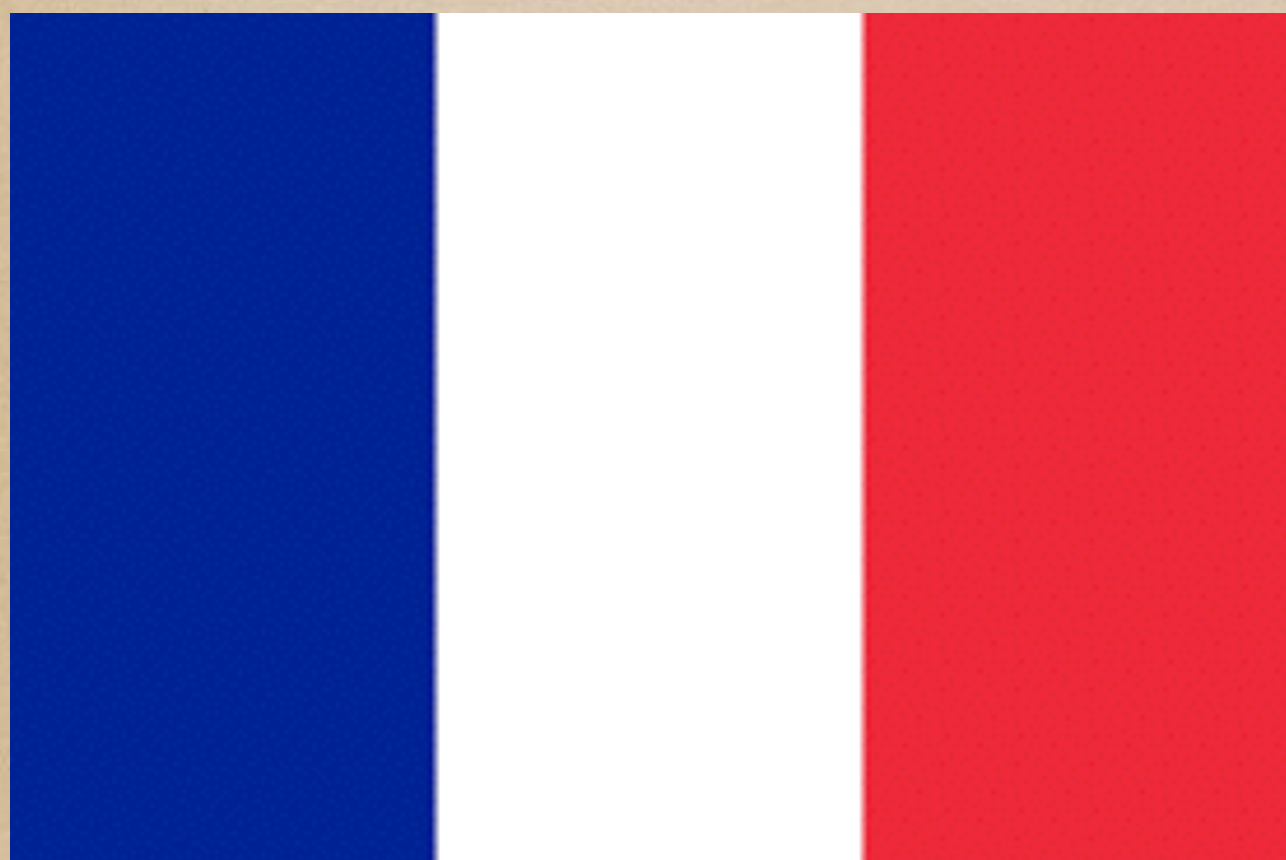


Thermal DM beyond 10-100 TeV



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DESY - Hamburg
Supervised by Geraldine Servant

J+2 after WC 2018
20 year after WC 1998



With the collaboration of Filippo Sala, Kallia Petrakí and Marco Cirelli.

Cargèse 2018

The Dark $U(1)$ model

Dark Matter:

$$\bar{\psi}_D i (\not{\partial} + ig_D \not{V}_D) \psi_D - m_{DM} \bar{\psi}_D \psi_D$$

Dark photon:

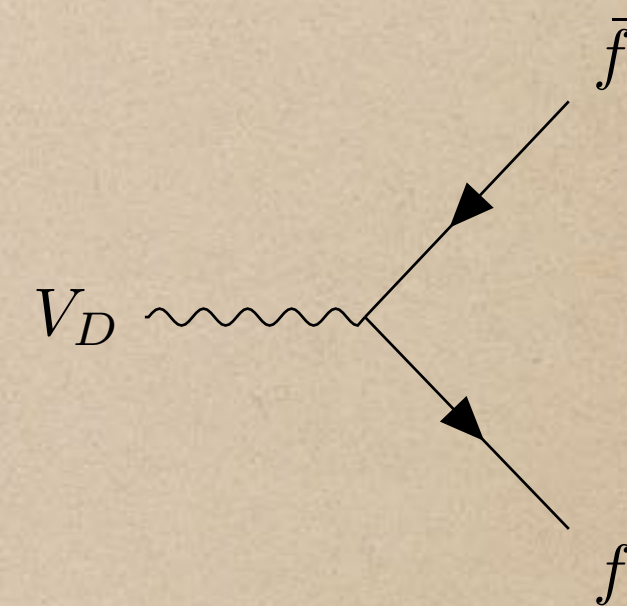
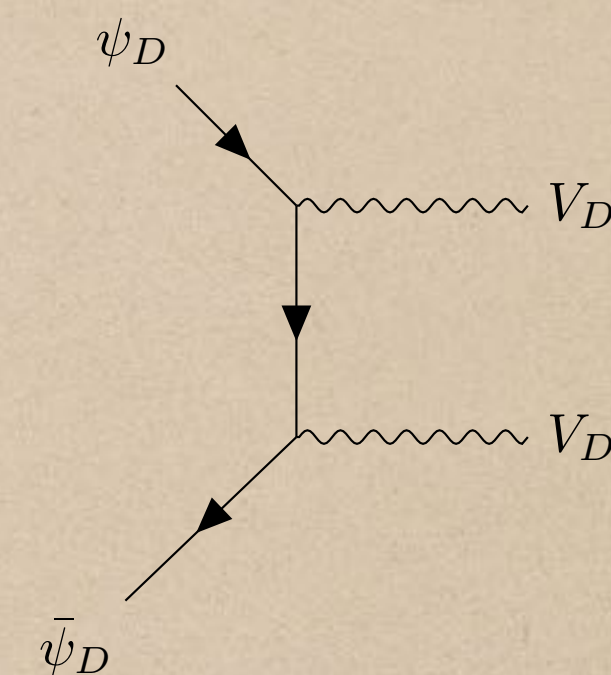
$$-\frac{1}{4} F_{D\mu\nu} F_D^{\mu\nu} - \frac{1}{2} m_{V_D}^2 V_{D\mu} V_D^\mu$$

Kinetic coupling to SM:

$$\frac{\epsilon}{c_w} B_{\mu\nu} F_D^{\mu\nu}$$

4 parameters:

$$m_{DM}, m_{V_D}, \alpha_D, \epsilon$$

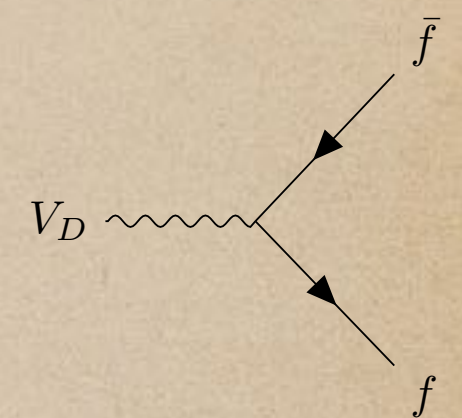


Motivation: current and planned telescopes have the ability to constrain Thermal DM with mass $O(100 \text{ TeV})$ and beyond.

Challenges:

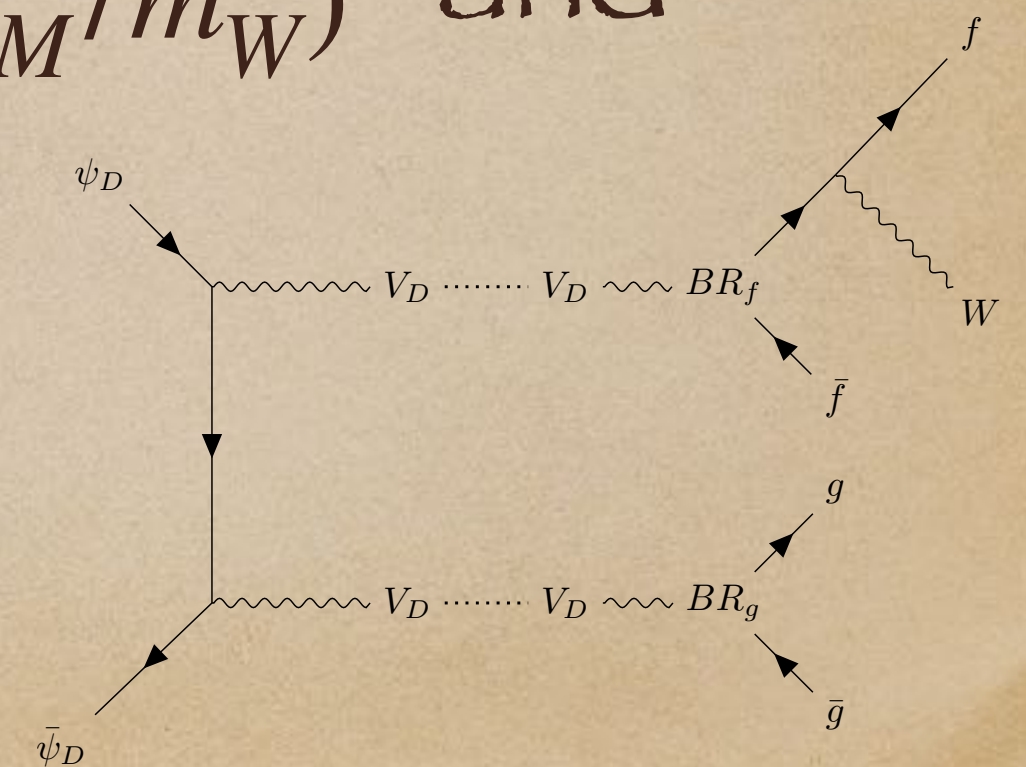
1. Unitarity bound constrains DM mass to be lower than $O(100 \text{ TeV})$

Solution: entropy dilution due to mediator decay



2. Electroweak radiations corrections scales as $\frac{\alpha_w}{2\pi} \log^2(m_{DM}^2/m_W^2)$ and are non-perturbative when $m_{DM} > 100 \text{ TeV}$.

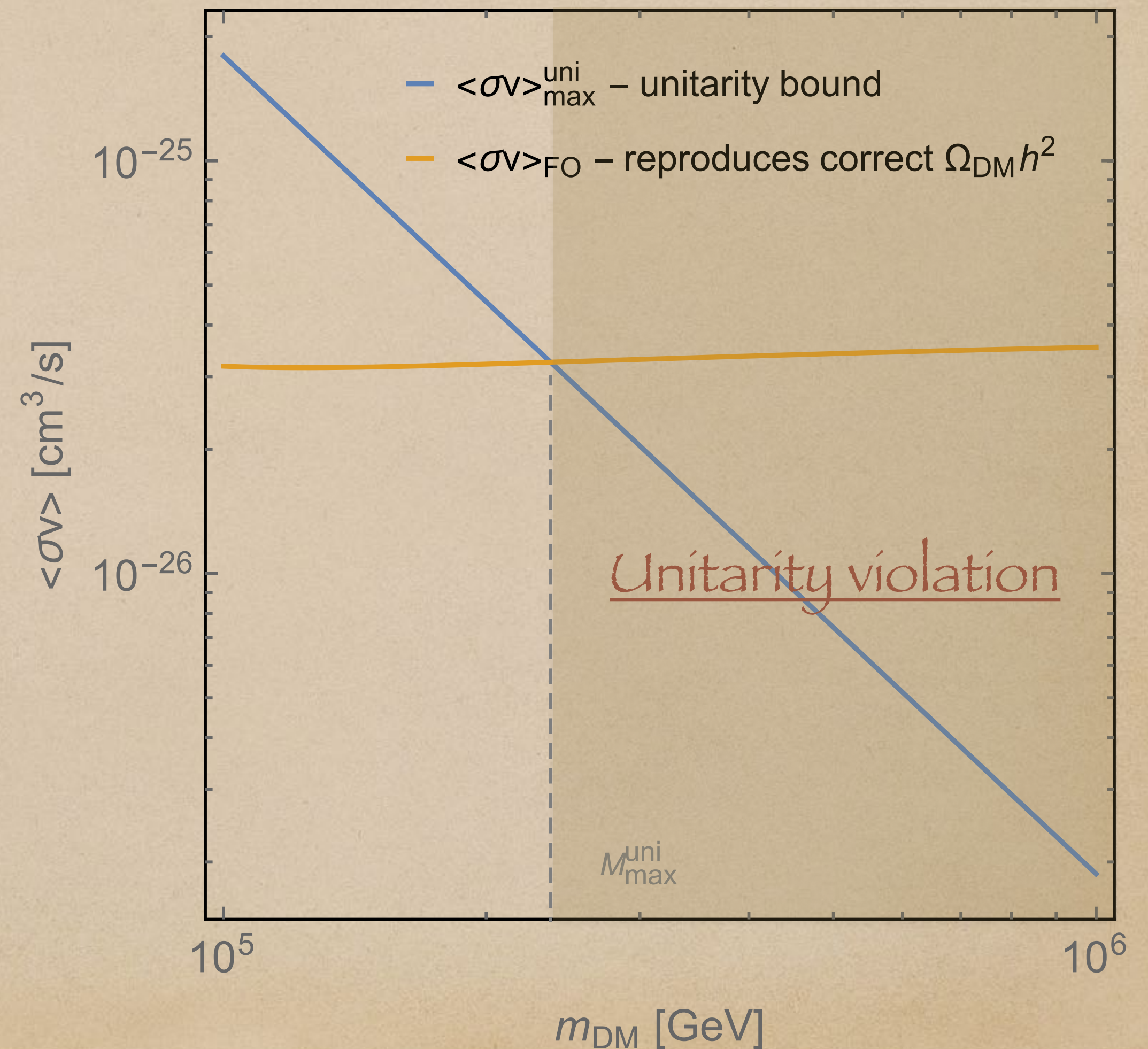
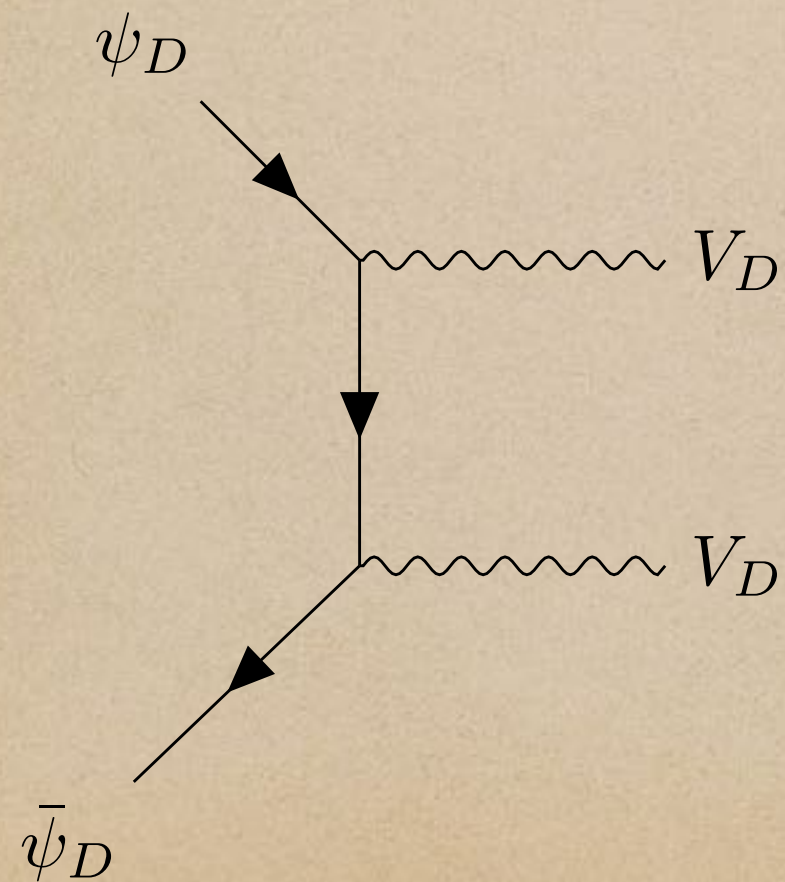
Solution: With a mediator it scales as $\frac{\alpha_w}{2\pi} \log^2(m_{V_D}^2/m_W^2)$



The Unitarity Bound

$$SS^\dagger = 1 \quad \rightarrow \quad \langle \sigma_{ine} v_{rel} \rangle_J < \frac{4\pi(2J+1)}{m_{DM}^2 v_{rel}}$$

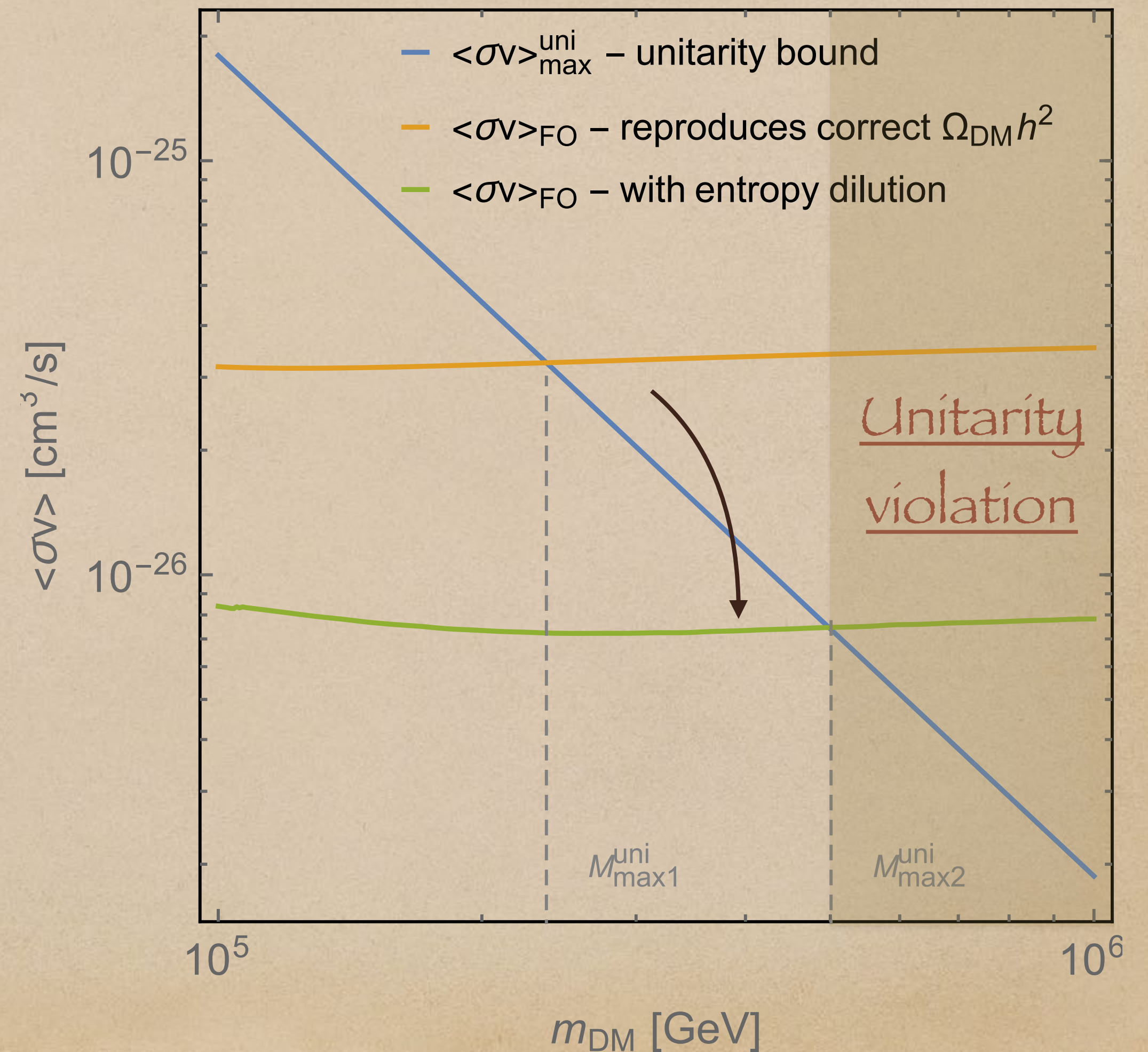
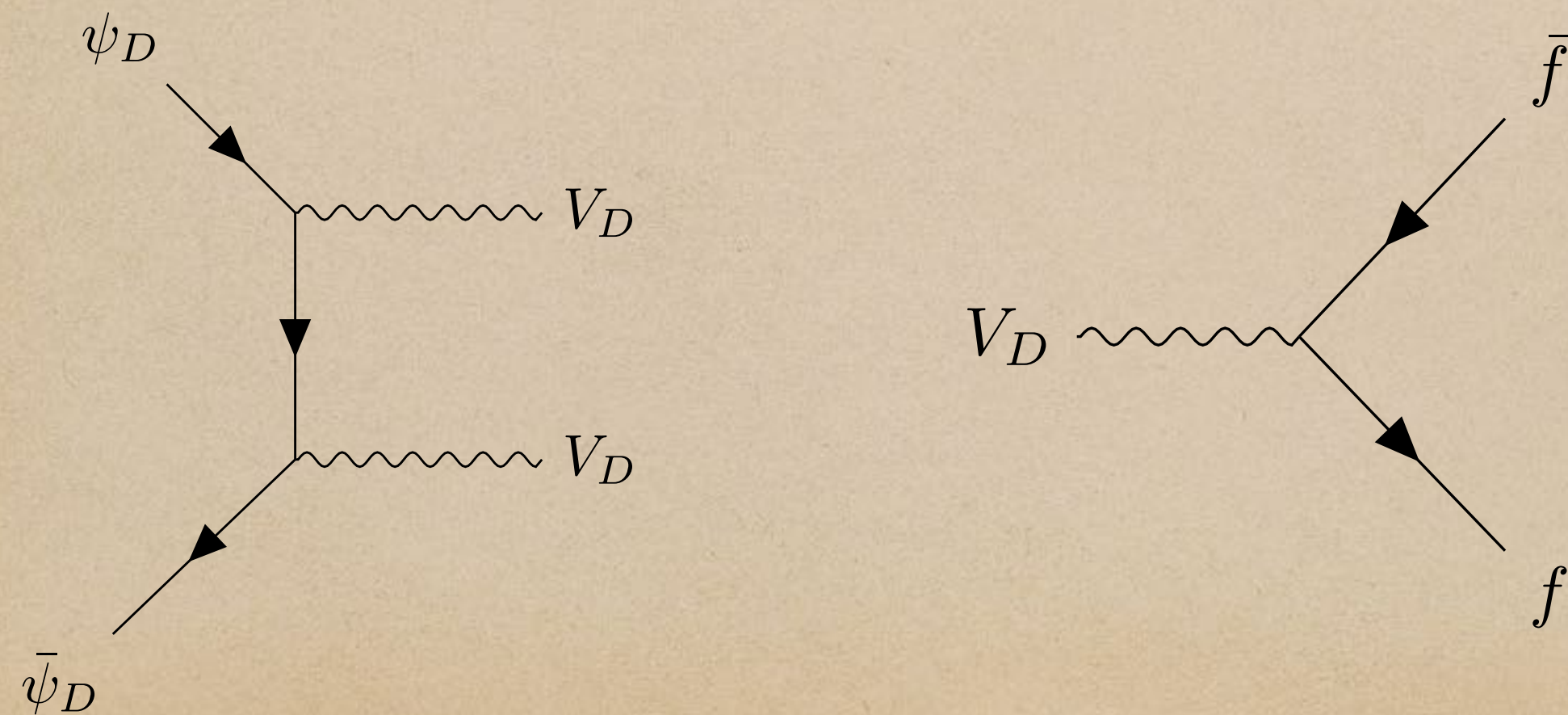
$$\rightarrow m_{DM}^{max} \approx 140 \text{ TeV}$$



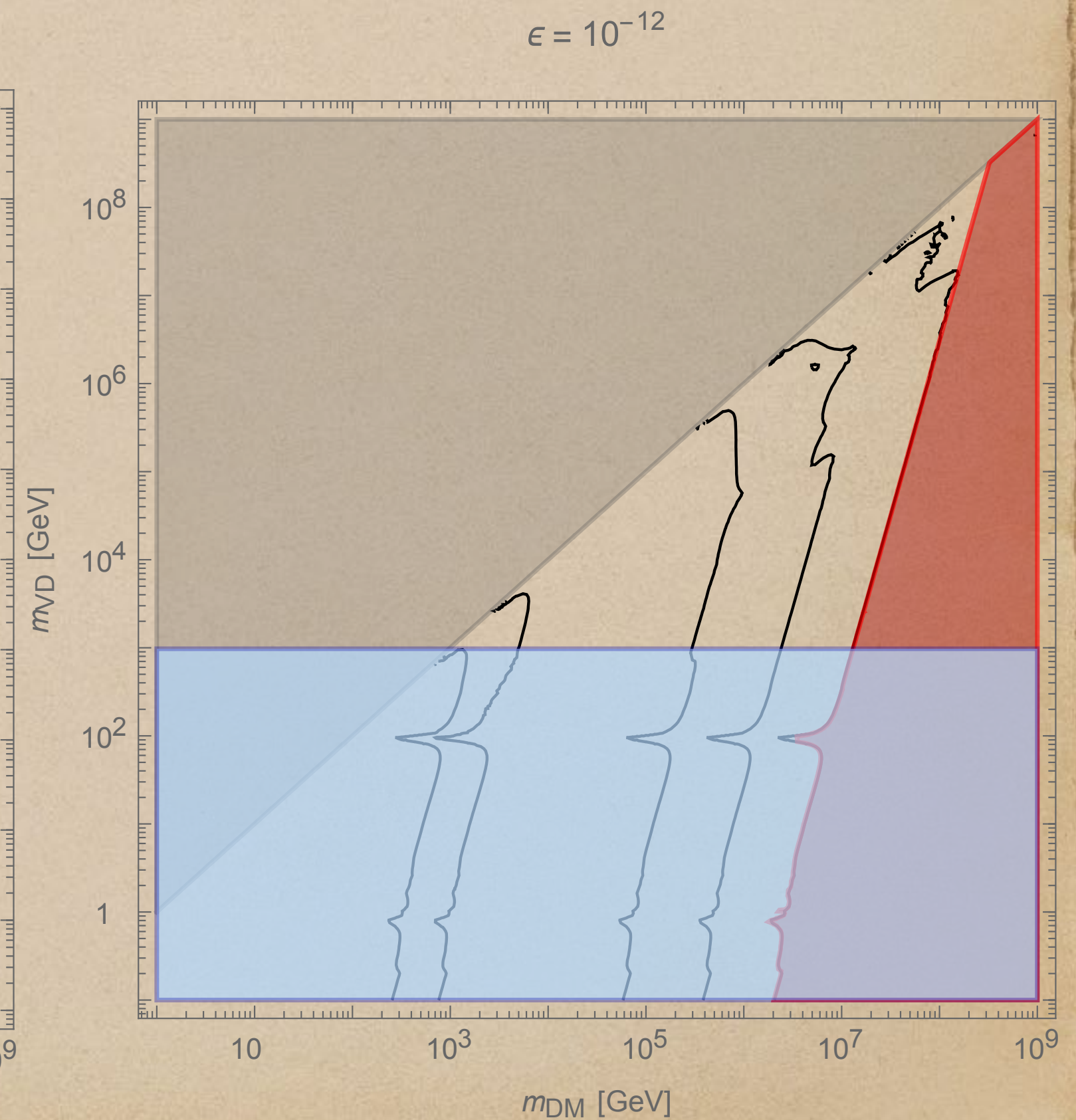
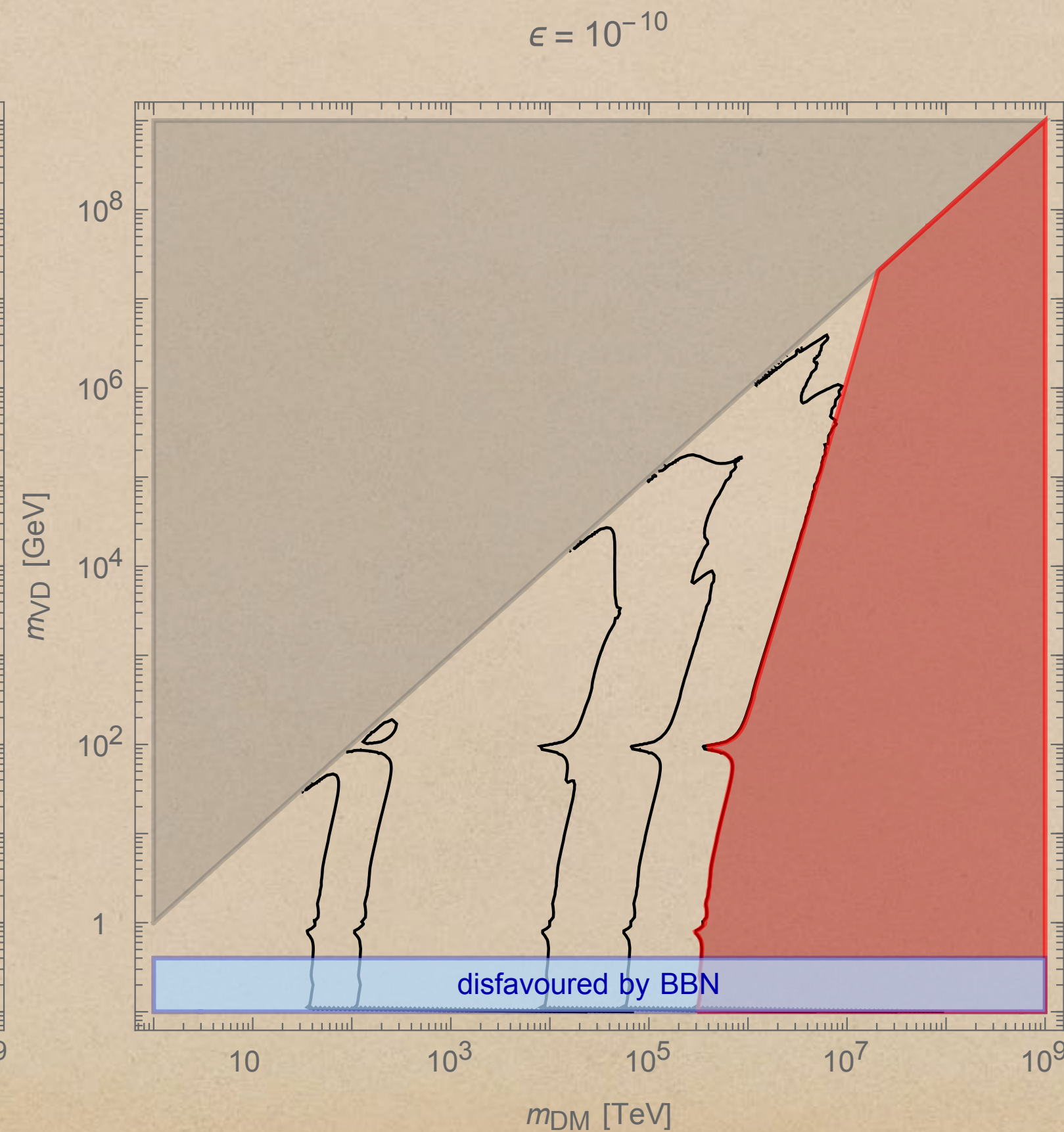
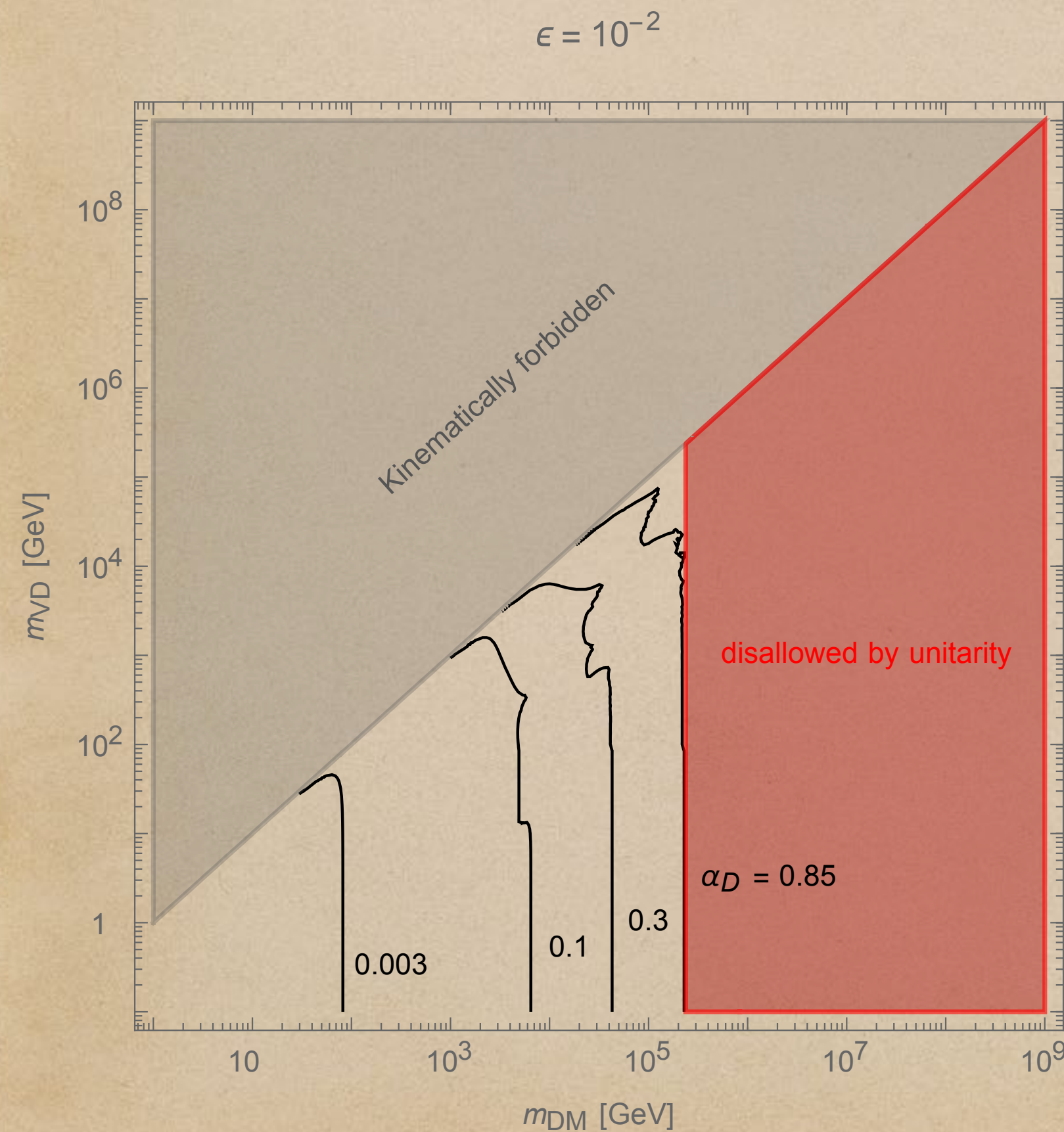
The Unitarity Bound

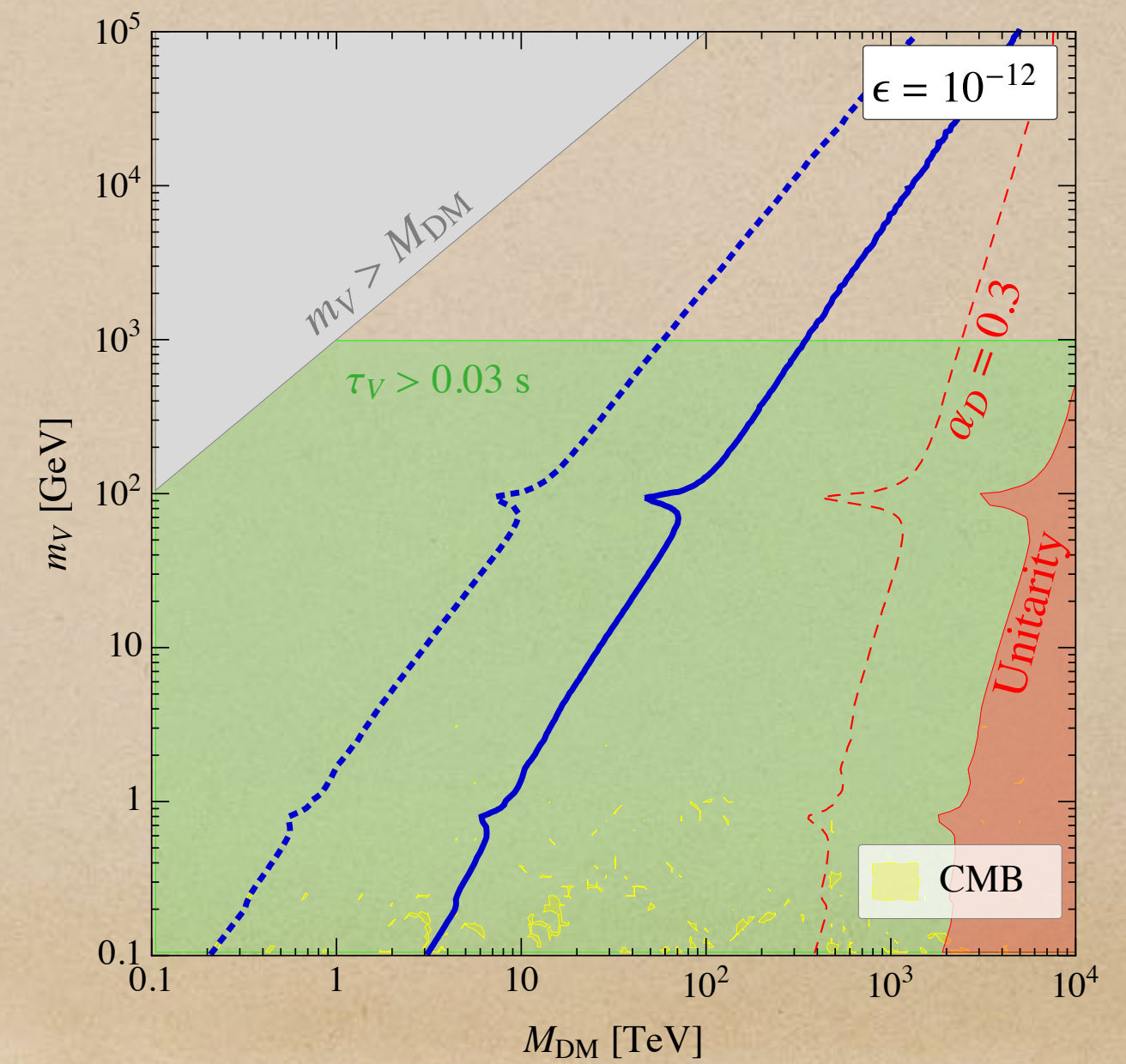
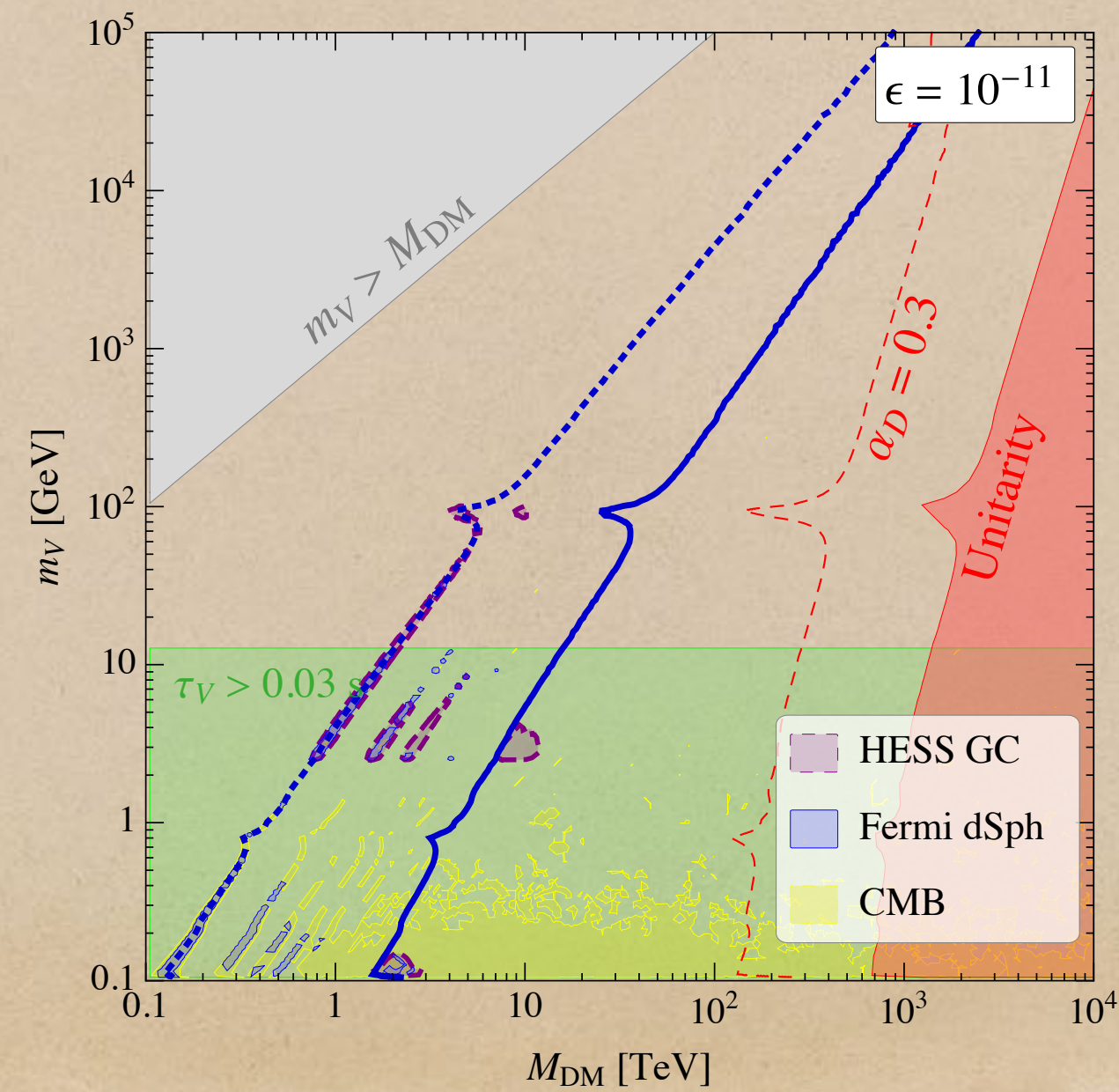
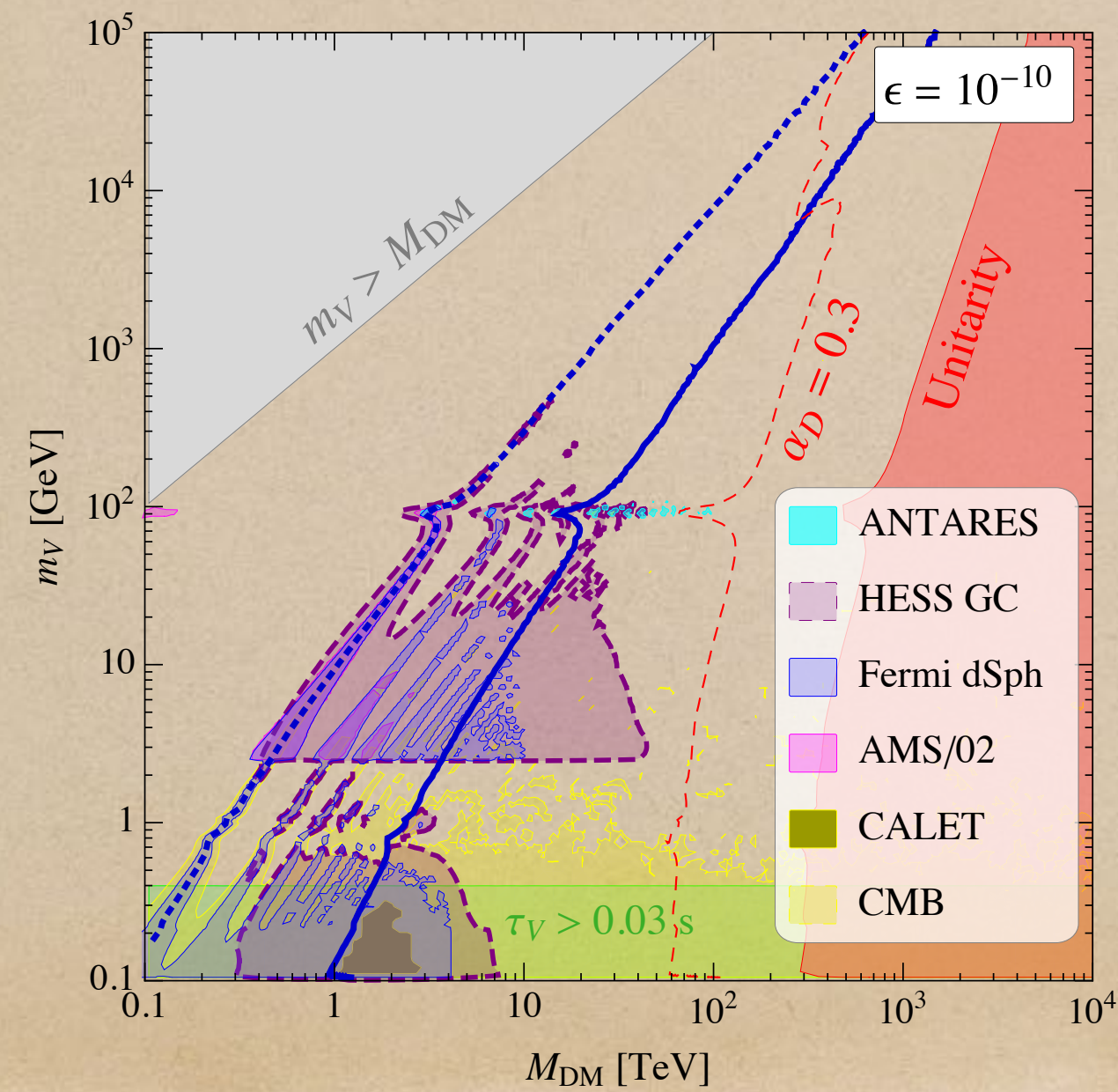
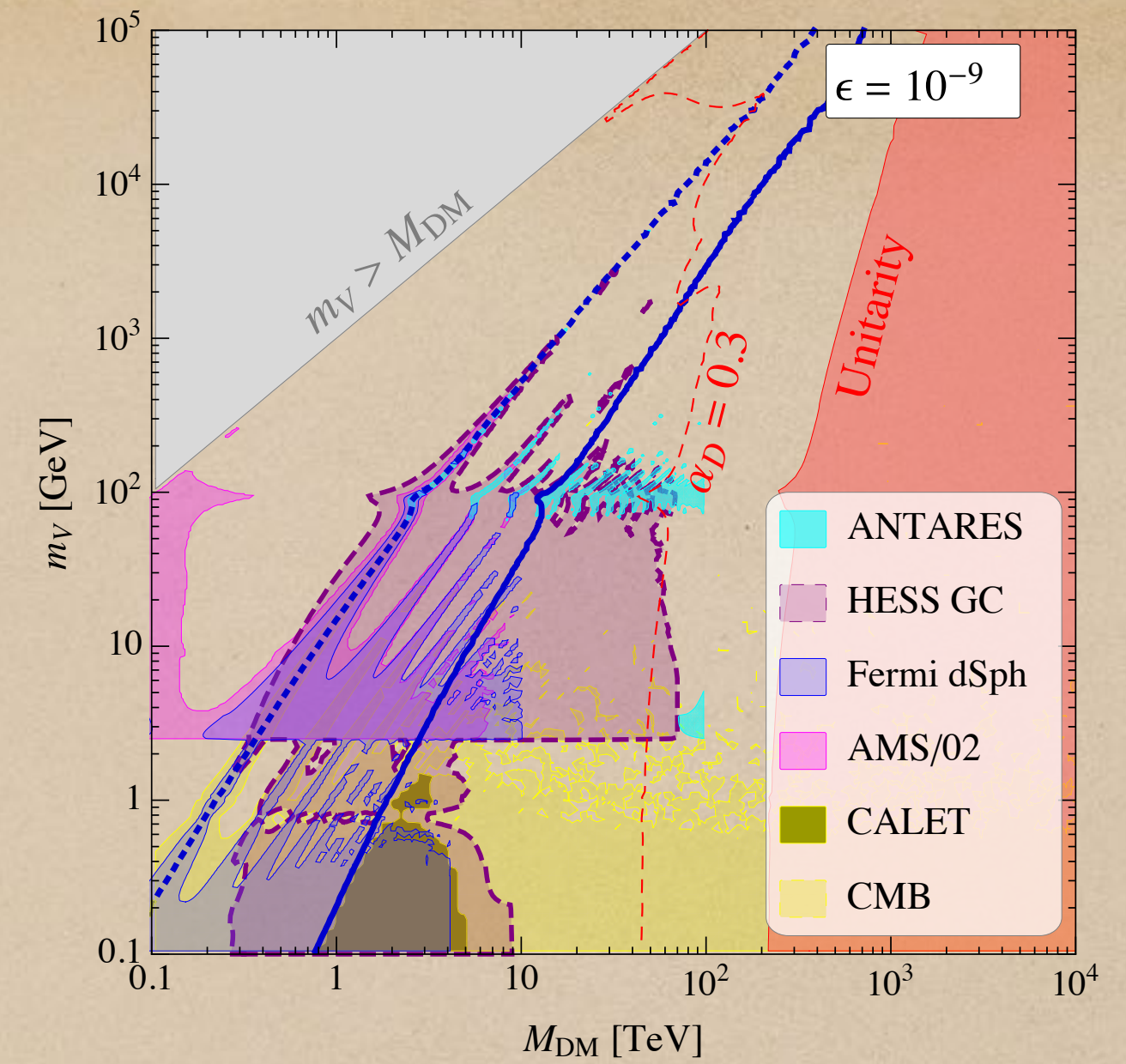
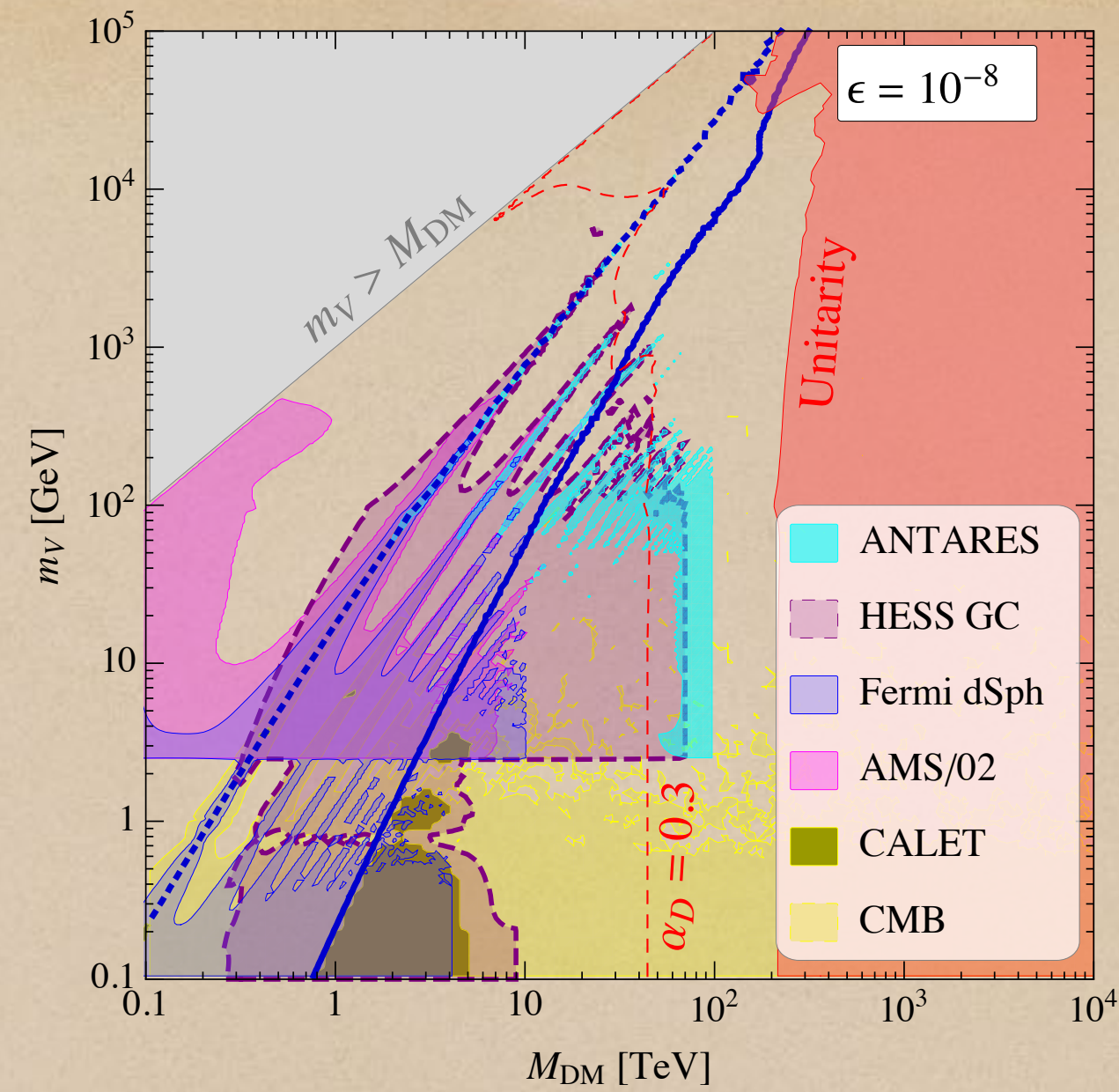
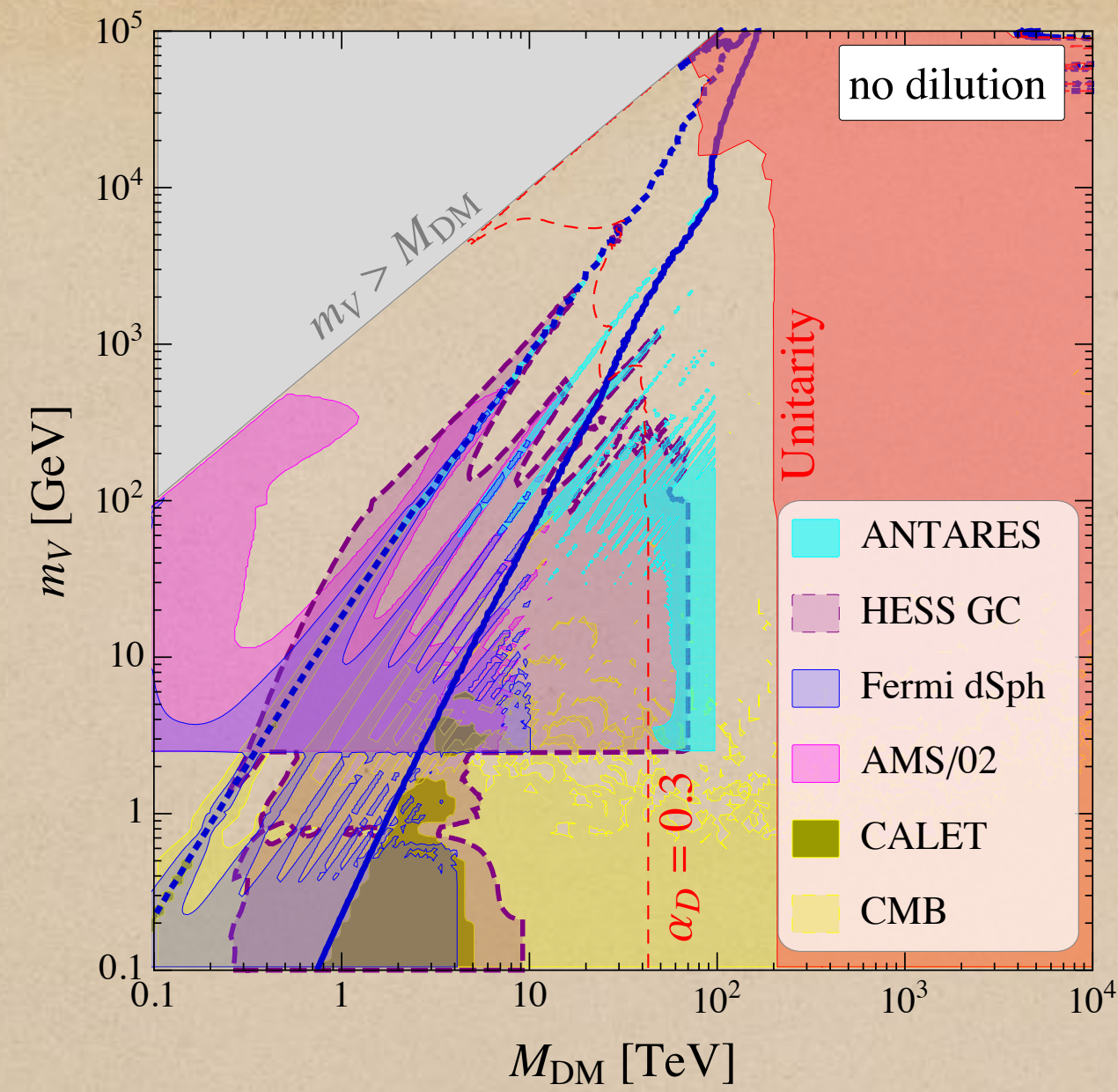
$$SS^\dagger = 1 \quad \rightarrow \quad \langle \sigma_{ine} v_{rel} \rangle_J < \frac{4\pi(2J+1)}{m_{DM}^2 v_{rel}}$$

$$\rightarrow m_{DM}^{max} \approx 140 \text{ TeV}$$



Consequences of the entropy dilution

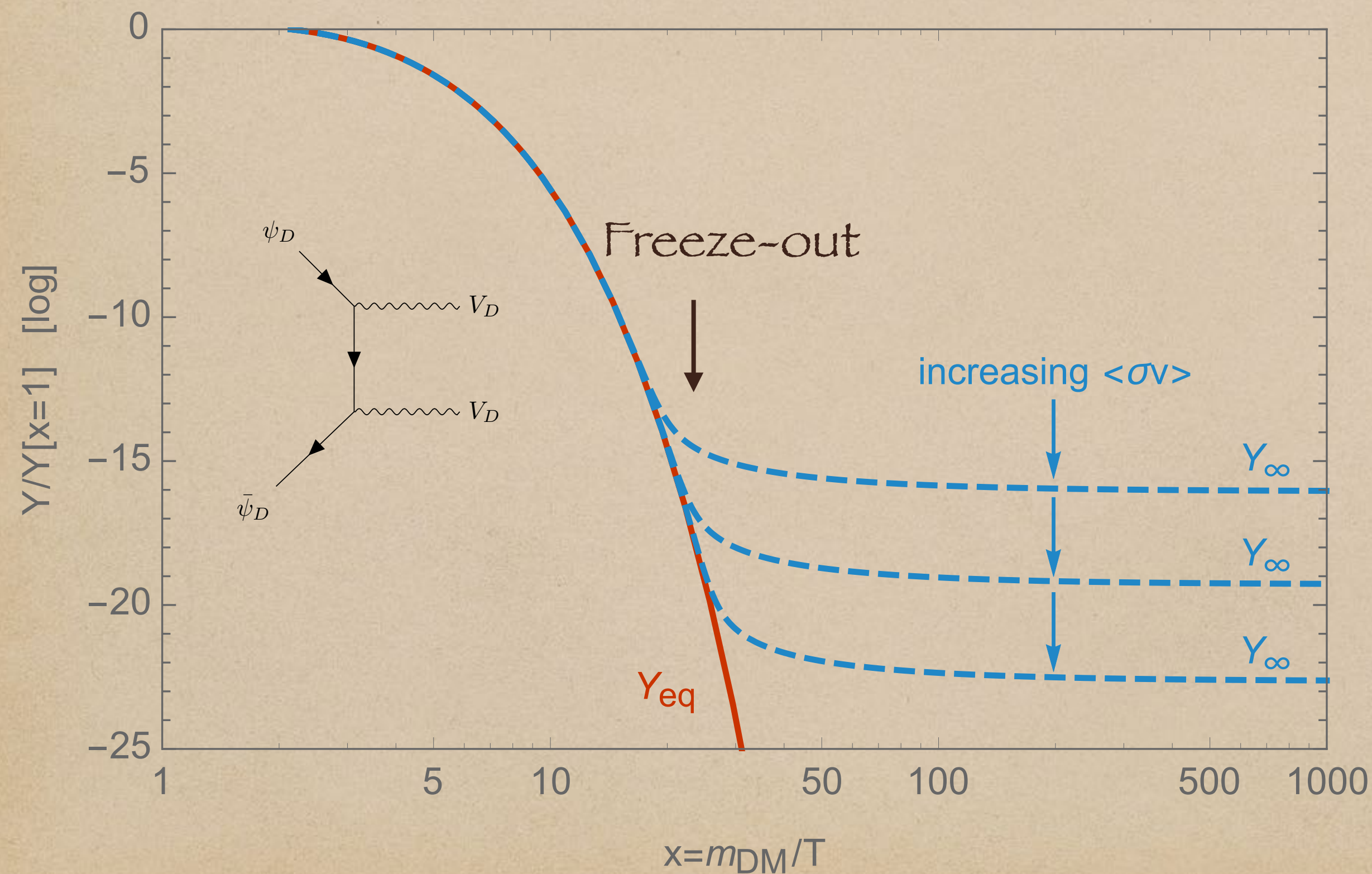




Back-up slides

Thermal Dark Matter

Assume thermal equilibrium between DM and SM at Early times

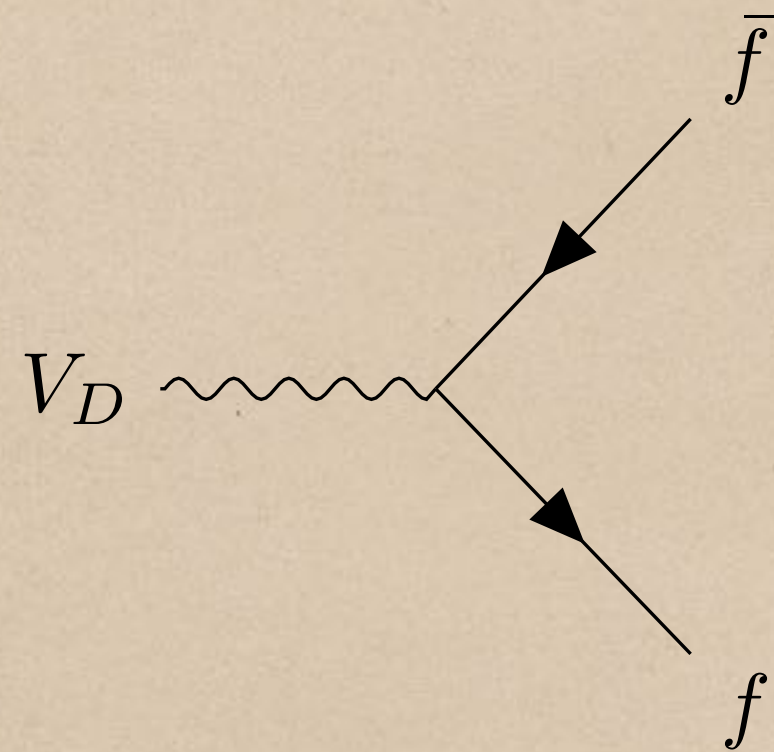


DM relic abundance today:

$$\Omega_{DM} h^2 = 0.1186 \quad (\text{Planck})$$

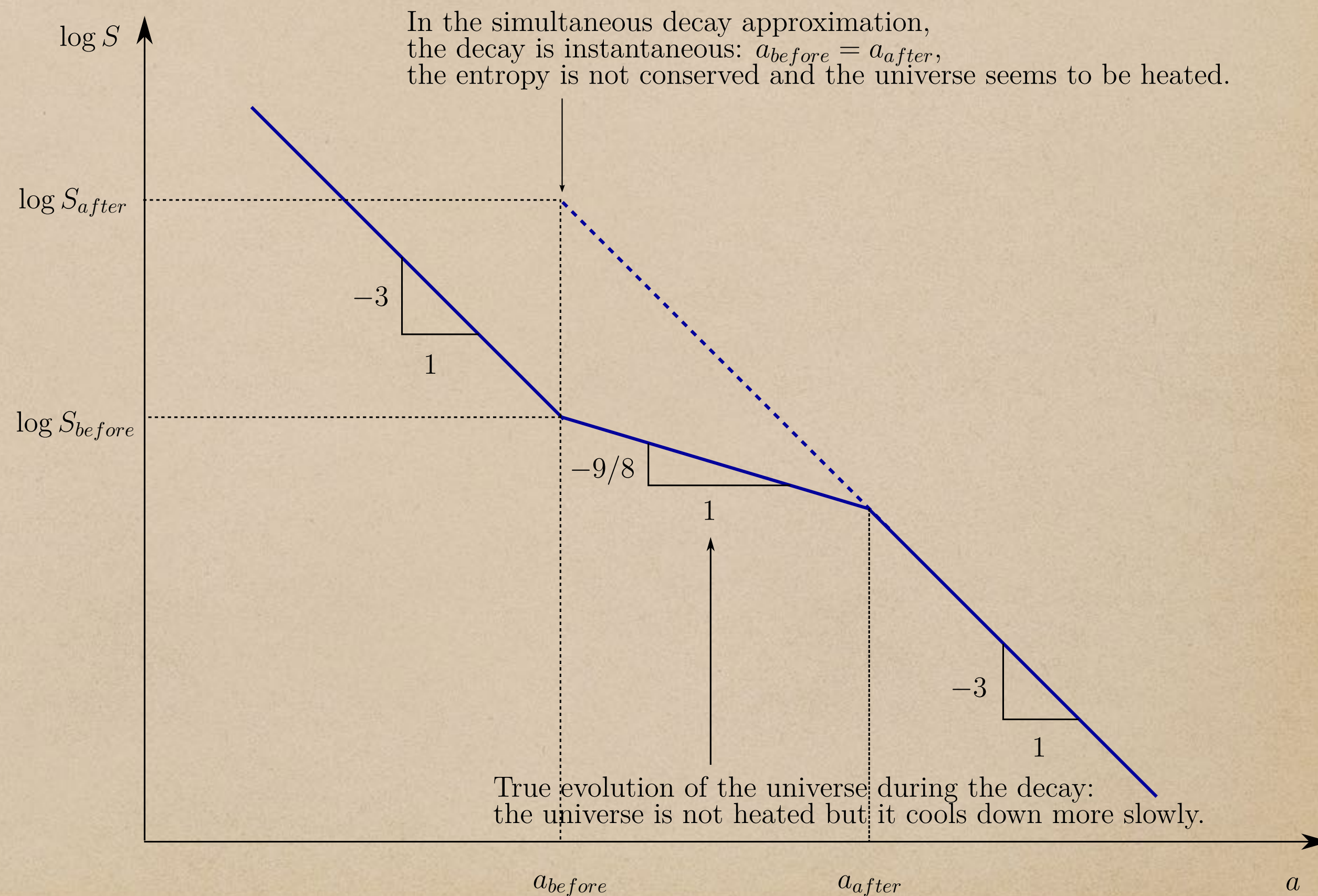
$$\rightarrow \langle \sigma_{ann} v \rangle \sim 3 \times 10^{-26} \text{ cm}^3/\text{s}$$

The entropy dilution



$\underbrace{\rho_{NR}^{V_D}}_{\text{non-contributing to } S} \rightarrow \underbrace{\rho_{rel}^{SM}}_{\text{contributing to } S}$

$$S_{SM} \rightarrow D S_{SM} \rightarrow m_{DM}^{max} \rightarrow \sqrt{D} m_{DM}^{max}$$

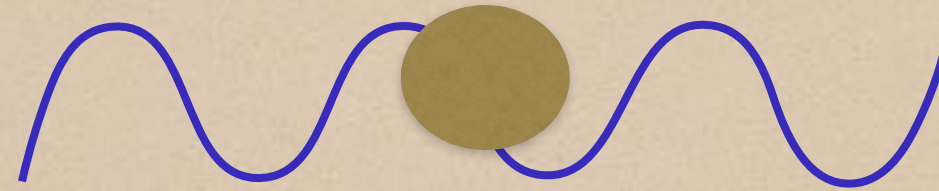


The Sommerfeld enhancement

With short range potential:



$$\psi_0(\vec{r}) = e^{i\vec{k} \cdot \vec{r}}$$

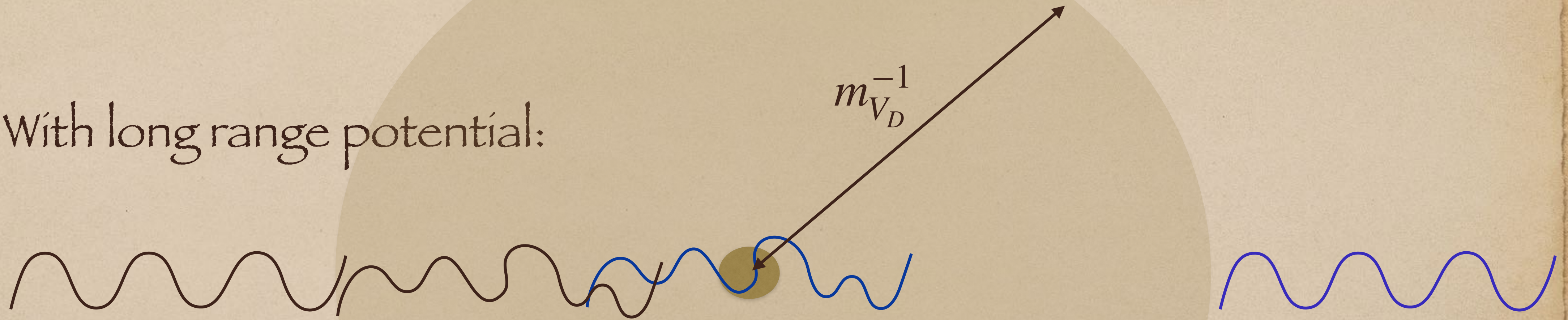


$$H_{ann} = U_{ann} \delta(\vec{r})$$

Interaction rate proportional to: $|\psi_0(0)|^2 = 1$

The Sommerfeld enhancement

With long range potential:



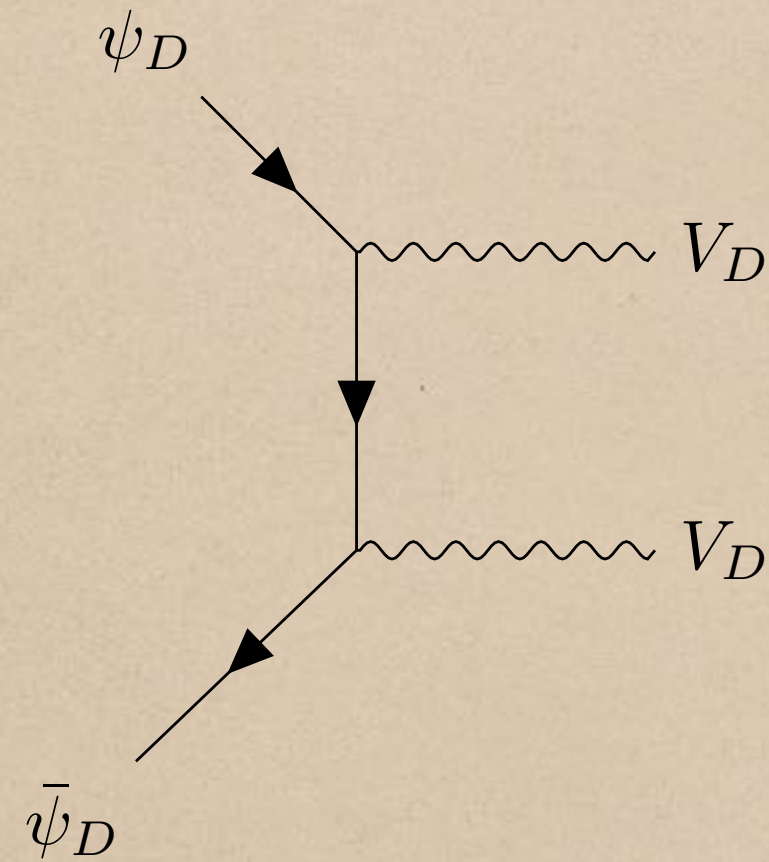
$$\psi(\vec{r}) \neq e^{i\vec{k}\cdot\vec{r}}$$

$$H = H_{ann} - \alpha \frac{e^{-m_{V_D} r}}{r}$$

Interaction rate proportional to: $|\psi(0)|^2 > 1$

Annihilation cross-section: $\sigma_{ann} \rightarrow \sigma_{ann} S_{ann}$ with $S_{ann} = \left| \frac{\psi(0)}{\psi_0(0)} \right|^2$

The Sommerfeld enhancement



$$\sigma_{ann} \rightarrow \sigma_{ann} S_{ann}$$

with

$$S_{ann} = 2\pi \frac{\alpha}{v} \frac{1}{1 - e^{-2\pi \frac{\alpha}{v}}} \quad \begin{array}{l} \xrightarrow{\frac{\alpha}{v} \rightarrow 0} 1 \\ \xrightarrow{\frac{\alpha}{v} \gg 1} 2\pi \frac{\alpha}{v} \end{array}$$

After freeze-out: $v \sim 0.3 \rightarrow 0.01$

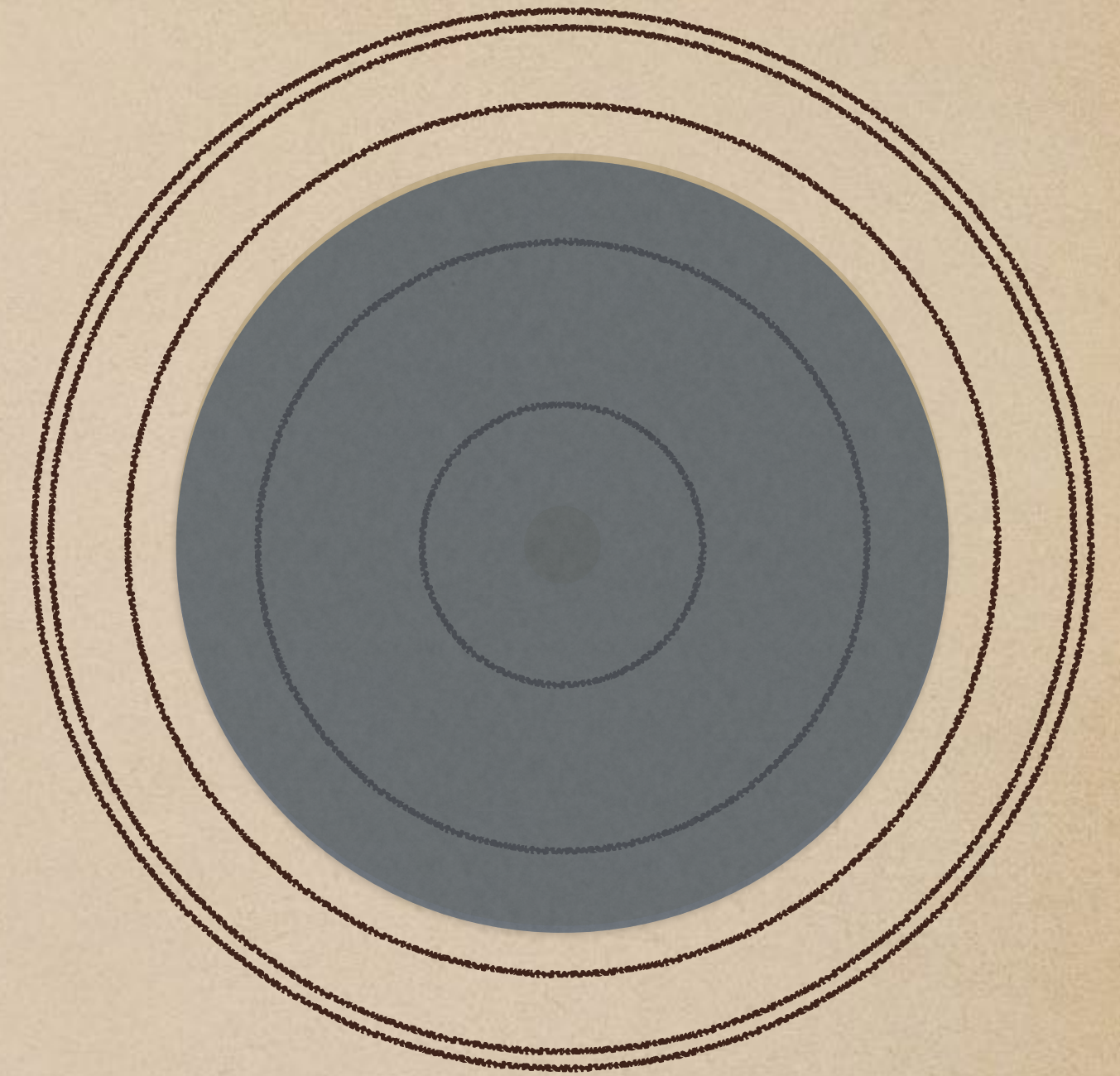
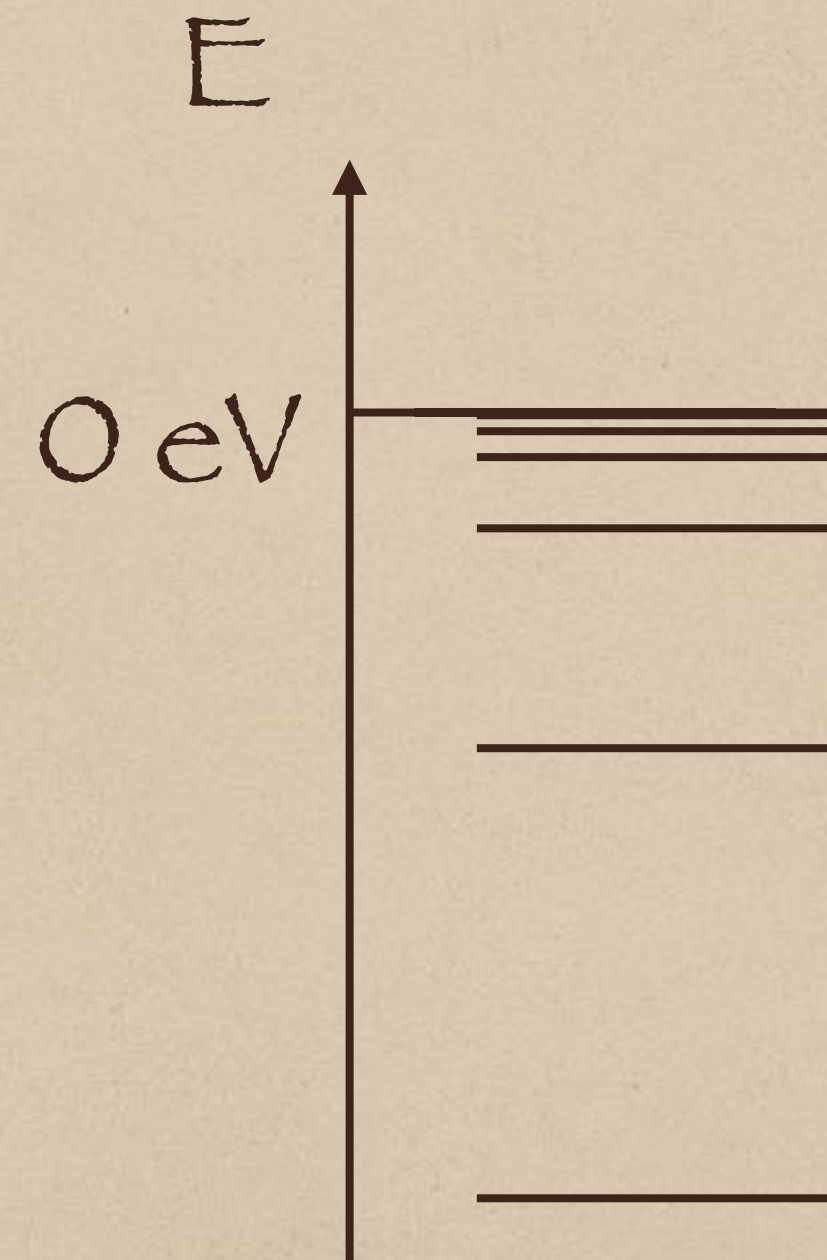
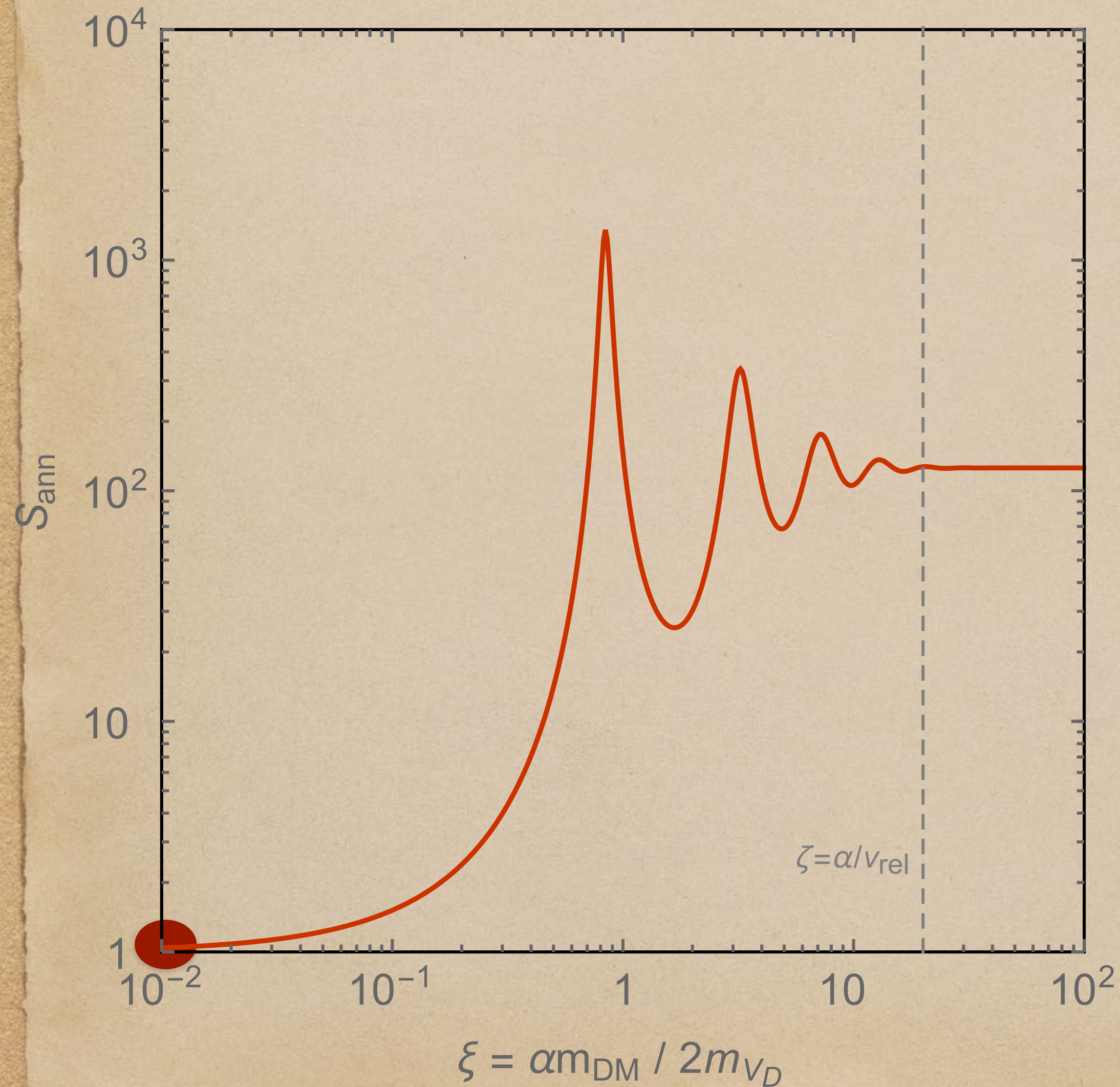
Extend DM annihilation after standard freeze-out


In Milky-Way: $v \sim 10^{-3}$


Boost collected cosmic rays fluxes on Earth


In Dwarf: $v \sim 5 \times 10^{-5}$

Resonance structures



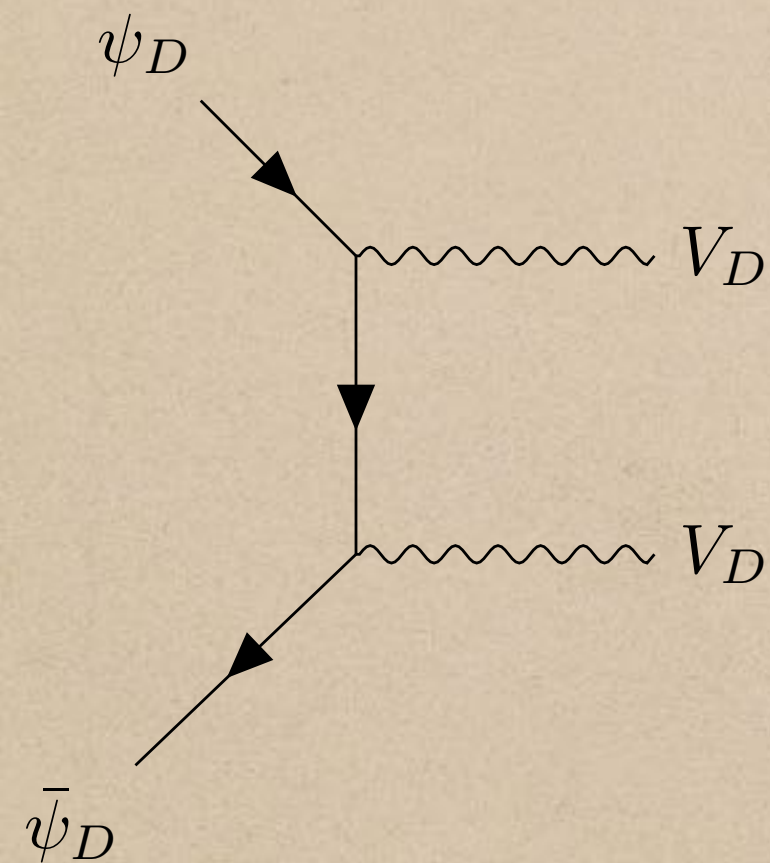
Bound state size $\alpha m_{\text{DM}}^{-1}$: 

Yukawa sphere $m_{V_D}^{-1}$: 

De Broglie sphere $m_{\text{DM}} v_{\text{rel}}^{-1}$: 

Bound State Formation

If the mediator range $m_{V_D}^{-1}$ is bigger than the size of the would-be bound state $(\alpha_D m_{DM})^{-1}$, we can form DM bound state



$$\sigma_{ann} = \sigma_{ann} S$$

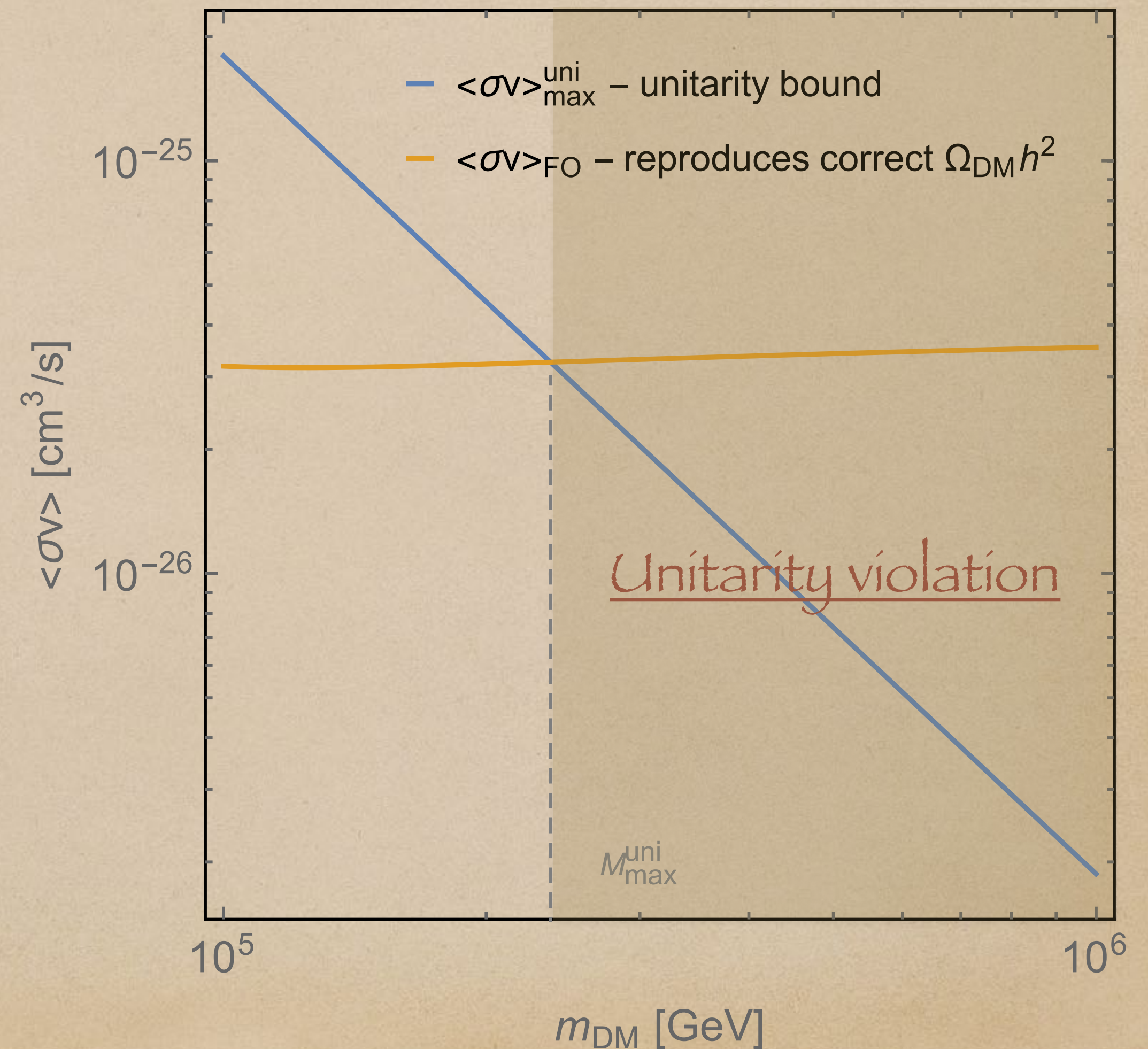
with

$$S = S_{ann} + S_{BSF}$$

The Unitarity Bound

$$SS^\dagger = 1 \quad \rightarrow \quad \langle \sigma_{ine} v_{rel} \rangle_J < \frac{4\pi(2J+1)}{m_{DM}^2 v_{rel}}$$

$$\rightarrow m_{DM}^{max} \approx 140 \text{ TeV}$$



The Unitarity Bound

$$SS^\dagger = 1 \quad \rightarrow \quad \langle \sigma_{\text{ine}} v_{\text{rel}} \rangle_J < \frac{4\pi(2J+1)}{m_{\text{DM}}^2 v_{\text{rel}}}$$

$$\rightarrow m_{\text{DM}}^{\text{max}} \approx 140 \text{ TeV}$$

With entropy dilution:

$$\begin{aligned} S_{\text{SM}} \rightarrow D S_{\text{SM}} &\rightarrow Y_\infty \rightarrow Y_\infty/D \\ &\rightarrow \langle \sigma_{\text{ann}} v_{\text{rel}} \rangle \rightarrow \langle \sigma_{\text{ann}} v_{\text{rel}} \rangle / D \\ &\rightarrow m_{\text{DM}}^{\text{max}} \rightarrow \sqrt{D} m_{\text{DM}}^{\text{max}} \end{aligned}$$

