

Dark matter direct detection at one loop

Michael A. Schmidt

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Planck 2018

based on

C. Hagedorn, J. Herrero-García, E. Molinaro, MS [1804.04117]

J. Herrero-García, E. Molinaro, MS [1803.05660]



THE UNIVERSITY OF
SYDNEY

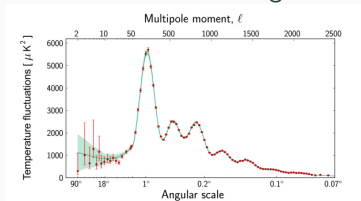


CoEPP
ARC Centre of Excellence for
Particle Physics at the Terascale

Gravitational evidence for dark matter

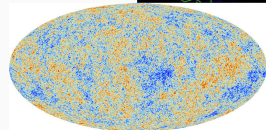
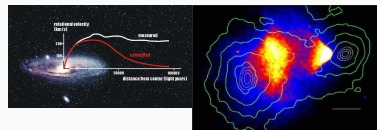
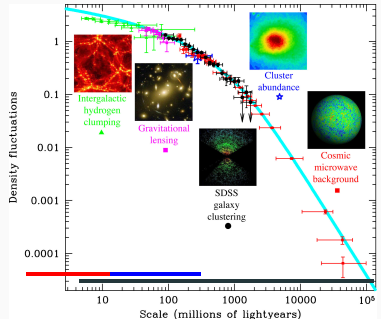
Evidences across all astrophysical scales

- Galaxy rotational curve
- Bullet cluster with grav. lensing
- Cosmic microwave background



- fit with ΛCDM
- dark matter abundance:

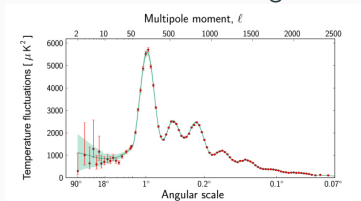
$$\Omega_{\text{CDM}} h^2 = 0.12$$



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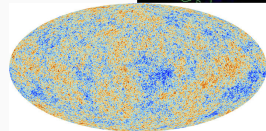
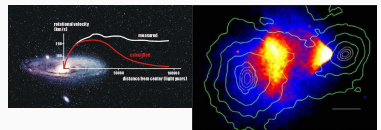
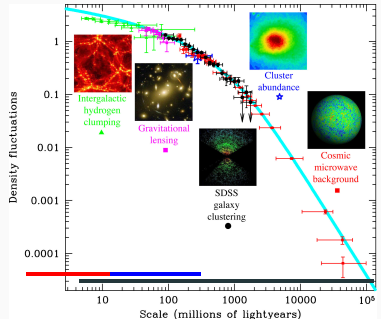


- fit with ΛCDM
- dark matter abundance:

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Popular candidate:

Weakly Interacting Massive Particles



No other clear signal in dark matter searches

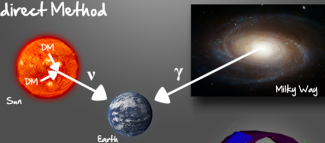
- ? dark matter mass
- ? spin and other quan. numbers
- ? interactions and strength

Dark Matter search strategies

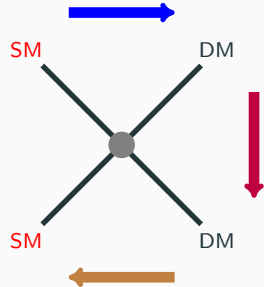
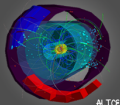
Direct Method



Indirect Method



Production at the Large Hadron Collider

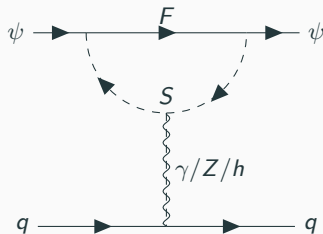
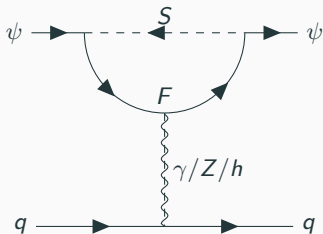


- **Direct detection:**
nuclear recoil
- **Indirect detection:**
cosmic rays
- **Collider search:**
missing transverse energy

So far **no clear evidence for DM** in direct/indirect detection or at LHC

Motivation for direct detection at loop level

- no clear evidence for DM in direct/indirect detection or at LHC
- only hints from DAMA.*
- option: DM is not directly coupled to quarks
- examples: fermionic singlet DM ψ such as bino, fermionic DM in scotogenic model, or models explaining the DAMPE result
- direct detection occurs at one loop
- next generation (liquid noble gas) experiments could probe it

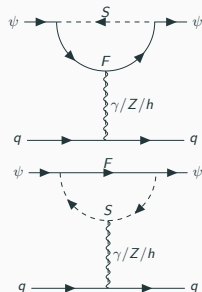


Simplified fermionic DM model

dark sector	field	$SU(3)_c$	$SU(2)_l$	$U(1)_Y$	$U(1)_{DM}$
dark matter	ψ	1	1	0	1
dark scalar	S	1	d_F	Y_F	q_S
dark fermion	F	1	d_F	Y_F	$q_S + 1$

$$\mathcal{L}_\psi = i \bar{\psi} \not{\partial} \psi - m_\psi \bar{\psi} \psi + i \bar{F} \not{D} F - m_F \bar{F} F + (D_\mu S)^\dagger D^\mu S \\ - (y_1 \overline{F_R} S \psi_L + y_2 \overline{F_L} S \psi_R + \text{h.c.}) - \lambda_{HS} v h S^\dagger S + \dots$$

- Higgs portal coupling may arise in different ways
- easy to generalise to larger dark symmetry groups



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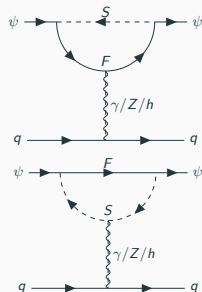
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SM fields in loop

1. $F \rightarrow L_L/e_R$: ψ or S have $L = 1$ LFV, EDM/AMMs, LNV
2. $F \rightarrow \nu_r$: ν_r and ψ or S have $L = 1$ Gonzalez-Macias, Escudero, ...
3. $S \rightarrow H$: mixing $\psi - F_0$, thus tree-level h/Z exchange



(Relevant) effective interactions for direct detection

Dirac DM

- Electric and magnetic dipoles: $\mathcal{L} = \mu_\psi \mathcal{O}_{\text{mag}} + d_\psi \mathcal{O}_{\text{edm}}$ [long-range]

$$\mathcal{O}_{\text{mag}} = \frac{e}{8\pi^2} (\bar{\psi} \sigma^{\mu\nu} \psi) F_{\mu\nu}, \quad \mathcal{O}_{\text{edm}} = \frac{e}{8\pi^2} (\bar{\psi} \sigma^{\mu\nu} i\gamma_5 \psi) F_{\mu\nu},$$

- Vector interactions from Z/γ penguins [anapole $(\bar{\psi} \gamma^\mu \psi)(\partial^\nu F_{\mu\nu}) \equiv \mathcal{O}_{VV}^q$ by eom]

$$\mathcal{O}_{VV}^q = (\bar{\psi} \gamma^\mu \psi)(\bar{q} \gamma_\mu q) \quad \mathcal{O}_{AA}^q = (\bar{\psi} \gamma^\mu \gamma_5 \psi)(\bar{q} \gamma_\mu \gamma_5 q),$$

- Scalar interactions [and gluon interaction induced by heavy quarks]

$$\mathcal{O}_{SS}^q = m_q (\bar{\psi} \psi)(\bar{q} q) \quad \mathcal{O}_g = \frac{\alpha_s}{8\pi} (\bar{\psi} \psi) G^{a\mu\nu} G_{\mu\nu}^a$$

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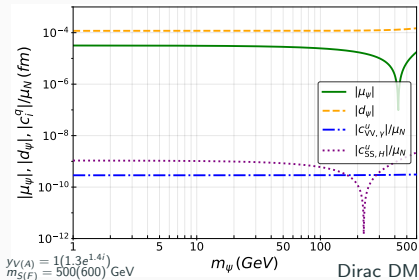
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Majorana DM

- no dipole and vector interactions
- P-violating vector interaction [momentum suppressed]

$$\mathcal{O}_{AV}^q = (\bar{\psi} \gamma^\mu \gamma_5 \psi)(\bar{q} \gamma_\mu q)$$

Dominant interactions: electric/magnetic dipole moments



for Dirac DM ψ [$m_\psi \ll m_F < m_S$]

$$\mu_\psi \approx -\frac{Q_F}{4m_S} \left(|y_V|^2 - |y_A|^2 \right) x_F \frac{1 - x_F^2 + 2 \ln x_F}{(1 - x_F^2)^2}$$

$$d_\psi \approx -\frac{Q_F}{2m_S} \text{Im}[y_V^* y_A] x_F \frac{1 - x_F^2 + 2 \ln x_F}{(1 - x_F^2)^2}$$

where

$$x_F \equiv \frac{m_F}{m_S} \quad \text{and} \quad y_{V,A} = \frac{y_2 \pm y_1}{2}$$

Dominant contribution:

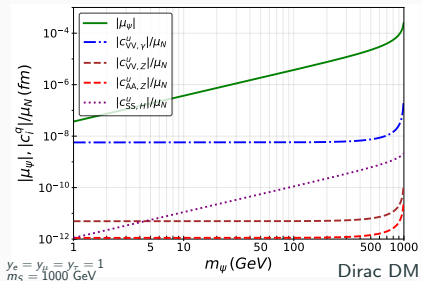
Dirac DM: electromagnetic dipole moment

Majorana DM Higgs and photon penguin

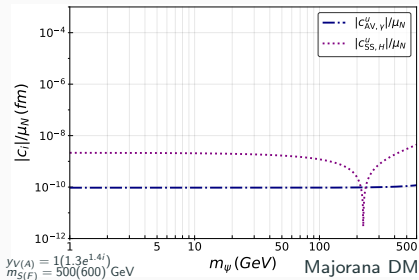
analytical expressions provided in paper
and compared to existing results

Berlin, Chang, Agrawal, Kumar, Schmidt, Kopp, Ibarra...

m_ψ dependence of μ_ψ and $c_{SS,H}^u$ due to helicity



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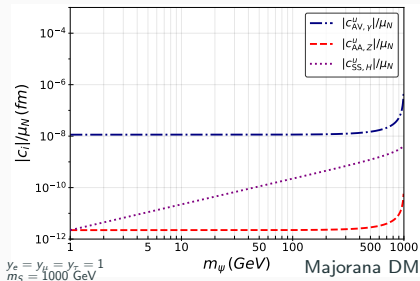
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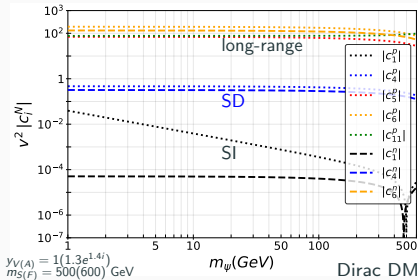
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Nucleon level (non-relativistic): vector-like fermions



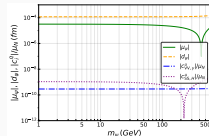
$$\mathcal{O}_1^N = I_\psi I_N$$

$$\mathcal{O}_4^N = \vec{S}_\psi \cdot \vec{S}_n$$

$$\mathcal{O}_5^N = \vec{S}_\psi \cdot \left(\vec{v}_\perp \times \frac{i\vec{q}}{m_N} \right) I_N$$

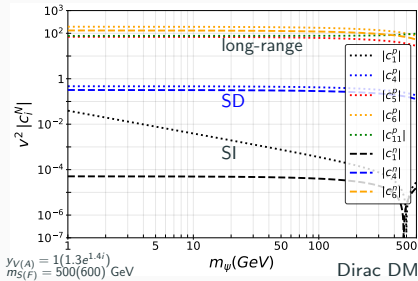
$$\mathcal{O}_6^N = \left(\vec{S}_\psi \cdot \frac{\vec{q}}{m_N} \right) \left(\vec{S}_n \cdot \frac{\vec{q}}{m_N} \right)$$

$$\mathcal{O}_{11}^N = - \left(\vec{S}_\psi \cdot \frac{\vec{q}}{m_N} \right) I_N$$



DirectDM_{1708.02678} to match to NR Wilson coefficients

Nucleon level (non-relativistic): vector-like fermions



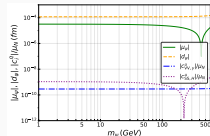
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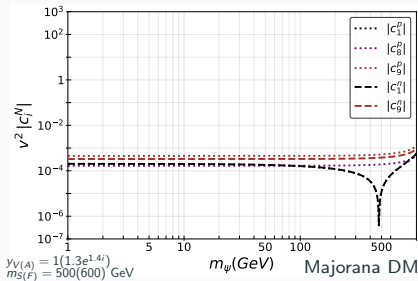
$$\mathcal{O}_5^N = \vec{S}_\psi \cdot \left(\vec{v}_\perp \times \frac{i\vec{q}}{m_N} \right) I_N$$

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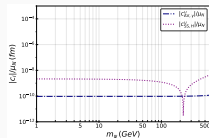
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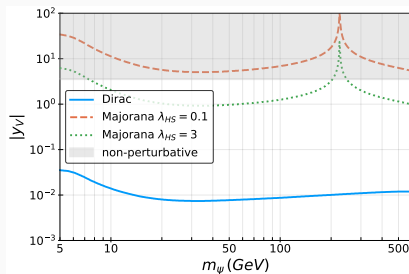
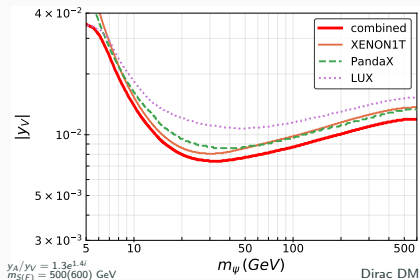
$$\mathcal{O}_8^N = \left(\vec{S}_\psi \cdot \vec{v}_\perp \right) I_N$$

$$\mathcal{O}_9^N = \vec{S}_\psi \cdot \left(\frac{i\vec{q}}{m_N} \times \vec{S}_N \right)$$



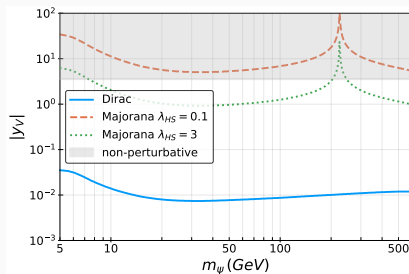
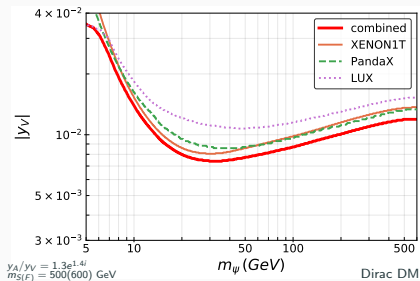
Direct detection limits

vector-like fermions we use LikeDM^{1708.04630} to calculate event rates and obtain limits

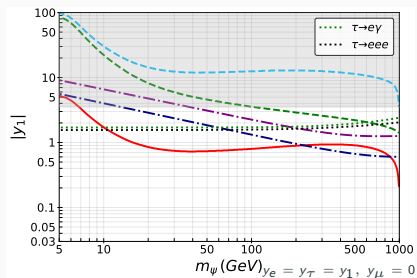
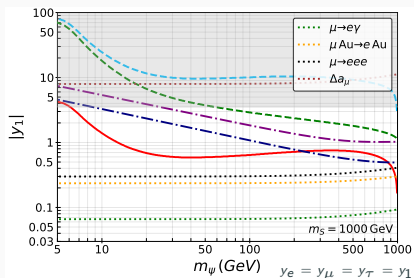


Direct detection limits

vector-like fermions we use LikeDM^{1708.04630} to calculate event rates and obtain limits



right-handed charged leptons



**connection to neutrino masses:
generalised scotogenic model**

Generalised scotogenic model with Dirac fermion DM

simple example of DD at loop level with radiative ν masses:

Dirac DM ψ , $F \equiv L_L$, $S = \Phi, \Phi'$. dark global (anomaly-free) $U(1)_{\text{DM}}$

field	$SU(3)_c$	$SU(2)_L$	$U(1)_Y$	$U(1)_{\text{DM}}$
Φ	1	2	1/2	1
Φ'	1	2	-1/2	1
ψ	1	1	0	1

just **one fermionic singlet** ψ needed. $\mathbf{y}_{\Phi^{(\prime)}}$ are 3-component vectors

$$\mathcal{L}_\psi \supset i \bar{\psi} \not{\partial} \psi - m_\psi \bar{\psi} \psi - (y_\Phi^\alpha \bar{\psi} \tilde{\Phi}^\dagger L_L^\alpha + (y_{\Phi'}^\alpha)^* \bar{\psi} \tilde{\Phi}'^\dagger \tilde{L}_L^\alpha + \text{h.c.}).$$

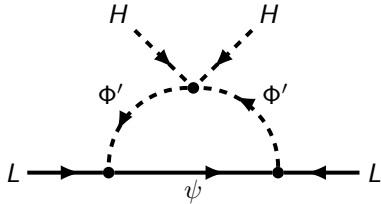
two neutral complex scalars $\eta_0^{(\prime)}$ (mixing angle θ),

two charged scalars $\eta^{(\prime)\pm}$ (no mixing)

$$V \supset \lambda_{H\Phi\Phi'} \left[(H^\dagger \tilde{\Phi}') (H^\dagger \Phi) + \text{h.c.} \right] \longrightarrow \sin 2\theta \propto \lambda_{H\Phi\Phi'}.$$

scalar DM heavily constrained by DD (mediated by Z-exchange).

Majorana neutrino mass



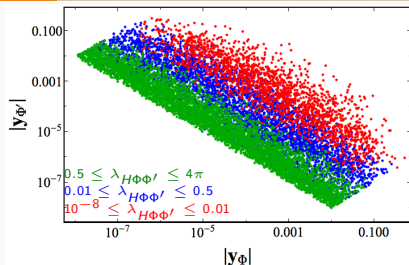
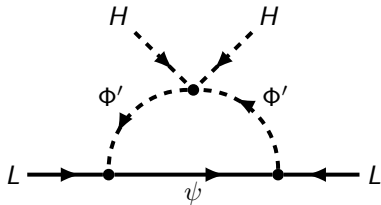
$$\mathcal{M}_\nu^{\alpha\beta} = \frac{\sin 2\theta m_\psi}{32 \pi^2} (y_\Phi^\alpha y_{\Phi'}^\beta + y_{\Phi'}^\alpha y_\Phi^\beta) \left[\frac{m_{\eta_0}^2}{m_{\eta_0}^2 - m_\psi^2} \log \frac{m_{\eta_0}^2}{m_\psi^2} - (\eta_0 \leftrightarrow \eta'_0) \right]$$

lepton number L violated by combination of $\mathbf{y}_\Phi$, $\mathbf{y}'_\Phi$, $\lambda_{H\Phi\Phi'}(\sin 2\theta)$, m_ψ

m_ν is rank 2 $\Rightarrow$ one massless neutrino

Yukawa vectors $\mathbf{y}_\Phi^{(\prime)}$ determined by low-energy data up to one parameter ζ which determines relative size of Yukawa vectors

Majorana neutrino mass



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Lepton flavour violation: $\mu \rightarrow e \gamma$ transition

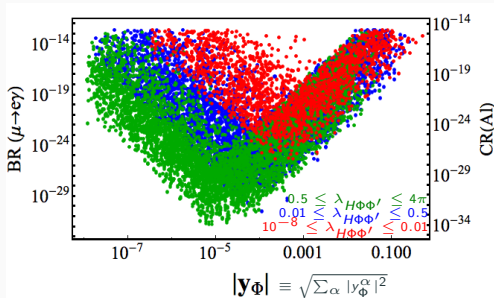
$$\text{BR}(\mu \rightarrow e \gamma) = \frac{3 \alpha_{\text{em}}}{64 \pi G_F^2} \left| \frac{y_{\Phi}^{e*} y_{\Phi}^{\mu}}{m_{\eta^{\pm}}^2} f\left(\frac{m_{\psi}^2}{m_{\eta^{\pm}}^2}\right) + \frac{y_{\Phi'}^{e*} y_{\Phi'}^{\mu}}{m_{\eta'^{\pm}}^2} f\left(\frac{m_{\psi}^2}{m_{\eta'^{\pm}}^2}\right) \right|^2$$

$$\text{CR(Al)} \simeq [0.0077, 0.011] \times \text{BR}(\mu \rightarrow e \gamma) \quad \text{dipole dominance}$$

only free parameters: masses m_{ψ} , $m_{\eta^{\pm}}$, and ζ

$$\text{NO} : \mathbf{y}_{\Phi'} = \sqrt{\frac{32\pi^2}{\sin 2\theta m_{\psi} F}} \frac{\zeta}{\sqrt{2}} (\sqrt{m_{\text{sol}}} u_2^* \pm i \sqrt{m_{\text{atm}}} u_3^*)$$

$$\mathbf{y}_{\Phi'} = \sqrt{\frac{32\pi^2}{\sin 2\theta m_{\psi} F}} \frac{1}{\zeta \sqrt{2}} (\sqrt{m_{\text{sol}}} u_2^* \mp i \sqrt{m_{\text{atm}}} u_3^*)$$



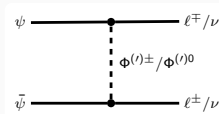
with u_i being the columns of the PMNS matrix

$$\text{using } f\left(\frac{m_{\eta^{\pm}}^2}{m_{\psi}^2}\right) \xrightarrow{m_{\eta^{\pm}} \rightarrow m_{\psi}} \frac{1}{12}$$

$$0.0003 \frac{100 \text{ GeV}}{m_{\eta'^{\pm}}} \lesssim |\zeta| \lesssim 4000 \frac{m_{\eta^{\pm}}}{100 \text{ GeV}}$$

$\tau \rightarrow \ell \gamma$ correlated with $\mu \rightarrow e \gamma$

DM s-wave annihilations into leptons and LFV



$$\xrightarrow{ch.lep.} \langle \nu \sigma_{\ell \ell} \rangle = \frac{1}{32\pi m_\psi^2} \left| y_\Phi^\alpha y_\Phi^{\beta*} \frac{m_\psi^2}{m_{\eta^\pm}^2 + m_\psi^2} - y_{\Phi'}^\alpha y_{\Phi'}^{\beta*} \frac{m_\psi^2}{m_{\eta'^\pm}^2 + m_\psi^2} \right|^2$$

only depends on masses and ζ and thus strongly constrained by LFV

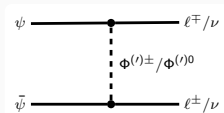
a conservative estimate

$$\frac{\sum_{\alpha,\beta} \langle \nu \sigma(\psi \bar{\psi} \rightarrow \ell_\alpha^- \ell_\beta^+, \nu_\alpha \nu_\beta) \rangle}{\langle \nu \sigma \rangle_{th}} \lesssim 2 \times 10^{-4} \left(\frac{2.2 \times 10^{-26} \text{cm}^3/\text{s}}{\langle \nu \sigma \rangle_{th}} \right) \left(\frac{m}{100 \text{ GeV}} \right)^2$$

for $m_{\eta'_0} \simeq m_{\eta^\pm} \simeq m_\psi \equiv m$. larger scalar masses lead to a further suppression. this is confirmed by numerical scan with micrOMEGAs.

caveat: MeV DM $m_\psi \simeq m_{\eta'_0} \ll m_{\eta^\pm}$ [Boehm,Farzan,Hambye,Palomares-Ruiz,Pascoli \[hep-ph/0612228\]](#)

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$$\xrightarrow{\text{ch. lep.}} \langle \nu \sigma \ell \ell \rangle = \frac{1}{32\pi m_\psi^2} \left| y_\Phi^\alpha y_\Phi^{\beta*} \frac{m_\psi^2}{m_{\eta^\pm}^2 + m_\psi^2} - y_{\Phi'}^\alpha y_{\Phi'}^{\beta*} \frac{m_\psi^2}{m_{\eta'^\pm}^2 + m_\psi^2} \right|^2$$

only depends on masses and ζ and thus strongly constrained by LFV

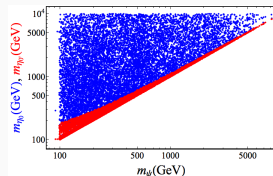
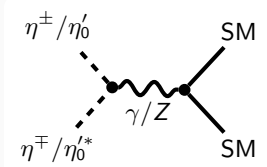
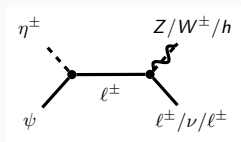
a conservative estimate

$$\frac{\sum_{\alpha,\beta} \langle \nu \sigma (\psi \bar{\psi} \rightarrow \ell_\alpha^- \ell_\beta^+, \nu_\alpha \nu_\beta) \rangle}{\langle \nu \sigma \rangle_{\text{th}}} \lesssim 2 \times 10^{-4} \left(\frac{2.2 \times 10^{-26} \text{cm}^3/\text{s}}{\langle \nu \sigma \rangle_{\text{th}}} \right) \left(\frac{m}{100 \text{ GeV}} \right)^2$$

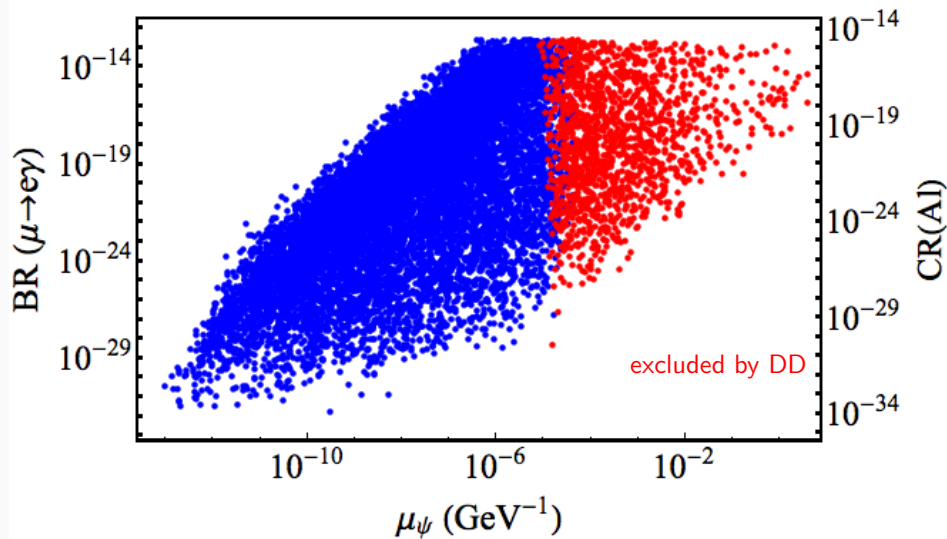
for $m_{\eta'_0} \simeq m_{\eta^\pm} \simeq m_\psi \equiv m$. larger scalar masses lead to a further suppression. this is confirmed by numerical scan with micrOMEGAs.

caveat: MeV DM $m_\psi \simeq m_{\eta'_0} \ll m_{\eta^\pm}$ [Boehm,Farzan,Hambye,Palomares-Ruiz,Pascoli \[hep-ph/0612228\]](#)

annihilations into leptons too small: need coannihilation with scalars $\eta^{(\prime)}$



Complementarity of LFV and DM direct detection



Conclusions

Conclusions

DM may not couple directly to quarks

DM - nucleus scattering only at 1-loop order (or higher)

discussion of simplified fermionic DM model

magnetic and electric dipole moment dominate

Higgs penguins are important for Majorana DM

generalised scotogenic model with Dirac fermion

fermionic DM requires coannihilation

interplay between LFV and direct detection

Review of radiative neutrino mass models

Different classifications

Survey of models in literature

Details for selected examples



Y. Cai, J. Herrero-Garcia, M.S. A. Vicente, R. Volkas [1706.08524]

REVIEW
published: 04 December 2017
doi: 10.3389/fphy.2017.00083



From the Trees to the Forest: A Review of Radiative Neutrino Mass Models

Yi Cai^{1,2}, Juan Herrero Garcia^{3*}, Michael A. Schmidt^{4*}, Avelino Vicente⁵ and
Raymond R. Volkas²

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Excellence for Particle Physics at the Terascale, School of Physics, The University of Sydney, Sydney, NSW, Australia, ⁵ Instituto de Física Corpuscular (CSIC)-Universitat de València, Valencia, Spain

A plausible explanation for the lightness of neutrino masses is that neutrinos
are loops, with their mass (typically Majorana) being generated from
fermion loops. The new couplings, together with the suppression of
the new couplings, imply that the new degrees of freedom cannot be too
heavy (TeV scale). Therefore, in these models, there are new particles
tested using different searches, making them interesting for
neutrinos). The new particles (neutrinos), which are not
space from

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Volante, R. Volkas [1706.08524]

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Thank you!

Y. Cai, J. Herrero
frontiers
in Physics

From the Tree
A Review of Radiative
Models

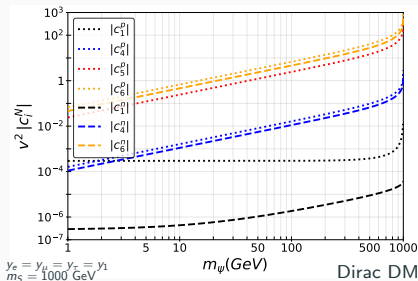
Yi Cai^{1,2}, Juan Herrero
Raymond R. Volkas²

¹ School of Physics, Sun Yat-sen University, Guangzhou, China, ² ARC Centre
Terrestrial Physics, School of Physics, The University of Melbourne, Melbourne, VIC, Australia
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A plausible explanation for the lightness of neutrino masses is that neutrinos
at tree level, with their mass (typically Majorana) being generated from
are loops. The new couplings, together with the suppression of
imply that the new degrees of freedom cannot be too heavy
tested using different searches, making the new particles
in particular, the new particles (neutrinos), which are
mixings. The main space for

Backup slides

Nucleon level (non-relativistic): leptons



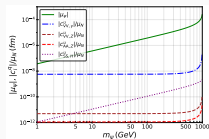
$$\mathcal{O}_1^N = I_\psi I_N$$

$$\mathcal{O}_4^N = \vec{S}_\psi \cdot \vec{S}_N$$

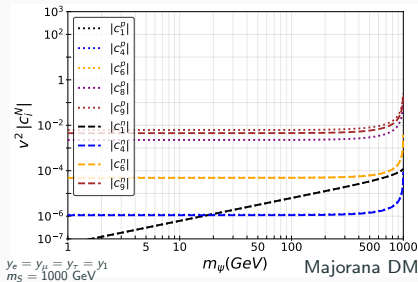
$$\mathcal{O}_5^N = \vec{S}_\psi \cdot \left(\vec{v}_\perp \times \frac{i\vec{q}}{m_N} \right) I_N$$

$$\mathcal{O}_6^N = \left(\vec{S}_\psi \cdot \frac{\vec{q}}{m_N} \right) \left(\vec{S}_N \cdot \frac{\vec{q}}{m_N} \right)$$

$$\mathcal{O}_{11}^N = - \left(\vec{S}_\psi \cdot \frac{\vec{q}}{m_N} \right) I_N$$



DirectDM_{1708.02678} to match to NR Wilson coefficients



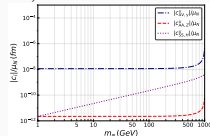
$$\mathcal{O}_1^N = I_\psi I_N$$

$$\mathcal{O}_4^N = \vec{S}_\psi \cdot \vec{S}_N$$

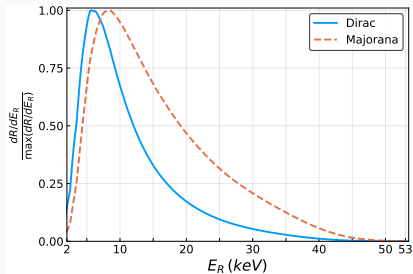
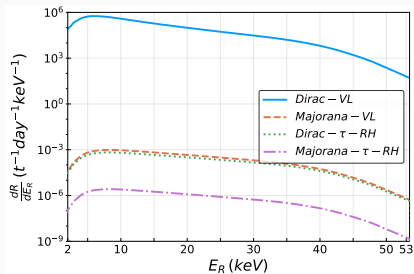
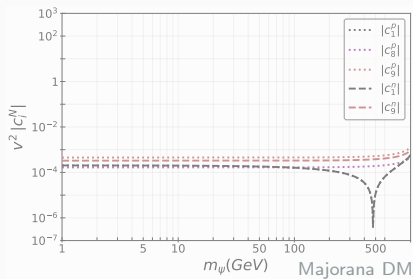
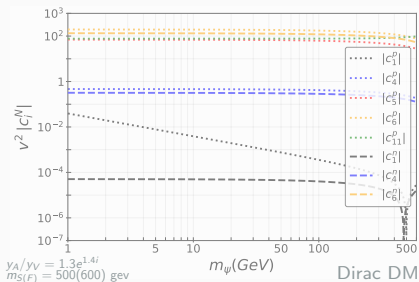
$$\mathcal{O}_6^N = \left(\vec{S}_\psi \cdot \frac{\vec{q}}{m_N} \right) \left(\vec{S}_N \cdot \frac{\vec{q}}{m_N} \right)$$

$$\mathcal{O}_8^N = \left(\vec{S}_\psi \cdot \vec{v}_\perp \right) I_N$$

$$\mathcal{O}_9^N = \vec{S}_\psi \cdot \left(\frac{i\vec{q}}{m_N} \times \vec{S}_N \right)$$



Differential event rates

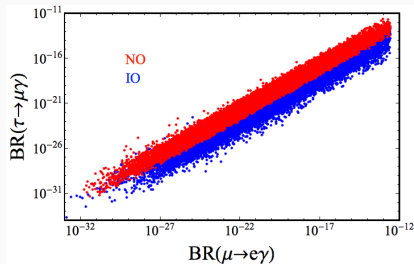
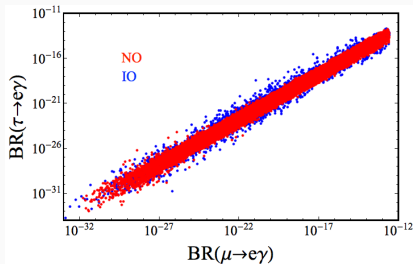


LikeDM_{1708.04630} to calculate event rates and obtain limits

Correlation between different LFV rates

$$\text{NO} : \frac{\text{BR}(\tau \rightarrow e \gamma)}{\text{BR}(\mu \rightarrow e \gamma)} \approx 0.2 \quad \text{and} \quad \frac{\text{BR}(\tau \rightarrow \mu \gamma)}{\text{BR}(\mu \rightarrow e \gamma)} \approx 5$$

$$\text{IO} : \frac{\text{BR}(\tau \rightarrow e \gamma)}{\text{BR}(\mu \rightarrow e \gamma)} \approx \frac{\text{BR}(\tau \rightarrow \mu \gamma)}{\text{BR}(\mu \rightarrow e \gamma)} \approx 0.2 ,$$



Papers on radiative neutrino mass generation

