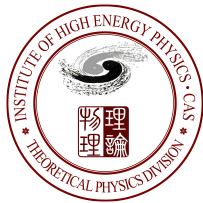


Standard Model Effective Field Theory for Top Quark Physics

Cen Zhang



Institute of High Energy Physics
Chinese Academy of Sciences



May 24, 2018
Desy Hamburg

Based on 1804.07773
(C. Degrande, F. Maltoni, K. Mimasu, E. Vryonidou, CZ),
and 1804.09766 (E. Vryonidou, CZ)

Outline

- 1 EFT interpretation of top measurements
- 2 Top EFT @ NLO QCD
 - Why we need NLO
 - Available processes and operators
 - Single top plus H/Z
 - Future plan
- 3 EW corrections
 - Higgs production & decay
- 4 Summary

Outline

1 EFT interpretation of top measurements

2 Top EFT @ NLO QCD

- Why we need NLO
- Available processes and operators
- Single top plus H/Z
- Future plan

3 EW corrections

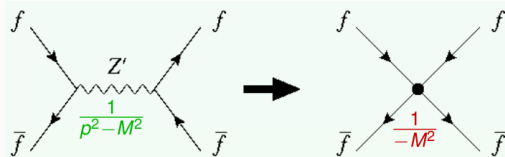
- Higgs production & decay

4 Summary

SMEFT

Starting with some BSM models

- Integrating out heavy states.
- Expanding the resulting non-standard interactions as a series of higher-dimensional operators.



$$\frac{1}{p^2 - M^2} = \frac{1}{-M^2} \left[1 + \left(\frac{p^2}{M^2} \right) + \left(\frac{p^2}{M^2} \right)^2 + \dots \right]$$

$$\mathcal{L}_{\text{Eff}} = \mathcal{L}_{\text{SM}} + \sum_i \frac{C_i^{(6)}}{\Lambda^2} \mathcal{O}_i^{(6)} + \sum_i \frac{C_i^{(8)}}{\Lambda^4} \mathcal{O}_i^{(8)} + \dots$$

SMEFT at dim-6

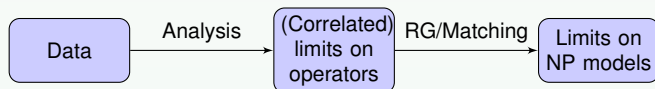
X^3		φ^6 and $\varphi^4 D^2$		$\psi^2 \varphi^3$	
Q_G	$f^{ABC} G_\mu^{A\nu} G_\nu^{B\rho} G_\rho^{C\mu}$	$Q_{\varphi\Box}$	$(\varphi^\dagger \varphi)^3$	$Q_{e\varphi}$	$(\varphi^\dagger \varphi)(\bar{l}_p e_r \varphi)$
$Q_{\tilde{G}}$	$f^{ABC} \tilde{G}_\mu^{A\nu} G_\nu^{B\rho} G_\rho^{C\mu}$	$Q_{\varphi\Box}$	$(\varphi^\dagger \varphi)\Box(\varphi^\dagger \varphi)$	$Q_{u\varphi}$	$(\varphi^\dagger \varphi)(\bar{q}_p u_r \tilde{\varphi})$
Q_W	$\varepsilon^{IJK} W_\mu^{I\nu} W_\nu^{J\rho} W_\rho^{K\mu}$	$Q_{\varphi D}$	$(\varphi^\dagger D^\mu \varphi)^* (\varphi^\dagger D_\mu \varphi)$	$Q_{d\varphi}$	$(\varphi^\dagger \varphi)(\bar{q}_p d_r \varphi)$
$Q_{\tilde{W}}$	$\varepsilon^{IJK} \tilde{W}_\mu^{I\nu} W_\nu^{J\rho} W_\rho^{K\mu}$				
$X^2 \varphi^2$		$\psi^2 X \varphi$		$\psi^2 \varphi^2 D$	
$Q_{\varphi G}$	$\varphi^\dagger \varphi G_{\mu\nu}^A G^{A\mu\nu}$	Q_{eW}	$(\bar{l}_p \sigma^{\mu\nu} e_r) \tau^I \varphi W_{\mu\nu}^I$	$Q_{\varphi l}^{(1)}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi)(\bar{l}_p \gamma^\mu l_r)$
$Q_{\varphi \tilde{G}}$	$\varphi^\dagger \varphi \tilde{G}_{\mu\nu}^A G^{A\mu\nu}$	Q_{eB}	$(\bar{l}_p \sigma^{\mu\nu} e_r) \varphi B_{\mu\nu}$	$Q_{\varphi l}^{(3)}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi)(\bar{l}_p \tau^I \gamma^\mu l_r)$
$Q_{\varphi W}$	$\varphi^\dagger \varphi W_{\mu\nu}^I W^{I\mu\nu}$	Q_{uG}	$(\bar{q}_p \sigma^{\mu\nu} T^A u_r) \tilde{\varphi} G_{\mu\nu}^A$	$Q_{\varphi c}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi)(\bar{e}_p \gamma^\mu e_r)$
$Q_{\varphi \tilde{W}}$	$\varphi^\dagger \varphi \tilde{W}_{\mu\nu}^I W^{I\mu\nu}$	Q_{uW}	$(\bar{q}_p \sigma^{\mu\nu} u_r) \tau^I \tilde{\varphi} W_{\mu\nu}^I$	$Q_{\varphi q}^{(1)}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi)(\bar{q}_p \gamma^\mu q_r)$
$Q_{\varphi B}$	$\varphi^\dagger \varphi B_{\mu\nu} B^{\mu\nu}$	Q_{uB}	$(\bar{q}_p \sigma^{\mu\nu} u_r) \tilde{\varphi} B_{\mu\nu}$	$Q_{\varphi q}^{(3)}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi)(\bar{q}_p \tau^I \gamma^\mu q_r)$
$Q_{\varphi \tilde{B}}$	$\varphi^\dagger \varphi \tilde{B}_{\mu\nu} B^{\mu\nu}$	Q_{dG}	$(\bar{q}_p \sigma^{\mu\nu} T^A d_r) \varphi G_{\mu\nu}^A$	$Q_{\varphi u}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi)(\bar{q}_p \gamma^\mu u_r)$
$Q_{\varphi WB}$	$\varphi^\dagger \tau^I \varphi W_{\mu\nu}^I B^{\mu\nu}$	Q_{dW}	$(\bar{q}_p \sigma^{\mu\nu} d_r) \tau^I \varphi W_{\mu\nu}^I$	$Q_{\varphi d}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi)(\bar{q}_p \gamma^\mu d_r)$
$Q_{\varphi \tilde{W}B}$	$\varphi^\dagger \tau^I \varphi \tilde{W}_{\mu\nu}^I B^{\mu\nu}$	Q_{dB}	$(\bar{q}_p \sigma^{\mu\nu} d_r) \varphi B_{\mu\nu}$	$Q_{\varphi ud}$	$i(\tilde{\varphi}^\dagger D_\mu \varphi)(\bar{u}_p \gamma^\mu d_r)$

$(LL)(LL)$		$(RR)(RR)$		$(LL)(RR)$	
Q_{ll}	$(\bar{l}_p \gamma_\mu l_r)(\bar{l}_s \gamma^\mu l_t)$	Q_{ee}	$(\bar{e}_p \gamma_\mu e_r)(\bar{e}_s \gamma^\mu e_t)$	Q_{le}	$(\bar{l}_p \gamma_\mu l_r)(\bar{e}_s \gamma^\mu e_t)$
$Q_{ll}^{(1)}$	$(\bar{q}_p \gamma_\mu q_r)(\bar{q}_s \gamma^\mu q_t)$	Q_{uu}	$(\bar{u}_p \gamma_\mu u_r)(\bar{u}_s \gamma^\mu u_t)$	Q_{lu}	$(\bar{l}_p \gamma_\mu l_r)(\bar{u}_s \gamma^\mu u_t)$
$Q_{ll}^{(3)}$	$(\bar{q}_p \gamma_\mu \tau^I q_r)(\bar{q}_s \gamma^\mu \tau^I q_t)$	Q_{dd}	$(\bar{d}_p \gamma_\mu d_r)(\bar{d}_s \gamma^\mu d_t)$	Q_{ld}	$(\bar{l}_p \gamma_\mu l_r)(\bar{d}_s \gamma^\mu d_t)$
$Q_{ll}^{(5)}$	$(\bar{l}_p \gamma_\mu \tau^I l_r)(\bar{q}_s \gamma^\mu q_t)$	Q_{eu}	$(e_p \gamma_\mu e_r)(\bar{u}_s \gamma^\mu u_t)$	Q_{eu}	$(\bar{q}_p \gamma_\mu q_r)(\bar{e}_s \gamma^\mu e_t)$
$Q_{ll}^{(5)}$	$(\bar{l}_p \gamma_\mu \tau^I l_r)(\bar{q}_s \gamma^\mu \tau^I q_t)$	Q_{ed}	$(e_p \gamma_\mu e_r)(\bar{d}_s \gamma^\mu d_t)$	$Q_{lu}^{(1)}$	$(\bar{q}_p \gamma_\mu q_r)(\bar{u}_s \gamma^\mu u_t)$
		$Q_{ud}^{(1)}$	$(u_p \gamma_\mu u_r)(\bar{d}_s \gamma^\mu d_t)$	$Q_{lu}^{(3)}$	$(\bar{q}_p \gamma_\mu \tau^I q_r)(\bar{u}_s \gamma^\mu \tau^I u_t)$
		$Q_{ud}^{(3)}$	$(u_p \gamma_\mu \tau^I u_r)(\bar{d}_s \gamma^\mu \tau^I d_t)$	$Q_{ld}^{(1)}$	$(\bar{q}_p \gamma_\mu q_r)(\bar{d}_s \gamma^\mu d_t)$
				$Q_{ld}^{(3)}$	$(\bar{q}_p \gamma_\mu \tau^I q_r)(\bar{d}_s \gamma^\mu \tau^I d_t)$
$(\bar{L}L)(\bar{R}L)$ and $(\bar{L}R)(\bar{L}R)$		B -violating			
Q_{leq}	$(\bar{l}_p^c e_r)(d_s q_t^c)$	Q_{duq}	$\varepsilon^{ab\gamma} \varepsilon_{jkl} [(d_p^{ab})^T C u_l^c] [(q_s^j)^T C l_t^k]$		
$Q_{leq}^{(1)}$	$(\bar{q}_p^c u_r) \varepsilon_{jkl} (q_s^k d_t^c)$	Q_{quq}	$\varepsilon^{ab\gamma} \varepsilon_{jkl} [(q_p^{ab})^T C q_l^c] [(u_s^j)^T C q_t^k]$		
$Q_{leq}^{(3)}$	$(\bar{q}_p^c T^A u_r) \varepsilon_{jkl} (q_s^k T^A d_t^c)$	$Q_{quq}^{(1)}$	$\varepsilon^{ab\gamma} \varepsilon_{jkl} [(q_p^{ab})^T C q_l^c] [(u_s^j)^T C q_t^k]$		
$Q_{leq}^{(1)}$	$(\bar{l}_p^c e_r) \varepsilon_{jkl} (q_s^k u_t^c)$	$Q_{quq}^{(3)}$	$\varepsilon^{ab\gamma} (\tau^I \varepsilon)_{jkl} (\tau^I \varepsilon)_{mn} [(q_p^{ab})^T C q_l^c] [(q_s^m)^T C q_t^k]$		
$Q_{leq}^{(3)}$	$(\bar{l}_p^c \sigma^{\mu\nu} e_r) \varepsilon_{jkl} (\bar{q}_s^k \sigma^{\mu\nu} u_t^c)$	Q_{duu}	$\varepsilon^{ab\gamma} [(d_p^{ab})^T C u_l^c] [(u_s^j)^T C e_t^k]$		

[B. Grzadkowski et al, '10]

Why useful?

- Efficiency: analysis done once and for all



- Precision: predictions can be systematically improved.
 - ▶ Renormalizability, Gauge symmetries, estimate of TH uncertainties. . .
 - ▶ NLO QCD already available in many cases. EW corrections are being studied and even automated.
- Global approach: capture the interplay between different sectors/measurements.
 - ▶ Higgs, top, EW, TGC, flavor, . . .

[A. Falkowski et al., '15]

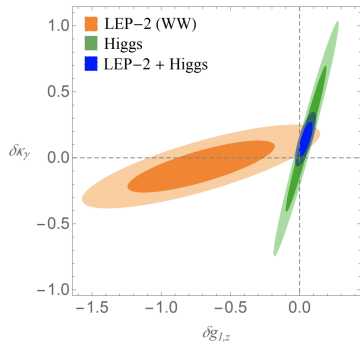


FIG. 1. Allowed 68% and 95% CL region in the $\delta g_{1,z}$ - $\delta \kappa_\gamma$ plane after considering LEP-2 WW production data (TGC), Higgs data, and the combination of both datasets.

First step taken by the TOPFITTER Collaboration [A. Buckley et al.'17]

Top-quark operators and how to look for them

$$O_{\varphi Q}^{(3)} = i\frac{1}{2}y_t^2 \left(\varphi^\dagger \overleftrightarrow{D}_\mu \varphi \right) (\bar{Q}\gamma^\mu \tau^I Q)$$

$$O_{\varphi Q}^{(1)} = i\frac{1}{2}y_t^2 \left(\varphi^\dagger \overleftrightarrow{D}_\mu \varphi \right) (\bar{Q}\gamma^\mu Q)$$

$$O_{\varphi t} = i\frac{1}{2}y_t^2 \left(\varphi^\dagger \overleftrightarrow{D}_\mu \varphi \right) (\bar{t}\gamma^\mu t)$$

$$O_{tW} = y_t g_w (\bar{Q}\sigma^{\mu\nu} \tau^I t) \tilde{\varphi} W_{\mu\nu}^I$$

$$O_{tB} = y_t g_Y (\bar{Q}\sigma^{\mu\nu} t) \tilde{\varphi} B_{\mu\nu}$$

$$O_{tG} = y_t g_s (\bar{Q}\sigma^{\mu\nu} T^A t) \tilde{\varphi} G_{\mu\nu}^A$$

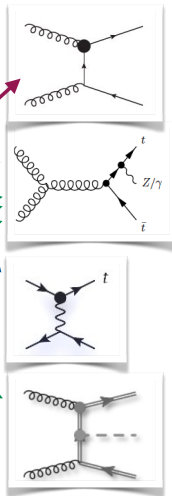
$$O_{t\phi} = y_t^3 \left(\phi^\dagger \phi \right) (\bar{Q}t) \tilde{\phi}$$

see for example: Aguilar-Saavedra (arXiv:0811.3842)

Zhang and Willenbrock (arXiv:1008.3869)

+four-fermion operators

+non-top operators (mixing)



Operators entering various processes: Global approach needed

In practice, we need a roadmap...

Interpreting top-quark LHC measurements in the standard-model effective field theory

J. A. Aguilar Saavedra,¹ C. Degrande,² G. Durieux,³
F. Maltoni,⁴ E. Vryonidou,² C. Zhang⁵ (editors),
D. Barducci,⁶ I. Brivio,⁷ V. Cirigliano,⁸ W. Dekens,^{8,9} J. de Vries,¹⁰ C. Englert,¹¹
M. Fabbri, ¹² C. Grojean,^{3,13} U. Haisch,^{2,14} Y. Jiang,⁷ J. Kamenik,^{15,16}
M. Mangano,² D. Marzocca,¹² E. Mereghetti,⁸ K. Mimasu,⁴ L. Moore,⁴ G. Perez,¹⁷
T. Plehn,¹⁸ F. Riva,² M. Russell,¹⁹ J. Santiago,¹⁹ M. Schulze,¹³ Y. Soreq,²⁰
A. Toneri,²¹ M. Trott,⁷ S. Westhoff,¹⁸ C. White,²² A. Wulzer,^{2,23,24} J. Zupan.²⁵

¹ Departamento de Física Teórica y del Cosmos, U. de Granada, E-18071 Granada, Spain

² CERN, Theoretical Physics Department, Geneva 23 CH-1211, Switzerland

³ DESY, Notkestraße 85, D-22607 Hamburg, Germany

⁴ Centre for Cosmology, Particle Physics and Phenomenology (CP3), Université catholique de Louvain, B-1348 Louvain-la-Neuve, Belgium

⁵ Institute of High Energy Physics, Chinese Academy of Sciences, Beijing 100049, China

⁶ SISSA and INFN, Sezione di Trieste, via Bonomea 265, 34136 Trieste, Italy

⁷ Niels Bohr International Academy and Discovery Center, Niels Bohr Institute, University of Copenhagen, DK-2100 Copenhagen, Denmark

⁸ Theoretical Division, Los Alamos National Laboratory, Los Alamos, NM 87545, USA

⁹ New Mexico Consortium, Los Alamos Research Park, Los Alamos, NM 87544, USA

¹⁰ Nikhef, Theory Group, Science Park 105, 1098 XG, Amsterdam, The Netherlands

¹¹ SUPA, School of Physics and Astronomy, University of Glasgow, Glasgow G12 8QQ, UK

¹² INFN, Sezione di Trieste, Via Valerio 2, 34127 Trieste, Italy

¹³ Institut für Physik, Humboldt-Universität zu Berlin, D-12489 Berlin, Germany

¹⁴ Rudolf Peierls Centre for Theoretical Physics, University of Oxford, OX1 3NP Oxford, UK

¹⁵ Jožef Stefan Institute, Jamova 39, 1000 Ljubljana, Slovenia

¹⁶ Faculty of Mathematics and Physics, University of Ljubljana, Jadranska 19, 1000 Ljubljana, Slovenia

¹⁷ Department of Particle Physics and Astrophysics, Weizmann Institute of Science, Rehovot 7610001, Israel

¹⁸ Institut für Theoretische Physik, Universität Heidelberg, Germany

¹⁹ CAFPE and Departamento de Física Teórica y del Cosmos, U. de Granada, E-18071 Granada, Spain

²⁰ Center for Theoretical Physics, Massachusetts Institute of Technology, Cambridge, MA 02139, USA

²¹ UNIFAL-MG, Rodovia José Aurélio Vilela 11999, 37715-400 Poços de Caldas, MG, Brazil

²² Centre for Research in String Theory, School of Physics and Astronomy, Queen Mary University of London, 327 Mile End Road, London E1 4NS, UK

²³ Institut de Théorie des Phénomènes Physiques, EPFL, Lausanne, Switzerland

²⁴ Dipartimento di Fisica e Astronomia, Università di Padova and INFN Padova, Italy

²⁵ Department of Physics, University of Cincinnati, Cincinnati, Ohio 45221, USA

[J. Aguilar Saavedra et al., '18]

Contents

- 1 Introduction
 - 2 Guiding principles
 - 3 Operator definitions
 - 4 Flavour assumptions
 - 5 Example of EFT analysis strategy
 - 6 Summary and outlook
- ### A Indicative constraints
- ### B UFO models
- ### C Flavour-, B - and L -conserving degrees of freedom
- ### D Less restrictive flavour symmetry
- ### E FCNC degrees of freedom

Interpreting top LHC measurements

- Reduce the number of OPs to start with (avoid 500+ 4-fermion OPs):

Baseline $U(2)_q \times U(2)_u \times U(2)_d$:

Forces the first two generation to appear as $\bar{q}q$, $\bar{u}u$, $\bar{d}d$.

Extended $U(2)_{q+d+u}$:

Allows right-handed $\bar{u}d$ and light chirality flipping ones $\bar{q}u$, $\bar{q}d$.

Restricted Top-philic:

All operators with SM bosons and (just) top. (and reduced to Warsaw basis)

Interpreting top LHC measurements

- Reduce the number of OPs to start with (avoid 500+ 4-fermion OPs):

Baseline $U(2)_q \times U(2)_u \times U(2)_d$:

Forces the first two generation to appear as $\bar{q}q$, $\bar{u}u$, $\bar{d}d$.

Extended $U(2)_{q+d+u}$:

Allows right-handed $\bar{u}d$ and light chirality flipping ones $\bar{q}u$, $\bar{q}d$.

Restricted Top-philic:

All operators with SM bosons and (just) top. (and reduced to Warsaw basis)

- Define the relevant degrees of freedom natural for top physics, and fix notations.

Top-specific d.o.f. definitions

Match SM interference structures
and interactions with physical gauge bosons

$$\bullet \begin{pmatrix} O_{\varphi q}^{1(33)} \\ O_{\varphi q}^{3(33)} \end{pmatrix} = \begin{pmatrix} (\varphi^\dagger \overleftrightarrow{D}_\mu \varphi)(\bar{q}_3 \gamma^\mu q_3) \\ (\varphi^\dagger \overleftrightarrow{D}'_\mu \varphi)(\bar{q}_3 \gamma^\mu \tau^I q_3) \end{pmatrix} = \begin{pmatrix} -1 & 1 \\ 1 & 1 \\ 0 & 1 \\ 0 & 1 \end{pmatrix}^T \begin{pmatrix} \frac{+e}{2s_W c_W} (\bar{t} \gamma^\mu P_L t) Z_\mu (\nu + h)^2 \\ \frac{-e}{2s_W c_W} (\bar{b} \gamma^\mu P_L b) Z_\mu (\nu + h)^2 \\ \frac{g}{\sqrt{2}} (\bar{t} \gamma^\mu P_L b) W_\mu^+ (\nu + h)^2 \\ \frac{g}{\sqrt{2}} (\bar{b} \gamma^\mu P_L t) W_\mu^- (\nu + h)^2 \end{pmatrix}$$

$$c_{\varphi Q}^- \equiv C_{\varphi q}^{1(33)} - C_{\varphi q}^{3(33)} \quad \text{enters in } pp \rightarrow t\bar{t}Z$$

$$c_{\varphi Q}^3 \equiv C_{\varphi q}^{3(33)} \quad \text{enters in } t \rightarrow bW^+$$

$$c_{\varphi Q}^+ \equiv C_{\varphi q}^{1(33)} + C_{\varphi q}^{3(33)} \quad \text{enters in } e^+e^- \rightarrow b\bar{b} \text{ (or } pp \rightarrow b\bar{b}Z)$$

$$\bullet \begin{pmatrix} O_{qq}^{1(ii33)} \\ O_{qq}^{1(i33i)} \\ O_{qq}^{3(ii33)} \\ O_{qq}^{3(i33i)} \end{pmatrix} = \begin{pmatrix} 1 & 1/6 & 0 & 1/2 \\ 0 & 1/6 & 1 & -1/6 \\ 0 & 1 & 0 & 3 \\ 0 & 1 & 0 & -1 \end{pmatrix}^T \begin{pmatrix} (\bar{q}_i \gamma^\mu q_i) (\bar{Q} \gamma_\mu Q) \\ (\bar{q}_i \gamma^\mu \tau^I q_i) (\bar{Q} \gamma_\mu \tau^I Q) \\ (\bar{q}_i \gamma^\mu T^A q_i) (\bar{Q} \gamma_\mu T^A Q) \\ (\bar{q}_i \gamma^\mu \tau^I T^A q_i) (\bar{Q} \gamma_\mu \tau^I T^A Q) \end{pmatrix}$$

$$c_{Qq}^{1,1} \equiv C_{qq}^{1(ii33)} + \frac{1}{6} C_{qq}^{1(i33i)} + \frac{1}{2} C_{qq}^{3(ii33)} \quad \text{interferes with EW NC}$$

$$c_{Qq}^{3,1} \equiv C_{qq}^{3(ii33)} + \frac{1}{6} (C_{qq}^{1(i33i)} - C_{qq}^{3(i33i)}) \quad \text{interferes with EW CC}$$

$$c_{Qq}^{1,8} \equiv C_{qq}^{1(i33i)} + 3 C_{qq}^{3(i33i)}, \quad \text{interferes with QCD}$$

$$c_{Qq}^{3,8} \equiv C_{qq}^{1(i33i)} - C_{qq}^{3(i33i)} \quad \text{doesn't interfere with EW CC}$$

Interpreting top LHC measurements

- Reduce the number of OPs to start with (avoid 500+ 4-fermion OPs):

Baseline $U(2)_q \times U(2)_u \times U(2)_d$:

Forces the first two generation to appear as $\bar{q}q$, $\bar{u}u$, $\bar{d}d$.

Extended $U(2)_{q+d+u}$:

Allows right-handed $\bar{u}d$ and light chirality flipping ones $\bar{q}u$, $\bar{q}d$.

Restricted Top-philic:

All operators with SM bosons and (just) top. (and reduced to Warsaw basis)

- Define the relevant degrees of freedom natural for top physics, and fix notations.
- Provide simulation tools and benchmarks: DIM6TOP

<https://feynrules.irmp.ucl.ac.be/wiki/dim6top>

Interpreting top LHC measurements

- Reduce the number of OPs to start with (avoid 500+ 4-fermion OPs):

Baseline $U(2)_q \times U(2)_u \times U(2)_d$:

Forces the first two generation to appear as $\bar{q}q$, $\bar{u}u$, $\bar{d}d$.

Extended $U(2)_{q+d+u}$:

Allows right-handed $\bar{u}d$ and light chirality flipping ones $\bar{q}u$, $\bar{q}d$.

Restricted Top-philic:

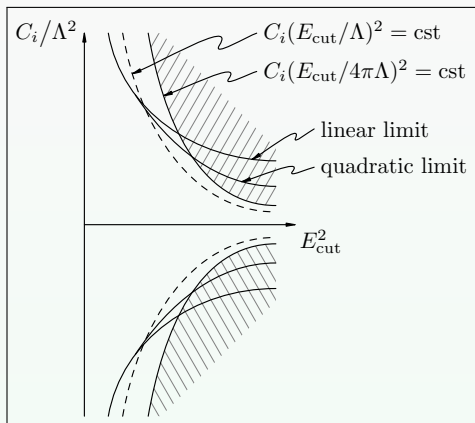
All operators with SM bosons and (just) top. (and reduced to Warsaw basis)

- Define the relevant degrees of freedom natural for top physics, and fix notations.

- Provide simulation tools and benchmarks: DIM6TOP

<https://feynrules.irmp.ucl.ac.be/wiki/dim6top>

- Strategy.



- Quote limits as a function of E_{cut} [Contino,Falkowski,Goertz,Grojean,Riva,'16]
 - ▶ Assess the validity of matching to models.
 - ▶ Compare with perturbativity.

Outline

1 EFT interpretation of top measurements

2 Top EFT @ NLO QCD

- Why we need NLO
- Available processes and operators
- Single top plus H/Z
- Future plan

3 EW corrections

- Higgs production & decay

4 Summary

Outline

1 EFT interpretation of top measurements

2 Top EFT @ NLO QCD

- Why we need NLO
- Available processes and operators
- Single top plus H/Z
- Future plan

3 EW corrections

- Higgs production & decay

4 Summary

Why we need NLO

- SMEFT is renormalizable order by order in $1/\Lambda$.
- We need higher-order corrections to control TH uncertainties for two classes of reasons:
 - ▶ Same as for SM: QCD corrections are important at hadron colliders; EW corrections are important for accuracy and for specific areas of phase space and observables; NLO corrections affect normalization, shapes, scale and PDF uncertainties.
 - ▶ Specific issues for SMEFT at $\text{dim}>4$: NLO could be the first order where non-trivial EFT structure becomes manifest: mixing, μ_{EFT} dependence, new contributions arise at NLO,...

Running & Mixing

- Scale separation: coefficients are matched to BSM at scale Λ , but are probed at much lower scales.
- Coefficients are defined with $\overline{\text{MS}}$ scheme to take care of the logs.
- This means coefficients depend on the scale at which they are defined.
- RG mixing

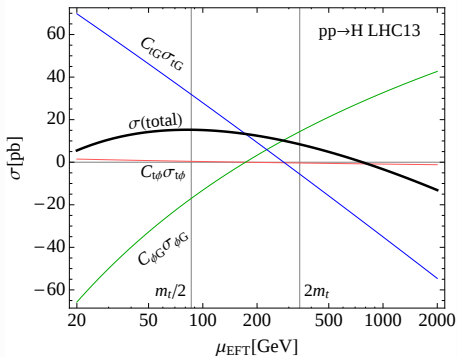
[R. Alonso et al., '13,'14]

$$\frac{dC_i(\mu)}{d\log\mu} = \frac{\alpha}{\pi} \gamma_{ij} C_j(\mu)$$

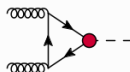
- One immediate consequence is that assumptions about some coefficients being zero at low scales are not valid.

EFT scale dependence

$gg \rightarrow H$ scale dependence

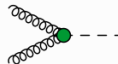


Op and diagrams



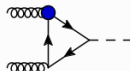
(NLO)

$$O_{t\phi} = y_t^3 (\varphi^\dagger \varphi) (\bar{Q}t)\tilde{\varphi}$$



(LO)

$$O_{\phi G} = y_t^2 (\varphi^\dagger \varphi) G_{\mu\nu}^A G^{A\mu\nu}$$



(NLO)

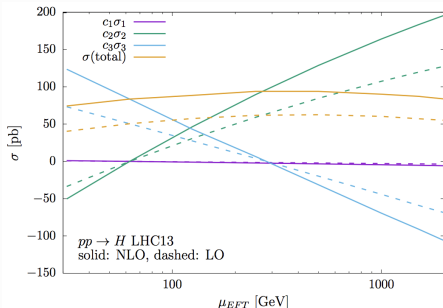
$$O_{tG} = y_t g_s (\bar{Q}\sigma^{\mu\nu} T^A t) \tilde{\varphi} G_{\mu\nu}^A$$

[Vryonidou, Maltoni, **CZ**, '16]
 $\Leftarrow C_{tG} = 1, C_{t\phi} = C_{\phi G} = 0 \text{ at } m_t.$

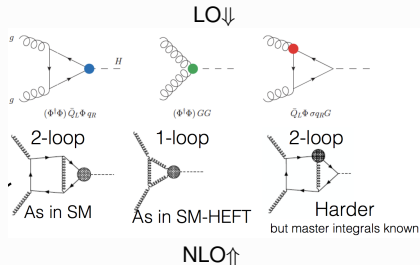
- Scale dependence of (LO) $O_{\phi G}$, from running coef., cancels that of (NLO) O_{tG} , from the loop.
- Only global point of view could make sense. To estimate TH uncertainty, must sum all ops.

EFT scale dependence: even higher order

$gg \rightarrow H$ scale dependence



Op and diagrams



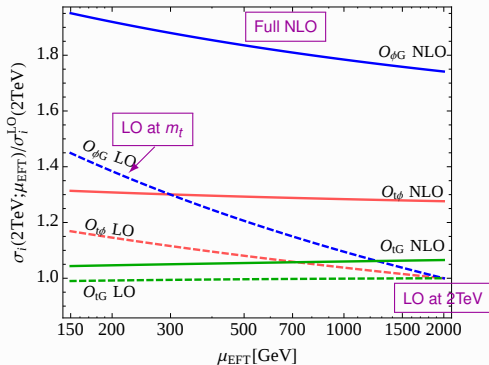
[Deutschmann, Duhr, Maltoni, Vryonidou, '17]

- Once global, SMEFT prediction can be improved order by order.

Genuine NLO corrections can be large

- RG structure of SMEFT is process and observable-independent, but does not fully encode the NLO corrections.
 - ▶ In fact, they are NOT part of NLO correction from a bottom-up point of view.
- In contrast, the finite terms depend on processes and observables. **Need to be studied on a process-by-process basis.**
- Often, they are the **dominant** effects.

$t\bar{t}H$: RG vs full NLO



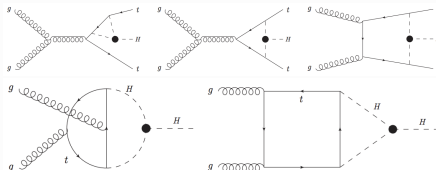
- Suppose a full theory is matched to an EFT with $O_{t\phi}$, $O_{\phi G}$, O_{tG} at 2 TeV.
- We can compute σ at LO $\mu = 2$ TeV, where we normalize results to 1.
- We can also improve these results by running the theory to m_t , and do another LO calculation. This increases σ by 0 ~ 50% depending on operators.
- However the full NLO corrections are much larger.

[Vryonidou, Maltoni, **CZ**, '16]

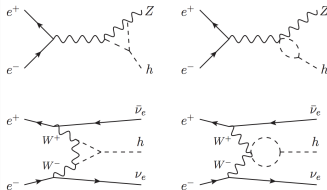
- Finite (QCD) corrections can be very important.
 - ▶ Similar cases in H and Z decay, see e.g. [R. Gauld, '16], [C. Hartmann, '16]
- Not to say RGEs are useless, but relying on them could be misleading.

New operators arise at NLO

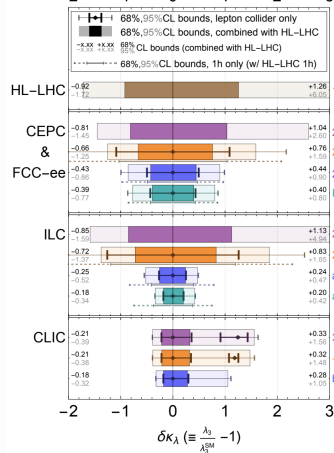
κ_λ at LHC [G. Degraassi et al., '16] [Gorbahn&Haisch, '16]



κ_λ at e^+e^- [M. McCullough, '13] [S. D. Vita et al., '17]

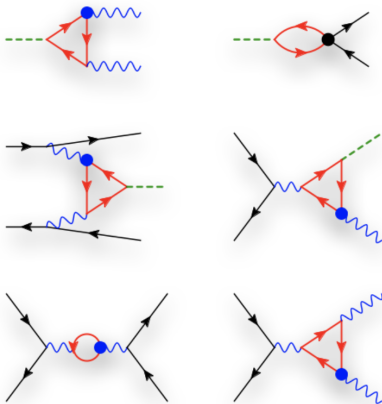


bounds on $\delta\kappa_\lambda$ from EFT global fit



New operators arise at NLO

Top loops in Higgs processes



[E. Vryonidou and CZ, '18]

Potentially large effects:

$$\frac{\sigma_{loop}}{\sigma_{tree}} \sim \alpha_{EW} \frac{C_{top}}{C_{Higgs}}$$

given that top operator constraints are in general much weaker.

One last reason for going to NLO...

If it's "free".

```
MG5_aMC>import model TopEFT
MG5_aMC>generate p p > t t~ EFT=1 [QCD]
MG5_aMC>output
MG5_aMC>launch
```

(imagine this is all you need to get (NLO+PS) events...)

Outline

1 EFT interpretation of top measurements

2 Top EFT @ NLO QCD

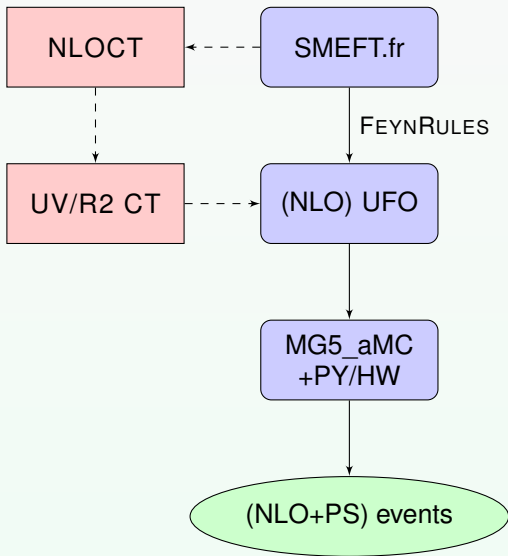
- Why we need NLO
- Available processes and operators
- Single top plus H/Z
- Future plan

3 EW corrections

- Higgs production & decay

4 Summary

Workflow (ideally) NLO



[C. Degrande,'14]

Strategy

- Instead of having the full SMEFT@NLO automation, we start with important processes, one by one, to make sure nothing goes wrong.
- This also allows us to identify the potential complication due to going to higher-dim, which is crucial for the final automation of the full theory.

Status for top processes

	ttg	ttZ/ γ , tbW					ttH	qqtt	ggH
Process	O_{tG}	O_{tB}	O_{tW}	$O_{\varphi Q}^{(3)}$	$O_{\varphi Q}^{(1)}$	$O_{\varphi t}$	$O_{t\varphi}$	O_{4f}	$O_{\varphi G}$
$t \rightarrow bW \rightarrow bl^+\nu$	✓		✓	✓					✓
$pp \rightarrow t\bar{q}$	✓		✓	✓					✓
$pp \rightarrow tW$	✓		✓	✓					
$pp \rightarrow t\bar{t}$	✓								✓
$pp \rightarrow t\bar{t}\gamma$	✓	✓	✓						✓
$pp \rightarrow t\gamma j$	✓	✓	✓	✓					✓
$pp \rightarrow t\bar{t}Z$	✓	✓	✓	✓	✓	✓			✓
$pp \rightarrow tZj$	✓	✓	✓	✓	✓	✓			✓
$pp \rightarrow t\bar{t}W$	✓								✓
$e^+e^- \rightarrow t\bar{t}$	✓	✓	✓	✓	✓	✓			✓
$pp \rightarrow t\bar{t}H$	✓						✓	✓	✓
$pp \rightarrow tHj$	✓		✓	✓			✓	✓	✓
$gg \rightarrow H, H_j, HZ$	✓			✓	✓	✓	✓		✓

Coupling measurements

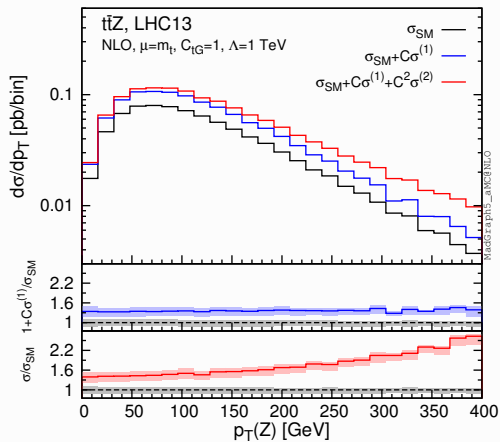
	tqZ/ γ					tqg	tqH	lltq
Process	$O_{\phi q}^{(3)}$	$O_{\phi q}^{(1)}$	$O_{\phi u}^{(1)}$	O_{uW}	O_{uB}	O_{uG}	$O_{u\phi}$	O_{4f}
$t \rightarrow ql^+l^-$	✓	✓	✓	✓	✓	✓		✓
$t \rightarrow q\gamma$				✓	✓	✓		
$t \rightarrow qH$						✓		✓
$pp \rightarrow t$						✓		
$pp \rightarrow t\bar{t}l^+l^-$	✓	✓	✓	✓	✓	✓		(✓)
$pp \rightarrow t\gamma$				✓	✓	✓		
$pp \rightarrow tH$						✓		✓

FCNC searches

*color-neutral operators are free.

```
shell> ./bin/mg5
MG5_aMC> import model TopEFT
MG5_aMC> generate p p > t t~ Z EFT=1 [QCD]
MG5_aMC> output some_DIR
MG5_aMC> launch
```

◀ ◻ ▶ ◀ ◻ ▶ ◀ ≡ ▶ ◀ ≡ ▶ ≡ ↺ 🔍 ↻



For more details, see...

Processes	Operators	Refs
FCNC production	tqX , $X = g, \gamma, Z, h$	[Degrande,Maltoni,Wang,CZ,'14]
$t\bar{t}$	chromo-dipole	[D.B.Franzosi,CZ,'15]
single t (s-&t-channel+tW)	tbW couplings	[CZ,'16]
$t\bar{t}Z, t\bar{t}\gamma, (gg \rightarrow HZ)$	$t\bar{t}X$, $X = Z, \gamma, g$	[O.B.Bylund et al,'16]
$t\bar{t}H$	chromo, ggH , top Yukawa	[Vryonidou,Maltoni,CZ,'16]
$e^+e^- \rightarrow t\bar{t}$	$t\bar{t}X$, 4-fermion	[G. Durieux,'17]
(Higgs production)	EW/Higgs	[C. Degrande et al.,'16]
$tHj, tZj, (t\gamma j)$	all above plus EW and Higgs plus 4-fermion	[C.Degrande et al.,'18]

Outline

1 EFT interpretation of top measurements

2 Top EFT @ NLO QCD

- Why we need NLO
- Available processes and operators
- **Single top plus H/Z**
- Future plan

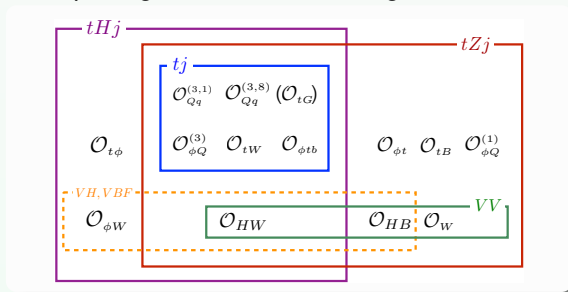
3 EW corrections

- Higgs production & decay

4 Summary

Single top with H/Z

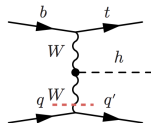
- Involve top, W/Z , H .
 - ▶ Nice test for putting all available stuff together.



- Unitarity cancellations: announced sensitivity at high mass.

Single top with H/Z

tHj ($tZj = h \rightarrow Z$)

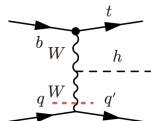


$$\mathcal{O}_{\varphi W} : \varphi^\dagger \varphi W_i^{\mu\nu} W_{\mu\nu}^i$$

HWW

TGC

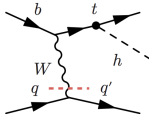
$$\mathcal{O}_W : \epsilon^{ijk} W_{i,\mu\nu} W_j^{\nu\rho} W_{k,\rho}^\mu$$



$$\mathcal{O}_{\varphi Q}^{(3)} : i(\varphi^\dagger \overleftrightarrow{D}_\mu^i \varphi)(\bar{Q} \gamma^\mu \sigma_i Q)$$

Wtb vertex

$$\mathcal{O}_{\varphi tb} : i(\bar{\varphi} D_\mu \varphi)(\bar{b} \gamma^\mu t)$$

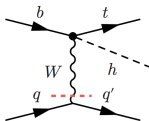


$$\mathcal{O}_{t\varphi} : (\varphi^\dagger \varphi)(\bar{Q} t) \tilde{\varphi}$$

top Yukawa

ttZ coupling

$$\mathcal{O}_{\varphi t} : i(\varphi^\dagger \overleftrightarrow{D}_\mu \varphi)(\bar{t} \gamma^\mu t)$$



$$\mathcal{O}_{\varphi Q}^{(3)} : i(\varphi^\dagger \overleftrightarrow{D}_\mu^i \varphi)(\bar{Q} \gamma^\mu \sigma_i Q)$$

Contact terms

$$\mathcal{O}_{tB} : (\bar{Q} \sigma_{\mu\nu} t) \tilde{\varphi} B^{\mu\nu}$$

- The tXj channels access the $2 \rightarrow 2$ sub-amplitudes, probe the energy dependence due to unitarity cancellation spoiled by BSM effects, and reveal the rich interplay between EFT operators from different sectors.
- See also [\[Maltoni,Paul,Stelzer,Willenbrock,'01\]](#), [\[Biswas,Gabrielli,Mele,12\]](#), [\[Farina,Grojean,Maltoni,Salvioni,Thamm,'12\]](#), [\[Demartin,Maltoni,Mawatari,Zaro,'15\]](#), [\[Dror,Farina,Salvioni,Serra,'16\]](#).

Single top with H/Z : sub-amplitudes

$bW \rightarrow tH$ amplitude

$\lambda_b, \lambda_W, \lambda_t$	SM	$\mathcal{O}_{t\phi}$	$\mathcal{O}_{\phi Q}^{(3)}$	$\mathcal{O}_{\phi W}$	$\mathcal{O}_{tW}$	$\mathcal{O}_{HW}$
$-, 0, -$	s^0	s^0	$\sqrt{s(s+t)}$	s^0	s^0	$\sqrt{s(s+t)}$
$-, 0, +$	$\frac{1}{\sqrt{s}}$	$m_t \sqrt{-t}$	$m_t \sqrt{-t}$	$\frac{1}{\sqrt{s}}$	$\frac{m_W s}{\sqrt{-t}}$	$\frac{1}{\sqrt{s}}$
$-, -, -$	$\frac{1}{\sqrt{s}}$	$\frac{1}{\sqrt{s}}$	$m_W \sqrt{-t}$	$\frac{m_W s}{\sqrt{-t}}$	$m_t \sqrt{-t}$	$\frac{m_W(s+t)}{\sqrt{-t}}$
$-, -, +$	$\frac{1}{s}$	s^0	s^0	$-$	$\sqrt{s(s+t)}$	$\frac{1}{s}$
$-, +, -$	$\frac{1}{\sqrt{s}}$	$-$	$\frac{1}{\sqrt{s}}$	$\frac{m_W(s+t)}{\sqrt{-t}}$	$\frac{1}{\sqrt{s}}$	$\frac{m_W(s+t)}{\sqrt{-t}}$
$-, +, +$	s^0	$-$	s^0	s^0	s^0	$\frac{1}{s}$

$\mathcal{O}_{\phi tb}, \lambda_b = +$

$\lambda_W \backslash \lambda_t$	0	+	-
+	$\sqrt{s(s+t)}$	$m_W \sqrt{-t}$	$\frac{1}{\sqrt{s}}$
-	$m_t \sqrt{-t}$	s^0	s^0

$$s \sim -t \gg v^2$$

$bW \rightarrow tZ$ amplitude

$\lambda_b, \lambda_W, \lambda_t, \lambda_Z$	SM	$\mathcal{O}_{\phi Q}^{(3)}$	$\mathcal{O}_{\phi Q}^{(1)}$	$\mathcal{O}_{\phi t}$	$\mathcal{O}_{tB}$	$\mathcal{O}_{tW}$	$\mathcal{O}_W$	$\mathcal{O}_{HW}$	$\mathcal{O}_{HB}$
$-, 0, -, 0$	s^0	$\sqrt{s(s+t)}$	$-$	$-$	$-$	s^0	s^0	$\sqrt{s(s+t)}$	s^0
$-, 0, +, 0$	$\frac{1}{\sqrt{s}}$	$m_t \sqrt{-t}$	$m_t \sqrt{-t}$	$m_t \sqrt{-t}$	$m_Z \sqrt{-t}$	$\frac{m_W(2s+3t)}{\sqrt{-t}}$	$-$	$m_t \sqrt{-t}$	$m_t \sqrt{-t}$
$-, -, -, 0$	$\frac{1}{\sqrt{s}}$	$m_W \sqrt{-t}$	$-$	$-$	$-$	$-$	$\frac{m_W(s+2t)}{\sqrt{-t}}$	$m_W \sqrt{-t}$	$\frac{1}{\sqrt{s}}$
$-, -, +, 0$	$\frac{1}{s}$	s^0	s^0	s^0	s^0	$\sqrt{s(s+t)}$	s^0	s^0	$\frac{1}{\sqrt{s}}$
$-, 0, -, -$	$\frac{1}{\sqrt{s}}$	$m_W \sqrt{-t}$	$-$	$-$	$m_t \sqrt{-t}$	$m_t \sqrt{-t}$	$\frac{m_W(s+2t)}{\sqrt{-t}}$	$\frac{m_W(ss_W^2+2t)}{\sqrt{-t}}$	$\frac{m_W s}{\sqrt{-t}}$
$-, 0, -, +$	$\frac{1}{\sqrt{s}}$	$-$	$-$	$-$	$-$	$-$	$\frac{m_W(s+t)}{\sqrt{-t}}$	$\frac{m_W(s+t)}{\sqrt{-t}}$	$\frac{m_W(s+t)}{\sqrt{-t}}$
$-, 0, +, -$	s^0	s^0	s^0	$-$	$-$	s^0	s^0	s^0	s^0
$-, 0, +, +$	$\frac{1}{s}$	s^0	s^0	s^0	$\sqrt{s(s+t)}$	$\sqrt{s(s+t)}$	$-$	s^0	s^0
$-, +, -, 0$	$\frac{1}{\sqrt{s}}$	$-$	$-$	$-$	$-$	$-$	$\frac{m_W(s+t)}{\sqrt{-t}}$	$\frac{1}{\sqrt{s}}$	$\frac{1}{\sqrt{s}}$
$-, +, +, 0$	s^0	s^0	$-$	$-$	$-$	s^0	$-$	s^0	$\frac{1}{s}$
$-, -, -, -$	s^0	s^0	$-$	$-$	s^0	s^0	s^0	s^0	s^0
$-, -, -, +$	$\frac{1}{s}$	$-$	$-$	$-$	$-$	$-$	$\sqrt{s(s+t)}$	s^0	s^0
$-, -, +, -$	$\frac{1}{\sqrt{s}}$	$-$	$-$	$-$	$-$	$\frac{m_Z(s_W^2 t - 3c_W^2(2s+t))}{\sqrt{-t}}$	$-$	$\frac{1}{\sqrt{s}}$	$\frac{1}{\sqrt{s}}$
$-, -, +, +$	$-$	$-$	$-$	$-$	$m_W \sqrt{-t}$	$m_Z \sqrt{-t}$	$m_t \sqrt{-t}$	$m_t \sqrt{-t}$	$m_t \sqrt{-t}$
$-, +, -, -$	$\frac{1}{s}$	s^0	s^0	$-$	$-$	$-$	$\sqrt{s(s+t)}$	s^0	s^0
$-, +, -, +$	$\frac{1}{s}$	s^0	s^0	$-$	$-$	$-$	$-$	s^0	s^0
$-, +, +, -$	$\frac{1}{\sqrt{s}}$	$-$	$-$	$-$	$-$	$-$	$m_t \sqrt{-t}$	$m_t \sqrt{-t}$	$m_t \sqrt{-t}$
$-, +, +, +$	$\frac{1}{\sqrt{s}}$	$-$	$-$	$-$	$-$	$\frac{m_W(s+t)}{\sqrt{-t}}$	$-$	$\frac{1}{\sqrt{s}}$	$\frac{1}{\sqrt{s}}$

 $\mathcal{O}_{\phi tb}, \lambda_b, \lambda_t = +, +$

$\lambda_W \backslash \lambda_Z$	0	+	-
0	$\sqrt{s(s+t)}$	$m_W \sqrt{-t}$	$-$
+	$m_Z \sqrt{-t}$	s^0	$-$
-	$-$	$-$	s^0

 $\mathcal{O}_{\phi tb}, \lambda_b, \lambda_t = +, -$

$\lambda_W \backslash \lambda_Z$	0	+	-
0	$-$	$-$	s^0
+	s^0	$-$	$-$
-	s^0	$-$	$-$

Inclusive results: $tHj@13$ TeV

- Parameterization:

$$\sigma = \sigma_{SM} + \sum_i \frac{1\text{TeV}^2}{\Lambda^2} C_i \sigma_i + \sum_{i \leq j} \frac{1\text{TeV}^4}{\Lambda^4} C_i C_j \sigma_{ij}.$$

- Large deviation $\gtrsim 1$ within current constraints (O_{tW} and $O_{t\varphi}$).
- K -factor not universal.
- Reduction of scale/PDF uncertainties.

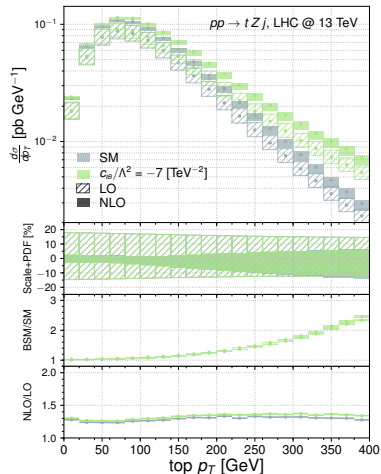
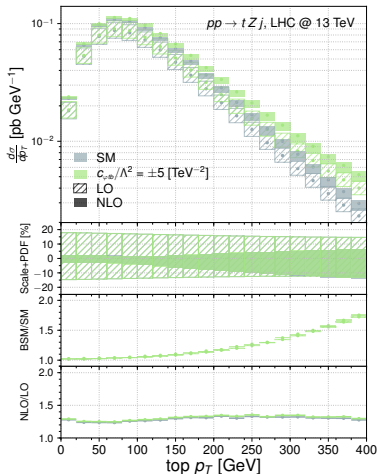
σ [fb]	LO	NLO	K-factor
σ_{SM}	57.56(4) $^{+11.2\%}_{-7.4\%} \pm 10.2\%$	75.87(4) $^{+2.2\%}_{-6.4\%} \pm 1.2\%$	1.32
$\sigma_{\phi W}$	8.12(2) $^{+13.1\%}_{-9.3\%} \pm 9.3\%$	7.76(2) $^{+7.0\%}_{-6.3\%} \pm 1.0\%$	0.96
$\sigma_{\phi W, \phi W}$	5.212(7) $^{+10.6\%}_{-6.8\%} \pm 10.2\%$	6.263(7) $^{+2.6\%}_{-7.8\%} \pm 1.3\%$	1.20
$\sigma_{t\phi}$	-1.203(6) $^{+12.0\%}_{-15.6\%} \pm 8.9\%$	-0.246(6) $^{+144.5[31.4]\%}_{-157.8[19.0]\%} \pm 2.1\%$	0.20
$\sigma_{t\phi, t\phi}$	0.6682(9) $^{+12.7\%}_{-8.9\%} \pm 9.6\%$	0.7306(8) $^{+4.6[0.6]\%}_{-7.3[0.2]\%} \pm 1.0\%$	1.09
σ_{tW}	19.38(6) $^{+13.0\%}_{-9.3\%} \pm 9.4\%$	22.18(6) $^{+3.8[0.4]\%}_{-6.8[0.9]\%} \pm 1.0\%$	1.14
$\sigma_{tW, tW}$	46.40(8) $^{+9.3\%}_{-5.5\%} \pm 11.1\%$	71.24(8) $^{+7.4[1.5]\%}_{-14.0[6.9]\%} \pm 1.9\%$	1.54
$\sigma_{\phi Q^{(3)}}$	-3.03(3) $^{+0.0\%}_{-2.2\%} \pm 15.4\%$	-10.04(4) $^{+11.1\%}_{-8.9\%} \pm 1.8\%$	3.31
$\sigma_{\phi Q^{(3)}, \phi Q^{(3)}}$	11.23(2) $^{+9.4\%}_{-5.6\%} \pm 11.2\%$	15.28(2) $^{+5.0\%}_{-10.9\%} \pm 1.8\%$	1.36
$\sigma_{\phi tb}$	0	0	—
$\sigma_{\phi tb, \phi tb}$	2.752(4) $^{+9.4\%}_{-5.5\%} \pm 11.3\%$	3.768(4) $^{+5.0\%}_{-10.9\%} \pm 1.8\%$	1.54
σ_{HW}	-3.526(4) $^{+5.6\%}_{-9.5\%} \pm 10.9\%$	-5.27(1) $^{+6.5\%}_{-2.9\%} \pm 1.5\%$	1.50
$\sigma_{HW, HW}$	0.9356(4) $^{+7.9\%}_{-4.0\%} \pm 12.3\%$	1.058(1) $^{+4.8\%}_{-11.9\%} \pm 2.3\%$	1.13
σ_{tG}	—	-0.418(5) $^{+12.3\%}_{-9.8\%} \pm 1.1\%$	—
$\sigma_{tG, tG}$	—	1.413(1) $^{+21.3\%}_{-30.6\%} \pm 2.5\%$	—
$\sigma_{Qq^{(3,1)}}$	-22.50(5) $^{+8.0\%}_{-11.8\%} \pm 9.7\%$	-20.10(5) $^{+13.8\%}_{-13.3\%} \pm 1.1\%$	0.89
$\sigma_{Qq^{(3,1)}, Qq^{(3,1)}}$	69.78(3) $^{+8.0\%}_{-4.1\%} \pm 12.1\%$	62.20(3) $^{+11.5\%}_{-15.9\%} \pm 2.3\%$	0.89
$\sigma_{Qq^{(3,8)}}$	—	0.25(3) $^{+25.4\%}_{-27.1\%} \pm 4.7\%$	—
$\sigma_{Qq^{(3,8)}, Qq^{(3,8)}}$	15.53(2) $^{+8.0\%}_{-4.1\%} \pm 12.1\%$	14.07(2) $^{+11.0\%}_{-15.7\%} \pm 2.1\%$	0.91

Inclusive results: $tZj@13$ TeV

- K -factor not universal.
- Reduction of scale/PDF uncertainties.
- Deviation $\sim 20\%$ within current constraints (O_{tW} and O_{tB}).
- EFT contributions smaller relative to SM.
 - Higgs always radiated from top/EW gauge boson, but Z boson can also come from light quark leg.

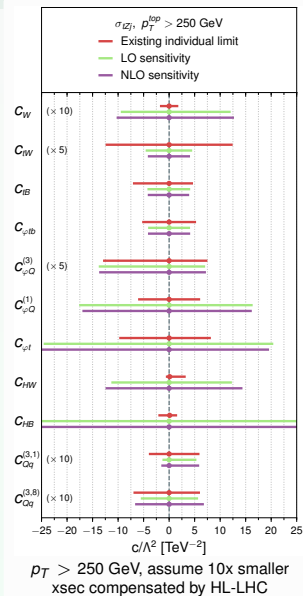
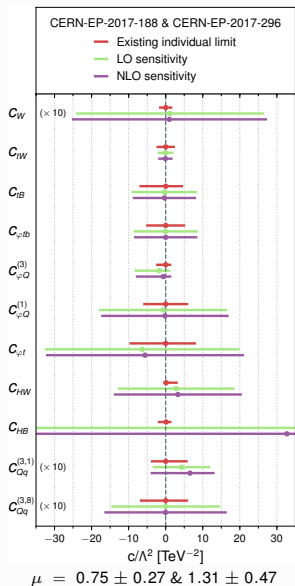
σ [fb]	LO	NLO	K-factor
σ_{SM}	660.8(4) $^{+13.7\%}_{-9.6\%} \pm 9.7\%$	839.1(5) $^{+1.1\%}_{-5.1\%} \pm 1.0\%$	1.27
σ_W	-7.87(7) $^{+8.4\%}_{-12.6\%} \pm 9.7\%$	-8.77(8) $^{+8.5\%}_{-4.3\%} \pm 1.1\%$	1.12
$\sigma_{W,W}$	34.58(3) $^{+8.2\%}_{-3.9\%} \pm 13.0\%$	43.80(4) $^{+6.6\%}_{-15.1\%} \pm 2.8\%$	1.27
σ_B	2.23(2) $^{+14.7(0.9)\%}_{-10.7(1.0)\%} \pm 9.4\%$	2.94(2) $^{+2.3(0.4)\%}_{-3.0(0.7)\%} \pm 1.1\%$	1.32
$\sigma_{B,B}$	2.833(2) $^{+10.5(1.7)\%}_{-6.3(1.9)\%} \pm 11.1\%$	4.155(3) $^{+4.7(0.9)\%}_{-10.1(1.4)\%} \pm 1.7\%$	1.47
σ_{tW}	2.66(4) $^{+18.8(0.9)\%}_{-15.3(1.0)\%} \pm 11.4\%$	13.0(1) $^{+15.8(2.1)\%}_{-22.8(0.0)\%} \pm 1.2\%$	4.90
$\sigma_{tW,W}$	48.16(4) $^{+10.0(1.7)\%}_{-5.8(1.9)\%} \pm 11.3\%$	80.00(4) $^{+7.9(1.3)\%}_{-14.7(1.6)\%} \pm 1.9\%$	1.66
$\sigma_{\phi BR}$	4.20(1) $^{+14.9\%}_{-10.9\%} \pm 9.3\%$	4.94(2) $^{+3.4\%}_{-6.7\%} \pm 1.0\%$	1.18
$\sigma_{\phi BR, \phi BR}$	0.3326(3) $^{+13.6\%}_{-9.5\%} \pm 9.6\%$	0.4402(5) $^{+3.7\%}_{-9.3\%} \pm 1.0\%$	1.32
$\sigma_{\phi Q}$	14.98(2) $^{+14.5\%}_{-10.5\%} \pm 9.4\%$	18.07(3) $^{+2.3\%}_{-1.6\%} \pm 1.0\%$	1.21
$\sigma_{\phi Q, \phi Q}$	0.7442(7) $^{+14.1\%}_{-10.0\%} \pm 9.5\%$	1.028(1) $^{+2.8\%}_{-7.3\%} \pm 1.0\%$	1.38
$\sigma_{\phi Q(3)}$	130.04(8) $^{+13.8\%}_{-9.8\%} \pm 9.5\%$	161.4(1) $^{+0.9\%}_{-4.8\%} \pm 1.0\%$	1.24
$\sigma_{\phi Q(3), \phi Q(3)}$	17.82(2) $^{+11.7\%}_{-7.5\%} \pm 10.5\%$	23.98(2) $^{+3.7\%}_{-9.3\%} \pm 1.4\%$	1.35
$\sigma_{\phi B}$	0	0	—
$\sigma_{\phi B, \phi B}$	2.949(2) $^{+10.5\%}_{-6.2\%} \pm 11.1\%$	4.154(4) $^{+5.1\%}_{-11.2\%} \pm 1.8\%$	1.41
σ_{HW}	-5.16(6) $^{+7.8\%}_{-12.0\%} \pm 10.5\%$	-6.88(8) $^{+6.4\%}_{-2.0\%} \pm 1.4\%$	1.33
$\sigma_{HW, HW}$	0.912(2) $^{+9.4\%}_{-5.2\%} \pm 12.0\%$	1.048(2) $^{+5.2\%}_{-12.8\%} \pm 2.1\%$	1.15
σ_{HB}	-3.015(9) $^{+9.9\%}_{-13.9\%} \pm 9.5\%$	-3.76(1) $^{+5.2\%}_{-1.0\%} \pm 1.0\%$	1.25
$\sigma_{HB, HB}$	0.02324(6) $^{+12.7\%}_{-8.5\%} \pm 9.9\%$	0.02893(6) $^{+2.3\%}_{-7.5\%} \pm 1.1\%$	1.24
σ_{tQ}	0.45(2) $^{+93.0\%}_{-148.8\%} \pm 4.9\%$	—	—
$\sigma_{tQ, tQ}$	2.251(4) $^{+20.9\%}_{-30.0\%} \pm 2.5\%$	—	—
$\sigma_{Qq(3,1)}$	-393.5(5) $^{+8.1\%}_{-12.3\%} \pm 10.0\%$	-498(1) $^{+8.9\%}_{-3.2\%} \pm 1.2\%$	1.26
$\sigma_{Qq(3,1), Qq(3,1)}$	462.25(3) $^{+8.4\%}_{-4.1\%} \pm 12.7\%$	545.50(5) $^{+7.4\%}_{-17.4\%} \pm 2.9\%$	1.18
$\sigma_{Qq(3,8)}$	0	-0.9(3) $^{+23.3\%}_{-26.3\%} \pm 19.2\%$	—
$\sigma_{Qq(3,8), Qq(3,8)}$	102.73(5) $^{+8.4\%}_{-4.1\%} \pm 12.7\%$	111.18(5) $^{+9.3\%}_{-18.4\%} \pm 2.8\%$	1.08

Differential: $tZj@13$ TeV

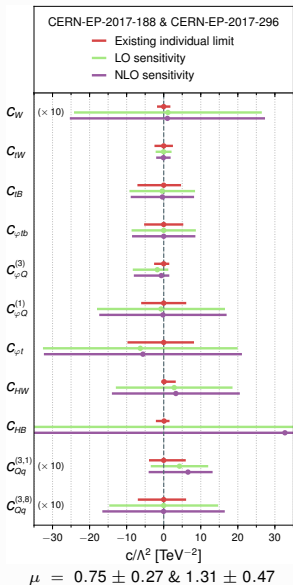


Potentially large deviation at the tails. . . (saturating current limits)

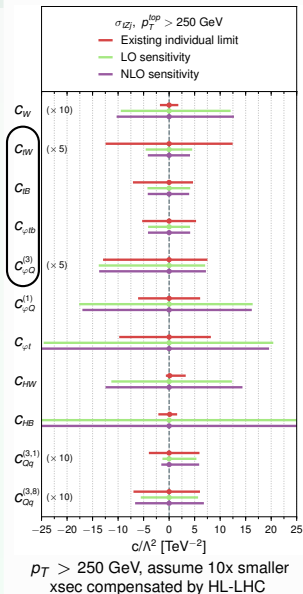
Current vs. future



Current vs. future



Expected
from
subamplitude
behaviours



Outline

1 EFT interpretation of top measurements

2 Top EFT @ NLO QCD

- Why we need NLO
- Available processes and operators
- Single top plus H/Z
- Future plan

3 EW corrections

- Higgs production & decay

4 Summary

Towards full SMEFT @ NLO in QCD implementation

We have started to work on a more complete SMEFT implementation @ NLO in QCD, including all relevant OPs for **top**, **Higgs** and **EW** measurements.

Towards full SMEFT @ NLO in QCD implementation

With two-quark and Higgs/EW operators implemented, we are still missing:

- $f^{ABC} G_{\mu}^{A\nu} G_{\nu}^{B\rho} G_{\rho}^{C\mu}$
- Four-fermion operators.
- Processes where QCD EW orders are mixed.

The three gluon operator

- Multijet processes impose so far the best bounds.

[F. Krauss, S. Kuttimalai, T. Plehn, '16]

- No interference with SM in di-jet at LO.

[Cho & Simmons '94]

- NLO being checked.

(Hirschi, Tsirikos, Vryondiou, ...)

Towards full SMEFT @ NLO in QCD implementation

With two-quark and Higgs/EW operators implemented, we are still missing:

- $f^{ABC} G_{\mu}^{A\nu} G_{\nu}^{B\rho} G_{\rho}^{C\mu}$ ✓
- Four-fermion operators.
- Processes where QCD QED orders are mixed.

Four-fermion operator

- Main difficulty is the “evanescent operator” basis, which now becomes automated in NLOCT.

Four-fermion operators are important, as they are tree-level induced and enter many processes.

- Two-light-two-heavy $qqtt$ operators are important for $t\bar{t}$ and $t\bar{t} + X$.
- $tttt$ and $ttbb$ production: rich phenomenology, more opportunities. . .

[Degrande, Gerard, Grojean, Maltoni, Servant, '10]

Four-top production

The four top production

- has a current upper bound about $4 \sim 5 \times \text{SM}$.
- ALREADY sensitive to $qqtt$ operators.
- Resulting constraints can compete with $t\bar{t}$.

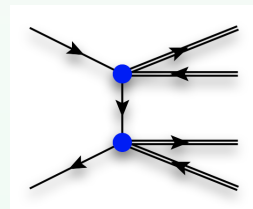
The special sensitivity comes from:

- 1 Large threshold energy.

$$C_{qqtt} \frac{E^2}{\Lambda^2} > 1$$

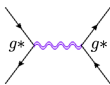
- 2 Multiple insertion.

$$\sigma_{dim-6} \sim \sigma_{SM} \left(C_{qqtt} \frac{E^2}{\Lambda^2} \right)^4$$



Is EFT@dim6 still valid with multiple insertion of operators, $\sim (CE^2/\Lambda^2)^4$?

- Consider the one-scale-one-coupling example in [\[Contino,Falkowski,Goertz,Grojean,Riva,'16\]](#)
- When the extra $1/\Lambda^2$ from expanding the amplitude:



$$\frac{1}{p^2 - \Lambda_{NP}^2} = -\frac{1}{\Lambda_{NP}^2} \left[1 + \frac{p^2}{\Lambda_{NP}^2} + \left(\frac{p^2}{\Lambda_{NP}^2} \right)^2 + \dots \right]$$

The expansion parameter is E^2/Λ_{NP}^2 .

Valid as far as $p^2 < \Lambda_{NP}^2$ (by imposing kinematic cut), so neglecting dim-8 operator is ok, independent of size of g_* .

- When the extra $1/\Lambda^2$ from squaring the amplitude:

$$M \sim g_{SM}^2 + \frac{g_*^2 E^2}{\Lambda_{NP}^2} \sim 1 + \frac{CE^2}{\Lambda^2}, \quad (\text{using } \frac{g_*^2}{\Lambda_{NP}^2} = \frac{C}{\Lambda^2})$$

$$|M|^2 \sim g_{SM}^4 + \frac{g_{SM}^2 g_*^2 E^2}{\Lambda_{NP}^2} + \frac{g_*^4 E^4}{\Lambda_{NP}^4} \sim 1 + \frac{CE^2}{\Lambda^2} + \left(\frac{CE^2}{\Lambda^2} \right)^2$$

"Expansion parameter" is CE^2/Λ^2 . it depends on g_* and if large, cannot truncate. But we can always include this term, as it does not involve dim-8 and higher operators.

Similar in four-top: $\sigma_{dim-6} \sim \sigma_{SM} \left(C^{(6)} \frac{E^2}{\Lambda^2} \right)^4$

- For multiple insertion and squaring amplitude, expansion parameter is

$$C^{(6)} E^2 / \Lambda^2$$

These will be kept. (Highest power is 4)

- For higher dim operators, if the expansion parameter is

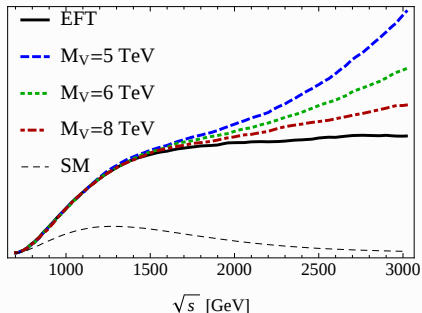
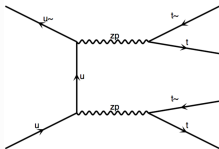
$$E^2 / \Lambda_{NP}^2$$

we impose kinematic cut so that

$$E^2 < M_{cut}^2 < \Lambda_{NP}^2$$

- Could be model dependent, but is natural for "one-scale-one-coupling" kind of models. (Also process-dependent: four-top will not be enhanced by more than four powers of g_* .)

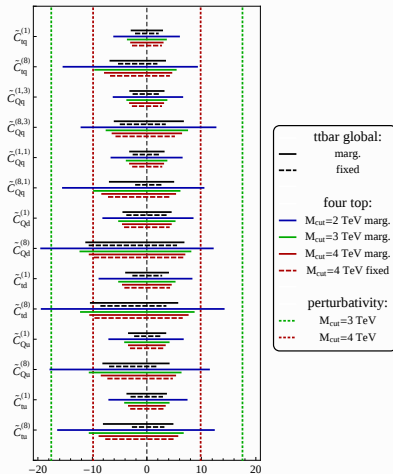
Example



Comparison with $t\bar{t}$

- Four top projection: $\mu < 1.87$ with 300 fb^{-1} .
- Compared with $t\bar{t}$: global fit including
 - xsec at Tevatron + LHC 8/13
 - A_{FB} and A_C at Tevatron + LHC 8
 - $m_{t\bar{t}}$ distribution at LHC 8
- Marginalized limits on $qqtt$ (also marginalized over $tttt$ operators).
- Still conservative: assume SM signal shape, and compare M_{cut} with total upper limit.

[CZ,'17]



More to be probed with $pp \rightarrow ttbb$ (PRELIMINARY)

[J. D'Hondt, A. Mariotti, K. Mimasu, S. Moortgat, **CZ**, in progress]

- $\sim 10\times$ larger cross section; kinematic information accessible.
- Lower threshold $\Rightarrow$ smaller $M_{cut} \Rightarrow$ more model-independence.
- Probe more 4-heavy operators:

$$O_{QQ}^1 = \frac{1}{2} (\bar{Q} \gamma_\mu Q) (\bar{Q} \gamma^\mu Q),$$

$$O_{QQ}^8 = \frac{1}{2} (\bar{Q} \gamma_\mu T^A Q) (\bar{Q} \gamma^\mu T^A Q),$$

$$O_{tb}^1 = (\bar{t} \gamma_\mu t) (\bar{b} \gamma_\mu b),$$

$$O_{tb}^8 = (\bar{t} \gamma_\mu T^A t) (\bar{b} \gamma_\mu T^A b),$$

$$O_{Qt}^1 = (\bar{Q} \gamma_\mu Q) (\bar{t} \gamma^\mu t),$$

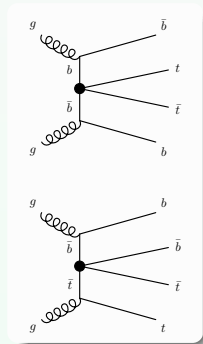
$$O_{Qt}^8 = (\bar{Q} \gamma_\mu T^A Q) (\bar{t} \gamma^\mu T^A t),$$

$$O_{Qb}^1 = (\bar{Q} \gamma_\mu Q) (\bar{b} \gamma^\mu b),$$

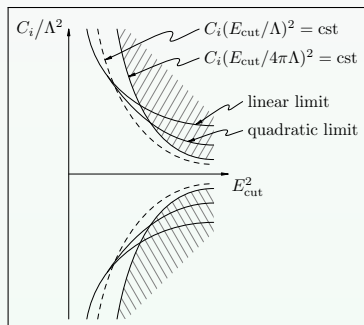
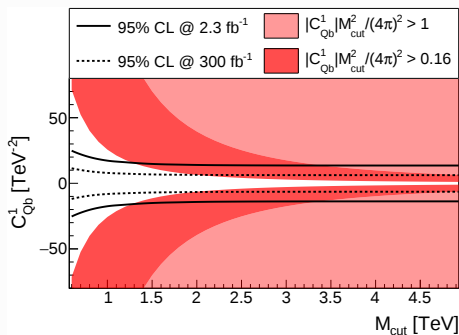
$$O_{Qb}^8 = (\bar{Q} \gamma_\mu T^A Q) (\bar{b} \gamma^\mu T^A b),$$

$$O_{QtQb}^1 = (\bar{Q} t) \varepsilon (\bar{Q} b),$$

$$O_{QtQb}^8 = (\bar{Q} T^A t) \varepsilon (\bar{Q} T^A b).$$



Validity & perturbativity (PRELIMINARY)

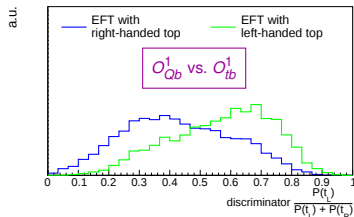
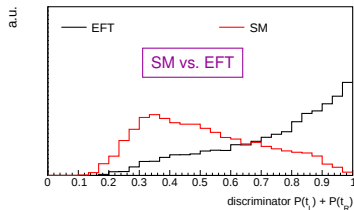
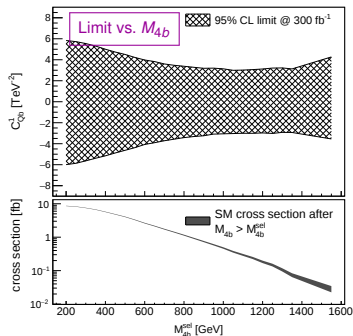


Limits at 95% CL on C_{Qb}^1 as a function of the mass cut M_{cut} for an integrated luminosity of 2.3 fb^{-1} (solid line) and 300 fb^{-1} (dashed line). The non-perturbative regime of the EFT in which $|C|M_{cut}^2/\Lambda^2 < (4\pi)^2$ is indicated with the light red shaded region. The darker red region represents the extension of the non-perturbative region for which the upper limit on the Wilson coefficient (at 300 fb^{-1}) crosses exactly the perturbativity threshold at a mass cut of $M_{cut} = 2 \text{ TeV}$.

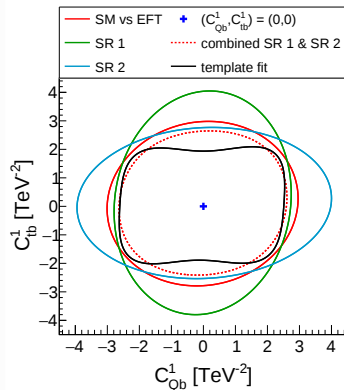
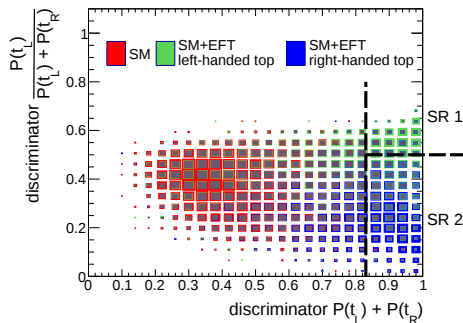
Approach (PRELIMINARY)

To improve sensitivity:

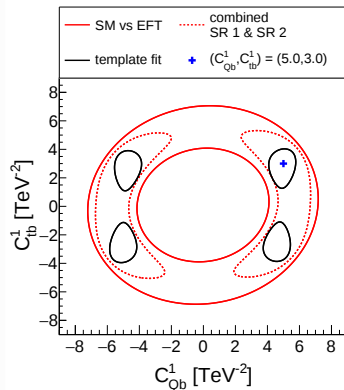
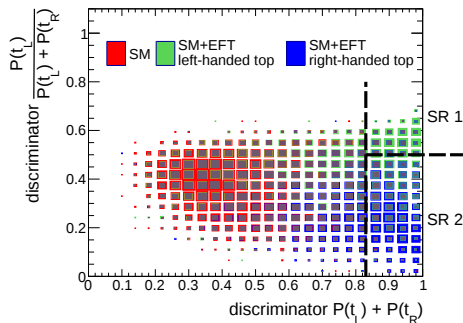
- Kinematic cut on $M_{4b} \downarrow$
- Use a multi-class shallow neural network $\Rightarrow$



NN outputs (PRELIMINARY)



NN outputs (PRELIMINARY)



Towards full SMEFT @ NLO in QCD implementation

With two-quark and Higgs/EW operators implemented, we are still missing:

- $f^{ABC} G_{\mu}^{A\nu} G_{\nu}^{B\rho} G_{\rho}^{C\mu}$ ✓
- Four-quark operators. Being worked out
- Processes where QCD QED orders are mixed.

Towards full SMEFT @ NLO in QCD implementation

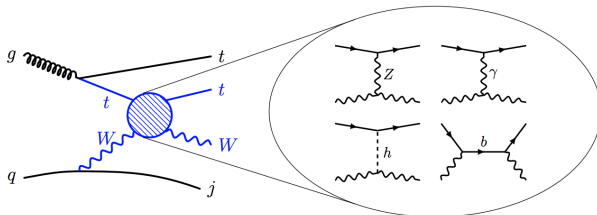


Figure 1: $tW \rightarrow tW$ scattering at the LHC. For definiteness, in the inset we show the diagrams corresponding to $tW^- \rightarrow tW^-$.

[Dror, Farina, Salvioni, Serra, '16]

Outline

1 EFT interpretation of top measurements

2 Top EFT @ NLO QCD

- Why we need NLO
- Available processes and operators
- Single top plus H/Z
- Future plan

3 **EW corrections**

- Higgs production & decay

4 Summary

Outline

1 EFT interpretation of top measurements

2 Top EFT @ NLO QCD

- Why we need NLO
- Available processes and operators
- Single top plus H/Z
- Future plan

3 EW corrections

- Higgs production & decay

4 Summary

Why EW?

[E. Vryonidou and CZ, '18]

In particular, focus on **top-loop induced contributions**.

- When saying “Higgs couplings”, what are we really talking about?



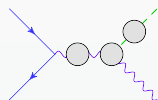
- Potentially, large relative corrections (unlike in the SM).

$$\frac{\sigma_{loop}}{\sigma_{tree}} \sim \alpha_{EW} \frac{C_{top}}{C_{Higgs}}$$

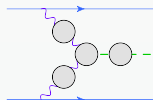
given that top operator constraints are in general much weaker.

- All Higgs production & decay are affected by same effects.

- A first step towards extending the existing NLO SMEFT implementation to incorporating EW corrections.
 - ▶ Some NLO EW results for Higgs decay, e.g.
[Hartmann & Trott, '15], [Ghezzi et al., '15],
[Gauld et al., '16], [Dawson & Giardino, '18]
- EW top-loop contribution in Higgs processes is a suitable starting point.



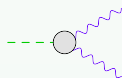
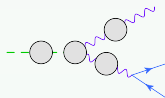
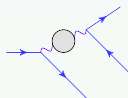
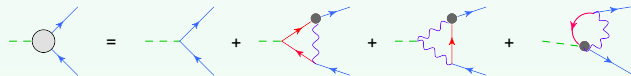
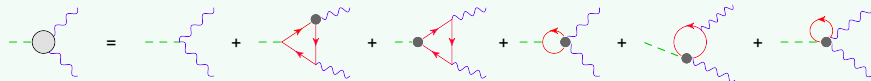
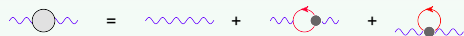
WH,ZH



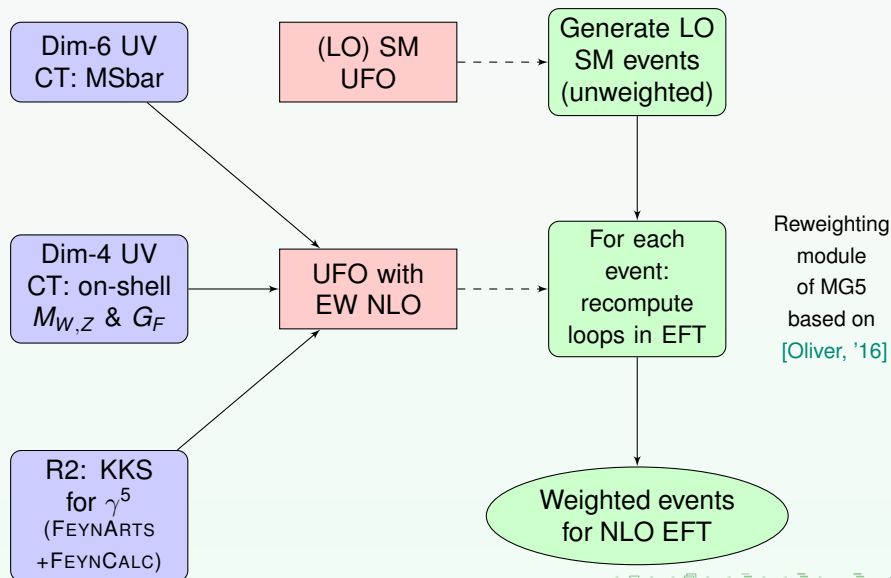
VBF

 $H \rightarrow \mu\mu, \tau\tau$ 

W,Z masses, oblique parameters

 $H \rightarrow \gamma\gamma, \gamma Z$  $H \rightarrow ZZ, WW$  $H \rightarrow b\bar{b}$  μ decay

How it works (for now)



Operator set

“Top operators” (top-gauge/top-Higgs couplings)

$$O_{t\varphi} = \bar{Q}t\tilde{\varphi}(\varphi^\dagger\varphi) + h.c.,$$

$$O_{\varphi Q}^{(3)} = (\varphi^\dagger \overleftrightarrow{D}_\mu^I \varphi)(\bar{Q}\gamma^\mu \tau^I Q),$$

$$O_{\varphi tb} = (\tilde{\varphi}^\dagger iD_\mu \varphi)(\bar{t}\gamma^\mu b) + h.c.,$$

$$O_{tB} = (\bar{Q}\sigma^{\mu\nu} t)\tilde{\varphi}B_{\mu\nu} + h.c.,$$

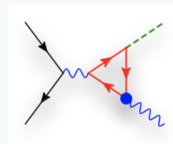
$$O_{\varphi Q}^{(+)} \equiv \frac{1}{2} (O_{\varphi Q}^{(1)} + O_{\varphi Q}^{(3)}),$$

$$O_{\varphi Q}^{(1)} = (\varphi^\dagger \overleftrightarrow{D}_\mu \varphi)(\bar{Q}\gamma^\mu Q),$$

$$O_{\varphi t} = (\varphi^\dagger \overleftrightarrow{D}_\mu \varphi)(\bar{t}\gamma^\mu t),$$

$$O_{tW} = (\bar{Q}\sigma^{\mu\nu} \tau^I t)\tilde{\varphi}W_{\mu\nu}^I + h.c.,$$

$$O_{\varphi Q}^{(-)} \equiv \frac{1}{2} (O_{\varphi Q}^{(1)} - O_{\varphi Q}^{(3)}).$$



“Higgs operators”

$$O_{\varphi WB} = \varphi^\dagger \tau^I \varphi W_{\mu\nu}^I B^{\mu\nu},$$

$$O_{\varphi B} = \varphi^\dagger \varphi B_{\mu\nu} B^{\mu\nu},$$

$$O_{\varphi D} = (\varphi^\dagger D^\mu \varphi)^* (\varphi^\dagger D_\mu \varphi),$$

$$O_B = iD^\mu \varphi^\dagger D^\nu \varphi B_{\mu\nu},$$

$$O_{\mu\varphi} = (\varphi^\dagger \varphi) \bar{l}_2 \not{e}_2 \varphi,$$

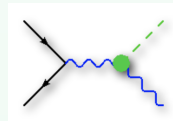
$$O_{\varphi W} = \varphi^\dagger \varphi W_{\mu\nu}^I W^{I\mu\nu},$$

$$O_{\varphi\Box} = (\varphi^\dagger \varphi) \Box (\varphi^\dagger \varphi),$$

$$O_W = iD^\mu \varphi^\dagger \tau^I D^\nu \varphi W_{\mu\nu}^I,$$

$$O_{b\varphi} = (\varphi^\dagger \varphi) \bar{Q}b\varphi,$$

$$O_{\tau\varphi} = (\varphi^\dagger \varphi) \bar{l}_3 \not{e}_3 \varphi.$$



RG mixing

	$O_{\varphi t}$	$O_{\varphi Q}^{(+)}$	$O_{\varphi Q}^{(-)}$	$O_{\varphi tb}$	O_{tW}	O_{tB}	$O_{t\varphi}$
$O_{\varphi WB}$	$\frac{1}{3s_W c_W}$	$\frac{1}{3s_W c_W}$	$-\frac{1}{6s_W c_W}$	0	$-\frac{5y_t}{2ec_W}$	$-\frac{3y_t}{2es_W}$	0
$O_{\varphi D}$	$-6\frac{y_t^2}{e^2}$	$3\frac{y_t^2 - y_b^2}{e^2}$	$3\frac{y_t^2 - y_b^2}{e^2}$	$-6\frac{y_t y_b}{e^2}$	0	0	0
$O_{\varphi \square}$	$-\frac{3}{2}\frac{y_t^2}{e^2}$	$-\frac{3y_t^2 + 6y_b^2}{2e^2}$	$\frac{6y_t^2 + 3y_b^2}{2e^2}$	$3\frac{y_t y_b}{e^2}$	0	0	0
$O_{\varphi W}$	0	$\frac{1}{4s_W^2}$	$-\frac{1}{4s_W^2}$	0	$\frac{3y_t}{2es_W}$	0	0
$O_{\varphi B}$	$\frac{1}{3c_W^2}$	$\frac{1}{12c_W^2}$	$\frac{1}{12c_W^2}$	0	0	$\frac{5y_t}{2ec_W}$	0
O_W	0	$\frac{1}{es_W}$	$-\frac{1}{es_W}$	0	0	0	0
O_B	$\frac{4}{3ec_W}$	$\frac{1}{3ec_W}$	$\frac{1}{3ec_W}$	0	0	0	0
$O_{b\varphi}$	0	$-\frac{y_b}{2c_W^2}$ $+y_b\frac{8\lambda - 3y_t^2 - 5y_b^2}{4e^2}$	$y_b\frac{-4\lambda + 3y_t^2 + 7y_b^2}{4e^2}$	$\frac{3y_t}{4s_W^2}$ $-y_t\frac{2\lambda + y_t^2 - 6y_b^2}{2e^2}$	$\frac{y_t y_b}{2es_W}$	0	$\frac{3y_t y_b}{4e^2}$
$O_{\mu\varphi}$	0	$-\frac{3y_\mu(y_t^2 + y_b^2)}{2e^2}$	$\frac{3y_\mu(y_t^2 + y_b^2)}{2e^2}$	$\frac{3y_t y_b y_\mu}{e^2}$	0	0	$\frac{3y_t y_\mu}{2e^2}$
$O_{\tau\varphi}$	0	$-\frac{3y_\tau(y_t^2 + y_b^2)}{2e^2}$	$\frac{3y_\tau(y_t^2 + y_b^2)}{2e^2}$	$\frac{3y_t y_b y_\tau}{e^2}$	0	0	$\frac{3y_t y_\tau}{2e^2}$

Consistent with [Alonso, Jenkins, Manohar, Trott]

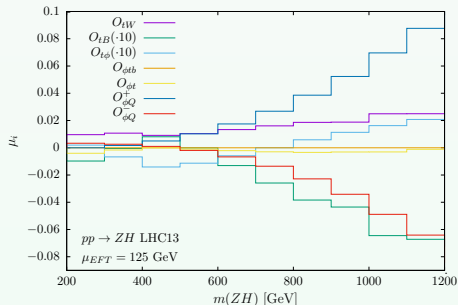
Renormalization

- Dim-6 coefficients are subtracted by $\overline{\text{MS}}$, except for $C_{\varphi WB}$ and $C_{\varphi D}$, which enter precision EW measurements.
- We use S and T parameters as “observables” to renormalize $C_{\varphi WB}$ and $C_{\varphi D}$.
 - ▶ so that $C_{\varphi WB} = C_{\varphi D} = 0$ is consistent with EWPO.
 - ▶ In some sense, this means we always turn on top-operators in such a way that is consistent with the most stringent constraints from EWPO.
- Remaining dim-6 effects are subtracted with SM counter terms, in M_W , M_Z and G_F scheme.
 - ▶ In particular we want to fix M_W because it enters the phase space.

NLO EW UFO

with which we can simulate **dim-6 top loop corrections** in many processes thanks to automation

- at LHC: WH, ZH, VBF
- at e^+e^- : ZH, WWF, ZZF
- H decay: $\gamma\gamma$, γZ , $Wl\nu$, Zll , bb , $\tau\tau$, $\mu\mu$
- Many others: W/Z-pole, widths, $ee \rightarrow ff$, Drell-Yan, ...
- Easy access to kinematic information.



Result 1: LHC

Within the current constraints, by how much can top operators affect Higgs signal strengths at the LHC?

	$\gamma\gamma$	γZ	bb	WW^*	ZZ^*	$\tau\tau, \mu\mu$
gg	(-100%,1980%)	(-88%,200%)	(-40%,48%)	(-40%,47%)	(-40%,46%)	(-40%,48%)
VBF	(-100%,1880%)	(-88%,170%)	(-6.1%,5.3%)	(-6.8%,6.7%)	(-8.8%,9.2%)	(-6.2%,5.9%)
WH	(-100%,1880%)	(-88%,170%)	(-5.5%,4.2%)	(-6.1%,5.6%)	(-7.8%,7.9%)	(-5.8%,5.1%)
ZH	(-100%,1880%)	(-87%,170%)	(-6.5%,5.9%)	(-7.1%,7.1%)	(-9.4%,9.9%)	(-6.8%,6.7%)

- Large in first two columns and first row, because SM is loop.
- The other pure NLO EW EFT effects are not negligible, $\sim 10\%$.

Result 2: future e^+e^- machine

- 250 GeV, with all top operators.

	$\gamma\gamma$	γZ	bb	WW*	ZZ*	$\tau\tau, \mu\mu$
ZH(+30%,-80%)	(-100%,1900%)	(-87%,160%)	(-7.5%,7.5%)	(-8.3%,8.6%)	(-11%,11%)	(-8%,8.3%)
ZH(-30%,+80%)	(-100%,1870%)	(-88%,180%)	(-7.6%,7.1%)	(-8.1%,7.9%)	(-10%,11%)	(-7.6%,7.3%)
WWF(+30%,-80%)	(-100%,1880%)	(-88%,170%)	(-5.7%,4.7%)	(-6.5%,6.2%)	(-8.1%,8.3%)	(-5.9%,5.3%)
WWF(-30%,+80%)	(-100%,1880%)	(-88%,170%)	(-5.7%,4.7%)	(-6.5%,6.2%)	(-8.1%,8.3%)	(-5.9%,5.3%)
ZZF(+30%,-80%)	(-100%,1790%)	(-88%,180%)	(-11%,8.6%)	(-11%,9.6%)	(-13%,12%)	(-11%,9%)
ZZF(-30%,+80%)	(-100%,1730%)	(-88%,180%)	(-14%,11%)	(-14%,12%)	(-15%,15%)	(-14%,11%)

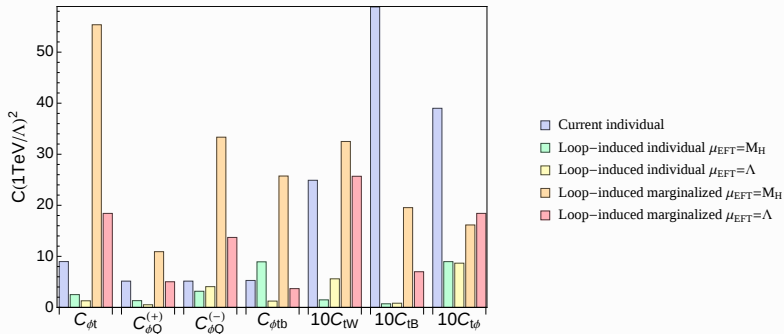
- 250 GeV, with only top Yukawa.

	$\gamma\gamma$	γZ	bb	WW*	ZZ*	$\tau\tau, \mu\mu$
ZH(+30%,-80%)	(-17%,19%)	(-7.3%,7%)	(-4%,3.3%)	(-4.5%,4%)	(-4.9%,4.4%)	(-3.6%,3%)
ZH(-30%,+80%)	(-17%,19%)	(-7.5%,7.2%)	(-4.1%,3.5%)	(-4.7%,4.2%)	(-5.1%,4.6%)	(-3.8%,3.2%)
WWF(+30%,-80%)	(-17%,18%)	(-7.2%,7%)	(-3.9%,3.3%)	(-4.4%,3.9%)	(-4.9%,4.3%)	(-3.5%,2.9%)
WWF(-30%,+80%)	(-17%,18%)	(-7.2%,7%)	(-3.9%,3.3%)	(-4.4%,3.9%)	(-4.9%,4.3%)	(-3.5%,2.9%)
ZZF(+30%,-80%)	(-17%,19%)	(-7.6%,7.3%)	(-4.2%,3.6%)	(-4.8%,4.3%)	(-5.2%,4.7%)	(-3.9%,3.3%)
ZZF(-30%,+80%)	(-17%,19%)	(-7.5%,7.2%)	(-4.1%,3.5%)	(-4.7%,4.2%)	(-5.1%,4.6%)	(-3.8%,3.2%)

It is possible to probe top couplings below the $t\bar{t}$ threshold

Result 3: HL-LHC

Projected “bounds” at HL-LHC



- **Neglecting Higgs operators, only a “sensitivity” study.**
- $\mu_{EFT} = M_H$: scale at the measurements. This is what should be done for a global fit.
- $\mu_{EFT} = \Lambda = 1 \text{ TeV}$: scale at BSM scale. In general better limits but more model-dependent.

Take-home message?

- Treating the dim-6 top-quark sector (top EFT) and the Higgs/EW sector (Higgs EFT) separately will not continue to be a good approximation in the future.
- A more global approach will be needed to take into account the interplay at loop level.

Outline

1 EFT interpretation of top measurements

2 Top EFT @ NLO QCD

- Why we need NLO
- Available processes and operators
- Single top plus H/Z
- Future plan

3 EW corrections

- Higgs production & decay

4 Summary

Summary

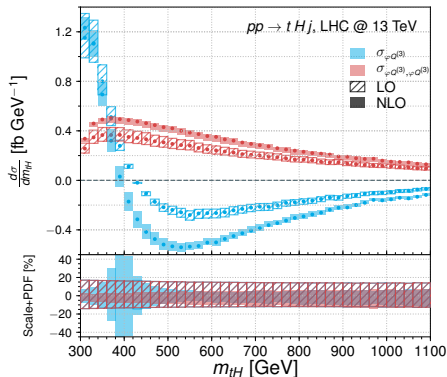
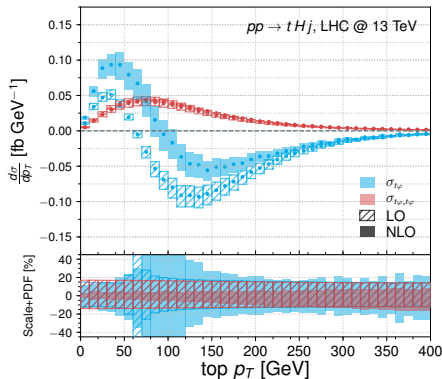
- Reasoning for higher orders in SMEFT.
- NLO QCD tools are available many processes and are becoming more complete.
- EW corrections are being studies, and can have non trivial implications.
- Let us know your needs.



Backups

Inclusive results: $tHj@13$ TeV

Phase space cancellation



Cancellations over the PS appear/disappear for the interference lead to strange K-factors and large scale uncertainties.

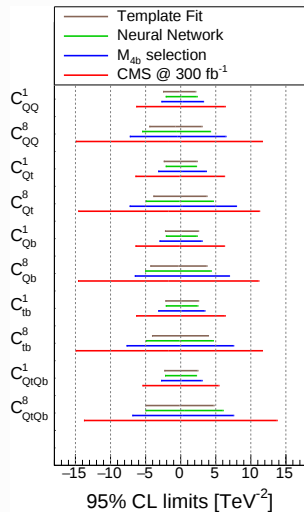
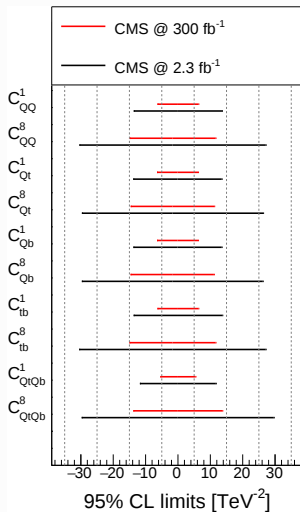
Sensitivities

	tj	tj ($p_T^t > 350$ GeV)	tZj	tZj ($p_T^t > 250$ GeV)	tHj
σ_{SM}	224 pb	880 fb	839 fb	69 fb	75.9 fb
r_{tW}	0.0275	0.024	0.016	0.010	0.292
$r_{tW,tW}$	0.0162	0.35	0.095	0.67	0.940
$r_{\varphi Q^{(3)}}$	0.1213	0.120	0.192	0.172	-0.132
$r_{\varphi Q^{(3)},\varphi Q^{(3)}}$	0.00368	0.0036	0.029	0.114	0.21
$r_{\varphi tb,\varphi tb}$	0.00090	0.0008	0.0050	0.027	0.050
r_{tG}	0.0003	-0.01	0.00053	-0.0048	-0.0055
$r_{tG,tG}$	0.00062	0.045	0.0027	0.022	0.025
$r_{Qq^{(3,1)}}$	-0.353	-4.4	-0.59	-2.22	-0.39
$r_{Qq^{(3,1)},Qq^{(3,1)}}$	0.126	11.5	0.65	5.1	1.21
$r_{Qq^{(3,8)},Qq^{(3,8)}}$	0.0308	2.73	0.133	1.01	1.08

Table 6: Comparison among the NLO sensitivities of tj (inclusive and with $p_T^t > 350$ GeV), tZj (inclusive and with $p_T^t > 250$ GeV), and tHj to the six operators which are common to the three processes, *i.e.*, those entering in tj . The interference term $r_i = \sigma_i/\sigma_{SM}$ (when non-zero) and the square $r_{i,i} = \sigma_{i,i}/\sigma_{SM}$ are given for each operator. σ_i and $\sigma_{i,i}$ are defined in Eq. (4.1).

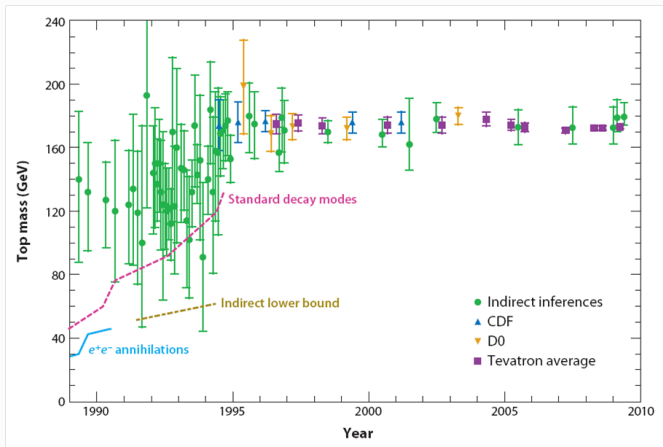
Prospects

- 95% CL on all the Wilson coefficients.
- Left: xsec measurement at 2.3 fb⁻¹ and prospects for 300 fb⁻¹.
- Right: xsec at 300 fb⁻¹ compared with M_{4b} selection and NN.



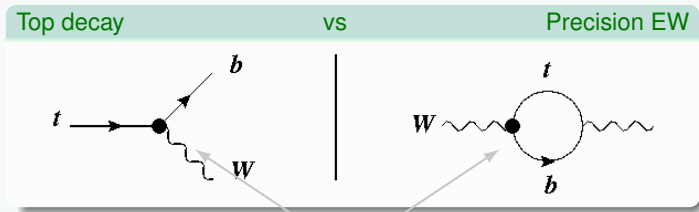
Constrain the Top using PEWD

History of top quark mass



Quigg

Constrain the Top using EWPO



$$O_{tW} = (\bar{Q}\sigma^{\mu\nu}\tau^I t) W_{\mu\nu}^I$$

Direct probe:

Pros Larger (LO) effect

Cons Larger background

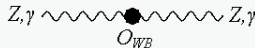
Precision EW:

Pros Better precision level

Cons Loop suppressed effect

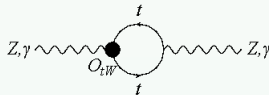
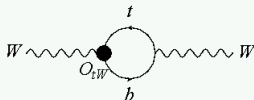
Need global fit

tree level:



$$O_{WB} = (\varphi^\dagger \tau^I \varphi) W_{\mu\nu}^I B^{\mu\nu}$$

loop level:



● with Dimensional Regularization and $\overline{MS}$

$$\alpha S = 4 \frac{C_{WB}(\mu) v^2}{\Lambda^2} s_W c_W + N_c \frac{C_{tW}}{2\pi^2} \frac{\sqrt{2} m_W m_t}{\Lambda^2} \frac{5}{3} s_W^2 \left(-\ln \frac{m_t^2}{\mu^2} - 2 \frac{\sqrt{4m_t^2 - m_Z^2}}{m_Z} \arctan \frac{m_Z}{\sqrt{4m_t^2 - m_Z^2}} + 2 \right)$$

... cannot distinguish C_{tW} from C_{WB} and set bound.

should avoid setting $C_{WB}(\mu) = 0$

Global Fit

However, if global:

- Include all 8 (t,b) operators at loop level.

$$\begin{aligned}
 O_{\phi Q}^{(3)} &= i(\phi^\dagger \tau^I D_\mu \phi)(\bar{Q} \gamma^\mu \tau^I Q), & O_{\phi Q}^{(1)} &= i(\phi^\dagger D_\mu \phi)(\bar{Q} \gamma^\mu Q), \\
 O_{\phi t} &= i(\phi^\dagger D_\mu \phi)(\bar{t} \gamma^\mu t), & O_{\phi b} &= i(\phi^\dagger D_\mu \phi)(\bar{b} \gamma^\mu b), \\
 O_{tW} &= (\bar{Q} \sigma^{\mu\nu} \tau^I t) \tilde{\phi} W_{\mu\nu}^I, & O_{bW} &= (\bar{Q} \sigma^{\mu\nu} \tau^I b) \phi W_{\mu\nu}^I, \\
 O_{tB} &= (\bar{Q} \sigma^{\mu\nu} t) \tilde{\phi} B_{\mu\nu}, & O_{bB} &= (\bar{Q} \sigma^{\mu\nu} b) \phi B_{\mu\nu}.
 \end{aligned}$$

- Include tree level EW operators.

$$O_{WB} = (\varphi^\dagger \tau^I \varphi) W_{\mu\nu}^I B^{\mu\nu}, \quad O_\varphi^{(3)} = (\varphi^\dagger D^\mu \varphi)[(D_\mu \varphi)^\dagger \varphi].$$

Correspond to S and T parameters.

- Include the full set of precision measurements (101 data points...)
- Enough d.o.f to constrain all!

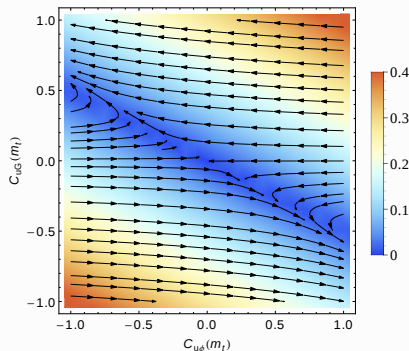
$$\begin{pmatrix} -0.702 & -0.701 & -0.000 & +0.128 & -0.003 & +0.000 & -0.000 & -0.000 \\ +0.094 & +0.087 & +0.002 & +0.992 & +0.019 & -0.001 & +0.001 & +0.000 \\ -0.244 & +0.251 & -0.228 & +0.019 & -0.901 & +0.071 & -0.080 & -0.041 \\ +0.405 & -0.404 & +0.675 & +0.004 & -0.408 & +0.049 & +0.218 & -0.005 \\ -0.136 & +0.136 & -0.126 & +0.000 & +0.002 & -0.138 & +0.936 & +0.229 \\ -0.035 & +0.034 & -0.039 & -0.001 & +0.094 & +0.745 & +0.244 & -0.610 \\ -0.004 & +0.004 & +0.007 & -0.000 & +0.025 & +0.646 & -0.090 & +0.757 \\ -0.505 & +0.505 & +0.689 & +0.000 & +0.108 & -0.014 & -0.054 & -0.009 \end{pmatrix} \\
\times \frac{1}{\Lambda^2} \begin{pmatrix} C_{\phi Q}^{(3)} \\ C_{\phi Q}^{(1)} \\ C_{\phi t} \\ C_{\phi b} \\ C_{tW} \\ C_{bW} \\ C_{tB} \\ C_{bB} \end{pmatrix} = \begin{pmatrix} -0.011 & \pm 0.014 \\ -0.59 & \pm 0.27 \\ +0.04 & \pm 1.17 \\ +2.84 & \pm 2.12 \\ +1.7 & \pm 11.9 \\ +8.7 & \pm 21.2 \\ +102.4 & \pm 50.4 \\ +1.10\text{e}+3 & \pm 1.41\text{e}+3 \end{pmatrix} \text{TeV}^{-2}.$$

Counting

- 3045 operators at dim-6 already
- 44807 at dim-8, 2092441 at dim-10, $\dots$, and at dim-15 everyone gets an operator. . .
[Buchmuller & Wyler, '86] [B. Grzadkowski et al., '10] [Lehman & Marin, '15] [B. Henning et al., '15]
- Even in top physics, 4-fermion operators count 572 in total.

Example in $t \rightarrow uh$

Mixing between color-dipole and Yukawa



Scale corresponds to the change from m_t to 2 TeV.

Example:

At $\mu = 1$ TeV: $C_{uG}^{(13)} = 1$, $C_{u\varphi}^{(13)} = 0$

$\Rightarrow$

At $\mu = 173$ GeV: $C_{uG}^{(13)} = 0.98$, $C_{u\varphi}^{(13)} = 0.23$

Operators

$$O_{uG}^{(13)} = y_t g_s (\bar{q} \sigma^{\mu\nu} T^A t) \bar{\varphi} G_{\mu\nu}^A$$

$$O_{uW}^{(13)} = y_t g_W (\bar{q} \sigma^{\mu\nu} \tau^I t) \bar{\varphi} W_{\mu\nu}^I$$

$$O_{uB}^{(13)} = y_t g_Y (\bar{q} \sigma^{\mu\nu} t) \bar{\varphi} B_{\mu\nu}$$

$$O_{u\varphi}^{(13)} = -y_t^3 (\varphi^\dagger \varphi) (\bar{q} t) \bar{\varphi}$$

Anomalous dimension

$$\gamma = \frac{2\alpha_s}{\pi} \begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & \frac{1}{3} & 0 & 0 \\ 0 & 0 & \frac{1}{3} & 0 \\ -2 & 0 & 0 & -1 \end{pmatrix}$$

Single top with H/Z : operators

tHj	• $\mathcal{O}_W$	$\varepsilon_{IJK} W_{\mu\nu}^I W^{J,\nu\rho} W_{\rho}^{K,\mu}$	• $\mathcal{O}_{\varphi Q}^{(3)}$	$i(\varphi^\dagger \overset{\leftrightarrow}{D}_\mu \tau_I \varphi)(\bar{Q} \gamma^\mu \tau^I Q) + \text{h.c.}$
tZj	• $\mathcal{O}_{\varphi W}$	$(\varphi^\dagger \varphi - \frac{v^2}{2}) W_I^{\mu\nu} W_{\mu\nu}^I$	• $\mathcal{O}_{\varphi Q}^{(1)}$	$i(\varphi^\dagger \overset{\leftrightarrow}{D}_\mu \varphi)(\bar{Q} \gamma^\mu Q) + \text{h.c.}$
both	• $\mathcal{O}_{\varphi WB}$	$(\varphi^\dagger \tau_I \varphi) B^{\mu\nu} W_{\mu\nu}^I$	• $\mathcal{O}_{\varphi t}$	$i(\varphi^\dagger \overset{\leftrightarrow}{D}_\mu \varphi)(\bar{t} \gamma^\mu t) + \text{h.c.}$
	• $\mathcal{O}_{\varphi D}$	$(\varphi^\dagger D^\mu \varphi)^\dagger (\varphi^\dagger D_\mu \varphi)$	• $\mathcal{O}_{\varphi tb}$	$i(\bar{\varphi} D_\mu \varphi)(\bar{t} \gamma^\mu b) + \text{h.c.}$
	• $\mathcal{O}_{\varphi \square}$	$(\varphi^\dagger \varphi) \square (\varphi^\dagger \varphi)$	• $\mathcal{O}_{\varphi q}^{(1)}$	$i(\varphi^\dagger \overset{\leftrightarrow}{D}_\mu \varphi)(\bar{q}_i \gamma^\mu q_i) + \text{h.c.}$
Rescaling of h couplings	• $\mathcal{O}_{t\varphi}$	$(\varphi^\dagger \varphi - \frac{v^2}{2}) \bar{Q} t \tilde{\varphi} + \text{h.c.}$	• $\mathcal{O}_{\varphi q}^{(3)}$	$i(\varphi^\dagger \overset{\leftrightarrow}{D}_\mu \tau_I \varphi)(\bar{q}_i \gamma^\mu \tau^I q_i) + \text{h.c.}$
	• $\mathcal{O}_{tW}$	$i(\bar{Q} \sigma^{\mu\nu} \tau_I t) \tilde{\varphi} W_{\mu\nu}^I + \text{h.c.}$	• $\mathcal{O}_{\varphi u}$	$i(\varphi^\dagger \overset{\leftrightarrow}{D}_\mu \varphi)(\bar{u}_i \gamma^\mu u_i) + \text{h.c.}$
	• $\mathcal{O}_{tB}$	$i(\bar{Q} \sigma^{\mu\nu} t) \tilde{\varphi} B_{\mu\nu} + \text{h.c.}$	• $\mathcal{O}_{Qq}^{(3,1)}$	$(\bar{q}_i \gamma_\mu \tau_I q_i)(\bar{Q} \gamma^\mu \tau^I Q)$
NLO	• $\mathcal{O}_{tG}^*$	$i(\bar{Q} \sigma^{\mu\nu} T_A t) \tilde{\varphi} G_{\mu\nu}^A + \text{h.c.}$	• $\mathcal{O}_{Qq}^{(3,8)}$	$(\bar{q}_i \gamma_\mu \tau_I T_A q_i)(\bar{Q} \gamma^\mu \tau^I T^A Q)$

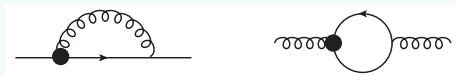
plus two “blind directions” from EW precision tests.

$$O_{HW} = (D^\mu \phi)^\dagger \tau_I (D^\nu \phi) W_{\mu\nu}^I, \quad O_{HB} = (D^\mu \phi)^\dagger (D^\nu \phi) B_{\mu\nu}.$$

[Grojean, Skiba, Terning, '06]

UV

- Comes from renormalization of the theory.
- What we do:
 - ▶ Dim-6: MSbar, for large logs and for we don't have ren conditions.
 - Running&mixing of coefficients: characterized by 2499×2499 matrix.
 - First computed by [\[R. Alonso et al.\]](#) (and refs therein) but we always check.
 - ▶ Remaining finite effects modify the SM renormalization, wave functions and masses, g_s etc. e.g. from O_{tG}



R2

- R2 comes from the fact that MadLoop works in 4 dimension.

- ▶ **Loop amplitude:** $\frac{1}{(2\pi)^4} \int d^d \bar{q} \frac{\bar{N}(\bar{q})}{\bar{D}_0 \bar{D}_1 \cdots \bar{D}_{m-1}}, \bar{D}_i = (\bar{q} + p_i)^2 - m_i^2$
- ▶ MadLoop: numerical evaluates the 4-dimensional part, but need to add the missing D-4 part.
- ▶ **Solution:** isolate the ε -dim part of numerator: $\bar{N}(\bar{q}) = N(q) + \tilde{N}(\tilde{q}, q, \varepsilon)$
Then calculate ε part analytically, once and for all.

$$R2 \equiv \lim_{\varepsilon \rightarrow 0} \frac{1}{(2\pi)^4} \int d^d \bar{q} \frac{\bar{N}(\bar{q})}{\bar{D}_0 \bar{D}_1 \cdots \bar{D}_{m-1}}$$

R2

- 4-fermion operators

- ▶ Fermion flow at one loop: $\gamma^\mu P_L \otimes \gamma_\mu P_L \Rightarrow \gamma^\mu \gamma^\nu \gamma^\rho P_L \otimes \gamma_\mu \gamma_\nu \gamma_\rho P_L$
- ▶ Problem: Cannot be reduced to the standard 4-fermion operator basis (which is not complete in D dimension)
- ▶ Solution: Need to define E ="evanescent" operators,

$$\gamma^\mu \gamma^\nu \gamma^\rho P_L \otimes \gamma_\mu \gamma_\nu \gamma_\rho P_L = 4(4 - (x)\varepsilon) \gamma^\mu P_L \otimes \gamma_\mu P_L + E$$
- ▶ Result: Scheme dependence enters R2.