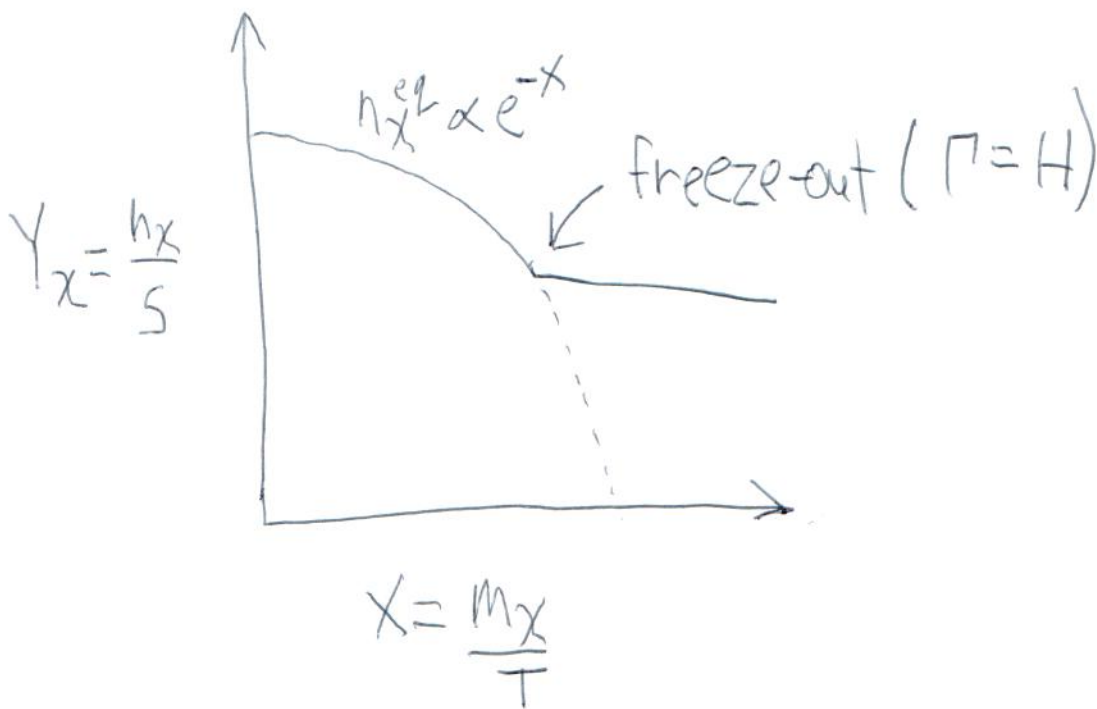


II Beyond WIMPs

PLAN

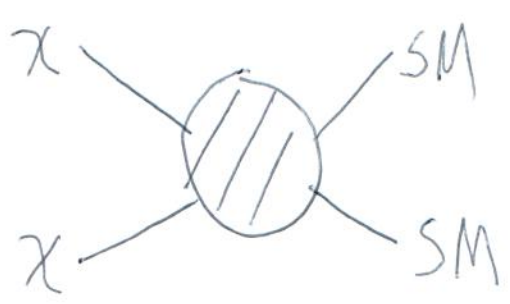
- I $2 \rightarrow 2$ Zoology
- II Thermal Relics Beyond $2 \rightarrow 2$
- III Non-Thermal DM

thermal relic



I 2 → 2 Zoology

WIMP



$$\langle \sigma v \rangle \sim \frac{1}{T_{eq} \cdot M_{pl} \langle \sigma v \rangle}$$

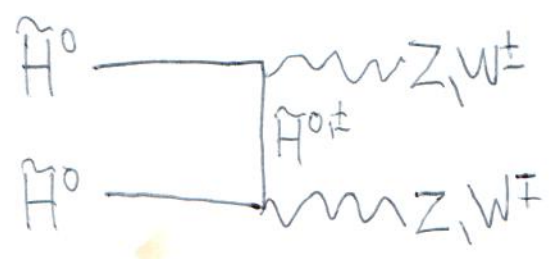
$$\dot{n}_\chi + 3H n_\chi = -\langle \sigma v \rangle (n_\chi^2 - (n_\chi^{eq})^2)$$

$$n \langle \sigma v \rangle \approx H \quad \Omega_\chi \sim \frac{1}{T_{eq} \cdot M_{pl} \langle \sigma v \rangle}$$

$m_\chi \sim \alpha \sqrt{T_{eq} \cdot M_{pl}}$

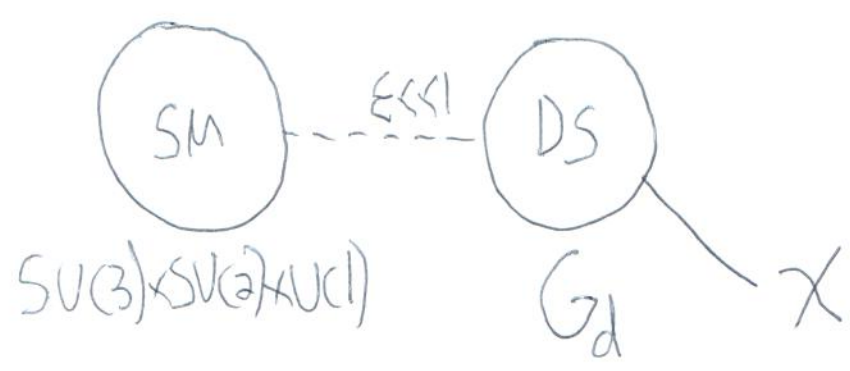
ex) $\tilde{H} = (1, 2)_{\pm \frac{1}{2}}$
 $\tilde{W} = (1, 3)_0$

$M_{\tilde{H}} \approx 1.1 \text{ TeV}$
 $m_{\tilde{W}} \approx 3 \text{ TeV}$



Minimal DM hep-ph/0512090

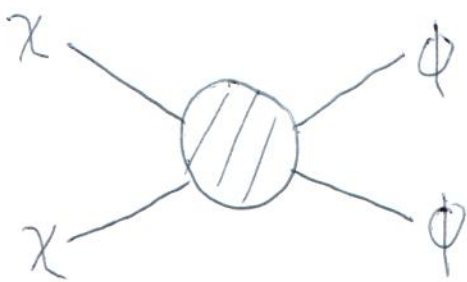
Dark Sector



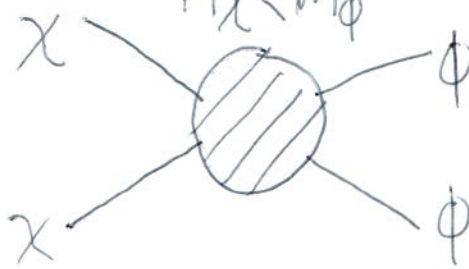
$2 \rightarrow 2$ Variations

3

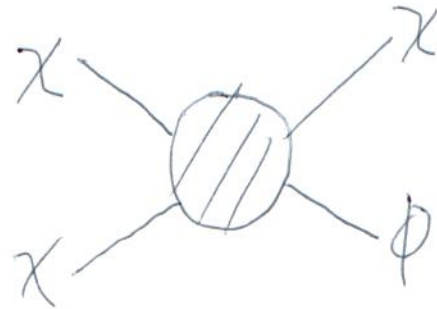
WIMP



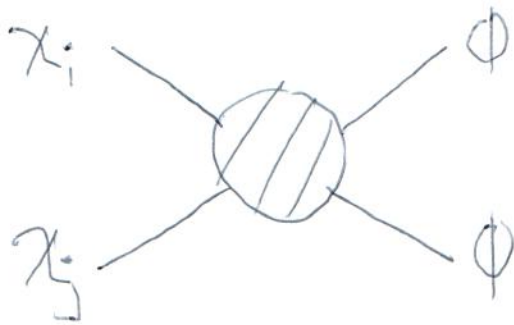
Forbidden
 $m_\chi < m_\phi$



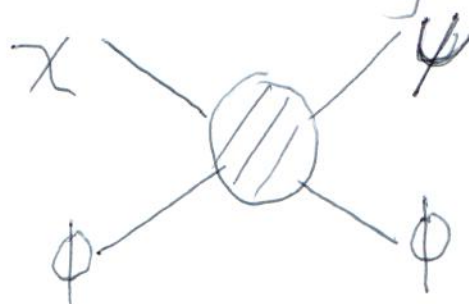
Semi-annihilation



Coannihilations

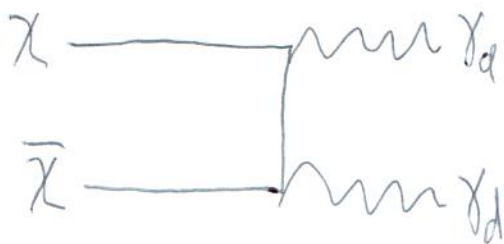


Co-scattering



WIMP w/ dark annihilations

$$G_d = U(1)_d$$



$$\langle \sigma v \rangle \approx \frac{\pi \alpha_d^2}{m_\chi^2} \frac{1}{m_\chi^2} \sim \frac{1}{T_{eq} \cdot M_{Pl}}$$

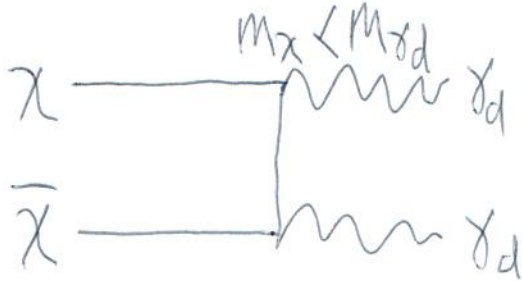
$$m_\chi \sim \alpha_d \sqrt{T_{eq} \cdot M_{Pl}} \sim \left(\frac{\alpha_d}{\alpha_w} \right) \times 1 \text{ TeV}$$

• can couple to SM through kinetic mixing

Forbidden DM

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- D'Agholo + JTR 1505.07107
- Griest + Seckel 1991



$$\langle \sigma V \rangle_{\chi\bar{\chi}} \sim \frac{1}{T_{\text{eq}} M_{\text{Pl}}}$$

- thermal average: (hep-ph/0310123 app. A)

$$\langle \sigma V \rangle_{\chi\bar{\chi}} = \frac{1}{(n_{\chi}^{\text{eq}})^2} \int d\vec{p}_\chi d\vec{p}_{\bar{\chi}} f_\chi f_{\bar{\chi}} \int d\vec{p}_{\chi d_1} d\vec{p}_{\chi d_2} |M|^2 \times (2\pi)^4 \delta^4(p_\chi + p_{\bar{\chi}} - p_{\chi d_1} - p_{\chi d_2})$$

$$d\vec{p}_i = \frac{d^3 p_i}{2 E_i (2\pi)^3}$$

- trick: detailed balance



$$(n_{\chi}^{\text{eq}})^2 \langle \sigma V \rangle_{\chi\bar{\chi}} = (n_{\chi_d}^{\text{eq}})^2 \langle \sigma V \rangle_{\chi_d\chi_d} \sim \frac{\alpha_d^2}{m_{\chi}^2}$$

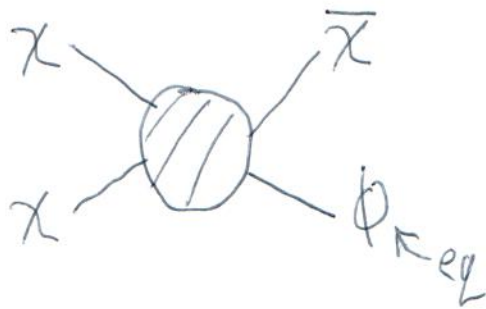
$$\langle \sigma V \rangle_{\chi\bar{\chi}} \sim e^{-2\delta M/T} \frac{\alpha_d^2}{m_{\chi}^2} \quad \delta M = m_{\chi_d} - m_{\chi}$$

$$m_{\chi} \sim e^{-\delta M/T_{\text{FO}}} \alpha_d \sqrt{T_{\text{eq}} M_{\text{Pl}}} \ll \text{TeV}$$

Semi-annihilations

-D'Eramo, Thaler 1003.5912

- Vanilla annihilations respect a Z_2 : $\chi \rightarrow -\chi$
- Z_3 stabilized DM: $\chi \rightarrow e^{\frac{2\pi i}{3}} \chi$
 $\bar{\chi} \rightarrow e^{\frac{4\pi i}{3}} \bar{\chi}$



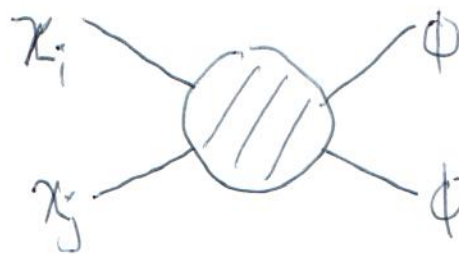
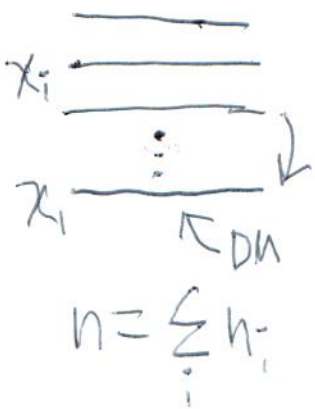
$$\dot{n}_\chi + 3Hn_\chi = -\langle \sigma V \rangle_{\chi\chi} (n_\chi^2 - n_\chi n_\chi^{eq})$$

$$\langle \sigma V \rangle_{\chi\chi} \sim \frac{1}{T_{eq} \cdot M_{Pl}}$$

~~coannihilations~~

coannihilations

- Griest + Seckel 1991



$$\langle \sigma V \rangle_{eff} = \sum_{i,j} \frac{n_i^{eq} n_j^{eq}}{(n_i^{eq})^2} \langle \sigma_{ij} V \rangle$$

$$\dot{n} + 3Hn = -\langle \sigma V \rangle_{eff} (n^2 - n_{eq}^2)$$

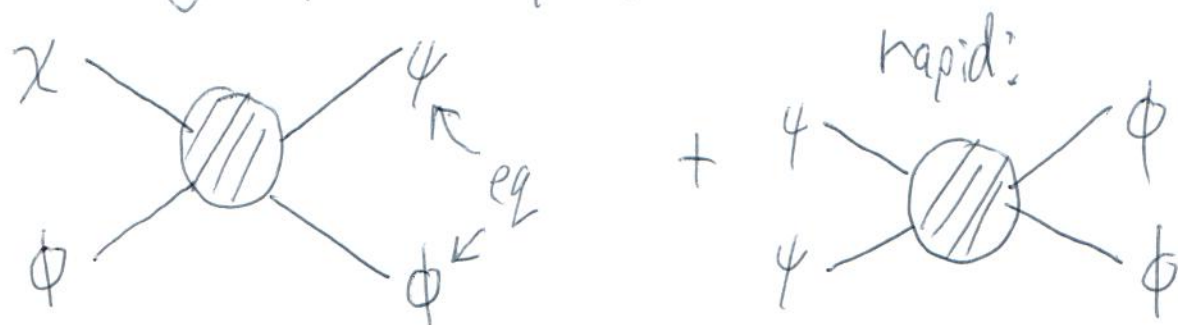
\nwarrow
 $\sim \frac{1}{T_{eq} \cdot M_{Pl}}$

ex) \tilde{B}/\tilde{A} , \tilde{B}/\tilde{W}

"Well-Tempered Neutralino" hep-ph/0601041

coscattering

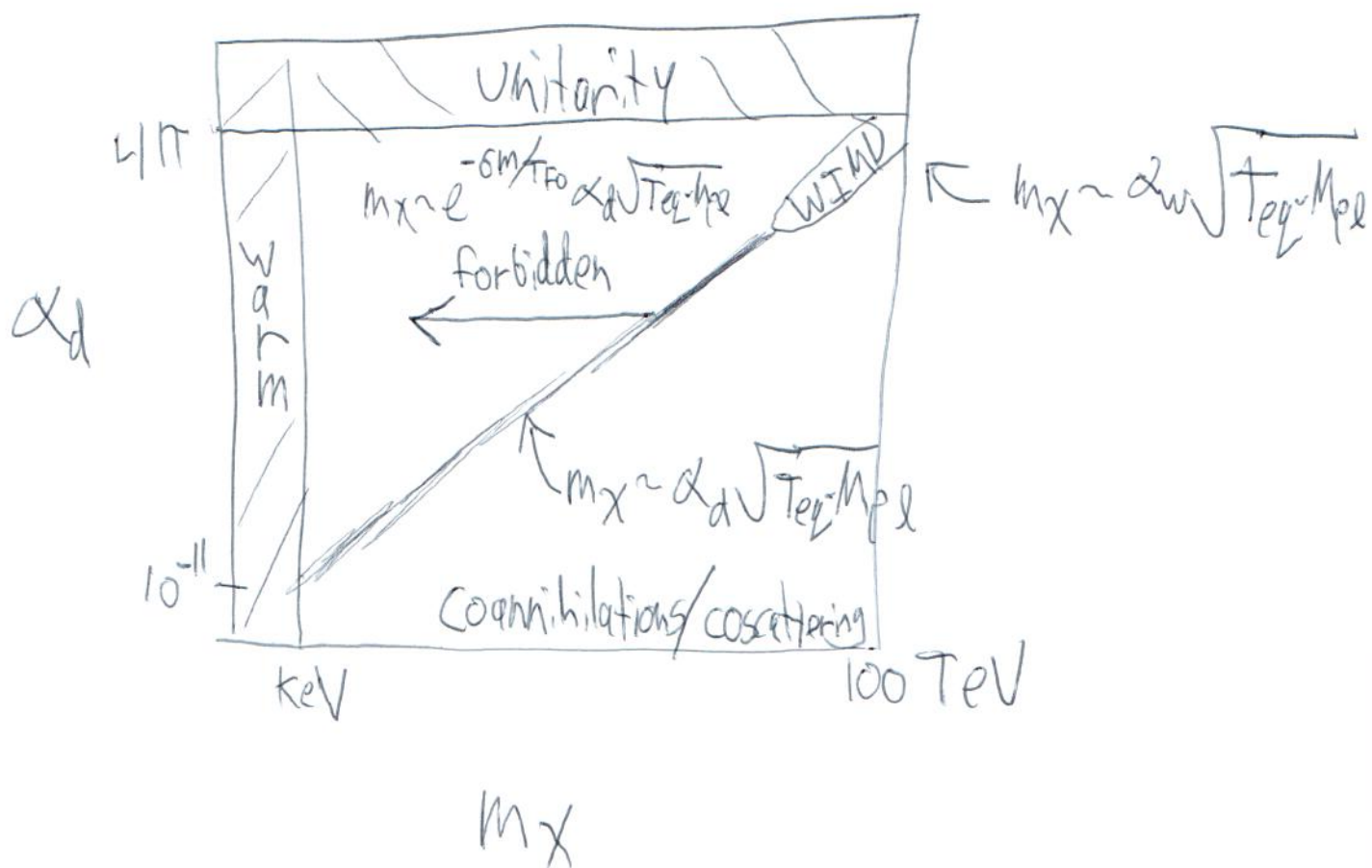
-D'Agnolo, Pappadopulo, JTR 1705.08458



$$\dot{n}_\chi + 3Hn_\chi = -\langle \sigma V \rangle_{\chi\phi} (n_\chi n_\phi^{eq} - n_\chi^{eq} n_\phi^{eq})$$

freeze-out: $n_\phi^{eq} \langle \sigma V \rangle_{\chi\phi} = H$

Phase Diagram

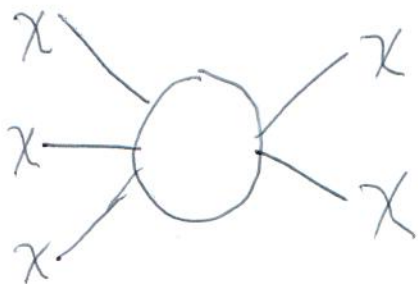


II Thermal Relics Beyond $2 \rightarrow 2$

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SIMPs

1402.5143



$$\dot{n}_\chi + 3Hn_\chi = -\langle \sigma v \rangle_{3\chi} (n_\chi^3 - n_\chi^2 n_\chi^{\text{eq}})$$

Freeze-out: $n_\chi^2 \langle \sigma v \rangle \approx H$

$$\Omega_\chi \sim \frac{m_\chi Y_\chi}{T_{\text{eq}}} = \frac{m_\chi n_\chi}{S T_{\text{eq}}} = \frac{m_\chi H^{1/2}}{S T_{\text{eq}} \langle \sigma v \rangle^{1/2}}$$

$$H \sim \frac{T^2}{M_{\text{pl}}}, \quad S \sim T^3, \quad T \sim m$$

$$\Omega_\chi \sim \frac{1}{m_\chi T_{\text{eq}} M_{\text{pl}}^{1/2} \langle \sigma v \rangle^{1/2}}$$

~~$\langle \sigma v \rangle \sim \frac{m_\chi^2 T_{\text{eq}}^2}{M_{\text{pl}}}$~~

$$\langle \sigma v \rangle \sim \frac{\alpha_d^3}{m_\chi^5} \Rightarrow$$

$$m_\chi \sim \alpha_d (T_{\text{eq}}^2 M_{\text{pl}})^{1/3}$$

$\sim 100 \text{ MeV}$

Asymmetric DM

0901.4117

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- primordial baryon asymmetry: $n_B - n_{\bar{B}}$

$$\Omega_b h^2 = \left(\frac{s_0}{\rho_c h^{-2}} \right) \left(\frac{n_B - n_{\bar{B}}}{s} \right) m_p$$

- DM asymmetry? $n_X - n_{\bar{X}}$

~~$$\Omega_{DM} h^2 = \left(\frac{s_0}{\rho_c h^{-2}} \right) \left(\frac{n_X - n_{\bar{X}}}{s} \right) m_X = \Omega_b h^2 \left(\frac{n_X - n_{\bar{X}}}{n_B - n_{\bar{B}}} \right) \left(\frac{m_X}{m_p} \right)$$~~

$$\frac{\Omega_{DM}}{\Omega_b} \approx 5.3$$

~~explained by mechanisms~~

- mechanisms

— dark phase transition

— out-of-equil. decay

— $B-L \Leftrightarrow X$ transfer

ex) $\Omega \supset \frac{\bar{\chi}^2 (LH)^2}{M^4}$ sets: $n_X - n_{\bar{X}} = C (n_B - n_{\bar{B}})$
 $C = \frac{-12}{49}$

$$\Gamma = n \langle \sigma v \rangle \sim \frac{T^9}{M^8}$$

$$\frac{\rho}{H} \propto T^7 \quad \text{"UV dominated"}$$

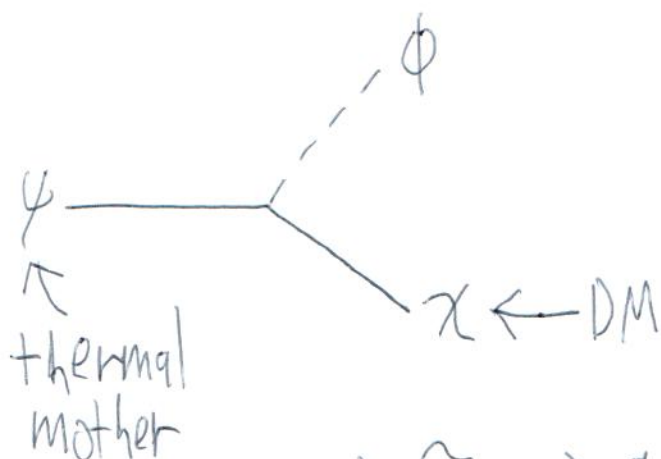


Non-Thermal DM

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FIMP: χ is kinetically/chemically decoupled

- initial condition? ex) $n_\chi(T_{RH}) = 0$



$$\Gamma_\psi < H(T=m_\psi)$$

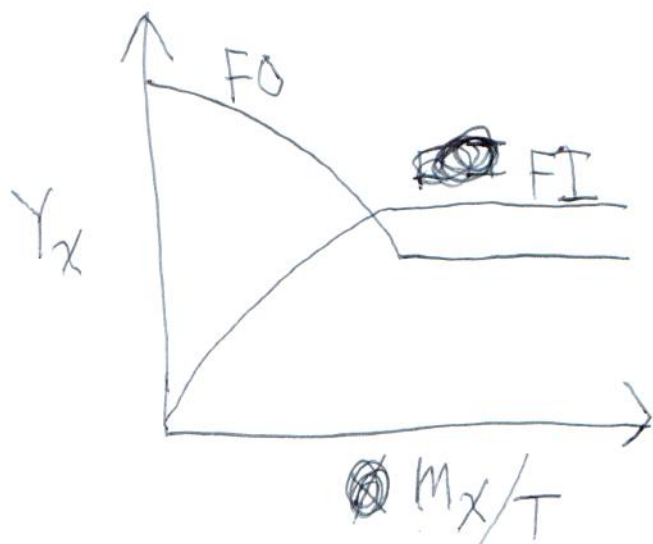
ex) $\tilde{q} \rightarrow q \tilde{G}$

A) freeze-in: χ produced when $n_\psi = n_\psi^{\text{eq}}$

B) Super-WIMP: χ produced after ψ freezes-out

A) Freeze-In

09/11/20



$$\dot{n}_\chi + 3Hn_\chi = n_\psi^{\text{eq}} \langle \Gamma_\psi \rangle$$

$$\langle \Gamma_\psi \rangle = \frac{k_1 (m_\psi/T)}{k_2 (m_\psi/T)} \Gamma_\psi$$

$$\rightarrow \begin{cases} \frac{m_\psi}{2T} & T \gg m_\psi \\ 1 & T \ll m_\psi \end{cases}$$

$$Y_\chi \approx \int \frac{dT}{T} Y_\psi^{eq} \frac{\langle \Gamma_\psi \rangle}{H}$$

- for $T \ll m_\psi$, suppressed by $Y_\psi^{eq} \propto e^{-m_\psi/T}$

- for $T \gg m_\psi$, $\frac{\langle \Gamma_\psi \rangle}{H} \propto T^{-3}$

• dominant production: $T \sim m_\psi$

$$Y_\chi \sim \frac{\Gamma_\psi}{H(T=m_\psi)} \sim \frac{\Gamma_\psi M_{Pl}}{m_\psi^2}$$

$$m_\chi \sim T_{eq} \Rightarrow \frac{m_\chi}{T_{eq}} \sim \frac{T_{eq} \cdot m_\psi}{\alpha_\chi \cdot M_{Pl}}$$

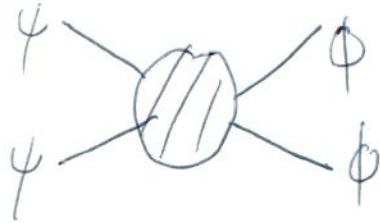
$$\Omega \sim \frac{m_\chi Y_\chi}{T_{eq}} \sim \frac{m_\chi \Gamma_\psi \cdot M_{Pl}}{m_\psi^2 T_{eq}}$$

B) Super WIMP

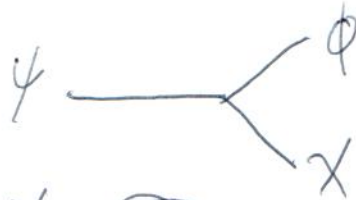
hep-ph/0302215

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1) ψ freezes out



2) ψ decays to DM



$$Y_\chi = Y_\psi \quad \Omega_\chi = m_\chi Y_\chi = m_\chi Y_\psi$$

~~$m_\chi \gg m_\psi$~~

$$\Omega_\chi = \frac{m_\chi}{m_\psi} \Omega_\psi^{Fo}$$

Dark Mechanisms

