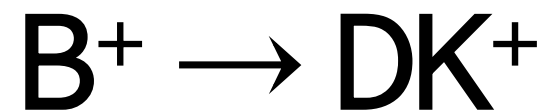


CKM gamma at LHCb



plan

- introduction
- B-Factory example
- LHCb
- expected sensitivity
- other channels

CKM quark mixing

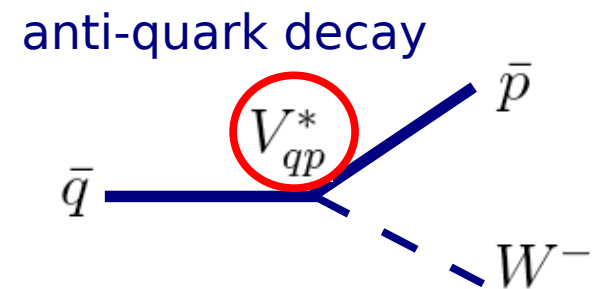
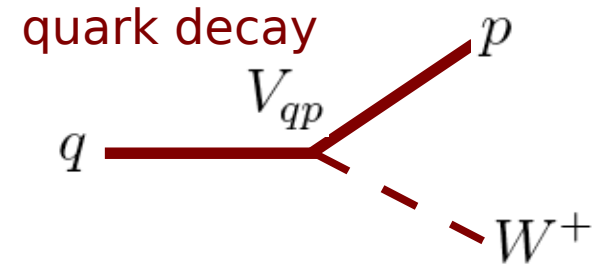
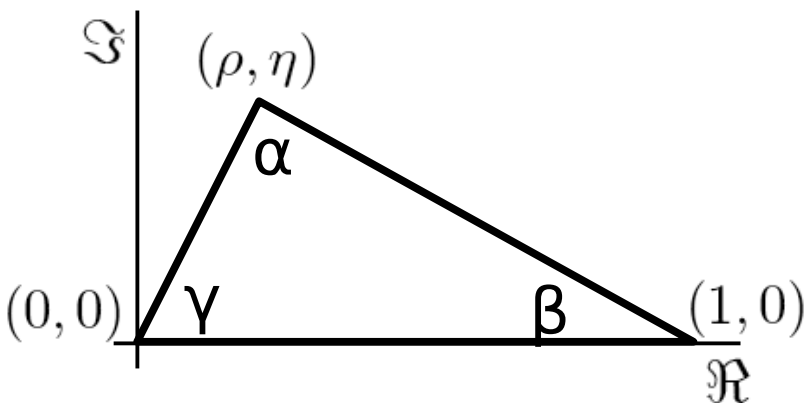
$$V_{CKM} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} \approx \begin{pmatrix} 1 - \lambda^2/2 & \lambda & A\lambda^3(\rho - i\eta) \\ -\lambda & 1 - \lambda^2/2 & A\lambda^2 \\ A\lambda^3(1 - \rho - i\eta) & -A\lambda^2 & 1 \end{pmatrix} + O(\lambda^4)$$

- flavor eigenstates are not mass eigenstates → relate them through a unitary matrix
- irreducible phase is the only source of CP violation in the Standard Model
- test the SM by over-constraining the unitarity triangle

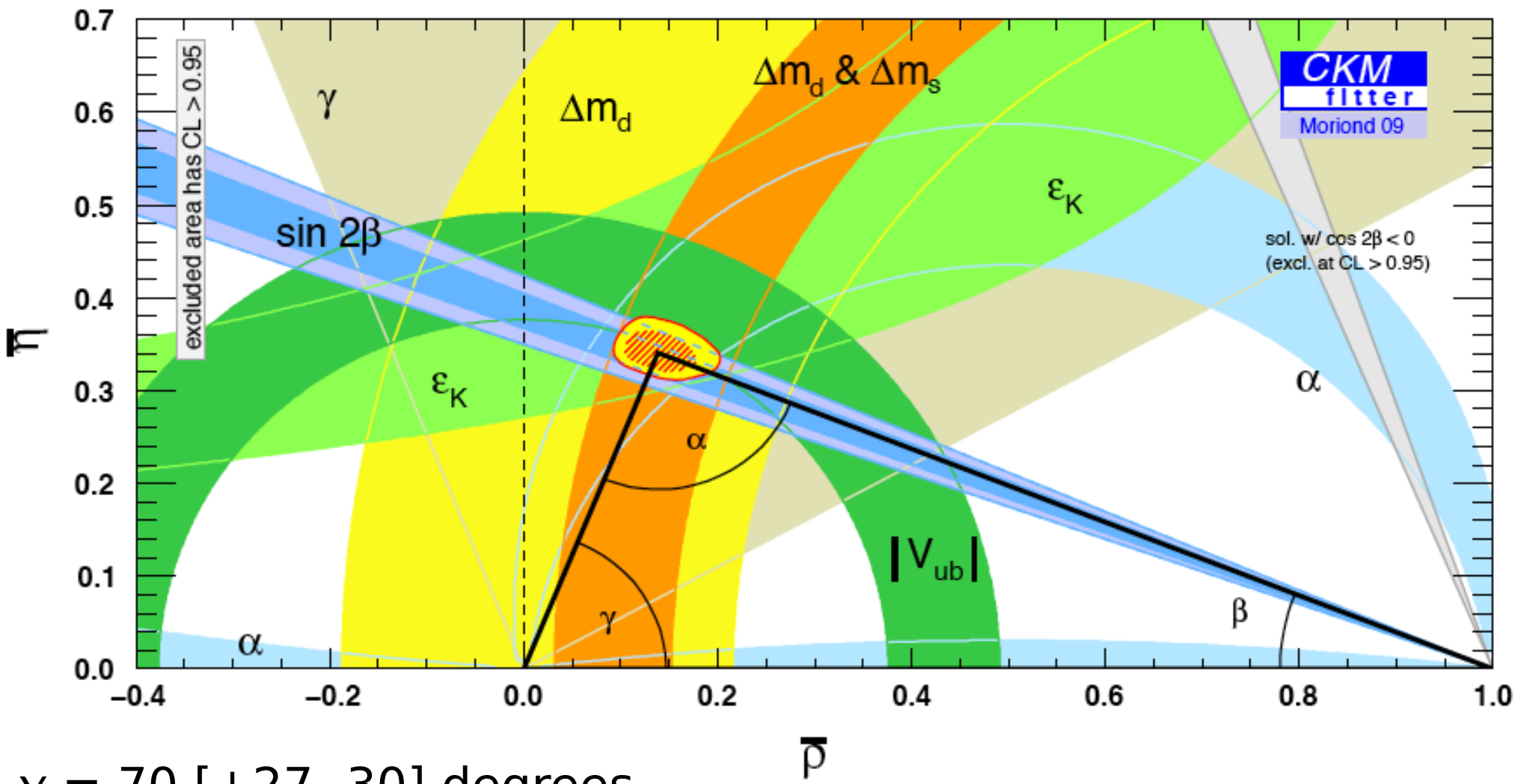
$$\begin{aligned} \lambda &\approx 0.23 \\ A &\approx 0.8 \\ \rho &\approx 0.2 \\ \eta &\approx 0.4 \end{aligned}$$

$$V_{ud}V_{ub}^* + V_{cd}V_{cb}^* + V_{td}V_{tb}^* = 0$$

$$\gamma = \arg \left(-\frac{V_{ud}V_{ub}^*}{V_{cd}V_{cb}^*} \right)$$



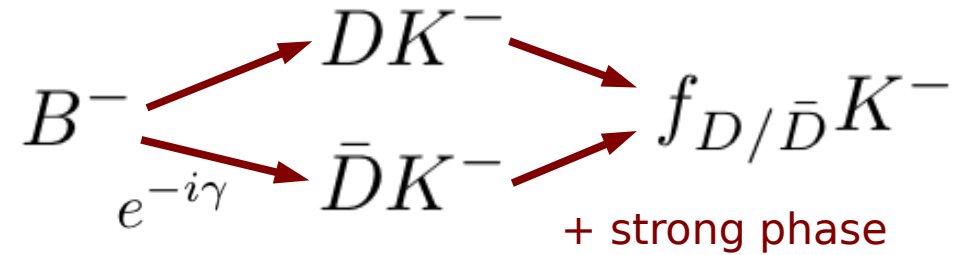
current situation



$\gamma = 70 [+27 -30]$ degrees

B → DK

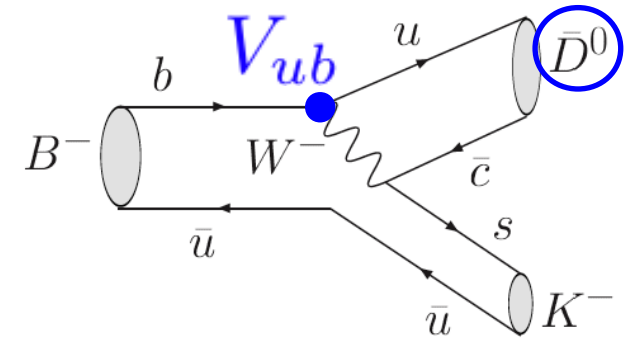
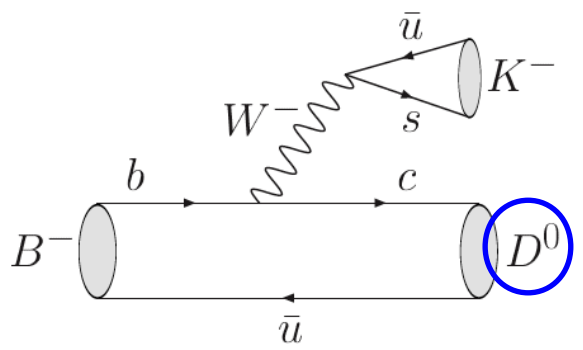
- Methods use final states accessible for both D^0 and \bar{D}^0 . Tree dominated, no new physics.



- Sensitivity on γ depends on amplitude ratio r . The uncertainty scales roughly like $1/r$.

$$r = \frac{|A(B \rightarrow \bar{D}^{(*)0} K)|}{|A(B \rightarrow D^{(*)0} K)|}$$

$$r \approx 0.1$$



- Several D final states can be used:
 - CP eigenstates (GLW)
 - Flavor eigenstates (ADS)
 - 3-body states (GGSZ Dalitz)

Gronau & London, PLB 253, 483 (1991)
 Gronau & Wyler, PLB 265, 172 (1991)
 Atwood, Dunietz, & Soni, PRL 78, 3257 (1997),
 Atwood, Dunietz, & Soni, PRD 63, 036005 (2001)
 Giri, Grossman, Soffer, & Zupan, PRD 68, 054018 (2003)
 Bondar, PRD 70, 072003 (2004)

BaBar GLW

- CP- D final states: $K_S \pi^0$ $K_S \omega$ $K_S \Phi$
- CP+ D final states: $\pi^+ \pi^-$ $K^+ K^-$
- flavor D final state: $K^+ \pi^-$

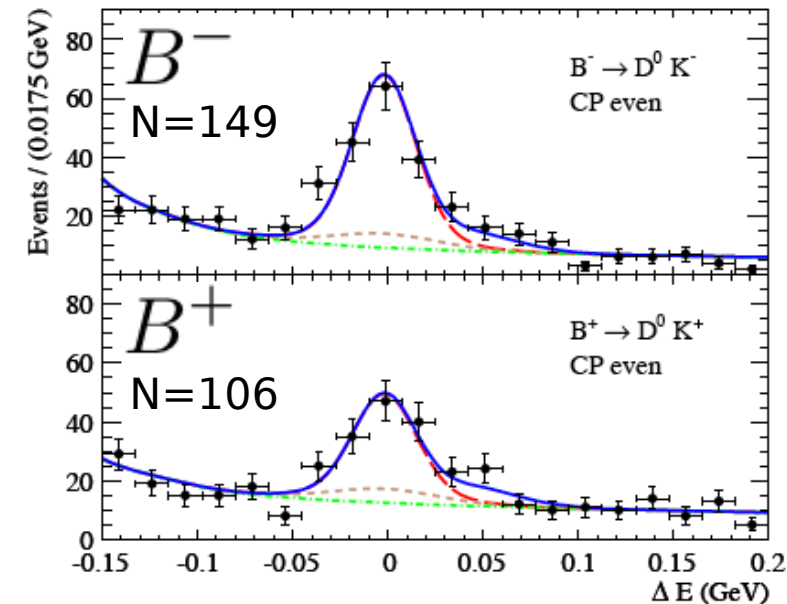
$$R_{CP\pm} = 1 + r^2 \pm 2r \cos \delta \cos \gamma$$

$$A_{CP\pm} = \pm 2r \sin \delta \sin \gamma / R_{CP\pm}$$

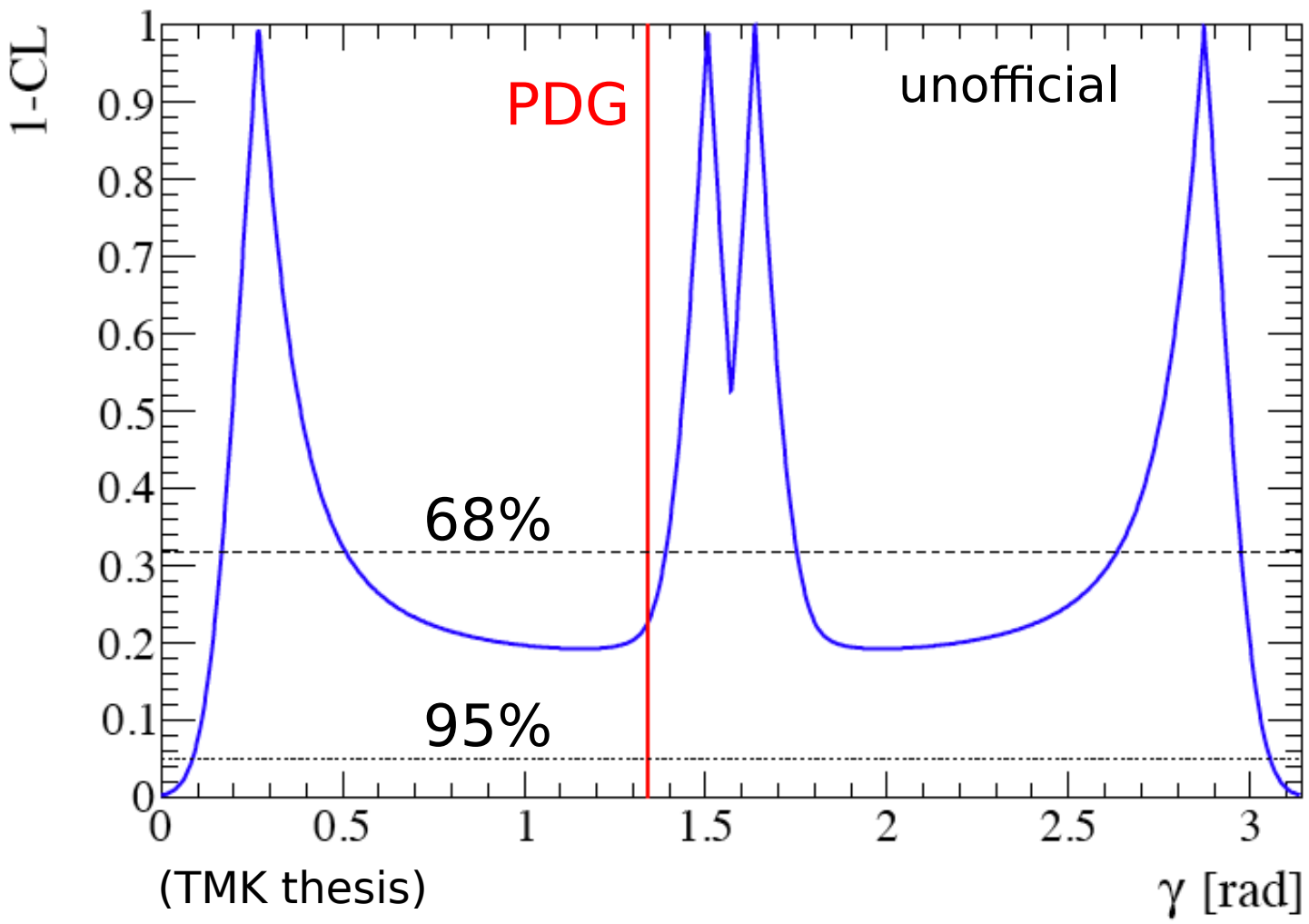
$$R_{CP\pm} = \frac{\Gamma(B^- \rightarrow D_{CP\pm}^0 K^-) + \Gamma(B^+ \rightarrow D_{CP\pm}^0 K^+)}{[\Gamma(B^- \rightarrow D^0 K^-) + \Gamma(B^+ \rightarrow \bar{D}^0 K^+)] / 2}$$

$$A_{CP\pm} = \frac{\Gamma(B^- \rightarrow D_{CP\pm}^0 K^-) - \Gamma(B^+ \rightarrow D_{CP\pm}^0 K^+)}{\Gamma(B^- \rightarrow D_{CP\pm}^0 K^-) + \Gamma(B^+ \rightarrow D_{CP\pm}^0 K^+)}$$

D^0 mode	R_{CP}	A_{CP}
CP+	$1.06 \pm 0.10 \pm 0.05$	$0.27 \pm 0.09 \pm 0.04$
CP-	$1.03 \pm 0.10 \pm 0.05$	$-0.09 \pm 0.09 \pm 0.02$

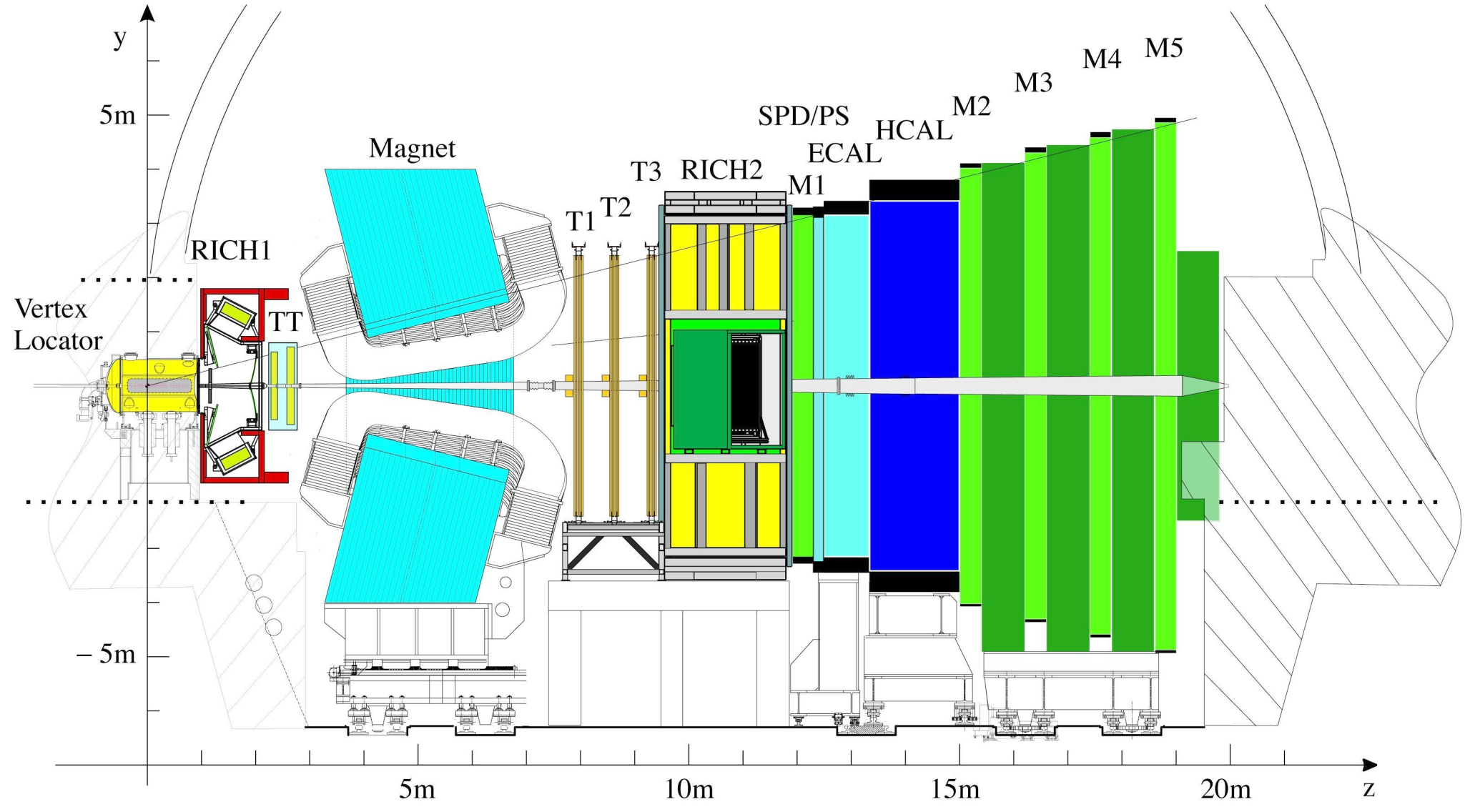


BaBar GLW



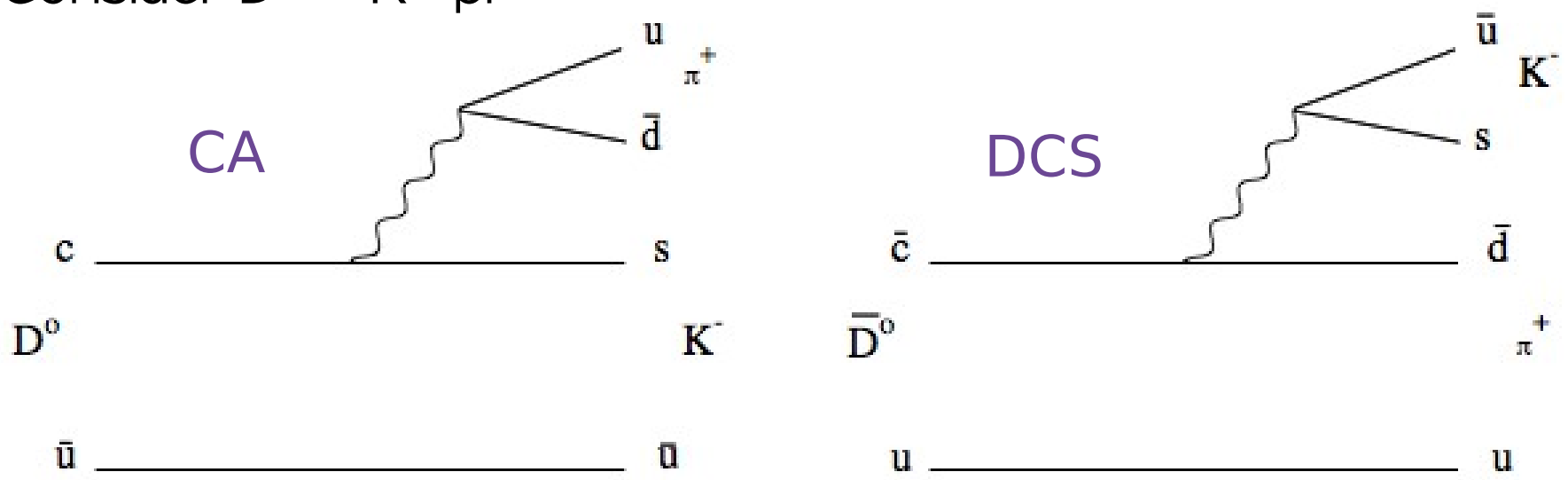
BaBar
final dataset

LHCb detector



GLW/ADS at LHCb

- At B-Factories, the “Dalitz analyses” are most successful:
 $B \rightarrow DK, D \rightarrow K_S \pi^+ \pi^-$
- LHCb’s strength are charged K’s and pi’s, therefore
 GLW/ADS channels are more promising
- Consider $D \rightarrow K^- \pi^+$



GLW/ADS at LHCb

- For the rates, it is:

allowed

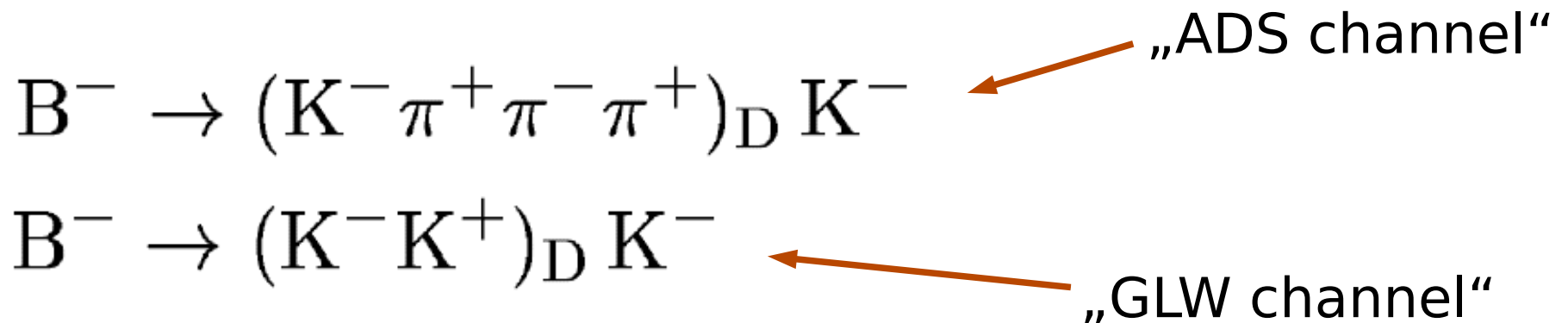
0.06 from CLEO

$$\begin{aligned} \Gamma(B^- \rightarrow (K^- \pi^+)_D K^-) &\propto 1 + (r_B r_D^{K\pi})^2 + 2 r_B r_D^{K\pi} \cos(\delta_B - \delta_D^{K\pi} - \gamma), \\ \Gamma(B^- \rightarrow (K^+ \pi^-)_D K^-) &\propto r_B^2 + (r_D^{K\pi})^2 + 2 r_B r_D^{K\pi} \cos(\delta_B + \delta_D^{K\pi} - \gamma), \\ \Gamma(B^+ \rightarrow (K^+ \pi^-)_D K^+) &\propto 1 + (r_B r_D^{K\pi})^2 + 2 r_B r_D^{K\pi} \cos(\delta_B - \delta_D^{K\pi} + \gamma), \\ \Gamma(B^+ \rightarrow (K^- \pi^+)_D K^+) &\propto r_B^2 + (r_D^{K\pi})^2 + 2 r_B r_D^{K\pi} \cos(\delta_B + \delta_D^{K\pi} + \gamma) \end{aligned}$$

- measuring relative rates gives **three** observables
- four** unknowns: γ , r_B , and strong phases differences in B and D decay

GLW/ADS at LHCb

- Solution: add more channels!
- Each channel adds **three** observables, but at max **two** unknown phases (ratios again taken from external sources)
- So the measurement seems possible by adding



expected yields in 2fb^{-1}

Channel	Signal	Background	
$B^\pm \rightarrow D(K^\pm \pi^\mp)K^\pm$	56k	35k	
$B^+ \rightarrow D(K^- \pi^+)K^+$	680	780	
$B^- \rightarrow D(K^+ \pi^-)K^-$	400	780	
$B^+ \rightarrow D(K^+ K^- + \pi^+ \pi^-)K^+$	3.3k	7.2k	x20 Babar
$B^- \rightarrow D(K^+ K^- + \pi^+ \pi^-)K^-$	4.4k	7.2k	
$B^\pm \rightarrow D(K^\pm \pi^\mp \pi^+ \pi^-)K^\pm$	61k	40k	
$B^+ \rightarrow D(K^- \pi^+ \pi^+ \pi^-)K^+$	470	1.2k	
$B^- \rightarrow D(K^+ \pi^- \pi^+ \pi^-)K^-$	350	1.2k	
$B^0 \rightarrow D(K^+ \pi^-)K^{*0}, \bar{B}^0 \rightarrow D(K^- \pi^+)\bar{K}^{*0}$	3.4k	1.7k	covered in this talk
$B^0 \rightarrow D(K^- \pi^+)K^{*0}$	350	850	
$\bar{B}^0 \rightarrow D(K^+ \pi^-)\bar{K}^{*0}$	230	850	
$B^0 \rightarrow D(K^+ K^- + \pi^+ \pi^-)K^{*0}$	150	500	
$\bar{B}^0 \rightarrow D(K^+ K^- + \pi^+ \pi^-)\bar{K}^{*0}$	550	500	
$B^\pm \rightarrow D(K_S^0 \pi^+ \pi^-)K^\pm$	5k	4.7k	
$B_s, \bar{B}_s \rightarrow D_s^\mp K^\pm$	6.2k	4.3k	
$B^0, \bar{B}^0 \rightarrow D^\mp \pi^\pm$	1,300k	290k	

expected global sensitivity

$\delta_{B^0} (\circ)$	0	45	90	135	180	
σ_γ for 0.5 fb^{-1} (\circ)	8.1	10.1	9.3	9.5	7.8	
σ_γ for 2 fb^{-1} (\circ)	4.1	5.1	4.8	5.1	3.9	$\sim 1\text{y}$
σ_γ for 10 fb^{-1} (\circ)	2.0	2.7	2.4	2.6	1.9	$\sim 10\text{y}$

contributing analyses (%):

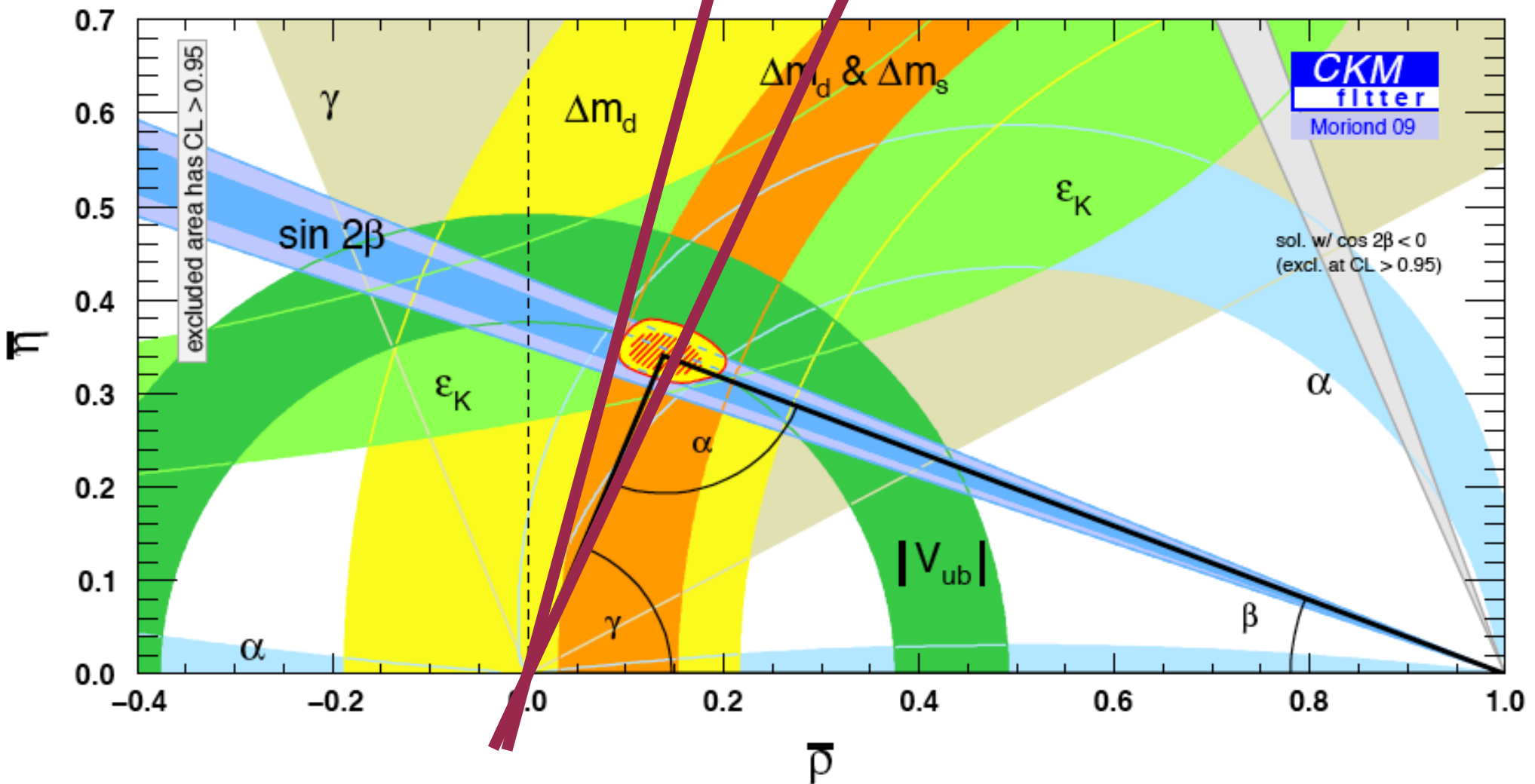
Analysis	$\delta_{B^0} = 0^\circ$	$\delta_{B^0} = 45^\circ$	
$B^- \rightarrow D^0(hh)K^-, B^- \rightarrow D^0(K^\pm \pi^\mp \pi^+ \pi^-)K^-$	25	38	GLW/ADS
$B^- \rightarrow D^0(K_s^0 \pi^+ \pi^-)K^-$	12	25	Dalitz
$B^0 \rightarrow D^0(hh)K^{*0}$	44	8	
$B_s \rightarrow D_s^\pm K^\mp$	16	24	r_{B^0} assumed to be 0.4
$B^0 \rightarrow D^\mp \pi^\pm$	3	5	

conclusion

- LHCb has great potential to measure CKM gamma
- Many modes couldn't be covered
(for instance the unique $B_s \rightarrow D_s K$ relying on β_s from $B \rightarrow J/\Psi \Phi$)
- A precision of **5 degrees** (stat) seems possible in 1y of nominal data taking.
- Will probably turn γ into a precision measurement!

Thanks to Guy Wilkinson et al.
for the relevant LHCb public notes.

expected sensitivity



$\gamma = 70 [+5 -5]$ degrees (1y nominal data)