

Multi-jet merging at tree-level and 1-loop level

Stefan Höche ¹

ITP, University of Zürich



Physics at LHC 2010
Hamburg, June 11th

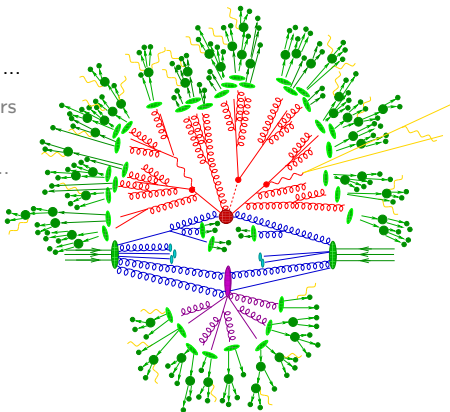


¹ in collaboration with T. Gehrmann, F. Krauss, M. Schönherr, F. Siegert

Multi-jet merging: Where do we stand?

ME $\otimes$ PS merging at tree level

- Well established around for $\gtrsim 10$ years
PRD57(1998)5767, NPB632(2002)343, JHEP11(2001)063, ...
- Strong recent activity Truncated showers
JHEP05(2009)053, JHEP11(2009)038
- Various approaches CKKW(L), MLM, ...
JHEP05(2002)046, JHEP02(2009)017, ...
- Several automated codes
e.g. in hep-ph/0602031, EPJC53(2008)473

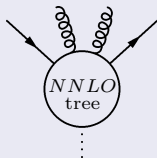


ME $\otimes$ PS merging at 1-loop level

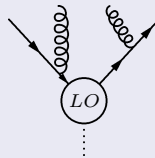
- Pioneered by MC@NLO & POWHEG
JHEP06(2002)029, JHEP11(2004)040, ...
- Multijets recently discussed NL^3 , MENLOPS
JHEP12(2008)070, arXiv:1004.1764 [hep-ph]
- Automation within reach ?



Problem: Higher-order ME and PS describe the same final state !



- σ from coherent sum of all Feynman graphs
- No resummation

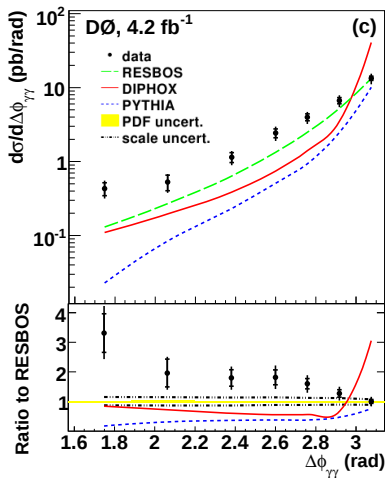
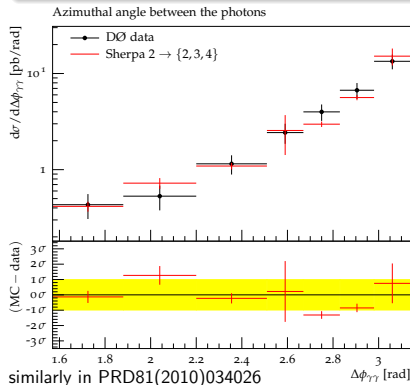


- σ from LO ME & PS splittings
- Proper resummation in parts of phase space

How do we run a parton shower on a $N^{\times}$ LO tree-level matrix element ?

- 1 Find suitable starting conditions for the parton shower
i.e. find a tree-structure corresponding to the full ME
which can be used by the parton shower as a branching history
- 2 Make sure not to double-count or miss out emissions
i.e. eventually populate the whole available real emission
phase space with *either* matrix elements *or* the parton shower

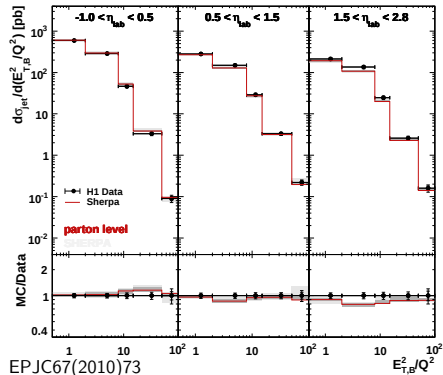
$$E_T^{\gamma^1} > 21 \text{ GeV}, \quad E_T^{\gamma^2} > 20 \text{ GeV}, \\ |\eta^\gamma| < 0.9, \quad E_T^{R=0.4} - E_T^\gamma < 2.5 \text{ GeV}$$



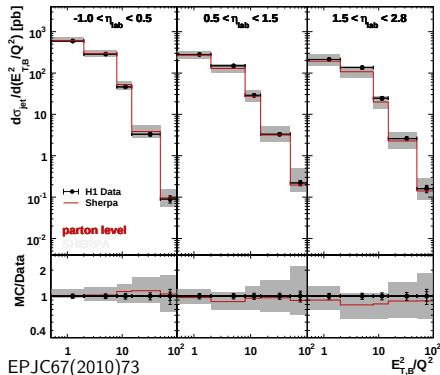
SHERPA prediction: Merged $2 \rightarrow \{2,3,4\}$ -jet/ γ plus $gg \rightarrow \gamma\gamma$ box

Example results: Inclusive jets in DIS PLB542(2002)193

$5 \text{ GeV}^2 < Q^2 < 100 \text{ GeV}^2$, $E_{T,B} > 5 \text{ GeV}$, $-1 < \eta_{\text{lab}} < 2.8$



Variation of ME $\otimes$ PS parameters



Scale variations $\mu_F = \mu_R$

SHERPA prediction: Merged $2 \rightarrow \{0,2,3,4,5\}$ -jet

Combining $\text{ME} \otimes \text{PS}$ with full NLO

At present ...

- We can merge “arbitrary” tree-level ME’s with PS’s
Several automated codes on the market
- Automation of 1-loop QCD corrections seems feasible
(Semi-)automated codes now emerging

We should make use of both and **automate $\text{ME} \otimes \text{PS}$ at 1-loop**

Strategy: Use whatever is available

- Process NLO parton-level events with PS’s
using MC@NLO or POWHEG method low multiplicity
- Combine NLO simulation with higher-order tree-level
using standard $\text{ME} \otimes \text{PS}$ technique high multiplicity

The POWHEG algorithm sketchy

The POWHEG master formula schematically

JHEP11(2004)040, JHEP11(2007)070, arXiv:1002.2581 [hep-ph], ...

$$d\sigma_{\text{NLO}} = d\Phi_B \bar{B}(\Phi_B) \left[\bar{\Delta}(k_{T,0}) + \sum \int_{k_{T,0}} d\Phi_{R|B} \frac{R(\Phi_R)}{B(\Phi_B)} \bar{\Delta}(k_T) \right]$$

with the NLO differential cross section $\bar{B} = B + V + I + d\Phi_{R|B} [R - S]$

and the POWHEG-Sudakov $\bar{\Delta}(k_T) = \exp \left\{ - \sum \int_{k_T} d\Phi_{R|B} \frac{R(\Phi_R)}{B(\Phi_B)} \right\}$

Two problems to be solved

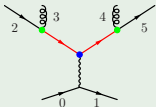
- Generate differential NLO cross section $d\Phi_B \bar{B}(\Phi_B)$
⇒ Requires integrator for N - and $N + 1$ -particle phase space
- Generate real emission according to POWHEG-Sudakov $\bar{\Delta}(k_T)$
⇒ Requires parton shower-like algorithm to exponentiate $\sum \int d\Phi_{R|B} R/B$

Implementing the POWHEG algorithm, Part I

Integration proceeds in two steps ...

Step I: The Born phase space via recycling

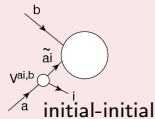
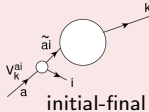
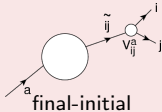
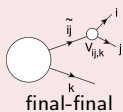
Standard phase-space generator, e.g. single channels from NPB9(1969)568
VEGAS-refined CLNS-80/447(1980) and combined in multi-channel CPC83(1994)141



$$D_{iso}(23, 45) \otimes P_0(23) \otimes P_0(45) \\ \otimes D_{iso}(2, 3) \otimes D_{iso}(4, 5)$$

Step II: The real-emission phase space new

Extra emission generator (EEG) produces additional parton starting from Φ_B
Kinematics according to CS dipole terms NPB485(1997)291, NPB627(2002)189



Implementing the POWHEG algorithm, Part I

Extra emission generator (EEG)
with multi-channeling over all
dipole configurations



Separate integration (sep)
of Born and real-emission kinematics
with (modified) standard integrator

Process	σ [pb] (EEG)	σ [pb] (sep)	σ [pb] (LO)
$e^+e^- \rightarrow 2jets$ $E_{\text{cms}}=91.2$ GeV	29449(19)	29454(18)	28381(18)
$e^+e^- \rightarrow 3jets$ as above, $y_{\text{cut}} = 10^{-1.92}$	9399(38)	9418(60)	7724(21)
$e^+e^- \rightarrow 4jets$ as above, $y_{\text{cut}} = 10^{-1.92}$	1377(14)	1357(21)	907(10)
$p\bar{p} \rightarrow e^- \bar{\nu}_e$ $E_{\text{cms}} = 1.96$ TeV, CTEQ 6.6	1331.7(5)	1332.2(4)	1098.6(3)
$p\bar{p} \rightarrow e^- \bar{\nu}_e + jet$ as above, $k_T = 10$ GeV, $D = 0.7$	389.0(16)	390.6(17)	282.9(5)
$p\bar{p} \rightarrow e^- \bar{\nu}_e + 2jets$ as above, $k_T = 10$ GeV, $D = 0.7$	104.2(7)	105.5(9)	73.9(2)

500k MC-points before cuts, no time limit, no error target
virtual part delivered by WhiteHat PRD78(2008)036003

Implementing the POWHEG algorithm, Part II

Need MC generator to exponentiate $\Gamma(k_T) = \sum \int_{k_T}^Q d\Phi_{R|B} R/B$

We know how to deal with this CPC82(1994)74

- Dice k_T of emission as $k_T = \Gamma^{-1} [-\log \#]$
- If Γ unknown, use overestimate $\tilde{\Gamma}$ and accept as $w = \Gamma(k_T)/\tilde{\Gamma}(k_T) > \#'$

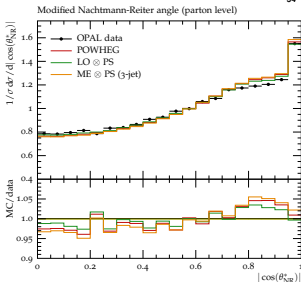
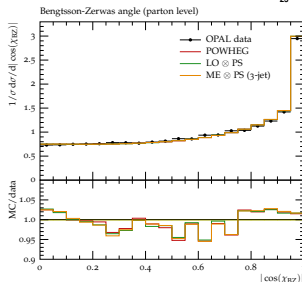
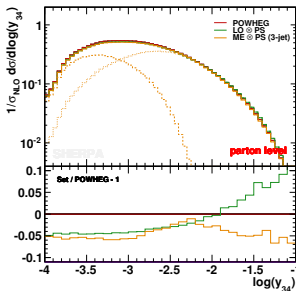
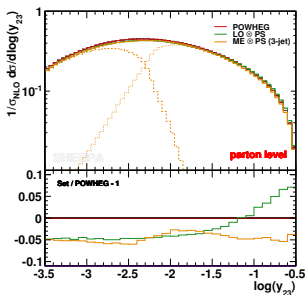
Now the whole trick is to find a suitable $\tilde{\Gamma}$

In fact, we have a pretty good estimate ...

Γ 's of existing parton showers are an ideal candidate

- We employ SHERPA's dipole-like parton shower (CSS) based on CS subtraction JHEP03(2008)038, PRD81(2010)034026
- Splitting functions are potentially enhanced, adapting to R/B larger than CSS approximation

Implementing the POWHEG algorithm, Part II



Jet rates and event shapes in $e^+e^- \rightarrow \text{jets}$

Compare:

- POWHEG
NLO rate & shape
→ reference
- $\text{ME} \otimes \text{PS}$ 3-jet
“NLO shape”

Shape agrees well with POWHEG result
Rate down by α_s/π
→ useful check !

- Parton shower
Shape & rate differ

⇒ POWHEG simulation ok for $e^+e^- \rightarrow 2 \text{ jets}$

Combining $\text{ME} \otimes \text{PS}$ with full NLO

POWHEG:

$$d\sigma_{\text{NLO}} = d\Phi_B \bar{B}(\Phi_B) \left[\bar{\Delta}(k_{T,0}) + \sum \int_{k_{T,0}} d\Phi_{R|B} \frac{R(\Phi_R)}{B(\Phi_B)} \bar{\Delta}(k_T) \right]$$

- $\bar{B}(\Phi_B)$ has NLO accuracy
- Bracket integrates to one

$\text{ME} \otimes \text{PS}$:

$$d\sigma_{\text{NLO}} = d\Phi_B B(\Phi_B) \left[\Delta(k_{T,0}) + \sum \int_{k_{T,0}} d\tilde{\Phi}_{R|B} \frac{R(\tilde{\Phi}_R)}{B(\Phi_B)} \Delta(k_T) \right]$$

- $B(\Phi_B)$ has LO accuracy
- Bracket integrates to $N(\Phi_B) \approx 1$

Striking similarity and similar accuracy up to **local K-factor** $\bar{B}(\Phi_B)/B(\Phi_B)$

⇒ **Recent proposal by K. Hamilton & P. Nason** arXiv:1004.1764 [hep-ph]

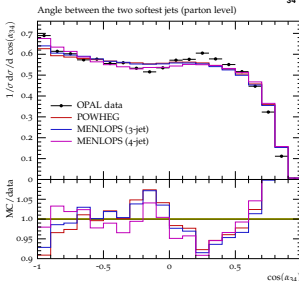
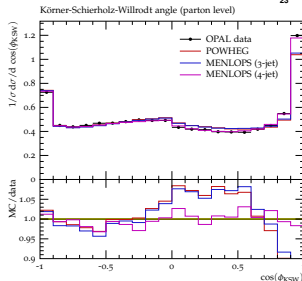
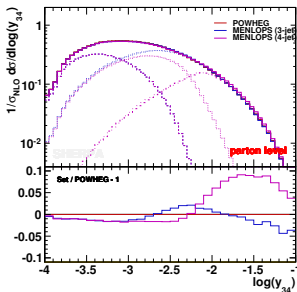
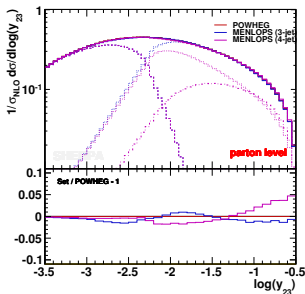
Combine POWHEG and $\text{ME} \otimes \text{PS}$ via phase-space slicing → MENLOPS

$\text{ME} \otimes \text{PS}$ rescaled to correct norm by global K-factor cut dependent

Sole drawback: Norm of event sample unknown due to non-unitarity of $\text{ME} \otimes \text{PS}$
Not an issue as long as correction is smaller than NLO effects!

We use a variant of this scheme: K-factor is local rather than global

MENLOPS Results



Jet rates and event shapes in $e^+e^- \rightarrow \text{jets}$

Compare:

- POWHEG
→ reference
- MENLOPS 3-jet
2 jets @ NLO
Shape & norm agree with POWHEG
- MENLOPS 4-jet
2 jets @ NLO
Shape & norm agree with POWHEG
Improved 4-jet predictions

⇒ MENLOPS ok for 2 jets @ NLO

Note that this is not a merging of NLO 2-jet with NLO 3-jet ! yet ...

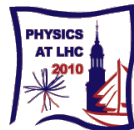
ME $\otimes$ PS at tree-level ...

- Becomes new standard in MC simulations
- Works well even for nontrivial processes
- No open questions except technical issues

ME $\otimes$ PS at 1-loop level

- NLO events at ME level largely automated
- POWHEG allows to shower these NLO events in principle
- Merging with higher-order tree-level straightforward
- The big challenge is to merge multiple NLO processes

We are on the way to automating ME $\otimes$ PS at 1-loop level !



ME $\otimes$ PS part I: Defining PS histories

Basic idea: **Interpret ME as if PS had produced it**

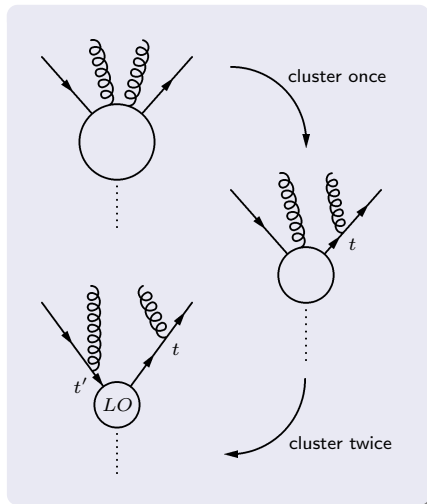
- Identify parton splittings acc. to PS branching probability
- Combine partons into mother parton acc. to inverse PS kinematics
- Continue until $2 \rightarrow 2$ core process

→ **Cluster algorithm similar to k_T algo**

PS starts at core process and possibly radiates additional partons on intermediate lines i.e. “between” ME partons

ME branchings must be respected
evolution-, splitting- & angular variable preserved

→ **Truncated shower**
universal concept for ME-PS merging



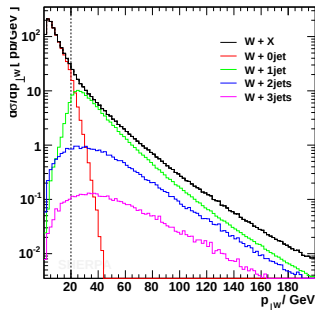
ME $\otimes$ PS part II: Slicing the phase space

Basic idea: **Separate phase space into “hard” and “soft” region**

- Matrix elements populate hard domain
- Parton shower populates soft domain

need criterion to define “hard” & “soft” as above and below a certain cut value

→ **Jet criterion** Q e.g. k_T -jet measure



First replace kernels $\mathcal{K}_{ab}$ in QCD evolution equations with

$$\mathcal{K}_{ab}^{\text{ME}}(\xi, \bar{t}) = \mathcal{K}_{ab}(\xi, \bar{t}) \Theta [Q_{ab}(\xi, \bar{t}) - Q_{\text{cut}}] \quad \mathcal{K}_{ab}^{\text{PS}}(\xi, \bar{t}) = \mathcal{K}_{ab}(\xi, \bar{t}) \Theta [Q_{\text{cut}} - Q_{ab}(\xi, \bar{t})]$$

Then replace evolution kernel in ME domain with ratio of full MEs

$$\mathcal{K}_{ab}^{\text{ME}}(z, t) \rightarrow \frac{2\pi/\alpha_s(z, t)}{d\hat{\sigma}_a^{(N)}(\Phi_N)} \frac{d\hat{\sigma}_b^{(N+1)}(z, t; \Phi_N)}{d \log(t/\mu^2) dz} \Theta [Q_{ab}(\xi, \bar{t}) - Q_{\text{cut}}]$$