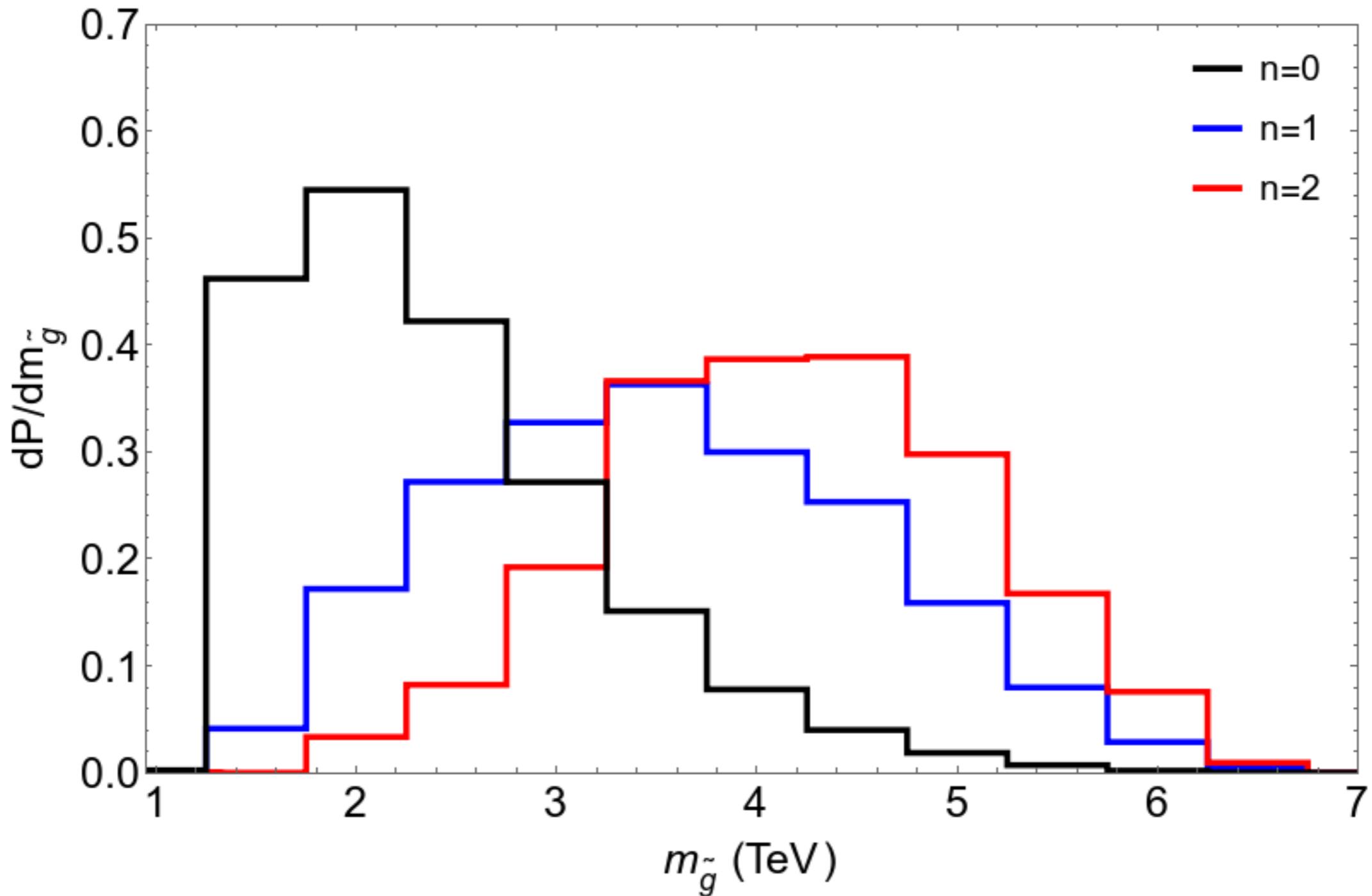
# Making the picture more quantitative:

$$dN_{vac}[m_{hidden}^2, m_{weak}, \Lambda] = f_{SUSY}(m_{hidden}^2) \cdot f_{EWFT} \cdot f_{cc} dm_{hidden}^2$$



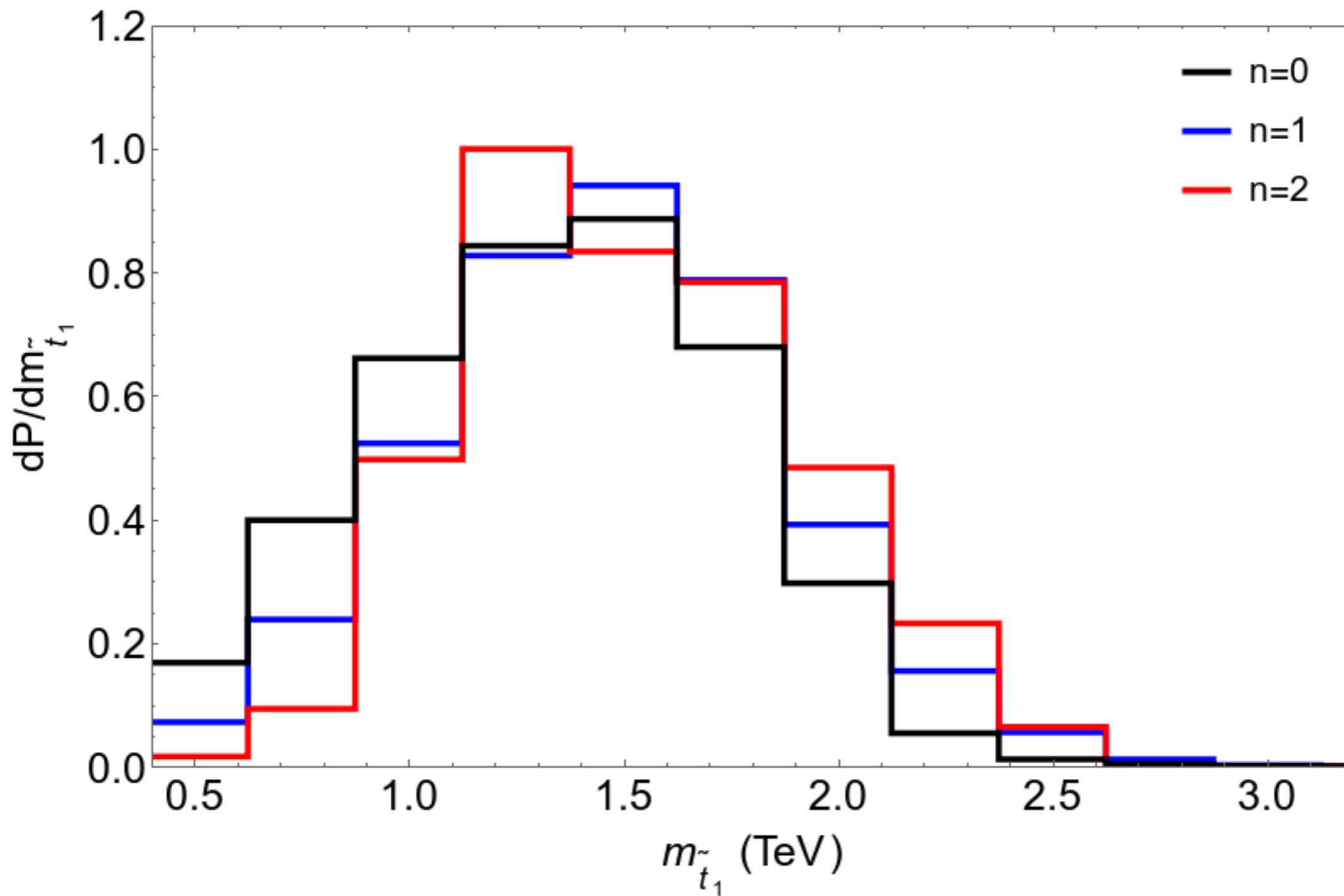
$m(h) \sim 125$  most favored for  $n=1,2$

# What is corresponding distribution for gluino mass?

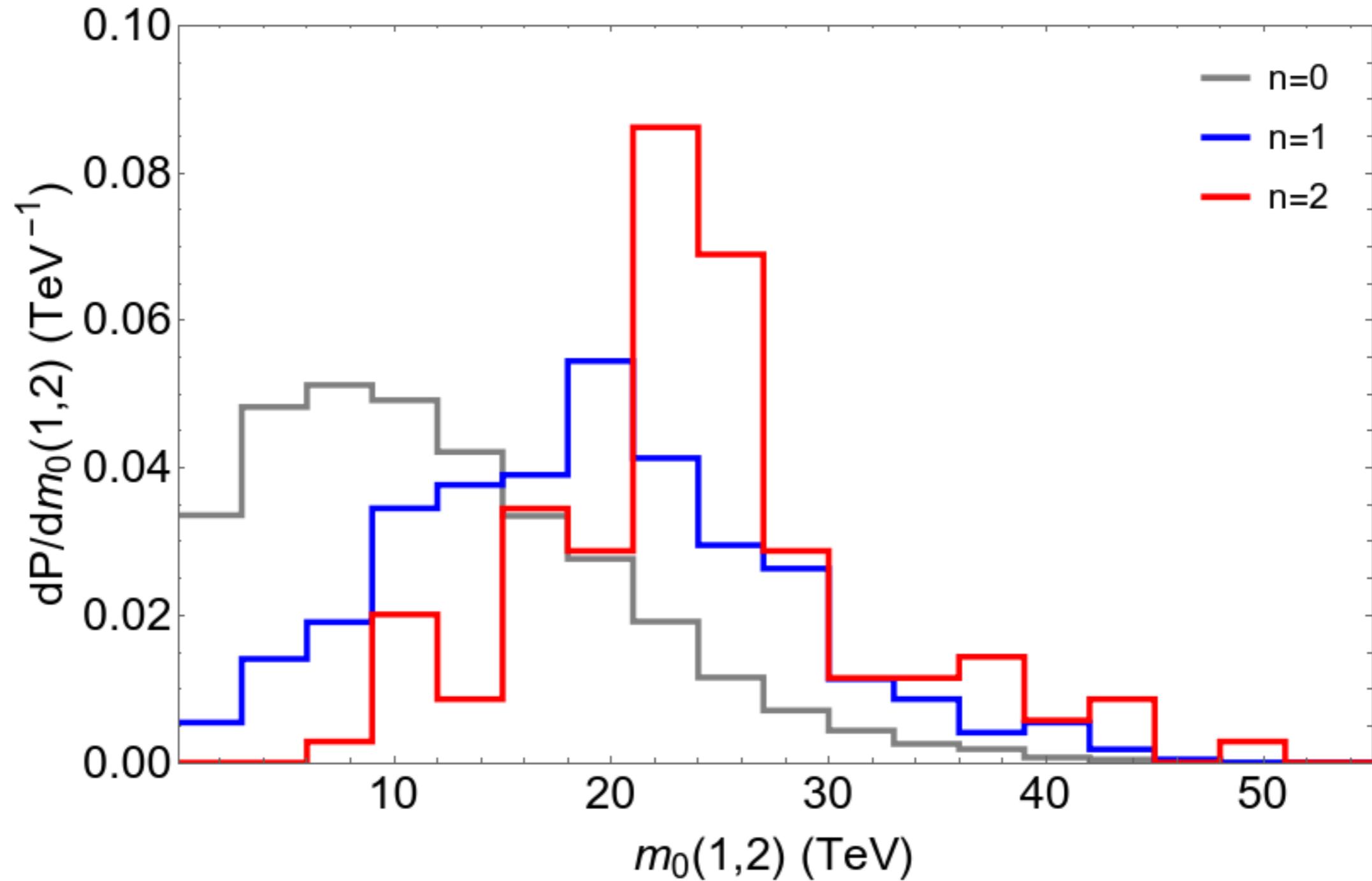


typically beyond LHC 14 reach (may need HE-LHC)

and  $m(t_1)$ ?



first/second generation sfermions pulled  
to 10-30 TeV thus softening any SUSY flavor/CP problems



# Summary n=1,2:

- $m_h \sim 125 \pm 2$  GeV
- $m_{\tilde{g}} \sim 4 \pm 2$  TeV,
- $m_{\tilde{t}_1} \sim 1.5 \pm 0.5$  TeV,
- $m_A \sim 3 \pm 2$  TeV,
- $\tan \beta \sim 13 \pm 7$ ,
- $m_{\widetilde{W}_1, \widetilde{Z}_{1,2}} \sim 200 \pm 100$  GeV and
- $m_{\widetilde{Z}_2} - m_{\widetilde{Z}_1} \sim 7 \pm 3$  GeV with
- $m_0(1, 2) \sim 20 \pm 10$  TeV (for first/second generation matter scalars)

n>=3 case: soft terms pulled so hard usually gives CCB or no EWSB minima in scalar potential or huge value of weak scale  $>^{\sim}$  TeV

# some conclusions

- $\Delta_{EW}$  provides model-independent naturalness bound valid in IR \*and\* correlated UV parameters: SUSY still natural  $\mu \sim 100-200$  GeV, RNS,  $m(t_1) \sim \text{TeV}$  but highly mixed!
- $\mu$  term linked to axion physics: Kim-Nilles/SUSY DFSZ
- PQ symmetry radiatively broken as consequence of SUSY breaking: unifies 3 intermediate mass scales: SUSY-breaking, PQ, Majorana nu
- A mild statistical draw on soft terms from the string landscape coupled with anthropic pull of weak scale to  $\sim 100$  GeV  $\rightarrow m(h) \sim 125$  GeV
- The same draw provides a decoupling solution to SUSY flavor, CP, gravitino problem (and cosmological moduli problem) and expect  $m(3/2) \sim 10-30$  TeV
- Explains why LHC has so far seen no sign of SUSY
- HL-LHC will probe only a portion of natural SUSY p-space
- HE-LHC ( $r_s=27$  TeV; 15 ab<sup>-1</sup>) may be needed for gluino/stop discovery
- dark matter a wimp/axion admixture?
- At ILC250, expect Higgs couplings very SM-like;  
need  $E(\text{CM}) \sim 500-600$  GeV  $> 2m(\text{higgsino})$  to establish SUSY discovery/BSM physics

# Backup

# Some topics for discussion

- What is correct measure for EW naturalness (in SUSY/other models)?  
 $\Delta_{HS}$ ? ,  $\Delta_{BG}$  (what are right  $p_i$ ?)  $\Delta_{EW}$ ? or is naturalness all *subjective*?
- Is naturalness/fine-tuning a path to falsifiability of weak scale SUSY?
- How should contributions to  $\Delta$  be organized? Factors of 2 etc. (Ross, Schmidt-Hoberg, Staub)
- What about non-holonomic soft terms (NHSTs)  $\mu' \tilde{H}_u \tilde{H}_d$ :heavy higgsinos while low fine-tuning?
- Are NHSTs large  $\sim m_{weak}$  or highly suppressed (Martin, 1999)?
- How much is too much fine-tuning? Important for sparticle mass upper limits/falsifiability
- What about fine-tuning in QCD sector- strong CP and  $\bar{\theta} F \tilde{F}$ : axions or other solutions?
- Should one insist on naturalness in both EW and QCD sectors? Interplay between axions and SUSY?
- $\mu$  problem:  $\mu \sim m_{3/2}$  or  $\mu \sim m_{weak} \ll m_{soft}$ ?
- Is there a mechanism behind barely broken EW symmetry in SUSY?
- What does naturalness imply for future accelerators? LHC, HL-LHC, HE-LHC, ILC250, ILC500-600?, FCC, CepC, CppC?
- What does naturalness imply for dark matter? WIMPs? axions? both? other?

# Mirage mediation: comparable moduli- & anomaly-mediation

Choi, Falkowski, Nilles, Olechowski, Pokorski

## Generalized mirage mediation model:

HB, Barger, Serce, Tata: arXiv:1610.06205

$$M_a = (\alpha + b_a g_a^2) m_{3/2} / 16\pi^2, \quad (10)$$

$$A_T = (-a_3 \alpha + \gamma_{L_3} + \gamma_{H_d} + \gamma_{E_3}) m_{3/2} / 16\pi^2, \quad (11)$$

$$A_b = (-a_3 \alpha + \gamma_{Q_3} + \gamma_{H_d} + \gamma_{D_3}) m_{3/2} / 16\pi^2, \quad (12)$$

$$A_t = (-a_3 \alpha + \gamma_{Q_3} + \gamma_{H_u} + \gamma_{U_3}) m_{3/2} / 16\pi^2, \quad (13)$$

$$m_i^2(1, 2) = (c_m \alpha^2 + 4\alpha \xi_i - \dot{\gamma}_i) (m_{3/2} / 16\pi^2)^2, \quad (14)$$

$$m_j^2(3) = (c_{m3} \alpha^2 + 4\alpha \xi_j - \dot{\gamma}_j) (m_{3/2} / 16\pi^2)^2, \quad (15)$$

$$m_{H_u}^2 = (c_{H_u} \alpha^2 + 4\alpha \xi_{H_u} - \dot{\gamma}_{H_u}) (m_{3/2} / 16\pi^2)^2, \quad (16)$$

$$m_{H_d}^2 = (c_{H_d} \alpha^2 + 4\alpha \xi_{H_d} - \dot{\gamma}_{H_d}) (m_{3/2} / 16\pi^2)^2, \quad (17)$$

elevate  $a_3, c_m, c_{m3}, c_{H_u}, c_{H_d}$  from discrete to continuous:  
soft terms depend on location of fields in compactified manifold!

p-space:  $\alpha, m_{3/2}, c_m, c_{m3}, a_3, c_{H_u}, c_{H_d}, \tan \beta \quad (GMM)$   
 $\alpha, m_{3/2}, c_m, c_{m3}, a_3, \tan \beta, \mu, m_A \quad (GMM'). \quad \Leftarrow$

allows for natural mirage mediation

Allows to generate **mini-landscape** spectra

Buchmuller, Hamaguchi, Lebedev, Ratz

Lebedev, Nilles, Raby, Ramos-Sanches, Ratz, Vaudrevange

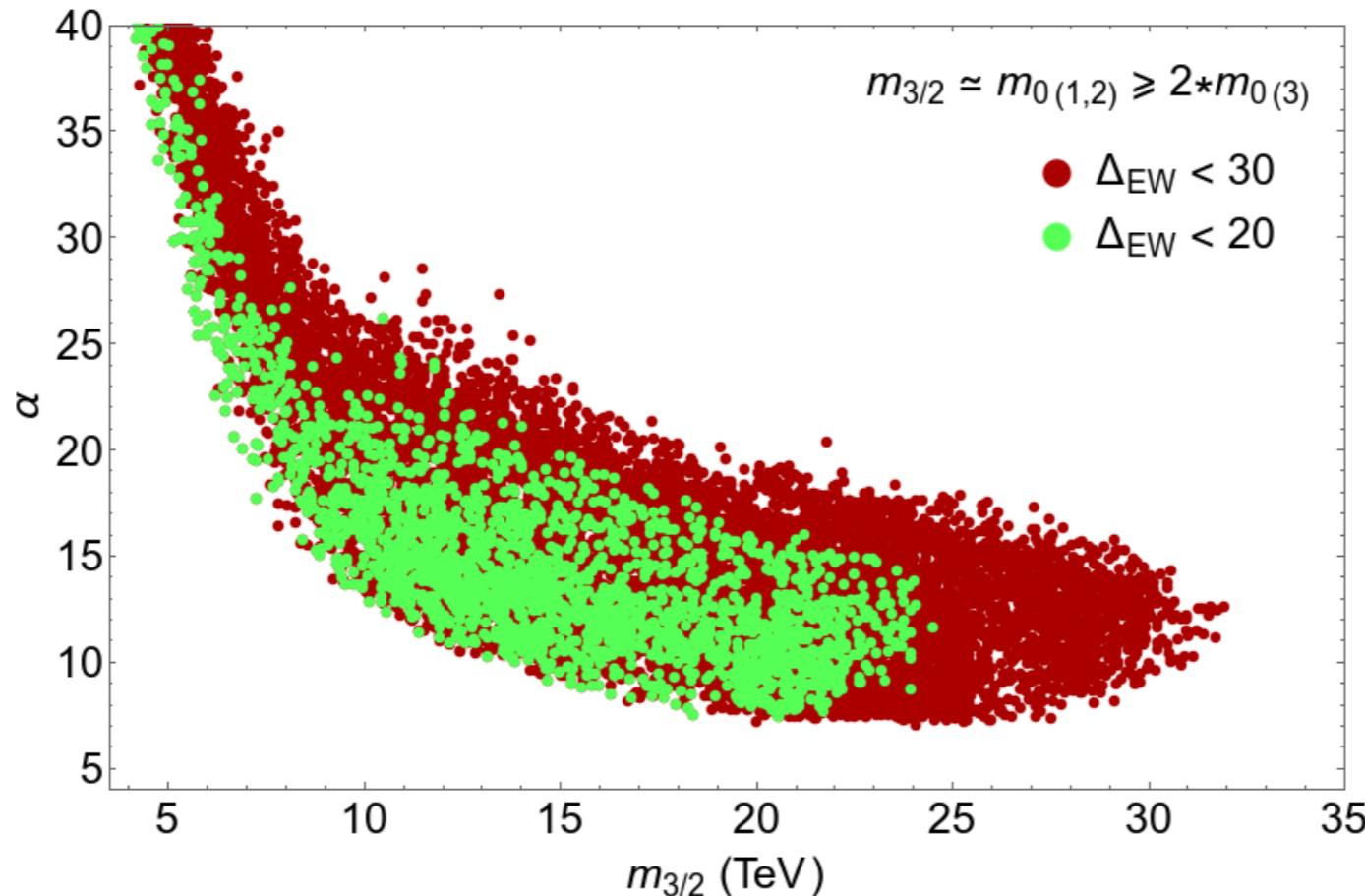
but with radiatively-driven naturalness

HB, Barger, Savoy, Serce, Tata, arXiv:1705.01578

- Begin with heterotic string with orbifold compactification
- Look for fertile patch of landscape giving MSSM
- 1,2 gen lives on orbifold fixed points/tori: in 16 of SO(10)
- 3rd gen, Higgs, gauge live more in bulk: split multiplets
- $m(1,2) \sim m(3/2) \sim 10\text{-}30 \text{ TeV}$
- $m(3) \sim m(H) \sim A's \sim m(\text{inos}) \sim 1\text{-}3 \text{ TeV}$
- soft terms that of mirage mediation
- programmed Isajet 7.86

To generate minilandscape, take:

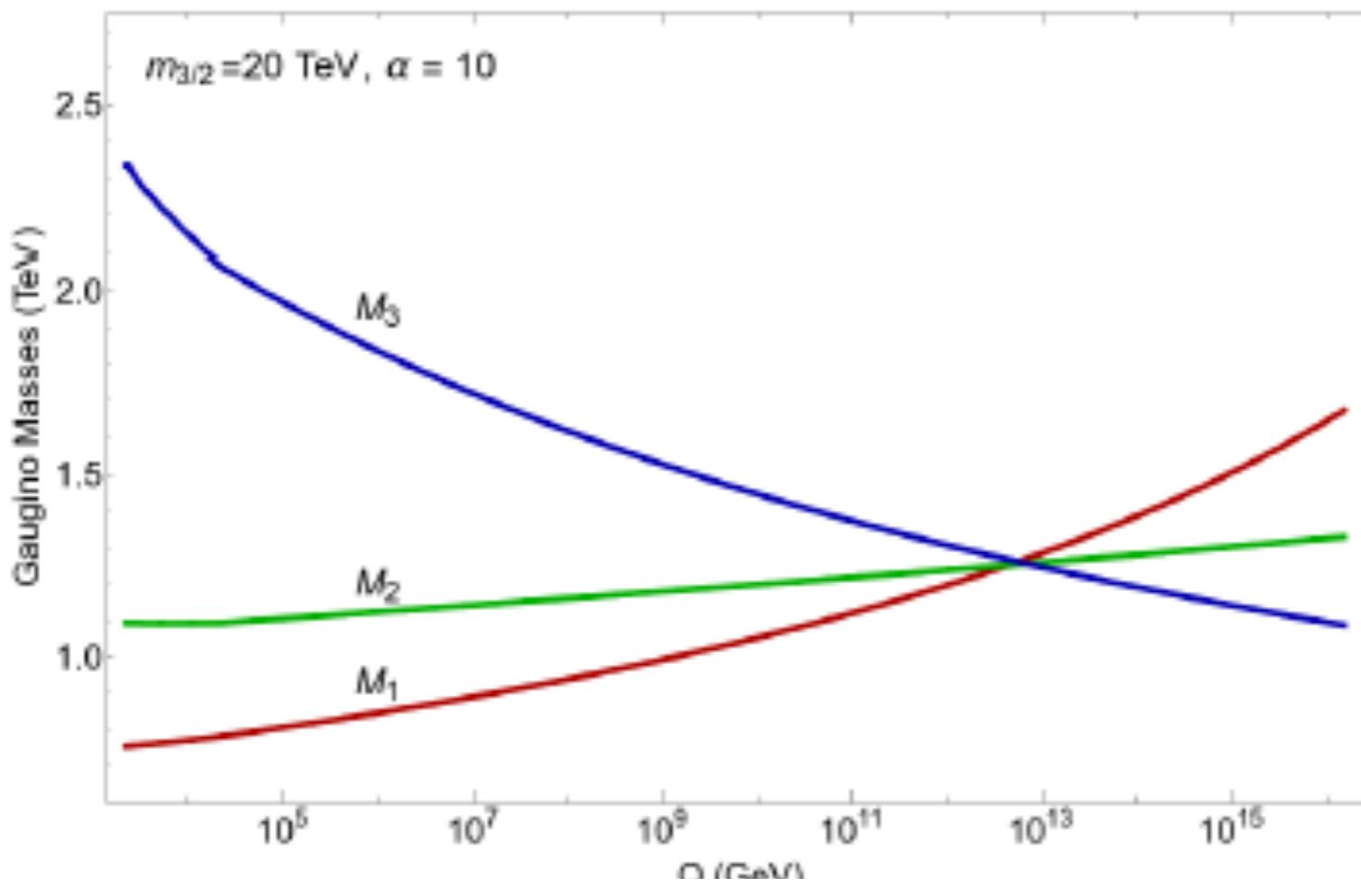
$$c_m = (16\pi^2/\alpha)^2 \text{ so that } m_0(1,2) \simeq m_{3/2}$$



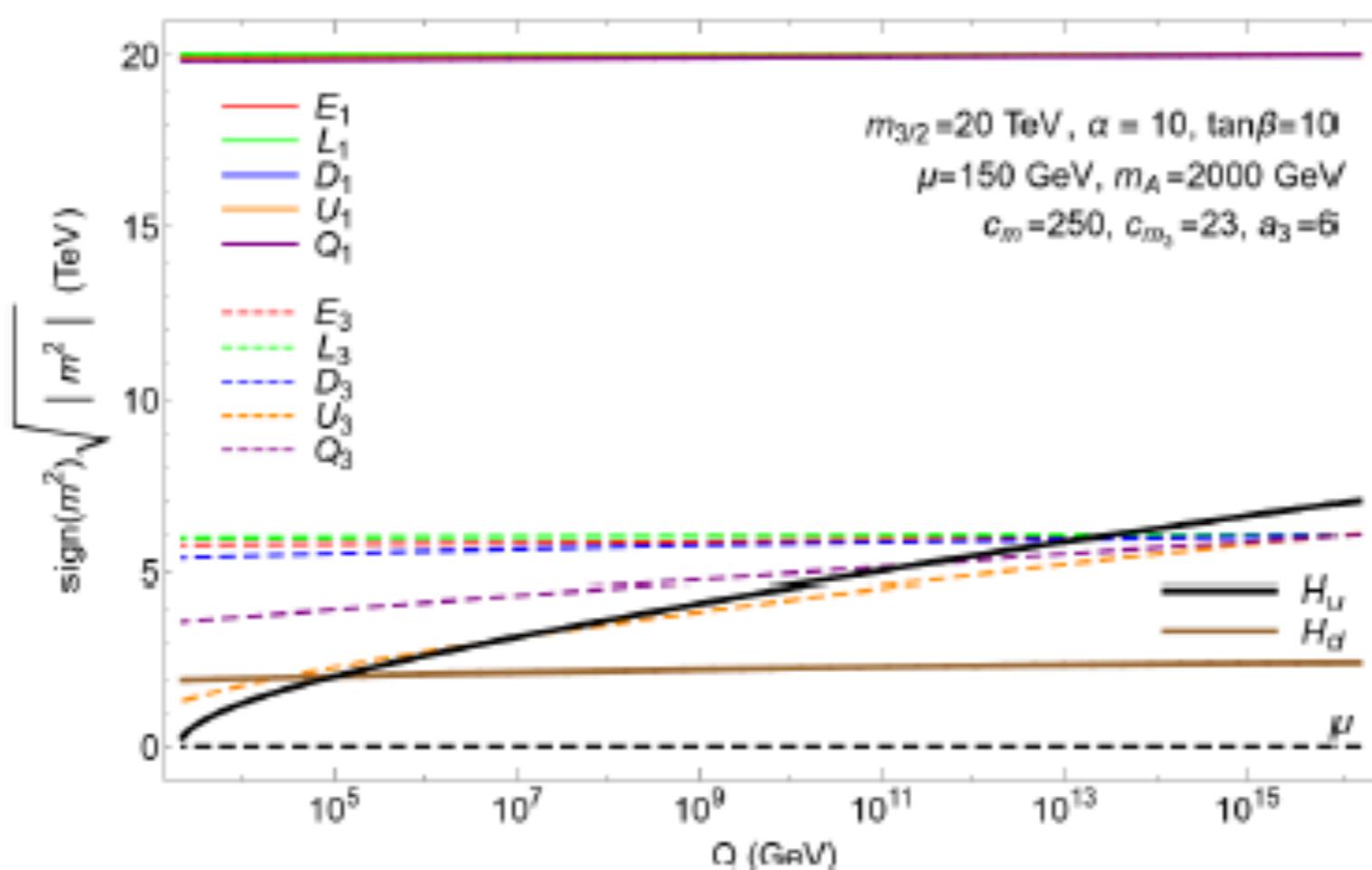
Then get upper bound  $m_{3/2} < 25 - 30$  TeV and  $\alpha > 7$   
else too large  $m_0(1,2)$  drives 3rd generation tachyonic  
Martin, Vaughn, 2-loop RGEs

Increased upper bound on  $m(\text{gluino}) < 6$  TeV

Alpha bound  $\Rightarrow$  mirage unif scale  $> 10^{11}$  GeV  
(not too much compression of inos)



$$\Delta_{EW} = 17.6$$



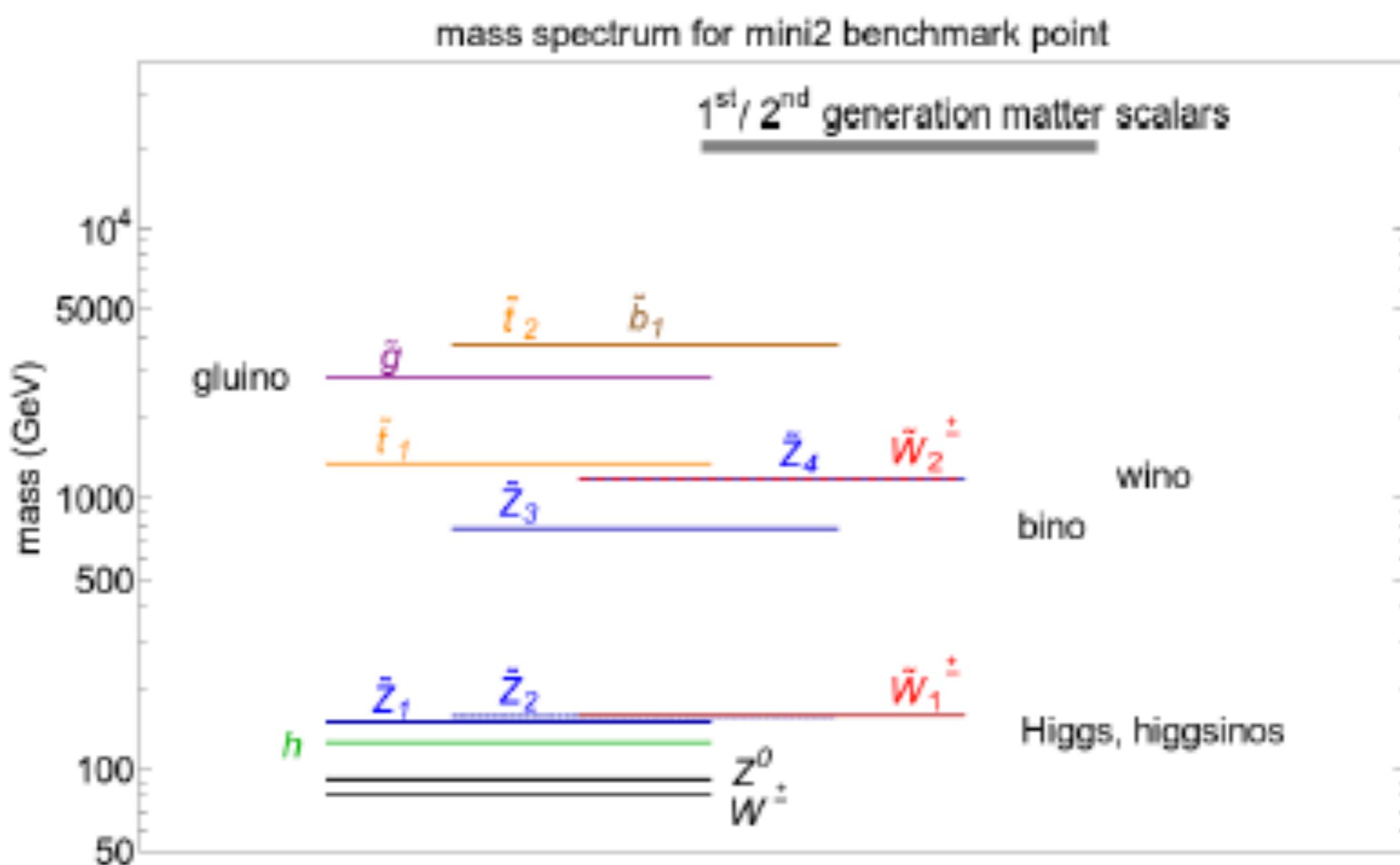
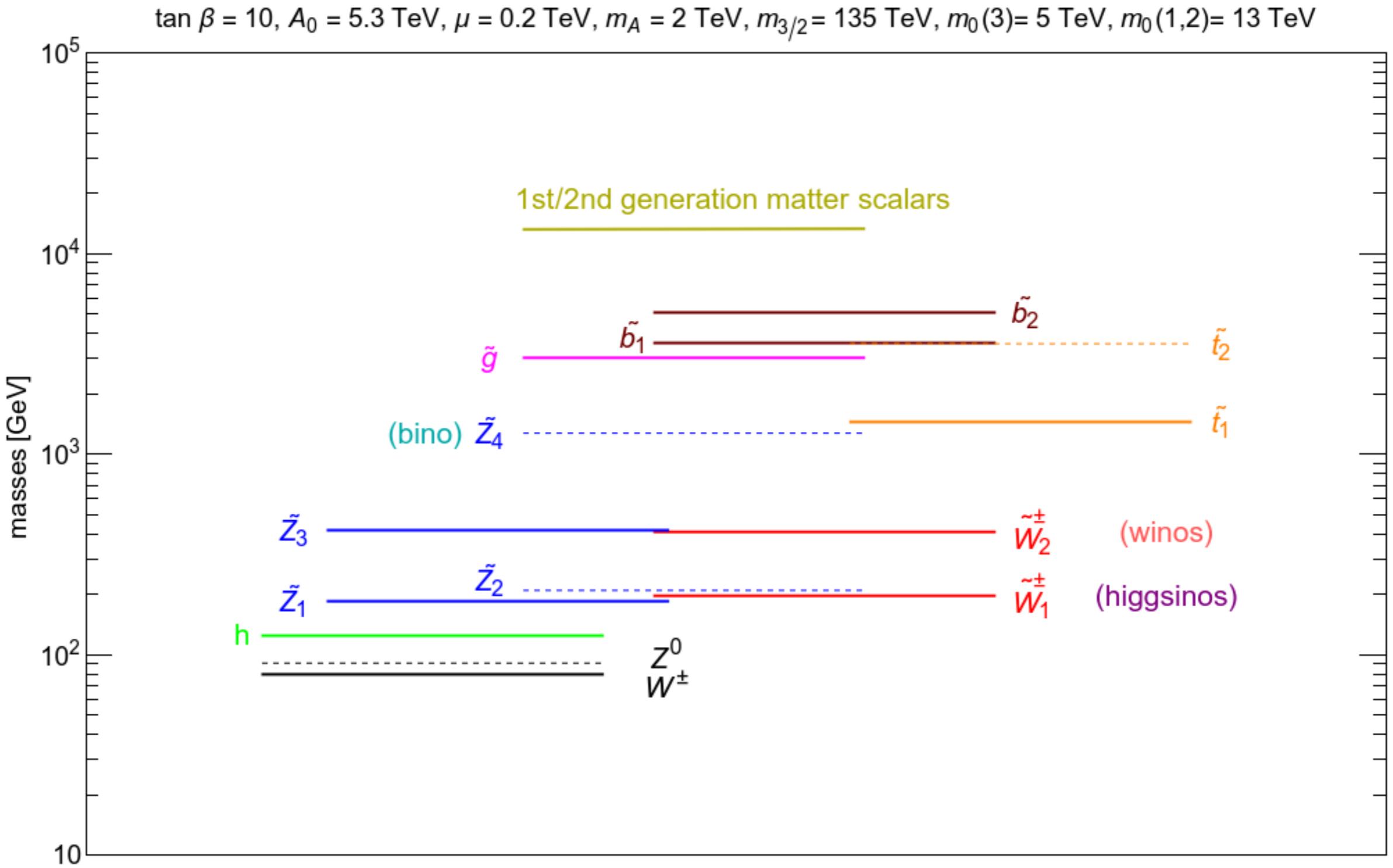


Figure 7: The superparticle mass spectra from the natural mini-landscape point mini2 of Table 1.

# Can also construct natural AMSB models

- Begin with usual mAMSB:  $m_0(\text{bulk}), m_{3/2}, \tan \beta$
- Allow Higgs fields to develop independent bulk soft terms: why shouldn't they? They live in different multiplets (RS)
- Allow small (compared to  $m_{3/2}$ ) bulk  $A_0$  terms (RS)
- Added freedom allows for light higgsinos, highly mixed stops
- Natural AMSB with  $m_h \sim 125$  GeV!
- gauginos still ordered as usual but:  $\mu < M_2 < M_1 < M_3$
- May need ILC with  $\sqrt{s} > 2m(\text{higgsino}) \sim 500 - 600$  GeV to sort out gaugino hierarchy (unified, mirage or AMSB?) via *Higgsino code!*

# natural AMSB with $m(h) \sim 125$ GeV



Summary so far:

First order question:

why is the weak scale  $m(W, Z, h) \sim 100$  GeV?

Because  $m_{\mu}(\text{weak})$ ,  $m_{H_u}(\text{weak}) \sim 100-200$  GeV  
and top squarks  $\sim$  few TeV but highly mixed

Second order question:

Why might  $m_{\mu} < m(\text{SUSY})$   
and why are soft terms such that  
 $m_{H_u}(\text{weak}) \sim 100-200$  GeV?

Some answers: see tomorrow talk!

SUSY mu problem: mu term is SUSY, not SUSY breaking:  
expect  $\mu \sim M_{\text{Pl}}$  but phenomenology requires  $\mu \sim m(Z)$

- NMSSM:  $\mu \sim m(3/2)$ ; but beware singlets!
- Giudice-Masiero:  $\mu$  forbidden by some symmetry:  
generate via Higgs coupling to hidden sector
- **Kim-Nilles**: invoke SUSY version of DFSZ axion  
solution to strong CP:  $W \ni \lambda_\mu S^2 H_u H_d / m_P$

KN: PQ symmetry forbids mu term,  
but then it is generated via PQ breaking

$$\mu \sim \lambda_\mu f_a^2 / m_P$$

Little Hierarchy due to mismatch between  
PQ breaking and SUSY breaking scales?

$$m_{3/2} \sim m_{hid}^2 / M_P$$
$$f_a \ll m_{hid}$$

Higgs mass tells us where  
to look for axion!

$$m_a \sim 6.2 \mu\text{eV} \left( \frac{10^{12} \text{ GeV}}{f_a} \right)$$

# Little Hierarchy from radiative PQ breaking? exhibited within context of MSY/CCK model

Murayama, Suzuki, Yanagida (1992);  
 Gherghetta, Kane (1995)  
 Choi, Chun, Kim (1996)

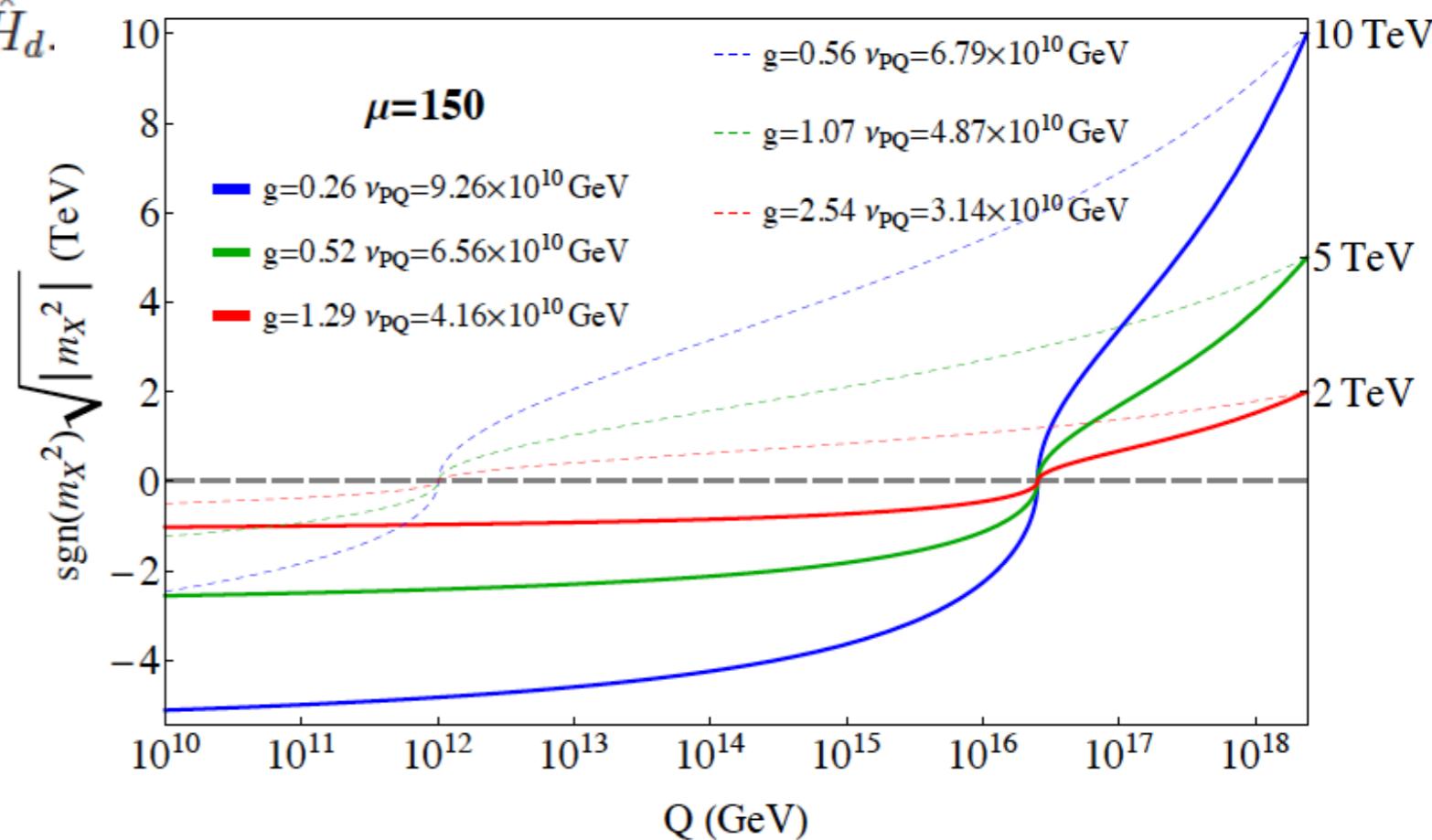
Bae, HB, Serce, PRD91 (2015) 015003

## augment MSSM with PQ charges/fields:

$$\hat{f}' = \frac{1}{2} h_{ij} \hat{X} \hat{N}_i^c \hat{N}_j^c + \frac{f}{M_P} \hat{X}^3 \hat{Y} + \frac{g}{M_P} \hat{X} \hat{Y} \hat{H}_u \hat{H}_d.$$

$$M_{N_i^c} = v_X h_i|_{Q=v_X}$$

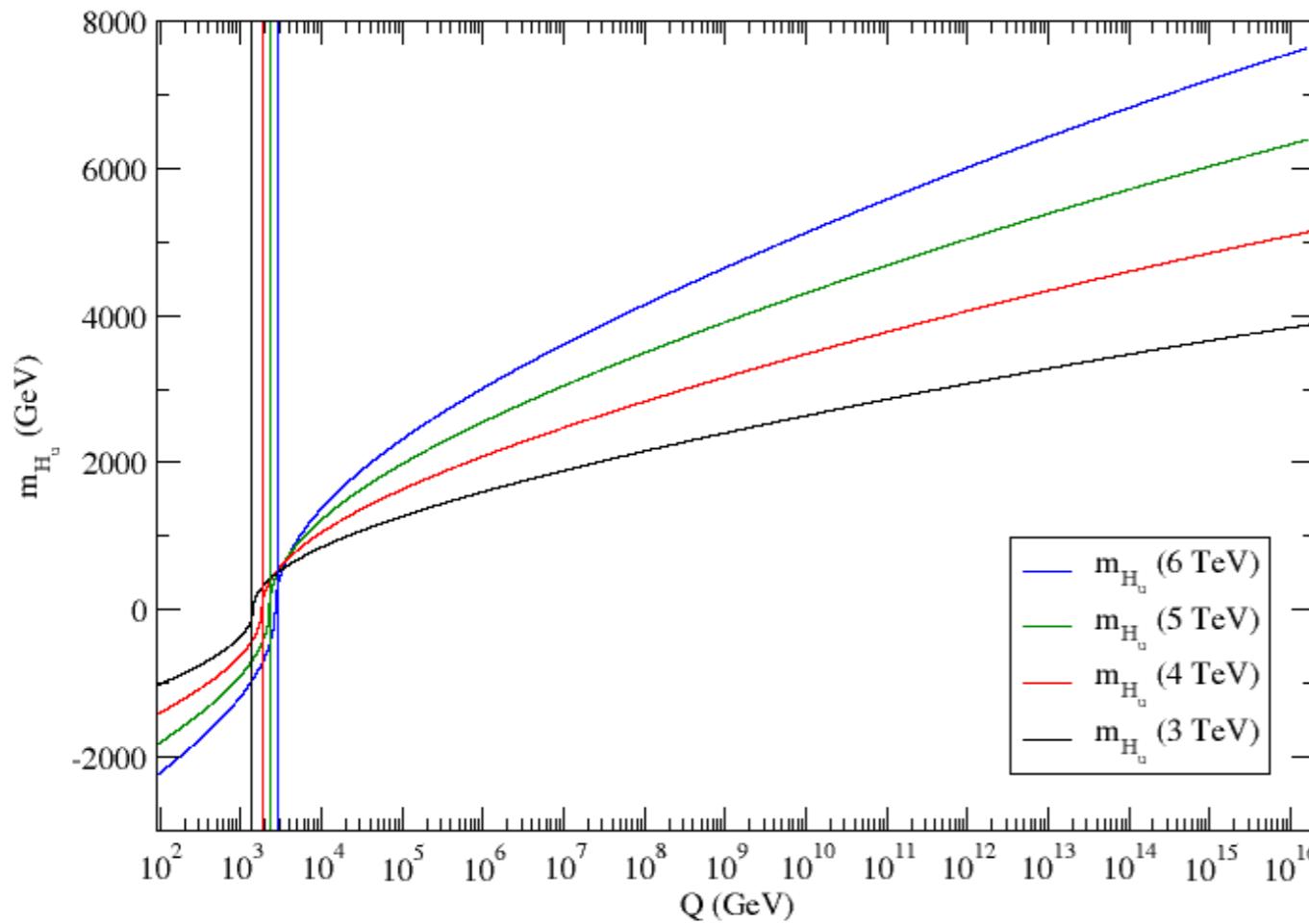
$$\mu = g \frac{v_X v_Y}{M_P} .$$



Large  $m_{3/2}$  generates small  $\mu \sim 100 - 200$  GeV!

# Why might $m_{Hu}$ have the value needed to give naturalness at weak scale?

1. For right correlations amongst soft terms, get “generalized focus point”



e.g.

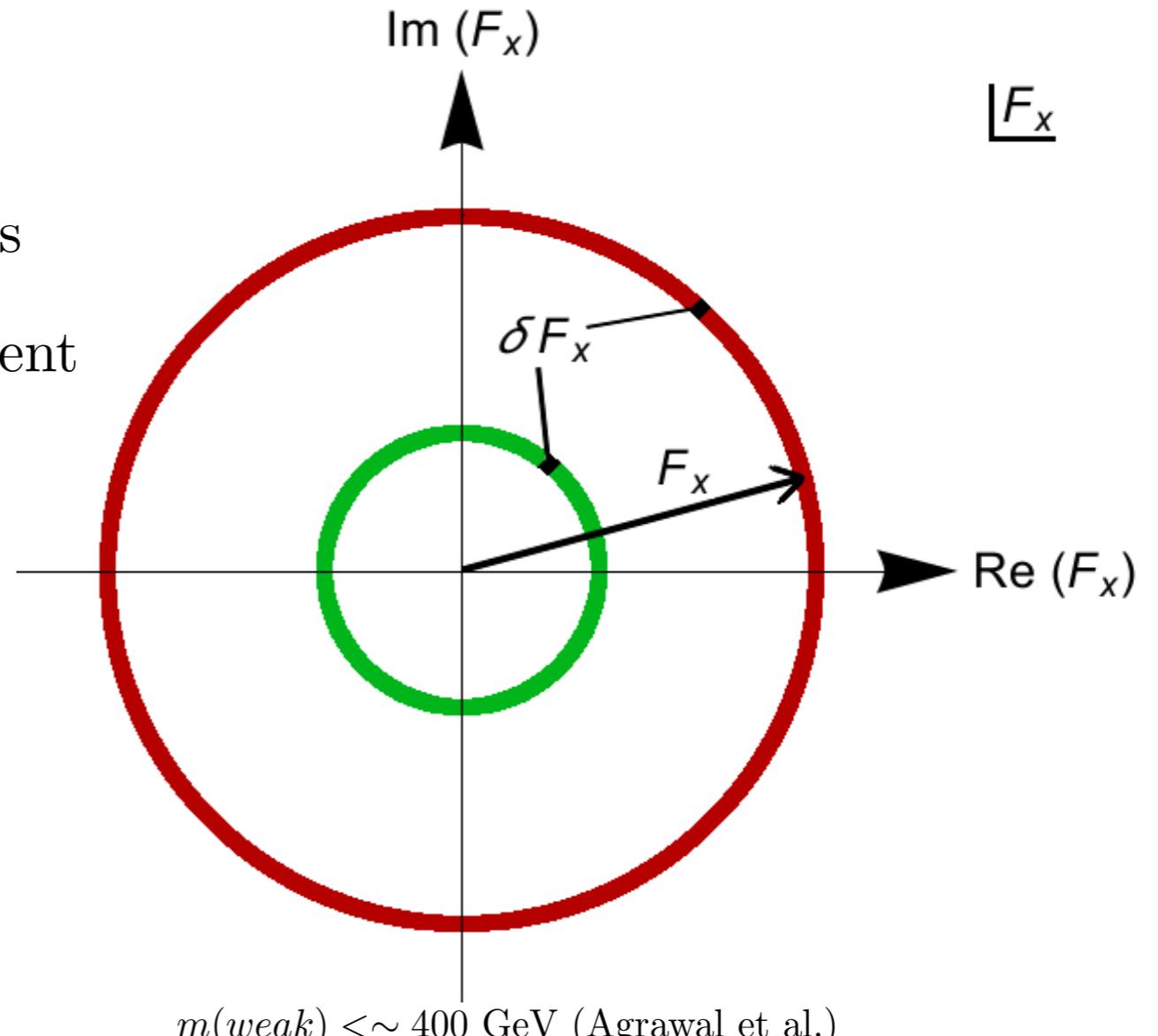
For  $\mu = 150$  GeV,  $\tan \beta = 10$  and

$$\begin{aligned} m_0^2 &= m_{3/2}^2 \\ A_0 &= -1.6m_{3/2} \\ m_{1/2} &= m_{3/2}/5 \\ m_{H_d}^2 &= m_{3/2}^2/2. \end{aligned}$$

# Why do soft terms take on values needed for natural (barely-broken) EWSB?

## 2. string theory landscape?

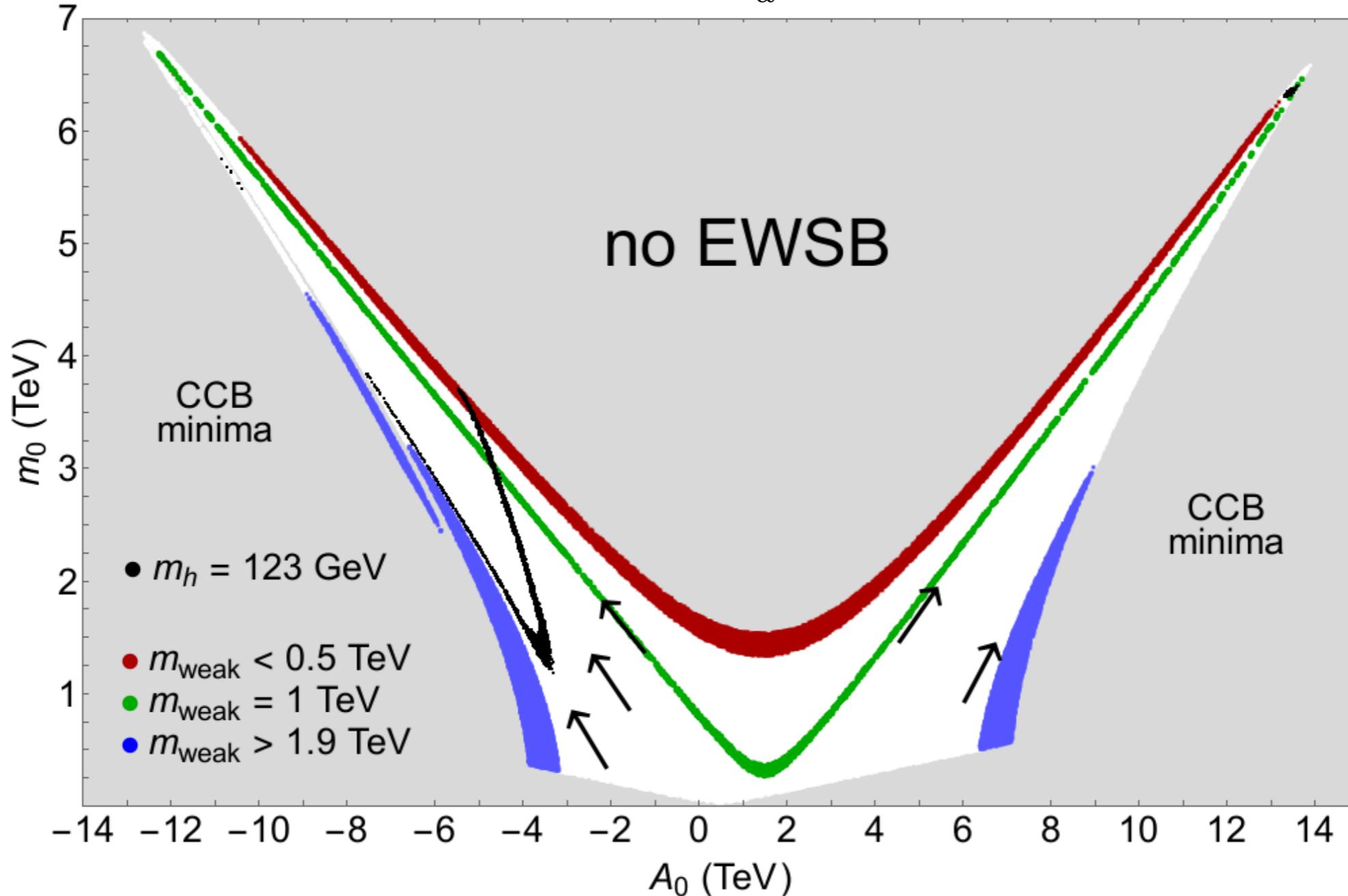
- assume model like MSY/CCK where  $\mu \sim 100$  GeV
- then  $m(\text{weak})^2 \sim |m_{H_u}^2|$
- If all values of SUSY breaking field  $\langle F_X \rangle$  equally likely, then mild (linear) statistical draw towards large soft terms
- This is balanced by anthropic requirement of weak scale  $m_{\text{weak}} \sim 100$  GEV



*Anthropic selection of  $m_{\text{weak}} \sim 100$  GeV:*

If  $m_W$  too large, then weak interactions  $\sim (1/m_W^4)$  too weak  
weak decays, fusion reactions suppressed  
elements not as we know them

$$m_{H_u} = 1.3m_0$$



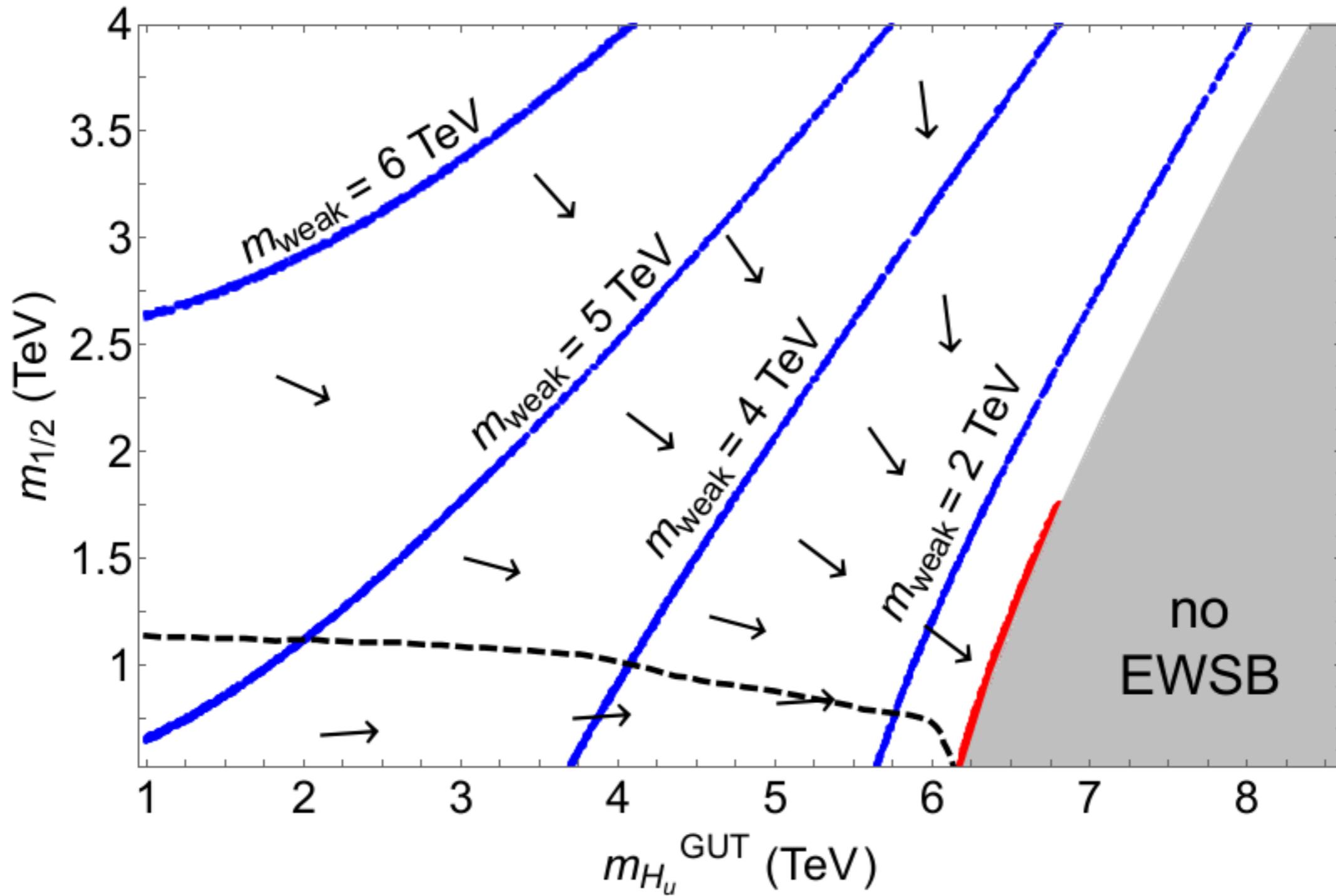
statistical draw to large soft terms balanced by  
anthropic draw toward red ( $m(\text{weak}) \sim 100$  GeV):  
then  $m(\text{Higgs}) \sim 125$  GeV and natural SUSY spectrum!

Denef, Douglas, JHEP0405 (2004) 072

Giudice, Rattazzi, NPB757 (2006) 19;

HB, Barger, Savoy, Serce, PLB758 (2016) 113

$$m_0 = 5 \text{ TeV}$$



statistical/anthropic draw toward FP-like region

# Statistical analysis of SUSY breaking scale:

M. Douglas, hep-th/0405279

## some reasonable assumptions

- string theory landscape contains vast ensemble of  $N=1$ ,  $d=4$  SUGRA EFTs at high scales
- the EFTs contain the SM as weak scale EFT
- the EFTs contain visible sector +potentially large hidden sector
- visible sector contains MSSM plus extra gauge singlets (e.g. a PQ sector, RN neutrinos,...)
- SUGRA is broken spontaneously via superHiggs mechanism via either F- or D- terms or in general a combination

Scalar potential is given by usual SUGRA form:

$$\begin{aligned} V &= e^{K/m_P^2} \left( g^{i\bar{j}} D_i W D_{\bar{j}} W^* - \frac{3}{m_P^2} |W|^2 \right) + \frac{1}{2} \sum_{\alpha} D_{\alpha}^2 \\ &= e^{K/m_P^2} \left( \sum_i |F_i|^2 - 3 \frac{|W|^2}{m_P^2} \right) + \frac{1}{2} \sum_{\alpha} D_{\alpha}^2 \end{aligned}$$

- $W$  = holomorphic superpotential
- $K$  = real Kähler function
- $F_i = D_i W = DW/D\phi^i \equiv \partial W/\partial\phi^i + (1/m_P^2)(\partial K/\partial\phi^i)W$  are  $F$ -terms
- $D_{\alpha} \sim \sum \phi^{\dagger} g t_{\alpha} \phi$  are  $D$ -terms
- $\phi^i$  are chiral superfields

**minimize**  $V$ :

- $\partial V/\partial\phi^i = 0$
- $\partial^2 V/\partial\phi^i\partial\phi^j > 0$
- $\Lambda_{cc} = m_{hidden}^4 - 3e^{K/m_P^2}|W|^2/m_P^2$  with
- $m_{hidden}^4 = \sum_i |F_i|^2 + \frac{1}{2} \sum_{\alpha} D_{\alpha}^2$  is hidden sector mass scale

gravitino mass  $m_{3/2} = e^{K/2m_P^2} m_P \sim m_{hidden}^2/m_P$  with  $m_{hidden} \sim 10^{12}$  GeV

# Denef&Douglas: statistics of SUSY breaking in landscape

DD observation:  $W_0$  distributed uniformly as complex variable allows dynamical neutralization of  $\Lambda$  while not influencing SUSY breaking

Then, number of flux vacua containing spontaneously broken SUGRA with SUSY breaking scale  $m_{hidden}^2$  is:

$$dN_{vac}[m_{hidden}^2, m_{weak}, \Lambda] = f_{SUSY}(m_{hidden}^2) \cdot f_{EWFT} \cdot f_{cc} dm_{hidden}^2$$

- $f_{cc} \sim \Lambda/m^4$  where DD maintain  $m \sim m_{string}$  and not  $m_{hidden}$
- $f_{SUSY}(m_{hidden}^2) \sim (m_{hidden}^2)^{2n_F+n_D-1}$  for uniformly distributed values of  $F$  and  $D$  breaking fields
- $f_{EWFT} \sim m_{weak}^2/m_{soft}^2$  (?) where  $m_{soft} \sim m_{3/2} \sim m_{hidden}^2/m_P$

$$n = 2n_F + n_D - 1$$

$$f_{SUSY} \sim m_{soft}^n$$

landscape favors high scale SUSY breaking  
tempered by f(EWFT) anthropic penalty!

$n_F$	$n_D$	$n$
0	1	0
1	0	1
0	2	1
1	1	2
0	3	2
2	0	3
2	1	4

What about DD/AD anthropic penalty  $f_{EWFT} \sim m_{weak}^2/m_{soft}^2$ ?

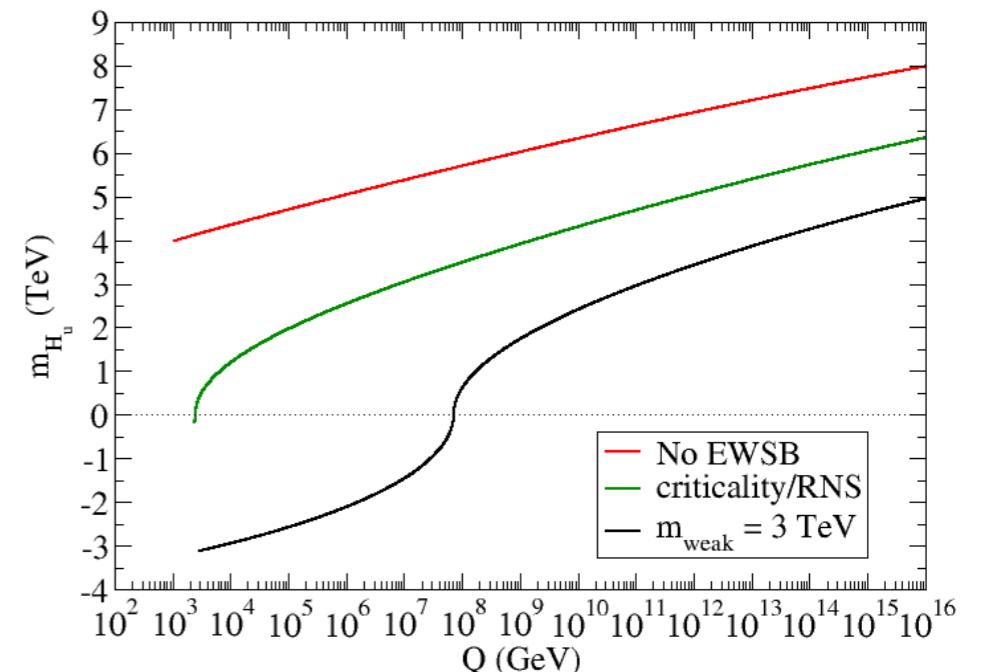
This fails in a variety of *practical* cases:

- $A$ -terms get large:  $\Rightarrow CCB$  minima
- $m_{H_u}^2$  too large: fail to break EW symmetry

Must require proper EWSB!

Even if EWS properly broken, then

- large  $A_t$  reduces EWFT in the  $\Sigma_u^u(\tilde{t}_{1,2})$
- large  $m_{H_u}^2(m_{GUT})$  needed to radiatively drive  $m_{H_u}^2$  to natural value at weak scale



Better proposal:  $f_{EWFT} \Rightarrow \Theta(30 - \Delta_{EW})$

keeps calculated weak scale within factor  $\sim 4$  of measured weak scale  
 $m_{weak} \equiv m_{W,Z,h} \sim 100$  GeV

Assume  $\mu \sim 100 - 200$  GeV via e.g. rad PW breaking: then  $m_Z$  variable and may be large depending on soft terms  $m_{H_{u,d}}^2$  and  $\Sigma_{u,d}^{u,d}(i)$

$$\frac{m_Z^2}{2} = \frac{m_{H_d}^2 + \Sigma_d^d - (m_{H_u}^2 + \Sigma_u^u) \tan^2 \beta}{\tan^2 \beta - 1} - \mu^2$$

For practical calculations, adopt NUHM3 SUGRA model:

- $m_0(1, 2) = \text{gen}(1, 2)$  common soft mass
- $m_0(3) = \text{gen}(3)$  common soft mass
- $m_{H_u}^2$  up-Higgs soft mass
- $m_{H_d}^2$  down-Higgs soft mass
- $m_{1/2}$  unified gaugino mass
- $A_0$  unified trilinear soft term
- $\tan \beta$

Trade  $m_{H_u}^2, m_{H_d}^2 \Leftrightarrow \mu, m_A$

$m_0(1, 2), m_0(3), m_{1/2}, A_0, \tan \beta, \mu, m_A$  (NUHM3)

Recent work: place on more quantitative footing:  
scan soft SUSY breaking parameters as  $m(\text{soft})^n$   
along with  $f(\text{EWFT})$  penalty

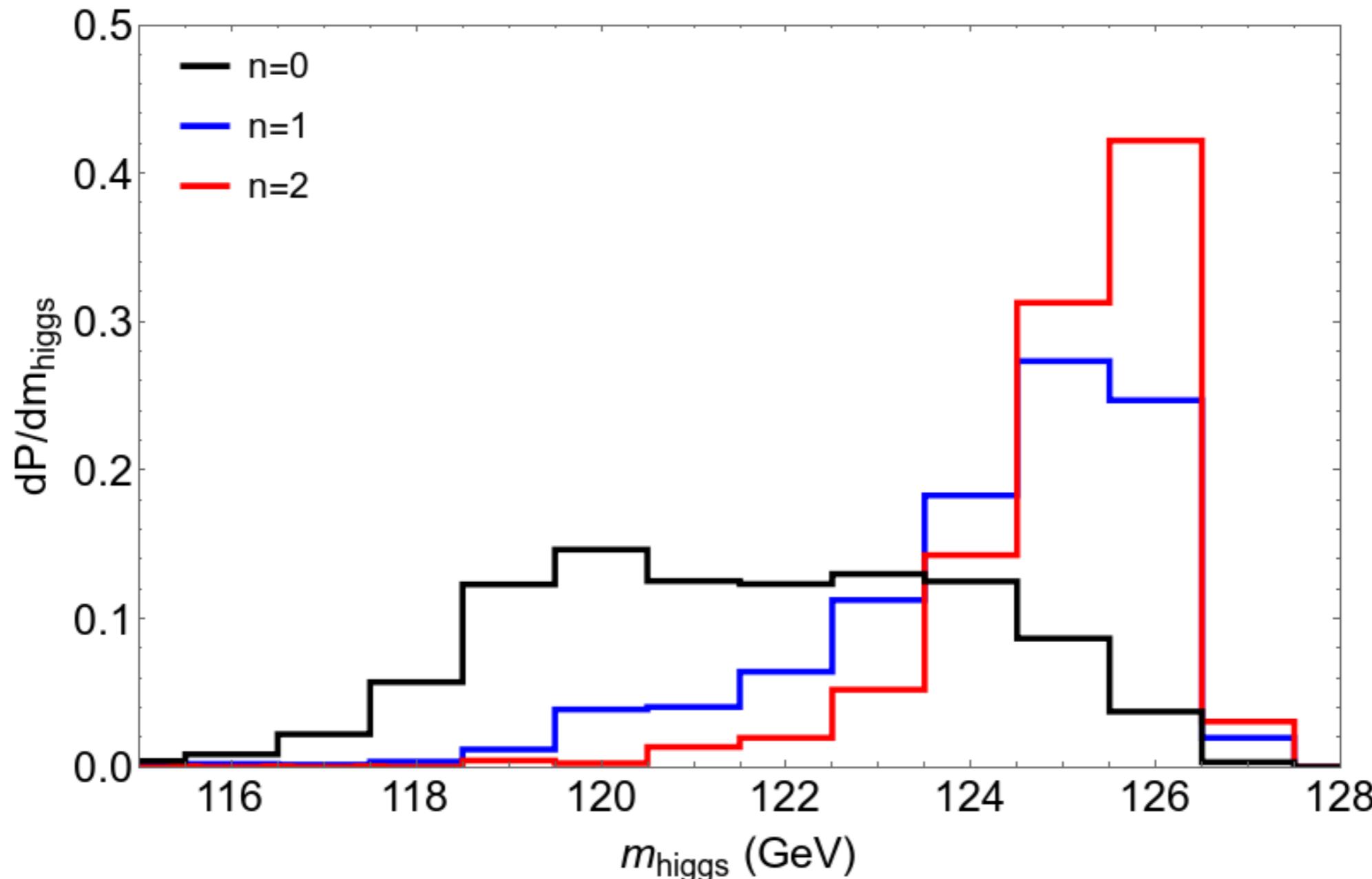
We scan according to  $m_{\text{soft}}^n$  over:

- $m_0(1, 2) : 0.1 - 40 \text{ TeV},$
- $m_0(3) : 0.1 - 20 \text{ TeV},$
- $m_{1/2} : 0.5 - 10 \text{ TeV},$
- $A_0 : 0 - -60 \text{ TeV},$
- $m_A : 0.3 - 10 \text{ TeV},$   
 $\tan \beta : 3 - 60 \quad (\text{flat})$

$\mu = 150 \text{ GeV}$  (fixed)

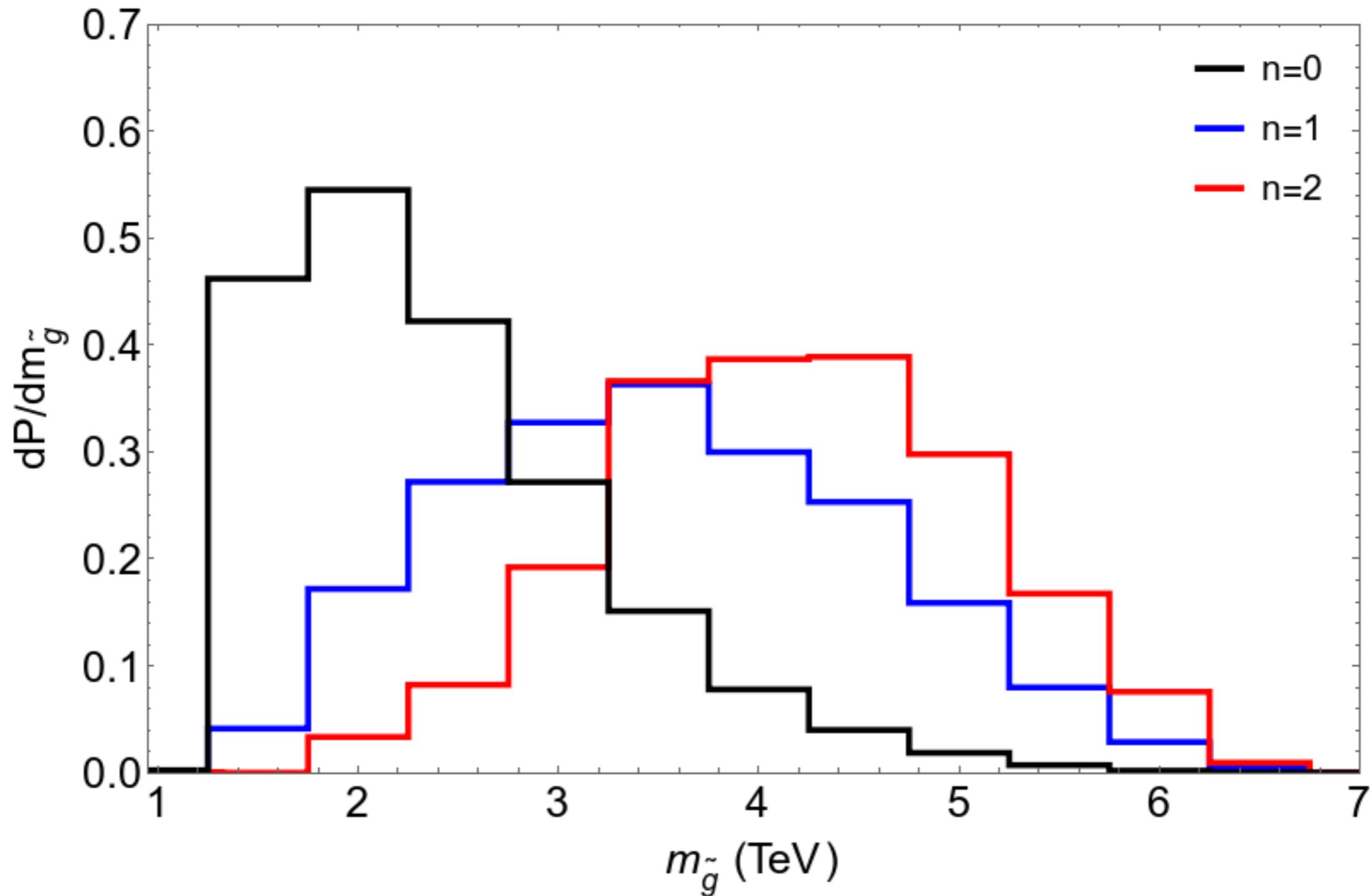
# Making the picture more quantitative:

$$\text{ac}[m_{\text{hidden}}^2, m_{\text{weak}}, \Lambda] = f_{SUSY}(m_{\text{hidden}}^2) \cdot f_{EWFT} \cdot f_{cc} dm_{\text{hidden}}^2$$



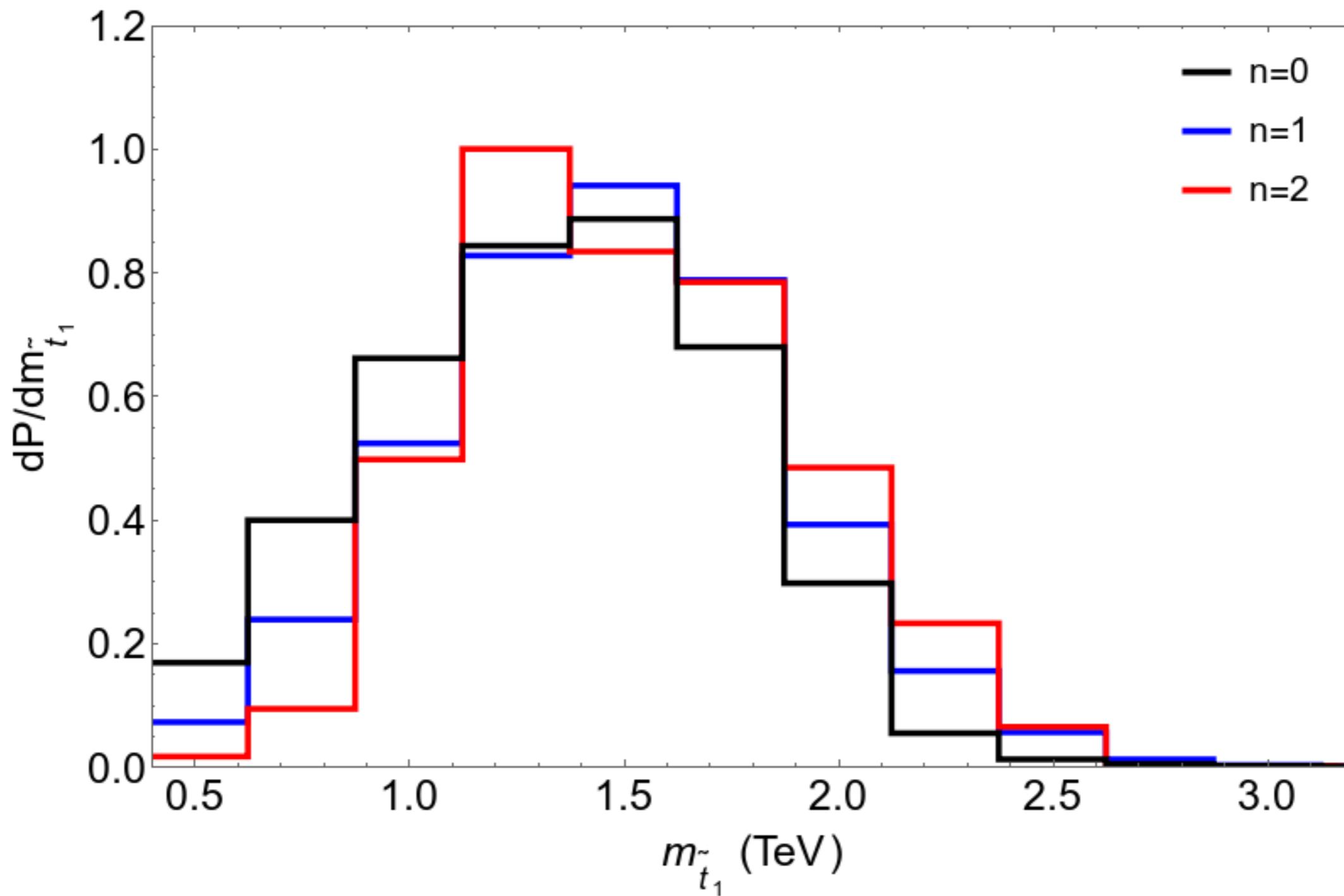
$m(h) \sim 125$  most favored for  $n=1,2$

# What is corresponding distribution for gluino mass?



typically beyond LHC 14 reach (may need HE-LHC)

and  $m(t_1)$ ?



# Conclusion: SUSY IS alive and well!

- old calculations of naturalness over-estimate fine-tuning
- naturalness: Little Hierarchy  $\mu \ll m(\text{SUSY})$  allowed
- radiatively-driven naturalness:  $\mu \sim 100-200 \text{ GeV}$ ,  $m(t_1) < 3 \text{ TeV}$ ,  $m(\text{gluino}) < 5-6 \text{ TeV}$
- SUSY DFSZ axion: solve strong CP, solve SUSY mu problem; generate  $\mu \ll m(\text{SUSY})$
- landscape pull on soft terms towards RNS,  $m(h) \sim 125 \text{ GeV}$
- natural mirage-mediation/mini-landscape
- natural NUHM2: HL-LHC can cover via  $S\bar{S}d\bar{B} + Z1Z2j$  channels
- natural mirage/mini-landscape may escape detection at HL-LHC; need LHC33!
- expect ILC as higgsino factory
- DM= axion+higgsino-like WIMP admixture: detect both?
- higgsino-like WIMP detection likely; axion more difficult

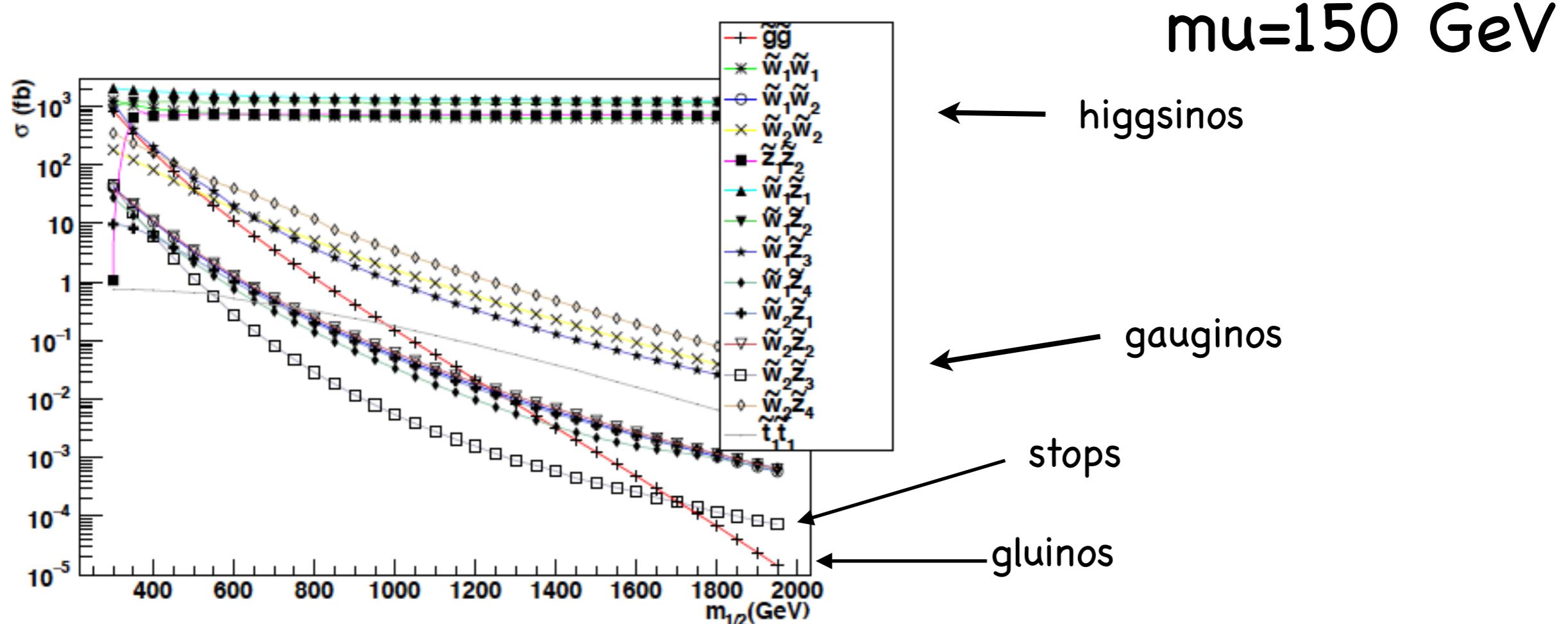
# Backup

# Prospects for SUSY at LHC:

signature list for radiatively-driven natural SUSY:

- $\tilde{g}\tilde{g}$
- $\tilde{t}_1\tilde{t}_1^*$
- $\tilde{Z}_1\tilde{Z}_2$  (higgsino pair production)
- $\tilde{W}_2^\pm\tilde{Z}_4$  (wino pair production)

# Sparticle prod'n along RNS model-line at LHC14:



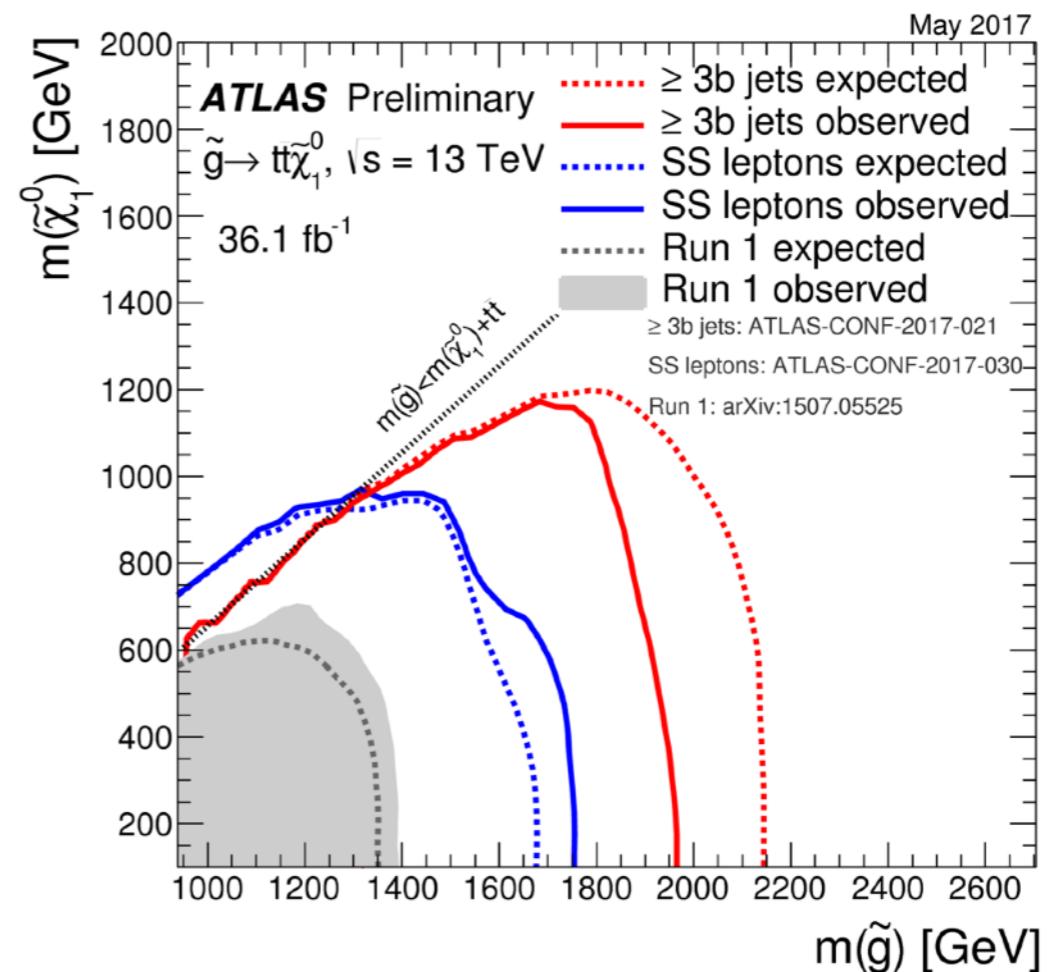
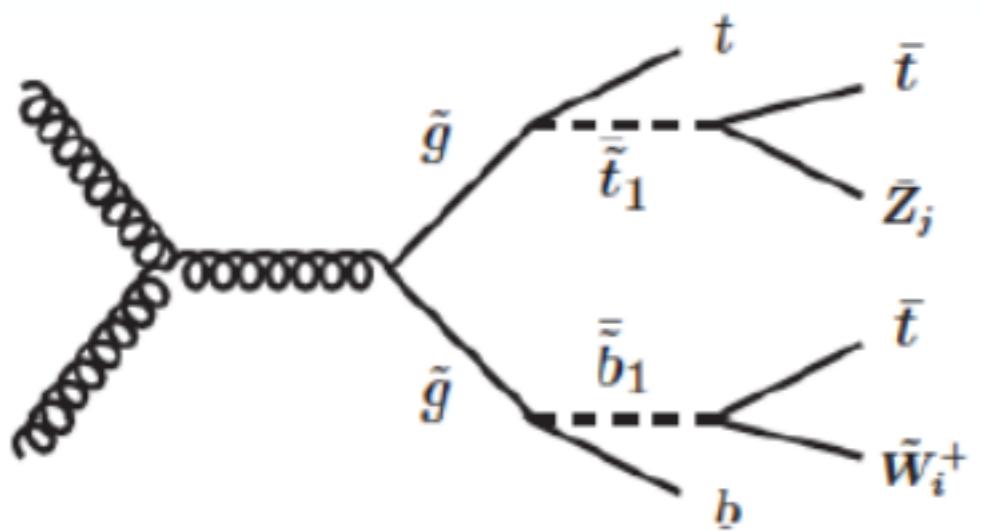
higgsino pair production dominant-but only soft visible energy release from higgsino decays

largest visible cross section: wino pairs

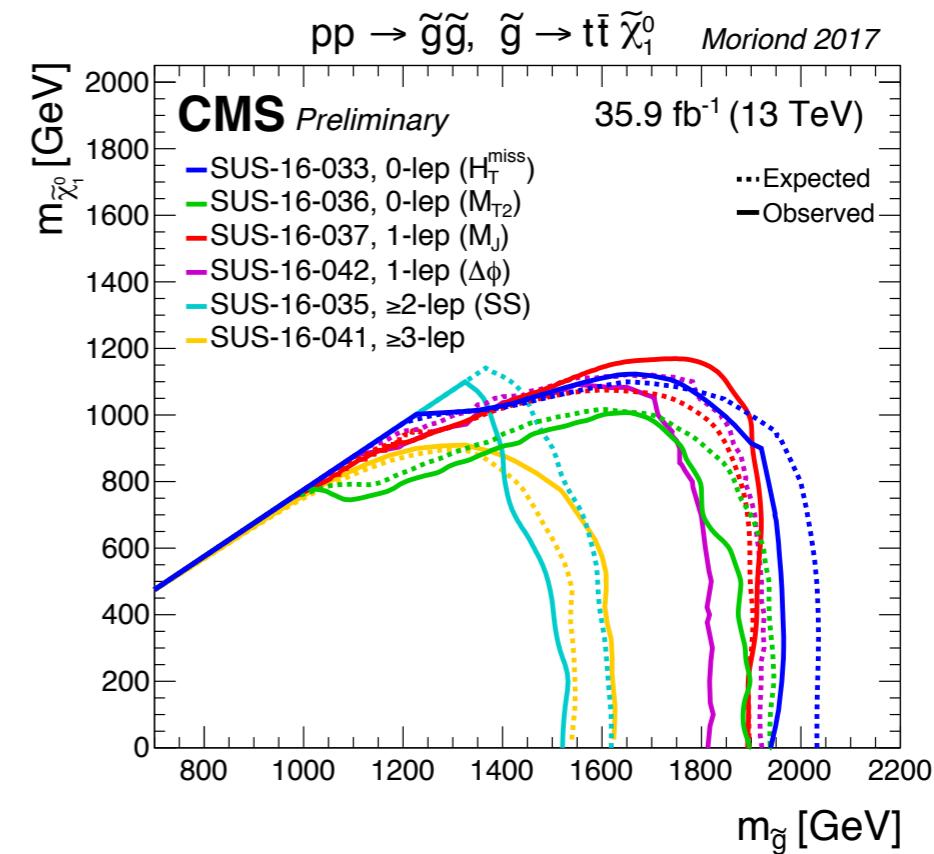
gluino pairs sharply dropping

stops at bottom

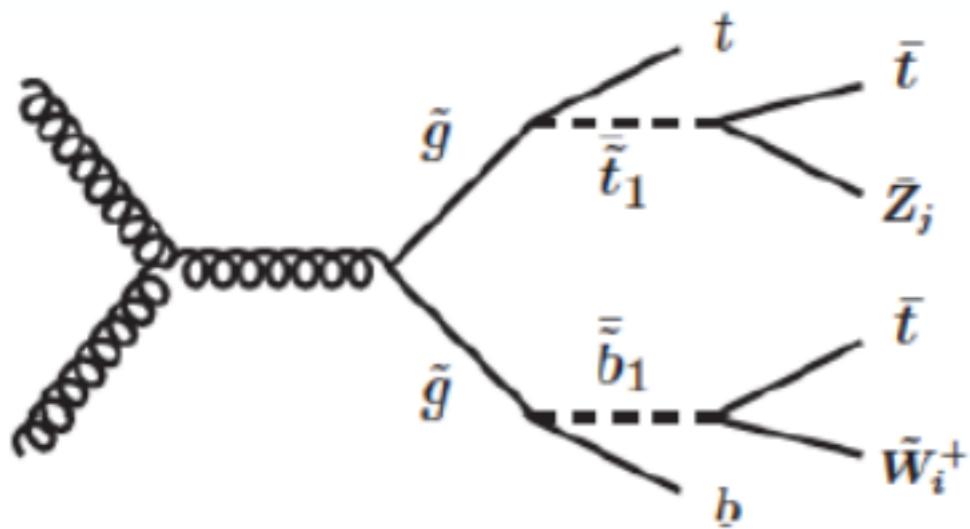
# gluino pair cascade decay signatures



Current limits for  $m(Z_1) \sim 150 \text{ GeV}$ :  
 $m(\text{glino}) > \sim 2 \text{ TeV}$

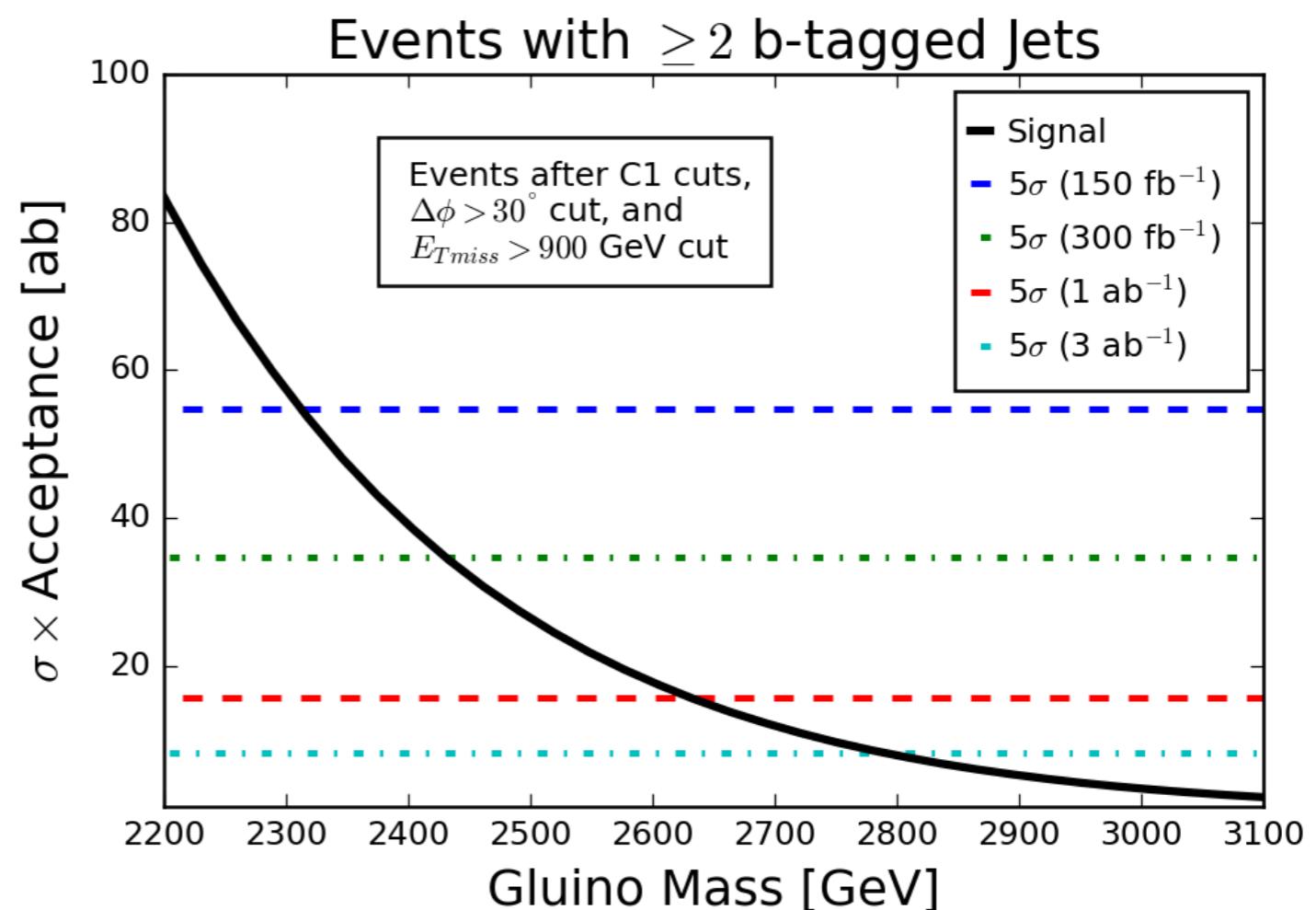


# gluino pair cascade decay signatures

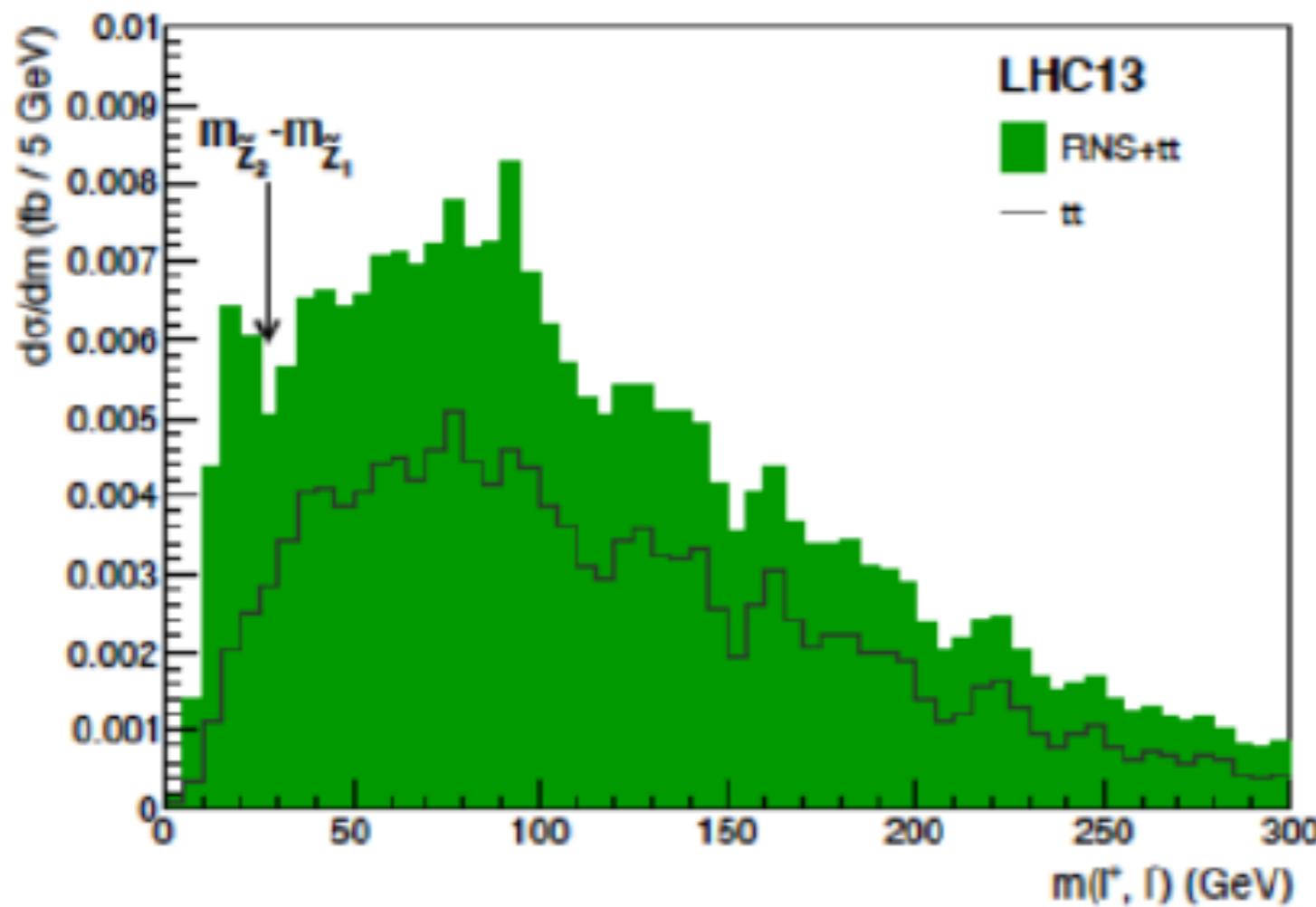


HL-LHC reach to  
 $m(\text{glno}) \sim 2.8 \text{ TeV};$   
RNS:  $m(\text{glno}) < \sim 5 \text{ TeV}$

Estimated HL-LHC reach for gluinos

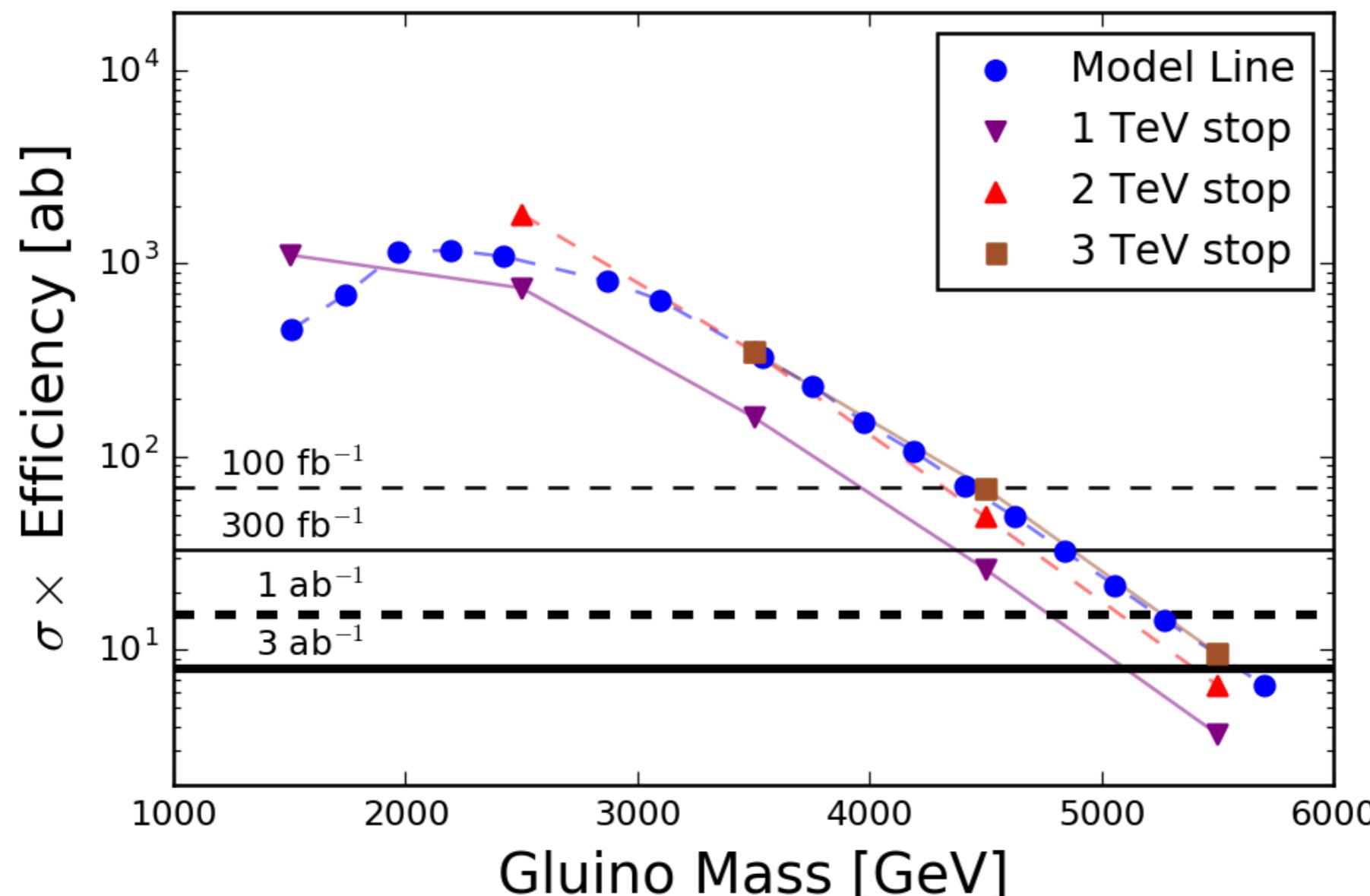


LHC14 has some reach for  
gluino pair production in RNS;  
if a signal is seen,  
should be distinctive



OS/SF dilepton mass  
edge apparent from  
cascade decays  
with  $Z_2 \rightarrow Z_1 + l + l\bar{b}$

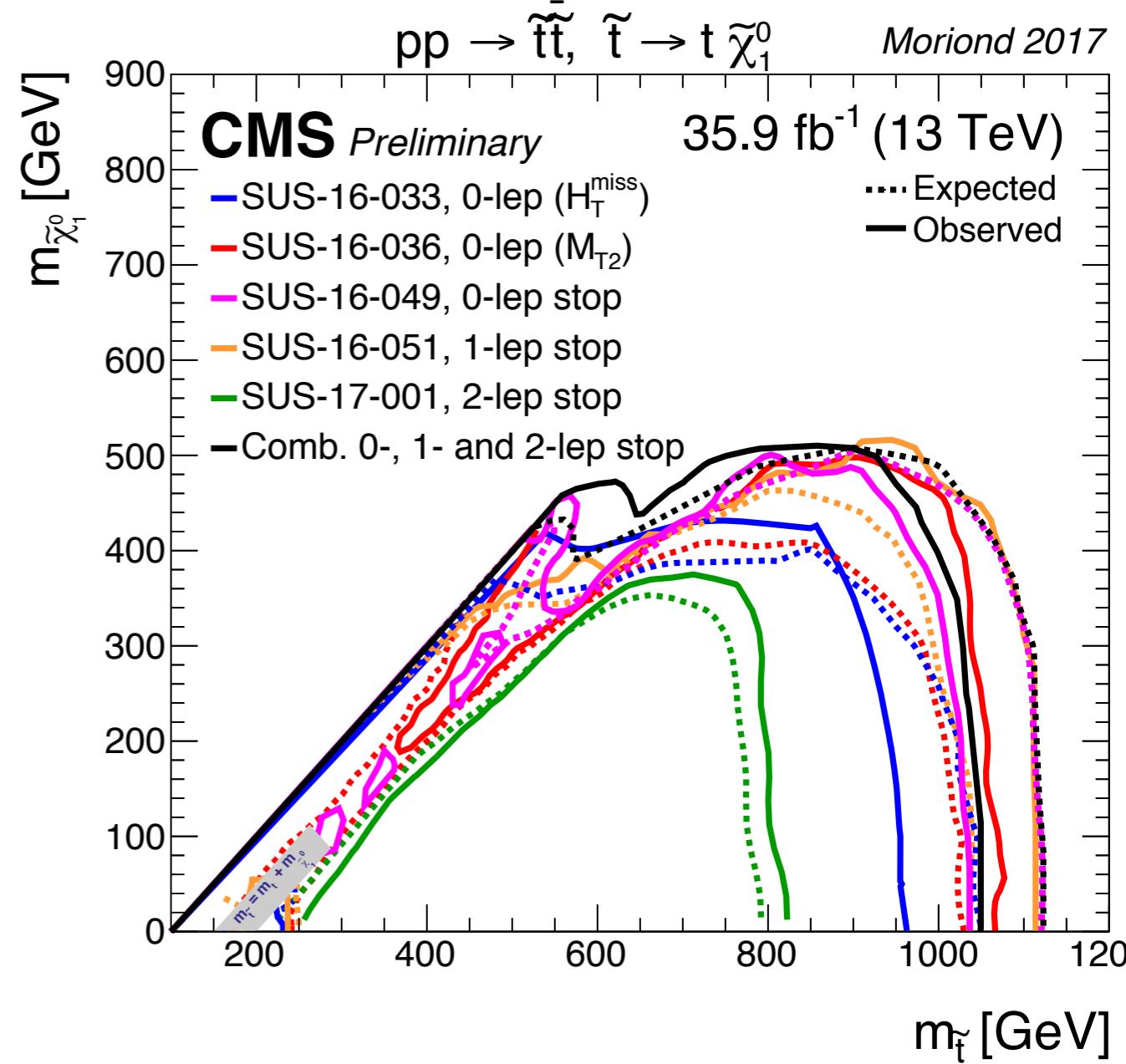
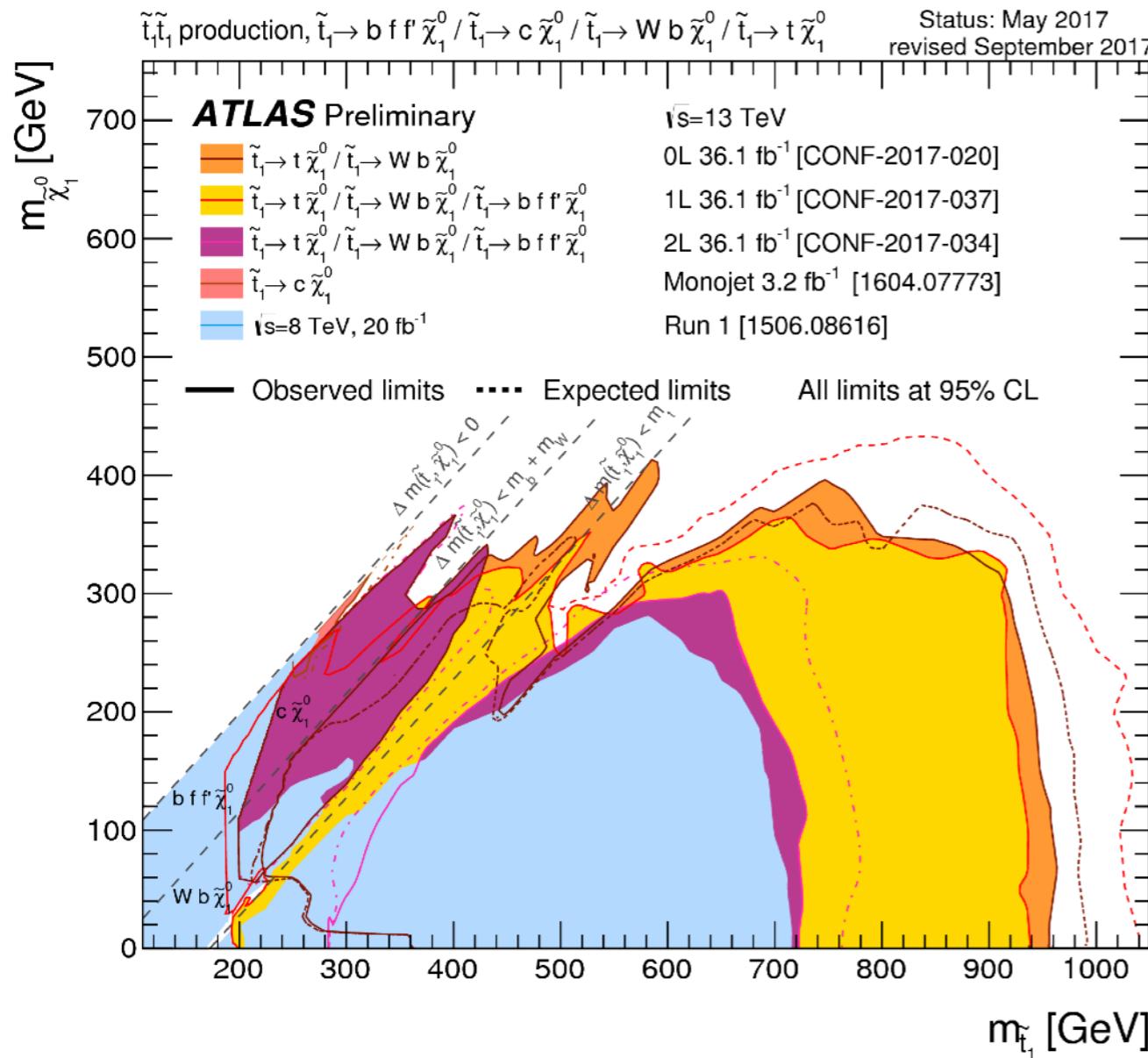
# Gluino 5-sigma reach at LHC33: to about $m(\text{glno}) \sim 5\text{-}5.5 \text{ TeV}$



$\geq 4$  jets;  $\geq 2$ - $b$ -jets; MET > 1500 GeV

HB,Barger, Gainer,Huang, Savoy, Serce, Tata

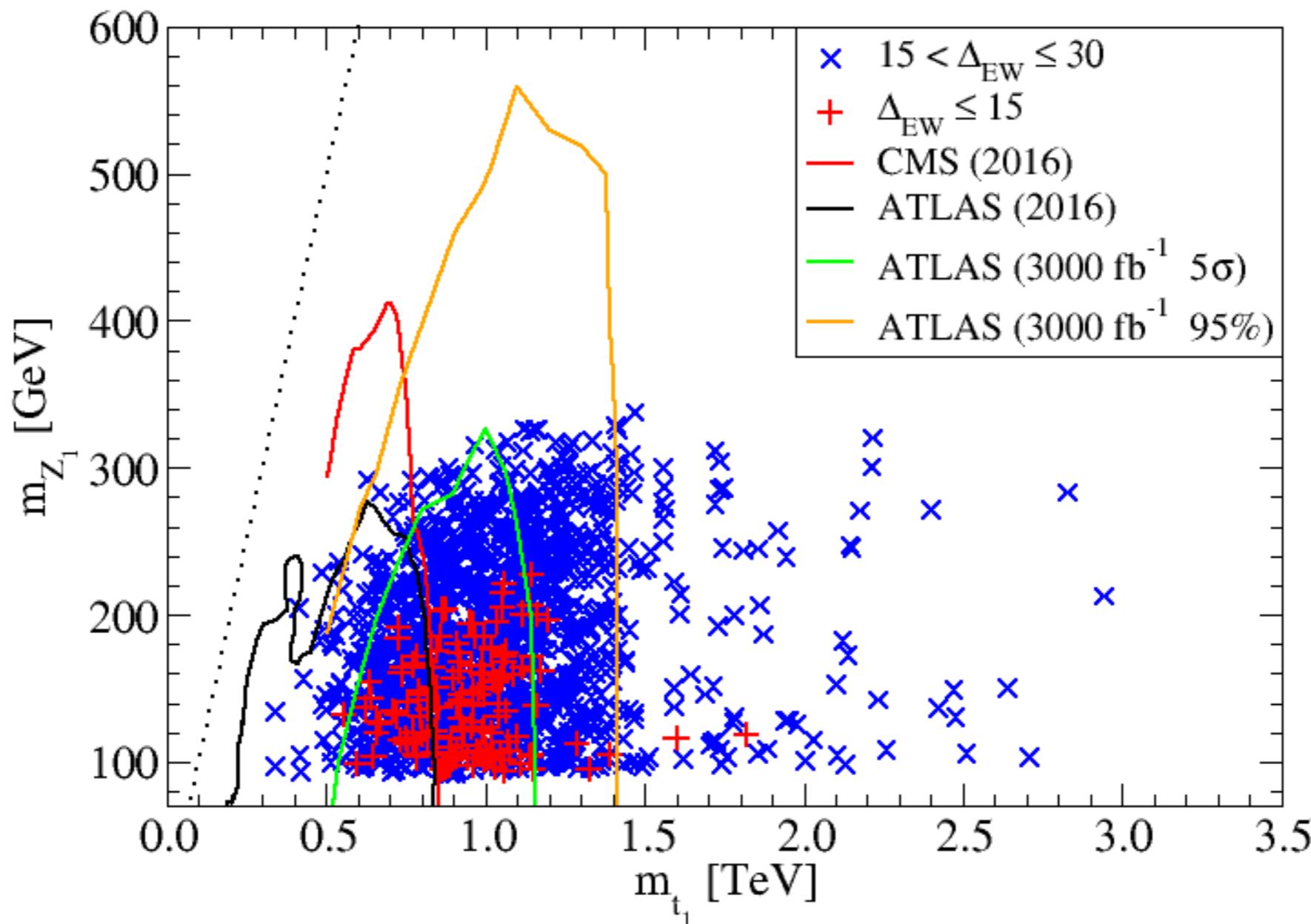
# Present limits on top squarks from LHC



Evidently  $m(t_1) > \sim 1 \text{ TeV}$  for  $m(\text{LSP}) \sim 150 \text{ GeV}$

- \* TeV-scale top squark needed for  $m(h) \sim 125 \text{ GeV}$
- \* Also needed for  $b \rightarrow s \gamma$

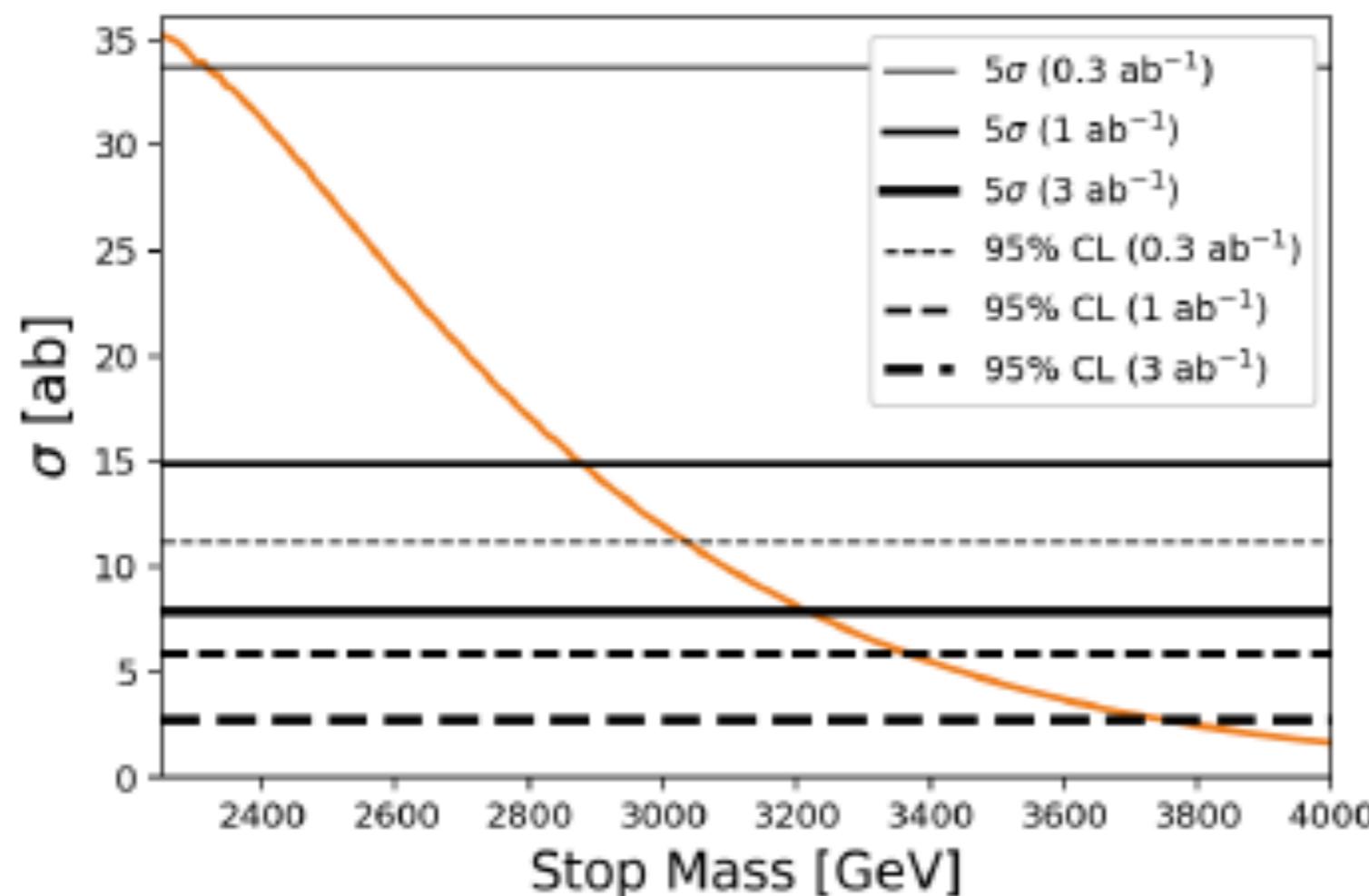
# Prospects for top squarks in natural SUSY



$m(t_1)$  can range up to 3 TeV with little cost to naturalness;  
the hunt for stops has only begun!

HL-LHC reach extends to  $m(t_1) \sim 1.2\text{--}1.4$  TeV

# Reach of LHC33 for top squarks



- $\tilde{t}_1 \rightarrow b\tilde{W}_1; \sim 50\%$
- $\tilde{t}_1 \rightarrow t\tilde{Z}_1; \sim 25\%$
- $\tilde{t}_1 \rightarrow t\tilde{Z}_2; \sim 25\%$
- A.  $\tilde{t}_1\tilde{t}_1^* \rightarrow b\bar{b} + E_T^{\text{miss}} \sim 25\%$  ,
- B.  $\tilde{t}_1\tilde{t}_1^* \rightarrow b\bar{t}, b\bar{t} + E_T^{\text{miss}} \sim 50\%$  ,
- C.  $\tilde{t}_1\tilde{t}_1^* \rightarrow t\bar{t} + E_T^{\text{miss}} \sim 25\%$  .

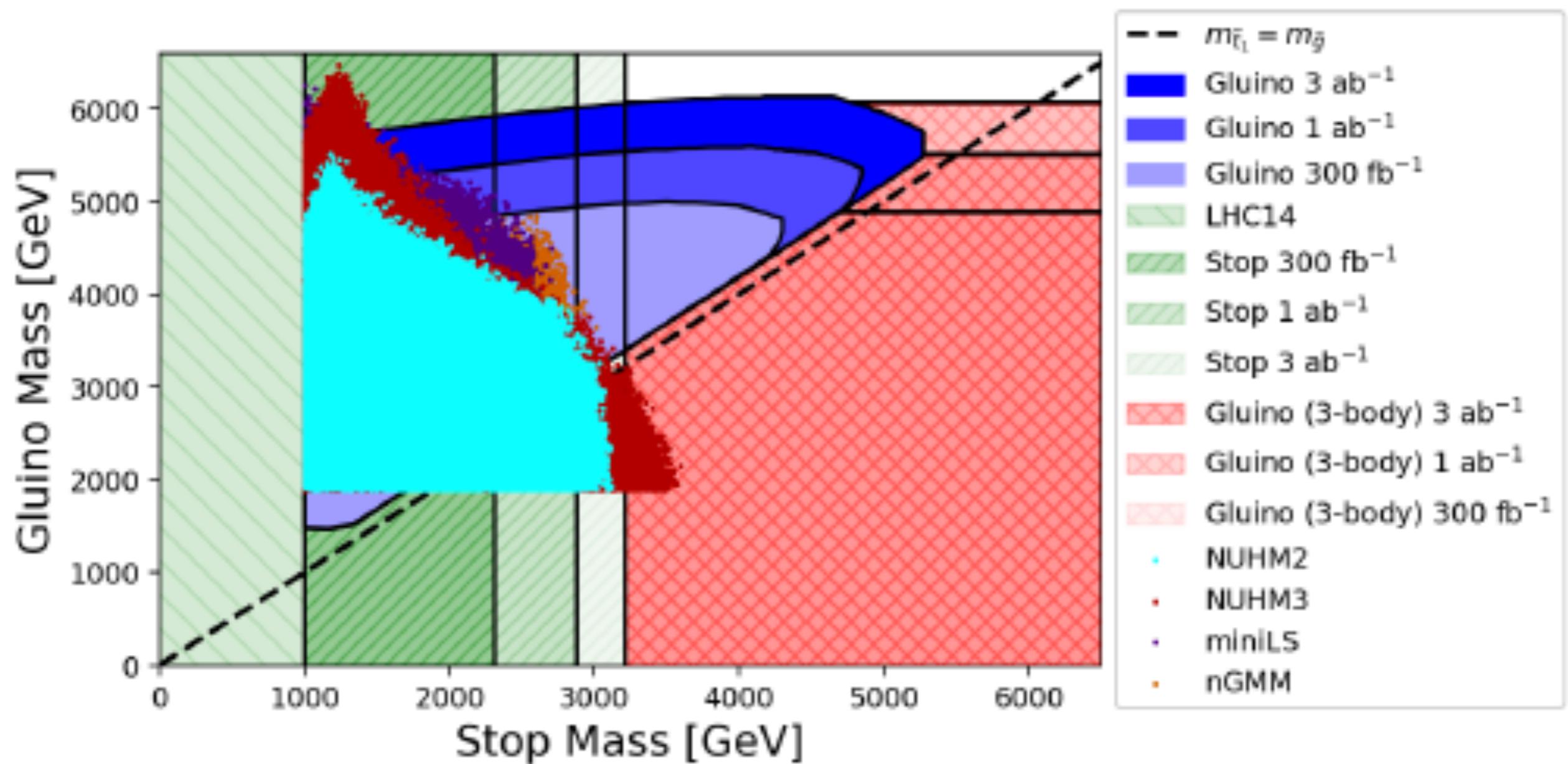
LHC33 reach extends to  $m(t_1) \sim 3-3.8 \text{ TeV}$

$n(\text{b-jets}) >= 2$ ;  $\text{MET} > 750 \text{ GeV}$

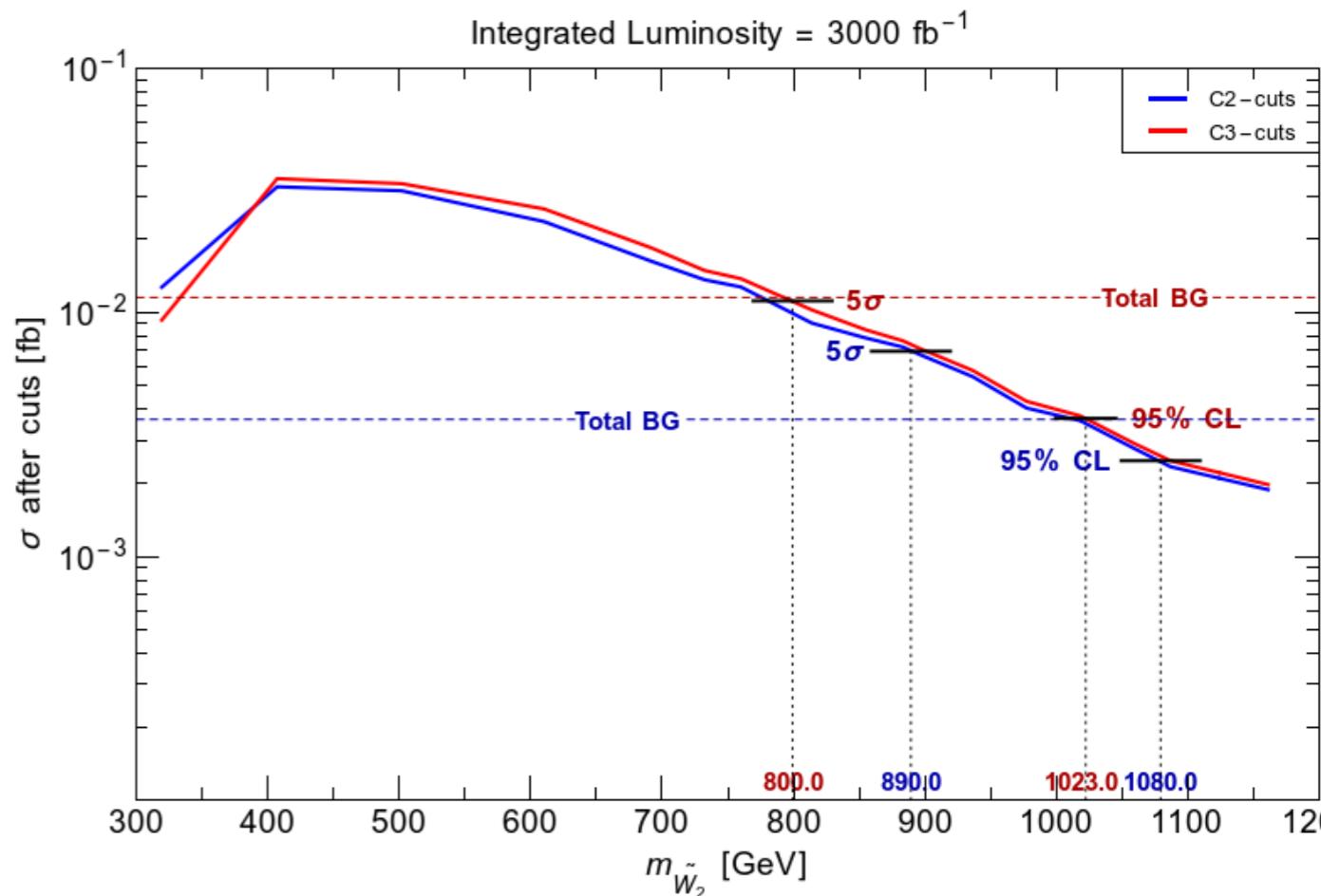
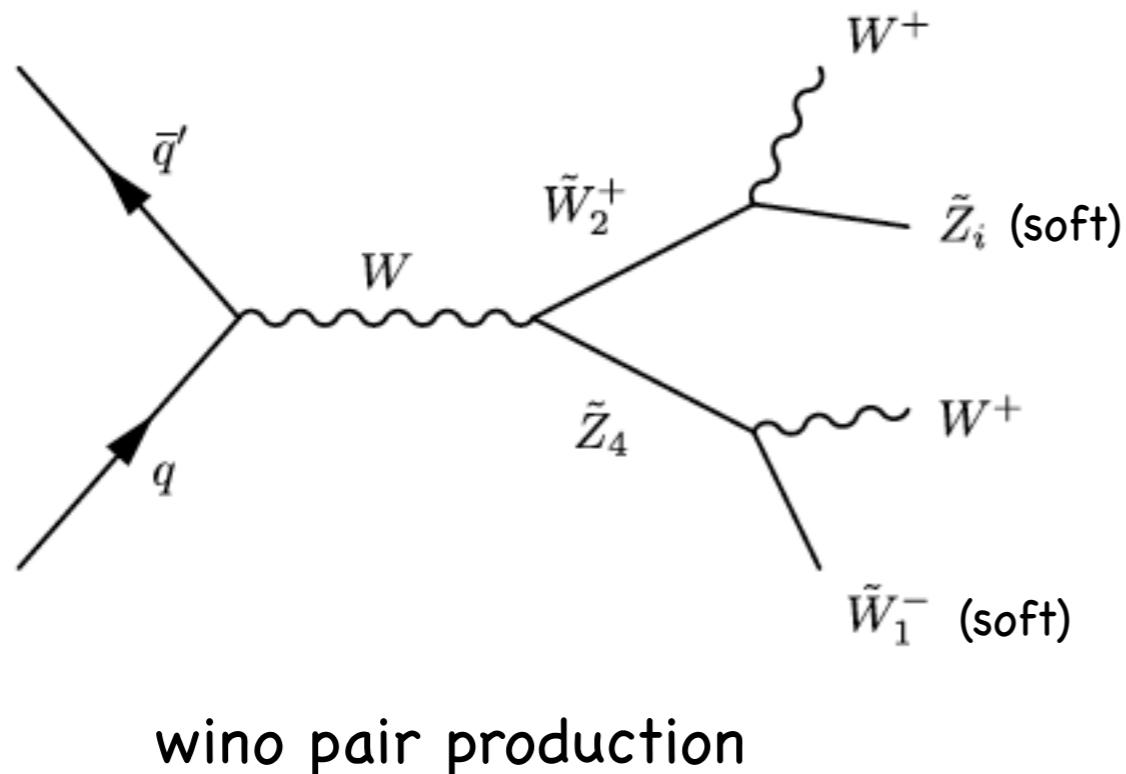
HB, Barger, Gainer, Serce, Tata

Combined LHC33 reach for  $t_1$  and  $g_{lno}$   
covers all natural SUSY p-space!

(need to re-do for LHC27)



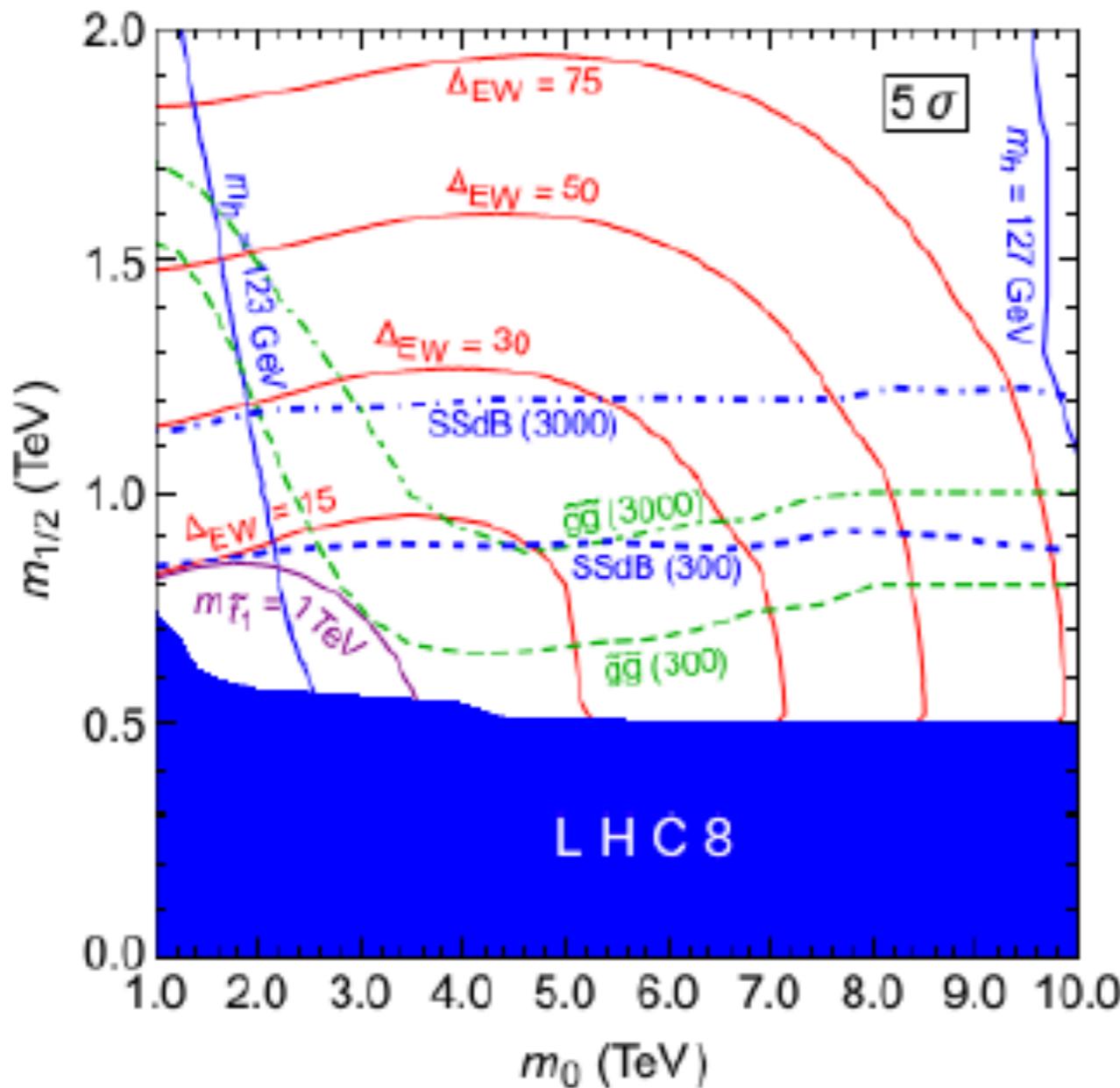
# Distinctive same-sign diboson (SSdB) signature from SUSY models with light higgsinos!



This channel offers good reach of LHC14 for RNS;  
it is also indicative of wino-pair prod'n  
followed by decay to higgsinos

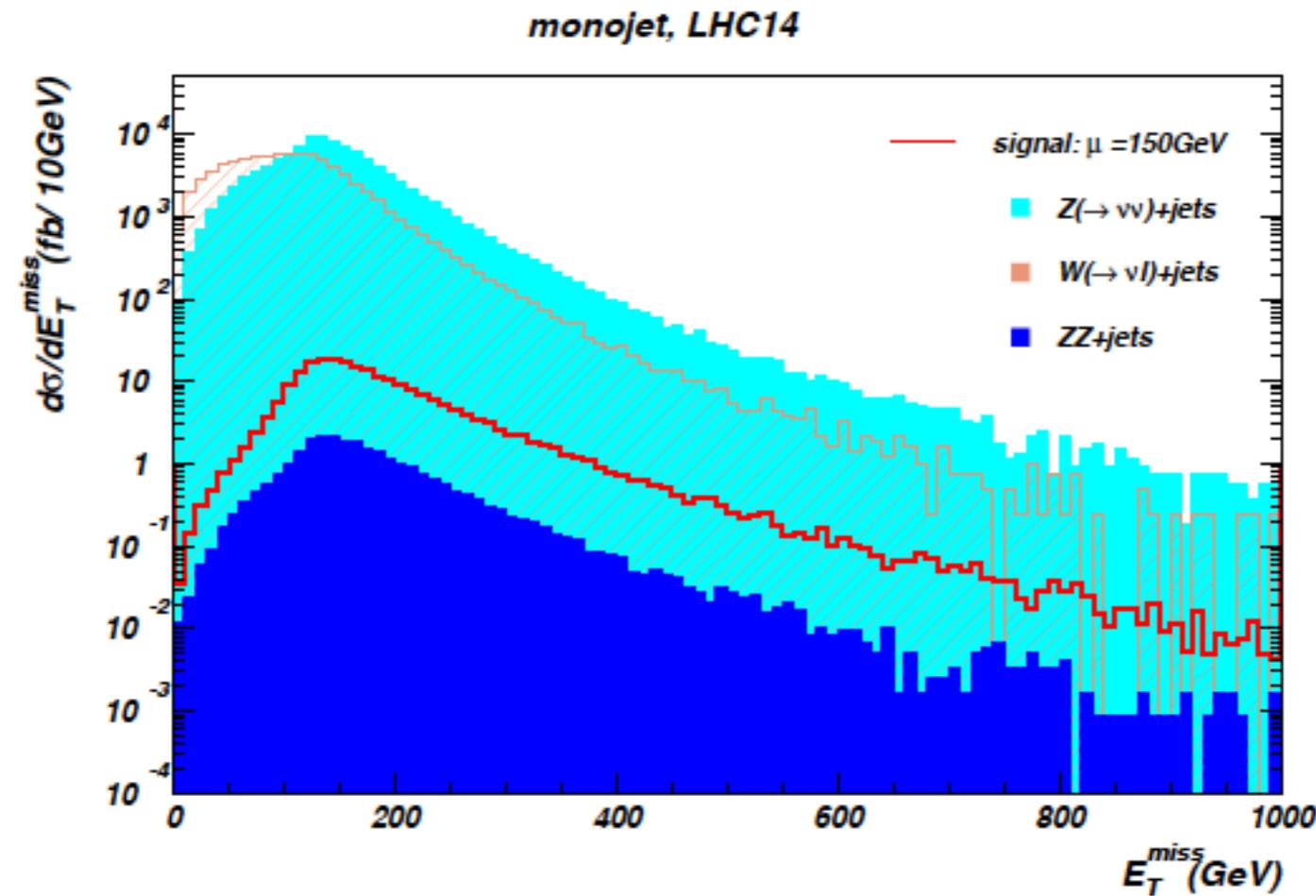
H. Baer, V. Barger, P. Huang, D. Mickelson, A. Mustafayev, W. Sreethawong and X. Tata,  
*Phys. Rev. Lett.* **110** (2013) 151801.

Good old  $m_0$  vs.  $m_{hf}$  plane still viable, but  
needs  $\mu \sim 100-200$  GeV as possible in NUHM2  
instead of CMSSM/mSUGRA



For models with ino mass unif'n,  
reach via SSdB may exceed glno pairs  
for high luminosity

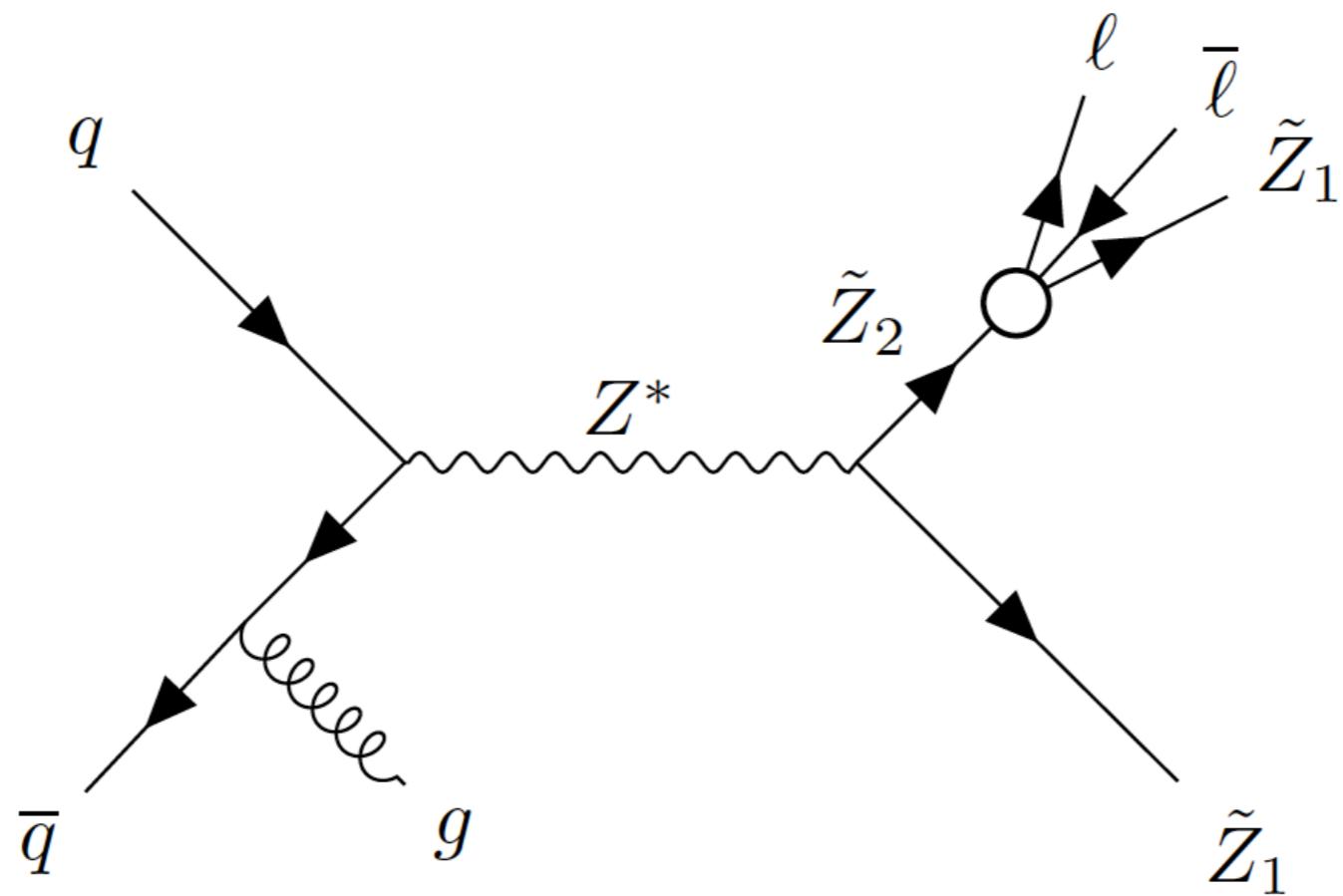
See direct higgsino pair production  
recoiling from ISR (monojet signal)?



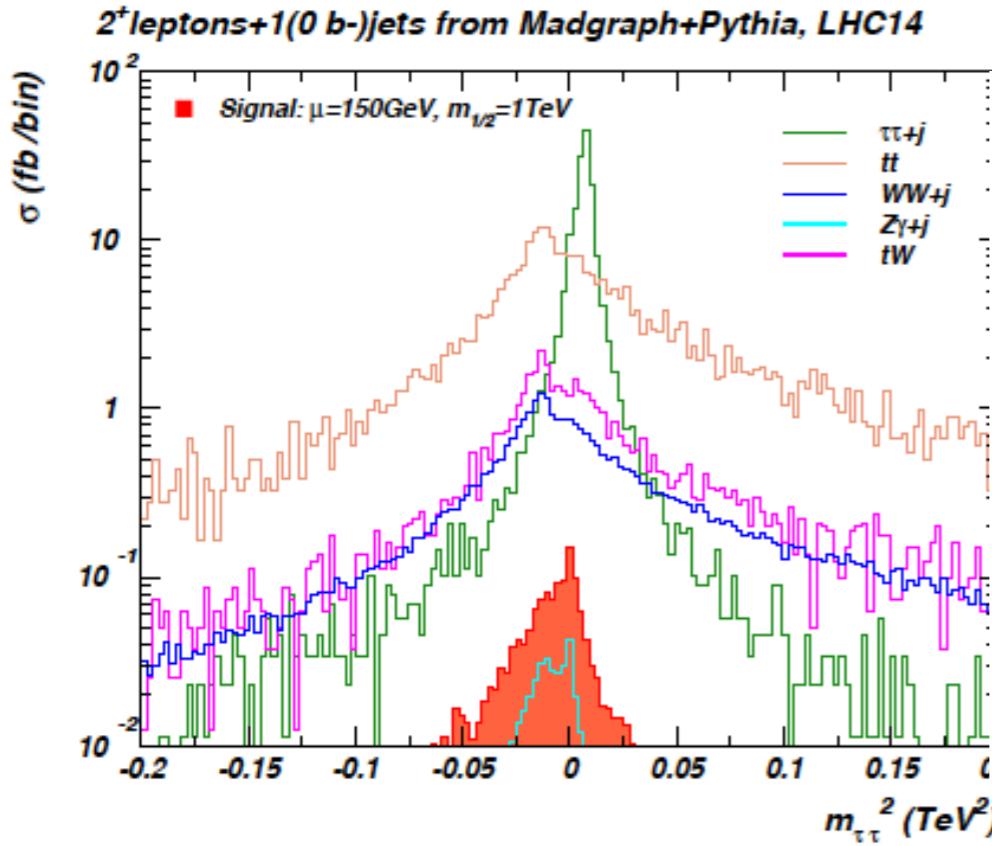
typically 1% S/BG after cuts:  
very tough to do!

What about  $pp \rightarrow \tilde{Z}_1 \tilde{Z}_2 j$  with  $\tilde{Z}_2 \rightarrow \tilde{Z}_1 \ell^+ \ell^-$  ?

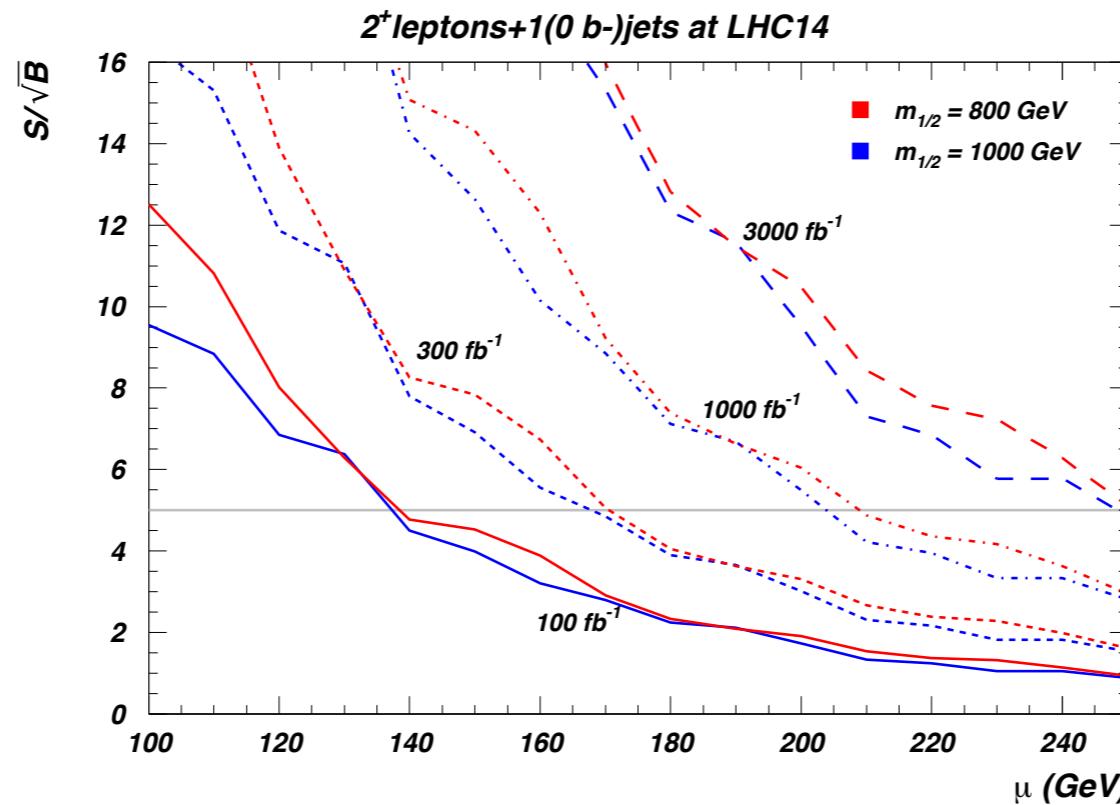
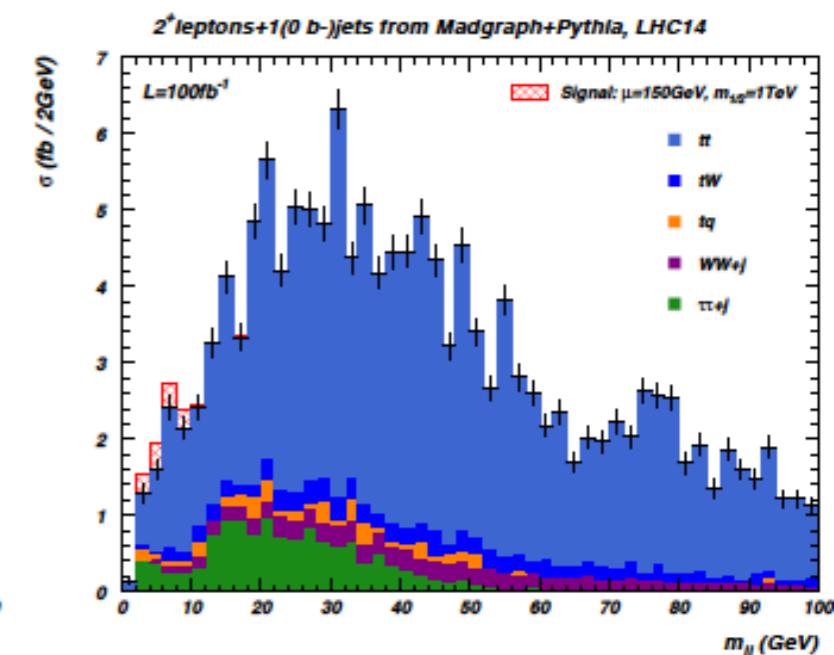
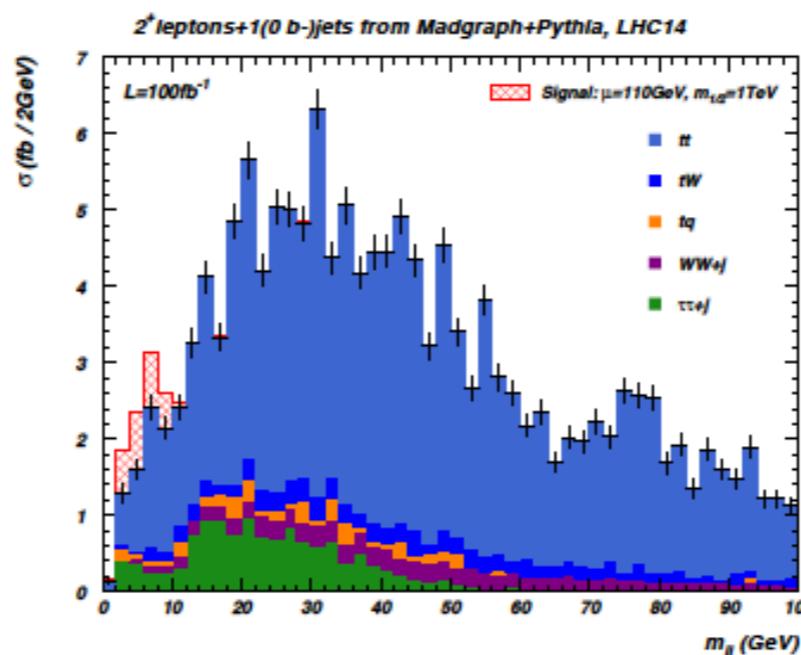
Han, Kribs, Martin, Menon, PRD89 (2014) 075007;  
HB, Mustafayev, Tata, PRD90 (2014) 115007;



# use MET to construct $m^2(\tau\tau)$



cut  $m(\text{ditaus})^2 < 0$



HL-LHC 5-sigma reach  
to  $\mu \sim 250\text{ GeV}!$

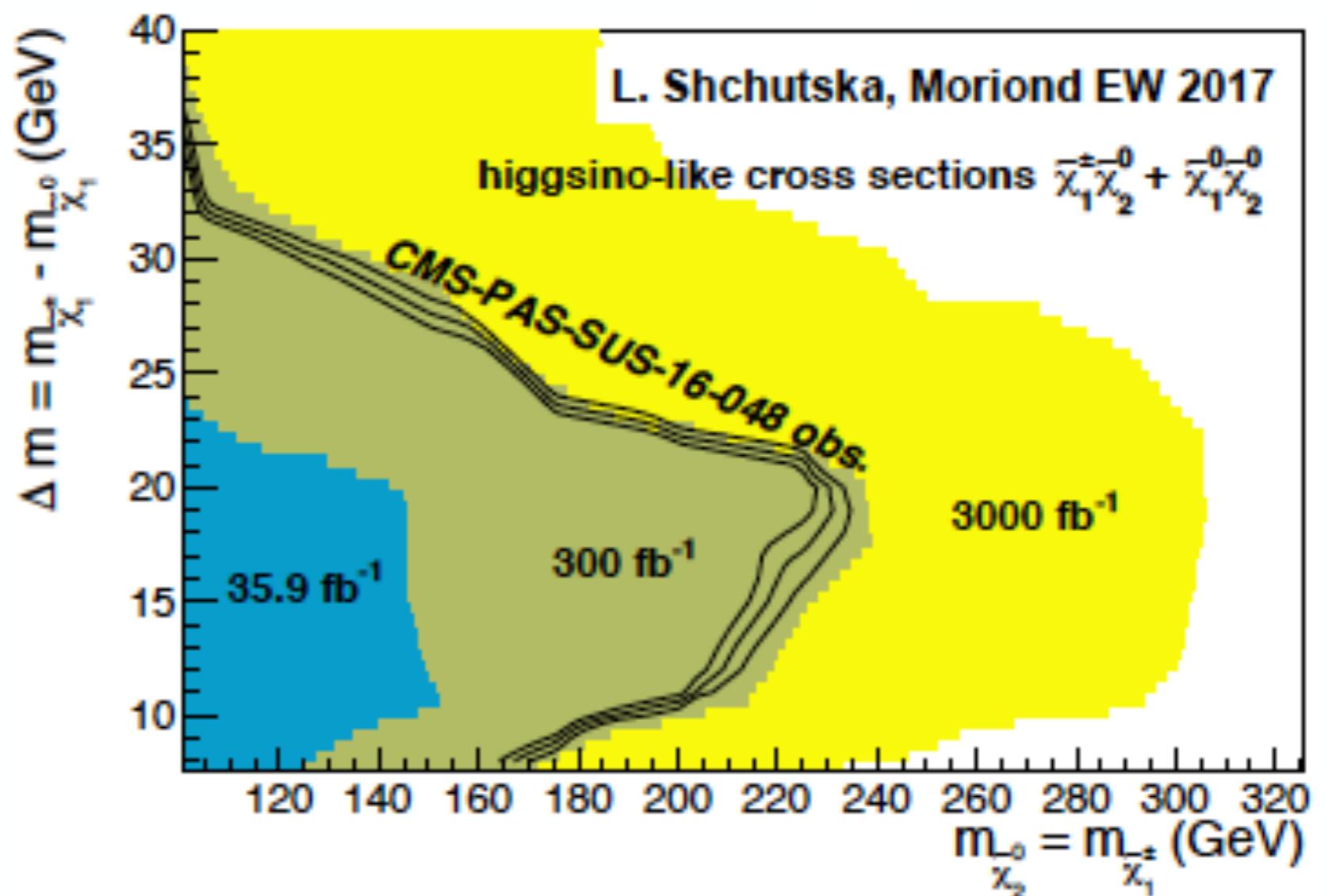
HB, Mustafayev, Tata

CMS analysis: this may be the most important SUSY discovery channel at LHC since it directly probes higgsinos which can't be too far from  $m(W, Z, h)$

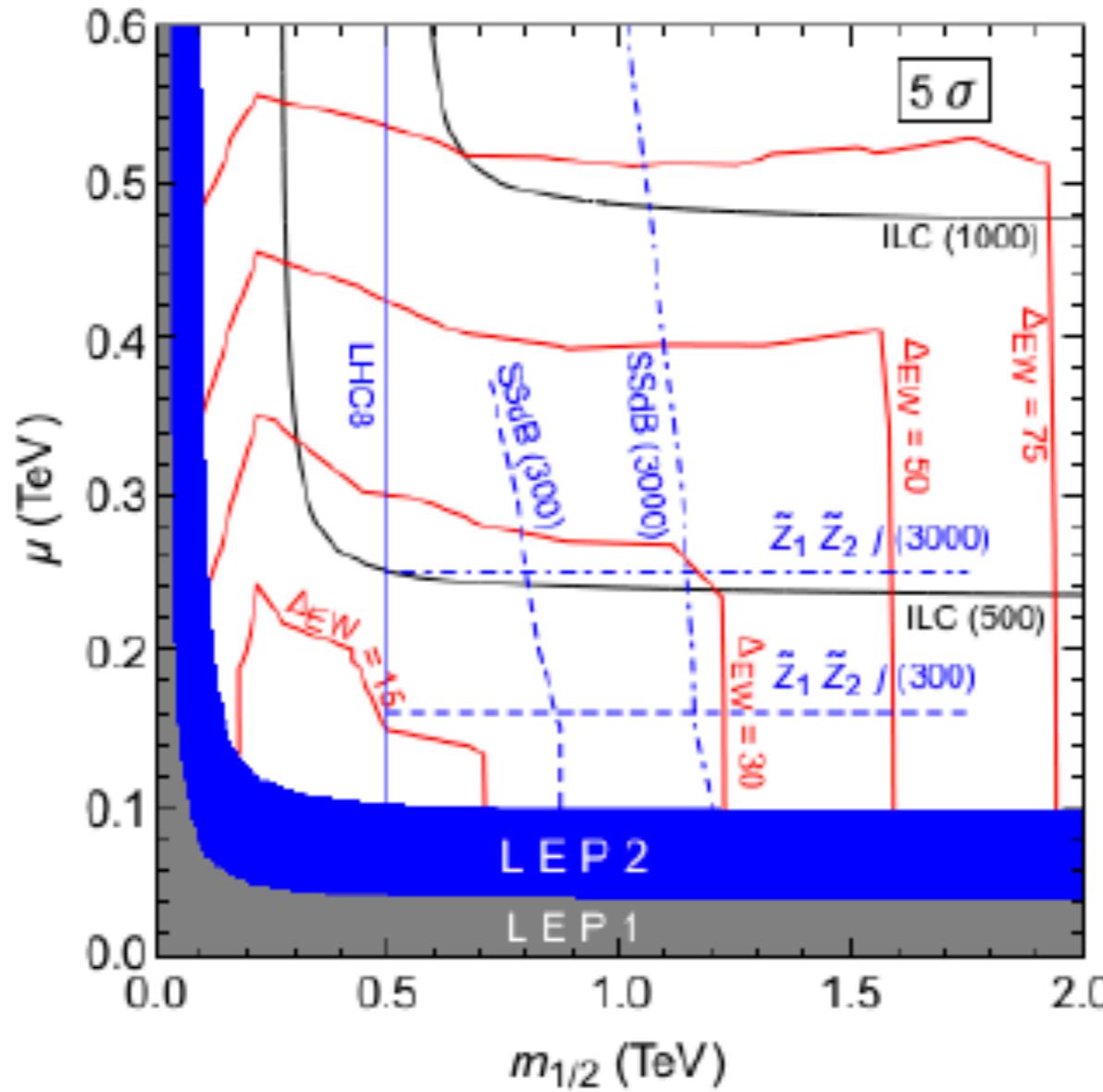
Atlas study underway- results soon?

### Higgsino cross section (projection only)

NatSUSY  $z_2-z_1$  mass gap may range down to 3 GeV so need to ID very soft, low  $m(l\bar{l})$  leptons



# panoramic view of reach of HL-LHC for natural SUSY



Combined SSdB/IIjMET searches may cover all Nat SUSY p-space at HL-LHC for models with ino mass unification; in mirage scenario,  $z_2-z_1$  mass gap can be reduced and  $M_2$  can be much higher than in NUHM2

# Summary of collider searches

- In light of recent LHC bounds ( $m(g_{\text{ino}}) > 2 \text{ TeV}$ ,  $m(t_1) > 1 \text{ TeV}$ ) and  $m(h)$  requiring TeV-scale highly mixed top squarks, concern has arisen about an emerging Little Hierarchy problem characterized by  $m(\text{weak}) \sim 100 \text{ GeV} \ll m(\text{SUSY}) \sim \text{multi-TeV}$  rendering perhaps SUSY as “unnatural”
- We propose an improved naturalness measure based upon scalar potential minimization condition

$$m_Z^2/2 = \frac{m_{H_d}^2 + \Sigma_d^d - (m_{H_u}^2 + \Sigma_u^u) \tan^2 \beta}{\tan^2 \beta - 1} - \mu^2 \simeq -m_{H_u}^2 - \Sigma_u^u(\tilde{t}_{1,2}) - \mu^2$$

This leads to upper bounds from naturalness:

- $m(\text{higgsinos}) \sim 100\text{-}300 \text{ GeV}$  (the lighter the better)
- $m(t_1) < \sim 3 \text{ TeV}$
- $m(g_{\text{ino}}) < \sim 6 \text{ TeV}$

DM=WIMP/axion mix?

Conclusions:

1. SUSY still natural;
2. hunt for nSUSY has only begun;
3. HL-LHC handle most SUSY with ino-mass unification;
4. other (e.g. mirage) may require HE-LHC to complete search

process	current	HL-LHC	HE-LHC
g <sub>ino</sub> -g <sub>ino</sub>	$m(g_{\text{ino}}) > 2 \text{ TeV}$	$\sim 2.8 \text{ TeV}$	$5.5 \text{ TeV}$
t <sub>1</sub> -t <sub>1</sub>	$m(t_1) > 1 \text{ TeV}$	$1.3 \text{ TeV}$	$3.5 \text{ TeV}$
SSdB (winos)	x	$m(W_2) \sim 1 \text{ TeV}$	?
z1z2j->l+l+b+j+MET	barely	$\mu \sim 250 \text{ GeV}$	?

HB, Barger,Gainer, Huang,Tata  
Savoy, Mustafayev  
Sengupta,Serce

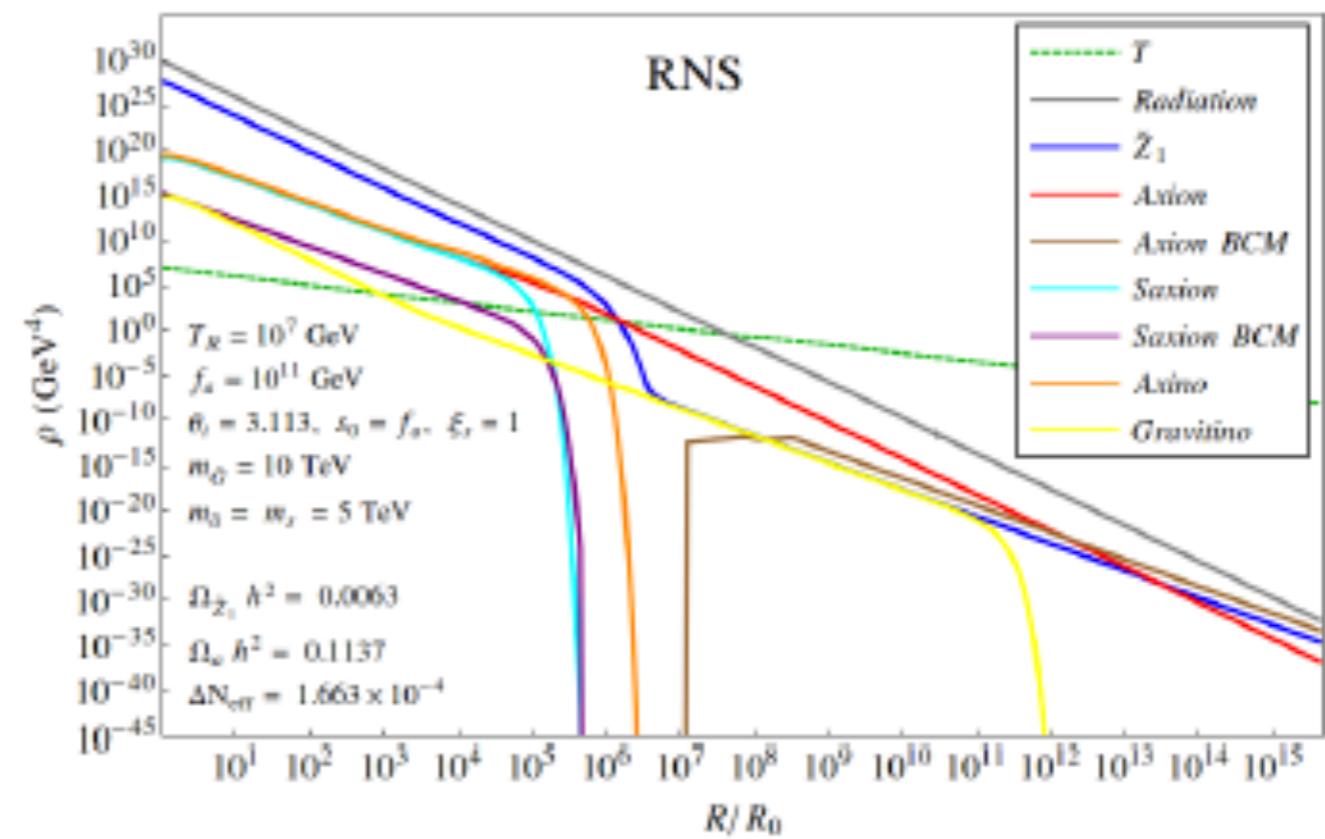
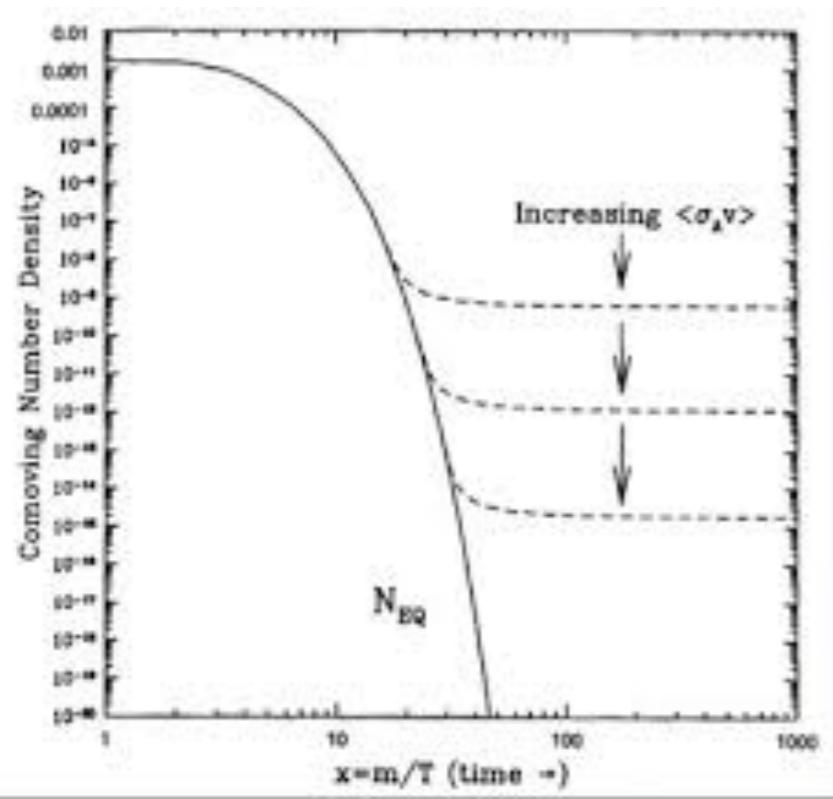
# What happens to SUSY WIMP dark matter?

- higgsino-like WIMPs thermally underproduced
- 3 not four light pions => QCD theta vacuum
- $F.F \sim$  term should be present but neutron(EDM)=> it is tiny
- strong CP problem => axions: no fine-tuning in QCD sector
- SUSY context: axion superfield, axinos and saxions
- DM= axion+higgsino-like WIMP admixture
- DFSZ SUSY axion: solves mu problem with  $\mu \ll m_{3/2}!$
- ultimately detect both WIMP and axion?

usual picture

=>

mixed axion/WIMP



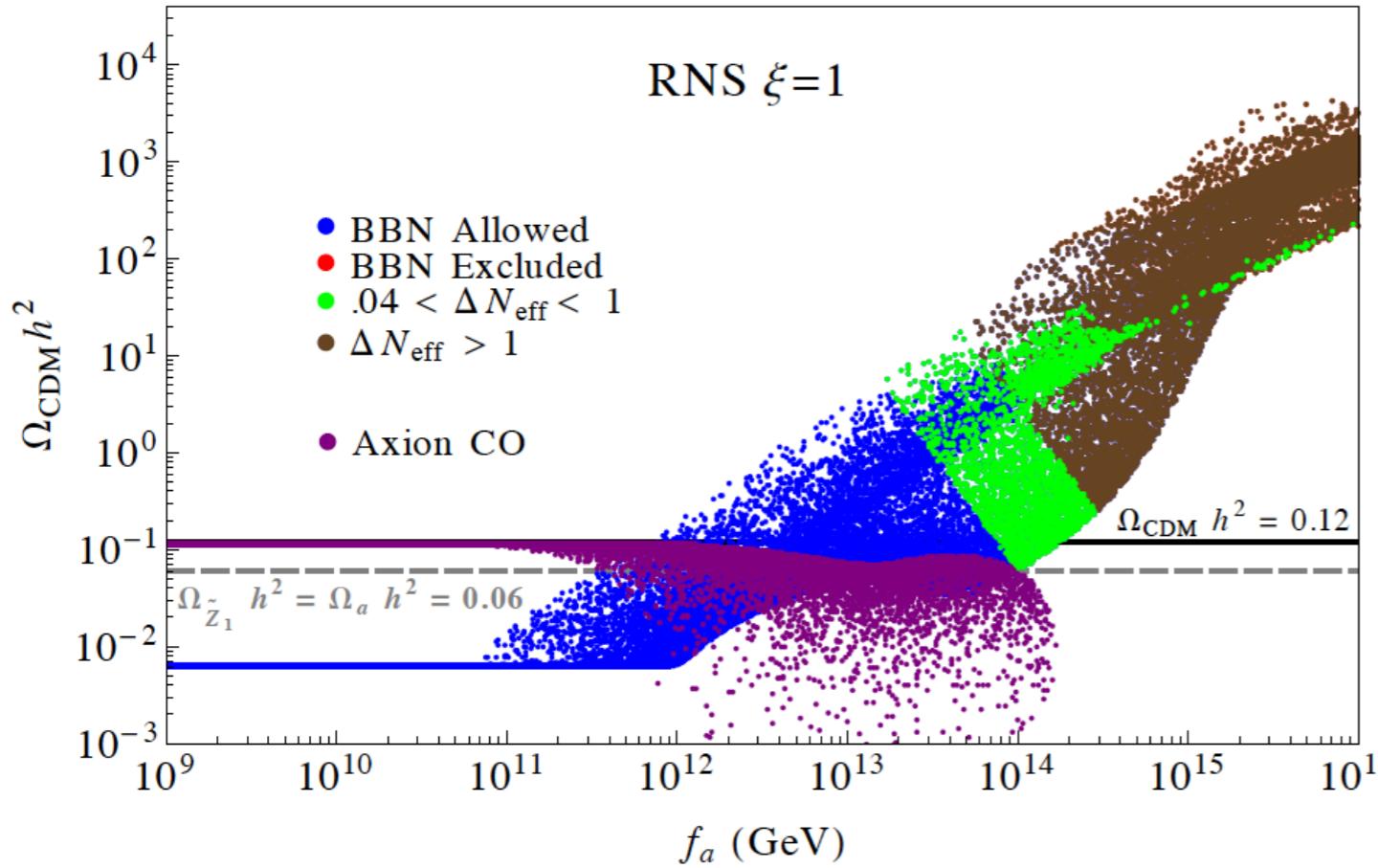
KJ Bae, HB, Lessa, Serce

much of parameter space is axion-dominated  
with 10-15% WIMPs



=>

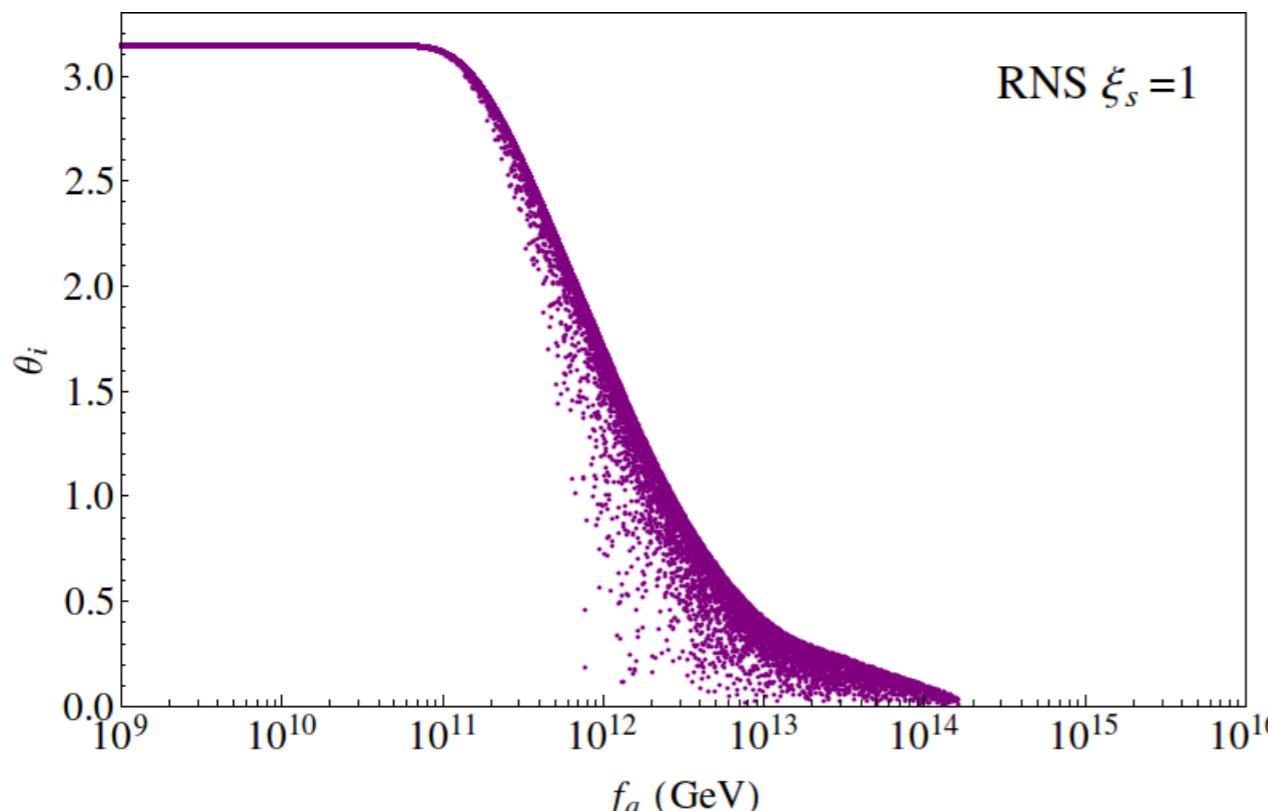




higgsino abundance

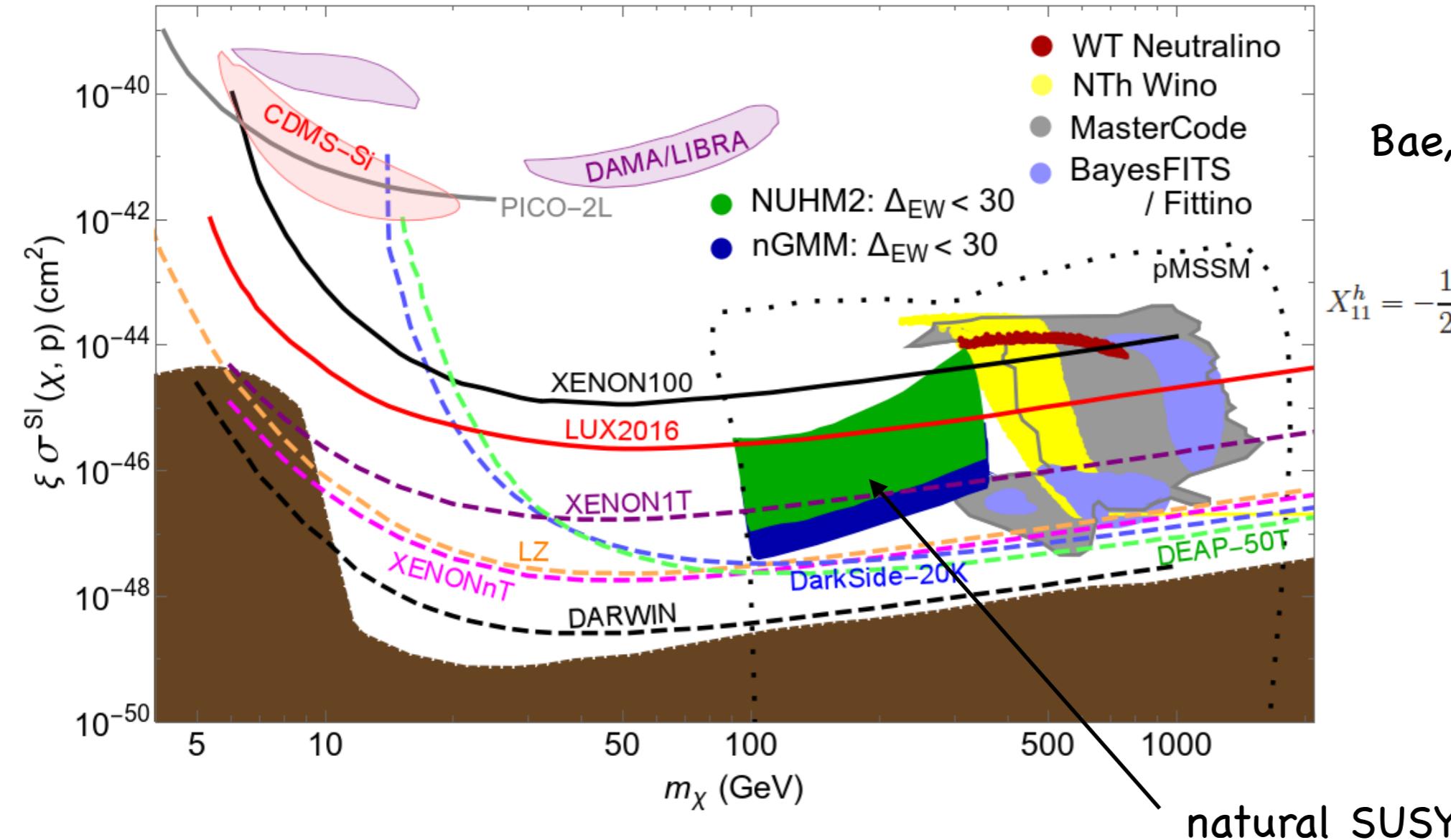
axion abundance

mainly axion CDM  
for  $f_a < \sim 10^{12}$  GeV;  
for higher  $f_a$ , then  
get increasing wimp  
abundance



# Direct higgsino detection rescaled for minimal local abundance

$\xi \equiv \Omega_\chi^{TP} h^2 / 0.12$



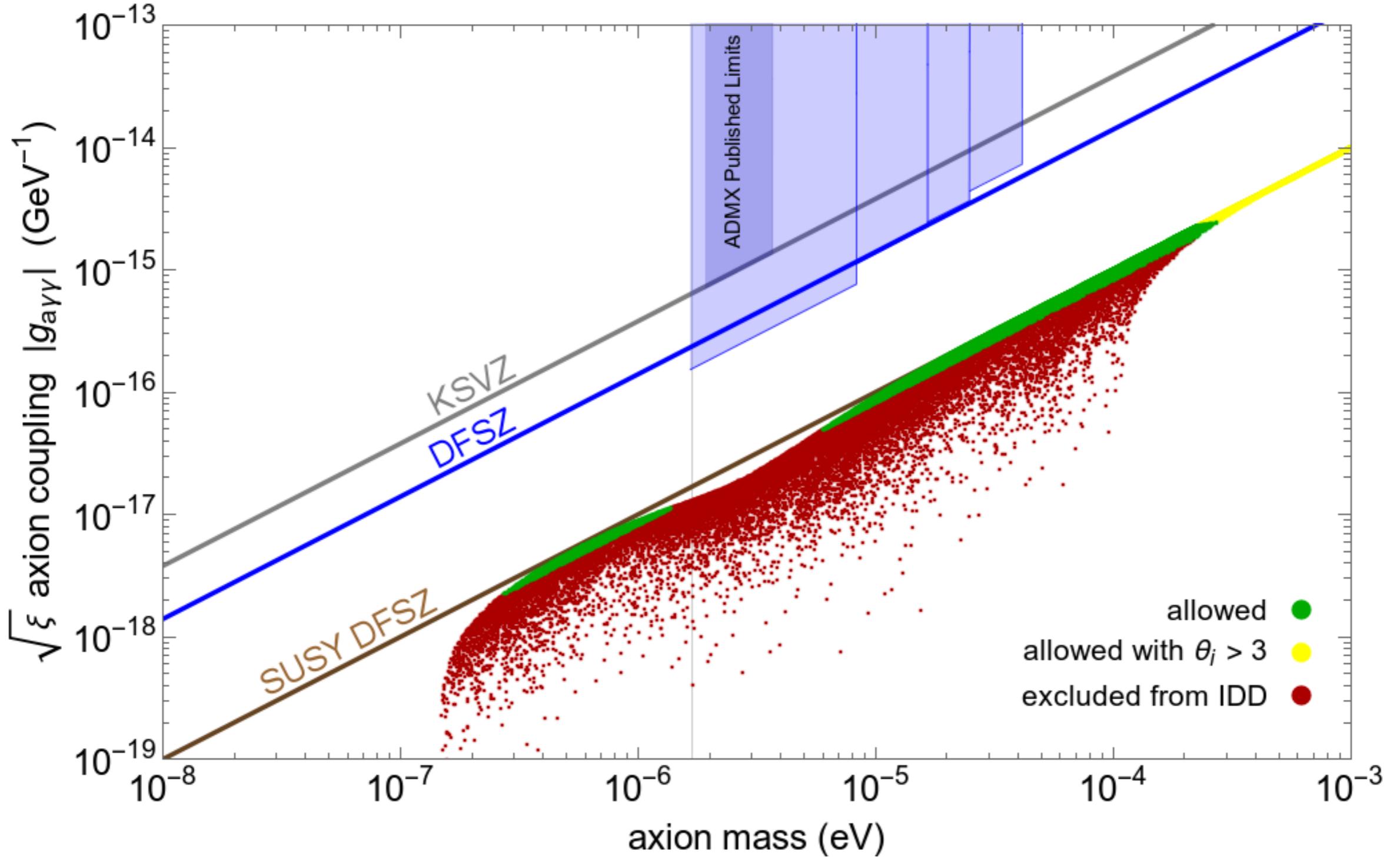
Bae, HB, Barger, Savoy, Serce

$$\mathcal{L} \ni -X_{11}^h \bar{Z}_1 \tilde{Z}_1 h$$

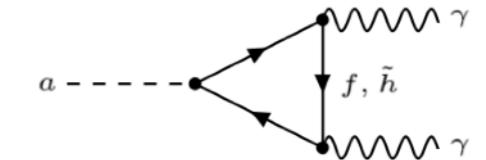
$$X_{11}^h = -\frac{1}{2} (v_2^{(1)} \sin \alpha - v_1^{(1)} \cos \alpha) (g v_3^{(1)} - g' v_4^{(1)})$$

Xe-1-ton  
now operating!

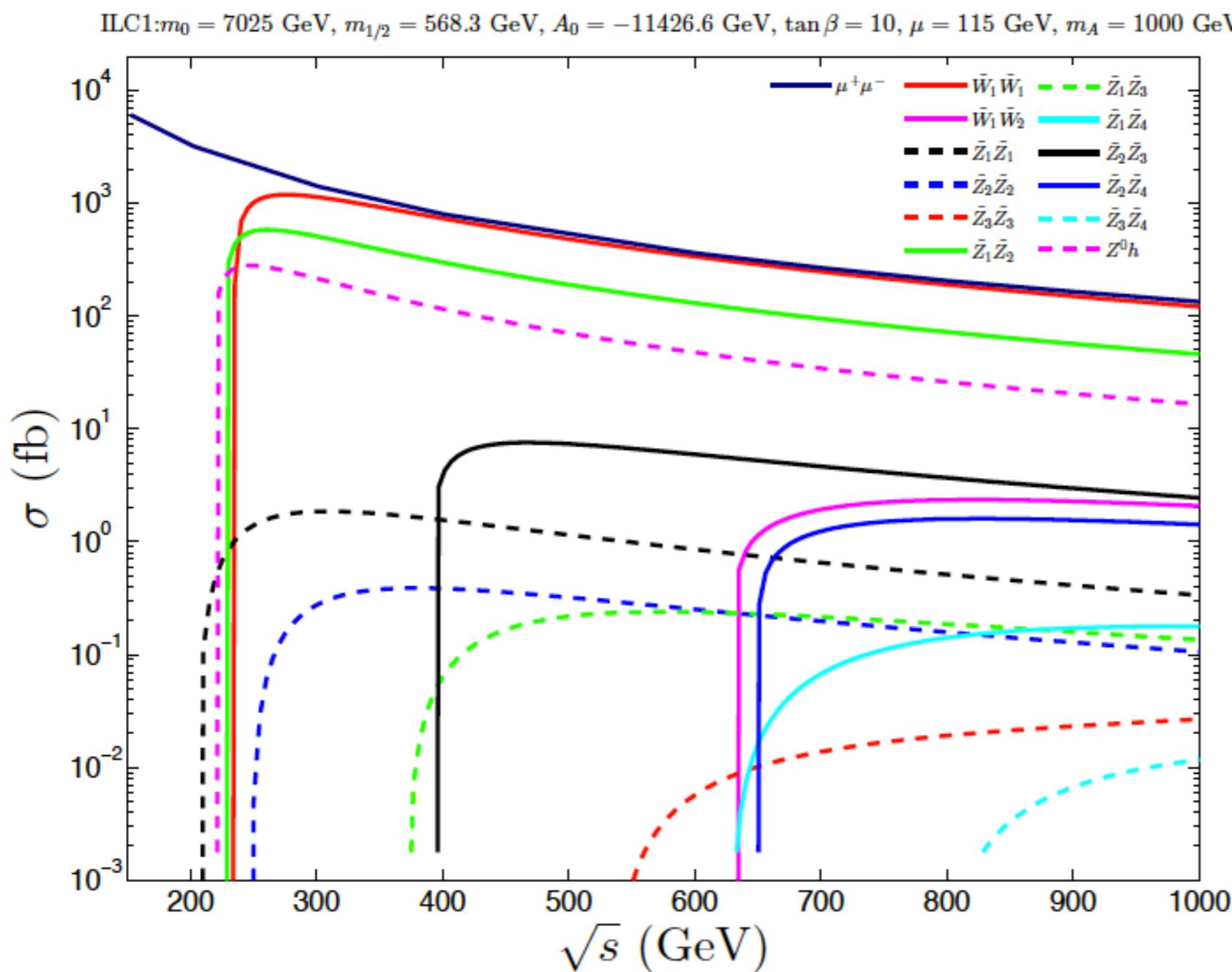
Can test completely with ton scale detector  
or equivalent (subject to minor caveats)



SUSY DFSZ axion: large range in  $m(a)$  but coupling reduced  
 may need to probe broader and deeper!



# Smoking gun signature: light higgsinos at ILC: ILC is Higgs/higgsino factory!



$\sigma(\text{higgsino}) \gg \sigma(Zh)$

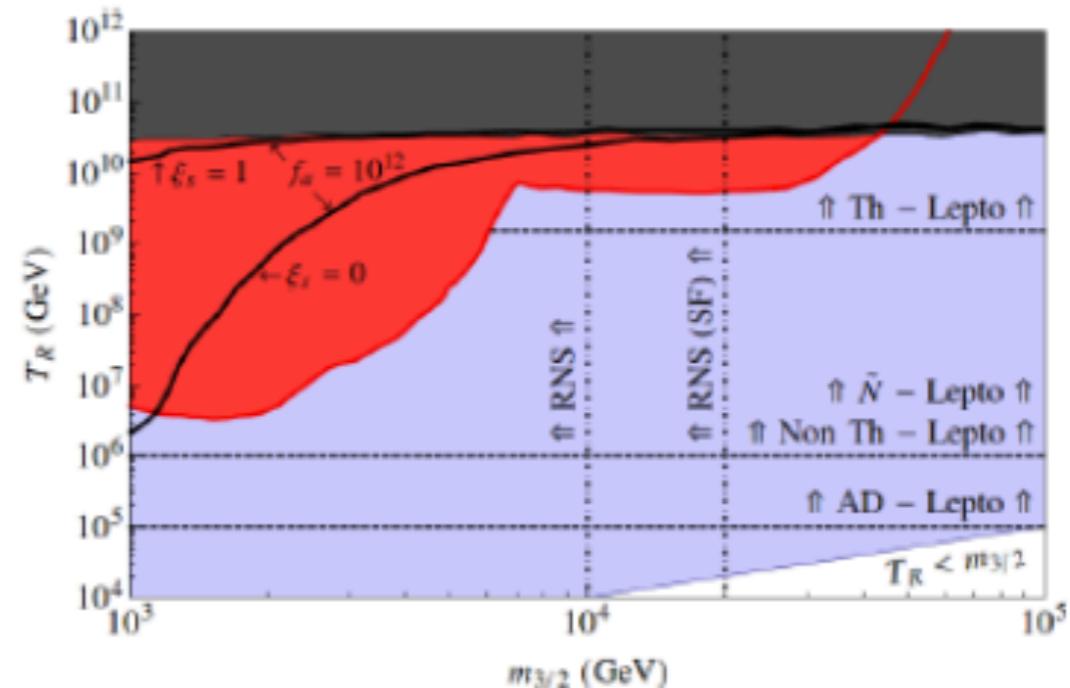
10-15 GeV higgsino mass  
gaps no problem  
in clean ILC environment

HB, Barger, Mickelson, Mustafayev,  
Tata  
arXiv:1404:7510

ILC either sees light higgsinos or MSSM dead

# Baryogenesis scenarios for radiative natural SUSY

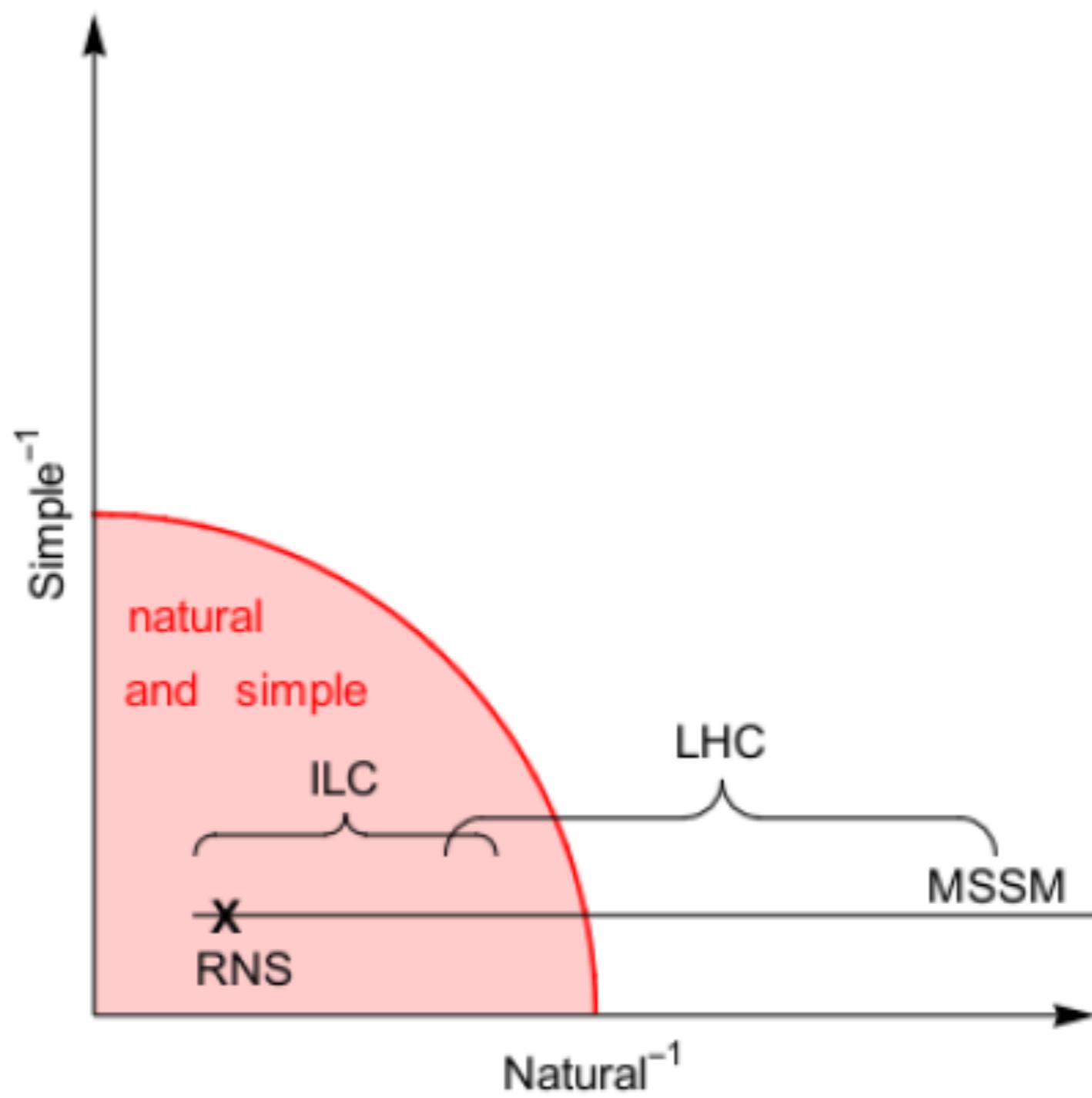
- thermal leptogenesis
- non-thermal (inflaton decay)
- oscillating sneutrino
- Affleck-Dine (AD)



gravitino problem plus  
axino/saxion problem:  
still plenty room

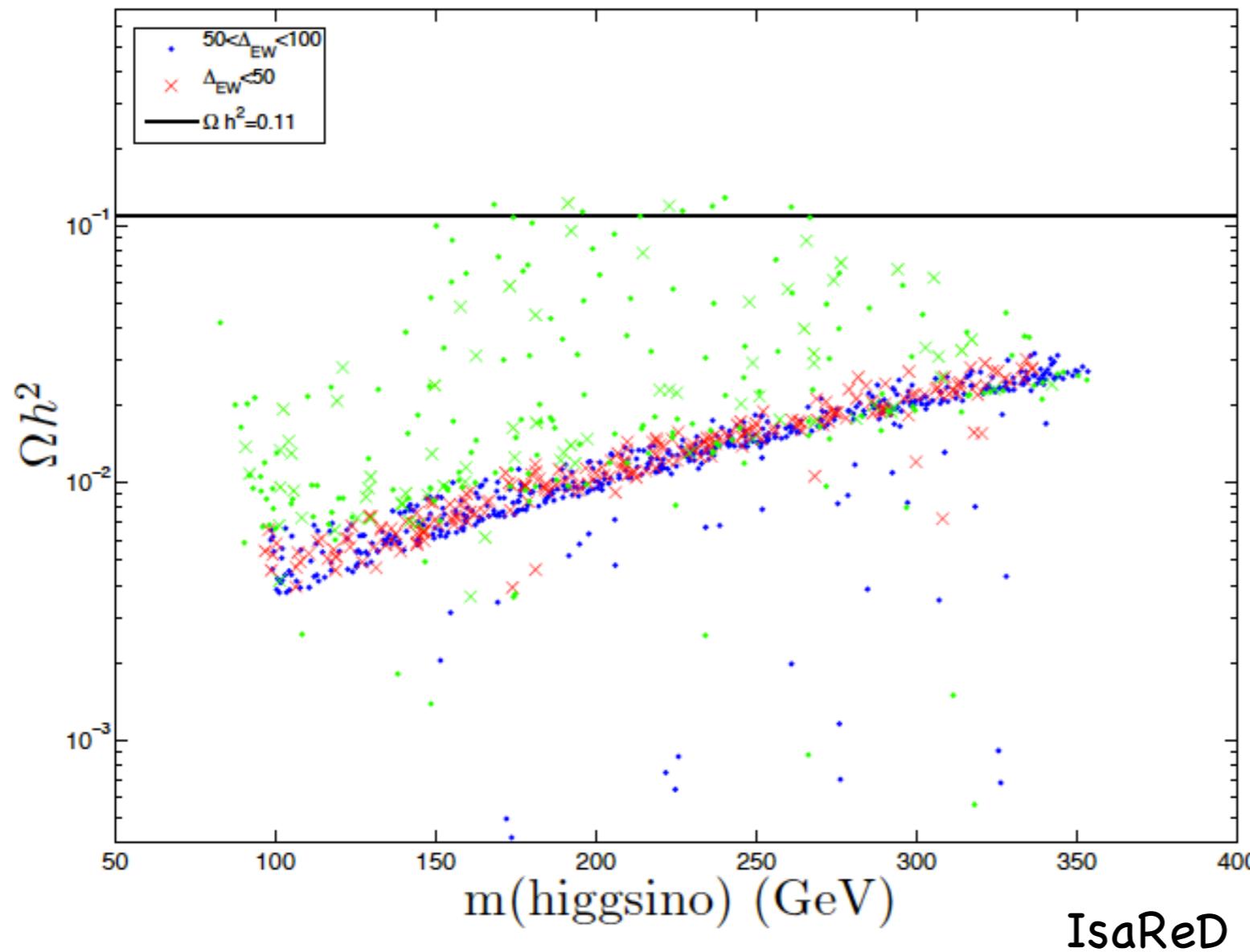
$$f_a = 10^{11}, 10^{12} \text{ GeV}$$

Bae,HB, Serce, Zhang, arXiv:1510.00724



# Dark matter in RNS

# Mainly higgsino-like WIMPs thermally underproduce DM



green: excluded;  
red/blue: allowed

HB, Barger, Mickelson

Factor of 10-15 too low

But so far we have addressed only **Part 1**  
of fine-tuning problem:

In QCD sector, the term  $\frac{\bar{\theta}}{32\pi^2} F_A{}_{\mu\nu} \tilde{F}_A^{\mu\nu}$  must occur

But neutron EDM says it is not there: strong CP problem

(frequently ignored by SUSY types)

Best solution after 35 years:

PQWW/KSVZ/DFSZ **invisible axion**

In SUSY, axion accompanied by axino and saxion

Changes DM calculus:  
expect mixed WIMP/axion DM (**2 particles**)

## Axion cosmology

★ Axion field eq'n of motion:  $\theta = a(x)/f_a$

- $\ddot{\theta} + 3H(T)\dot{\theta} + \frac{1}{f_a^2} \frac{\partial V(\theta)}{\partial \theta} = 0$

- $V(\theta) = m_a^2(T)f_a^2(1 - \cos \theta)$

- Solution for  $T$  large,  $m_a(T) \sim 0$ :

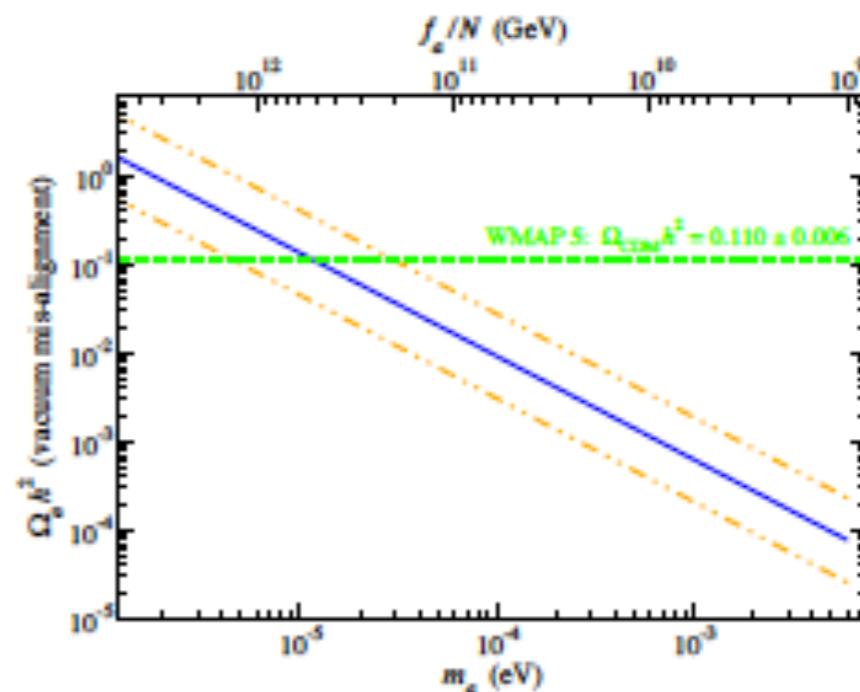
$\theta = \text{const.}$

- $m_a(T)$  turn-on  $\sim 1$  GeV

★  $a(x)$  oscillates,  
creates axions with  $\vec{p} \sim 0$ :  
production via vacuum mis-alignment

★  $\Omega_a h^2 \sim \frac{1}{2} \left[ \frac{6 \times 10^{-6} \text{ eV}}{m_a} \right]^{7/6} \theta_i^2 h^2$

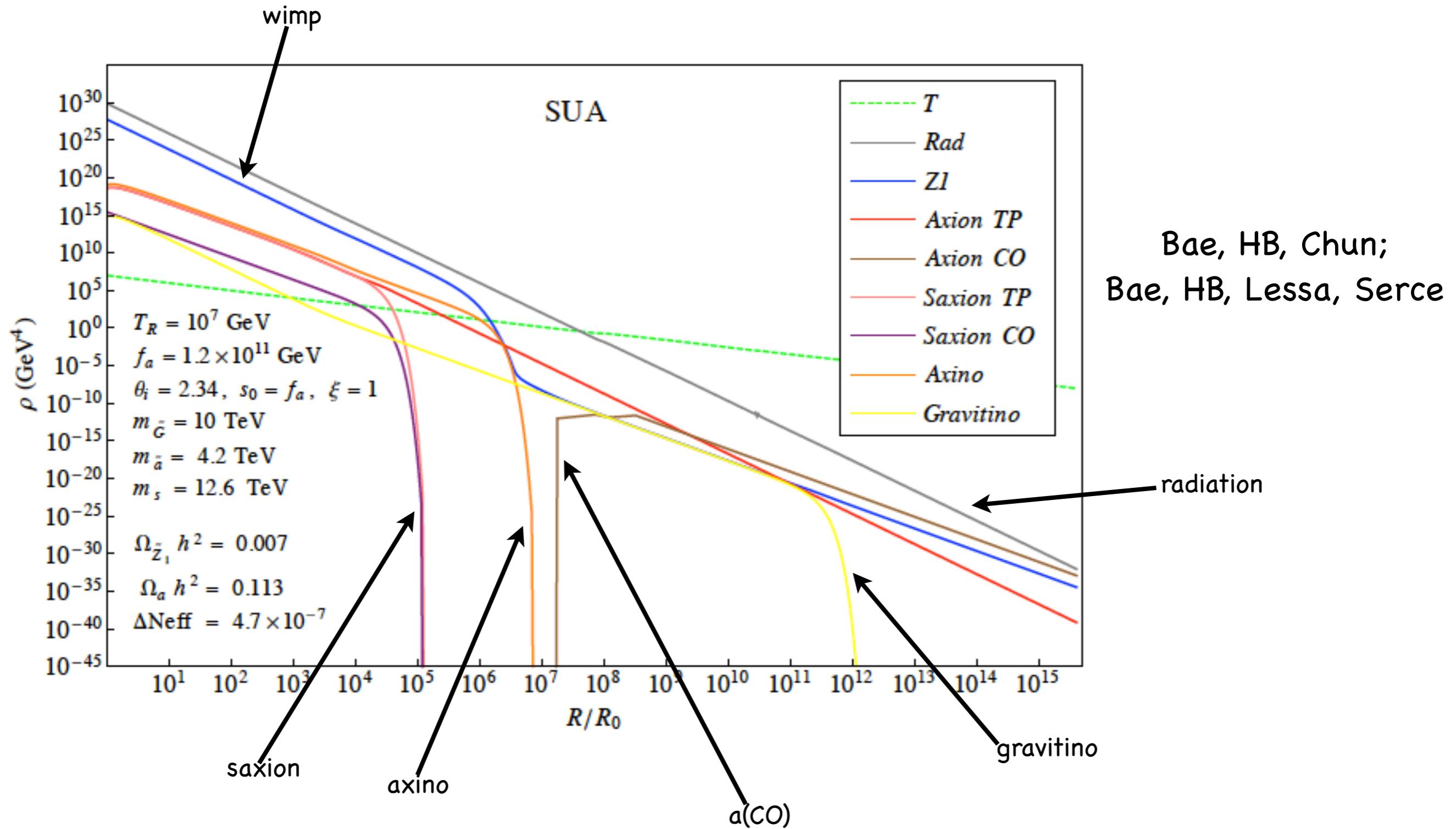
★ astro bound: stellar cooling  $\Rightarrow f_a \gtrsim 10^9 \text{ GeV}$

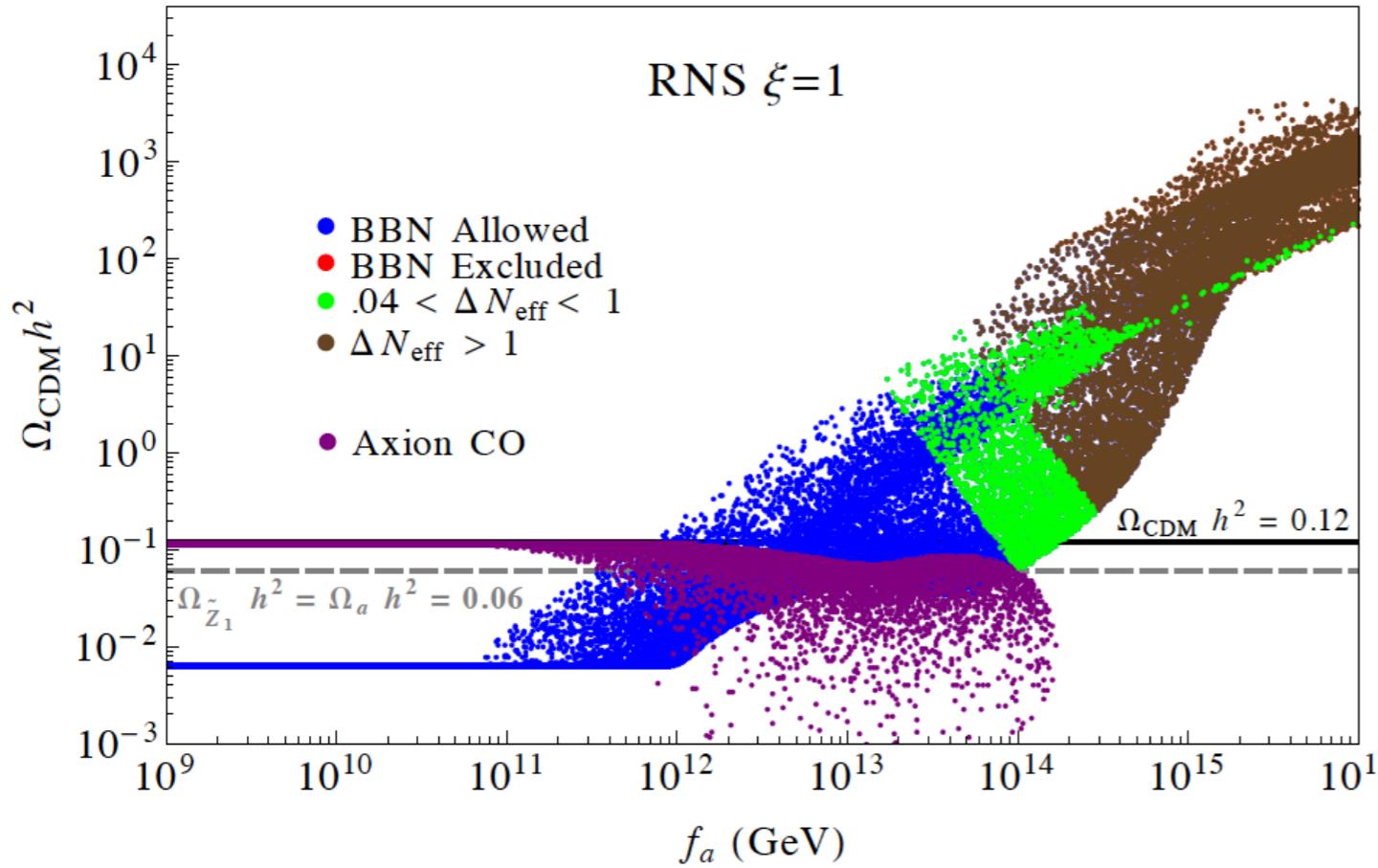


# mixed axion-neutralino production in early universe

- neutralinos: thermally produced (TP) or NTP via  $\tilde{a}$ ,  $s$  or  $\tilde{G}$  decays
  - re-annihilation at  $T_D^{s,\tilde{a}}$
- axions: TP, NTP via  $s \rightarrow aa$ , bose coherent motion (BCM)
- saxions: TP or via BCM
  - $s \rightarrow gg$ : entropy dilution
  - $s \rightarrow SUSY$ : augment neutralinos
  - $s \rightarrow aa$ : dark radiation ( $\Delta N_{eff} < 1.6$ )
- axinos: TP
  - $\tilde{a} \rightarrow SUSY$  augments neutralinos
- gravitinos: TP, decay to SUSY

# DM production in SUSY DFSZ: solve eight coupled Boltzmann equations

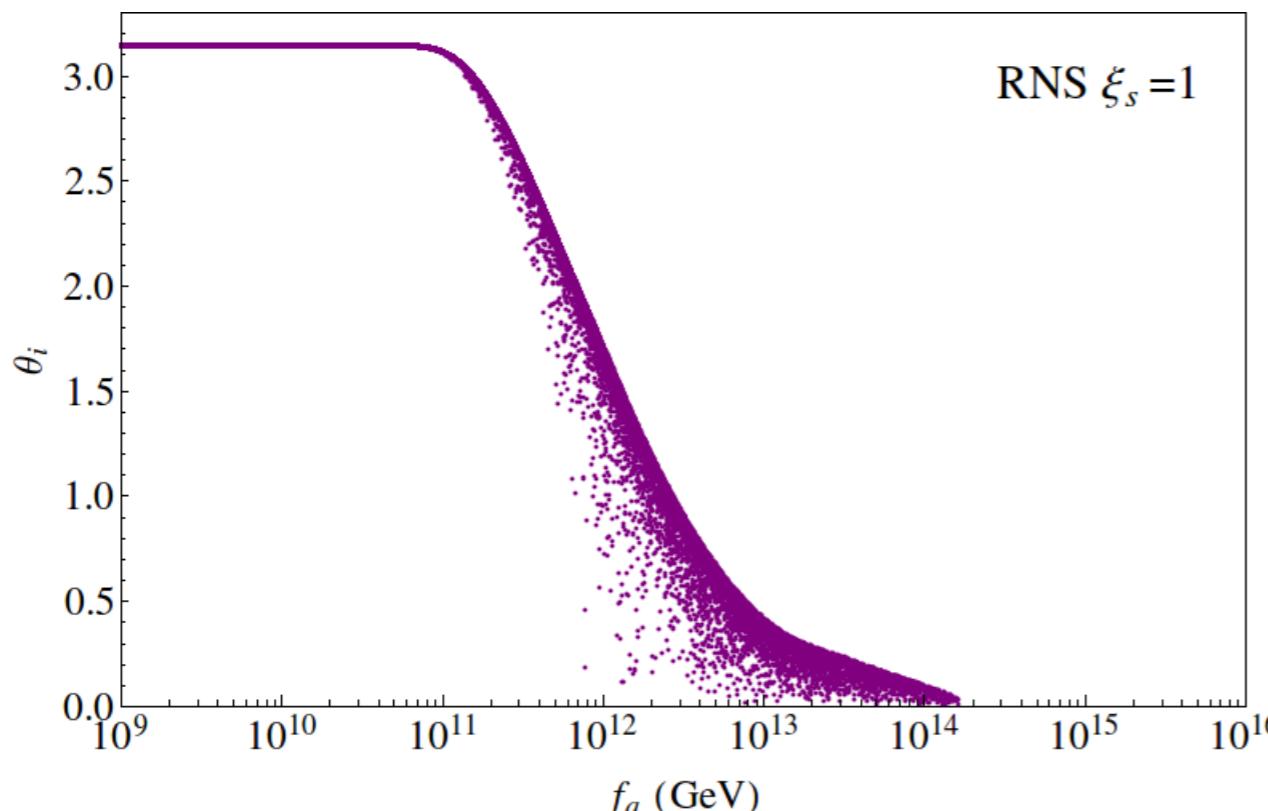




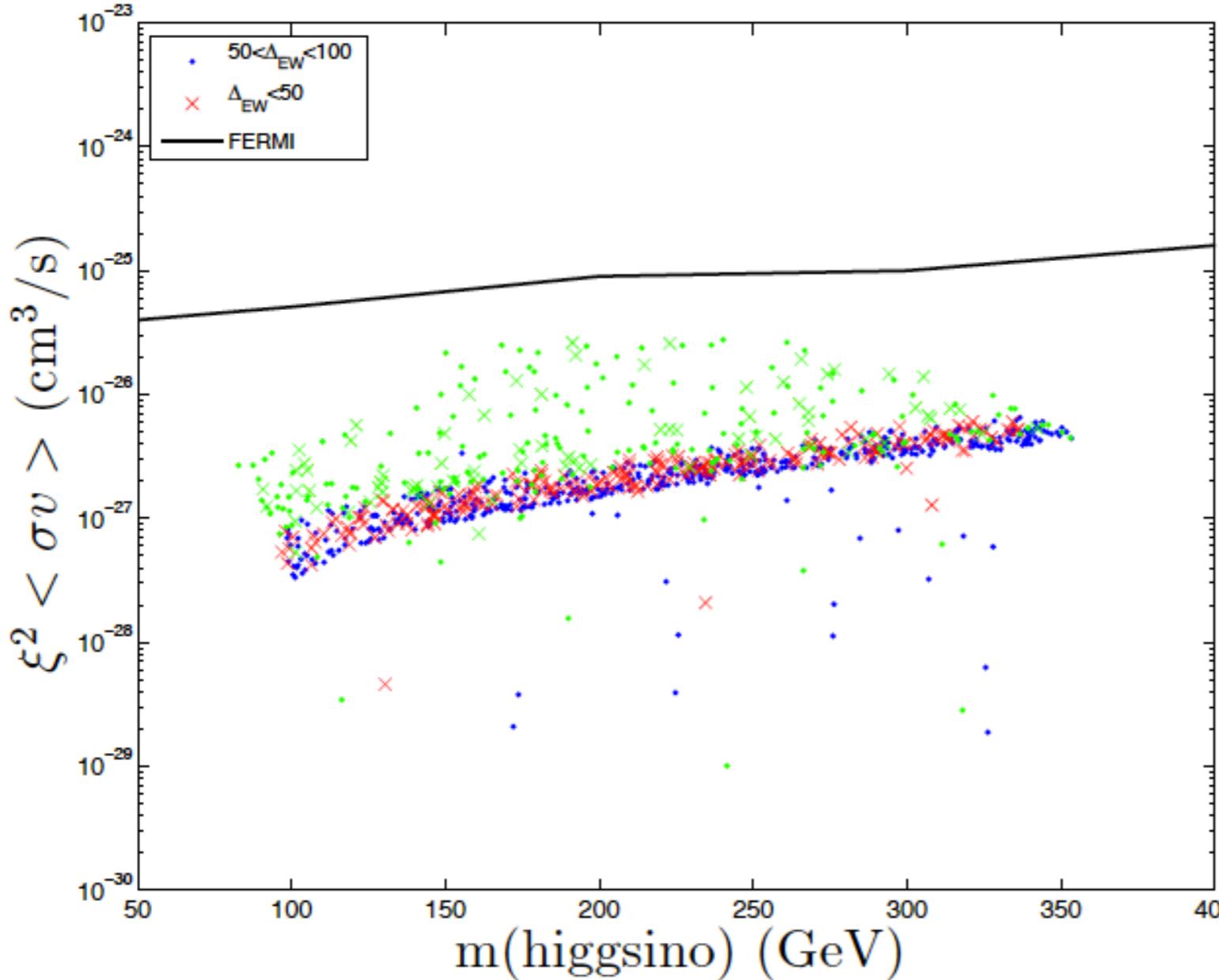
higgsino abundance

axion abundance

mainly axion CDM  
for  $f_a < \sim 10^{12}$  GeV;  
for higher  $f_a$ , then  
get increasing wimp  
abundance



# Higgsino detection via halo annihilations:



green: excluded by Xe-100

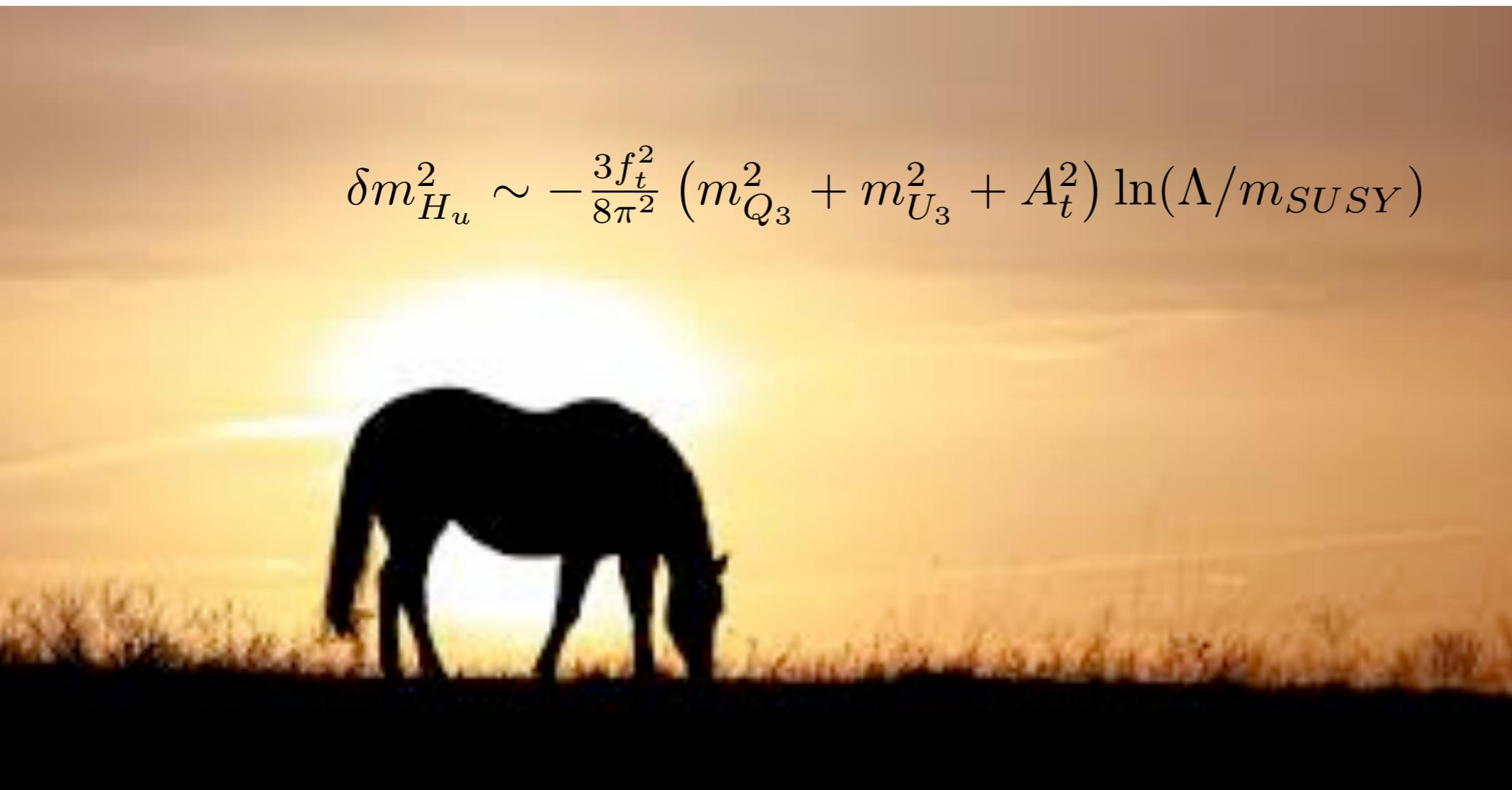
annihilation rate is high but rescaling is **squared**

Gamma-ray sky signal is factor 10-20 below current limits

Recommendation: put this horse out to pasture

$$\delta m_{H_u}^2 \sim -\frac{3f_t^2}{8\pi^2} (m_{Q_3}^2 + m_{U_3}^2 + A_t^2) \ln(\Lambda/m_{SUSY})$$

R.I.P.



sub-TeV 3rd generation squarks **not** required for naturalness