

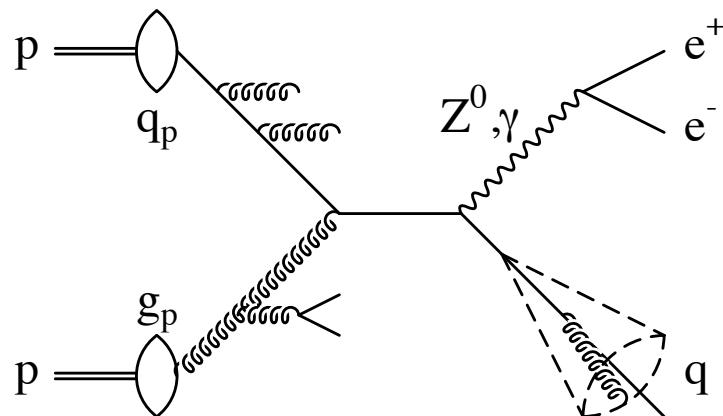
Status of (N)NLO Calculations

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QCD at High Energy Colliders

- ▶ QCD: successful theory of strong interactions
- ▶ QCD is omnipresent in high energy collisions



QCD effects

- initial state: parton distributions
- final state: jets
- hard scattering matrix elements
- higher order corrections
- multiple radiation

- ▶ Detailed understanding of QCD mandatory for
 - ▶ Interpretation of collider data
 - ▶ Precision studies
 - ▶ Searches for new physics



Topics

- 1.Jets and event shapes
- 2.Multiparticle production at NLO
- 3.Precision observables at NNLO
- 4.Infrared structure and resummation



Jets and event shapes



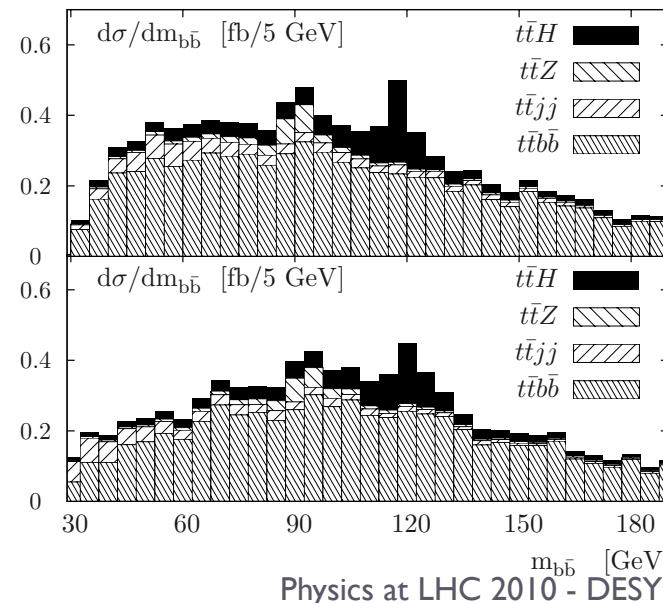
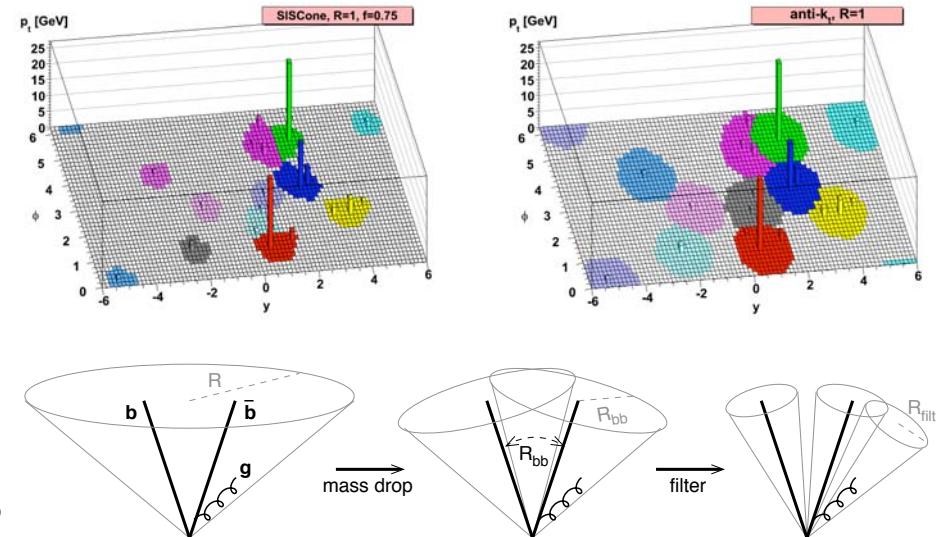
Jets

- ▶ final-state signature of quark and gluon production
- ▶ defined through a jet algorithm
 - ▶ infrared-safety: jets insensitive to collinear and soft radiation
 - ▶ cone algorithms
 - ▶ intuitive picture, numerically fast
 - ▶ splitting and merging nearby cones: infrared sensitivity
 - ▶ IR-safe formulation: SISCone (G. Salam, G. Soyez)
 - ▶ recombination algorithms (e.g. Durham k_T)
 - ▶ less intuitive, numerically slow
 - ▶ infrared safety ensured
 - ▶ cone-formed jets obtained by anti- k_T algorithm (M. Cacciari, G. Salam)
 - ▶ fast implementation: FastJet (M. Cacciari, G. Salam)



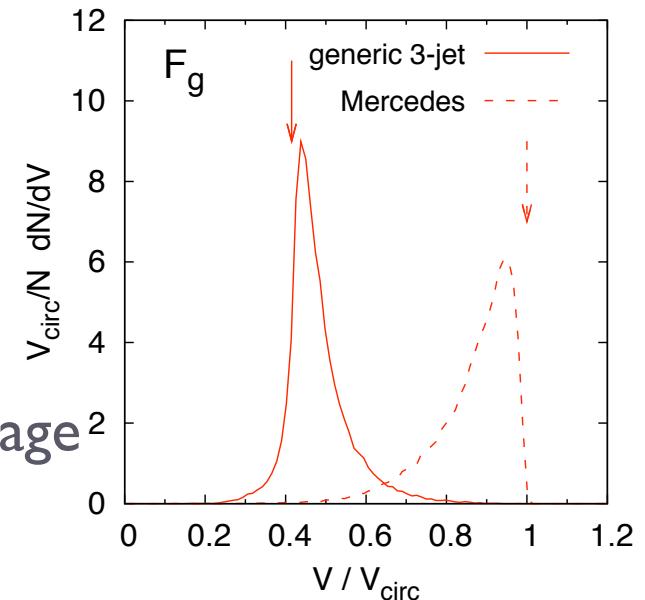
Jets as analysis tool

- ▶ Jet catchment area (M. Cacciari, G. Salam)
 - ▶ allows study of outside-jet activity (underlying event)
- ▶ Jet substructure
 - ▶ aim: reconstruction of boosted massive particles decaying into jets
 - ▶ all decay products inside one ‘fat jet’
 - ▶ resolve decay products by jet substructure
(J. Butterworth, A. Davison, M. Rubin, G. Salam)
 - ▶ reconstruction of $t\bar{t}H$ final states becomes feasible
(T. Plehn, G. Salam, M. Spannowsky)



Event shapes

- ▶ characterize geometrical properties of hadronic final state
 - ▶ e.g. thrust: momentum flow along event axis $T = \max_{\vec{n}} \left(\frac{\sum_i |\vec{p}_i \cdot \vec{n}|}{\sum_i |\vec{p}_i|} \right)$
 - ▶ ideal case: global variables (depend on all hadrons in event)
- ▶ extensively measured at LEP for precision QCD studies
 - ▶ measurements of α_s
 - ▶ resummation effects
 - ▶ power corrections
- ▶ event shapes at hadron colliders
 - (A. Banfi, G. Salam, G. Zanderighi)
 - ▶ defined usually from transverse momenta
 - ▶ tools for model-independent searches
 - ▶ global variables must account for finite coverage
 - ▶ extensive classification of different variables



Multiparticle production at NLO



Multi-particle production

Multi-particle final states (with jets, leptons, photons) very frequent at colliders

- ▶ decay signatures of short-lived massive particles (e.g. top quarks)
- ▶ are signal and background for new particle searches
- ▶ want reliable predictions

Why NLO?

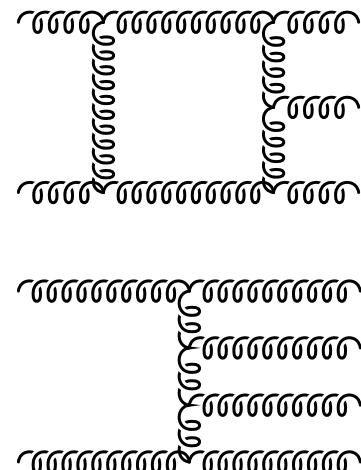
- ▶ reduce uncertainty of theory prediction
 - ▶ reliable normalization
 - ▶ reliable error estimate
- ▶ jet algorithm dependence
- ▶ effects of extra radiation



NLO calculations

Require two principal ingredients (here: $\text{pp} \rightarrow 3j$)

- ▶ one-loop matrix elements
 - ▶ explicit infrared poles from loop integral
 - ▶ known for all $2 \rightarrow 2$ processes
 - ▶ known for many $2 \rightarrow 3$ processes
 - ▶ current frontier $2 \rightarrow 4$: major challenge
- ▶ tree-level matrix elements
 - ▶ implicit poles from soft/collinear emission



Combining virtual corrections and real emission

- ▶ extract process-independent implicit poles from real emission
 - ▶ residue subtraction (S. Frixione, Z. Kunszt, A. Signer)
 - ▶ dipole subtraction (S. Catani, S. Dittmaier, M. Seymour, Z. Trocsanyi)
 - ▶ antenna subtraction (D. Kosower; J. Campbell, M. Cullen, E.W.N. Glover; A. Daleo, D. Maitre, TG)



NLO: multi-leg one-loop amplitudes

- ▶ Challenges of one-loop multileg-amplitudes
 - ▶ complexity: number of diagrams, number of scales
 - ▶ stability: linear dependence among external momenta

▶ General structure

$$\mathcal{A} = \sum_i d_i \text{ Box}_i + \sum_i c_i \text{ Triangle}_i + \sum_i b_i \text{ Bubble}_i + \sum_i a_i \text{ Tadpole}_i + R$$

- ▶ Enormous recent progress
 - ▶ tensor reduction and form factor decomposition
(A. Denner, S. Dittmaier; T. Binoth, J.P. Guillet, G. Heinrich, E. Pilon, C. Schubert)
 - ▶ unitarity and multi-particle cuts to fix coefficients
(Z. Bern, L. Dixon, D. Dunbar, D.A. Kosower; R. Britto, F. Cachazo, B. Feng; P. Mastrolia; D. Forde; S. Badger)
 - ▶ reduction at integrand level (G. Ossola, C. Papadopoulos, R. Pittau)
 - ▶ numerical D-dimensional unitarity (R.K. Ellis, W. Giele, Z. Kunszt, K. Melnikov)



Automating NLO calculations

Real radiation: based on LO event generators

- ▶ dipole subtraction
 - ▶ **SHERPA** (T. Gleisberg, F. Krauss)
 - ▶ **MadDipole** (R. Frederix, N. Greiner, TG)
 - ▶ **TeVJet** (M. Seymour, C. Tevlin)
 - ▶ **AutoDipole** (K. Hasegawa, S. Moch, P. Uwer)
 - ▶ **Helac/Phegas** (M. Czakon, C.G. Papadopoulos, M. Worek)
- ▶ residue subtraction
 - ▶ **MadFKS** (R. Frederix, S. Frixione, F. Maltoni, T. Stelzer)
- ▶ extensive libraries in existing NLO packages
 - ▶ **MCFM** (J. Campbell, R.K. Ellis)
 - ▶ **NLOJET++** (Z. Nagy, Z. Trocsanyi)



Automating NLO calculations

Virtual corrections: implementations

- ▶ semi-numerical form factor decomposition: **GOLEM**
(T. Binoth, J.P. Guillet, G. Heinrich, E. Pilon, T. Reiter)
- ▶ unitarity and multi-particle cuts: **BlackHat**
(C.F. Berger, Z. Bern, L.J. Dixon, F. Febres Cordero, D. Forde, H. Ita, D.A. Kosower, D. Maitre)
- ▶ reduction at integrand level: **CutTools** (G. Ossola, C. Papadopoulos, R. Pittau)
- ▶ generalized D-dimensional unitarity: **Rocket** (W. Giele, G. Zanderighi)
- ▶ generalized D-dimensional unitarity: **Samurai**
(P. Mastrolia, G. Ossola, T. Reiter, F. Tranmontano)
- ▶ several more packages in progress
(A. Lazopoulos; W. Giele, Z. Kunszt, J. Winter; K. Melnikov, M. Schulze)



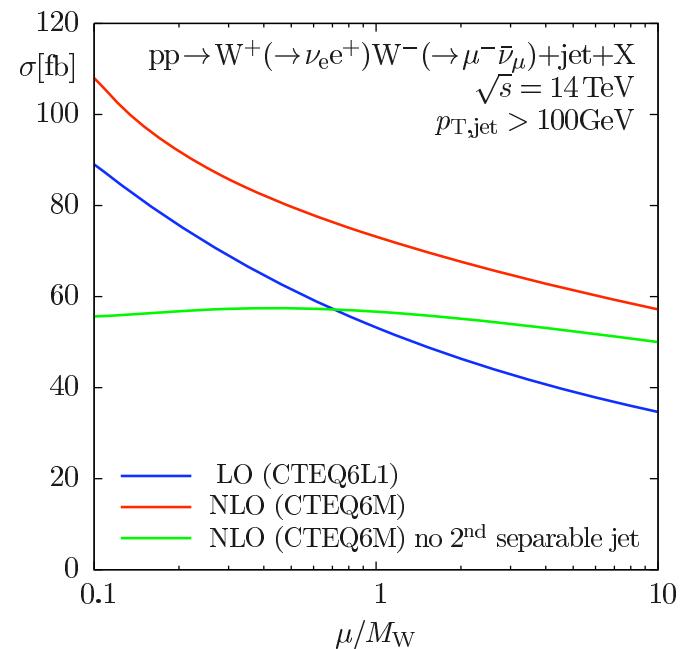
NLO: multi-leg processes

► recent results for $2 \rightarrow 3$ processes

- $pp \rightarrow VV + j$ (S. Dittmaier, S. Kallweit, P. Uwer; J. Campbell, R.K. Ellis, G. Zanderighi; T. Binoth, T. Gleisberg, S. Karg, N. Kauer, G. Sanguinetti)
- $pp \rightarrow H + 2j$ (J. Campbell, R.K. Ellis, G. Zanderighi; M. Ciccolini, A. Denner, S. Dittmaier; S. Badger, E.W.N. Glover, P. Mastrolia, C. Williams)
- $pp \rightarrow VVV$ (A. Lazopoulos, K. Melnikov, F. Petriello; G. Bozzi, F. Campanario, V. Hankele, D. Zeppenfeld; T. Binoth, G. Ossola, C. Papadopoulos, R. Pittau)

► vector boson fusion processes

- VBFNLO (D. Zeppenfeld et al.)



NLO multileg: $t\bar{t} + b\bar{b}$ and $t\bar{t} + 2j$

- ▶ $pp \rightarrow t\bar{t}b\bar{b}: 2 \rightarrow 4$ including masses

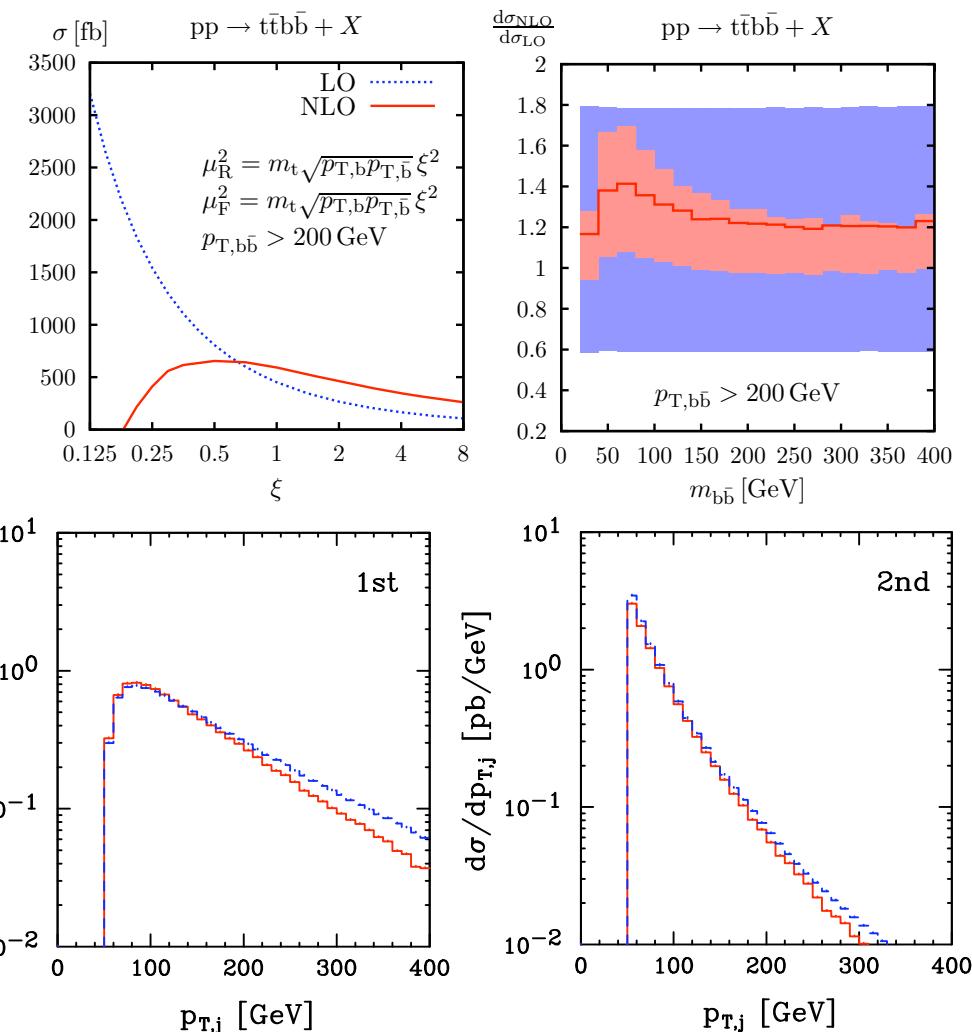
- ▶ using numerical tensor reduction
(A. Bredenstein, A. Denner, S. Dittmaier, S. Pozzorini)
- ▶ using CutTools/Helac
(G. Bevilacqua, M. Czakon, C. Papadopoulos, M. Worek)
- ▶ NLO corrections affect shape
- ▶ background to Higgs studies

- ▶ $pp \rightarrow t\bar{t} + 2j$

- ▶ using CutTools/Helac
(G. Bevilacqua, M. Czakon, C. Papadopoulos, M. Worek)

- ▶ in progress: $pp \rightarrow b\bar{b}b\bar{b}$

(T. Binoth, N. Greiner, A. Guffanti, J.P. Guillet, T. Reiter, J. Reuter)



NLO multileg: $W^\pm + 3j$, $Z^0 + 3j$

▶ Calculations of $W^\pm + 3j$

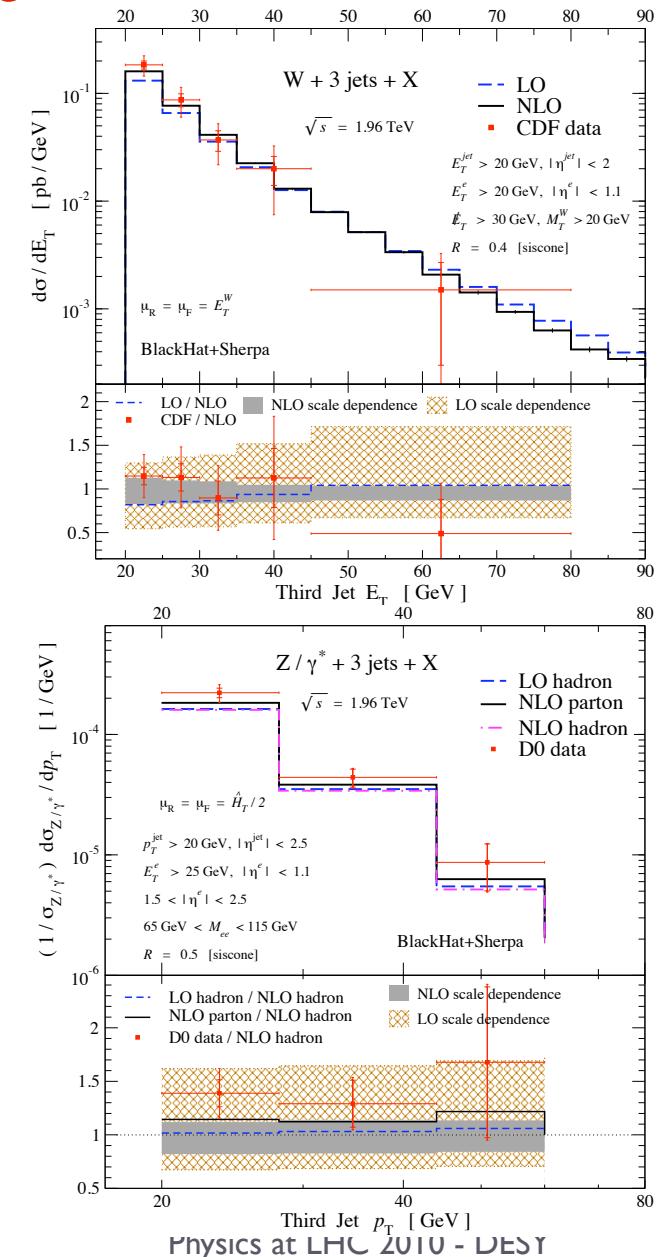
- ▶ Blackhat + Sherpa (C.F. Berger, Z. Bern, L.J. Dixon, F. Febres Cordero, D. Forde, T. Gleisberg, H. Ita, D.A. Kosower, D. Maitre)
- ▶ Rocket (R.K. Ellis, K. Melnikov, G. Zanderighi)

▶ excellent description of Tevatron data

- ▶ moderate corrections
- ▶ precise prediction
- ▶ rich phenomenology
 - ▶ scale setting
 - ▶ final state correlations between lepton and jets

▶ Calculation of $Z^0 + 3j$

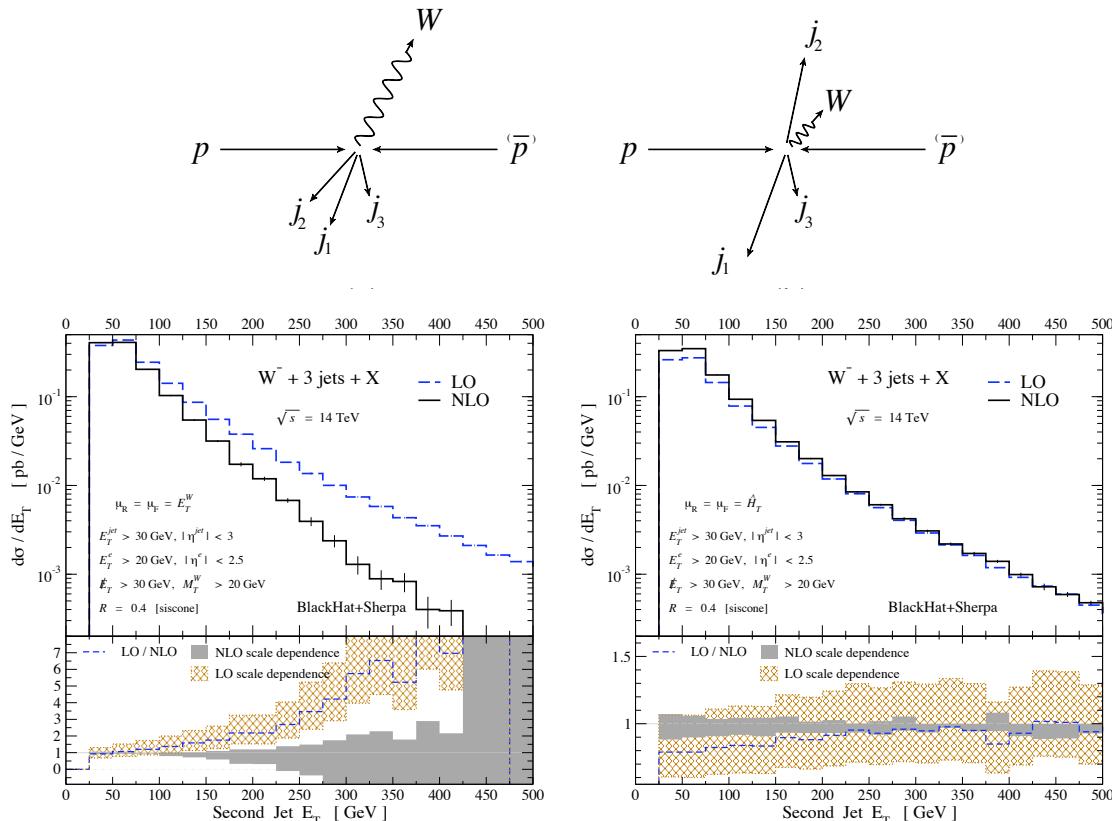
- ▶ Blackhat + Sherpa



NLO multileg: $W^\pm + 3j$

► Scale choice in multileg processes (Blackhat+Sherpa)

- $\mu = E_{TW}$ is inappropriate: poor perturbative convergence
- $\mu = H_T$ accounts for full hard final state dynamics



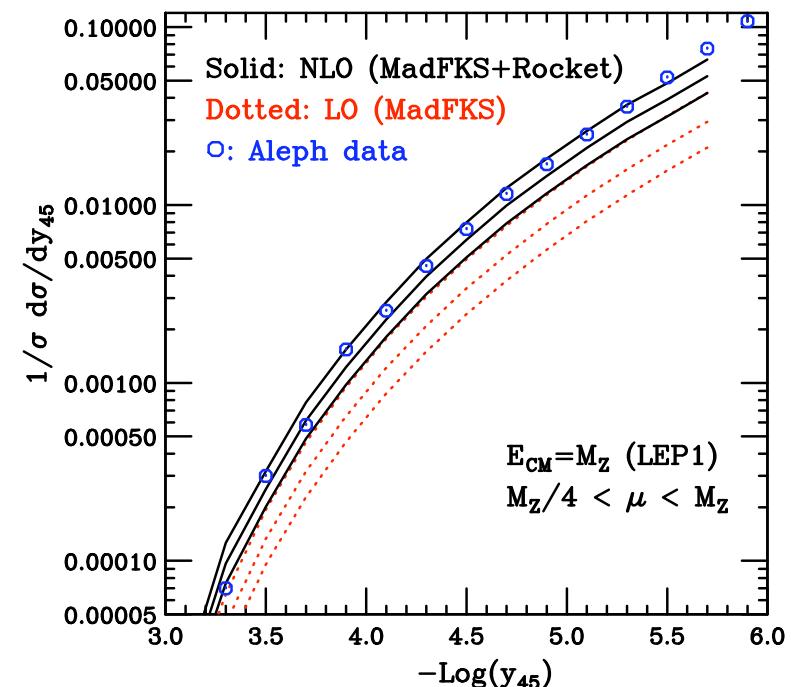
Allows optimization of LO studies

- local choice at each vertex
- important for background studies
- e.g. $pp \rightarrow W(\rightarrow \tau\nu) + 3j$ for SUSY
(K. Melnikov, G. Zanderighi)



NLO multileg: $e^+e^- \rightarrow 5$ jets

- ▶ one-loop amplitudes are crossing of hadron-collider V+3j
 - ▶ computed using Rocket package
- ▶ real radiation from MadGraph
 - ▶ subtraction using MadFKS
- ▶ improved scale dependence
- ▶ better agreement with data
- ▶ possibly new extraction of α_s



R. Frederix, S. Frixione, F. Maltoni, K. Melnikov, H. Stenzel, G. Zanderighi



Precision observables at NNLO



Status of (N)NLO Calculations

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Precision observables

Processes measured to few per cent accuracy

- ▶ $e^+e^- \rightarrow 3$ jets
- ▶ 2+1 jet production in deep inelastic scattering
- ▶ jet production at hadron colliders
- ▶ vector boson production at hadron colliders
- ▶ vector boson plus jet production at hadron colliders
- ▶ top quark pair production at hadron colliders

Processes with potentially large perturbative corrections

- ▶ Higgs production at hadron colliders
- ▶ vector boson pairs at hadron colliders

Require NNLO corrections for

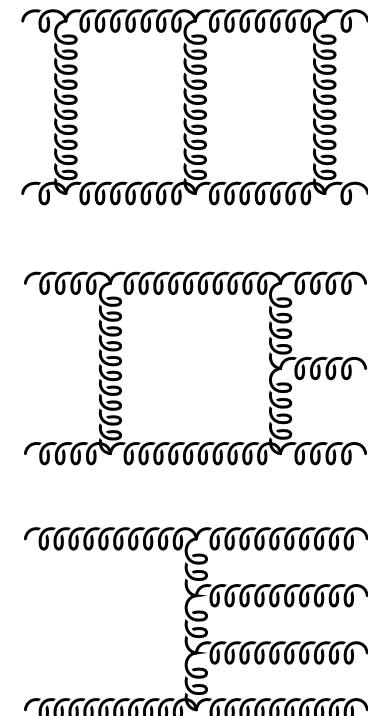
- ▶ meaningful interpretation of experimental data
- ▶ precise determination of fundamental parameters



NNLO calculations

Require three principal ingredients (here: $\text{pp} \rightarrow 2j$)

- ▶ two-loop matrix elements
 - ▶ explicit infrared poles from loop integral
 - ▶ known for all massless $2 \rightarrow 2$ processes
- ▶ one-loop matrix elements
 - ▶ explicit infrared poles from loop integral
 - ▶ and implicit poles from soft/collinear emission
 - ▶ usually known from NLO calculations
- ▶ tree-level matrix elements
 - ▶ implicit poles from two partons unresolved
 - ▶ known from LO calculations



need method to extract implicit poles



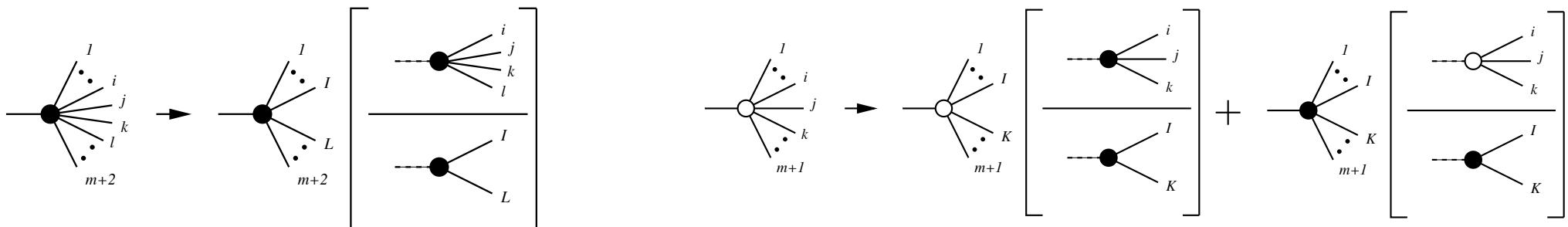
NNLO calculations: real radiation

Technical challenge: real radiation for arbitrary final state cuts

- ▶ two unresolved partons at tree level, one parton at one loop
- ▶ infrared limits are process-independent

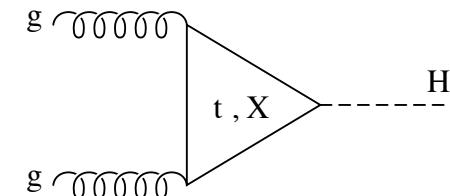
Solutions

- ▶ sector decomposition: expansion in distributions, numerical integration
(T. Binoth, G. Heinrich; C. Anastasiou, K. Melnikov, F. Petriello; M. Czakon)
- ▶ subtraction: approximation in all unresolved limits, analytical integration
 - ▶ several well-established methods at NLO
 - ▶ NNLO for specific hadron collider processes: q_T subtraction (S. Catani, M. Grazzini)
 - ▶ NNLO for e^+e^- processes : antenna subtraction (A. Gehrmann-De Ridder, E.W.N. Glover, TG)

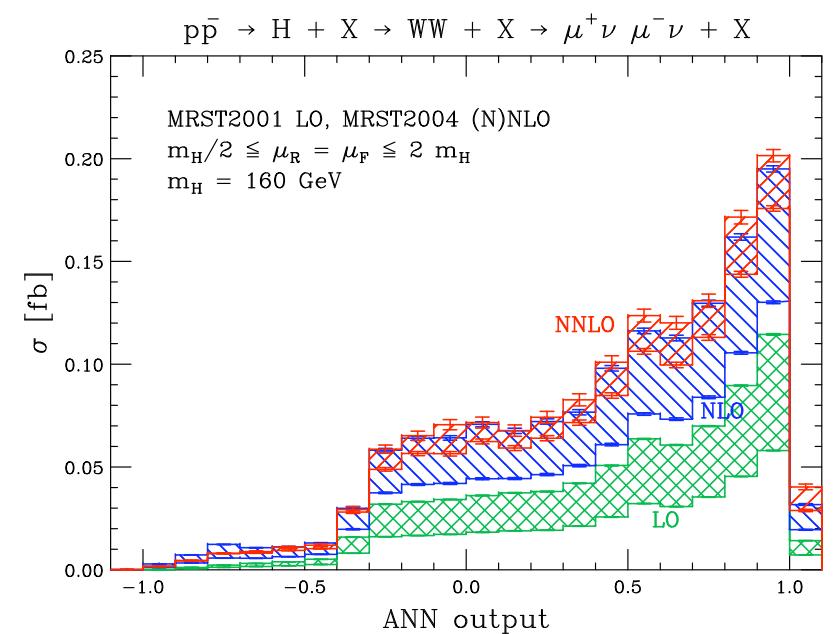


Higgs boson production at NNLO

Dominant production process: gluon fusion



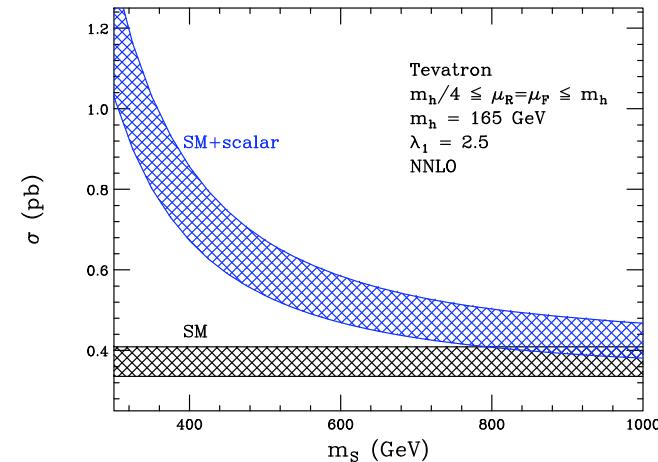
- ▶ exclusive calculations to NNLO, including H decay to $\gamma\gamma$ or VV
 - ▶ using sector decompostion
(C.Anastasiou, K. Melnikov, F. Petriello)
 - ▶ using q_T -subtraction (S. Catani, M. Grazzini)
- ▶ Higgs at Tevatron: $H \rightarrow WW \rightarrow l\nu l\nu$
 - ▶ all distributions to NNLO
(C.Anastasiou, G. Dissertori, M. Grazzini, F. Stöckli, B. Webber)
 - ▶ cuts on jet activity
 - ▶ neural-network output to NNLO
- ▶ precise prediction requires mixed QCD/EW corrections
(C.Anastasiou, R. Boughezal, F. Petriello)



Higgs boson production

Gluon fusion cross section: sensitive to new physics effects

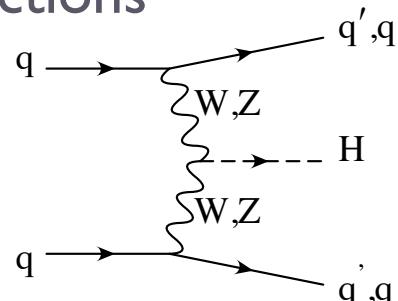
- ▶ squark/gluino loops
(C.Anastasiou, S. Beerli, A. Daleo; M. Mühlleitner, H. Rzehak, M. Spira)
- ▶ extra heavy quark families
(C.Anastasiou, R. Boughezal, E. Furlan)
- ▶ colour-octet scalars (R. Boughezal, F. Petriello)



Higgs production in vector boson fusion

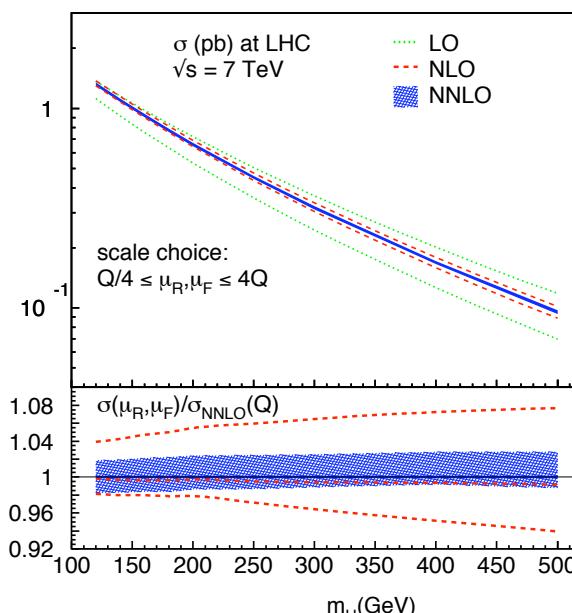
- ▶ factorizable NNLO corrections

(P. Bolzoni, F. Maltoni, S. Moch, M. Zaro)



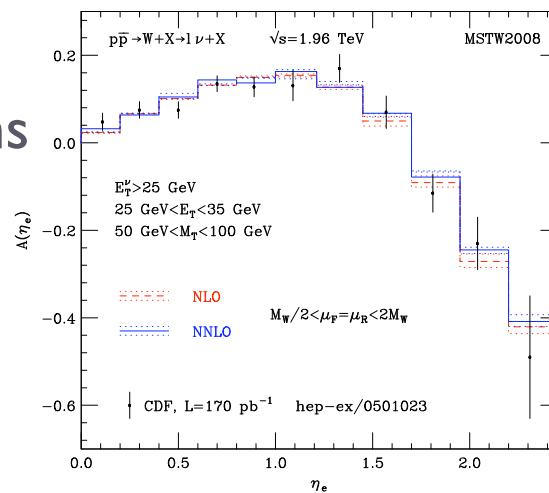
- ▶ SUSY loop corrections

(M. Rauch, W. Hollik, T. Plehn, H. Rzehak)

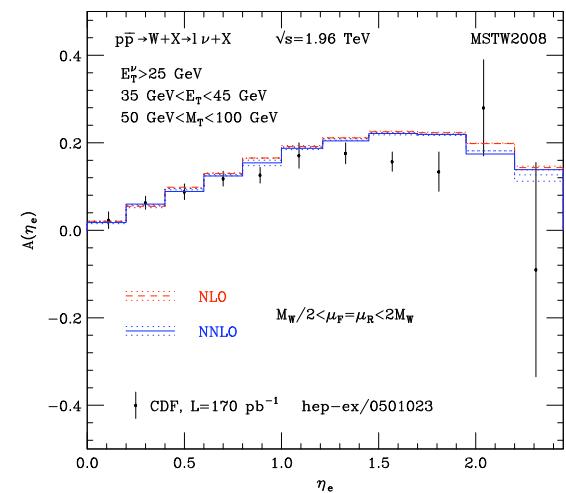


Vector boson production at NNLO

- ▶ Inclusive NNLO coefficient functions known for long time
- ▶ Recent results: fully exclusive calculations
 - ▶ parton-level event generator
 - ▶ using sector decomposition (K. Melnikov, F. Perriello)
 - ▶ using q_T subtraction (S. Catani, L. Cieri, G. Ferrera, D. de Florian, M. Grazzini)
 - ▶ including vector boson decay
 - ▶ allowing arbitrary final-state cuts
- ▶ Application: lepton charge asymmetry (S. Catani, G. Ferrera, M. Grazzini)
 - ▶ small NNLO corrections
 - ▶ determine quark distributions



Status of (N)NLO Calculations

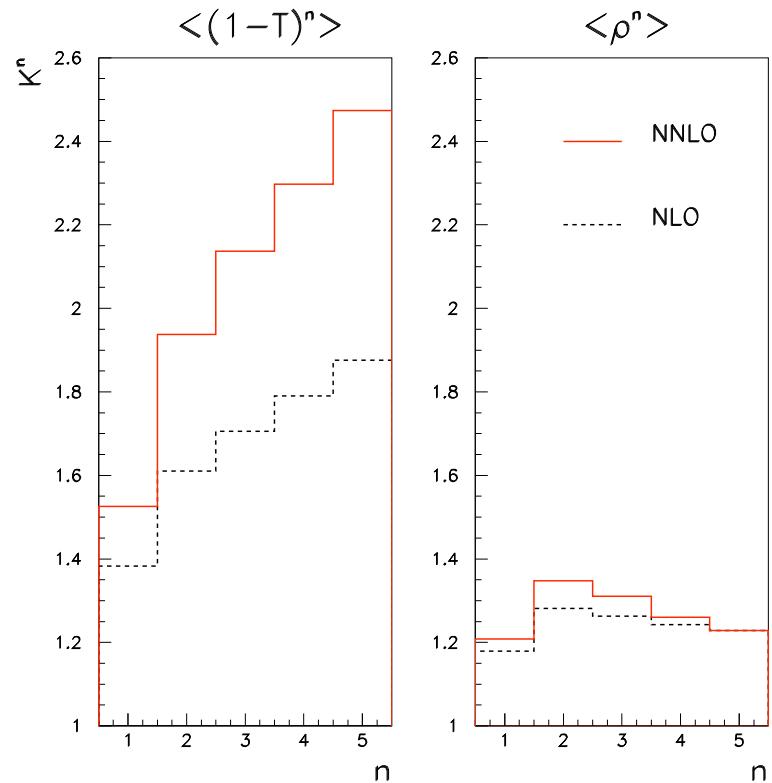


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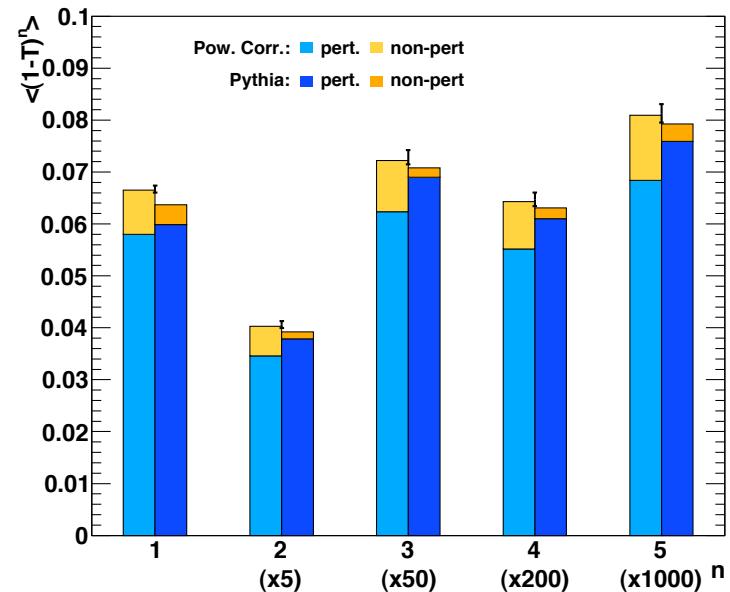
Jet production at NNLO: e^+e^- collisions

- ▶ Two calculations of NNLO corrections to $e^+e^- \rightarrow 3$ jets
 - ▶ using antenna subtraction (A. Gehrmann-De Ridder, E.W.N. Glover, G. Heinrich, TG; S. Weinzierl)
 - ▶ as parton-level event generator
 - ▶ allow evaluation of event shape distributions/moments and jet rates
- ▶ NNLO corrections differ substantially between observables
 - ▶ e.g. moments of thrust/heavy jet mass
 - ▶ improved consistency among shapes
- ▶ NNLO scale uncertainty
 - ▶ few per cent for most shape variables
 - ▶ one per cent for three-jet rate
- ▶ use to extract α_s from LEP data



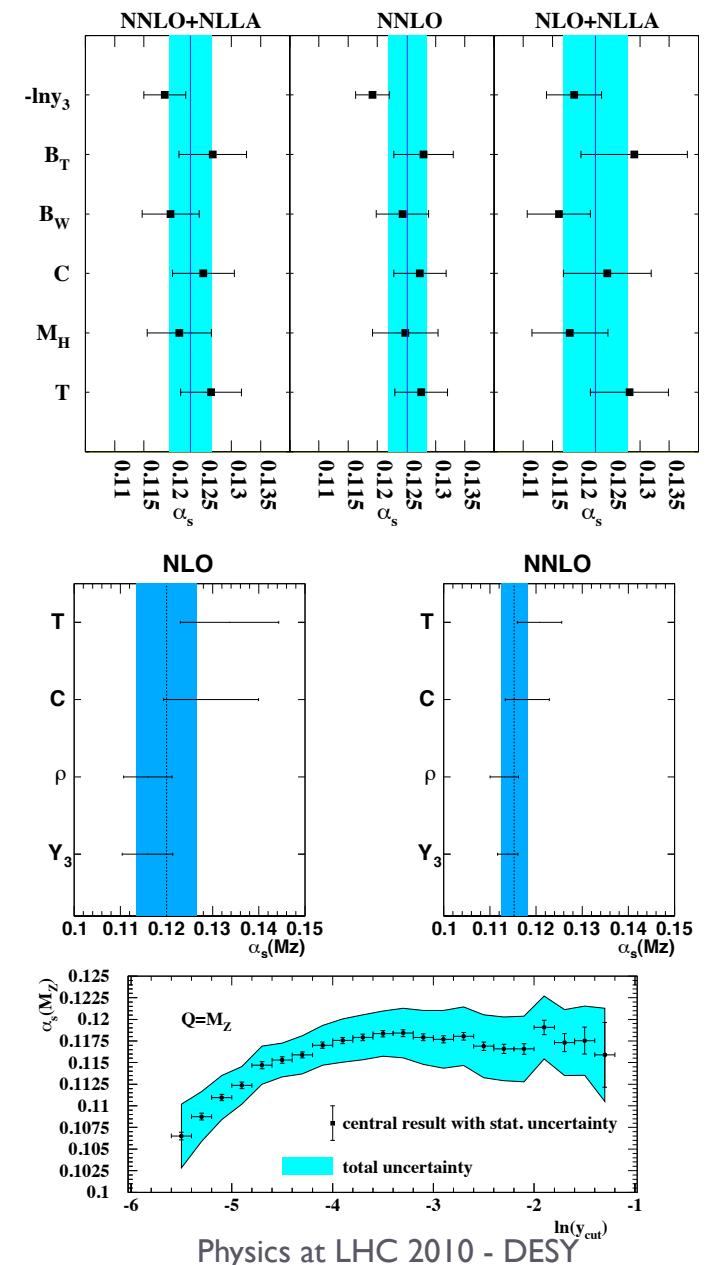
Jet production at NNLO: e^+e^- collisions

- ▶ Event shapes: matching NNLO onto resummation in 2-jet limit
 - ▶ NNLO+NLLA for all shapes (G. Luisoni, H. Stenzel, TG)
 - ▶ NNLO+N³LLA for thrust and heavy jet mass (T. Becher, M. Schwartz; Y.T. Chien)
- ▶ hadronization corrections
 - ▶ from LL parton-shower event generators
 - ▶ from renormalon-based dispersive model (Y. Dokshitzer, G. Marchesini, B. Webber)
 - ▶ extend dispersive model to NNLO
(M. Jaquier, G. Luisoni, TG)
 - ▶ power corrections differ substantially



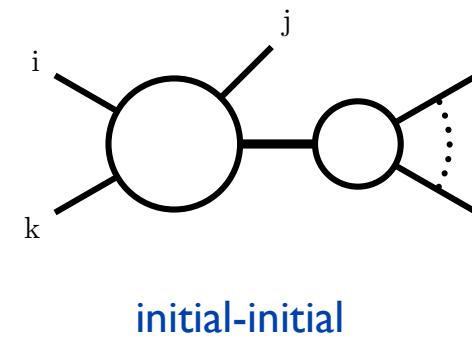
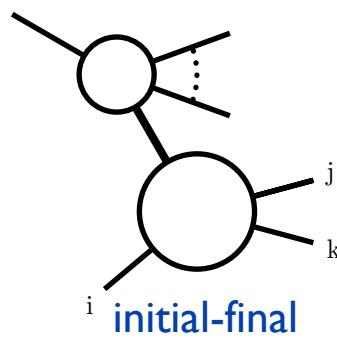
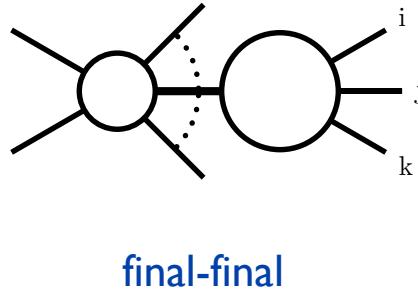
$\alpha_s(M_Z)$ from NNLO jet observables

- ▶ event shapes at NNLO+NLLA
 - ▶ JADE (S. Bethke, S. Kluth, C. Pahl, J. Schieck)
 - ▶ $0.1172 \pm 0.0006 \text{ (st)} \pm 0.0040 \text{ (sy)} \pm 0.0030 \text{ (th)}$
 - ▶ ALEPH (G. Dissertori, A. Gehrmann-De Ridder, E.W.N. Glover, G. Heinrich, G. Luisoni, H. Stenzel, TG)
 - ▶ $0.1224 \pm 0.0009 \pm 0.0015 \pm 0.0035$
- ▶ thrust at NNLO+ N^3LLA (T. Becher, M. Schwartz)
 - ▶ $0.1172 \pm 0.0010 \pm 0.0014 \pm 0.0012$
- ▶ thrust: NNLO+dispersive model (R. Davison, B. Webber)
 - ▶ 0.1164 ± 0.0027
- ▶ moments: NNLO+dispersive model
 - ▶ JADE/OPAL (M. Jaquier, G. Luisoni, TG)
 - ▶ $0.1153 \pm 0.0017 \text{ (exp)} \pm 0.0023 \text{ (th)}$
- ▶ three-jet rate at NNLO
 - ▶ ALEPH (G. Dissertori et al.)
 - ▶ $0.1175 \pm 0.0020 \text{ (exp)} \pm 0.0015 \text{ (th)}$



NNLO jet cross sections at hadron colliders

- ▶ two-loop matrix elements known for:
 - ▶ two-jet production
(C.Anastasiou, E.W.N. Glover, C. Oleari, M.E.Tejeda-Yeomans; Z. Bern, A. De Freitas, L.J. Dixon)
 - ▶ vector-boson-plus-jet production (E. Remiddi,TG)
 - ▶ (2+l) jet production in DIS (E.W.N. Glover,TG)
- ▶ antenna subtraction formalism at NNLO: radiators in initial state
 - ▶ final-final antennae known
 - ▶ initial-final antennae derived recently: sufficient for (2+l) jets in DIS
(A. Daleo,A. Gehrmann-De Ridder, G. Luisoni,TG)
 - ▶ initial-initial in progress (N. Glover, J. Pires; R. Boughezal,A. Gehrmann-De Ridder, M. Ritzmann)



Towards top quark pairs at NNLO

- ▶ two-loop matrix elements: $q\bar{q} \rightarrow t\bar{t}$ and $gg \rightarrow t\bar{t}$
 - ▶ known in large-energy limit (M. Czakon, A. Mitov, S. Moch)
 - ▶ quark-initiated process: known numerically (M. Czakon)
 - ▶ quark-initiated process: fermionic contributions and leading-colour terms confirmed analytically (R. Bonciani, A. Ferroglia, D. Maitre, C. Studerus, TG)
 - ▶ one-loop self-interference known (J. Körner, Z. Merebashvili, M. Rogal; C. Anastasiou, M. Aybat)
- ▶ one-loop and tree-level matrix elements known from NLO corrections to $pp \rightarrow t\bar{t} + j$ (S. Dittmaier, P. Uwer, S. Weinzierl)
- ▶ requires: method to handle NNLO real radiation
 - ▶ including hadronic initial states and massive particles
 - ▶ using sector decomposition (M. Czakon)
 - ▶ developments towards massive antenna subtraction
(A. Gehrmann-De Ridder, M. Ritzmann)



Infrared Structure and Resummation



Status of (N)NLO Calculations

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Resummation of large logarithms

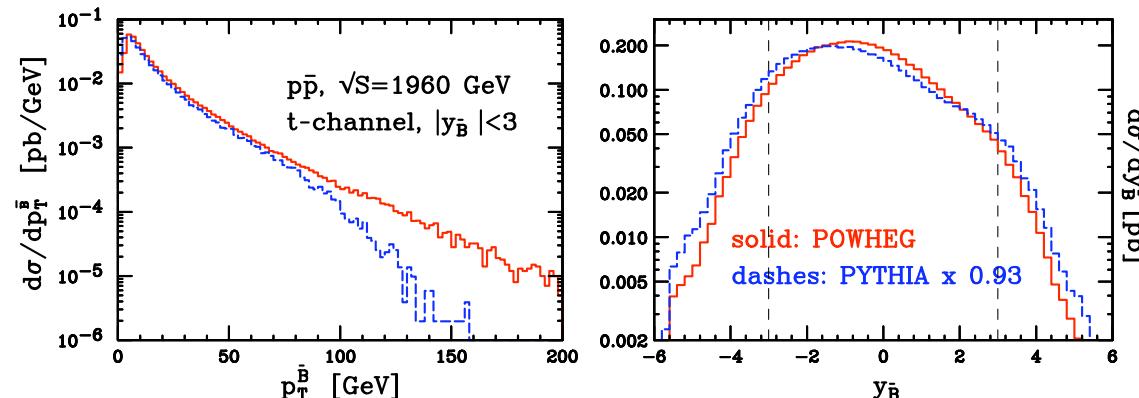
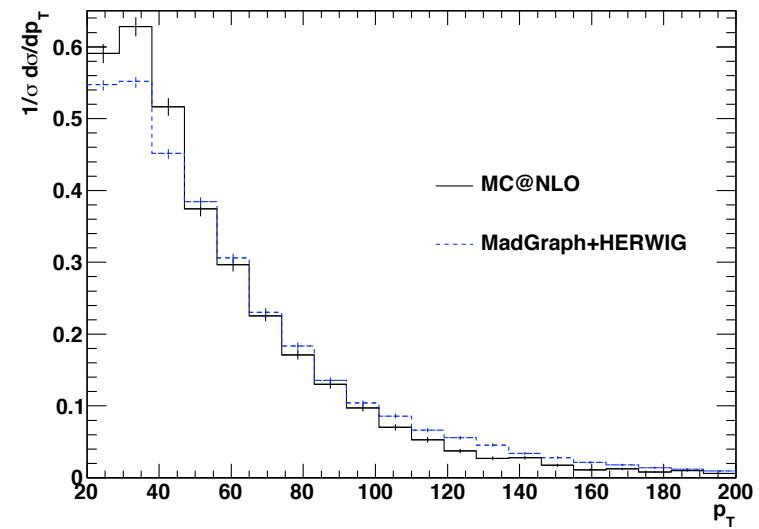
- ▶ QCD perturbative expansion in α_s
 - ▶ reliable, if process is defined by single hard scale
 - ▶ problematic, if several largely different scales contribute
 - ▶ encounter large logarithms at each perturbative order (e.g. $\log^n (p_T/M_W)$)
 - ▶ problematic, if specific restrictions apply to final state
 - ▶ phase space for soft radiation is limited (e.g. $\log^n (1-x)$ in DIS, Drell-Yan)
 - ▶ problematic if final state multiplicity is unrestricted
 - ▶ large corrections in high energy limit (e.g. $\log^n x$ in DIS: BFKL)
- ▶ need for rearranging perturbative series
 - ▶ resummation of large logarithmic corrections to all orders
- ▶ leading logarithmic resummation
 - ▶ parton shower based event generators (HERWIG, PYTHIA, SHERPA,...)



Resummation and fixed order

► Combining NLO and parton shower generators

- ▶ MC@NLO approach (B.Webber, S. Frixione)
 - ▶ $W^\pm t$ production, including interference effects (C.White, S. Frixione, E. Laenen, F. Maltoni)
 - ▶ $H^\pm t$ production (C.Weydert, S. Frixione, M. Herquet, M. Klasen, E. Laenen, T. Plehn, G. Stavenga, C.White)
- ▶ POWHEG approach (S. Frixione, P. Nason, C. Oleari)
 - ▶ single top production (S.Alioli, P. Nason, C. Oleari, E. Re)
 - ▶ Higgs in vector boson fusion (P. Nason, C. Oleari)
 - ▶ general framework: POWHEG box



Understanding infrared structure

Infrared poles in loop amplitudes \leftrightarrow logarithms in real emission

- ▶ predict IR poles at two loop from resummation
(S.Catani; G. Sterman, M. Tejeda-Yeomans)
- ▶ predict large-x resummation coefficients for DIS, DY, Higgs production from IR poles of three-loop from factors (S. Moch, J. Vermaseren, A. Vogt)
- ▶ IR poles in QCD \leftrightarrow UV poles in soft-collinear effective theory (SCET)
 - ▶ pole structure from multiplicative renormalization in SCET (T. Becher, M. Neubert)

$$|\mathcal{M}_n(\{\underline{p}\}, \mu)\rangle = \lim_{\epsilon \rightarrow 0} Z^{-1}(\epsilon, \{\underline{p}\}, \mu) |\mathcal{M}_n(\epsilon, \{\underline{p}\})\rangle$$

- ▶ all-order conjecture: IR poles of massless multi-loop multi-leg determined by cusp anomalous dimension and collinear anomalous dimensions
(T. Becher, M. Neubert; L. Dixon, E. Gardi, L. Magnea)

$$Z(\epsilon, \{\underline{p}\}, \mu) = P \exp \left[\int_\mu^\infty \frac{d\mu'}{\mu'} \Gamma(\{\underline{p}\}, \mu') \right], \quad \Gamma(\{\underline{p}\}, \mu) = \sum_{(i,j)} \frac{\mathbf{T}_i \cdot \mathbf{T}_j}{2} \gamma_{\text{cusp}}(\alpha_s) \ln \frac{\mu^2}{-s_{ij}} + \sum_i \gamma^i(\alpha_s)$$

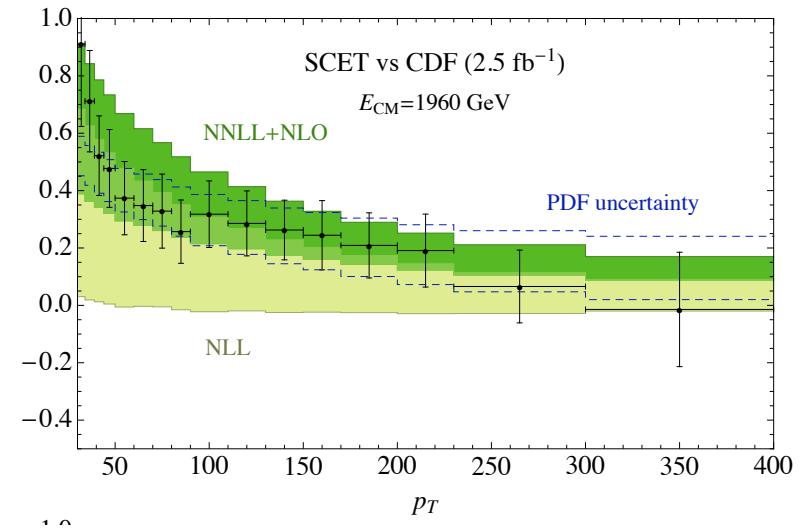


Resummation in SCET

General structure of resummation (J. Collins, G. Sterman, D. Soper)

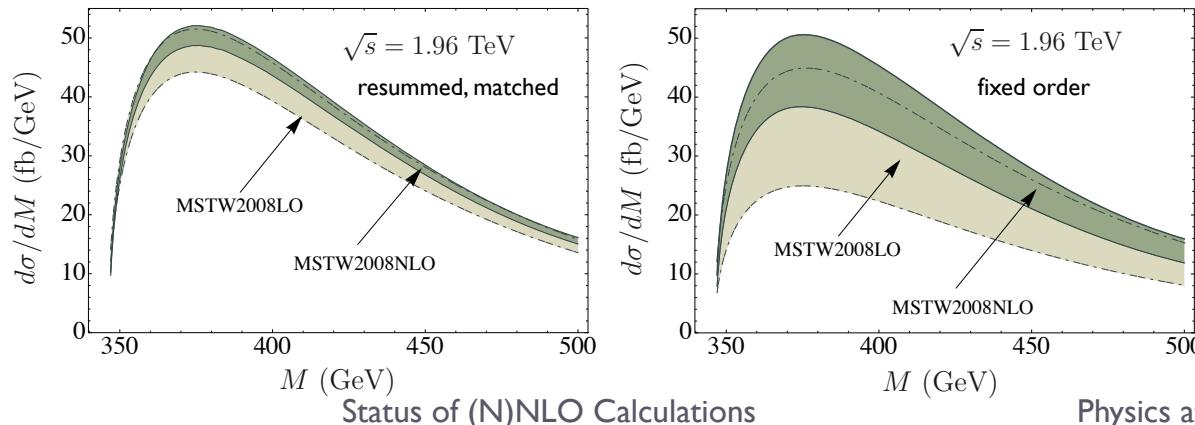
$$\sigma = (\text{hard}) \times (\text{soft}) \times (\text{jet functions - final state collinear}) \times (\text{parton distributions})$$

- ▶ only hard coefficient is process dependent
- ▶ SCET identifies each element with an operator or a non-local function
(A. Idilbi, X. Ji, F.Yuan; T. Becher, M. Neubert, B. Pecjak)
 - ▶ each element has natural scale (hard, collinear, soft)
 - ▶ compute anomalous dimensions
 - ▶ resum large logarithms by solving evolution equations
- ▶ applications, matched onto fixed order
 - ▶ thrust in e^+e^- (T. Becher, M. Schwartz)
 - ▶ inclusive Drell-Yan and Higgs production
(A. Idilbi, X. Ji, F.Yuan; V.Ahrens, T. Becher, M. Neubert, L.L.Yang)
 - ▶ inclusive photons (T. Becher, M. Schwartz)
- ▶ open issues
 - ▶ jet production, radiation off incoming partons



Top quark pair production: resummation

- ▶ Soft-gluon resummation: previously NLO+NLL
- ▶ infrared structure more involved with massive quarks
 - ▶ multi-particle correlations appear (A. Ferroglia, M. Neubert, B. Pecjak, L.L. Yang)
 - ▶ can predict IR poles to two-loop order (M. Beneke, M. Czakon, P. Falgari, A. Mitov)
- ▶ recent progress: NLO+NNLL
 - ▶ dominant contributions derived previously (S. Moch, P. Uwer; N. Kidonakis)
 - ▶ full corrections obtained from massive soft anomalous dimensions (M. Czakon, A. Mitov, G. Sterman)
 - ▶ and using SCET (V. Ahrens, A. Ferroglia, M. Neubert, B. Pecjak, L.L. Yang)



Conclusions

Precision QCD crucial for successful LHC physics

- ▶ masses, couplings and parton distributions
- ▶ jets and event shapes as observables and tools
- ▶ understanding signals and backgrounds

Theory is getting ready for future challenges

- ▶ improved jet algorithms and event shape definitions
- ▶ enormous progress on NLO multi-leg calculations
- ▶ first NNLO calculations for precision observables
- ▶ turn into NNLO parton distributions
- ▶ understanding of infrared structure enables resummation

