

# Interdisciplinary Research between Particle Physics and Mathematics

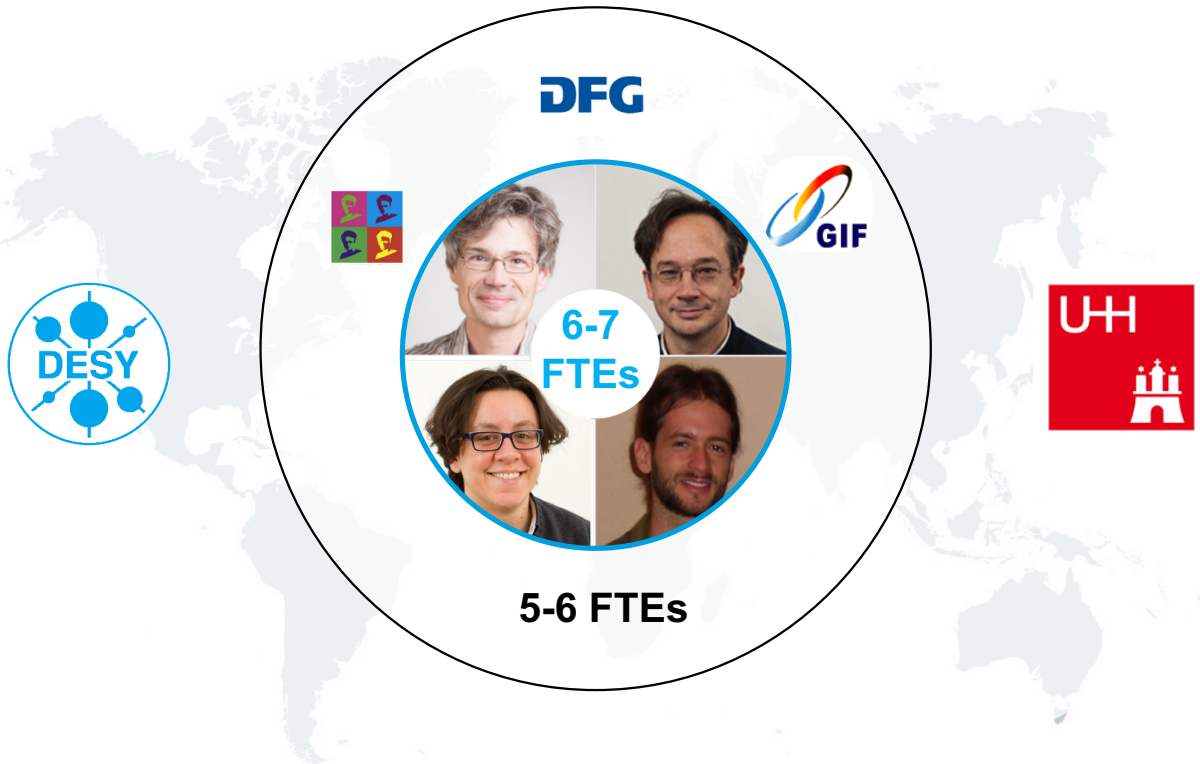
DESY Research Unit: Theoretical Particle Physics

Center Evaluation DESY, 5 – 9 February 2018

# String Theory and Mathematical Physics

## The Group and its Mission

A small group  
strongly interacting  
with its environment

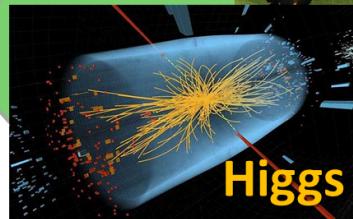


# String Theory and Mathematical Physics

## The Group and its Mission

**Rethinking Quantum Field Theory at the interface  
between particle physics and mathematics**

Develop and apply modern techniques  
from String Theory & Mathematical Physics  
to access physics of matter and space-time  
**deep in the quantum regime**



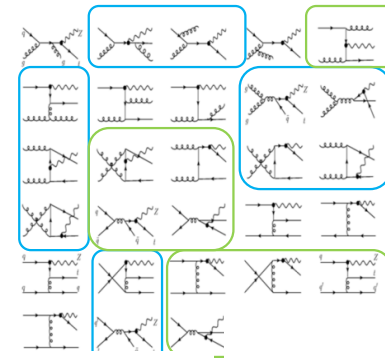
# String Theory and Mathematical Physics

## Introduction to Scientific Goals

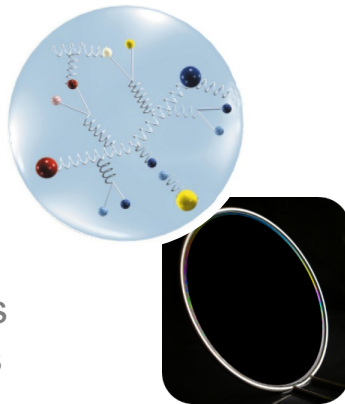
### Example: Quantum Chromodynamics (QCD)

Perturbative paradigm  
of QFT very inefficient

$$Y - Y + X = X$$

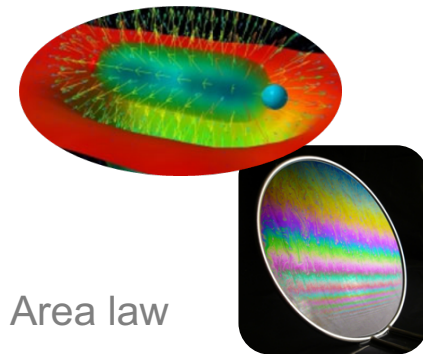


High energy regime  
quarks and gluons



Wilson line observables  
detect different phases

Low energy regime  
colorless hadrons



Phase  
transition  
crossover

Area law

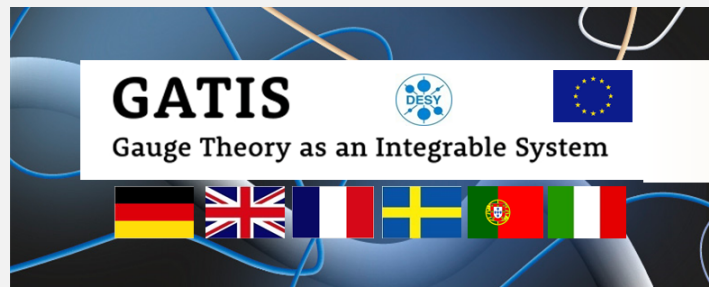
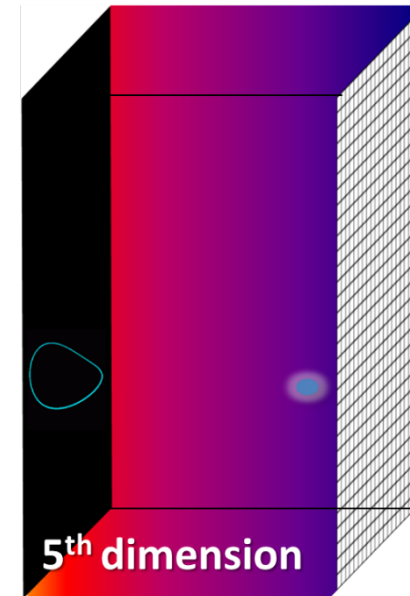
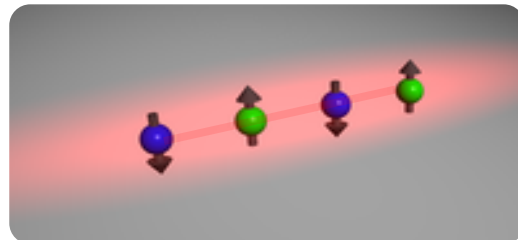
Area law - signal for a **string theory** description?

# Highlights: Strings for Gauge Theory

## Integrability of Gauge Theory Flux Tube

Holography: The QCD-like flux tube of **maximally supersymmetric** multi-color 4D Yang-Mills theory is an integrable/solvable [solved] 1D quantum system.

~ Heisenberg spin chain, Bethe Ansatz



Central research topic of the ITN GATIS,  
coordinated & managed @ DESY<sub>2013--2016</sub>



# Highlights: Strings for Gauge Theory

## High Energy Scattering Amplitudes

We computed scattering amplitudes in collider kinematics at small and large gauge theory coupling  $\lambda$  (multi-colored)

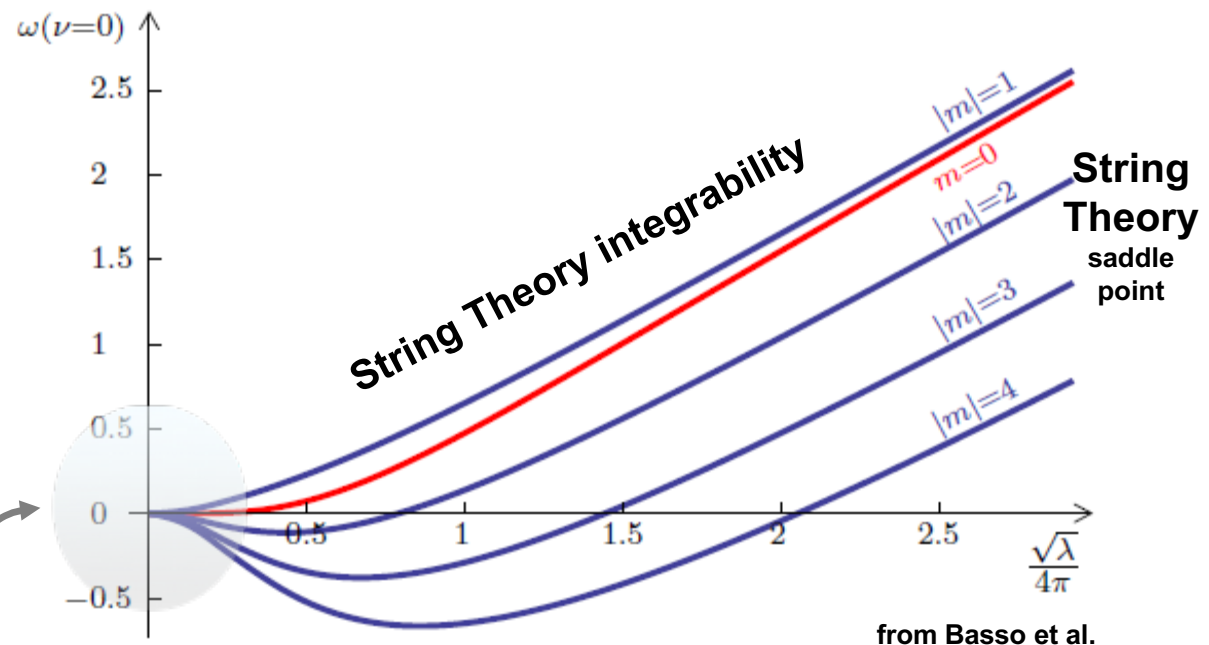
Bartels, Schomerus,  
Sprenger DESY 14-208

### Reggeon intercept $\omega_\lambda(\nu, m)$

For 2 produced particles  
with total CMS energy  $s$

$$A_{\nu, m}^\lambda \sim s^{\omega_\lambda(\nu, m)}$$

**Tremendous simplification**  
compared to the perturbative  
gauge theory calculations



# Highlights: Dualities and Non-local Observables

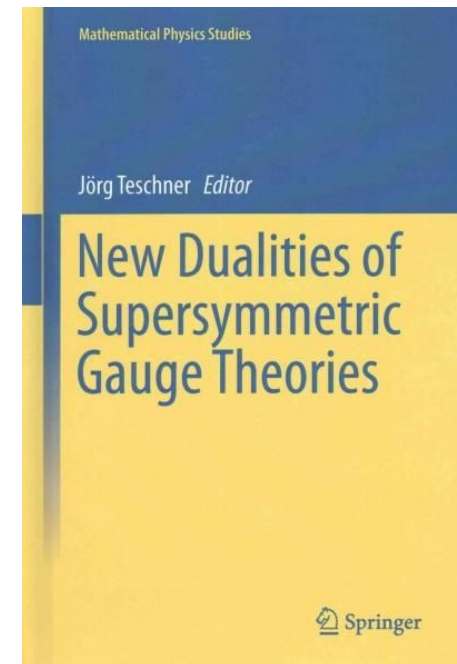
## Dualities and Non-perturbative Physics

By definition, a **duality** provides a simple (perturbative) computational prescription for all observables in a strongly coupled phase/regime of a Quantum Field Theory.

Cp. the description of maximally supersymmetric gauge theory through string theory / supergravity.

**An important task is to find dualities among  $N=2$  (half-maximally) supersymmetric gauge theories**

Many such theories exist: ``Space of theories''



# Highlights: Dualities and Non-local Observables

## Computing Non-local Observables

**Non-local observables play a key role for testing and explaining dualities**

We extended the exact computation of Wilson- and 't Hooft loop expectation values to large classes of  $SU(2)$   $N=2$  supersymmetric gauge theories

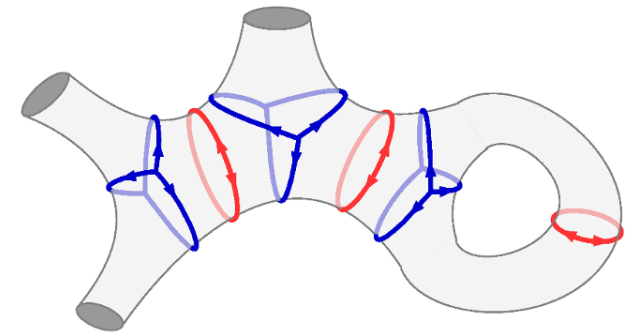
Teschner, Vartanov

different matter content  
multiple  $W, Z$  bosons

We developed world leading expertise in defining & computing new line-observables for theories with  **$SU(3)$  gauge group(s)**.

Coman, Mitev, Pomoni, Teschner

$SU(2) \rightarrow SU(3)$

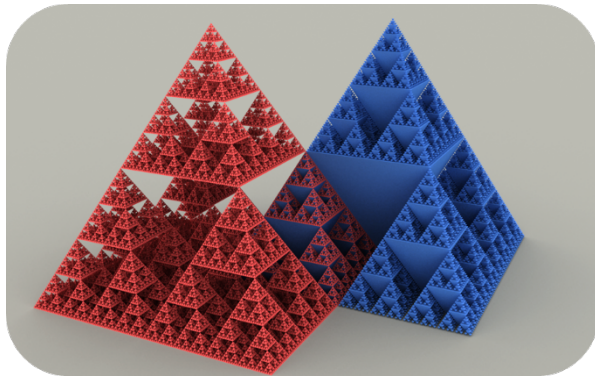


Opened a new chapter in the Mathematics of Riemann surfaces



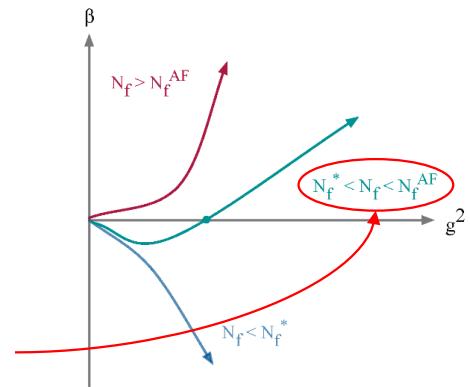
# Highlights: Scale Invariant Quantum Systems

## Non-perturbative Dynamics without Supersymmetry: The Bootstrap



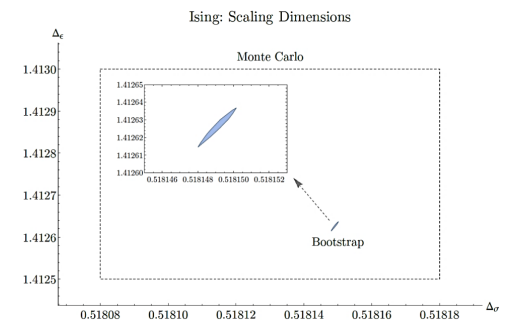
**Scale invariant quantum systems:**  
Fixed point of renormalization group  
possess infinite correlation length &  
describe 2<sup>nd</sup> order phase transition

e.g. conformal window of QCD



Polyakov's bootstrap program exploits the **conformal symmetry** of many low energy systems to calculate observables selfconsistently without using theory of high energy excitations (microscopic theory).

Through a recent numerical incarnation, the conformal bootstrap became a remarkable new source of insight into non-perturbative physics.



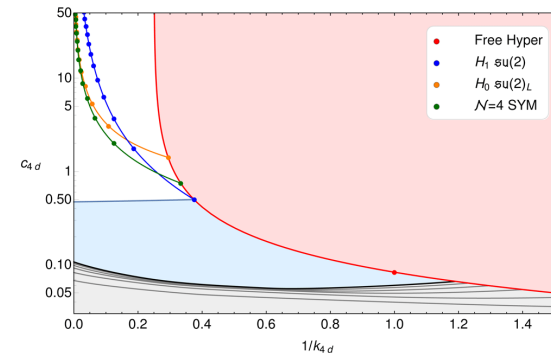
from Kos et al.

# Highlights: Scale Invariant Quantum Systems

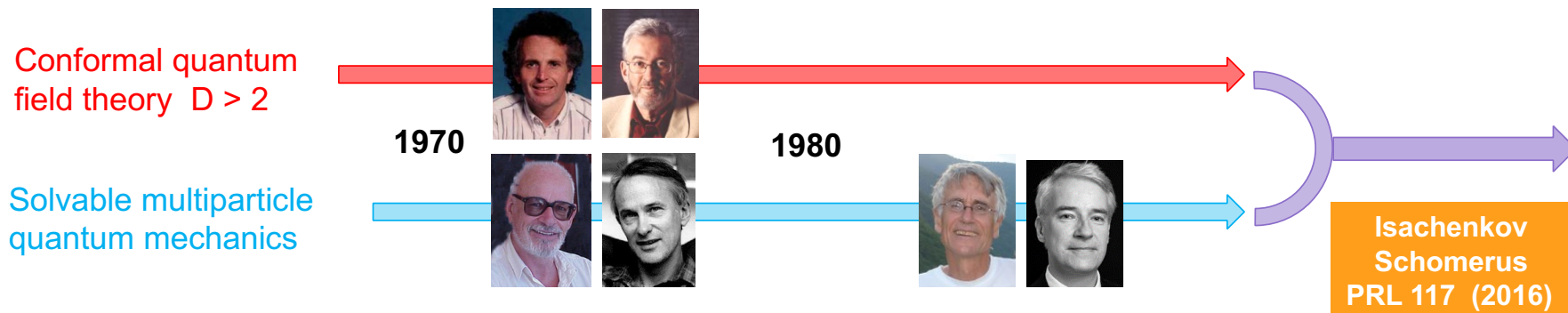
## Applying and Advancing the Bootstrap

Group members pioneered the use of *exact results* in the numerical bootstrap to chart out the space of **superconformal field theories**.

Lemos, Liendo, DESY 15-230



We developed the **mathematical theory of conformal symmetry** through a previously unobserved connection with solvable Schrödinger problems [\[like Poeschl-Teller problem\]](#)



# String Theory and Mathematical Physics

## The Center for Mathematical Physics (ZMP)

Hamburg Center for Mathematical Physics inaugurated in 2005

Today ~10 full professorships (3 from 2005)

Since 2006 supported by SFB 676, section A [ projects A1-11 ]

Extended in 2010 and 2014, terminates 2018

Since 2012 joint graduate school GRK 1670

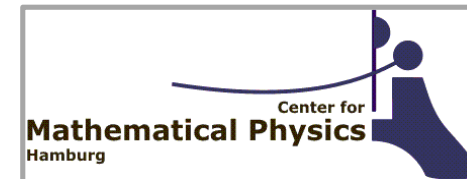
Extended in 2016

Since 2016 J.Teschner jointly appointed by DESY/UHH (Math)

Professorship for Quantum Geometry

Application for Transregio (DFG) with institutions in Berlin area

Geometry, integrability, scattering amplitudes

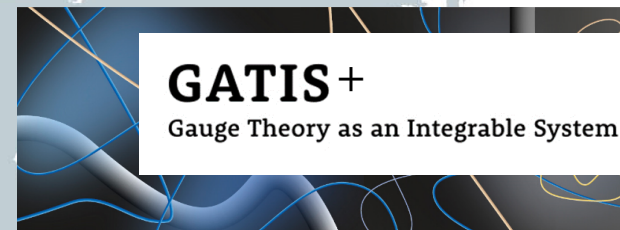


**ZMP grew into world-class center for Mathematical Physics**

# String Theory and Mathematical Physics

## International Networking

We host major international conferences: Amplitudes 2012, IGST 2014, StringMath 2017



MoU signed in 2016/17 by  
15 leading European Institutions  
[www: gatisplus.desy.de](http://www.gatisplus.desy.de)

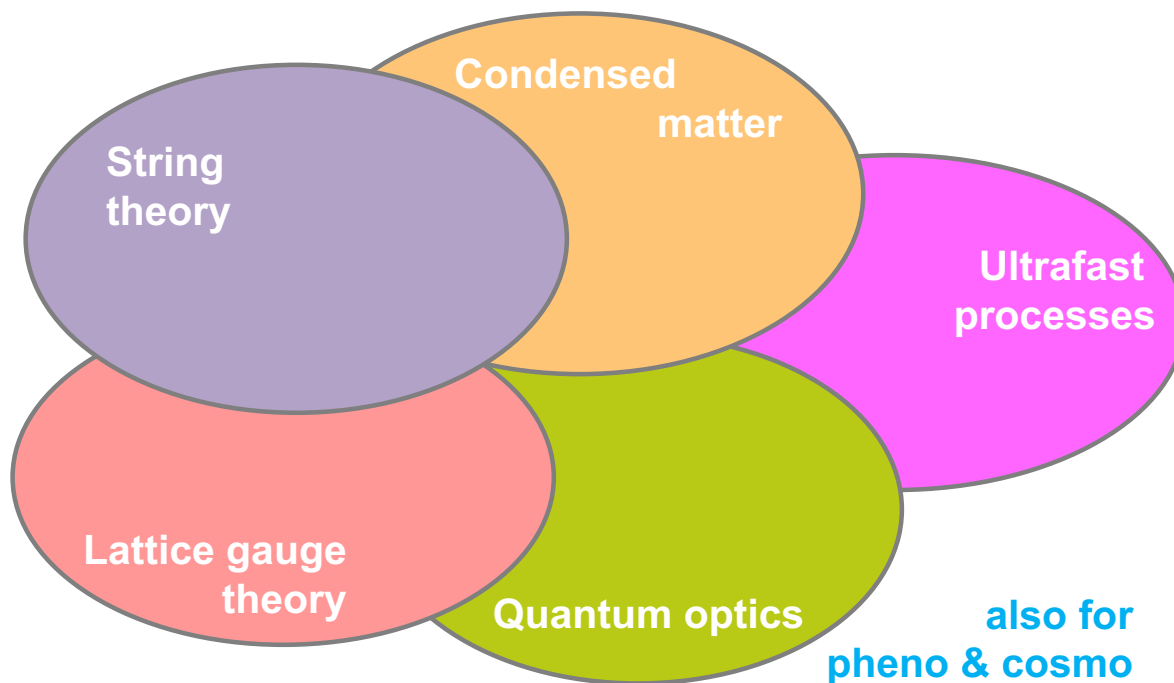
MC ETN **Scattering Amplitudes from Geometry to Experiment** (SAGEX) submitted

# String Theory and Mathematical Physics

## Conclusion and Outlook

With strong roots in particle physics and a world-class center for mathematical physics, DESY is the ideal place to conduct interdisciplinary research in string theory

Through the Wolfgang-Pauli-Centre the interdisciplinary environment could grow another dimension



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