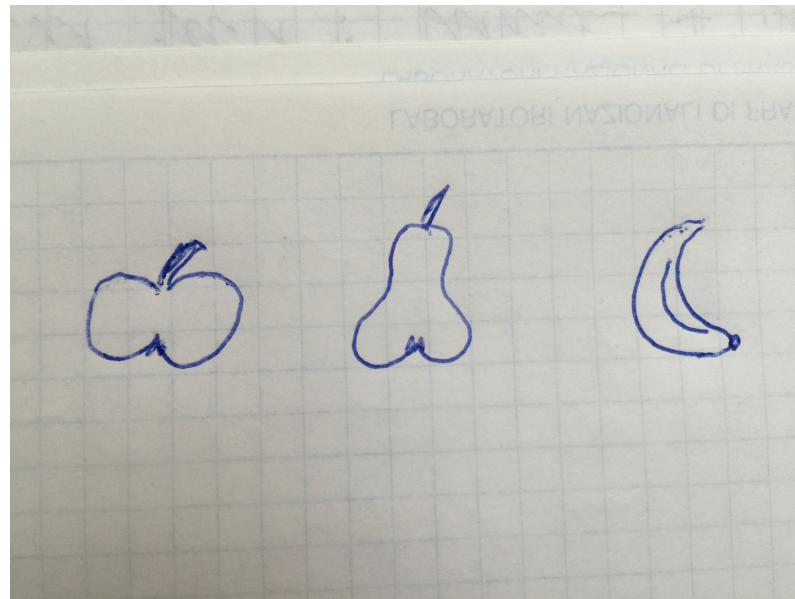


# **Flavor Theory 2017 plus a primer**

Gudrun Hiller, TU Dortmund

Works supported in part by the DFG research Unit FOR 1873 and the Federal Ministry for Education and Research (BMBF)



the same yet not the same  
symmetry, and symmetry-breaking

---

Matter comes in 3 generations  $\psi \rightarrow \psi_i, i = 1, 2, 3.$

quarks: 
$$\begin{pmatrix} u \\ d \end{pmatrix}, \begin{pmatrix} c \\ s \end{pmatrix}, \begin{pmatrix} t \\ b \end{pmatrix}$$
 leptons: 
$$\begin{pmatrix} \nu_e \\ e \end{pmatrix}, \begin{pmatrix} \nu_\mu \\ \mu \end{pmatrix}, \begin{pmatrix} \nu_\tau \\ \tau \end{pmatrix}$$

Fermions mix, change "flavor" in weak processes and violate CP!

$$\mathcal{L}_{SM} = -\frac{1}{4}F^2 + \bar{\psi}i\not{D}\psi + \frac{1}{2}(D\Phi)^2 - \bar{\psi}Y\psi\Phi + \mu^2\Phi^2 - \lambda\Phi^4$$

Strength of couplings, forces:  $\alpha_s, \alpha_w, \alpha_e:$  3

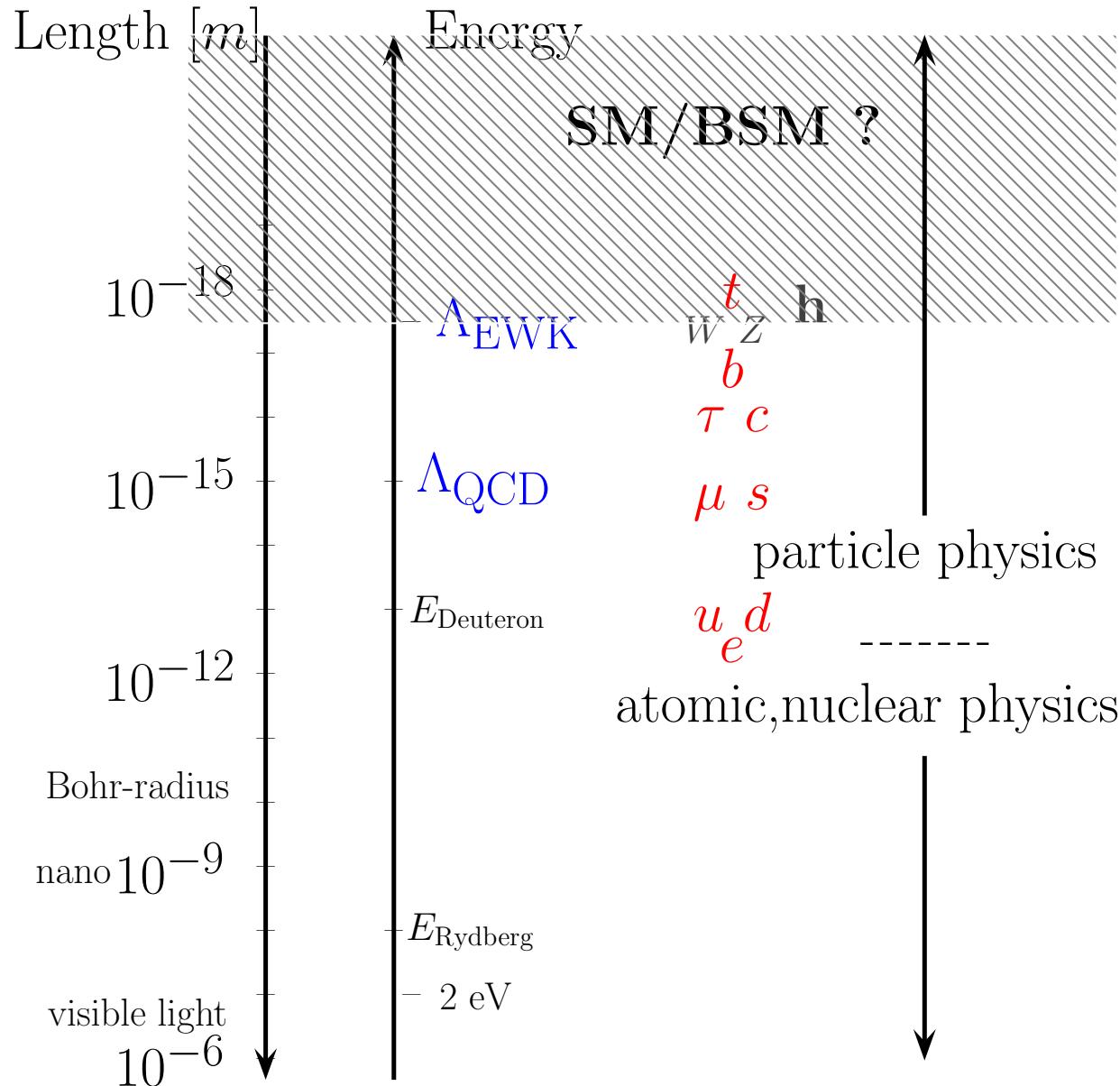
Electroweak scale, e.g.,  $m_Z:$  1

Scalar potential, e.g.,  $m_h:$  1

Fermions: 13

18 parameters (minimal, without neutrino masses and strong phase)  
flavor most uneconomical part of SM, masses and mixing puzzling

# Physics at highest Energies



# The Standard Model of Particle Physics: Flavor

---

fields in representations under the SM group  $SU(3)_C \times SU(2)_L \times U(1)_Y$

Higgs:  $\Phi(1, 2, 1/2)$  hypercharge  $Y = Q - T^3$

quarks:  $Q_L(3, 2, 1/6)_i, D_R(3, 1, -1/3)_i, U_R(3, 1, 2/3)_i$

leptons:  $L_L(1, 2, -1/2)_i, E_R(1, 1, -1)_i$  L: doublet, R:singlet under  $SU(2)_L$

$$\begin{aligned} \mathcal{L}_{SM} = & \sum_{\psi=Q,U,D,L,E} \bar{\psi}_i i \not{D} \psi_i \\ & - \bar{Q}_{L_i}(Y_{\textcolor{red}{u}})_{ij} \Phi^C U_{R_j} - \bar{Q}_{L_i}(Y_{\textcolor{red}{d}})_{ij} \Phi D_{R_j} - \bar{L}_{L_i}(Y_{\textcolor{red}{e}})_{ij} \Phi E_{R_j} \\ & + \mathcal{L}_{higgs} + \mathcal{L}_{gauge}, \quad \Phi^C = i\sigma^2 \Phi^* \end{aligned}$$

$Y_{u,d,e}$ : Yukawa matrices ( $3 \times 3$ , complex), off diagonal entries mix generations; sole sources of flavor in SM.

In hypothetical limit  $Y_{u,d,e} \rightarrow 0$  SM gains large "flavor-symmetry"

$$G_F = U(3)_{QL} \times U(3)_{UR} \times U(3)_{DR} \times U(3)_{LL} \times U(3)_{ER}$$

---

# The Standard Model of Particle Physics: Flavor

---

masses from spontaneous breaking of electroweak symmetry

$$\Phi^T(x) \rightarrow 1/\sqrt{2}(0, v + h(x)), \text{ Higgs vev } \langle \Phi \rangle = v/\sqrt{2} \simeq 174 \text{ GeV}$$

$$\mathcal{L}_{SM}^{yukawa} = -\bar{Q}_L \mathbf{Y}_u \Phi^C U_R - \bar{Q}_L \mathbf{Y}_d \Phi D_R - \bar{L}_L \mathbf{Y}_e \Phi E_R$$

Want mass eigenstates rather than the above gauge eigenstates:  
perform unitary trasfos on quark fields  $Q_L = (U_L, D_L), U_R, D_R$   
 $q_A(\text{gauge}) \rightarrow \tilde{q}_A(\text{mass}) = V_{A,q} q_A$  with  $V_{A,q} V_{A,q}^\dagger = 1$ .

$$\mathcal{L}_{SM}^{yukawa} = -\bar{U}_L \underbrace{V_{L,u}^\dagger V_{L,u}}_{=1} \underbrace{\mathbf{Y}_u \Phi^C}_{\rightarrow \text{masses}} \underbrace{V_{R,u}^\dagger V_{R,u}}_{=1} U_R + \text{down quarks}$$

$$\text{diag}(m_u, m_c, m_t) = \langle \Phi \rangle \cdot \text{diag}(y_u, y_c, y_t) = \langle \Phi \rangle \cdot V_{L,u} \mathbf{Y}_u V_{R,u}^\dagger$$

$$\text{diag}(m_d, m_s, m_b) = \langle \Phi \rangle \cdot \text{diag}(y_d, y_s, y_b) = \langle \Phi \rangle \cdot V_{L,d} \mathbf{Y}_d V_{R,d}^\dagger$$

# The Standard Model of Particle Physics: Flavor

---

unitary trasfos:  $\tilde{q}_A = V_{A,q} q_A$  with  $V_{A,q} V_{A,q}^\dagger = 1$ .

$$\mathcal{L}_{SM}^{yukawa} = -\bar{U}_L \underbrace{V_{L,u}^\dagger V_{L,u}}_{=1} \textcolor{red}{Y_u} \Phi^C \underbrace{V_{R,u}^\dagger V_{R,u}}_{=1} U_R + \text{down quarks.}$$

$$\text{diag}(m_u, m_c, m_t) = \langle \Phi \rangle \cdot \text{diag}(y_u, y_c, y_t) = \langle \Phi \rangle \cdot V_{L,u} \textcolor{red}{Y_u} V_{R,u}^\dagger$$

$$\text{diag}(m_d, m_s, m_b) = \langle \Phi \rangle \cdot \text{diag}(y_d, y_s, y_b) = \langle \Phi \rangle \cdot V_{L,d} \textcolor{red}{Y_d} V_{R,d}^\dagger$$

$$\mathcal{L}_{SM}^{up-mass} = -\underbrace{\bar{U}_L V_{L,u}^\dagger}_{\tilde{U}_L} \underbrace{V_{L,u} \textcolor{red}{Y_u} V_{R,u}^\dagger}_{\text{diagonal}} \Phi^C \underbrace{V_{R,u} U_R}_{\equiv \tilde{U}_R} = -\tilde{U}_{Li} m_{ui} \Phi^C \tilde{U}_{Ri}.$$

The tilde basis are mass eigenstates, down quarks analogously.

What else happened under the basis change in  $\mathcal{L}_{SM}$ ?

# The Standard Model of Particle Physics: CKM

---

The SM higgs interactions are strictly flavor diagonal and neutral current gauge interactions  $\gamma, Z, g$  stay being flavor universal, since they dont mix the chiralities, for instance:

$$\begin{aligned}\bar{U}_L \gamma^\mu A_\mu U_L &= \bar{U}_L (V_{L,u}^\dagger V_{L,u}) \gamma^\mu A_\mu (V_{L,u}^\dagger V_{L,u}) U_L \\ &= \tilde{\bar{U}}_L \gamma^\mu A_\mu V_{L,u} V_{L,u}^\dagger \tilde{U}_L = \tilde{\bar{U}}_L \gamma^\mu A_\mu \tilde{U}_L \quad \text{nothing has happened!}\end{aligned}$$

However, lets look at the charged currents  $W^\pm$ :

$$\begin{aligned}\bar{U}_L \gamma^\mu W_\mu^+ D_L &= \bar{U}_L (V_{L,u}^\dagger V_{L,u}) \gamma^\mu W_\mu^+ (V_{L,d}^\dagger V_{L,d}) D_L \\ &= \tilde{\bar{U}}_L \gamma^\mu W_\mu^+ \underbrace{V_{L,u} V_{L,d}^\dagger}_{\equiv V_{CKM}=V \neq 1} \tilde{D}_L\end{aligned}$$

Since  $Y_u$  and  $Y_d$  dont diagonalize (as observed!) under same unitary transformations, there is one important net effect related to flavor.

---

# The Standard Model of Particle Physics: CKM

---

The charged current interaction gets a flavor structure, encoded in the Cabibbo Kobayashi Maskawa (CKM) matrix  $V$ .

$$\mathcal{L}_{\text{CC}} = -\frac{g}{\sqrt{2}} \left( \bar{U}_L \gamma^\mu W_\mu^+ V \tilde{D}_L + \bar{D}_L \gamma^\mu W_\mu^- V^\dagger \tilde{U}_L \right).$$

$V_{ij}$  connects left-handed up-type quark of the  $i$ th gen. to left-handed down-type quark of  $j$ th gen. Intuitive labelling by flavor:

$$V = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix}, \quad V_{13} = V_{ub} \text{ etc}$$

$W$  exchange is the only way to change flavor in the SM.

# The Standard Model: CKM properties

---

$V$  is unitary, is in general complex, and induces CP violation

$V$  has 4 physical parameters, 3 angles and 1 phase.

"PDG" parametrization (exact, fully general)

$$V = \begin{pmatrix} c_{12}c_{13} & s_{12}c_{13} & s_{13}e^{-i\delta} \\ -s_{12}c_{23} - c_{12}s_{23}s_{13}e^{i\delta} & c_{12}c_{23} - s_{12}s_{23}s_{13}e^{i\delta} & s_{23}c_{13} \\ s_{12}s_{23} - c_{12}c_{23}s_{13}e^{i\delta} & -c_{12}s_{23} - s_{12}c_{23}s_{13}e^{i\delta} & c_{23}c_{13} \end{pmatrix}$$

$s_{ij} \equiv \sin \Theta_{ij}$ ,  $c_{ij} \equiv \cos \Theta_{ij}$ .  $\delta$  is the CP violating phase.

In Nature,  $\delta \sim \mathcal{O}(1)$  and  $V$  is hierarchical  $\Theta_{13} \ll \Theta_{23} \ll \Theta_{12} \ll 1$ .

Very different – large mixing angles for leptons (PMNS-Matrix):

$$\Theta_{23} \sim 45^\circ, \Theta_{12} \sim 35^\circ, \Theta_{13} \sim \mathcal{O}(10^\circ) \quad \text{all } \mathcal{O}(1) - \text{anarchy?}$$

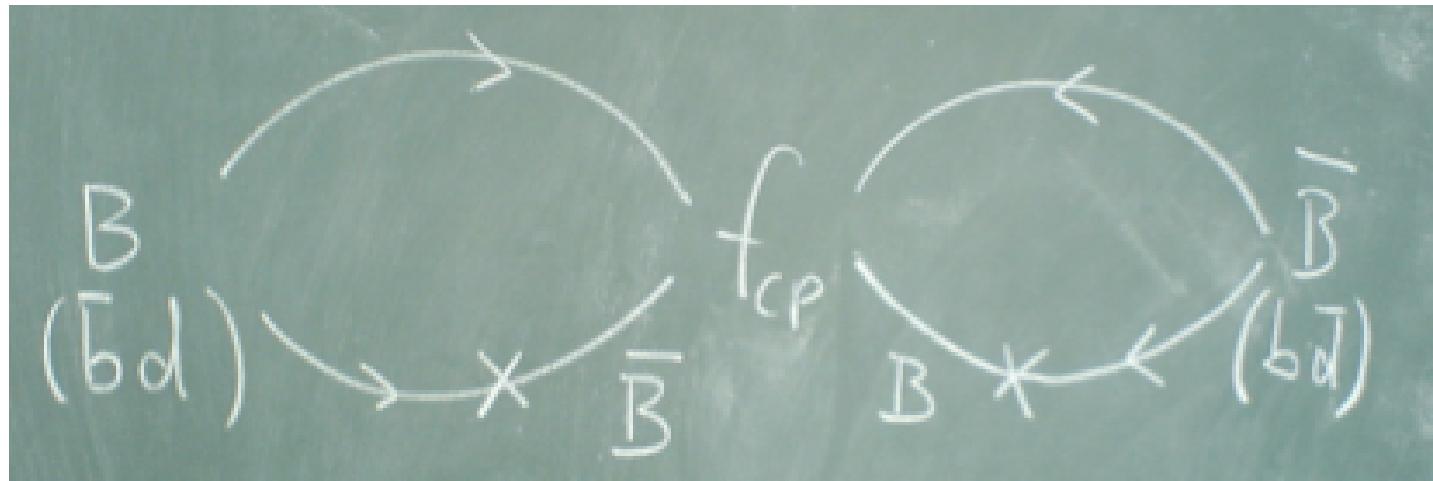
# CP is violated!.. together with Quark Flavor

---

Quark mixing matrix has 1 physical CP violating phase  $\delta_{CKM}$ .

Verified in  $B\bar{B}$  mixing

$$\sin 2\beta = 0.672 \pm 0.023 \text{ HFAG Aug 2010}$$



$\delta_{CKM}$  is large,  $O(1)!$

CPX also observed in  $B$ -decay  $A_{CP}(B \rightarrow K^\pm \pi^\mp) = -0.098 \pm 0.013$

HFAG Aug 2010

$$\Gamma(B \rightarrow K^+ \pi^-) \neq \Gamma(\bar{B} \rightarrow K^- \pi^+)$$

# The Standard Model: CKM properties

---

$V$  in Nature is hierarchical  $\Theta_{13} \ll \Theta_{23} \ll \Theta_{12} \ll 1$ . Wolfenstein parametrization; expansion in  $\lambda = \sin \Theta_C$ ,  $A, \rho, \eta \sim \mathcal{O}(1)$

$$V = \begin{pmatrix} 1 - \lambda^2/2 & +\lambda & A\lambda^3(\rho - i\eta) \\ -\lambda & 1 - \lambda^2/2 & +A\lambda^2 \\ A\lambda^3(1 - \rho - i\eta) & -A\lambda^2 & 1 \end{pmatrix} + \mathcal{O}(\lambda^4)$$

fits:  $\lambda = 0.225$ ,  $A = 0.82$ ,  $\bar{\rho} = 0.13$ ,  $\bar{\eta} = 0.34$

beyond lowest order  $\bar{\rho} = \rho(1 - \lambda^2/2)$  and  $\bar{\eta} = \eta(1 - \lambda^2/2)$

$\eta \neq 0$  signals CP violation; third gen. quarks decoupled at order  $\lambda^2$ .

There are in total 10 (known!) param. in quark flavor & CP sector:

**6 masses, 3 angles and 1 phase in CKM-matrix**

with accuracy:  $|V_{us}| = 0.225$  (permille),  $|V_{cb}| = 42 \cdot 10^{-3}$  (percent),  
 $|V_{ub}| = 4 \cdot 10^{-3}$  (ten percent),  $\sin 2\beta$ (measured) = 0.67 (percent)

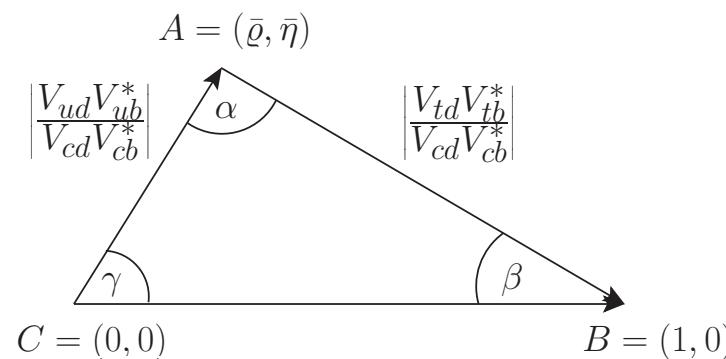
PS: enormous progress from  $B$ -factories over past decade. PPS: still improving precision.

All hadronic flavor violation, including decays, production rates at colliders and meson mixing effects should be described by these 10 parameters alone, if SM is correct. Since all parameters are known, this statement is very predictive and subject to numerous tests.

$V$  is unitary  $VV^\dagger = 1$  or,  $\sum_j V_{ij}V_{kj}^* = \delta_{ik}$ .

*the unitarity triangle*

$V_{ub}V_{ud}^* + V_{cb}V_{cd}^* + V_{tb}V_{td}^* = 0$ , all terms order  $\lambda^3$ .

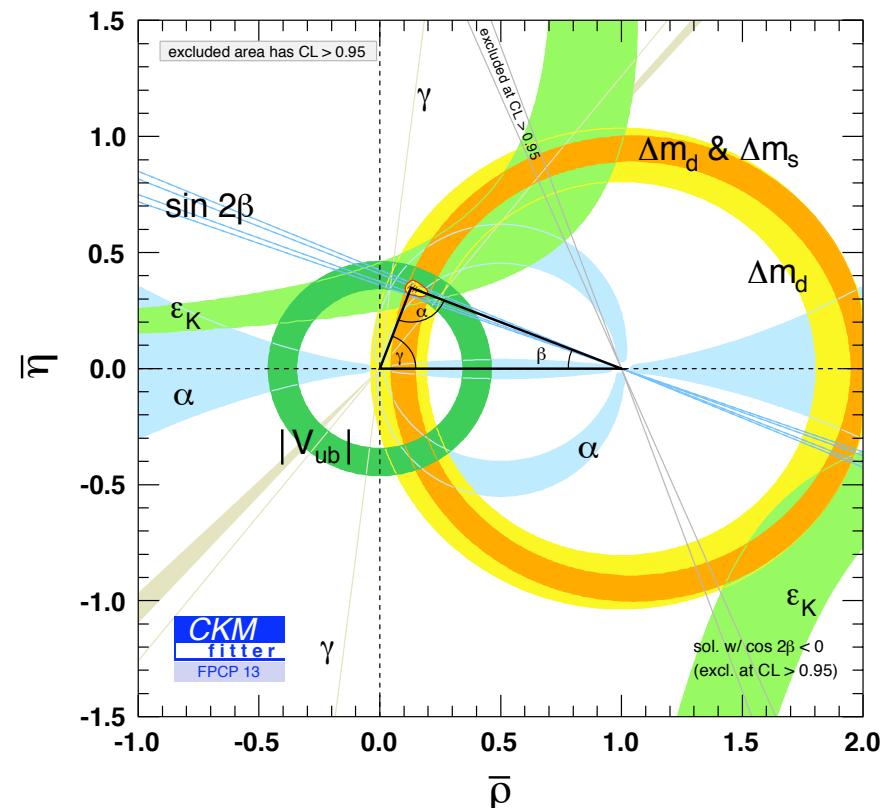
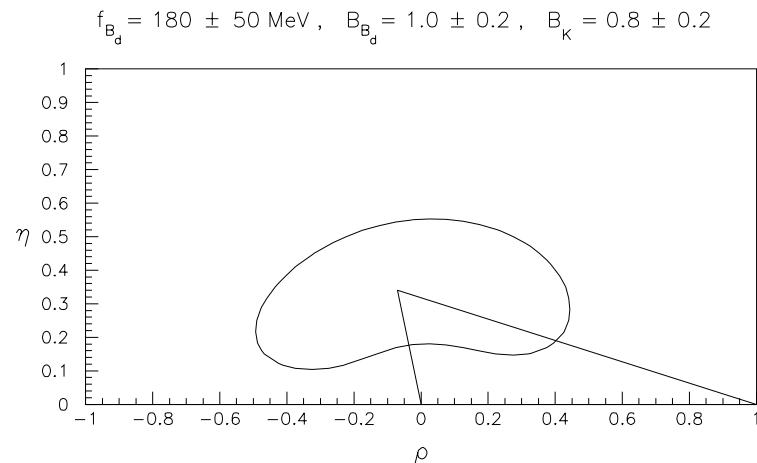


Its apex determines the Wolfenstein parameters  $\bar{\rho}, \bar{\eta}$ . In the absence of CP viol., the triangle would be squashed.

Information on the apex can come from various processes, measuring angles or sides.

# SM tests with Quark flavor/CKM 1995 vs today

The CKM-picture of flavor and CP violation is currently consistent with all – and quite different – laboratory observations, although some tensions exist.



$$V_{CKM} V_{CKM}^\dagger = 1$$

the Yukawa coupling  $\textcolor{red}{Y}$  in  $\mathcal{L}_{SM} = -\bar{\psi} \textcolor{red}{Y} \psi \Phi + \dots$  is a  $3 \times 3$  matrix.

Experimentally:

$$Y_u \sim \begin{pmatrix} 10^{-5} & -0.002 & 0.008 + i 0.003 \\ 10^{-6} & 0.007 & -0.04 \\ 10^{-8} + i 10^{-7} & 0.0003 & 0.94 \end{pmatrix}$$

$$Y_d \sim \text{diag}(10^{-5}, 5 \cdot 10^{-4}, 0.025)$$

$$Y_e \sim \text{diag}(10^{-6}, 6 \cdot 10^{-4}, 0.01)$$

very peculiar structure

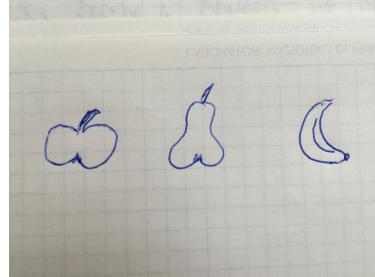
quark mixing is hierachal, lepton mixing anarchical  $O(1)$  entries

Generational structure & mixing is a feature of the SM and many beyond-SM particles. VIRTUES:

- i) high sensitivity to BSM in flavor violation; predictive, and suppressed in SM therefore ideal to look for New Physics in, e.g.,  
 $b \rightarrow s\ell\ell, \mu \rightarrow e\gamma, \dots$
- ii) flavorful processes are intrinsically linked to the "flavor puzzle": masses, i.e., Yukawa matrices in  $\mathcal{L}_{SM} = -\bar{Q}Y_u H^C U - \bar{Q}Y_d H D + \dots$  do not appear to be random but rather structured - from where? with a BSM-signal, we may be able to progress here
- iii) plenty of modes  $s \rightarrow d, c \rightarrow u, b \rightarrow s, d, t \rightarrow c, u, \mu \rightarrow e, \tau \rightarrow \mu, e$  plus charged ones and  $h \rightarrow f\bar{f}'$ ; ongoing & future experiments, too. we may identify  $\mathcal{L}_{BSM}$ ; complementary to direct searches

# Lepton Non-universality?

$$\begin{pmatrix} \nu_e \\ e \end{pmatrix}, \begin{pmatrix} \nu_\mu \\ \mu \end{pmatrix}, \begin{pmatrix} \nu_\tau \\ \tau \end{pmatrix}$$



Anomalies in semileptonic  $B$ -meson decays:

$$R_K = \frac{\mathcal{B}(B \rightarrow K \mu \mu)}{\mathcal{B}(B \rightarrow K ee)} \quad 2.6\sigma \quad (\text{LHCb'14})$$

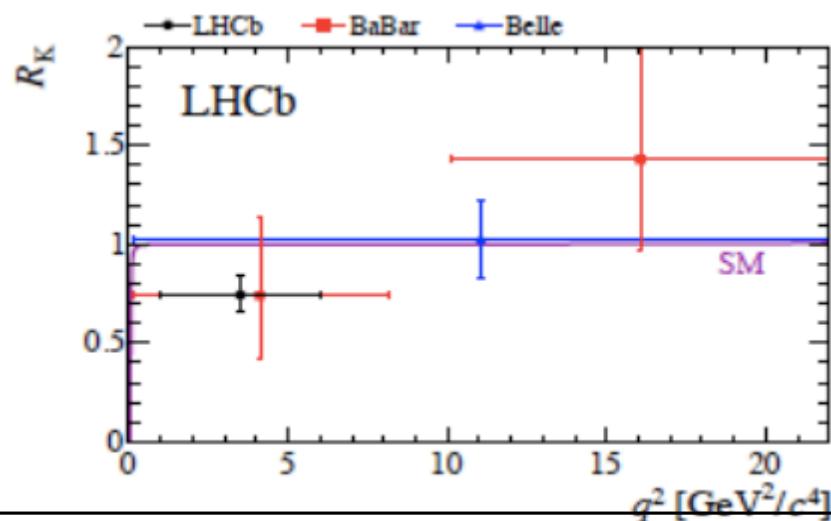
$$R_{K^*} = \frac{\mathcal{B}(B \rightarrow K^* \mu \mu)}{\mathcal{B}(B \rightarrow K^* ee)} \quad 2.6\sigma \quad (\text{LHCb'17})$$

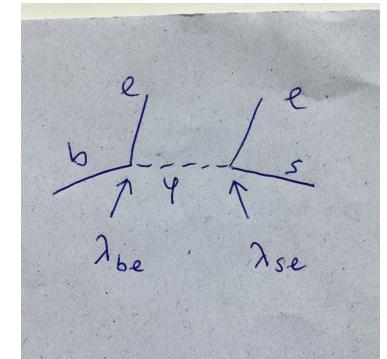
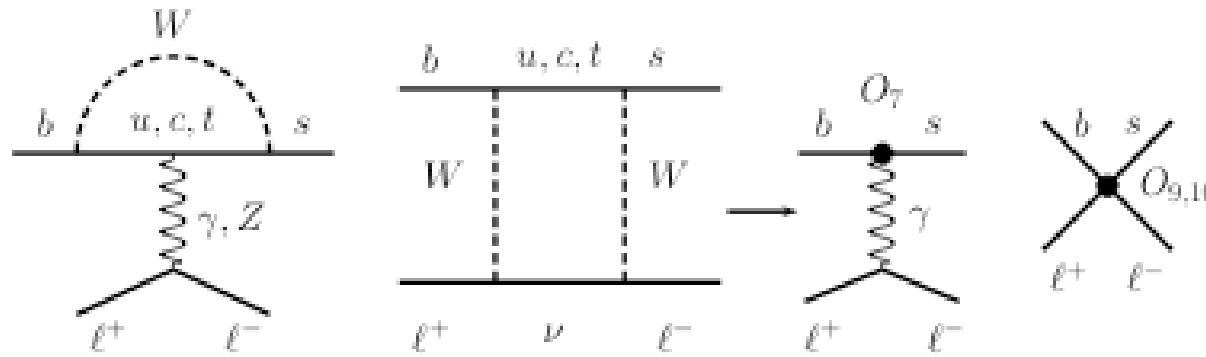
$$R_{D^{(*)}} = \frac{\mathcal{B}(B \rightarrow D^{(*)} \tau \nu_\tau)}{\mathcal{B}(B \rightarrow D^{(*)} \ell \nu_\ell)} \quad 3.4.\sigma \ (D^*), 2.1\sigma \ (D) \quad (\text{LHCb'15, B-factories})$$

$$R_H = \frac{\mathcal{B}(B \rightarrow H\mu\mu)}{\mathcal{B}(B \rightarrow Hee)}, \quad H = K, K^*, X_s, \Phi, \dots$$

In models with lepton universality (incl. SM):  $R_H = 1 + \text{tiny}$  GH, Krüger '03

	LHCb	SM
$\mathcal{B}(B \rightarrow K\mu\mu)_{[1,6]}$	$(1.21 \pm 0.09 \pm 0.07) \cdot 10^{-7}$	$(1.75^{+0.60}_{-0.29}) \cdot 10^{-7}$
$\mathcal{B}(B \rightarrow Kee)_{[1,6]}$	$(1.56^{+0.19+0.06}_{-0.15-0.04}) \cdot 10^{-7}$	same
$R_K _{[1,6]}$	$0.745 \pm^{0.090}_{0.074} \pm 0.036$	$\approx 1$



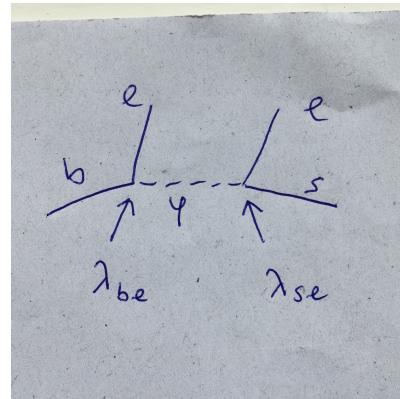


$R_K, R_{K^*}$  tells us at face value  $C_9^\mu = -C_{10}^\mu \simeq -0.6$  vs  $C_9^{\text{SM}} \simeq -C_{10}^{\text{SM}} \simeq 4$

about 20 % BSM contribution to  $O_{LL} = \bar{s}_L \gamma_\mu b_L \bar{\mu}_L \gamma^\mu \mu_L$ .

This actually is "according to plan": FCNCs are suppressed (GIM, CKM, loop) in SM and BSM physics can show up without big competition.

$R_{K^{(*)}} \neq 1$  would not only be a (loud) breakdown of the SM, it tells us something about flavor  $\rightarrow$  possibly learn something about flavor



Tree level explanations:

$$\frac{\lambda^2}{M^2} \sim \frac{1}{5} \frac{g^4}{m_W^2} \frac{1}{16\pi^2} V_{tb} V_{ts}^* \sim \frac{1}{(30\text{TeV})^2}$$

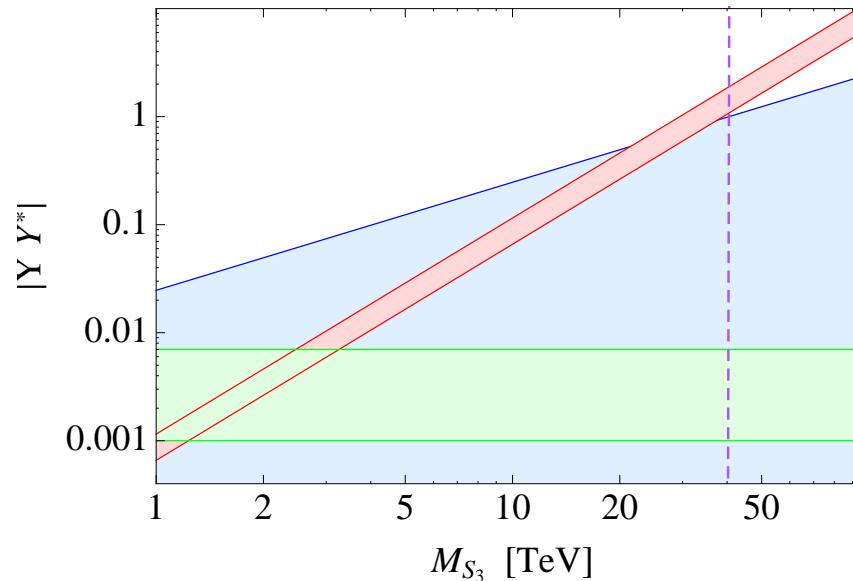
for order one couplings this points to a collider-mass scale.

With (minimal) flavor violating BSM  $\frac{\lambda^2}{M^2} \sim \frac{1}{5} \frac{g^4}{m_W^2} \frac{1}{16\pi^2} \sim \frac{1}{(6\text{TeV})^2}$   
this is within reach of the LHC.

In flavor models that explain quark, lepton masses, CKM, PMNS the BSM couplings can be further suppressed  $\rightarrow$  TeV-ish BSM mass.

# Mass scales versus couplings

$$R_{K,K^*} : \frac{Y_{b\mu} Y_{s\mu}^* - Y_{be} Y_{se}^*}{M^2} \simeq \frac{1.1}{(35 \text{ TeV})^2}, (S_3) \text{ LQ scalar triplet } \textcolor{violet}{\text{GH, Nisandzic, 1704.05444}}$$



red: explains  $R_K, R_{K^*}$ , blue: allowed by  $B_s - \bar{B}_s$ -mixing, green: flavor model prediction

$Y_{q_3 \ell} \sim c_l$ ,  $Y_{q_2 \ell} \sim c_l \lambda^2$ ,  $q_3 = b, t$ ,  $q_2 = s, c$ ,  $\lambda, c_l \lesssim 0.2$  points to TeV-ish mass  $M$ !

Model-independent upper limit by  $B_s$ -mixing  $\propto \lambda^4/M^2$  at 40 TeV.

Expected mass scale  $M$  depends on flavor couplings       $\lambda^2/M^2$  fixed

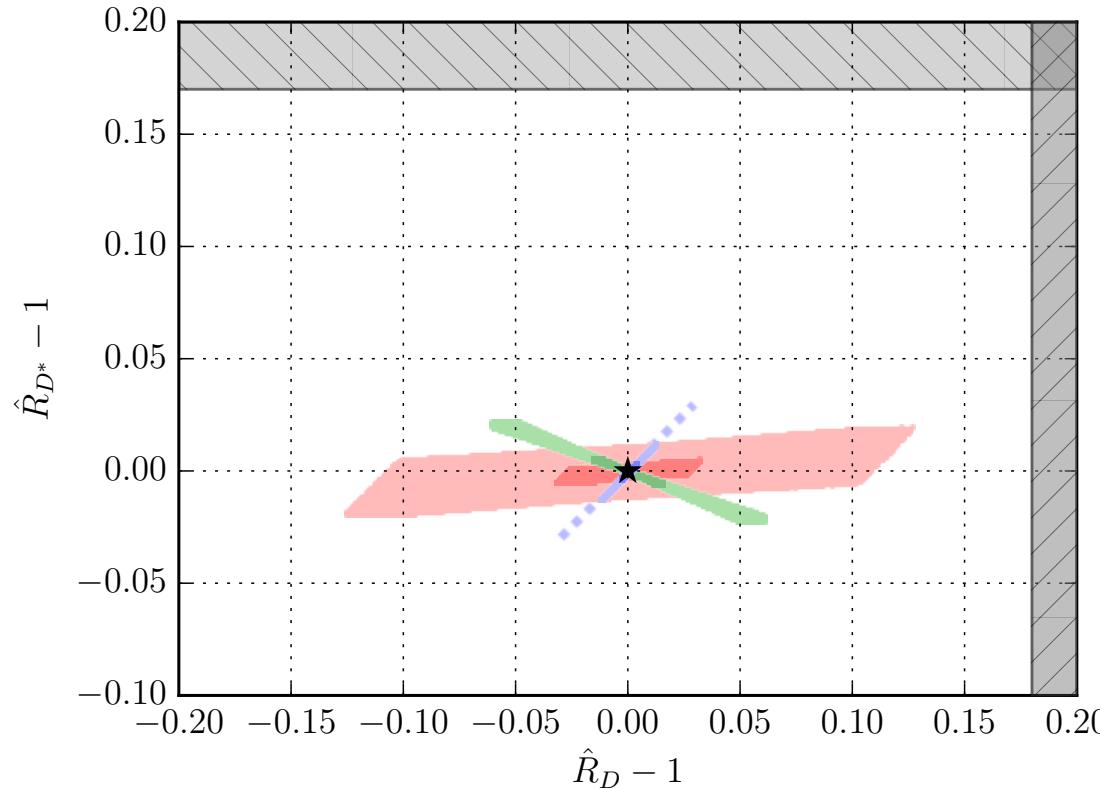
The size of the effect – current hints for SM deviation – in  $R_{K^{(*)}}$  is "natural", in the core of parameter space. How about  $R_{D^{(*)}}$ ?

Tree-level in SM, similar order of anomalous data as  $R_{K^{(*)}}$  implies large couplings and very low BSM:

flavor	generic	minimal	PMNS/CKM
$R_{K^{(*)}}$ tree	30 TeV	6 TeV	few TeV
$R_{K^{(*)}}$ loop	few TeV	0.5 TeV	expected similar to $R_{D^{(*)}}$
$R_{D^{(*)}}$ tree	$\sim$ a TeV	0.3 TeV	not viable <a href="#">1609.08895</a>

Linking the anomalies is intriguing however not straightforward, lower deviation in  $R_{D^{(*)}}$ , in particular  $R_{D^*}$  more "natural".

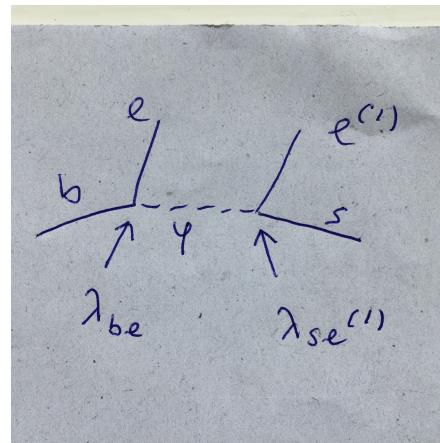
# $R_{D^{(*)}}$ from leptoquarks with flavor?



$\hat{R}_{D^{(*)}} = R_{D^{(*)}}/R_{D^{(*)}}^{\text{SM}}$ ; star: SM, grey: exp  $1\sigma$  band (too far away from SM to fit the plot); red:  $V_1$ , blue  $V_3$ , green  $S_2$ . LQs with flavor patterns, constraints: rare  $K$  decays,  $\mu - e$  conversion,  $B \rightarrow K\nu\nu$ , perturbativity [1609.08895](#) — Ignoring the flavor model ones, only model  $V_1$  can avoid exp constraints. **All models  $S_3, V_1, V_3$  can explain  $R_{K^{(*)}}$ .**

$R_{K^{(*)}}$ 

- triggered new type of BSM model-building:  $Z'$ , leptoquarks
- its plausible (OK order of magnitude)
- its an opportunity (highly informative clash with SM)
- how to consolidate? rule out?
- if this really stays, decipher
  - 4 points



Leptoquark coupling matrix:  $\lambda_{ql} = \begin{pmatrix} \lambda_{q_1 e} & \lambda_{q_1 \mu} & \lambda_{q_1 \tau} \\ \lambda_{q_2 e} & \lambda_{q_2 \mu} & \lambda_{q_2 \tau} \\ \lambda_{q_3 e} & \lambda_{q_3 \mu} & \lambda_{q_3 \tau} \end{pmatrix}$

columns=leptons

rows=quarks

mixed structures, not present in standard model!

columns=leptons, discrete non-abelian flavor symmetries  
 (sub-groups of  $SU(3)$ ), e.g.  $A_4$  Altarelli, Feruglio      "zeros and ones"

Rows=quarks, hierarchical,  $U(1)$ -Froggatt-Nielsen-Symmetry  
 $1 \gg \rho \gg \rho_d$       "hierarchies"

We can use these symmetries to explain quark and lepton properties. Then predict leptoquark textures, for instance,

$$\lambda_{ql} \sim \begin{pmatrix} \rho_d & \rho_d & \rho_d \\ \rho & \rho & \rho \\ 1 & 1 & 1 \end{pmatrix}, \quad \begin{pmatrix} 0 & \rho_d & 0 \\ 0 & \rho & 0 \\ 0 & 1 & 0 \end{pmatrix}, \dots$$

second matrix can explain  $R_K$  – leptoquark couples to muons only.

# Diagnosing quark and lepton flavor

---

Very general ansatz [1503.01084](#)

LQ coupling matrix:  $\lambda_{ql} \equiv \begin{pmatrix} \lambda_{q_1 e} & \lambda_{q_1 \mu} & \lambda_{q_1 \tau} \\ \lambda_{q_2 e} & \lambda_{q_2 \mu} & \lambda_{q_2 \tau} \\ \lambda_{q_3 e} & \lambda_{q_3 \mu} & \lambda_{q_3 \tau} \end{pmatrix} \sim \begin{pmatrix} \rho_d \kappa & \rho_d & \rho_d \\ \rho \kappa & \rho & \rho \\ \kappa & 1 & 1 \end{pmatrix}$

rows =quarks, columns= leptons

data:

$$\rho_d \lesssim 0.02, \quad \kappa \lesssim 0.5, \quad 10^{-4} \lesssim \rho \lesssim 1, \quad \kappa/\rho \lesssim 0.5, \quad \rho_d/\rho \lesssim 1.6.$$

Froggatt-Nielsen:  $\rho \sim \epsilon^2$ ,  $\rho_d \sim \epsilon^3$  or  $\epsilon^4$ ,  $(Q_L)$  with  $\epsilon \sim 0.2$ .

Ready to use for correlations for  $B$ , charm, lepton and collider processes

- 
1. Study more LNU ratios and do this more precisely including the high  $q^2$  bins

$$R_H = \frac{\mathcal{B}(\bar{B} \rightarrow \bar{H} \mu\mu)}{\mathcal{B}(\bar{B} \rightarrow \bar{H} ee)}, \quad H = K, K^*, X_s, \dots$$

GH, Krüger '03

At linear approximation it suffices to measure 2 different (by spin parity of final hadron)  $R_H$  ratios and then all others serve as consistency checks

1411.4773

Wilson coefficients  $C$ : V-A,  $C'$ : V+A currents

$$C + C' : \quad K, K_{\perp}^*, \dots$$

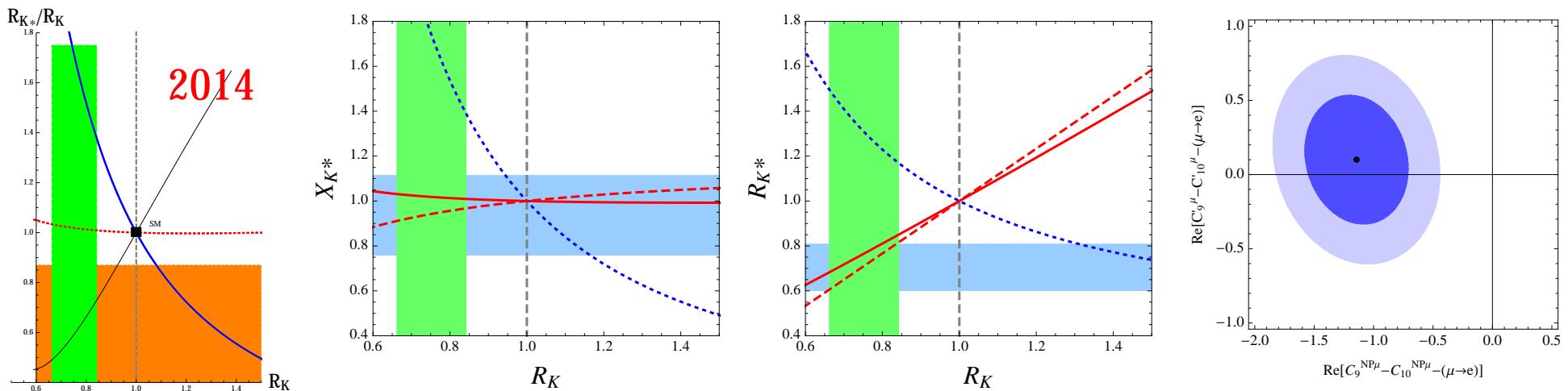
$$C - C' : \quad K_0(1430), K_{0,\parallel}^*, \dots$$

and  $K_{\perp}^*$  subleading at both high and low  $q^2$  windows. **Predictions:**  
 $R_K \simeq R_{\eta}$ ,  $R_{K^*} \simeq R_{\Phi} \simeq R_{K_0(1430)}$  and all  $R_H$  equal if no V+A currents.

---

The measurement of  $R_K$  and  $R_{K^*}$  does this diagnozing job. SM-like chirality operators are the dominant source behind the anomalies.

**Prediction:**  $R_{X_s} \simeq 0.73 \pm 0.07$  inclusive decays, Belle II



Green band:  $R_K$   $1\sigma$  LHCb, blue band  $R_{K^*}$   $1\sigma$  LHCb. Different BSM scenarios are red dashed: pure  $C_{LL}$  (LQ triplet). Black solid:  $C_{LL} = -2C_{RL}$ . Blue:  $C_{RL}$  (LQ doublet)/disfavored as dominant source of LNU. Orange: data from  $B \rightarrow X_s \ell \ell$ .  $R_{X_s}^{\text{Belle}'09} = 0.42 \pm 0.25$ ,  $R_{X_s}^{\text{BaBar}'13} = 0.58 \pm 0.19$ .

$R_H < 1$ : too few muons, or too many electrons, or combination thereof.

2. To disentangle this lepton specific modes are required.

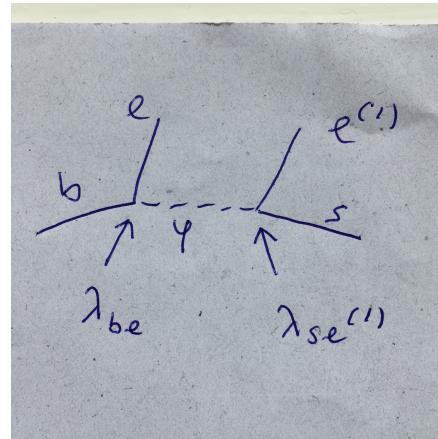
$B \rightarrow Hee$  and  $B \rightarrow H\mu\mu$  studies; global fits Bobeth, van Dyk, Mahmoudi, Matias, Virto, Straub, Camalich, Altmannshofer, Hurth, Hofer, Jäger

It is interesting that also  $B \rightarrow K, K^*\mu\mu$  has presently an anomaly, that even can point to the same direction as  $R_{K,K^*}$ .

LNU in explicit models can be arranged by gauging lepton flavor ( $Z'$ )  
Altmannshofer, Straub, Fuentes, Bishara, Quiros, Panico LQs can be charged under  
flavor group Varzielas, GH, Loose, Schönwald

From a flavor perspective, LNU quite generically implies LFV

Guadagnoli, Lane



### 3. Search for LFV

in B-decays, in charm decays, and with charged leptons ( $\mu$  -e conversion, rare decays), at colliders

observable	current 90 % CL limit	constraint	future sens.
$\mathcal{B}(\mu \rightarrow e\gamma)$	$5.7 \cdot 10^{-13}$ MEG	$ \lambda_{qe}\lambda_{q\mu}^*  \lesssim \frac{M^2}{(34\text{TeV})^2}$	$6 \cdot 10^{-14}$ MEG
$\mathcal{B}(\tau \rightarrow e\gamma)$	$1.2 \cdot 10^{-8}$ Belle	$ \lambda_{qe}\lambda_{q\tau}^*  \lesssim \frac{M^2}{(1\text{TeV})^2}$	
$\mathcal{B}(\tau \rightarrow \mu\gamma)$	$4.4 \cdot 10^{-8}$ Babar	$ \lambda_{q\mu}\lambda_{q\tau}^*  \lesssim \frac{M^2}{(0.7\text{TeV})^2}$	$5 \cdot 10^{-9}$ [B2]
$\mathcal{B}(\tau \rightarrow \mu\eta)$	$6.5 \cdot 10^{-8}$ Belle	$ \lambda_{s\mu}\lambda_{s\tau}^*  \lesssim \frac{M^2}{(3.7\text{TeV})^2}$	$2 \cdot 10^{-9}$ [B2]
$\mathcal{B}(B \rightarrow K\mu^\pm e^\mp)$	$3.8 \cdot 10^{-8}$ BaBar	$\sqrt{ \lambda_{s\mu}\lambda_{be}^* ^2 +  \lambda_{b\mu}\lambda_{se}^* ^2} \lesssim \frac{M^2}{(19.4\text{TeV})^2}$	
$\mathcal{B}(B \rightarrow K\tau^\pm e^\mp)$	$3.0 \cdot 10^{-5}$ PDG	$\sqrt{ \lambda_{s\tau}\lambda_{be}^* ^2 +  \lambda_{b\tau}\lambda_{se}^* ^2} \lesssim \frac{M^2}{(3.3\text{TeV})^2}$	
$\mathcal{B}(B \rightarrow K\mu^\pm \tau^\mp)$	$4.8 \cdot 10^{-5}$ PDG	$\sqrt{ \lambda_{s\mu}\lambda_{b\tau}^* ^2 +  \lambda_{b\mu}\lambda_{s\tau}^* ^2} \lesssim \frac{M^2}{(2.9\text{TeV})^2}$	$\lesssim 10^{-6}$ K.Petridis
$\mathcal{B}(B \rightarrow \pi\mu^\pm e^\mp)$	$9.2 \cdot 10^{-8}$ BaBar	$\sqrt{ \lambda_{d\mu}\lambda_{be}^* ^2 +  \lambda_{b\mu}\lambda_{de}^* ^2} \lesssim \frac{M^2}{(15.6\text{TeV})^2}$	

**Table 1:** Selected LFV data, constraints and future sensitivities. Here,  $q = d, s, b$ . The Belle II projections [B2] are for  $50 ab^{-1}$ .

For the constraint from  $\mathcal{B}(\tau \rightarrow \mu\eta)$  we ignored the possibility of cancellations with  $\lambda_{d\mu}\lambda_{d\tau}^*$ . We ignore tuning between leading order

diagrams in the  $\ell \rightarrow \ell'\gamma$  amplitudes.  $R_K: 0.7 \lesssim \text{Re}[\lambda_{se}\lambda_{be}^* - \lambda_{s\mu}\lambda_{b\mu}^*] \frac{(24\text{TeV})^2}{M^2} \lesssim 1.5$ ,  $K$ -decays  $|\lambda_{d\mu}\lambda_{s\mu}^*| \lesssim \frac{M^2}{(183\text{TeV})^2}$ .

Next round of  $\mu$ - $e$  conversion experiments reaching  $10^{-16}$  sensitive to the  $R_{K,K^*}$  parameter space!

---

predictions semileptonic  $B$ -decays:

$$\mathcal{B}(B \rightarrow K\mu^\pm e^\mp) \simeq 3 \cdot 10^{-8} \kappa^2 \left( \frac{1 - R_K}{0.23} \right)^2, \quad (1)$$

$$\mathcal{B}(B \rightarrow Ke^\pm \tau^\mp) \simeq 2 \cdot 10^{-8} \kappa^2 \left( \frac{1 - R_K}{0.23} \right)^2, \quad (2)$$

$$\mathcal{B}(B \rightarrow K\mu^\pm \tau^\mp) \simeq 2 \cdot 10^{-8} \left( \frac{1 - R_K}{0.23} \right)^2, \quad (3)$$

predictions  $\mu$  and  $\tau$  decays:

$$\mathcal{B}(\mu \rightarrow e\gamma) \simeq 2 \cdot 10^{-12} \frac{\kappa^2}{\rho^2} \left( \frac{1 - R_K}{0.23} \right)^2, \quad (4)$$

$$\mathcal{B}(\tau \rightarrow e\gamma) \simeq 4 \cdot 10^{-14} \frac{\kappa^2}{\rho^2} \left( \frac{1 - R_K}{0.23} \right)^2, \quad (5)$$

$$\mathcal{B}(\tau \rightarrow \mu\gamma) \simeq 3 \cdot 10^{-14} \frac{1}{\rho^2} \left( \frac{1 - R_K}{0.23} \right)^2, \quad (6)$$

$$\mathcal{B}(\tau \rightarrow \mu\eta) \simeq 4 \cdot 10^{-11} \rho^2 \left( \frac{1 - R_K}{0.23} \right)^2. \quad (7)$$

predictions purely leptonic decays (asymmetric branching ratios):

$$\frac{\mathcal{B}(B_s \rightarrow \ell^+ \ell'^-)}{\mathcal{B}(B_s \rightarrow \ell^- \ell'^+)} \simeq \frac{m_\ell^2}{m_{\ell'}^2} \quad \text{assuming left-handed leptons only} \quad (8)$$

$$\frac{\mathcal{B}(B_s \rightarrow \mu^+ e^-)}{\mathcal{B}(B_s \rightarrow \mu^+ \mu^-)_{\text{SM}}} \simeq 0.01 \kappa^2 \cdot \left( \frac{1 - R_K}{0.23} \right)^2, \quad (9)$$

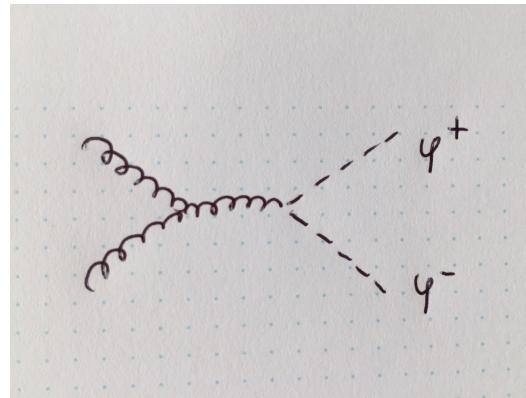
$$\frac{\mathcal{B}(B_s \rightarrow \tau^+ e^-)}{\mathcal{B}(B_s \rightarrow \mu^+ \mu^-)_{\text{SM}}} \simeq 4 \kappa^2 \cdot \left( \frac{1 - R_K}{0.23} \right)^2, \quad (10)$$

$$\frac{\mathcal{B}(B_s \rightarrow \tau^+ \mu^-)}{\mathcal{B}(B_s \rightarrow \mu^+ \mu^-)_{\text{SM}}} \simeq 4 \cdot \left( \frac{1 - R_K}{0.23} \right)^2, \quad (11)$$

## 4. Producing LQs at the LHC

Pair production, e.g. recent works Bastian Diaz, Martin Schmaltz, Yi-Ming Zhong

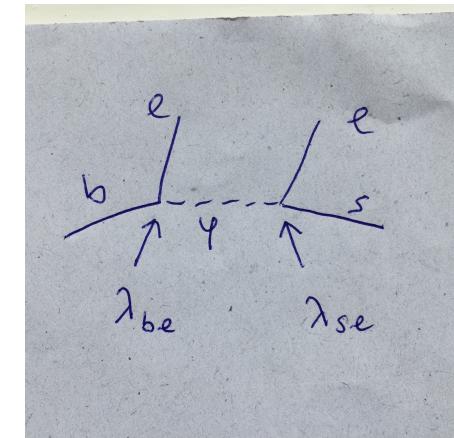
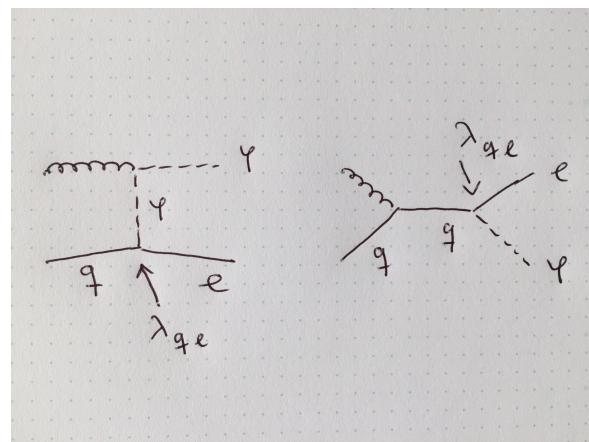
1706.05033  $\sigma(pp \rightarrow \varphi^+ \varphi^-) \propto \alpha_s^2$



Single LQ production from  $b$ -anomalies GH, Dennis Loose, Ivan Nisandzic, DO-TH

17/27, in preparation in association with a lepton  $\sigma(pp \rightarrow \varphi l) \propto |\lambda_{ql}|^2 \alpha_s$

depends on flavor



- We discussed flavor in the SM. Its parameters are known, and to date – modulo anomalies – all observed flavor and CP violation is consistent with them. – Very predictive
- There are strong flavor constraints for model building: In the absence of O(1) New Physics observations in FCNC-processes implies that physics at the TeV-scale has non-generic flavor properties, and suppression mechanisms of similar power as the SM ones need to be at work.
- Several avenues exist to improve reach: employing fits and correlations, and using observables designed to have small SM backgrounds.

- Current anomalies – LNU in quark decays – inspired new bottom-up model building Leptoquarks,  $Z'$
- Understanding LNU anomalies involves measurements at LHCb, B-Factories, Belle II and direct searches, ATLAS, CMS.
- Great prospects to link with direct searches. → see talk on leptoquarks at the LHC by Dennis Loose in Exotics session
- Linking lepton to quark physics may provide opportunities towards the understanding of flavor.