

Third Family Quark-Lepton Unification at the TeV Scale

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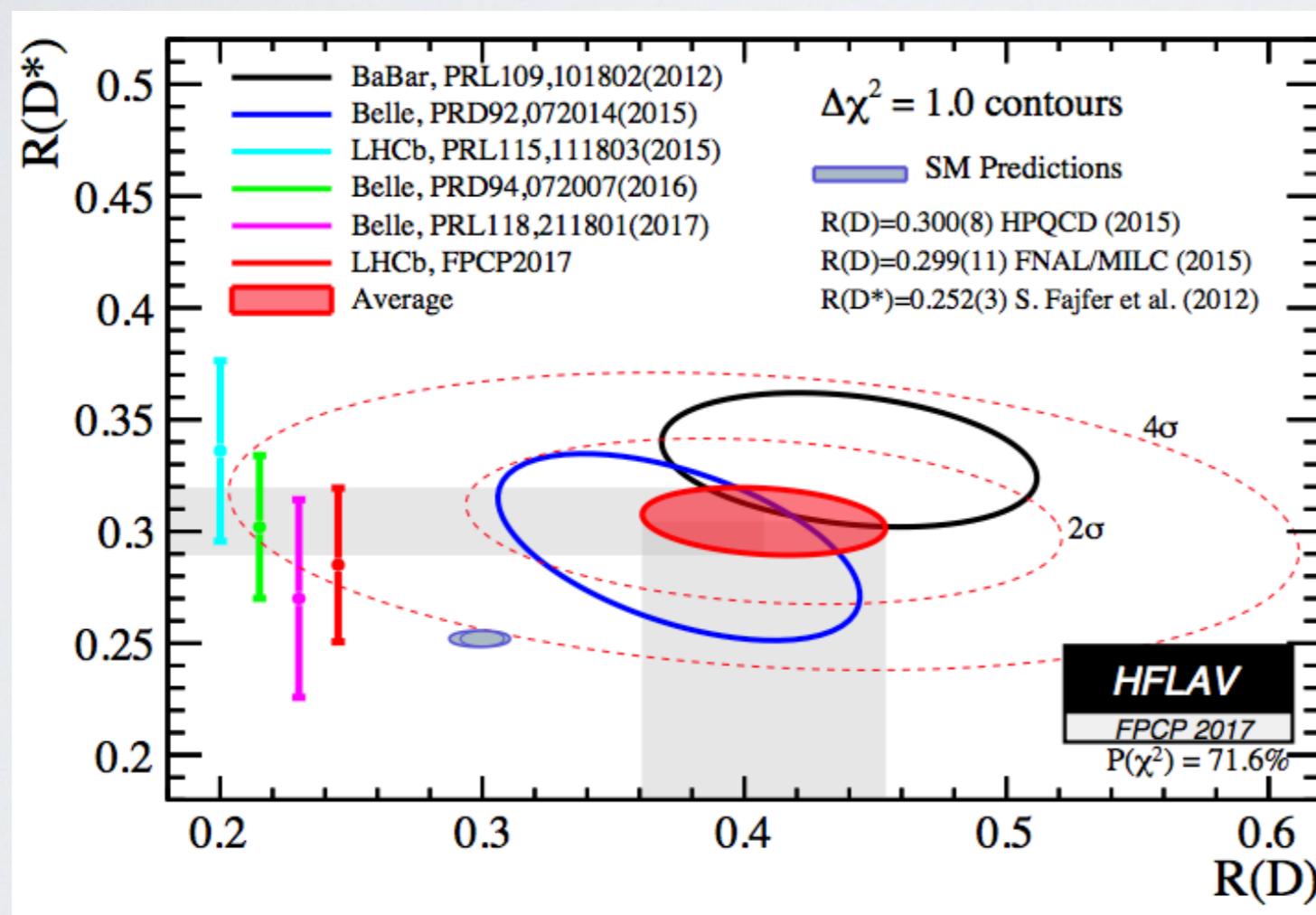
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arXiv:1802.04274

$$b \rightarrow c \ell \bar{\nu}$$

$$R(D^{(*)}) = \frac{\text{Br}(B \rightarrow D^{(*)} \tau \nu_\tau)}{\text{Br}(B \rightarrow D^{(*)} \ell \nu_\ell)}$$

- Charged current B meson decay. Deviation from τ/ℓ universality.

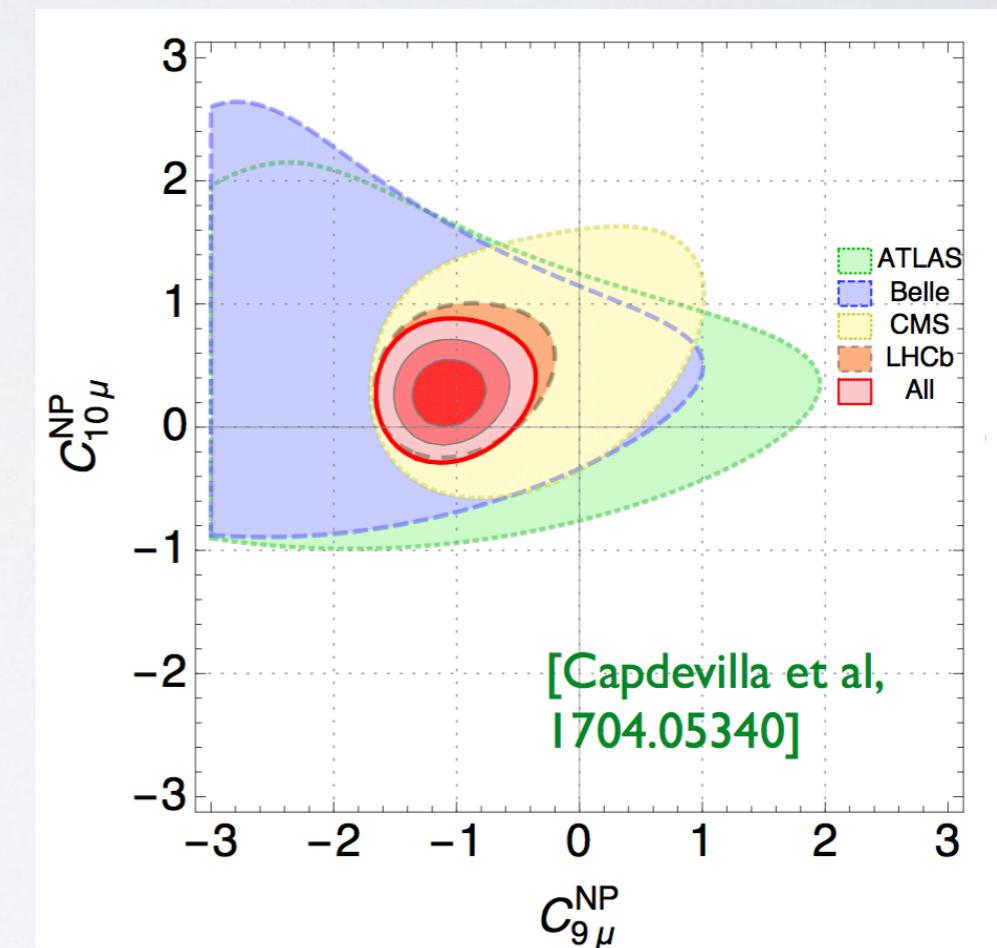
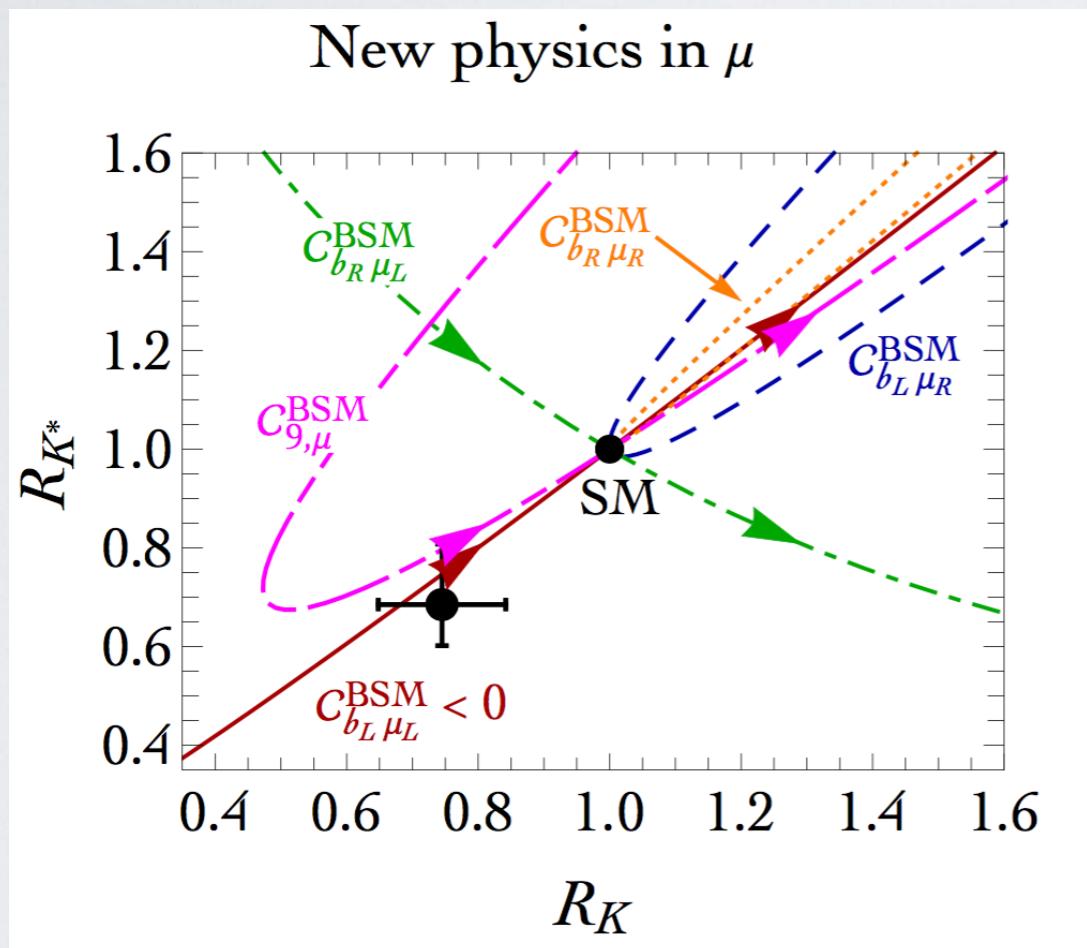


- Measurement by BaBar, Belle, and LHCb.
- Combined 4 σ excess over the SM prediction.

$$b \rightarrow s \bar{\ell} \ell$$

$$R(K^{(*)}) = \frac{\text{Br}(B \rightarrow K^{(*)}\mu^+\mu^-)}{\text{Br}(B \rightarrow K^{(*)}e^+e^-)}$$

- **Neutral current** B meson decay. Deviation from μ/e universality.
Measurement by LHCb, new physics fit preferred at 4σ .



$$\mathcal{O}_9^\ell = (\bar{s}\gamma_\mu P_L b)(\bar{\ell}\gamma^\mu \ell)$$

$$\mathcal{O}_{10}^\ell = (\bar{s}\gamma_\mu P_L b)(\bar{\ell}\gamma^\mu \gamma_5 \ell)$$

Combined Explanation via New Physics?

- LFU violation in both anomalies.
- Both anomalies involve a bottom quark decaying to a 2nd generation quark.
- Data favors mainly left-handed effective interactions for both anomalies.

$$\mathcal{L}_{\text{eff}} = -\frac{1}{v^2} \lambda_{ij}^q \lambda_{\alpha\beta}^\ell \left[C_T (\bar{Q}_L^i \gamma_\mu \sigma^a Q_L^j)(\bar{L}_L^\alpha \gamma^\mu \sigma^a L_L^\beta) + C_S (\bar{Q}_L^i \gamma_\mu Q_L^j)(\bar{L}_L^\alpha \gamma^\mu L_L^\beta) \right]$$

$$\lambda^q \sim \begin{pmatrix} \epsilon & \epsilon & \epsilon \\ \epsilon & V_q^2 & V_q \\ \epsilon & V_q & 1 \end{pmatrix} \quad \lambda^\ell \sim \begin{pmatrix} \epsilon & \epsilon & \epsilon \\ \epsilon & V_\ell^2 & V_\ell \\ \epsilon & V_\ell & 1 \end{pmatrix} \quad Q_L^i \sim \begin{pmatrix} V_{ki}^* u_L^k \\ d_L^i \end{pmatrix}$$

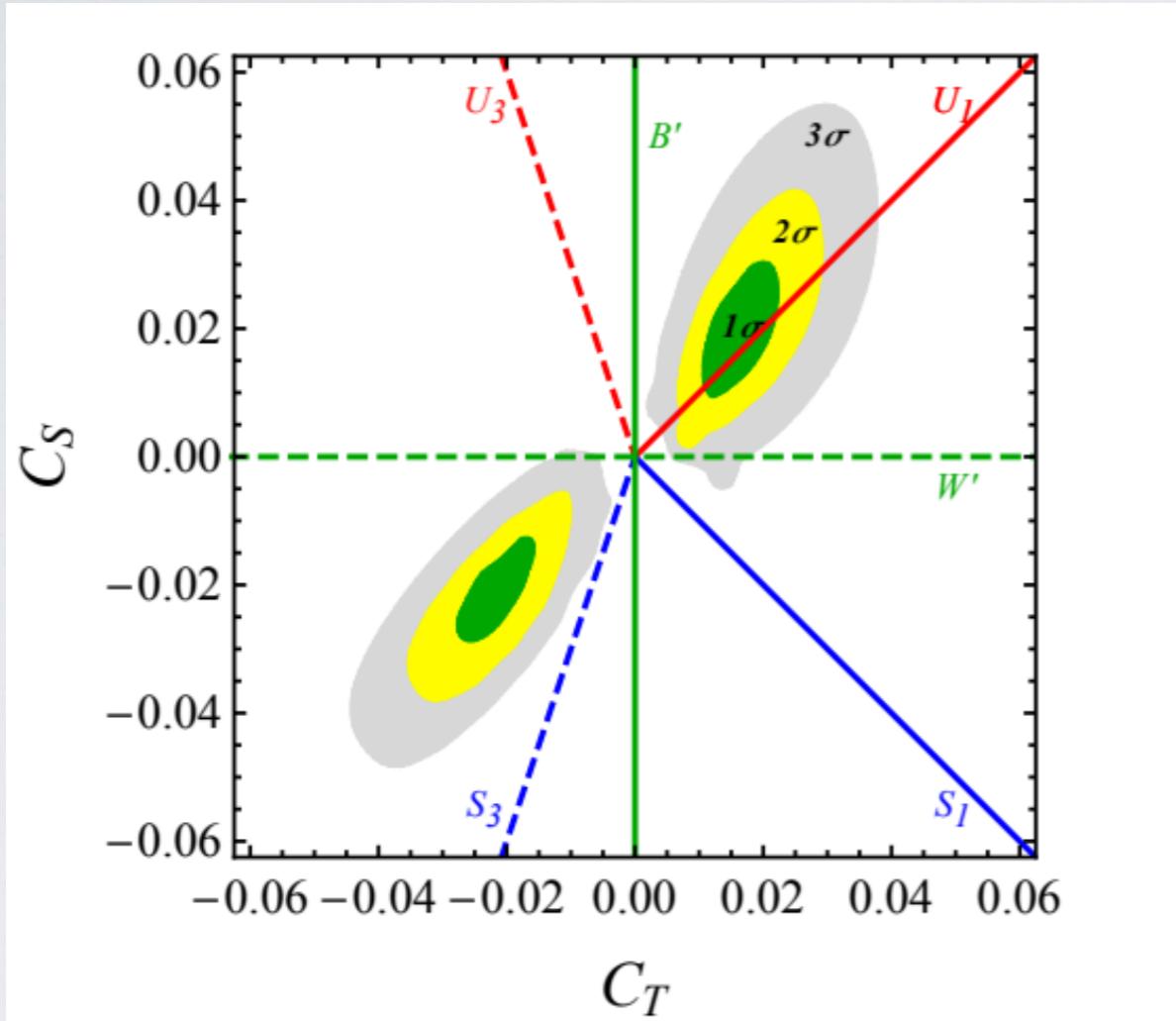
$$|V_q| \sim |V_{cb}|$$

$$|V_\ell^2| \sim 10^{-2}$$

Competes with V_{cb}
suppressed tree level
SM process

Competes with 1-loop
SM process

Single Mediator Model



Vectors

$$W'^\mu = (1, \mathbf{3}, 0)$$

$$Z'^\mu = (1, \mathbf{1}, 0)$$

Scalar Leptoquarks

$$S_1^\mu = (\bar{\mathbf{3}}, \mathbf{1}, 1/3)$$

$$S_3^\mu = (\bar{\mathbf{3}}, \mathbf{3}, 1/3)$$

Vector Leptoquarks

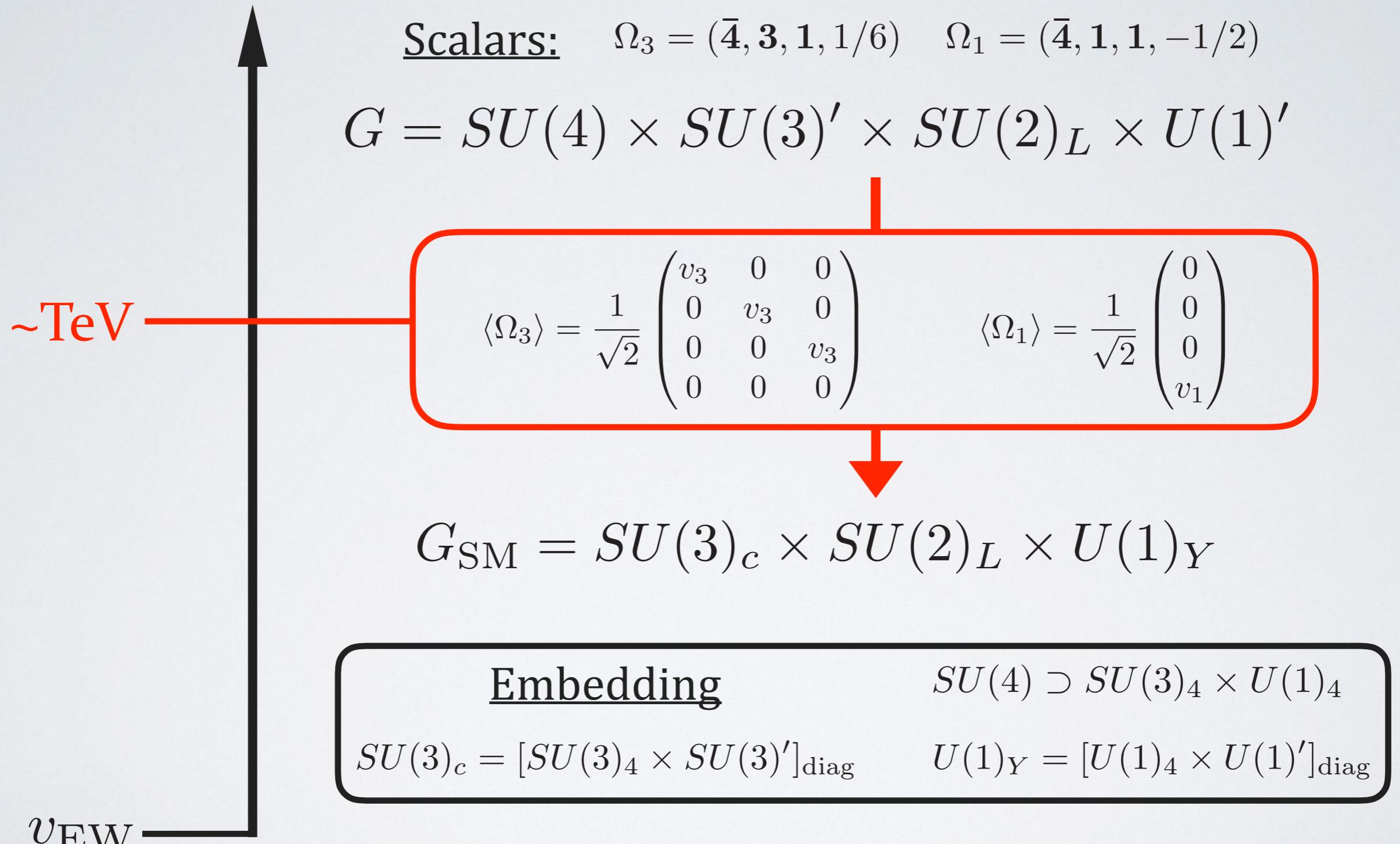
$$U_1^\mu = (\mathbf{3}, \mathbf{1}, 2/3)$$

$$U_3^\mu = (\mathbf{3}, \mathbf{3}, 2/3)$$

*Stands out as the best option
for a single mediator model.*



Extended Gauge Group: The “4321” Model



Extended Gauge Group: The “4321” Model

$$G = SU(4) \times SU(3)' \times SU(2)_L \times U(1)'$$

 ~TeV

$$G_{\text{SM}} = SU(3)_c \times SU(2)_L \times U(1)_Y$$

15 Broken Generators

$$G' = (8, 1, 0)$$

$$Z' = (1, 1, 0)$$

✓ $U_1 = (3, 1, 2/3)$

New SM Fermion Embedding

- 1st and 2nd family SM fermions charged under “321” and are not coupled directly to the LQ.
- 3rd family SM fermions charged under “421” and are coupled directly to the LQ.

“4321” with Family Dependent Gauge Charges

- 1st and 2nd family quarks and leptons charged under “321” but are SU(4) singlets. Here, $i = 1, 2$.
- Third family quarks and leptons are embedded in fundamentals of SU(4).

Dominantly Light Family SM Fermions						
	Gauge				Global	
Field	$SU(4)$	$SU(3)'$	$SU(2)_L$	$U(1)'$	$U(1)_{B'}$	$U(1)_{L'}$
$q_L'^i$	1	3	2	1/6	1/3	0
$u_R'^i$	1	3	1	2/3	1/3	0
$d_R'^i$	1	3	1	-1/3	1/3	0
$\ell_L'^i$	1	1	2	-1/2	0	1
$e_R'^i$	1	1	1	-1	0	1

Dominantly Third Family SM Fermions						
	Gauge				Global	
Field	$SU(4)$	$SU(3)'$	$SU(2)_L$	$U(1)'$	$U(1)_{B'}$	$U(1)_{L'}$
ψ_L	4	1	2	0	1/4	1/4
ψ_R^u	4	1	1	1/2	1/4	1/4
ψ_R^d	4	1	1	-1/2	1/4	1/4

$$\psi_L = \begin{pmatrix} q_L'^3 \\ \ell_L'^3 \end{pmatrix}$$

$$\psi_R^u = \begin{pmatrix} u_R'^3 \\ \nu_R'^3 \end{pmatrix}$$

$$\psi_R^d = \begin{pmatrix} d_R'^3 \\ e_R'^3 \end{pmatrix}$$

First Attempt at a Lagrangian

- The Lagrangian for the light families looks just like the SM.

$$\mathcal{L}_{12} = -\bar{q}'_L Y_u \tilde{H} u'_R - \bar{q}'_L Y_d H d'_R - \bar{\ell}'_L Y_\nu \tilde{H} \nu'_R - \bar{\ell}'_L Y_e H e'_R + \text{h.c.},$$

*All 1st and 2nd family Yukawas are small

→ Approximate Flavor Symmetry: $U(2)_q^3 \times U(2)_\ell^3$

- The 3rd family Lagrangian contains just the following terms

$$\mathcal{L}_3 = -y_H^u \bar{\psi}_L \tilde{H} \psi_R^u - y_H^d \bar{\psi}_L H \psi_R^d + \text{h.c.}$$



Predicts the same mass for the top quark and tau neutrino.



Predicts the same mass for the bottom quark and tau lepton.



- Light family - 3rd family mixing not allowed without new fields.

Third Family Quark and Lepton Masses

- Can add another Higgs to split the 3rd family quark and lepton masses.

$$\langle \Phi_0^{15} \rangle \equiv v_\Phi / \sqrt{2}$$

$$y_H^u, y_H^d, y_\Phi^u, y_\Phi^d$$

Scalar Fields						
Field	Gauge				Global	
	SU(4)	SU(3)'	SU(2) _L	U(1)'	U(1) _{B'}	U(1) _{L'}
H	1	1	2	1/2	0	0
Φ	15	1	2	1/2	0	0
Ω_3	$\bar{4}$	3	1	1/6	1/12	-1/4
Ω_1	$\bar{4}$	1	1	-1/2	-1/4	3/4

Up-type masses

$$m'_t = \frac{v_{\text{EW}}}{\sqrt{2}} \left(y_H^u \cos \beta + \frac{1}{2\sqrt{6}} y_\Phi^u \sin \beta \right) \checkmark$$

$$m'_{\nu_\tau} = \frac{v_{\text{EW}}}{\sqrt{2}} \left(y_H^u \cos \beta - \frac{3}{2\sqrt{6}} y_\Phi^u \sin \beta \right) \times$$

Requires Tuning: $\frac{\text{meV}}{v_{\text{EW}}} \sim 10^{-14}$

Down-type masses

$$m'_b = \frac{v_{\text{EW}}}{\sqrt{2}} \left(y_H^d \cos \beta + \frac{1}{2\sqrt{6}} y_\Phi^d \sin \beta \right) \checkmark$$

$$m'_\tau = \frac{v_{\text{EW}}}{\sqrt{2}} \left(y_H^d \cos \beta - \frac{3}{2\sqrt{6}} y_\Phi^d \sin \beta \right) \checkmark$$

Bottom/Tau Splitting: $\frac{m_b}{m_\tau} \sim 2$

*Generic problem with low-scale QL-unification.
Resolved in our model- later in the talk.

$$v_{\text{EW}}^2 = v_H^2 + v_\Phi^2$$

$$\tan \beta = v_\Phi / v_H$$

Light with Third Family Mixing

- Light with 3rd family mixing is required, e.g. must generate the CKM.
- A single new vector-like fermion with the same quantum numbers as ψ_L can do the job. Contains vector-like partners to SM doublets.

New Vector-like Fermions						
	Gauge				Global	
Field	$SU(4)$	$SU(3)'$	$SU(2)_L$	$U(1)'$	$U(1)_{B'}$	$U(1)_{L'}$
$\chi_{L,R}$	4	1	2	0	1/4	1/4

↗

$$\chi_{L,R} = \begin{pmatrix} Q'_{L,R} \\ L'_{L,R} \end{pmatrix}$$

$$\Psi_L = \begin{pmatrix} \psi_L \\ \chi_L \end{pmatrix} \quad \mathbf{y}_H^{u,d} \equiv \begin{pmatrix} y_H^{u,d} \\ \lambda_H^{u,d} \end{pmatrix}$$

$$\begin{aligned} \mathcal{L}_3 \rightarrow \mathcal{L}_{3\chi} = & - \bar{\Psi}_L \mathbf{y}_H^u \tilde{H} \psi_R^u - \bar{\Psi}_L \mathbf{y}_H^d H \psi_R^d + (H \rightarrow \Phi) \\ & - \bar{q}'_L \lambda_q \Omega_3^T \chi_R - \bar{\ell}'_L \lambda_\ell \Omega_1^T \chi_R - \bar{\Psi}_L \mathbf{m} \chi_R + \text{h.c.} \end{aligned}$$

Higher Dimensional Operators

- When the new vector-like fermion is integrated out, the following operators are generated:

Dimension-5

✓ Light with 3rd family quark and lepton mixings generated.

$$\begin{aligned}\mathcal{L}_{d5} = & \frac{\lambda_q}{m_\chi} \left(\lambda_H^u \bar{q}'_L \Omega_3^T \tilde{H} \psi_R^u + \lambda_H^d \bar{q}'_L \Omega_3^T H \psi_R^d \right) \\ & + \frac{\lambda_\ell}{m_\chi} \left(\lambda_H^u \bar{\ell}'_L \Omega_1^T \tilde{H} \psi_R^u + \lambda_H^d \bar{\ell}'_L \Omega_1^T H \psi_R^d \right) + (H \rightarrow \Phi) + \text{h.c.}\end{aligned}$$

Dimension-6

✓ Suppressed leptoquark coupling to the light families generated.

$$\mathcal{L}_{d6} \supset \frac{i}{m_\chi^2} \bar{q}'_L \lambda_q \Omega_3^T \not{D} \Omega_1^* \lambda_\ell^\dagger \ell'_L \longrightarrow \frac{g_4}{\sqrt{2}} \left(\frac{v_1 v_3}{m_\chi^2} \right) \bar{q}'_L \lambda_q \gamma^\mu U_{1\mu} \lambda_\ell^\dagger \ell'_L ,$$

Return to the Neutrino Mass Problem

Up-type Dirac masses

$$m'_t = \frac{v_{\text{EW}}}{\sqrt{2}} \left(y_H^u \cos \beta + \frac{1}{2\sqrt{6}} y_\Phi^u \sin \beta \right) \quad \checkmark$$
$$m'_{\nu_\tau} = \frac{v_{\text{EW}}}{\sqrt{2}} \left(y_H^u \cos \beta - \frac{3}{2\sqrt{6}} y_\Phi^u \sin \beta \right) \quad \times \rightarrow \boxed{\text{Requires Tuning: } \frac{\text{meV}}{v_{\text{EW}}} \sim 10^{-14}}$$

Solution

- Accept a natural tau neutrino Dirac mass of order the electroweak scale.
- Add singlet fermions such that the inverse seesaw mechanism (ISS) can be implemented to obtain the correct neutrino masses.

Neutrino Lagrangian and Mass Matrix

Right Handed Singlet Fermions						
Field	Gauge				Global	
	$SU(4)$	$SU(3)'$	$SU(2)_L$	$U(1)'$	$U(1)_{B'}$	$U(1)_{L'}$
ν'_R^i	1	1	1	0	0	1
S_R^a	1	1	1	0	0	-1

Lepton Number Conserving Lepton Number Violating

$$\mathcal{L}_S = -\Omega_1^T \overline{S_R^c} \lambda_R \psi_R^u - \overline{S_R^c} M_R \nu'_R - \frac{1}{2} \overline{S_R^c} \mu_S S_R + \text{h.c.}$$

- After EWSB, the complete neutrino mass matrix takes the form:

$$\mathcal{M}_\nu = \begin{pmatrix} 0 & M_\nu^D & 0 \\ (M_\nu^D)^T & 0 & \widetilde{M}_R^T \\ 0 & \widetilde{M}_R & \mu_S \end{pmatrix}$$

$$\widetilde{M}_R = (M_R \quad \frac{v_1}{\sqrt{2}} \lambda_R)$$

SU(4) breaking VEV: $\sim \text{TeV}$

Inverse Seesaw Mechanism

$$\mathcal{M}_\nu = \begin{pmatrix} 0 & M_\nu^D & 0 \\ (M_\nu^D)^T & 0 & \widetilde{M}_R^T \\ 0 & \widetilde{M}_R & \mu_S \end{pmatrix} \quad M_\nu^D = \begin{pmatrix} \frac{v_H}{\sqrt{2}} U Y_\nu^{\text{diag}} & -f_\nu \lambda_\ell \\ 0 & m'_{\nu_\tau} \end{pmatrix}$$

- ISS Hierarchy $\mu_S \ll M_\nu^D < \widetilde{M}_R$ gives 3 light Majorana neutrinos.

$$M_{\text{light}} \approx M_\nu^D \widetilde{M}_R^{-1} \mu_S (\widetilde{M}_R^T)^{-1} (M_\nu^D)^T$$

- Parametrically, if $m_D \sim \text{GeV}$, $m_R \sim \text{TeV}$, works for $\mu_S \sim \text{keV}$.

$$m_\nu \sim \left(\frac{m_D}{m_R} \right)^2 \mu_S$$

PMNS Non-Unitarity and B-Anomalies

- 3x3 light neutrino mixing matrix is now non-unitary:

$$N = \left[\mathbf{1} - \frac{1}{2} \Theta \Theta^\dagger \right] U_{\text{PMNS}}, \quad \Theta \approx M_\nu^D \widetilde{M}_R^{-1}$$

- PMNS Non-Unitarity probed by $\epsilon = 1 - NN^\dagger \approx \Theta \Theta^\dagger$, so parametrically there is a contribution at least as large as:

$$\epsilon \sim \frac{m_D^2}{m_R^2} \sim \frac{m_D^2}{v_1^2 |\lambda_R|^2}$$

- Meanwhile,

$$\Delta R_D^{\tau\ell} \approx 2.2 \Delta R_{D^*}^{\tau\ell} \approx \frac{5 v_{\text{EW}}^2}{v_1^2 + v_3^2}$$

LHC Direct Search
Coloron Bound:
 $v_3 \gtrsim 1 \text{ TeV}$

$$\implies v_1 \lesssim 1 \text{ TeV},$$

$$\epsilon \sim 10^{-2} \left(\frac{m_D}{100 \text{ GeV}} \right)^2 \left(\frac{1 \text{ TeV}}{v_1 |\lambda_R|} \right)^2$$

*Sizable effect in B-physics
implies sizable PMNS
unitarity violation.*

Conclusions

- We present a model based on the “4321” extended gauge group with family dependent gauge charges.
- Gauge vector leptoquark $U_1 = (\mathbf{3}, \mathbf{1}, 2/3)$ coupled dominantly to the 3rd family offers a single mediator explanation for B-anomalies.
- Neutrino mass problem is naturally resolved in our model by implementing the inverse seesaw mechanism.
- PMNS unitarity violation is controlled by the $SU(4)$ breaking scale, which also controls the size of the effect in $\Delta R(D^{(*)})$.

Backup Slides

Gauge Boson Masses

$$m_{U_1} = \frac{1}{2} g_4 \sqrt{v_1^2 + v_3^2},$$

$$m_{g'} = \frac{1}{\sqrt{2}} v_3 \sqrt{g_4^2 + g_3^2},$$

$$m_{Z'} = \frac{1}{2} \sqrt{\frac{3}{2}} \sqrt{g_4^2 + \frac{2}{3} g_1^2} \sqrt{v_1^2 + \frac{1}{3} v_3^2}.$$

- Gauge boson spectrum cannot be split very much. To avoid direct search bounds we need $g_4 > g_3 > g_1$ and $v_3 > v_1$, then the approximate relation is

$$m_{g'} \sim \sqrt{2} m_{U_1} \qquad \qquad m_{Z'} \sim \frac{1}{\sqrt{2}} m_{U_1}$$

$$m_{Z'} \sim 1.1 \text{ TeV}, \quad m_{U_1} \sim 1.6 \text{ TeV}, \quad m_{g'} \sim 2.3 \text{ TeV}$$

Gauge Boson Couplings

$$\mathbf{Q}'_L = (q'^i_L, q'^3_L, Q'_L)^T$$

- Coloron Couplings

$$\mathcal{L}_{g'} \supset g_s \left(\bar{\mathbf{Q}}'_L C_{g'}^L \gamma^\mu T^a \mathbf{Q}'_L \right) g_\mu'^a$$

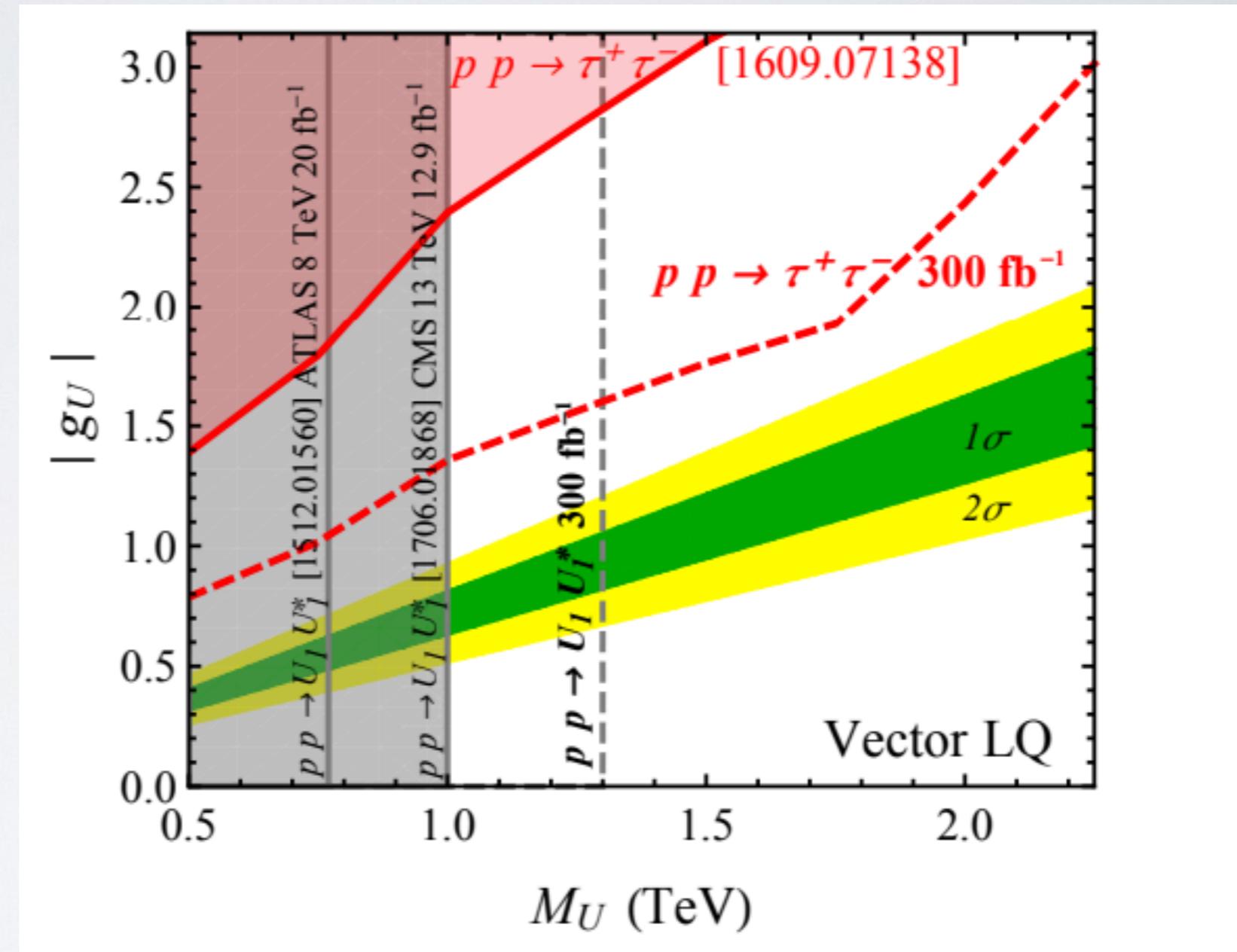
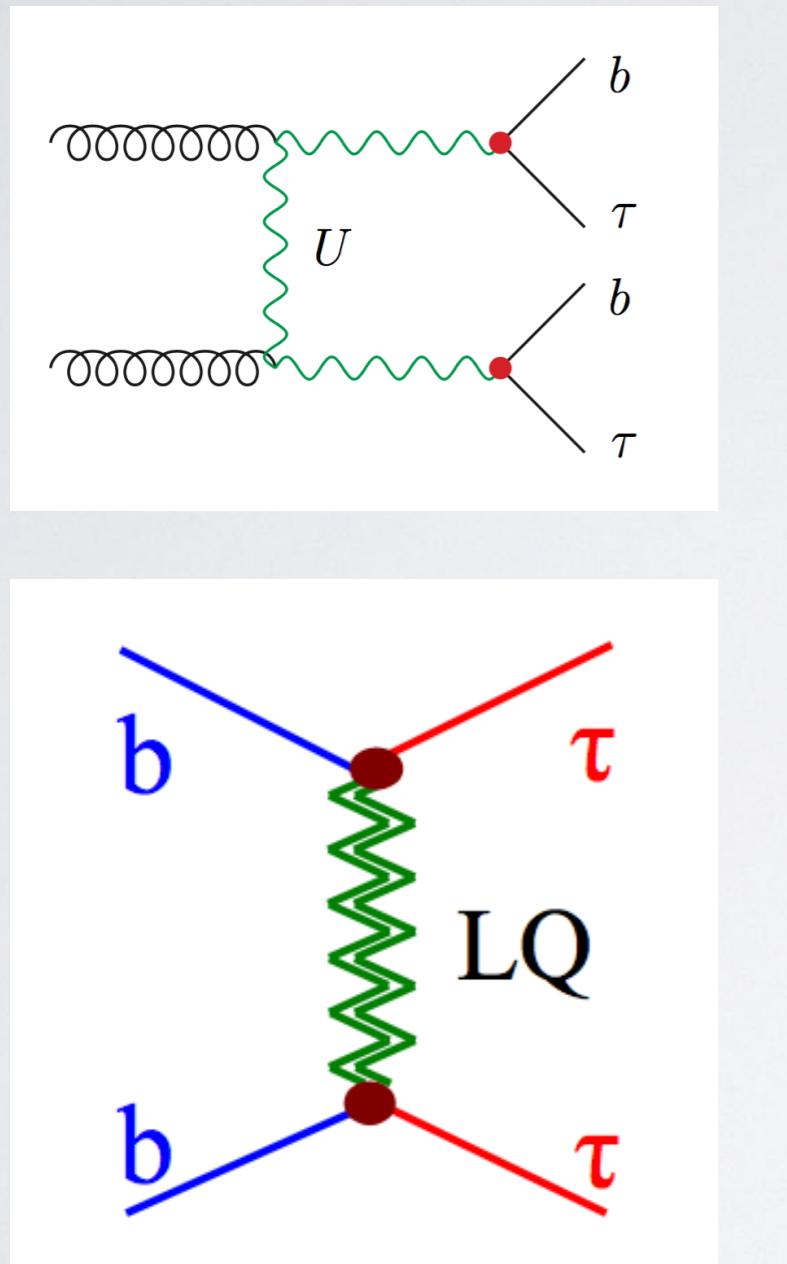
$$C_{g'}^L = \text{diag} \left(-\frac{g_3}{g_4}, -\frac{g_3}{g_4}, \frac{g_4}{g_3}, \frac{g_4}{g_3} \right)$$

- Z' Couplings

$$\mathcal{L}_{Z'} \supset -\frac{g_Y}{2} \sqrt{\frac{3}{2}} \left(\bar{\mathbf{L}}'_L C_{Z'}^L \gamma^\mu \mathbf{L}'_L \right) Z'_\mu$$

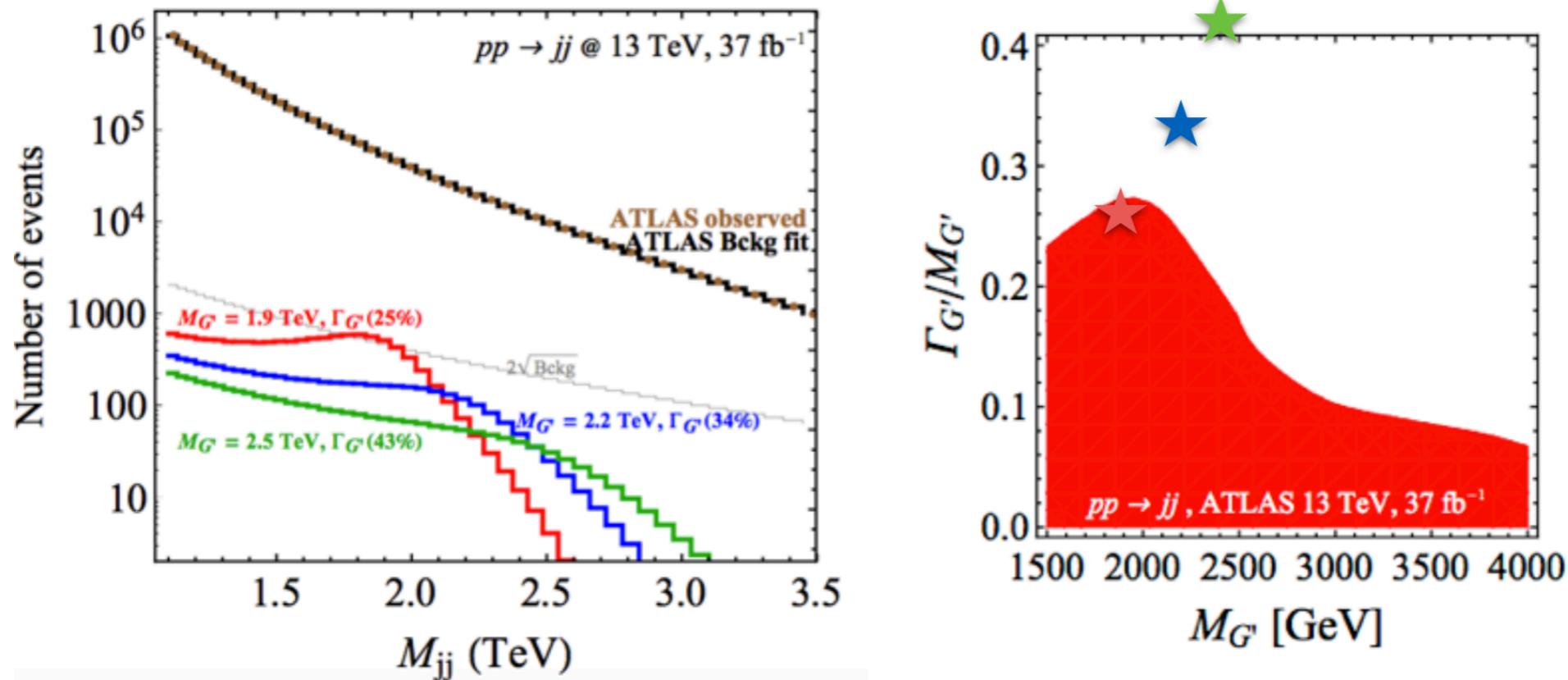
$$C_{Z'}^L = \text{diag} \left(-\frac{2}{3} \frac{g_1}{g_4}, -\frac{2}{3} \frac{g_1}{g_4}, \frac{g_4}{g_1}, \frac{g_4}{g_1} \right)$$

Leptoquark Direct Search Bounds: $m_U \gtrsim 1.5$ TeV



Coloron Direct Search Bounds

[LDL, Fuentes-Martin, Greljo, Nardecchia, Renner (work in progress)]



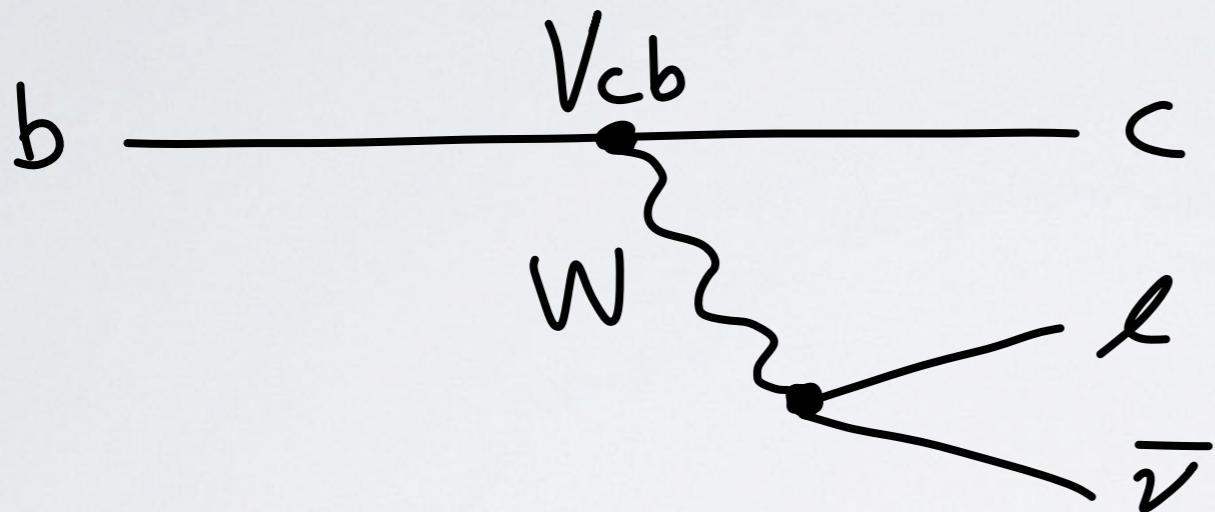
- However, bump-searches loose in sensitivity for large width/mass

$$\frac{\Gamma}{m} \lesssim 15\% \quad (\text{exp. analysis})$$

$$\frac{\Gamma_{g'}}{m_{g'}} \simeq 25\% \quad (\text{unavoidable in our scenario: large } g_4 + \text{extra channel in VLF})$$

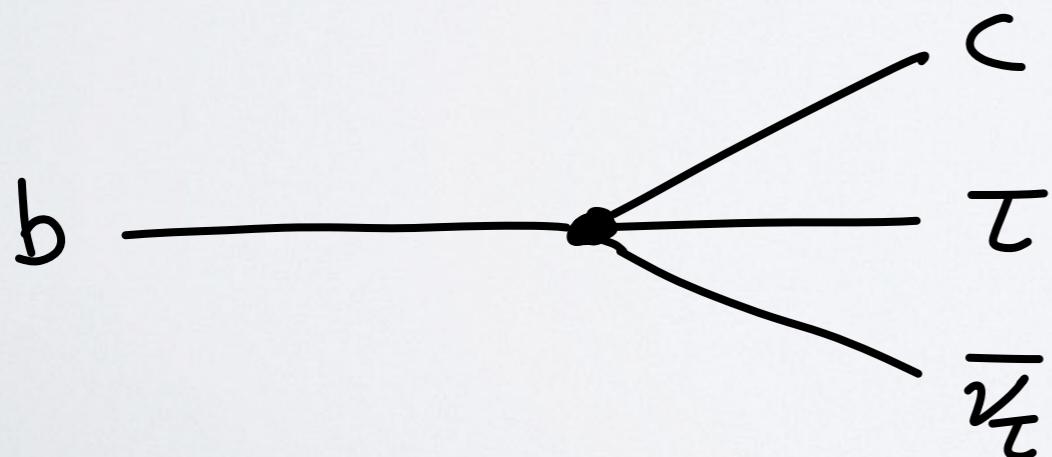
$$b \rightarrow c l \bar{\nu}$$

- Tree-level W-mediated process in SM, V_{cb} suppressed.



$$\mathcal{A}_{\text{SM}} \sim \frac{g^2 V_{cb}}{m_W^2} \sim \frac{V_{cb}}{v^2}$$

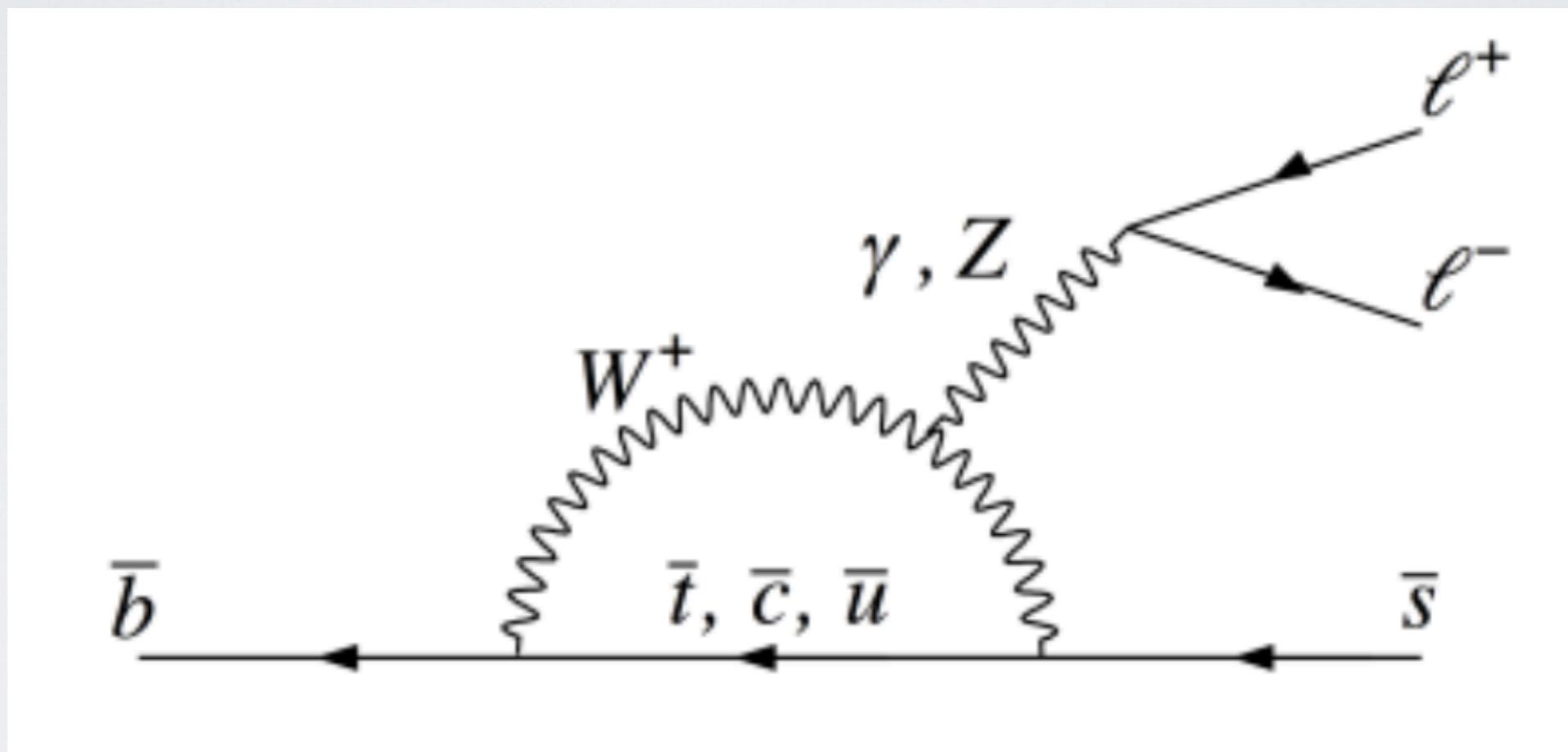
- Tree Level MFV New Physics in 3rd generation



$$\mathcal{A}_{\text{NP}} \sim \frac{V_{cb}}{\Lambda^2}$$

$$b \rightarrow s \bar{l} l$$

- Occurs at 1-loop in the SM, additional V_{ts} ($\sim V_{cb}$) suppression.



Up-Type Leptoquark Couplings

- Up-type leptoquark coupling matrix

$$\mathcal{L} \supset \frac{g_4}{\sqrt{2}} (\bar{u}_L^i V_{ij}^u) \mathcal{C}_{j\alpha} \gamma^\mu U_{1\mu} \nu_L^\alpha$$

$$\mathcal{K}_{i\alpha}^u \equiv V_{ij}^u \mathcal{C}_{j\alpha}$$

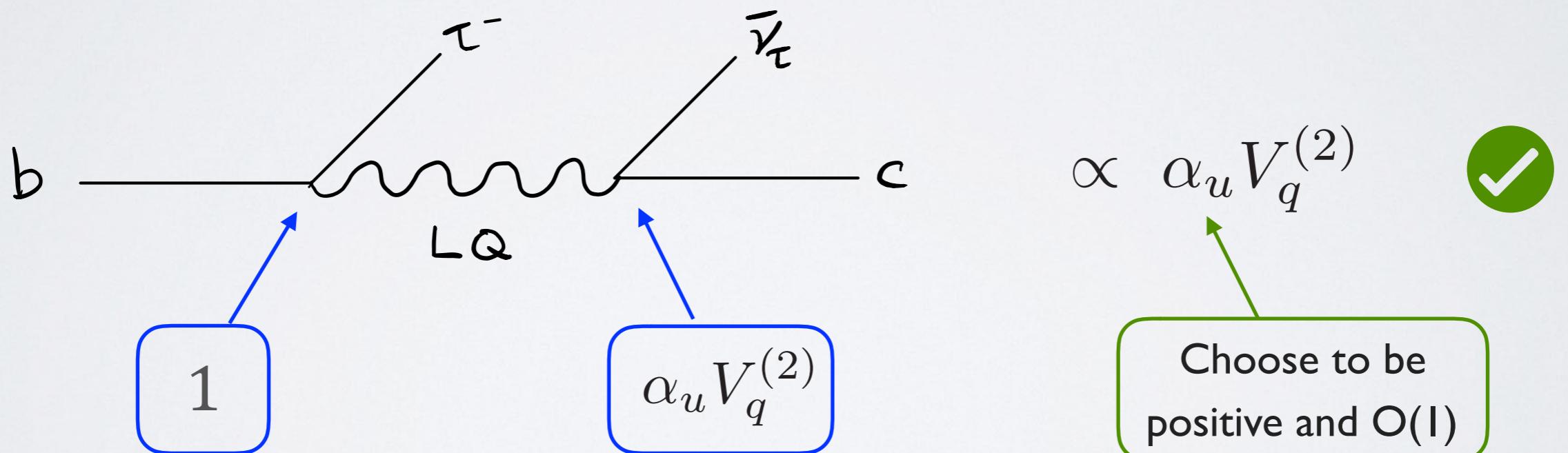
$$\mathcal{K}^u = \begin{pmatrix} V_\ell^{*(1)} (V_{ud} V_q^{(1)} + V_{us} V_q^{(2)}) & V_\ell^{*(2)} (V_{ud} V_q^{(1)} + V_{us} V_q^{(2)}) & \alpha_u (V_{ud} V_q^{(1)} + V_{us} V_q^{(2)}) \\ V_\ell^{*(1)} (V_{cd} V_q^{(1)} + V_{cs} V_q^{(2)}) & V_\ell^{*(2)} (V_{cd} V_q^{(1)} + V_{cs} V_q^{(2)}) & \alpha_u (V_{cd} V_q^{(1)} + V_{cs} V_q^{(2)}) \\ -\alpha_u^* V_\ell^{*(1)} |V_q|^2 & -\alpha_u^* V_\ell^{*(2)} |V_q|^2 & 1 \end{pmatrix}$$

$$V_\ell^{(i)} = \frac{v_1}{m_\chi} \lambda_\ell^{(i)} \quad V_q^{(i)} = \frac{v_3}{m_\chi} \lambda_q^{(i)}$$

Leptoquark Contribution: $b \rightarrow c\ell\bar{\nu}$

$$\mathcal{K}_{23}^u = \alpha_u (V_{cd} V_q^{(1)} + V_{cs} V_q^{(2)}) \approx \alpha_u V_q^{(2)}$$

- Take couplings to be real, need $V_q \sim V_{cb}$



Down-Type Leptoquark Couplings

- Down-type leptoquark coupling matrix

$$\mathcal{L} \supset \frac{g_4}{\sqrt{2}} (\bar{d}_L^i V_{ij}^d) \mathcal{C}_{j\alpha} \gamma^\mu U_{1\mu} (V_{\alpha\beta}^e e_L^\beta)$$

$$\mathcal{K}_{i\beta}^d \equiv V_{ij}^d \mathcal{C}_{j\alpha} V_{\alpha\beta}^e$$

$$\mathcal{K}^d = \begin{pmatrix} V_q^{(1)} V_\ell^{*(1)} & V_q^{(1)} V_\ell^{*(2)} & \alpha_d V_q^{(1)} \\ V_q^{(2)} V_\ell^{*(1)} & V_q^{(2)} V_\ell^{*(2)} & \alpha_d V_q^{(2)} \\ \alpha_e^* V_\ell^{*(1)} & \alpha_e^* V_\ell^{*(2)} & 1 \end{pmatrix}$$

$$V_\ell^{(i)} = \frac{v_1}{m_\chi} \lambda_\ell^{(i)} \quad V_q^{(i)} = \frac{v_3}{m_\chi} \lambda_q^{(i)}$$

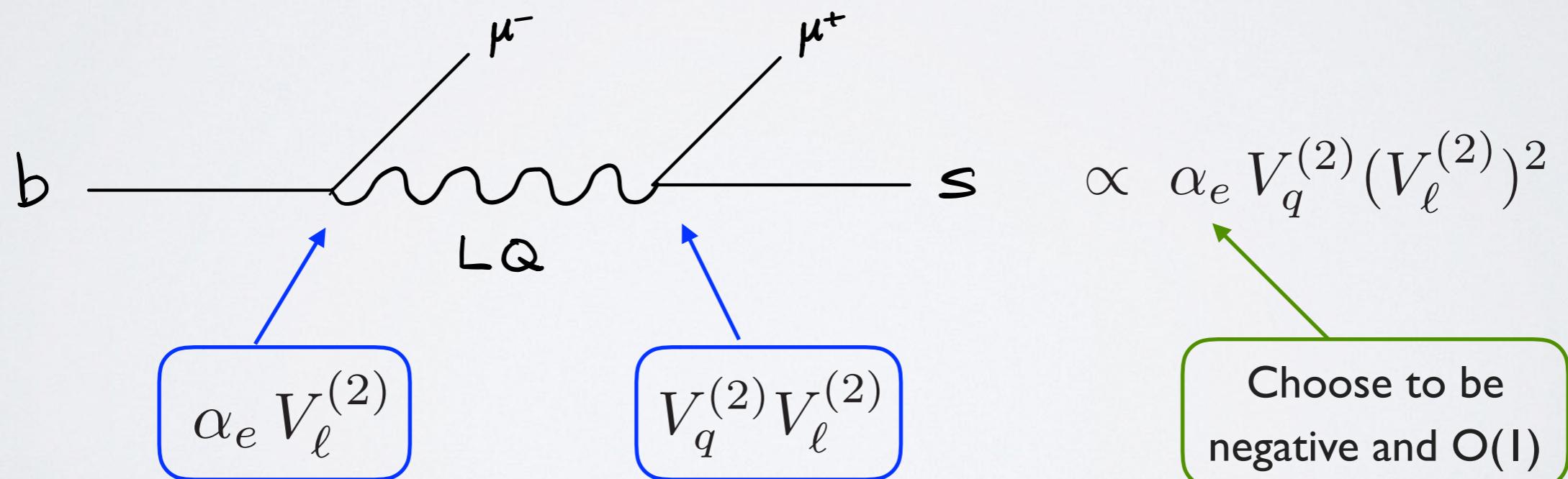
Leptoquark Contribution: $b \rightarrow s\bar{\ell}\ell$

$$\mathcal{K}^d = \begin{pmatrix} V_q^{(1)} V_\ell^{*(1)} & V_q^{(1)} V_\ell^{*(2)} & \alpha_d V_q^{(1)} \\ V_q^{(2)} V_\ell^{*(1)} & V_q^{(2)} V_\ell^{*(2)} & \alpha_d V_q^{(2)} \\ \alpha_e^* V_\ell^{*(1)} & \alpha_e^* V_\ell^{*(2)} & 1 \end{pmatrix}$$

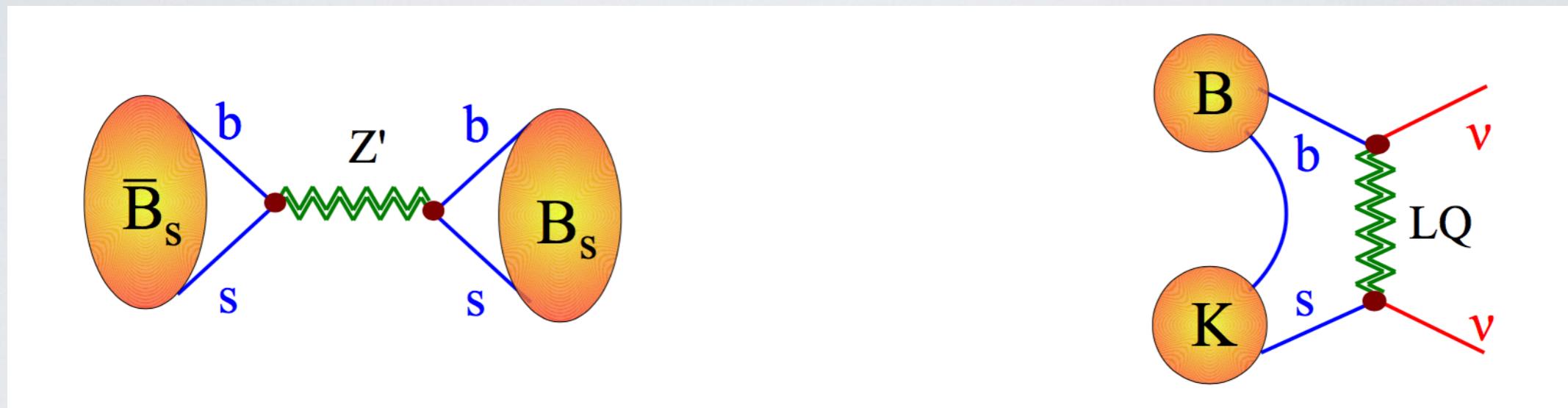
$$V_q^{(i)} = \frac{v_3}{m_\chi} \lambda_q^{(i)}$$

$$V_\ell^{(i)} = \frac{v_1}{m_\chi} \lambda_\ell^{(i)}$$

- Take couplings to be real, need destructive -15% effect:



B_s Mixing and $B \rightarrow K\nu\nu$



- FCNC generated only at 1-loop with a LQ mediator.
- Vanishes due to dynamics for U_1 vector LQ.

$$\mathcal{B}(B \rightarrow K^*\nu\nu) \propto (C_T - C_S)$$