New particles' masses from transverse mass kinks: The case of Yukawa-unified SUSY GUTs

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- **SUSY GUTs with YU:** status and expected SUSY spectrum
- \mathbf{M}_{T_2} : why it is suitable for that spectrum
- \mathbf{M}_{T_2} : application (highlights)

Based on:

Choi, DG, Im, Park (arXiv:1005.0618)

DG, Raby, Straub (JHEP 09)

Altmannshofer, DG, Raby, Straub (PLB 08)

1993: Hall-Rattazzi-Sarid see also: Carena *et al.* Use YU to predict the top mass, with input from the (measured!) bottom and tau masses It was realized that, when tan β is large, the bottom and tau masses get large EW-scale threshold corrections, due to loops proportional to the "wrong" vev.

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2001: Blazek- Dermisek-Raby	Rather than using YU to predict the top mass, use its measured value to make predictions for the SUSY spectrum.
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1999: Bagger e <i>t al.</i>	Interestingly, the very same relations among soft terms emerge as fixed-point solution of the RGEs (under the assumption of GUT-scale YU).			
	This solution gives rise to inverted scalar mass hierarchy, namely light 3 rd generation and heavy 1 st and 2 nd generation squarks.			
	The reason is the O(1) 33-entry in the Yukawa matrix.			

More recent studies appraise the above scenario in the light of low-energy data.

Different approaches pursued on:

Many refs:

Tobe+Wells; Auto *et al.* (x 2); Balazs+Dermisek; Baer *et al.* (x 6); Albrecht *et al.*; Altmannshofer *et al.*; D.G. *et al.*; Antusch+Spinrath (x 2); Gogoladze *et al.*

- ① data considered (fermion masses, EWPO, FCNCs)
- ② boundary conditions for the soft terms
- 3 techniques to explore the parameter space

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Our approach

Technique

- *a.* Construct a X^2 function with all the best known low-energy observables, including:
 - EW observables (M_W , M_Z , G_F , $\alpha_{e.m.}$, α_s) and 3rd generation quark masses
 - quark FCNCs: $\Delta M_s / \Delta M_d$, $B \to X_s \gamma$, $B \to X_s \ell^+ \ell^-$, $B \to \tau \nu$
- **b.** Minimize this x^2 function upon variation of the model parameters. One can thus **enforce exact YU**.

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- **b.** Minimize this x^2 function upon variation of the model parameters. One can thus **enforce exact YU**.
 - Provides a global assessment of the model in a reparameterization-invariant way (what matters is the χ^2 minimum)
 - "Exploits" the errors on the low-energy param's, to which the high-energy param's carry very strong sensitivity [see discussion in Tobe-Wells, 2003]

Scenarios consider	ed ① SUSY GUTs with YU and universal GUT-scale soft terms
Assumptions here:	Soft terms consist of a universal bilinear (m_{16}) , a universal trilinear (A_0) , a universal gaugino mass $(m_{1/2})$ and split soft terms for the Higgses (m_{Hu}, m_{Hd})

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The combined **info from FCNCs** (in particular $B \rightarrow X_s \gamma$ and $B_s \rightarrow \mu^+ \mu^-$) **favors** <u>values of tan</u> β <u>lower than O(50)</u>

Conversely, it is known that m_b prefers tan β O(50) (or else, tan β close to 1, excluded by LEP)



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Pheno viability can be recovered without decoupling, by relaxing t – b – τ YU to just b – τ unification: Compromise between the FCNC and m_b constraints

Spectrum predictions are robust, because of the cross-fire among the constraints



Scenarios considered

Assumptions here: With respect to scenario 1, trilinears are allowed to be split: A_U , A_D (In principle also bilinears, e.g. between the Q, U, D multiplets, but fits indicate a marginal impact)



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Agreement with data clearly selects the region with large $\mu = O(m_{16})$ and sizable $A_{\mu} - A_{p}$ splitting

In this region:

The lightest (RH) stop (and the gluino) are required to be very close to their exp bounds, i.e. are veeery light.

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So, substantial improvement on the fine tuning on the above quantities.

Price: achieving EWSB with precisely the right value of M_z does require increased fine tuning, because of the large μ

Again, spectrum predictions are robust



" Upon discovery of new particles, the first fundamental question to ask is what is the mass of these particles "

Spectrum predictions

S	cenario 1	sce	enario 2	
M_{h^0}	121	M_{h^0}	126	
M_{H^0}	585	M_{H^0}	1109	
M_A	586	M_A	1114	
M_{H^+}	599	M_{H^+}	1115	
$m_{\tilde{t}_1}$	783	$M_{\tilde{t}_1}$	192	
$m_{\tilde{t}_2}$	1728	$m_{\tilde{t}_2}$	2656	
$m_{\tilde{b}_1}$	1695	$m_{\tilde{b}_1}$	2634	
$m_{\tilde{b}_2}$	2378	$m_{\tilde{b}_2}$	3759	
$m_{\tilde{\tau}_1}$	3297	$m_{\tilde{\tau}_1}$	3489	
$m_{\tilde{\chi}_1^0}$	59	$m_{\tilde{\chi}_1^0}$	53	
$m_{\tilde{\chi}_2^0}$	118	$m_{\tilde{\chi}^0_2}$	104	
$m_{\tilde{\chi}_1^+}$	117	$m_{\tilde{\chi}_1^+}$	104	
$M_{\tilde{g}}$	470	$M_{\tilde{g}}$	399	

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- Main difference: a stop respectively lighter and heavier than the gluino
- For neutralino1,2 and chargino1 and basically also the gluino, predictions are the same.
- **glu-glu** production is substantial in both scenarios (60 vs. 40%)
- stop1 stop1 production is also large (40% !) in scenario 2 (and basically zero in the other)
- chargino1 neutralino2 associated production is also interesting in both scenarios (25 vs. 10%)

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$M_{\tilde{g}}$	470	$M_{\tilde{g}}$	399				is also interesting in both scenarios (25 vs. 10%)	

A suitable mass-determination strategy should be able to determine the masses of all the light gauginos and, for scenario 2, of the stop1 as well.

Can one construct such a strategy ?

Would it realistically work on LHC data ?

Note: gluino and (for scenario 2) stop1 are light, hence one can expect 2- or 3-steps decay chains: *short decay chains*



determination of the gluino, chargino1, neutralino1,2 and stop1 masses within scenario 2 Choi, DG, Im, Park, 2010

Step (1)

Construct $M_{_{T2}}$ for $\tilde{g} - \tilde{g}$ production followed by the decay

- In about 100/fb of data, one expects around 1.1 million such events
- The alternative channel with $\tilde{X}_1^{\pm} \rightarrow \tilde{X}_1^{0} q q'$ (where namely only the \tilde{X}_1^{0} is invisible) is affected by a much larger combinatoric error

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- **Trigger on 2** W + 4 b + 2 ℓ + missing p_{T}
- Apply suitable kinematical cuts on the event sample
- In the construction of M_{T2} , include the whole \tilde{X}_1^{\pm} initiated decay chain in the missing p_T

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Construct M_{τ_2} for $\tilde{g} - \tilde{g}$ production followed by the decay

Trigger on 2 W + 4 b + 2 ℓ + missing p_{T}

- In about 100/fb of data, one expects around 1.1 million such events
- The alternative channel with $\tilde{\chi}_1^{\pm} \rightarrow \tilde{\chi}_1^{0} q q'$ (where namely only the $\tilde{\chi}_1^{0}$ is invisible) is affected by a much larger combinatoric error

The kink location allows to determine simultaneously the gluino and chargino1 masses:

In the construction of M_{T2} , include the whole

 \tilde{X}_1^{\pm} initiated decay chain in the missing p_{T}

Apply suitable kinematical cuts on the event sample

$$m_{\tilde{g}} = 395(16) \text{ GeV}, \ m_{\tilde{\chi}_1^{\pm}} = 109(17) \text{ GeV}$$

Application example: continued

Step (2)

Consider $\tilde{t}_1 - \tilde{t}_1$ production, followed by the decay

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Step ③

Finally, consider $\tilde{X}_{2}{}^{\scriptscriptstyle 0}-\tilde{X}_{1}{}^{\pm}$ associated production, followed by

Conclusions

- Within SUSY GUTs with Yukawa unification, we have considered **two representative scenarios** – both experimentally viable, but with important **differences in the SUSY spectrum and decay modes**.
- For these scenarios, we have addressed the question to which extent is it possible to determine the lightest part of the SUSY spectrum at the LHC.

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- For these scenarios, we have addressed the question to which extent is it possible to determine the lightest part of the SUSY spectrum at the LHC.
- The event topologies of interest are characterized by **short decay chains**. **This suggests M_{\tau_2} variables** as the most promising quantities for our problem.
- We have elaborated a stategy based on M_{τ2} and studied it on 100/fb of data of 14 TeV LHC collisions. We included hadronization / detector-level effect with Pythia / PGS.

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- We have elaborated a stategy based on M_{T2} and studied it on 100/fb of data of 14 TeV LHC collisions. We included hadronization / detector-level effect with Pythia / PGS.
- We showed this strategy to be able to **determine**, within about 20 GeV, themasses of all the light gauginos (neutralino1,2, chargino1, gluino) and also the mass of the lightest stop (for the scenario where it is below the gluino).