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# The $\mathcal{CP}$ -Violationong 2HDM in Light of a Strong First Order Phase Transition - Implications for Higgs Physics

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Milada Margarete Mühlleitner (KIT)

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# Outline

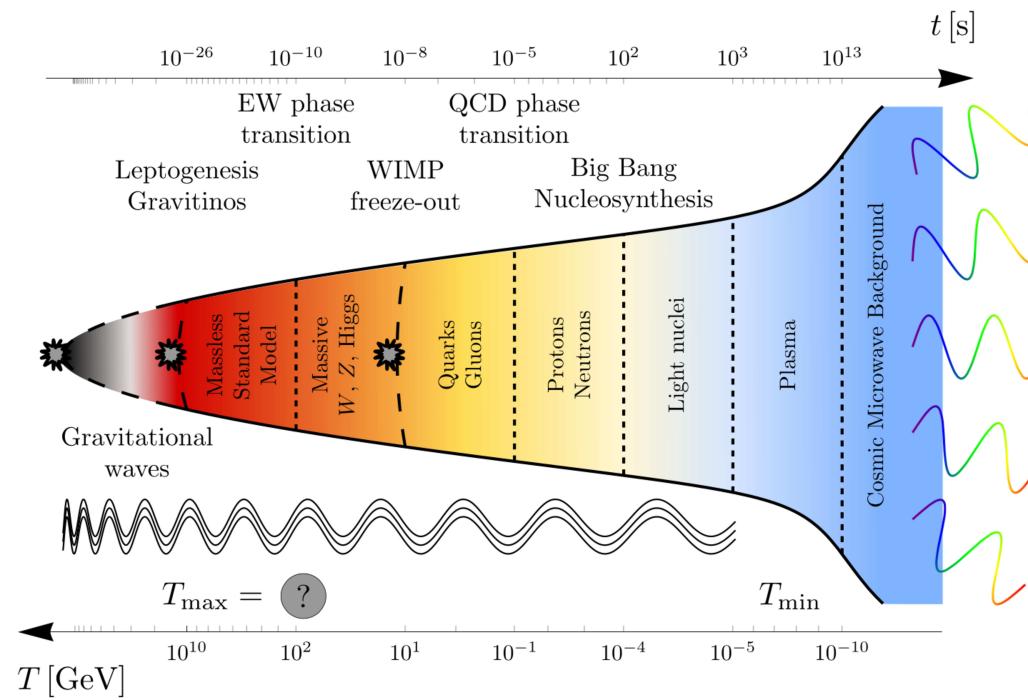
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◊ Introduction

◊ The C2HDM

◊ Results

◊ Conclusions



From K. Schmitz, DESY-THESIS-2012-039

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# *Introduction*

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## Motivation

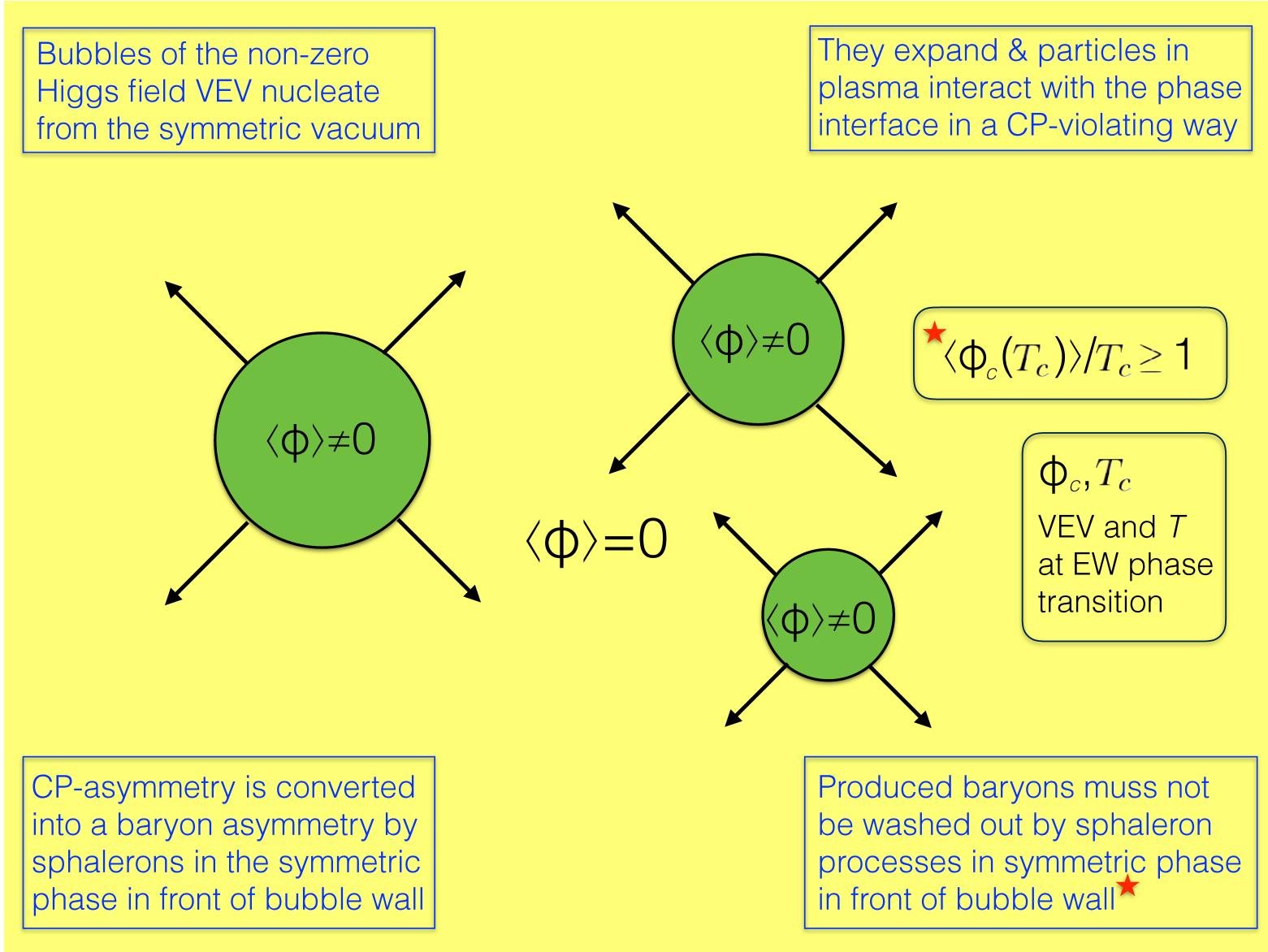
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- **Electroweak Baryogenesis (EWBG):** generation of the observed baryon-antibaryon asymmetry in the electroweak phase transition (EWPT) [Riemer-Sorensen, Jenssen '17]

$$5.8 \cdot 10^{-10} < \frac{n_B - n_{\bar{B}}}{n_\gamma} < 6.6 \cdot 10^{-10}$$

- **Sakharov Conditions:** [Sakharov '67]
  - \* (i)  $B$  number violaton (sphaleron processes)
  - \* (ii)  $C$  and  $CP$  violation
  - \* (iii) Departure from thermal equilibrium

# Baryogenesis in a Nutshell



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## Motivation

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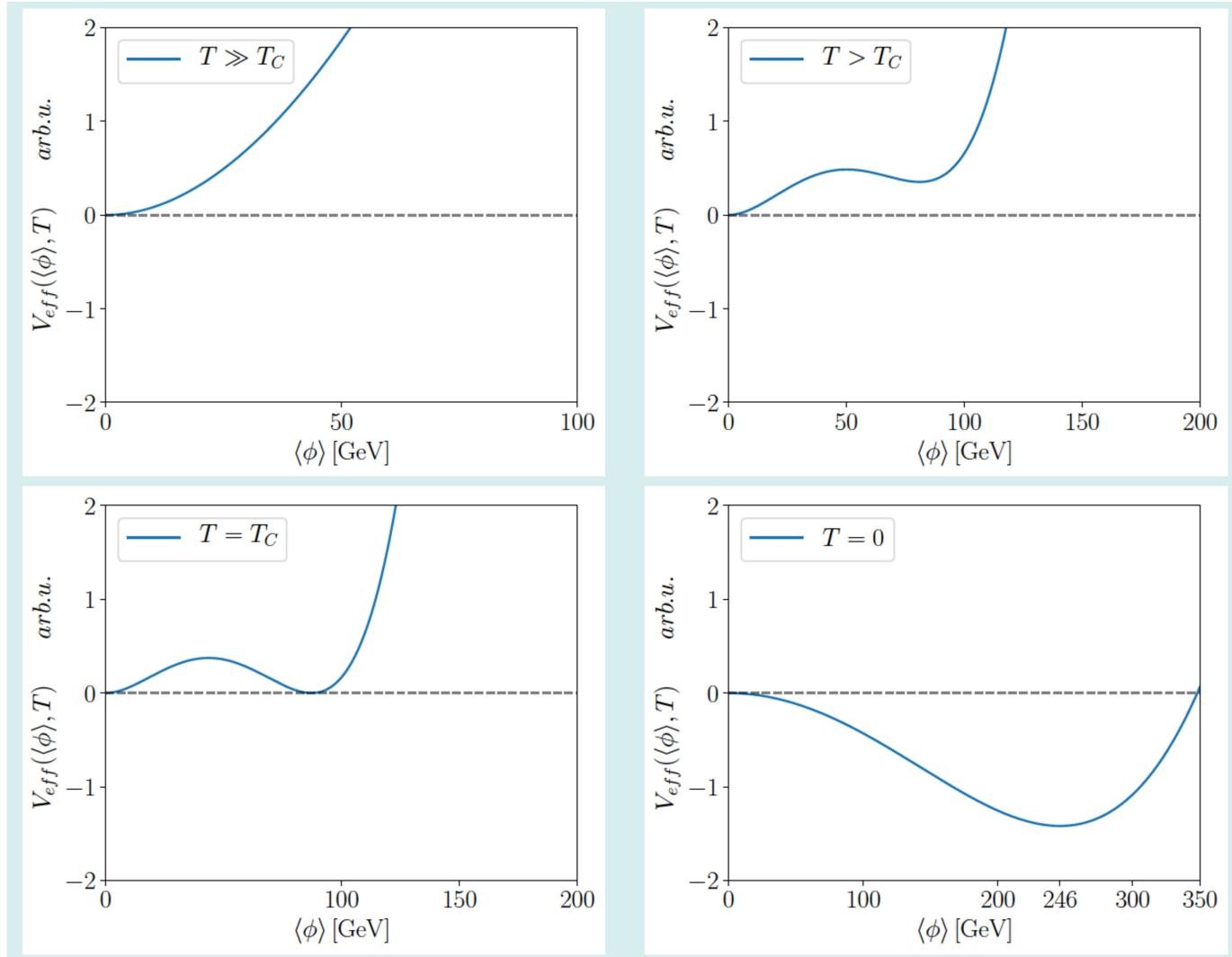
$$5.8 \cdot 10^{-10} < \frac{n_B - n_{\bar{B}}}{n_\gamma} < 6.6 \cdot 10^{-10}$$

- **Sakharov Conditions:** [Sakharov '67]
  - \* (i)  $B$  number violaton (sphaleron processes)
  - \* (ii)  $C$  and  $CP$  violation
  - \* (iii) Departure from thermal equilibrium
- **Additional constraint:** EW phase transition must be strong first order PT [Quiros '94; Moore '99]

$$\xi_c \equiv \frac{\langle \Phi_c \rangle}{T_c} \geq 1$$

$\langle \Phi_c \rangle$  and  $T_c$  field configuration and temperature at phase transition

# Strong $\mathcal{F}$ irst Order Electroweak Phase $\mathcal{T}$ ransition



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## Motivation

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- **Electroweak Baryogenesis in the Standard Model:**

- \* all ingredients required for EWBG contained in the SM, **but**
- \* EW phase transition of strong first order only if  $m_H \lesssim 70$  GeV

[Bochkarev,Shaposhnikov '87; Kajantje eal '95; Fodor eal '96]

- \* CP violation induced by CKM phase not sufficient to generate large enough chiral asymmetries

[Gavela eal '93,'94; Huet,Sather '94]

⇒ consider extended Higgs sectors

- **Extended Higgs sectors:**

- \* additional scalar degrees of freedom can strengthen the PT:
  - additional massive particles
  - enhanced Higgs self-couplings
- \* additional sources of CP violation

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## The C2HDM

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## Baryogenesis in the C2HDM

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- **EWPT in the 2HDM:**

[Bochkarev eal; McLerran eal; Turok eal; Cohen eal; Nelson eal; Funakubo eal; Davies eal; Cline eal; Dorsch eal; Fromme eal; Haarr eal; Basler eal; Gorda eal; Laine,Rummukainen; Bernon eal; Andersen eal]

- **This talk:** based on

2HDM: [Basler,Krause,MM,Wittbrodt,Wlotzka, JHEP 1702 (2017) 121]

C2HDM: [Basler,MM,Wittbrodt, JHEP 1803 (2018) 061]

- **Features:**

- \* Inclusion of theoretical and newest experimental constraints
- \* 'On-shell' renormalization
- \* Inclusion of CP violation - investigation of possible spontaneously generated CP violation
- \* Detailed analysis of implications on collider observables

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## The Tree-Level Higgs Potential

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- The tree-level Higgs potential:

$$V_{\text{tree}} = m_{11}^2 \Phi_1^\dagger \Phi_1 + m_{22}^2 \Phi_2^\dagger \Phi_2 - \left[ \textcolor{blue}{m_{12}^2} \Phi_1^\dagger \Phi_2 + \text{h.c.} \right] + \frac{1}{2} \lambda_1 (\Phi_1^\dagger \Phi_1)^2 + \frac{1}{2} \lambda_2 (\Phi_2^\dagger \Phi_2)^2 \\ + \lambda_3 (\Phi_1^\dagger \Phi_1)(\Phi_2^\dagger \Phi_2) + \lambda_4 (\Phi_1^\dagger \Phi_2)(\Phi_2^\dagger \Phi_1) + \left[ \frac{1}{2} \textcolor{blue}{\lambda_5} (\Phi_1^\dagger \Phi_2)^2 + \text{h.c.} \right].$$

- CP Violation:  $m_{12}^2, \lambda_5$  can be complex (all others real);  $\textcolor{blue}{m_{12}^2} \neq \lambda_5 \rightsquigarrow$  CP violation
- Higgs fields after EWSB: at  $T \neq 0$

$$\Phi_1 = \frac{1}{\sqrt{2}} \begin{pmatrix} \rho_1 + i\eta_1 \\ \textcolor{blue}{\omega_1} + \zeta_1 + i\psi_1 \end{pmatrix}$$
$$\Phi_2 = \frac{1}{\sqrt{2}} \begin{pmatrix} \omega_{\text{CB}} + \rho_2 + i\eta_2 \\ \omega_2 + i\omega_{\text{CP}} + \zeta_2 + i\psi_2 \end{pmatrix}$$

includes possibility of (unphysical) charge breaking  $\omega_{\text{CB}}$  and CP breaking  $\omega_{\text{CP}}$  minima

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## The Tree-Level Higgs Potential

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- CP Violation:  $m_{12}^2, \lambda_5$  can be complex (all others real);  $\textcolor{blue}{m_{12}^2} \neq \lambda_5 \rightsquigarrow$  CP violation
- Higgs fields after EWSB: at  $T = 0$

$$\Phi_1 = \frac{1}{\sqrt{2}} \begin{pmatrix} \rho_1 + i\eta_1 \\ \textcolor{blue}{v}_1 + \zeta_1 + i\psi_1 \end{pmatrix}$$
$$\Phi_2 = \frac{1}{\sqrt{2}} \begin{pmatrix} +\rho_2 + i\eta_2 \\ \textcolor{blue}{v}_2 + \zeta_2 + i\psi_2 \end{pmatrix}$$

$$T = 0: \omega_{\text{CP}}, \omega_{\text{CB}} \rightarrow 0, \omega_1 \rightarrow v_1, \omega_2 \rightarrow v_2 \quad v_1^2 + v_2^2 = (246 \text{ GeV})^2, \tan \beta \equiv \frac{v_2}{v_1}$$

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## The Tree-Level Higgs Potential

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- **Particle content:**

3 neutral CP-mixing Higgs bosons  $H_1, H_2, H_3$

1 charged Higgs pair  $H^\pm$

- **Flavour-Changing Neutral Currents (FCNC) at tree-level:** forbidden by  $\mathbb{Z}_2$  symmetry

$$\Phi_1 \rightarrow \Phi_1 , \quad \Phi_2 \rightarrow -\Phi_2 .$$

$\rightsquigarrow$  4 types of 2HDM

- **Classification of the Yukawa sector:**

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	Type I	Type II	Lepton-Specific	Flipped
Up-type quarks	$\Phi_2$	$\Phi_2$	$\Phi_2$	$\Phi_2$
Down-type quarks	$\Phi_2$	$\Phi_1$	$\Phi_2$	$\Phi_1$
Leptons	$\Phi_2$	$\Phi_1$	$\Phi_1$	$\Phi_2$

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# The Loop-Corrected Effective Potential at Finite Temperature

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- **Investigate phase transition:** determine

$$\xi_c \equiv \frac{\langle \Phi_c \rangle}{T_c}$$

for C2HDM taking into account all theoretical and experimental constraints

- **Effective potential at finite temperature:**

$$V_{\text{eff}}^{(1)}(\vec{\omega}, \textcolor{red}{T}) = V_{\text{tree}}(\vec{\omega}) + V_{\text{CW}}(\vec{\omega}) + V_{\text{CT}}(\vec{\omega}) + V_T(\vec{\omega}, \textcolor{red}{T})$$

- **$T = 0$  1-loop contribution:** Coleman-Weinberg contribution

[Coleman, Weinberg '73]

$$V_{\text{CW}} = \sum_i \frac{n_i}{64\pi^2} (-1)^{2s_i} m_i^4(\vec{\omega}) \left[ \ln \left( \frac{m_i^2(\vec{\omega})}{\mu^2} \right) - c_i \right]$$

$n_i$  number of degrees of freedom

$\mu$  renormalization scale, set to VEV  $v \approx 246$  GeV

$\overline{\text{MS}}$  renormalization constants  $c_i = 5/6$  for bosons,  $c_i = 3/2$  otherwise

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## The Loop-Corrected Effective Potential at Finite Temperature

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- **The counterterm potential:**

Choose  $V_{CT}$  such that the minimum, the masses and the mixing angles at  $T = 0$  remain the same at one-loop level

[Basler,Krause,MM,Wittbrodt,Wlotzka '16]

$$\begin{aligned} 0 &= (\partial_{\phi_i} V_{CT} + \partial_{\phi_i} V_{CW})|_{\langle\phi\rangle_{T=0}} \\ 0 &= (\partial_{\phi_i} \partial_{\phi_j} V_{CT} + \partial_{\phi_i} \partial_{\phi_j} V_{CW})|_{\langle\phi\rangle_{T=0}} \end{aligned}$$

- **$T \neq 0$  contribution:**

- Thermal loops (fermionic (+) and bosonic (−) integral  $J_{\pm}$ )

[Carena et al '08]

$$V_T = \sum_i n_i \frac{T^4}{2\pi^2} J_{\pm}(m_i^2(\vec{\omega})/T^2)$$

- Thermal mass corrections

[Arnold,Espinosa '94]

$$J_- \left( \frac{m_i^2}{T^2} \right) \rightarrow J_- \left( \frac{m_i^2}{T^2} \right) - \frac{\pi}{6} (\bar{m}_i^3 - m_i^3), \quad i = W_L^{\pm}, Z_L, \gamma_L, \Phi^0, \Phi^{\pm}$$

with the thermal masses  $\bar{m}_i$

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## Parameter Scan

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- **Scan over parameter space:**

with ScannerS, checks for: [Coimbra,Sampaio,Santos '13; Ferreira,Guedes,Sampaio,Santos '14]

- **Theoretical constraints:**

boundedness from below, tree-level perturbative unitarity, EW vacuum is global minimum of tree-level potential at  $T = 0$

- **Experimental constraints::**

- \*  $S, T, U$  parameters for EW precision observables [Baak eal '14]
- \*  $R_b = \Gamma(Z \rightarrow b\bar{b})/\Gamma(Z \rightarrow \text{hadrons})$  and  $B \rightarrow X_s \gamma$  [Haber,Logan '99; Deschamps eal '09; Mahmoudi,Stal '09; Steinhauser eal '17]
- \* Higgs exclusion bounds by HiggsBounds [Bechtle eal '08,'11,'13]
- \* Higgs rates checked via SUSHI and C2HDM\_HDECAY [Harlander eal; Fontes eal]
- \* Electric dipole moment of the electron [The ACME Collaboration]

- **Calculation of the global electroweak minimum:**

as function of  $T$  to determine  $\xi_c \leftarrow$  use of code BSMPT [Basler,MM '18]

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# BSMPT

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- **BSMPT - Beyond the Standard Model Phase Transitions:**

[Basler,MM '18]

A C++ tool for the electroweak phase transition in extended Higgs sectors

Computation of loop-corrected effective potential at  $T \neq 0$  including the thermal masses

Renormalization based on physical conditions (see previous slides)

- **Features:**

- \* Computation of  $\xi_c = v_c/T_c$
- \* Calculation of evolution of the VEV(s) with  $T$
- \* Calculation of the global minimum of the 1-loop-corrected potential at  $T = 0$
- \* Computation of the loop-corrected trilinear Higgs self-couplings in the “on-shell” scheme

- **Models:** generic code allows for easy implementation of new models

implemented models: 2HDM, C2HDM, N2HDM

- **Webpage:** <https://github.com/phbasler/BSMPT>

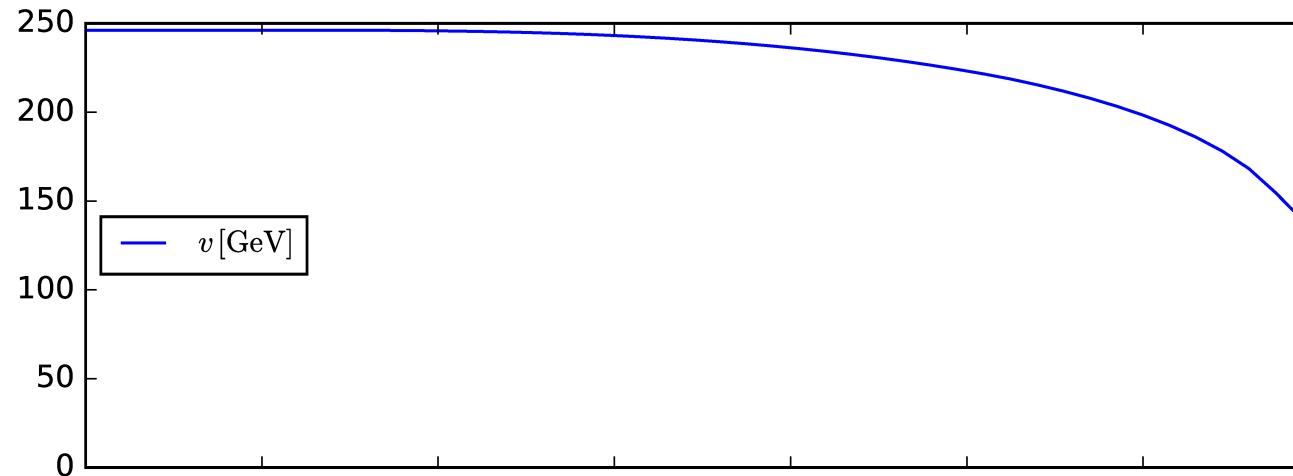
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# Results

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## Evolution of the Vacuum

[Basler,MM,Wittbrodt '17]



Type I

$$m_{H_1} = 125.09 \text{ GeV}$$

$$m_{H_2} = 236.99 \text{ GeV}$$

$$m_{H_3} = 542.95 \text{ GeV}$$

$$m_{H^\pm} = 223.76 \text{ GeV}$$

$$\tan \beta = 6.95$$

$$\text{Re}(m_{12}^2) = 8044.9 \text{ GeV}^2$$

$$\alpha_1 = 0.41\pi$$

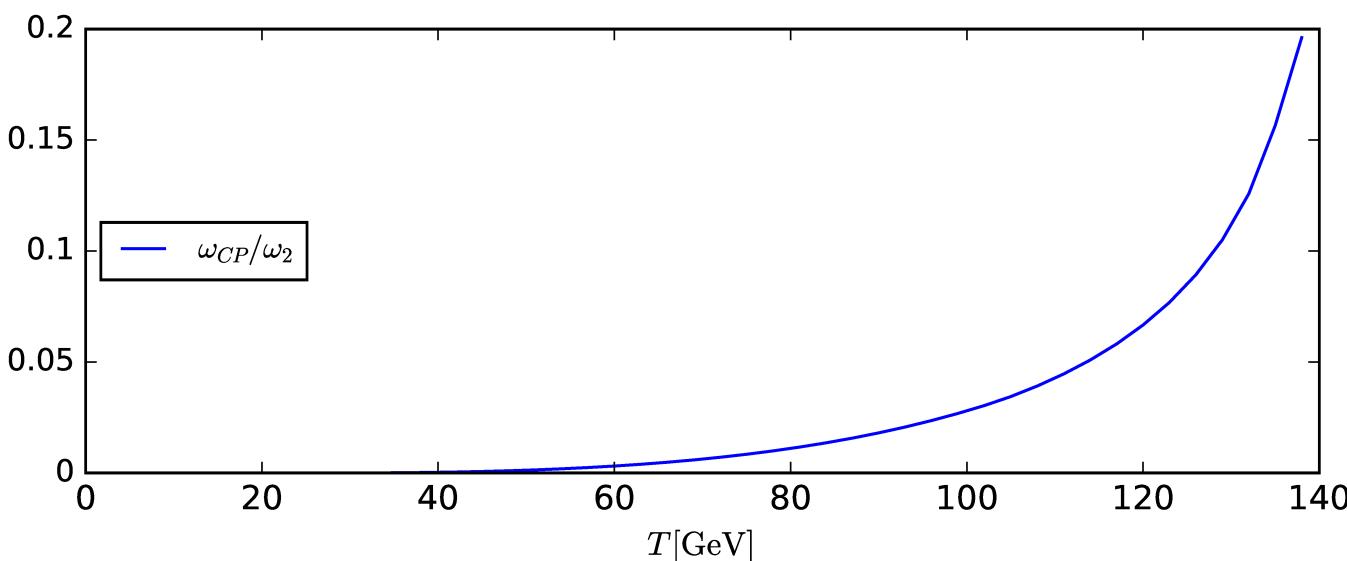
$$\alpha_2 = -0.016\pi$$

$$\alpha_3 = 0.041\pi$$

$$v_c = 139.274 \text{ GeV}$$

$$T_c = 138.913 \text{ GeV}$$

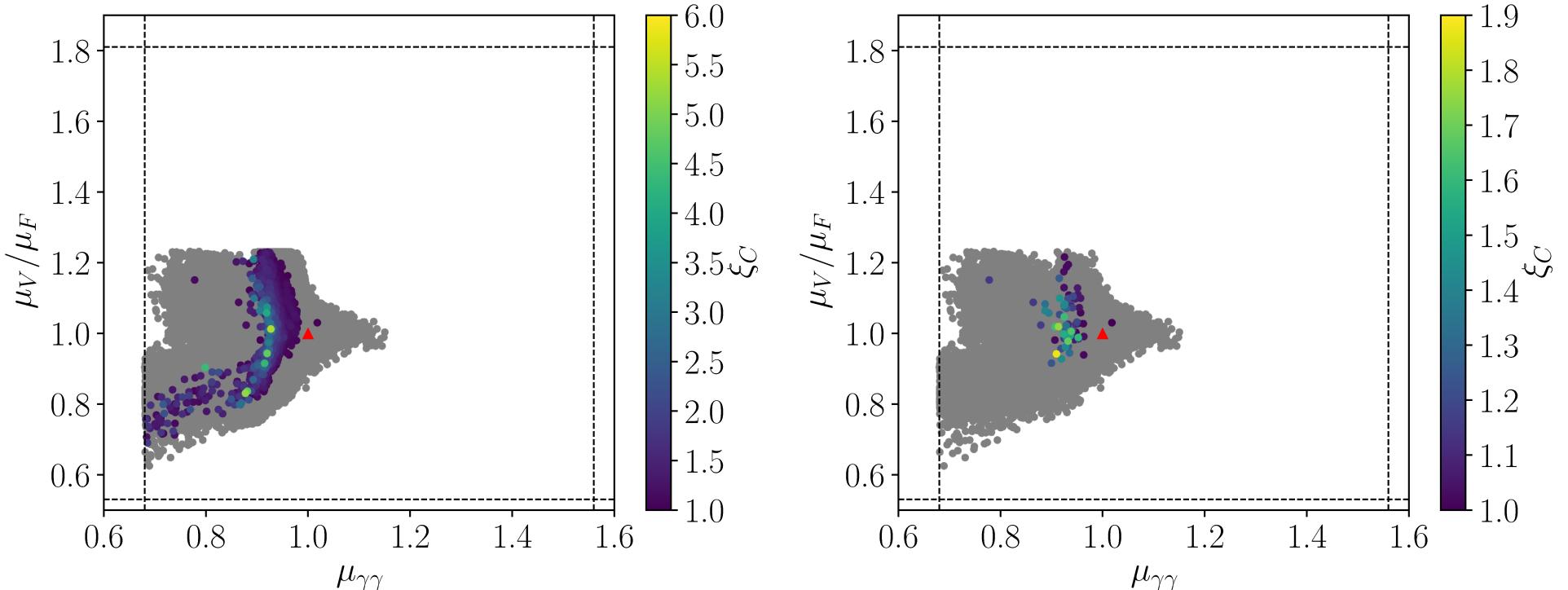
$$\xi_c = 1.0026 \text{ GeV}$$



## Signal Rates at the LHC

Type I,  $H_1 = h$  - right plot: only CP-violating points

[Basler,MM,Wittbrodt '17]



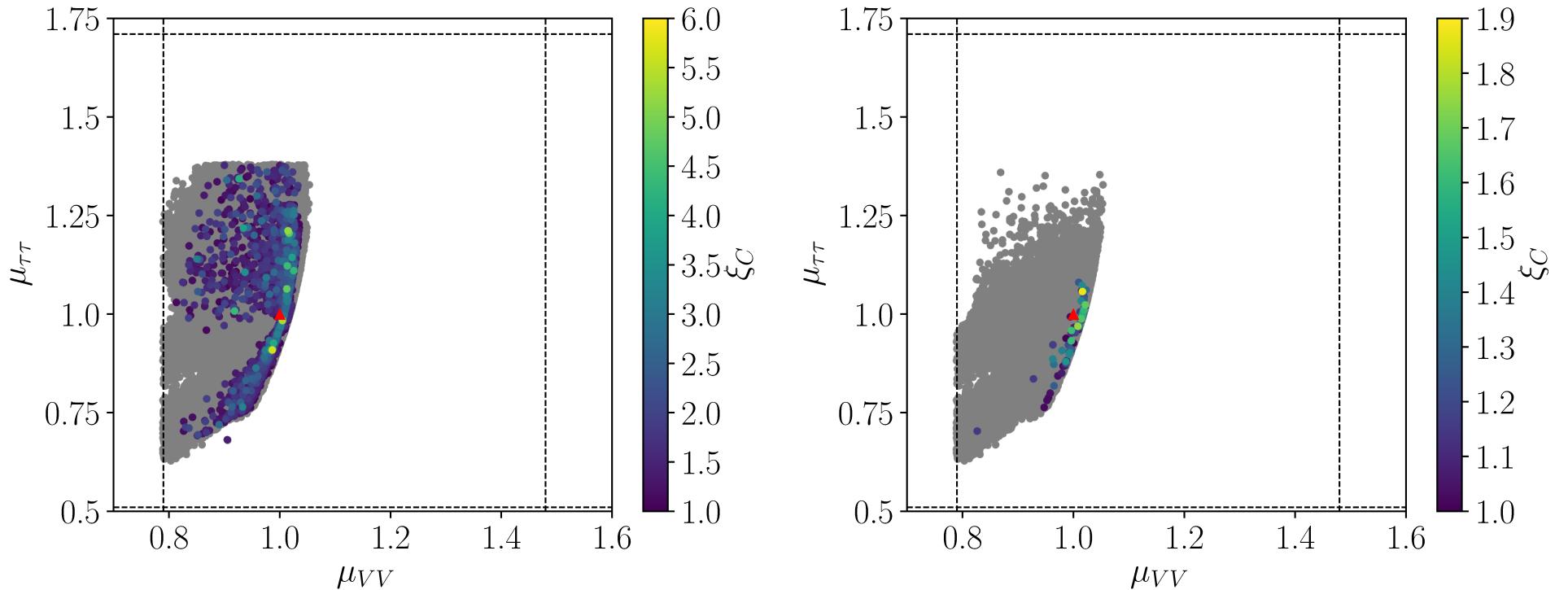
- \*  $\mu_F = \sigma_{\text{C2HDM}}(ggF + bbF)/\sigma_{\text{SM}}(ggF)$  and  $\mu_V = \sigma_{\text{C2HDM}}(VBF + VH)/\sigma_{\text{SM}}(VBF + VH)$
- \* Signal rates: ( $H_i = h_{125}$ )

$$\mu_{xx} = \mu_F \times \frac{\text{BR}_{\text{C2HDM}}(H_i \rightarrow xx)}{\text{BR}_{\text{SM}}(H_i \rightarrow xx)}$$

## Signal Rates at the LHC

Type I,  $H_1 = h$  - right plot: only CP-violating points

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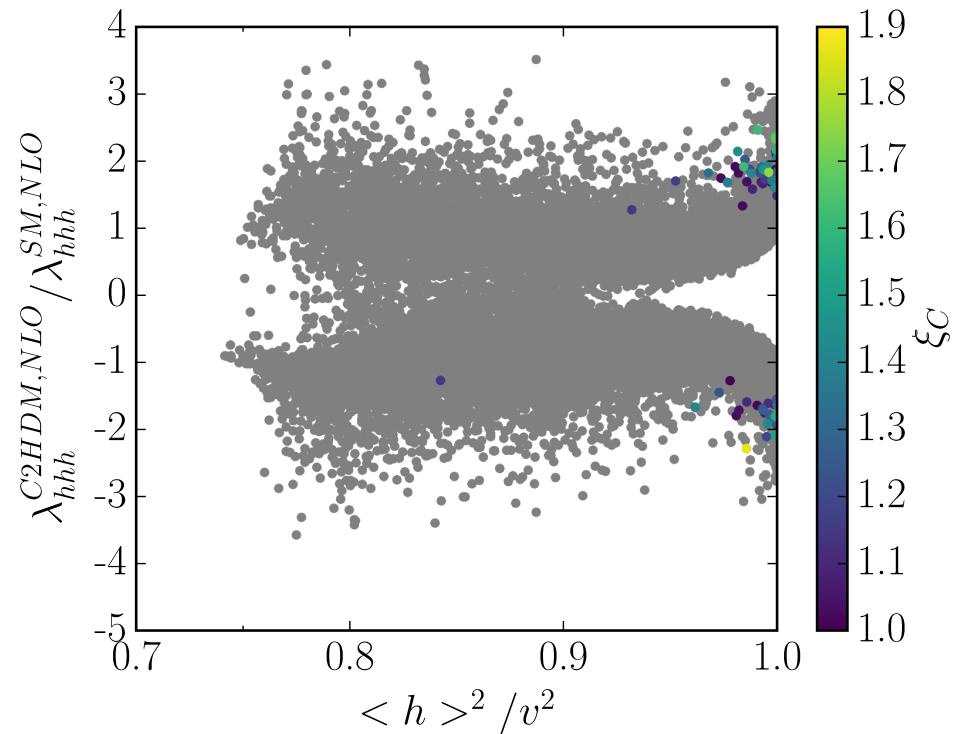
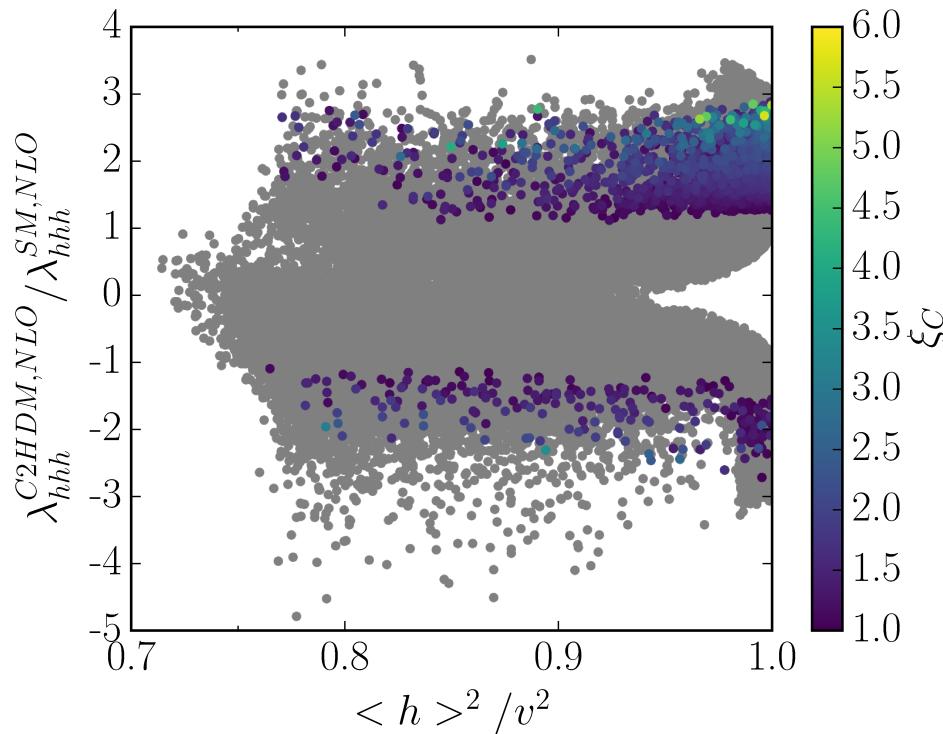
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$$\mu_{xx} = \mu_F \times \frac{\text{BR}_{\text{C2HDM}}(H_i \rightarrow xx)}{\text{BR}_{\text{SM}}(H_i \rightarrow xx)}$$

# Effects on the Trilinear Higgs Self-Coupling

Type I,  $H_1 = h$  - right plot: only CP-violating points

[Basler,MM,Wittbrodt '17]



- \* Plots include unitarity constraints

$$* \quad 1.1 \lesssim \left| \frac{\lambda_{hhh}^{\text{C2HDM,NLO}}}{\lambda_{hhh}^{\text{SM,NLO}}} \right| \lesssim 2.9$$

- \* Most CP-violating points require  $\frac{\langle h \rangle^2}{v^2} \gtrsim 0.95$

- \* CP-odd part of  $h \lesssim 24\% \xrightarrow{\text{EWPT}} \sim 2.5\%$

## Benchmark Point

$m_{H_1}$ [GeV]	125.09	$\text{BR}(H_2)$	$\text{BR}(H_2 \rightarrow H_1 H_1) = 0.400$
$m_{H_2}$ [GeV]	291.49		$\text{BR}(H_2 \rightarrow Z H_1) = 0.294$
$m_{H^\pm}$ [GeV]	543.30		$\text{BR}(H_2 \rightarrow WW) = 0.156$
$\text{Re}(m_{12}^2)$ [GeV $^2$ ]	15590	$\text{BR}(H_3)$	$\text{BR}(H_3 \rightarrow Z H_2) = 0.940$
$\alpha_1$	1.366		$\text{BR}(H_3 \rightarrow t\bar{t}) = 0.056$
$\alpha_2$	-0.028		$\text{BR}(H_3 \rightarrow WW) = 0.002$
$\alpha_3$	0.086	$\text{BR}(H^\pm)$	$\text{BR}(H^\pm \rightarrow W H_2) = 0.943$
$\tan \beta$	5.08		$\text{BR}(H^\pm \rightarrow t\bar{b}) = 0.054$
$m_{H_3}$ [GeV]	548.97		$\text{BR}(H^\pm \rightarrow W H_1) = 0.002$
$\xi_c$	1.52		
$R_{13}^2$	$7.641 \cdot 10^{-4}$		Combination of rates to identify CP violation:
$R_{23}^2$	$7.436 \cdot 10^{-3}$		* type I, $H_1$ SM-like, mostly CP-even
$R_{33}^2$	0.992		* $H_2 \rightarrow Z H_1 \wedge H_2 \rightarrow WW$ forbidden w/o CP violation
$\sigma_{hh}^{\text{NLO}}$ [fb]	217.95		see also, [Branco eal '99; Fontes eal '15, King eal '15]

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## Conclusions

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- \* Detailed phenomenological analysis taking into account recent bounds and constraints
- \* Strong first order EWPT possible in the C2DHM
- \* Overall  $\xi_c = v_c/T_c$  smaller than in CP-conserving 2HDM
- \* Explicit CP violation at  $T = 0$  induces spontaneous CP violation at the EWPT
- \* Trilinear Higgs self-coupling larger than in SM
- \*  $\mu$ -values of SM-like Higgs boson in C2HDM with strong PT more restricted than in CP-conserving 2HDM
- \* Like in 2HDM, strong PT prefers hierarchy with mass gap between the non-SM-like Higgs bosons, but: also approximately mass degenerate scenarios possible

Successful link between cosmology and collider phenomenology

*Thank You For Your Attention!*



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## Input Parameters

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- Tadpole conditions:

$$\begin{aligned} m_{11}^2 &= \operatorname{Re}(m_{12}^2) \frac{v_2}{v_1} - \frac{v_1^2}{2} \lambda_1 - \frac{v_2^2}{2} \lambda_{345} \\ m_{22}^2 &= \operatorname{Re}(m_{12}^2) \frac{v_1}{v_2} - \frac{v_2^2}{2} \lambda_2 - \frac{v_1^2}{2} \lambda_{345} \\ 2 \operatorname{Im}(m_{12}^2) &= v_1 v_2 \operatorname{Im}(\lambda_5), \end{aligned}$$

fix one of the parameters

- Input parameters:

$$v, \quad t_\beta, \quad \alpha_{1,2,3}, \quad m_{H_i}, \quad m_{H_j}, \quad m_{H^\pm} \quad \text{and} \quad \operatorname{Re}(m_{12}^2).$$

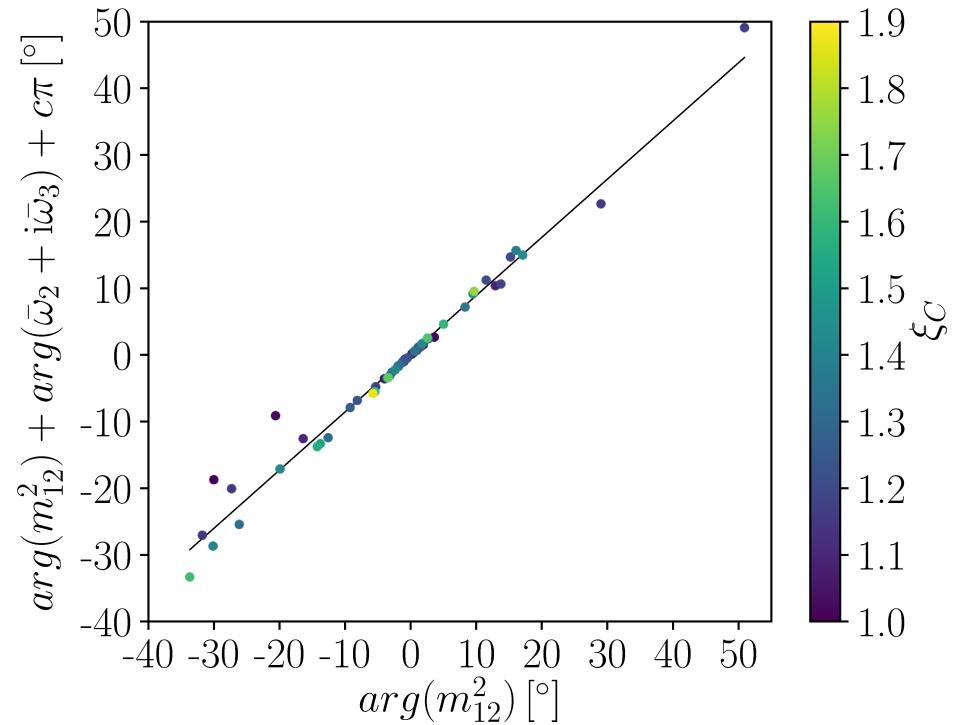
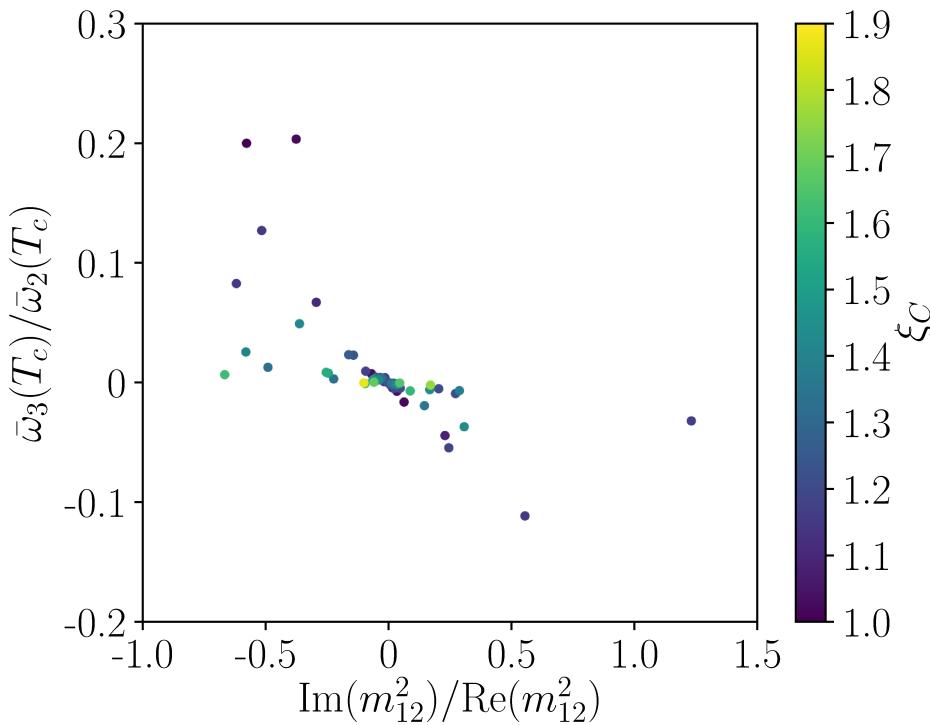
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## Spontaneous Generation of a $\mathcal{CP}$ -Violating Phase

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Type I,  $H_1 = h$

[Basler,MM,Wittbrodt '17]



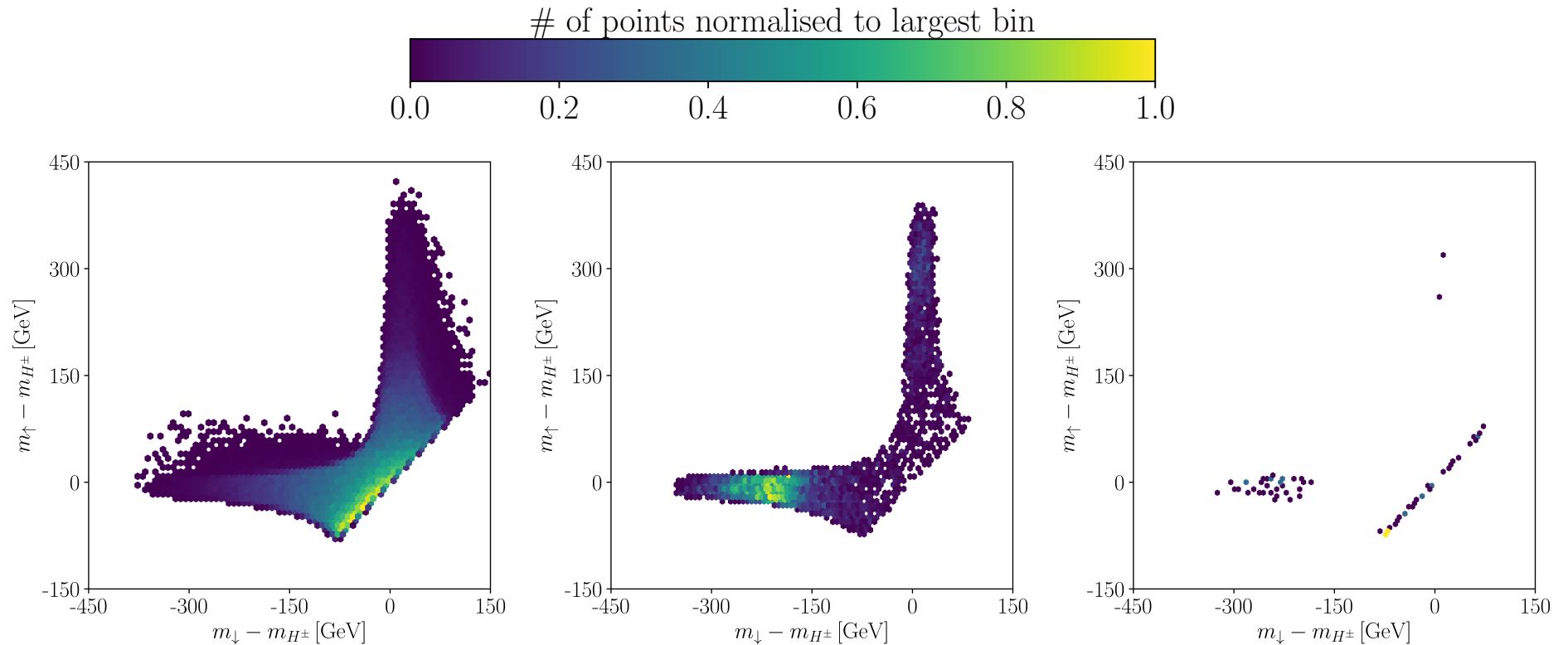
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## Mass Differences

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Type I,  $H_1 = h$

[Basler,MM,Wittbrodt '17]



left: all points passing the constraints; middle: all points with a strong PT and CP conservation;  
right: all points with  $\xi_c > 1$  and explicit CP violation

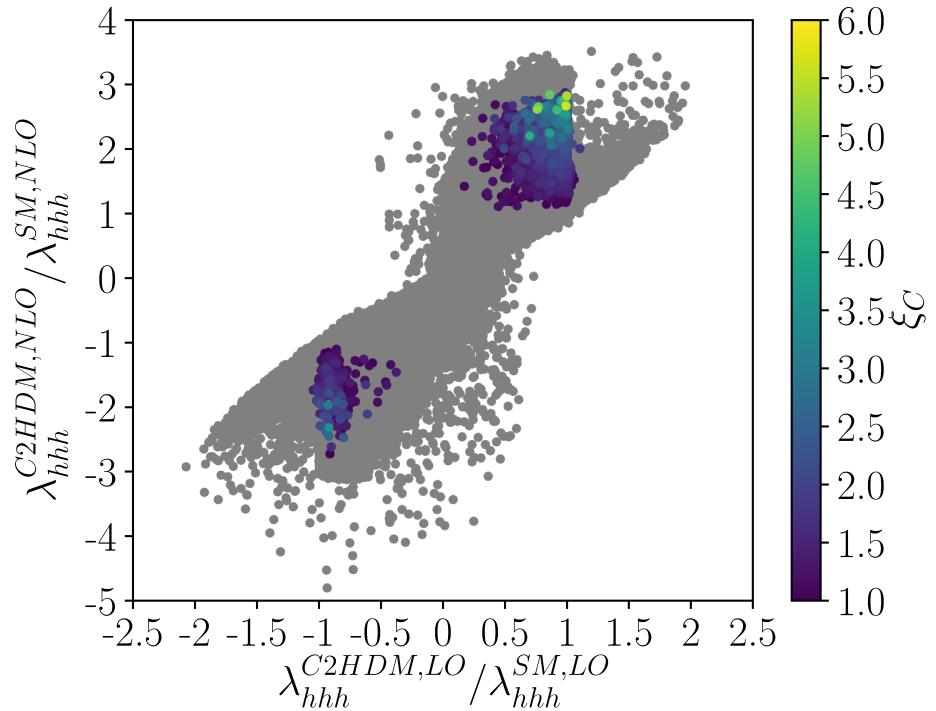
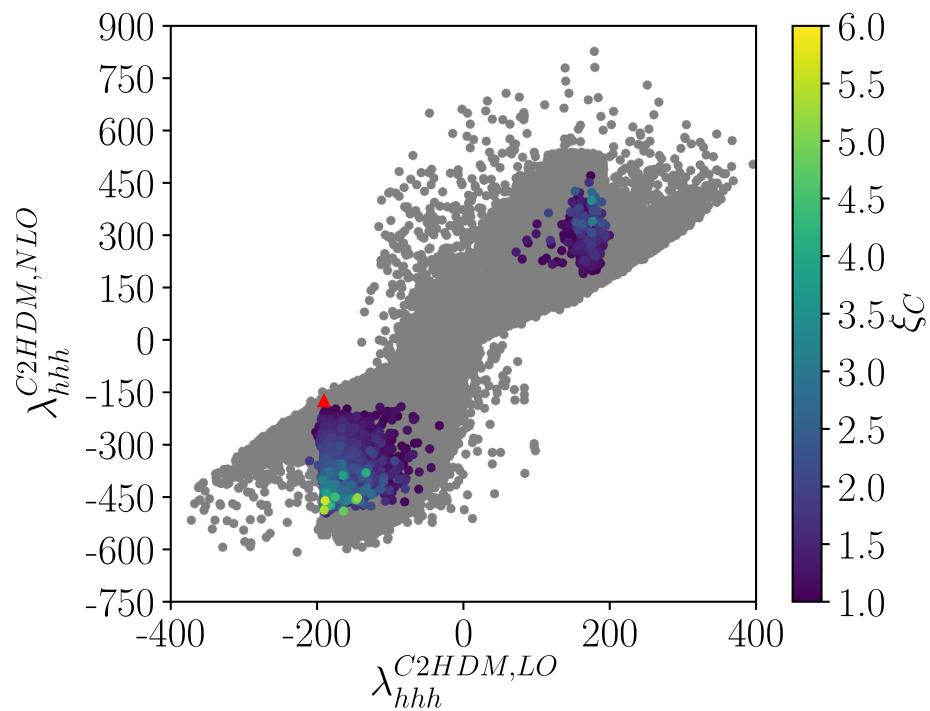
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## Corrections to the $\mathcal{T}$ rilinear Higgs Self-Coupling

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Type I,  $H_1 = h$

[Basler,MM,Wittbrodt '17]



red triangle: SM point; coloured points  $\xi_c > 1$

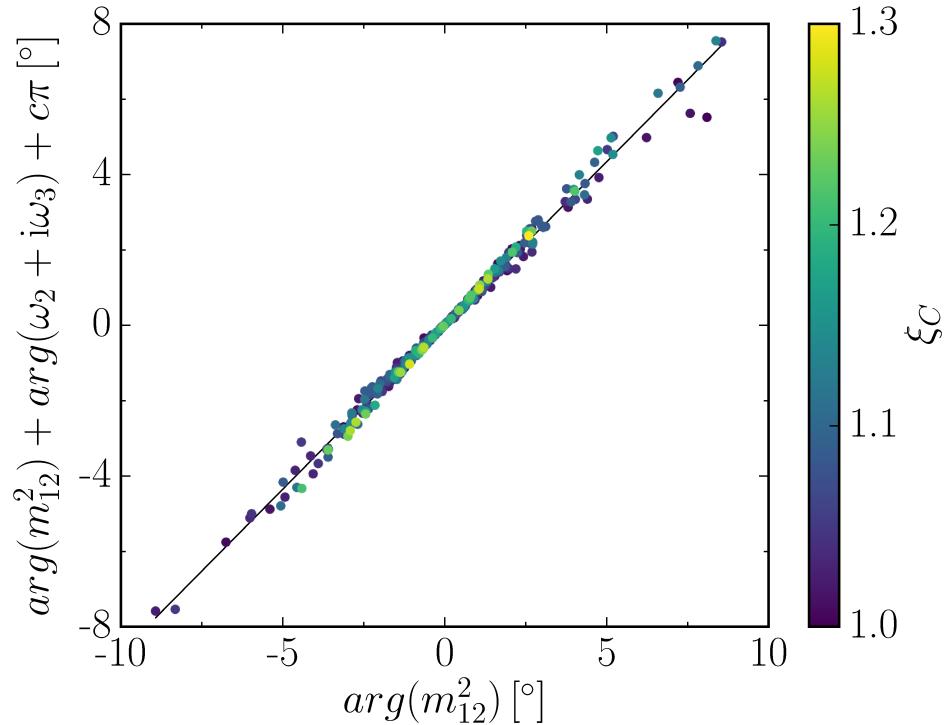
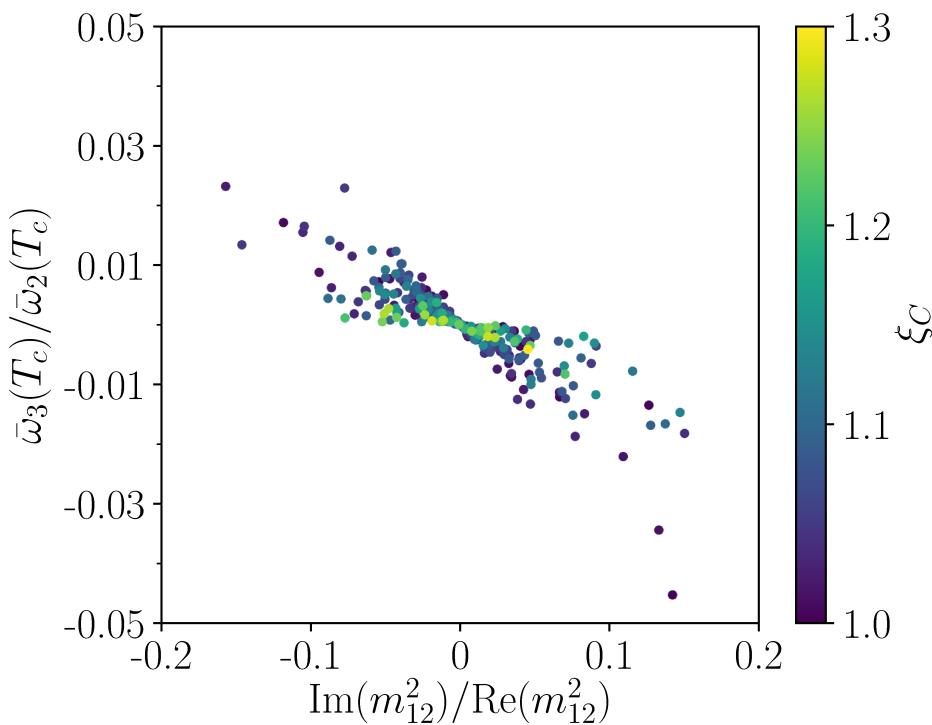
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## Spontaneous Generation of a $\mathcal{CP}$ -Violating Phase

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Type II,  $H_1 = h$

[Basler,MM,Wittbrodt '17]



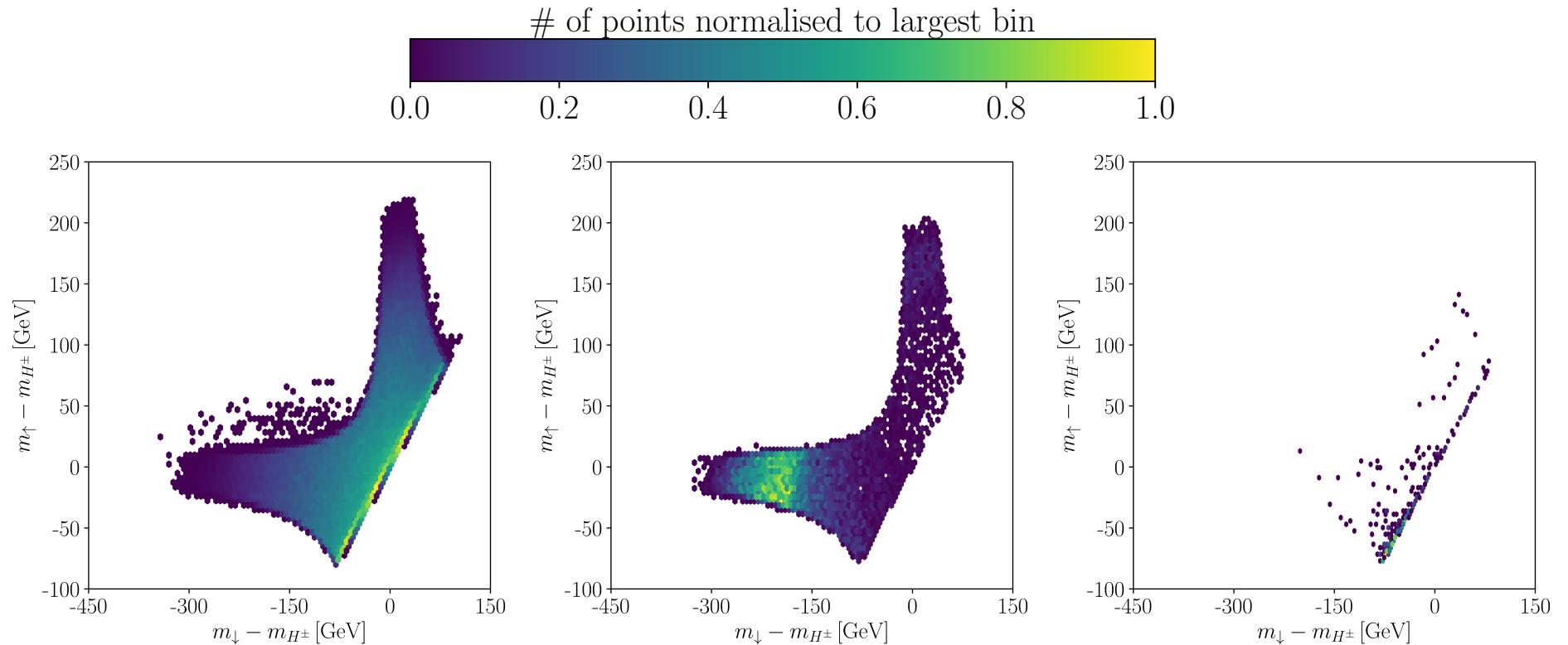
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## Mass Differences

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Type II,  $H_1 = h$

[Basler,MM,Wittbrodt '17]

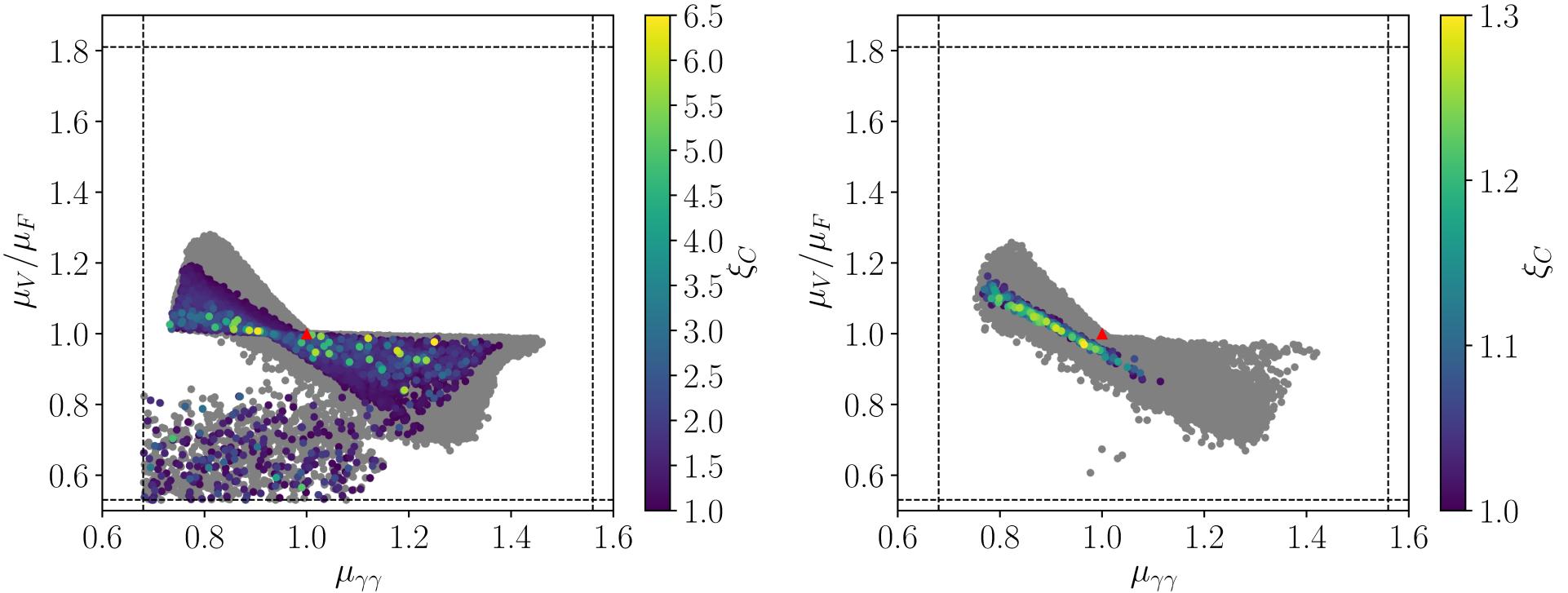


left: all points passing the constraints; middle: all points with a strong PT and CP conservation;  
right: all points with  $\xi_c > 1$  and explicit CP violation

## Signal Rates at the LHC

Type II,  $H_1 = h$  - right plot: only CP-violating points

[Basler,MM,Wittbrodt '17]



\*  $\mu_F = \sigma_{\text{C2HDM}}(ggF + bbF)/\sigma_{\text{SM}}(ggF)$  and  $\mu_V = \sigma_{\text{C2HDM}}(VBF + VH)/\sigma_{\text{SM}}(VBF + VH)$

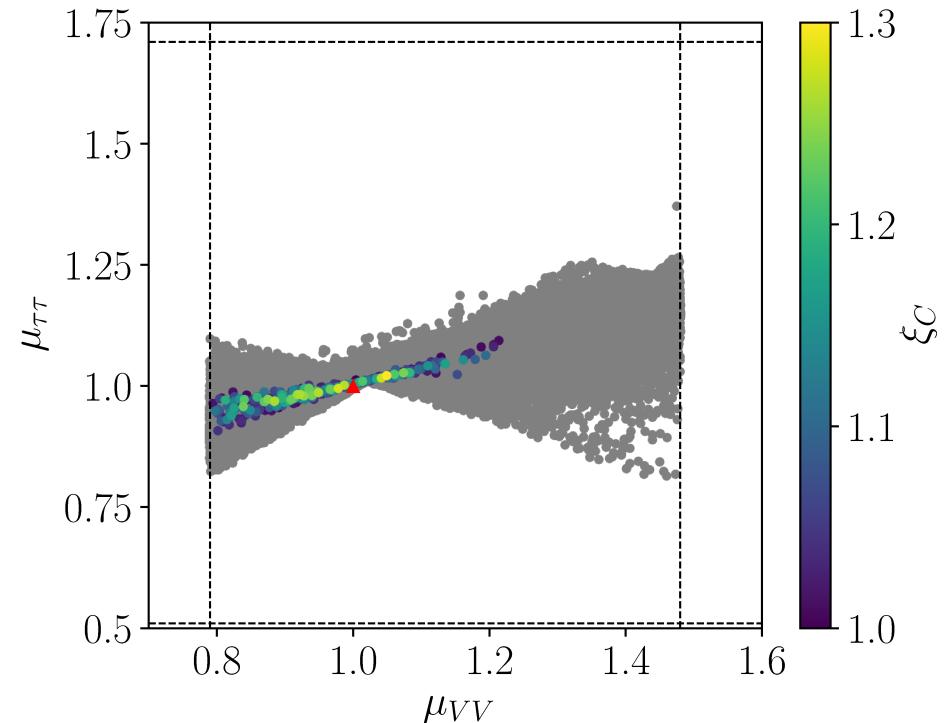
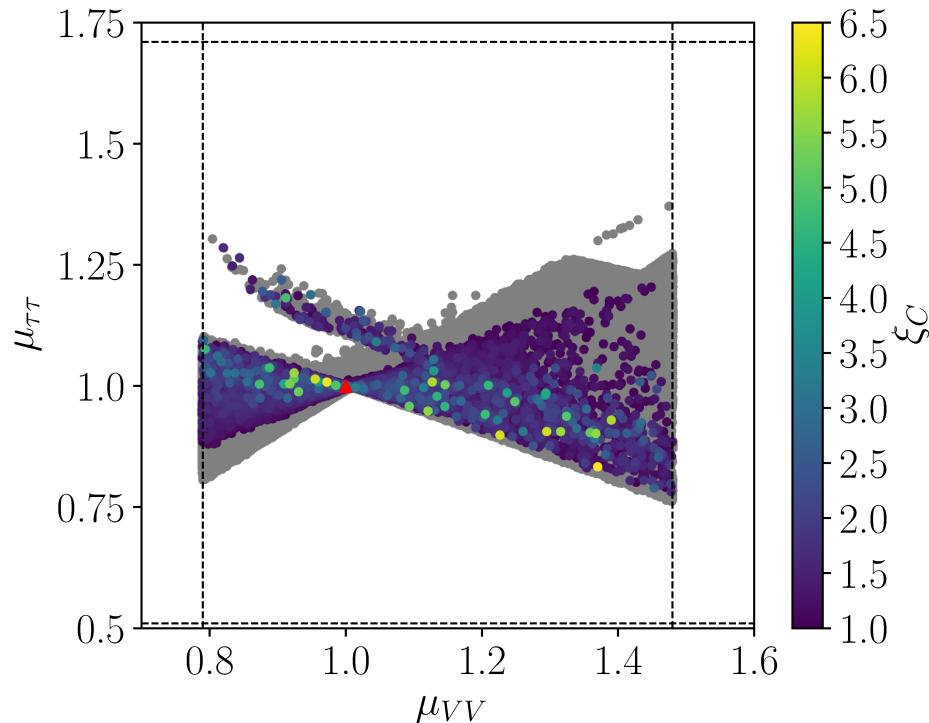
\* Signal rates: ( $H_i = h_{125}$ )

$$\mu_{xx} = \mu_F \times \frac{\text{BR}_{\text{C2HDM}}(H_i \rightarrow xx)}{\text{BR}_{\text{SM}}(H_i \rightarrow xx)}$$

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# The Different Contributions to the EDM

[Fontes,MM,Romao,Santos,Silva,Wittbrodt '17]

