

# Higgs pair production in the ElectroWeak Chiral Lagrangian framework

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für Physik



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Particle Physics Challenges - DESY  
Hamburg

# Motivations

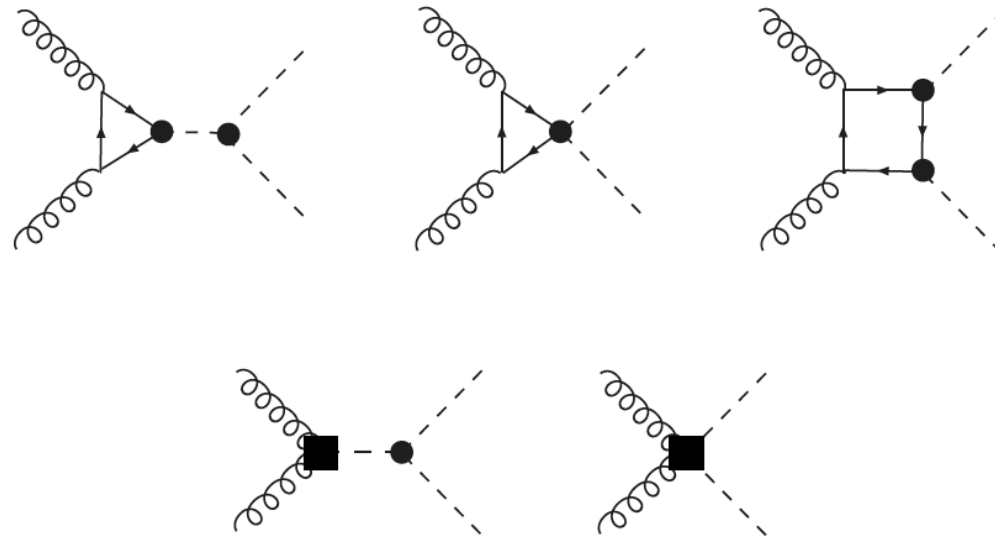
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- No evidences of new physics have been found yet.
- New physics may hide at higher scales, therefore an Effective Field Theory (EFT) can allow us to parametrize new physics contributions.
- We work in the non-linear EFT framework provided by the ElectroWeak Chiral Lagrangian (EWChL) [Buchalla et al. arXiv:1307.5017].
- Many of the Higgs couplings are well constrained already or can be obtained from other processes, but this is not true for the Higgs boson self coupling.
- We focus on the  $gg$  to  $HH$  process.

$$\begin{aligned} L_{gg \rightarrow hh} \supset & -m_t \bar{t}t \left( c_t \frac{h}{v} + c_{tt} \frac{h^2}{2v^2} \right) - c_{hhh} \frac{1}{6} \left( \frac{3m_h^2}{v} \right) h^3 \\ & + \frac{g_s^2}{16\pi^2} \langle G_{\mu\nu} G^{\mu\nu} \rangle \left( c_{ggh} \frac{h}{v} + c_{gghh} \frac{h^2}{2v^2} \right) \end{aligned}$$

# EWChL for $gg \rightarrow HH$

- At leading order there are 5 different diagrams: 2 SM-like diagrams and 3 totally new diagrams.



- The Feynman amplitude of this process can be written as: 
$$M^{\mu\nu} = F_1 T_1^{\mu\nu} + F_2 T_2^{\mu\nu}$$

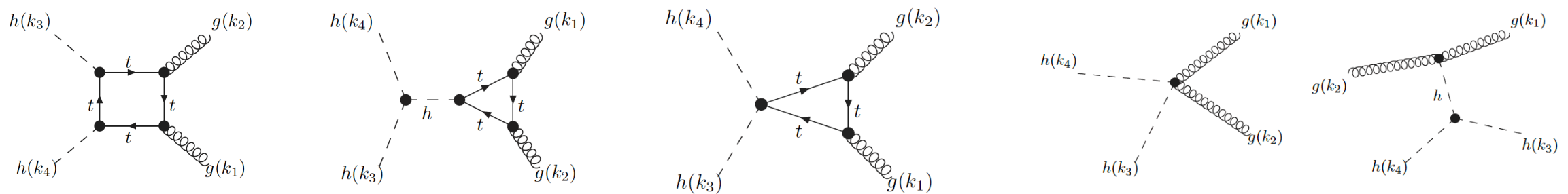
$$T_1^{\mu\nu} = -g^{\mu\nu} + \frac{k_1^\nu k_2^\mu}{(k_1 \cdot k_2)} \quad T_2^{\mu\nu} = g^{\mu\nu} + \frac{1}{k_T^2 (k_1 \cdot k_2)} (m_h^2 k_1^\nu k_2^\mu - 2(k_1 \cdot k_3) k_3^\nu k_2^\mu - 2(k_2 \cdot k_3) k_3^\mu k_1^\nu) + 2(k_1 \cdot k_2) k_3^\mu k_3^\nu$$

- In order to compute the deviations of the model, we need to know the contributions of these new diagrams to the form factors  $F_1$  and  $F_2$ .

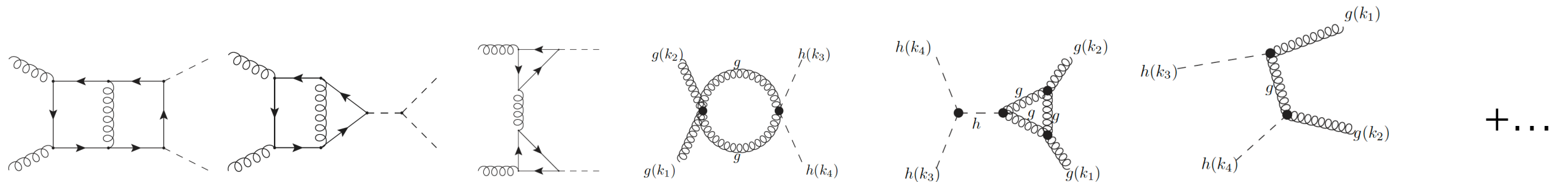
$$\hat{\sigma}^{LO} = \frac{\alpha_s^2}{2^{12} v^4 (2\pi)^3 \hat{s}^2} \int_{\hat{t}_-}^{\hat{t}^+} d\hat{t} \{ |F_1|^2 + |F_2|^2 \}$$

# $gg \rightarrow HH$ contributions in the EWChL framework

## Leading order

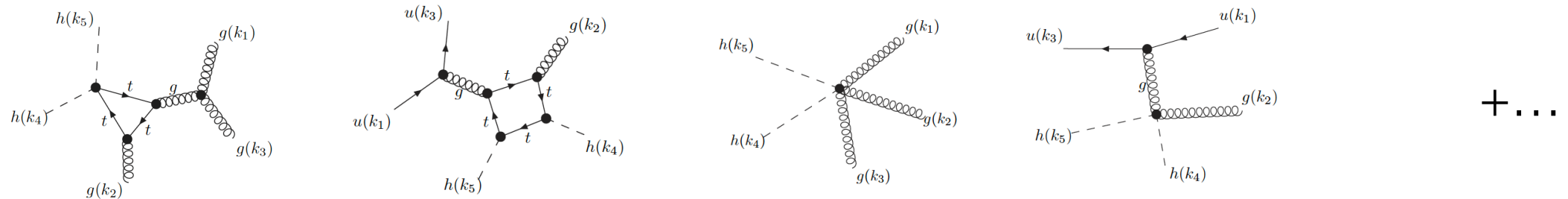


## NLO QCD virtual



## NLO QCD real

Borowka et al. arXiv:1608.04798



# Method of the calculation

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- In order to obtain the LO QCD cross section and the NLO QCD real corrections we used a C++ code linked to GoSam [Cullen et al. [arXiv:1404.7096](#) ].
- For the NLO QCD virtual correction we used the two-loop integrals computed numerically for the SM (using the program SecDec) case [Borowka et al. [arXiv:1608.04798](#)] as far as possible and then manipulated the results using a python script.
- Within our setup we can produce the full top mass dependent NLO QCD cross section and differential distributions.
- In the following we will show distributions for some benchmark points and compare them with SM results.

# Benchmark points

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- Benchmark points introduced in Carvalho et al. [[arXiv:1507.02245](#), [arXiv:1608.06578](#) and [arXiv:1710.08261](#)], calculating LO distributions.
- According to the values of the five anomalous couplings the shape of the differential distribution can change.
- The idea of the benchmark points is to define 12 clusters with different shapes, which characterize distributions attributed to a given choice of couplings.
- We produced the inclusive and differential cross sections at NLO with full top mass dependence.

Benchmark	$c_{hhh}$	$c_t$	$c_{tt}$	$c_{ggh}$	$c_{gghh}$
1	7.5	1.0	-1.0	0.0	0.0
2	1.0	1.0	0.5	$-\frac{1.6}{3}$	-0.2
3	1.0	1.0	-1.5	0.0	$\frac{0.8}{3}$
4	-3.5	1.5	-3.0	0.0	0.0
5	1.0	1.0	0.0	$\frac{1.6}{3}$	$\frac{1.0}{3}$
6	2.4	1.0	0.0	$\frac{0.4}{3}$	$\frac{0.2}{3}$
7	5.0	1.0	0.0	$\frac{0.4}{3}$	$\frac{0.2}{3}$
8a	1.0	1.0	0.5	$\frac{0.8}{3}$	0.0
9	1.0	1.0	1.0	-0.4	-0.2
10	10.0	1.5	-1.0	0.0	0.0
11	2.4	1.0	0.0	$\frac{2.0}{3}$	$\frac{1.0}{3}$
12	15.0	1.0	1.0	0.0	0.0
SM	1.0	1.0	0.0	0.0	0.0

# Benchmark points

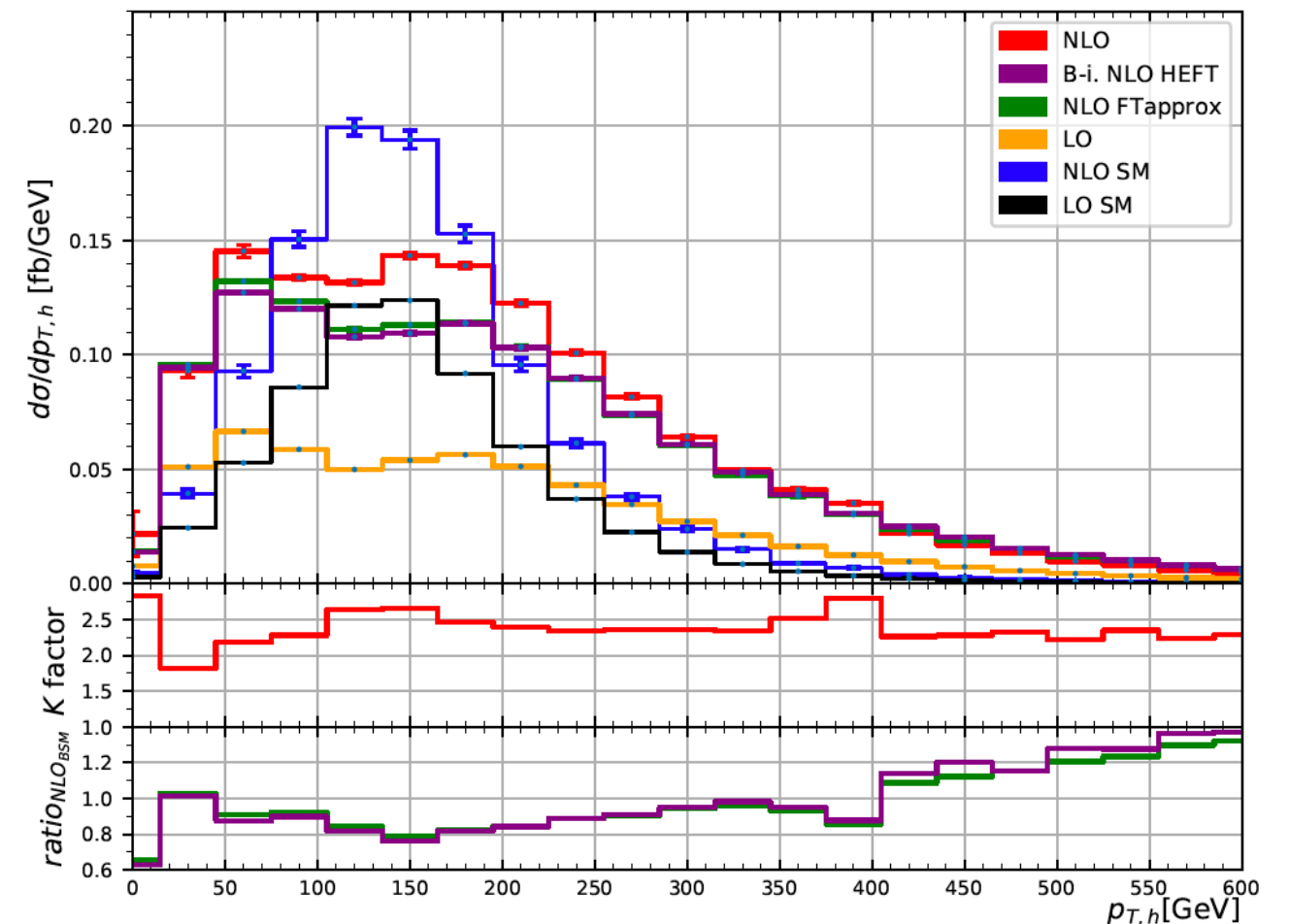
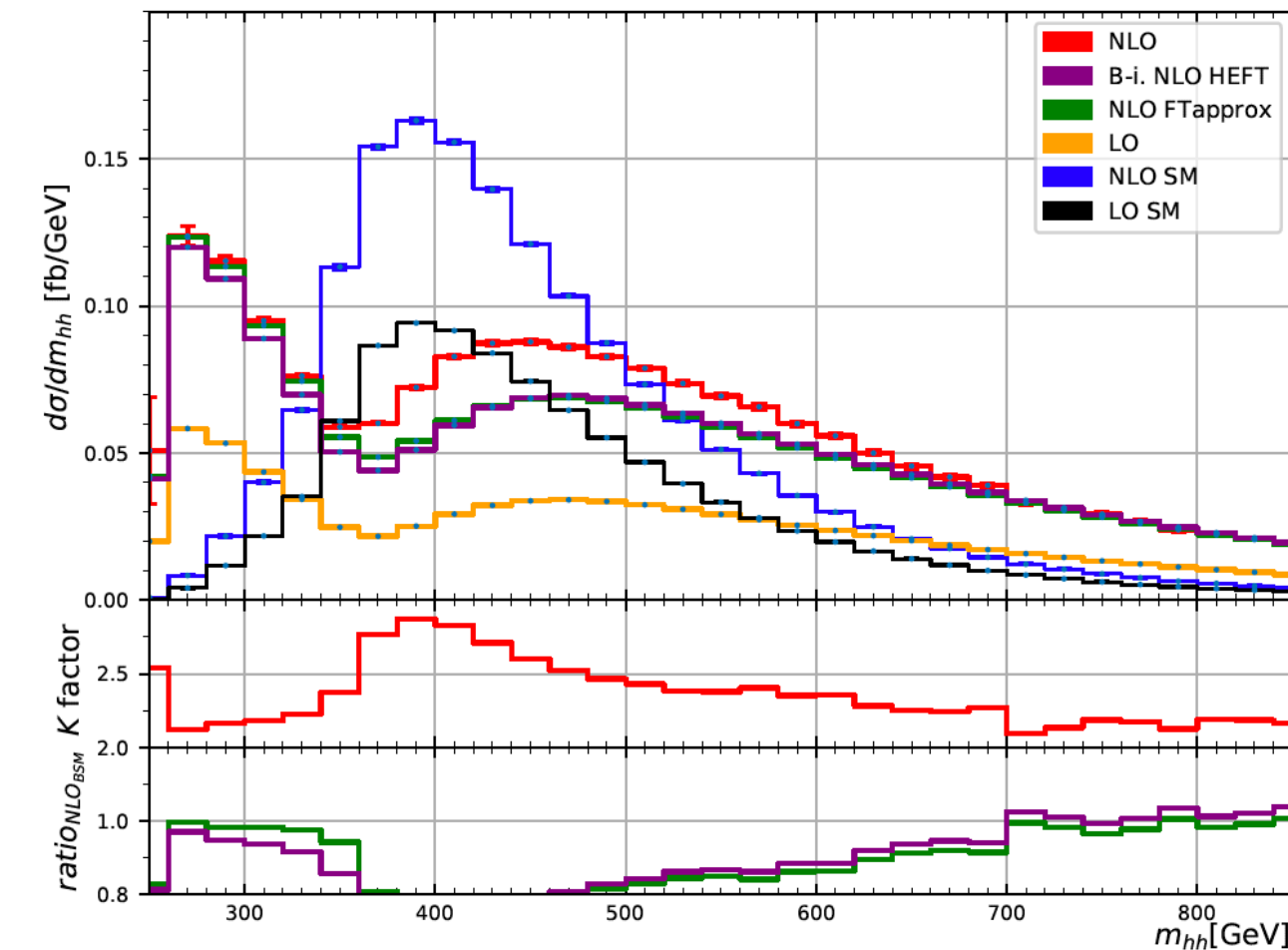
Benchmark	$\sigma_{NLO}$ [fb]	K-factor	scale uncert. [%]	stat. uncert. [%]	$\frac{\sigma_{NLO}}{\sigma_{NLO,SM}}$
$B_1$	194.89	1.88	$+19$ $-15$	1.6	5.915
$B_2$	14.55	1.88	$+5$ $-13$	0.56	0.4416
$B_3$	1047.37	1.98	$+21$ $-16$	0.15	31.79
$B_4$	8922.75	1.98	$+19$ $-16$	0.39	270.8
$B_5$	59.325	1.83	$+4$ $-15$	0.36	1.801
$B_6$	24.69	1.89	$+2$ $-11$	2.1	0.7495
$B_7$	169.41	2.07	$+9$ $-12$	2.2	5.142
$B_{8a}$	41.70	2.34	$+6$ $-9$	0.63	1.266
$B_9$	146.00	2.30	$+22$ $-16$	0.31	4.431
$B_{10}$	575.86	2.00	$+17$ $-14$	3.2	17.48
$B_{11}$	174.70	1.92	$+24$ $-8$	1.2	5.303
$B_{12}$	3618.53	2.07	$+16$ $-15$	1.2	109.83
$SM$	32.95	1.66	$+14$ $-13$	0.1	1

- Some of them already ruled out [[arXiv:1806.00408](#), [ATLAS-CONF-2018-043](#)].

# Benchmark points: $m_{hh}$ and $p_{T,h}$ distributions

## Benchmark 8-a

$$\frac{\sigma_{NLO}}{\sigma_{NLO,SM}} = 1.266$$



$$c_{hhh} = 1.0, c_t = 1.0, c_{tt} = 0.5, c_{ggh} = \frac{0.8}{3}, c_{gghh} = 0$$



# Cross section parametrization

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- In general the LO cross section for the process can be parametrized as function of the 5 BSM couplings in terms of 15 parameters.

$$\begin{aligned} \frac{\sigma_{LO}}{\sigma_{LO,SM}} = & [A_1 c_t^4 + A_2 c_{tt}^2 + A_3 c_{thh}^2 c_{hhh}^2 + A_4 c_{ghh}^2 c_{hhh}^2 + A_5 c_{gghh}^2 + A_6 c_{tt} c_t^2 + A_7 c_t^3 c_{hhh} \\ & + A_8 c_{tt} c_t c_{hhh} + A_9 c_{tt} c_{ggh} c_{hhh} + A_{10} c_{tt} c_{cgghh} + A_{11} c_t^2 c_{ggh} c_{hhh} + A_{12} c_t^2 c_{gghh} \\ & + A_{13} c_t c_{hhh}^2 c_{ggh} + A_{14} c_t c_{hhh} c_{gghh} + A_{15} c_{ggh} c_{hhh} c_{gghh}] \end{aligned}$$

- We determined the value of the 15 parameters via projections.
- We checked our results with the ones of Azatov et al. [[arXiv:1502.00539](https://arxiv.org/abs/1502.00539)] and found agreement.
- At NLO QCD the 15 coefficients change plus there are 8 new ones.

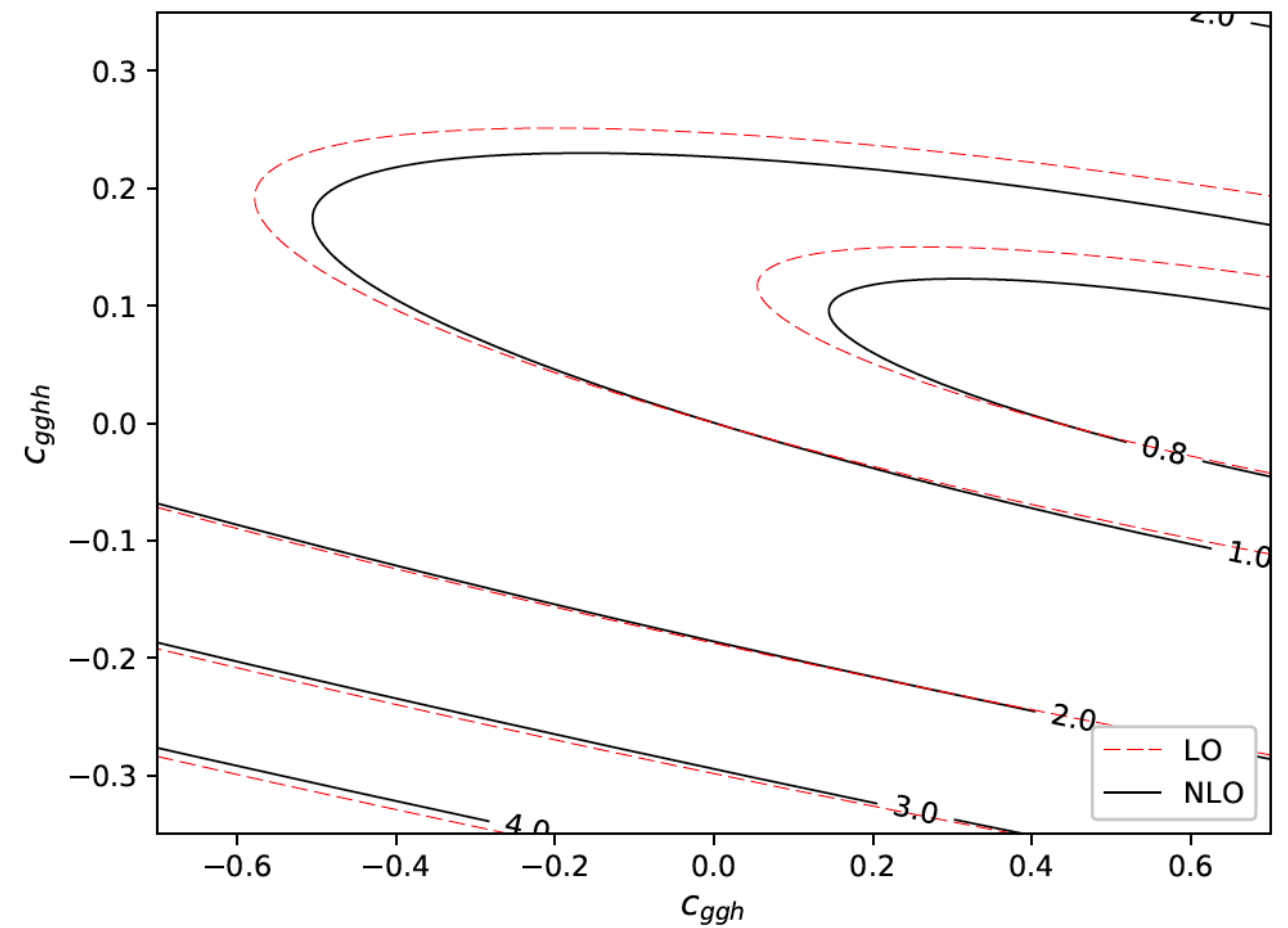
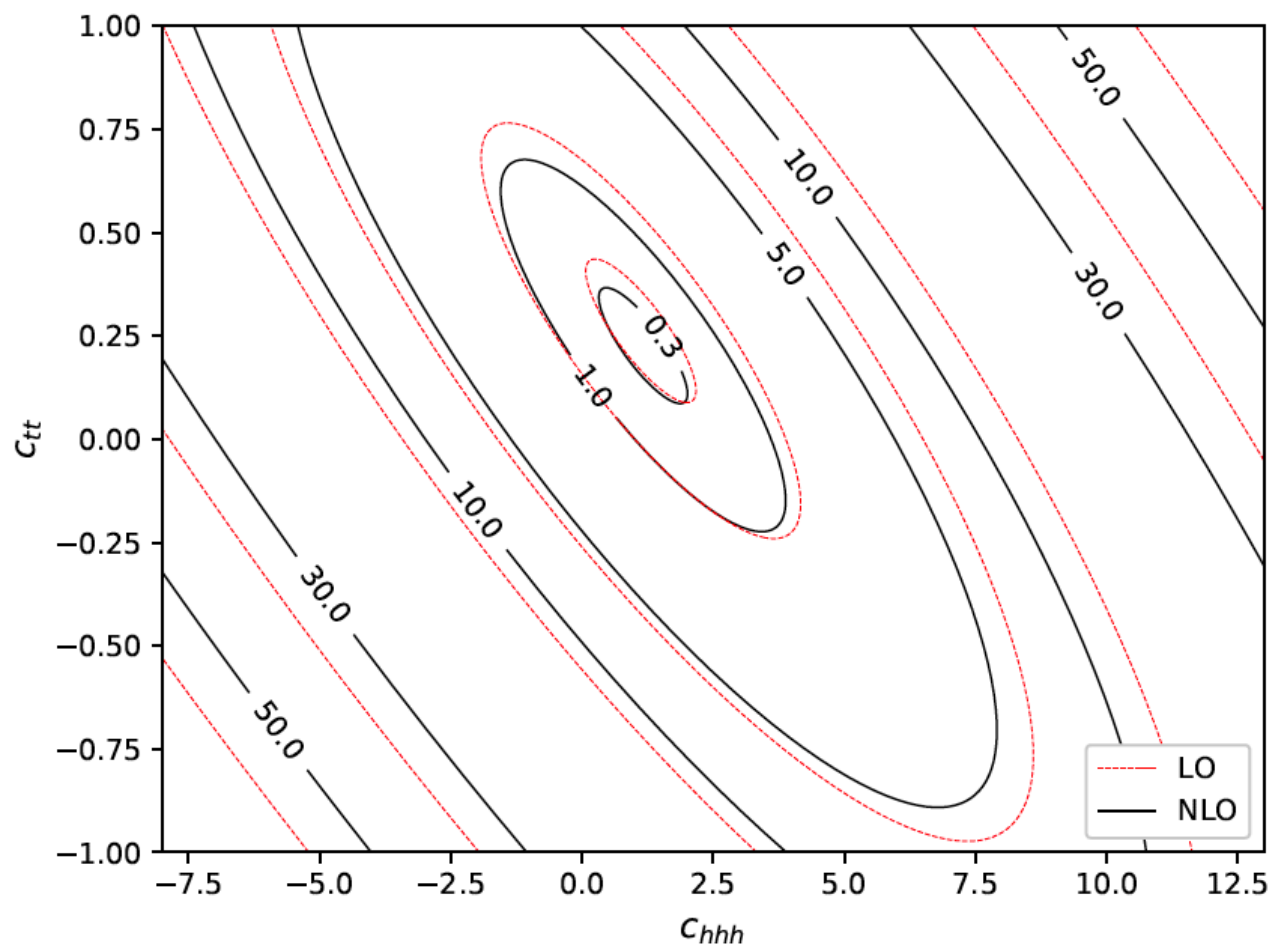
$$\begin{aligned} \frac{\sigma_{NLO}}{\sigma_{NLO,SM}} = & [A'_1 c_t^4 + A'_2 c_{tt}^2 + A'_3 c_{thh}^2 c_{hhh}^2 + A'_4 c_{ghh}^2 c_{hhh}^2 + A'_5 c_{gghh}^2 + A'_6 c_{tt} c_t^2 + A'_7 c_t^3 c_{hhh} \\ & + A'_8 c_{tt} c_t c_{hhh} + A'_9 c_{tt} c_{ggh} c_{hhh} + A'_{10} c_{tt} c_{cgghh} + A'_{11} c_t^2 c_{ggh} c_{hhh} + A'_{12} c_t^2 c_{gghh} \\ & + A'_{13} c_t c_{hhh}^2 c_{ggh} + A'_{14} c_t c_{hhh} c_{gghh} + A'_{15} c_{ggh} c_{hhh} c_{gghh} + \underline{A'_{16} c_t^3 c_{ggh} + A'_{17} c_t c_{tt} c_{ggh}} \\ & + \underline{A'_{18} c_t c_{ggh}^2 c_{hhh} + A'_{19} c_t c_{ggh} c_{gghh} + A'_{20} c_t^2 c_{ggh}^2 + A'_{21} c_{tt} c_{ggh}^2 + A'_{22} c_{ggh}^3 c_{hhh} + A'_{23} c_{ggh}^2 c_{gghh}}] \end{aligned}$$

# Cross section fit

A coeff	LO value	LO uncertainty	NLO value	NLO uncertainty
$A_1$	2.08059	0.00163127	2.23389	0.0100989
$A_2$	10.2011	0.00809032	12.4598	0.0424131
$A_3$	0.27814	0.00187658	0.342248	0.0153637
$A_4$	0.314043	0.000312416	0.346822	0.00327358
$A_5$	12.2731	0.0101351	13.0087	0.0962361
$A_6$	-8.49307	0.00885261	-9.6455	0.0503776
$A_7$	-1.35873	0.00148022	-1.57553	0.0136033
$A_8$	2.80251	0.0130855	3.43849	0.0771694
$A_9$	2.48018	0.0127927	2.86694	0.0772341
$A_{10}$	14.6908	0.0311171	16.6912	0.178501
$A_{11}$	-1.15916	0.00307598	-1.25293	0.0291153
$A_{12}$	-5.51183	0.0131254	-5.81216	0.134029
$A_{13}$	0.560503	0.00339209	0.649714	0.0287388
$A_{14}$	2.47982	0.0190299	2.85933	0.193023
$A_{15}$	2.89431	0.0157818	3.14475	0.148658
$A_{16}$			-0.00816241	0.000224985
$A_{17}$			0.0208652	0.000398929
$A_{18}$			0.0168157	0.00078306
$A_{19}$			0.0298576	0.000829474
$A_{20}$			-0.0270253	0.000701919
$A_{21}$			0.0726921	0.0012875
$A_{22}$			0.0145232	0.000703893
$A_{23}$			0.123291	0.00650551

- We present the results for the coefficients at LO and NLO.
- Using the fitted cross section we study the behavior of the cross section as a function of the BSM parameters.
- We show some of the iso-contours produced using the fit.

# NLO Iso-contours

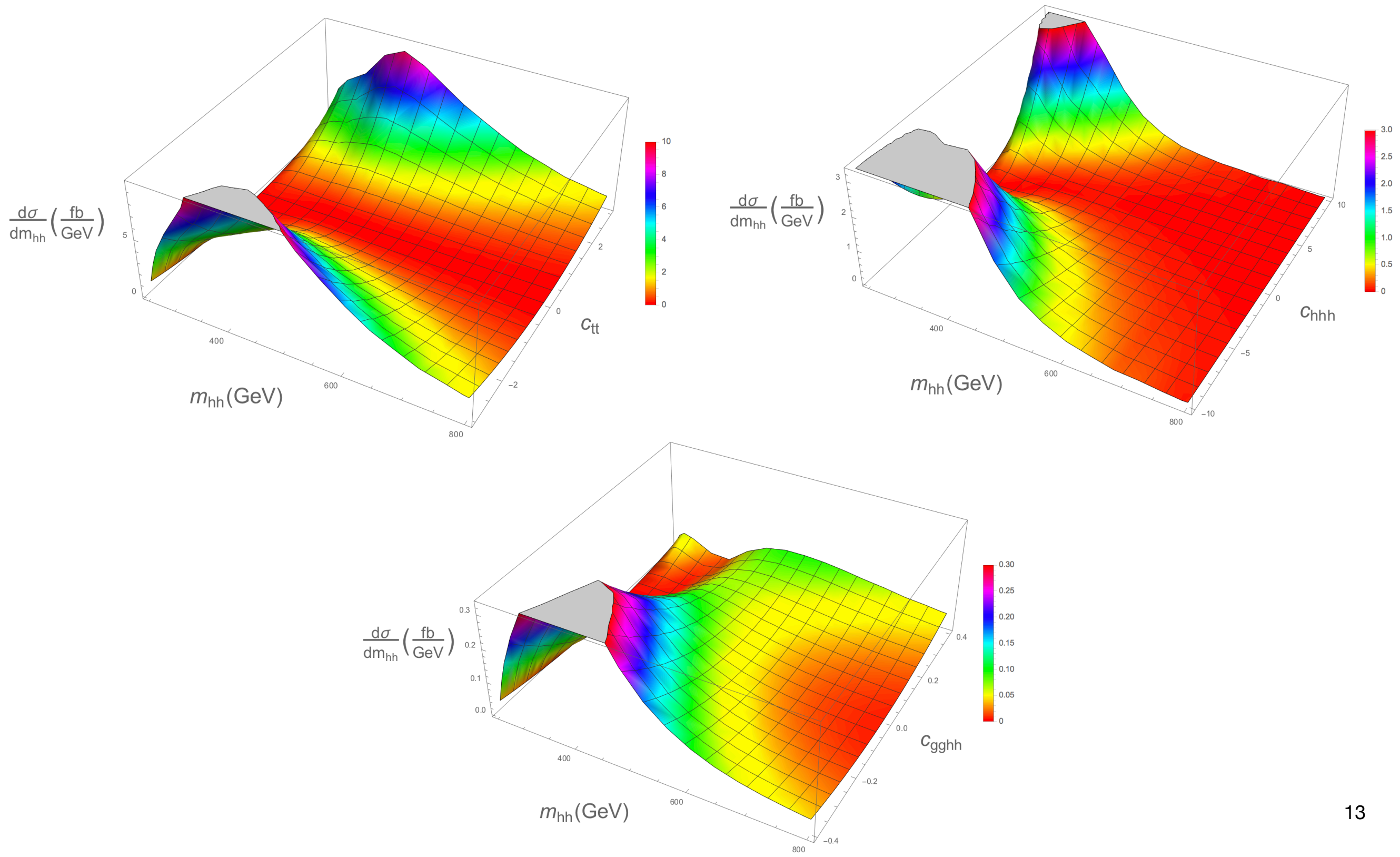


# NLO 3D plots

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- We performed the parametrization also at differential level, attached as ancillary files to 1806.05162.
- We used the differential fit to produce 3D plots.
- From the 3D plot one can understand the behavior of the differential distribution changing one of the BSM parameters.
- We made a study of the behavior of the differential  $m_{hh}$  cross section as a function of the 3 couplings which are difficult to constrain from other processes.
- In each plot we varied just one coupling in a range allowed by experimental constraints, fixing the others to the SM values.

# NLO 3D plots



# Conclusions

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- We computed NLO QCD corrections for Higgs boson pair production in the gluon fusion channel within the EWChL framework, working within a five dimensional parameter space.
- We evaluated the full top mass dependent cross sections and differential  $m_{hh}$  and  $p_T$  distributions for 12 benchmark points up to NLO QCD.
- The analysis shows that in a BSM framework the differential cross section can deviate substantially from the SM prediction or be almost degenerate; studying the differential cross section allows to break the degeneracy.
- We analyzed the total cross section as a function of the five anomalous couplings.
- We studied the behavior of the total and differential cross section as a function of the 3 parameters which are difficult to constrain from other processes.
- We gave a parameterization of the total and differential  $m_{hh}$  cross section (available as ancillary files) in terms of 23 coefficients which can allow experimentalists to make further analysis.



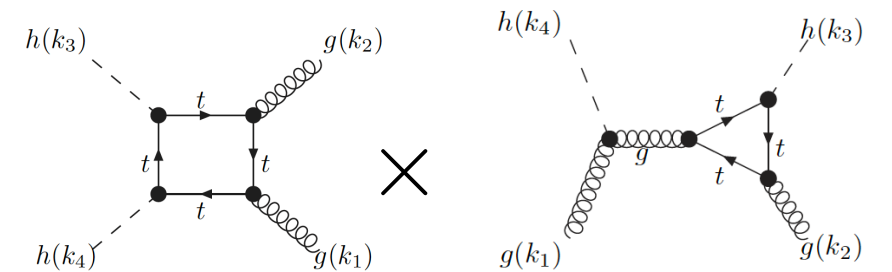


**BACKUP SLIDES**

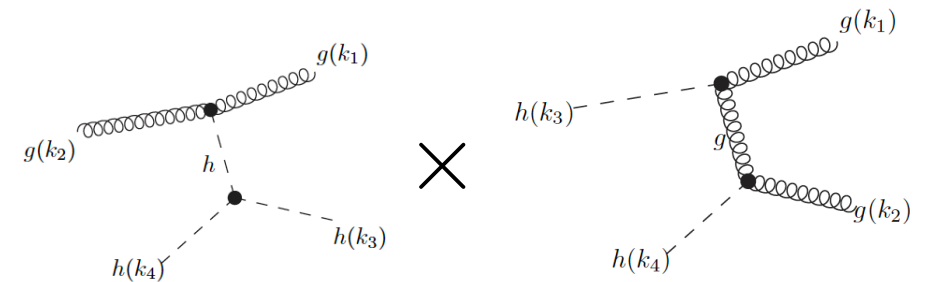
# Virtual contributions to NLO coefficients

- In order to evaluate the virtual coefficients of the parametrization formula we used a different approach.
- In our setup for the virtual corrections we can isolate the contribution of each diagram to the form factors.
- So we can compute each interference and determine directly all the 23 coefficients.

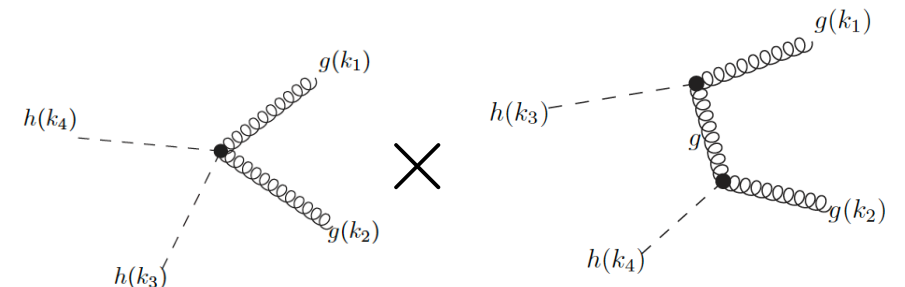
$$A_{16} \propto$$



$$A_{22} \propto$$



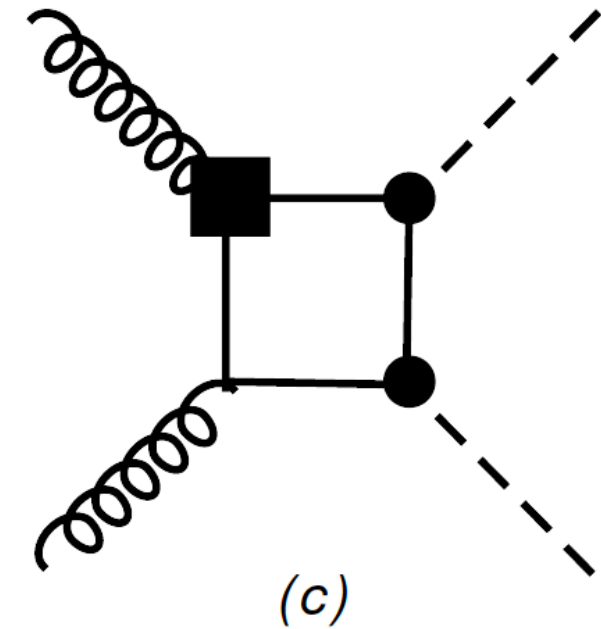
$$A_{23} \propto$$





# Chromo-magnetic operator

- Operator at least of chiral dimension 4 and loop order 1 and the diagram of loop order 2 but not of order  $g_s^4$ .
- Because of the change of chirality and the structure of the lagrangian there is likely one more weak coupling to the new physics sector.
- This would imply loop order 3 and so chiral dimension 6.



$$y_t g_s \bar{t}_L \sigma_{\mu\nu} G_{\mu\nu} t_R$$

$$\begin{aligned}
 \mathcal{L}_2 = & -\frac{1}{2}\langle G_{\mu\nu}G^{\mu\nu}\rangle - \frac{1}{2}\langle W_{\mu\nu}W^{\mu\nu}\rangle - \frac{1}{4}B_{\mu\nu}B^{\mu\nu} + \sum_{\psi=q_L,l_L,u_R,d_R,e_R} \bar{\psi}i\not{D}\psi \\
 & + \frac{v^2}{4} \langle D_\mu U^\dagger D^\mu U \rangle (1 + F_U(h)) + \frac{1}{2}\partial_\mu h \partial^\mu h - V(h) \\
 & - v \left[ \bar{q}_L \left( Y_u + \sum_{n=1}^{\infty} Y_u^{(n)} \left( \frac{h}{v} \right)^n \right) U P_+ q_R + \bar{q}_L \left( Y_d + \sum_{n=1}^{\infty} Y_d^{(n)} \left( \frac{h}{v} \right)^n \right) U P_- q_R \right. \\
 & \left. + \bar{l}_L \left( Y_e + \sum_{n=1}^{\infty} Y_e^{(n)} \left( \frac{h}{v} \right)^n \right) U P_- l_R + \text{h.c.} \right] .
 \end{aligned} \tag{2.1}$$