

Search for 4th generation fermions: Motivation, status and prospects

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**Workshop on single top physics and fourth generation quarks
DESY, 14th and 15th September, 2009**

CONTENT

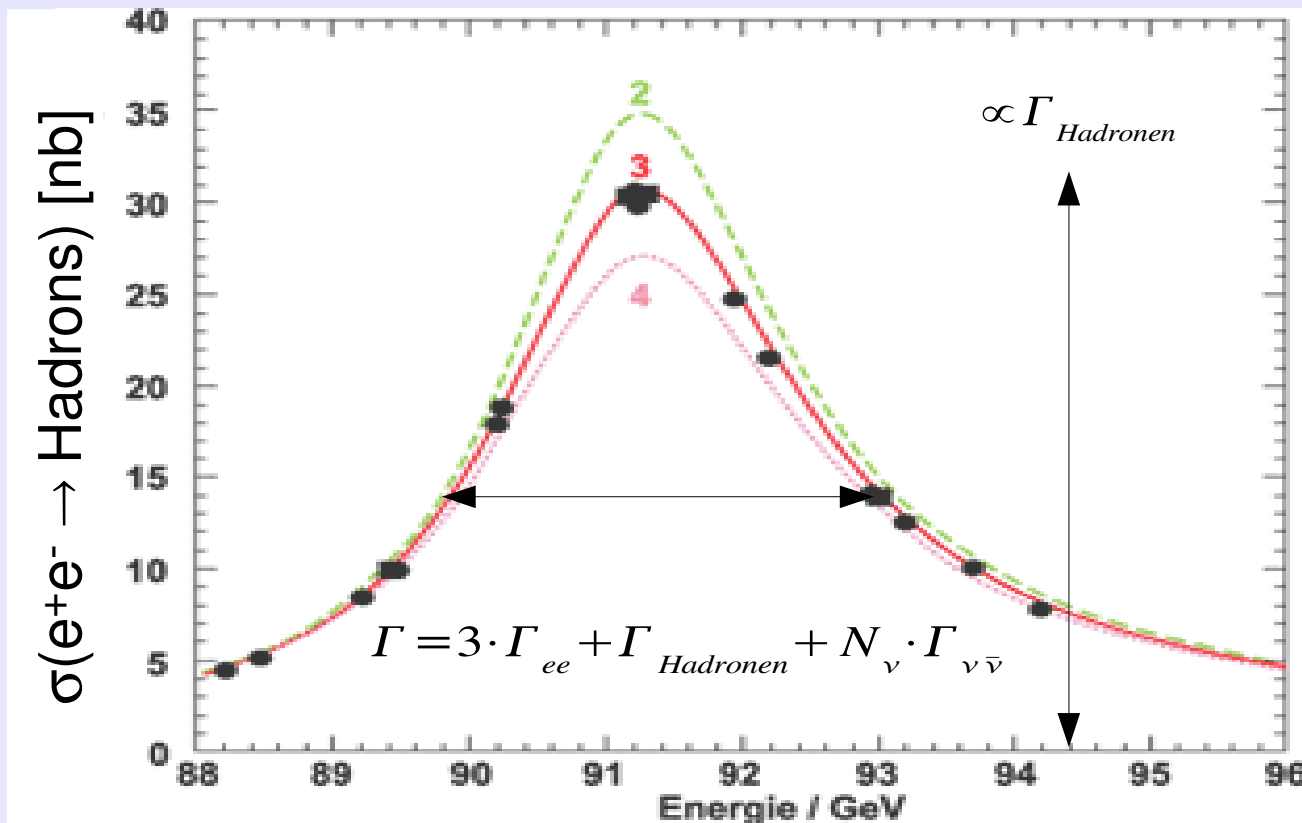
(only covering an additional Dirac generation)

1. Why is it interesting?
2. Mass constraints (Γ_Z , Direct searches @ LEP2 & Tevatron)
3. Effects of/constraints on a 4th generation:
 - Flavour physics: ---> Alexander Lenz
 - Higgs prod. & decays: ---> Tilman Plehn
 - Single Top production: ---> Fabio Maltoni
4. Constraints on masses from electroweak precision fit
5. What do we know about the CKM and PMNS matrix elements?
6. Search strategies @ LHC
7. Summary

1. Why is it interesting?

- No good argument yet for only $N_{\text{gen}}=3$ (Why generations at all?)
 $N_{\text{gen}} \geq 3 \Rightarrow$ CP violation in CKM matrix, but $N_{\text{gen}}=3$ not sufficient for baryogenesis
- $N_{\text{gen}}=4$: sufficient CP violation for SM baryogenesis in e.w. symmetry breaking (EWSB) due to large quark masses (Hou, Chin. J. Phys.47:134, 2009)
- Heavy 4th gen. quark masses $\Rightarrow$ strong EWSB
 $\rightarrow$ 2nd problem with $N_{\text{gen}}=3$ baryogenesis (M_{Higgs} too large) possibly solvable (Carena et al., NPB 716, 319, 2005)
- SU(5) gauge coupling unification w/o SUSY possible (Hung, PRL80, 3000, 1998)
- E.w. precision fit: 4th gen. not excluded (e.g. Kribs et al., PRD76:075016, 2007)
 $\Rightarrow$ significantly larger Higgs mass (up to ~ 600 GeV) allowed
 $\Rightarrow$ Quite different Higgs phenomenology possible ($\rightarrow$ T. Plehn)

2.1 Constraints on a 4th generation: Γ_Z



$$N_v = 2,984 \pm 0,008$$

in agreement
with primordial
nucleosynthesis

In case of a 4. generation:

$$m_{\nu_4} > M_Z/2$$

LEP2: $m_{l_4} > 100.8 \text{ GeV}$

$m_{\nu_4} > 90.3 \text{ GeV (Dirac)}$

$m_{\nu_4} > 80.5 \text{ GeV (Majorana)}$

All limits for unstable heavy leptons

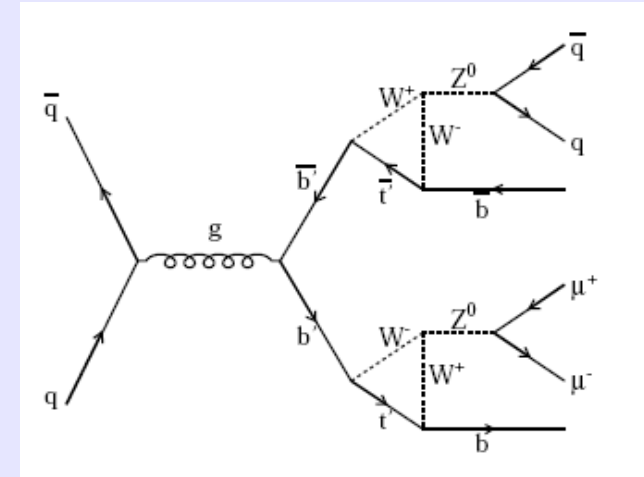
2.2 TEVATRON constraints: FCNC decay

CDF (1.06 fb⁻¹), PRD 76, 072006 (2007):

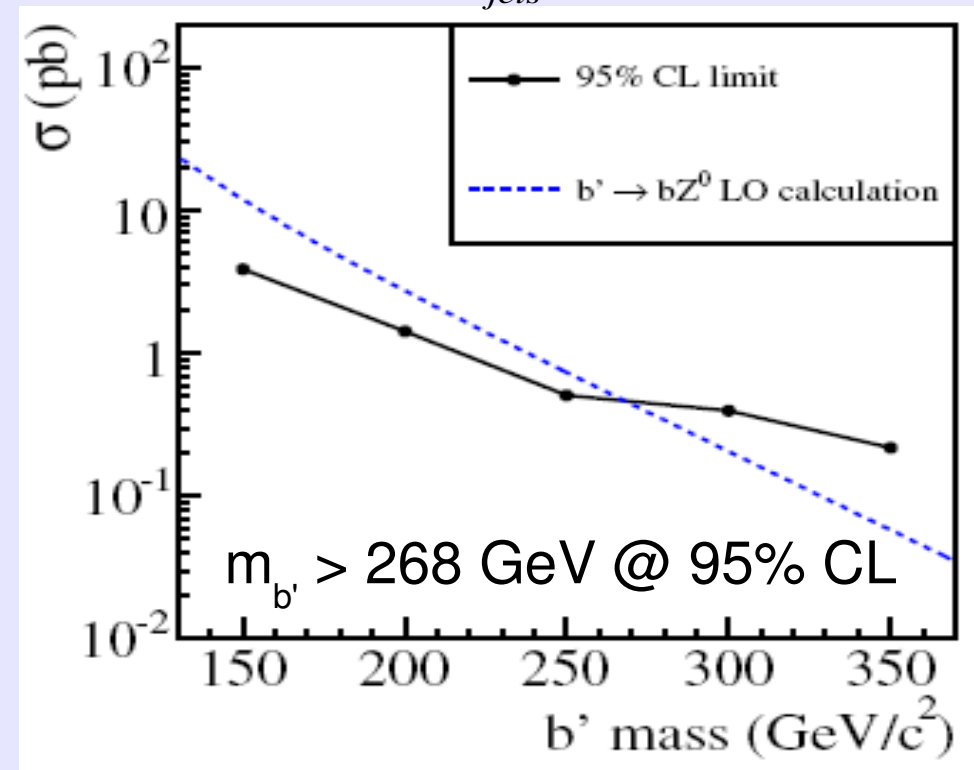
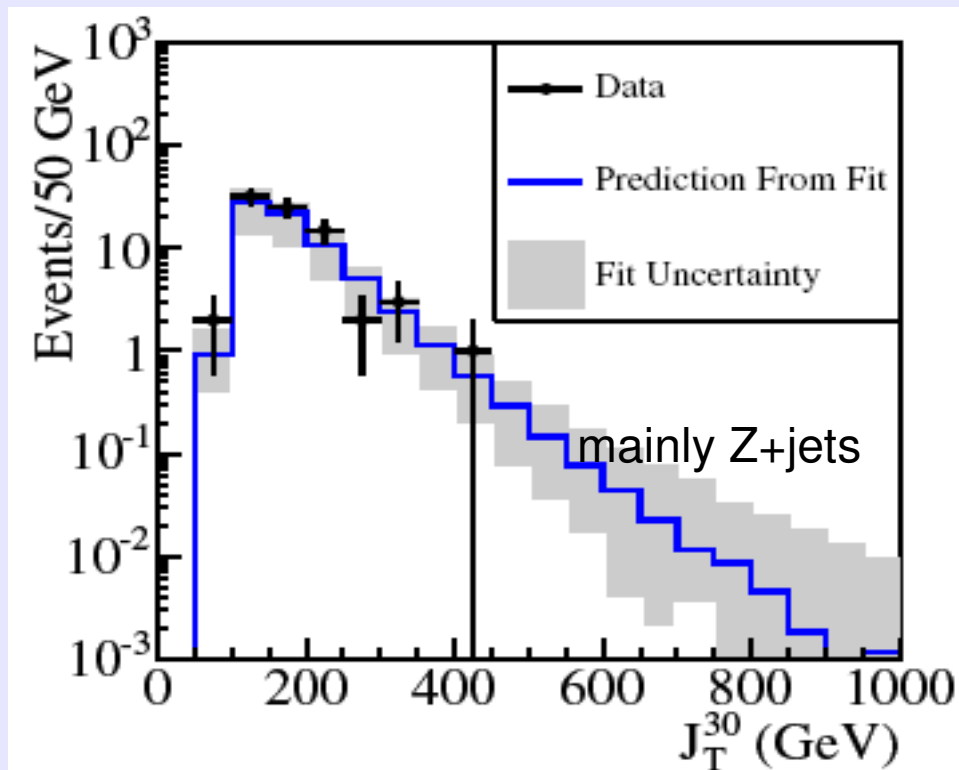
$$p \bar{p} \rightarrow b' \bar{b}', b' (d_4) \rightarrow b + Z$$

assumption:

BF(b'→Z+b)=100% & prompt b' decay



$$Z \rightarrow e^+ e^-, \mu^+ \mu^- \quad N_{jet}^{30} \geq 3 (30 \equiv E_{T,jet} \geq 30 \text{ GeV}) \quad J_T^{30} = \sum_{jets} E_T (E_T > 30 \text{ GeV})$$



2.3 TEVATRON constraint: top-like search

CDF note 9446, 2.8 fb⁻¹

$$p \bar{p} \rightarrow t' \bar{t}' + X, t' \rightarrow W + q, W \rightarrow l \nu, W \rightarrow q \bar{q}$$

Note:

no distinction between
t' and b' possible

$N_{\text{lepton}} = 1$, at least 4 jets with $E_T > 20$ GeV

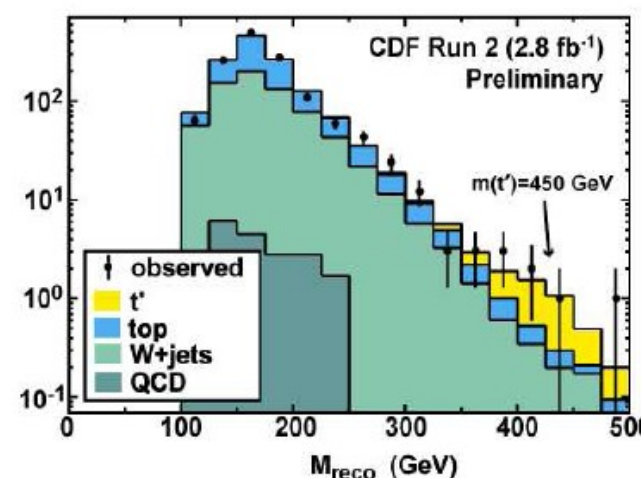
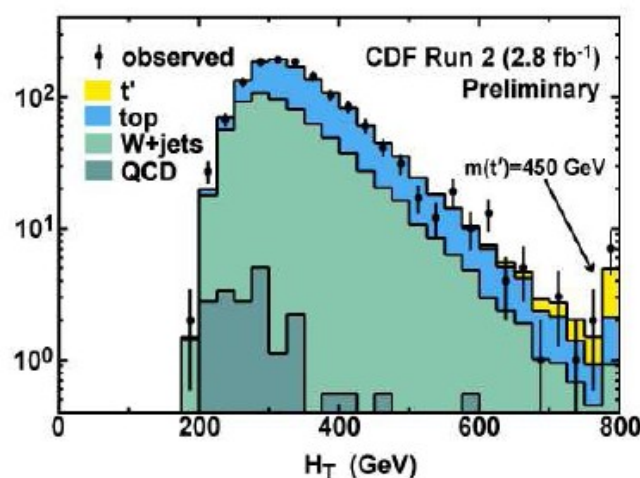
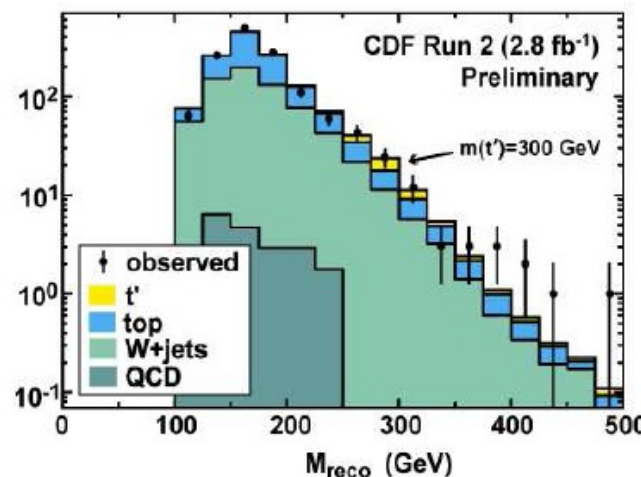
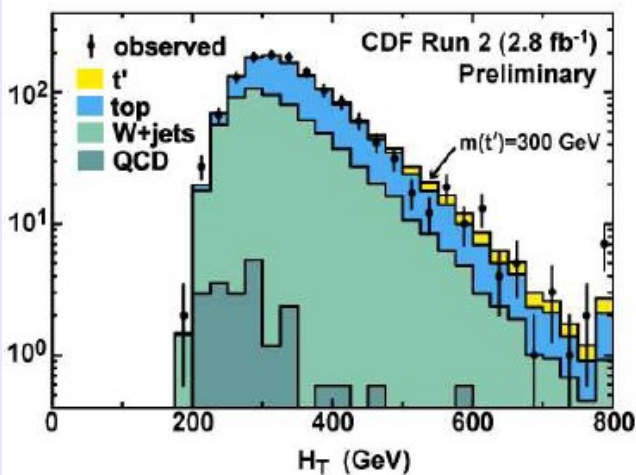
Kinematic fit like in
top reconstruction

No b-tagging

$$M_{\text{reco}} = M_{bjj} = M_{bl\nu}$$

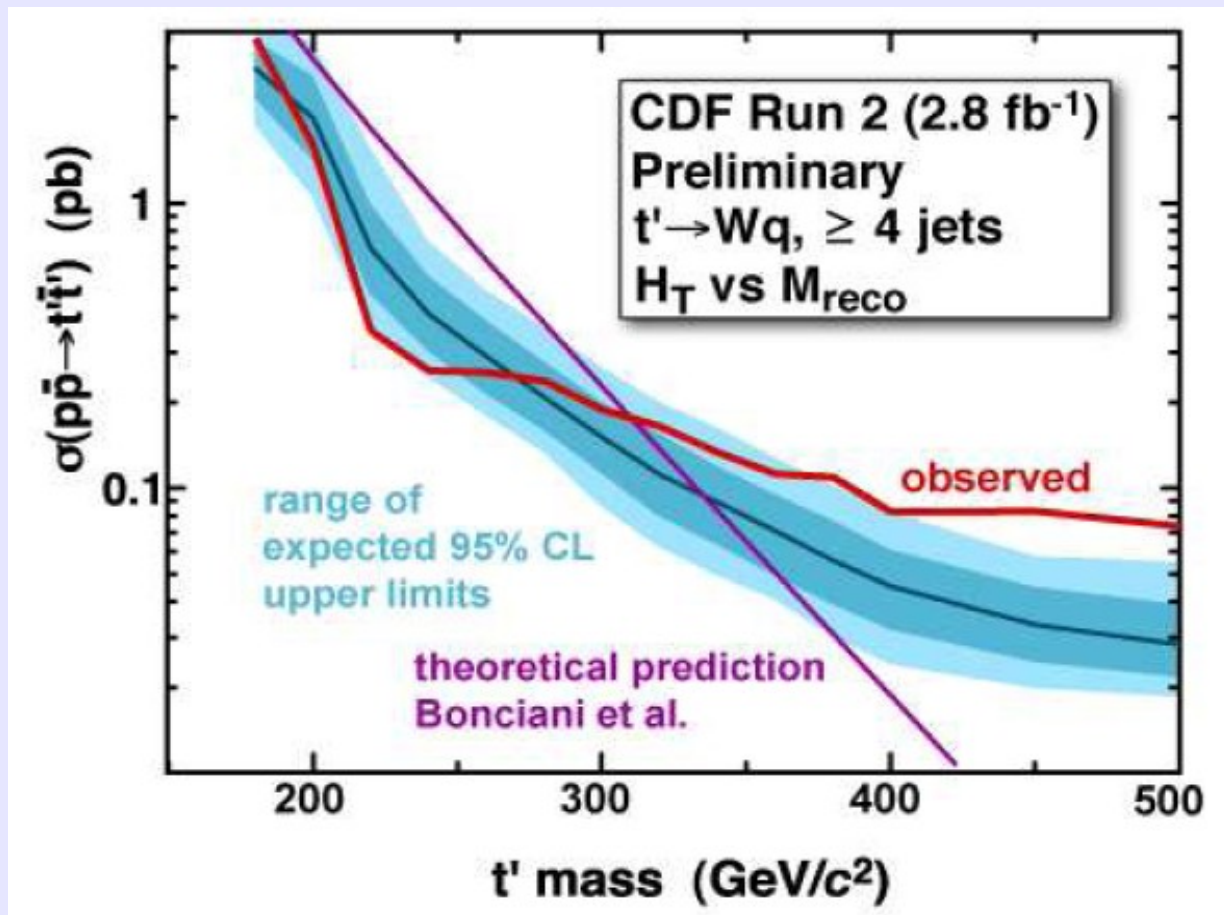
$$H_T = \sum_{\text{jets}} E_T + E_{T,l} + E_{T,\text{miss}}$$

=> Likelihood fit



2.3 TEVATRON constraint: top-like search

- Limit: $m_{t'} > 311 \text{ GeV}$ @ 95% C.L.



- Excess @ 450 GeV?
P-value=0.01 for SM hypothesis
- $\sigma_{\text{observed}} > \sigma_{\text{expected}}$!
- Possibilities for excess:
 - * fluctuation
 - * badly understood SM BG
 - * NP signal:
 - a) no 4th gen. quark
 - b) 4th gen.: contributions from t' and b' decays ?

- Caveat: exclusion limit assumes
 - a) final state BF of 100% => mass limit could be lower
 - b) short lifetime => no limit for very small CKM elements

2.4 TEVATRON constraint: same-sign dilepton

In many mass/CKM scenarios: $p \bar{p} \rightarrow b' \bar{b}' + X$, $b' \rightarrow W + t (\rightarrow b + W)$

Striking search scenario: same-sign dilepton final state + high jet multiplicity

CDF, note 9759, 2.7 fb⁻¹:

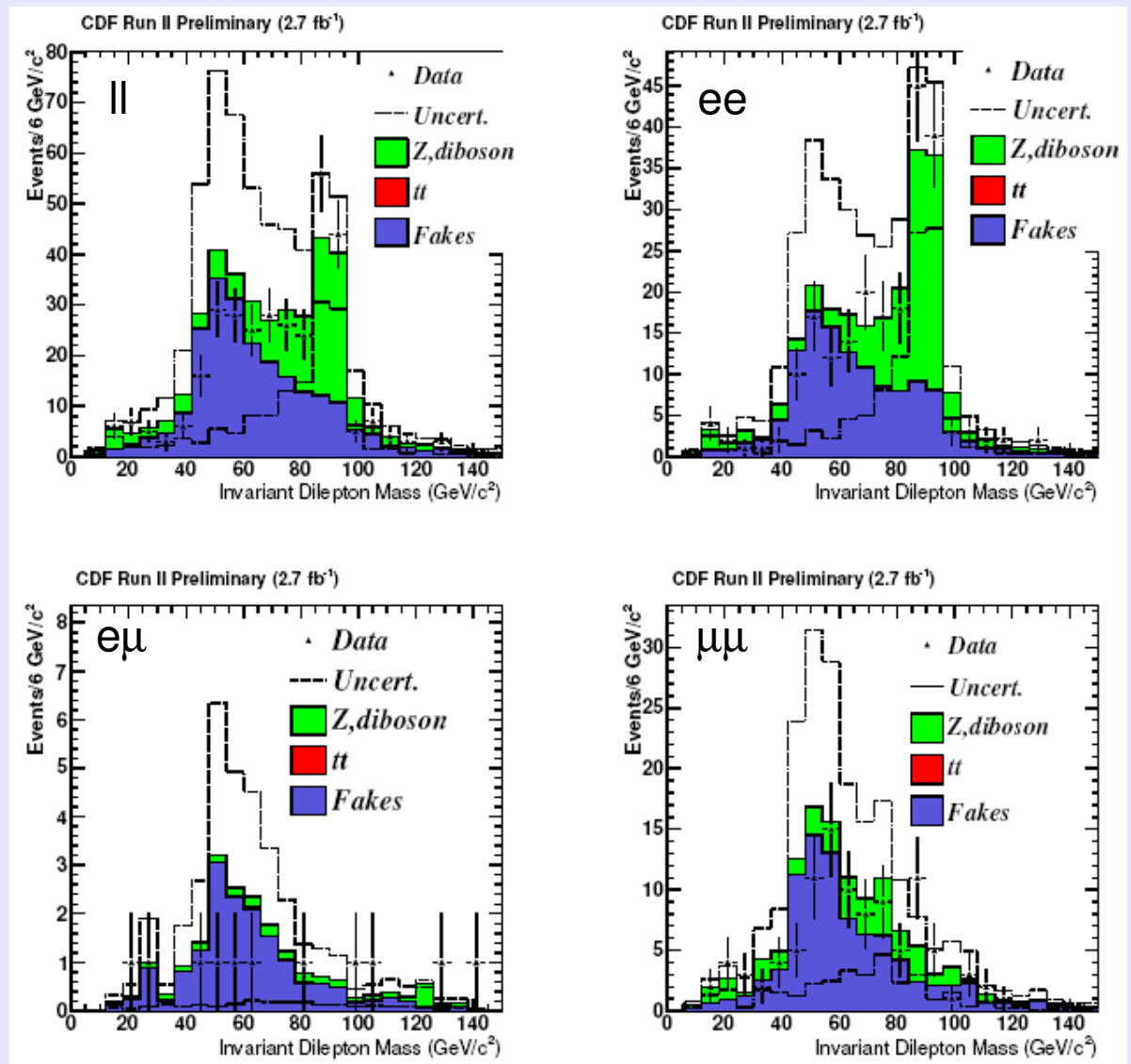
same-sign dilepton
invariant mass

- Fakes: mainly W+jets

- Z+jets:

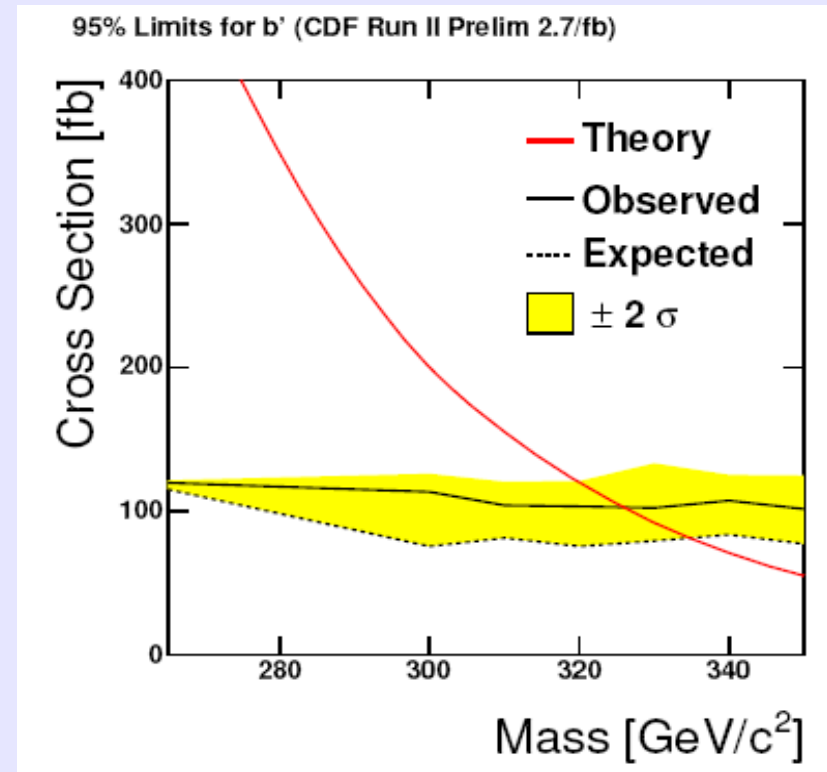
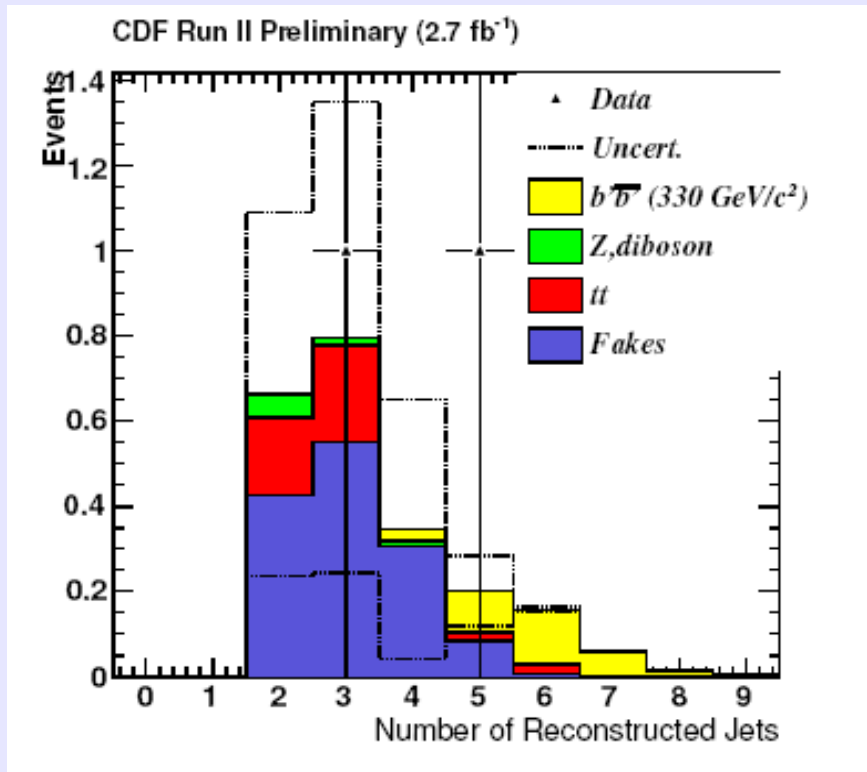
$Z \rightarrow e^+e^-$ with hard bremsstr.
+ asymmetric conversion

$\gamma \rightarrow e^+e^-$



2.4 TEVATRON constraint: same-sign dilepton

Extraction method: likelihood fit in jet multiplicity



Usual caveat: CDF assumes $\text{BF}(b' \rightarrow W+t)=100\%$ & prompt b' decay

2.5 TEVATRON constraints: assumptions

The following is based on Hung & Sher, PRD77, 037302 (2008)

$t' \rightarrow W + q$: CDF assumes $\text{BF}(t' \rightarrow W+q)=100\%$ & prompt t' decay

$m_{t'} - m_{b'} > m_W$: $\text{BF}(t' \rightarrow W+b')$ dominant $\Rightarrow \text{BF}(t' \rightarrow W+q)$ small

$0 < m_{t'} - m_{b'} < m_W$: $t' \rightarrow W^* + b'$ can still dominate for small $V_{t'q}$

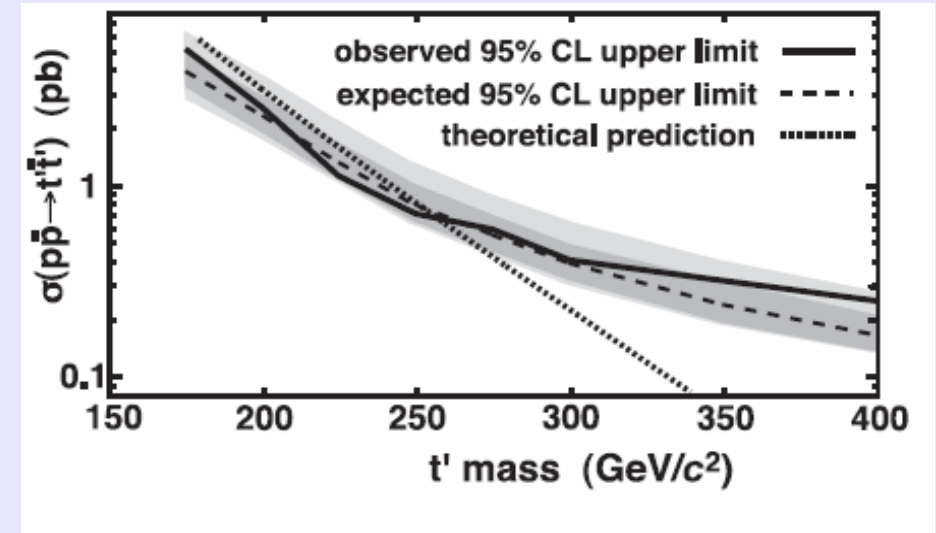
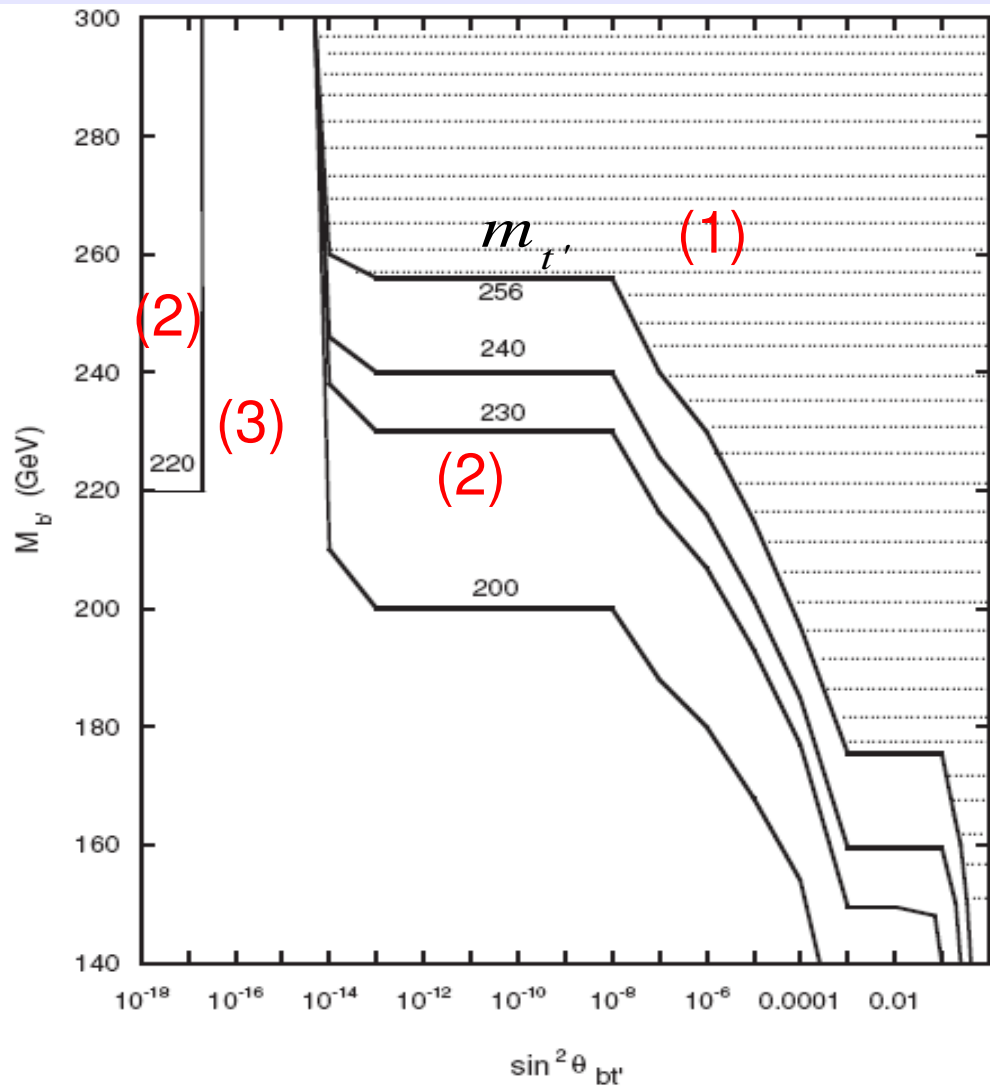
$m_{t'} - m_{b'} < 0$: $\tau_{t'}$ could be so small (for tiny $V_{t'q}$) that quark could transverse cm-m before decaying (stable quark searches exclude more than ~ 3 m)

$\Rightarrow$ Constraint dependent on $m_{b'}$ and $V_{t'q}$

2.5 TEVATRON constraints: assumptions

First CDF result (760 pb⁻¹), PRL 100, 161803 (2008): $m_{t'} > 256$ GeV, 95% CL

Hung & Sher, PRD77, 037302 (2008):

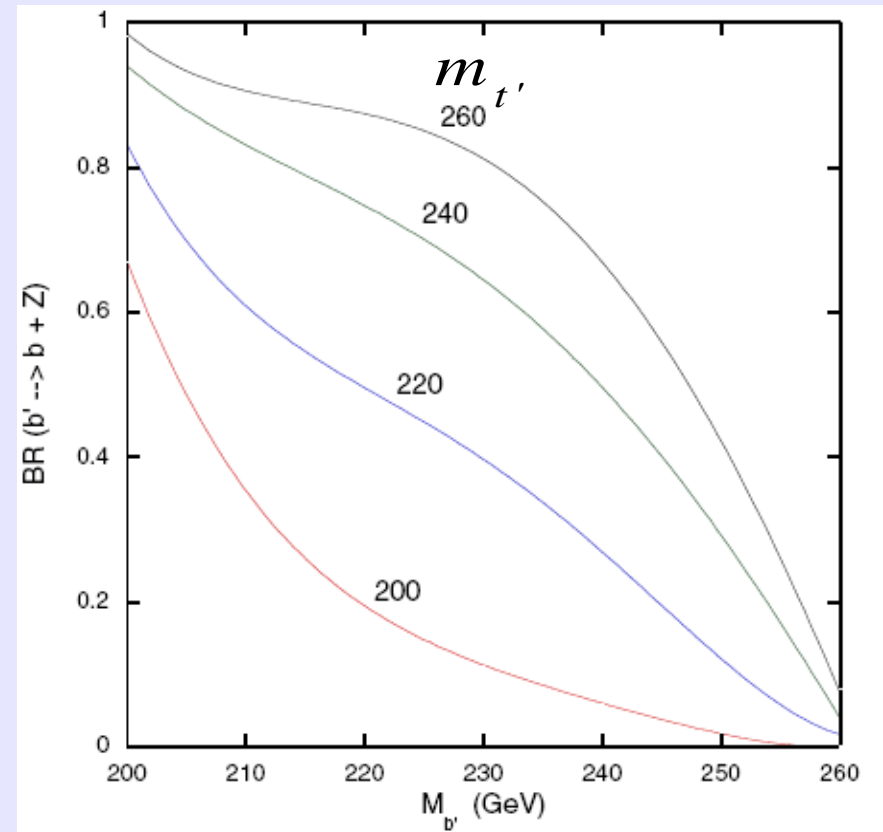
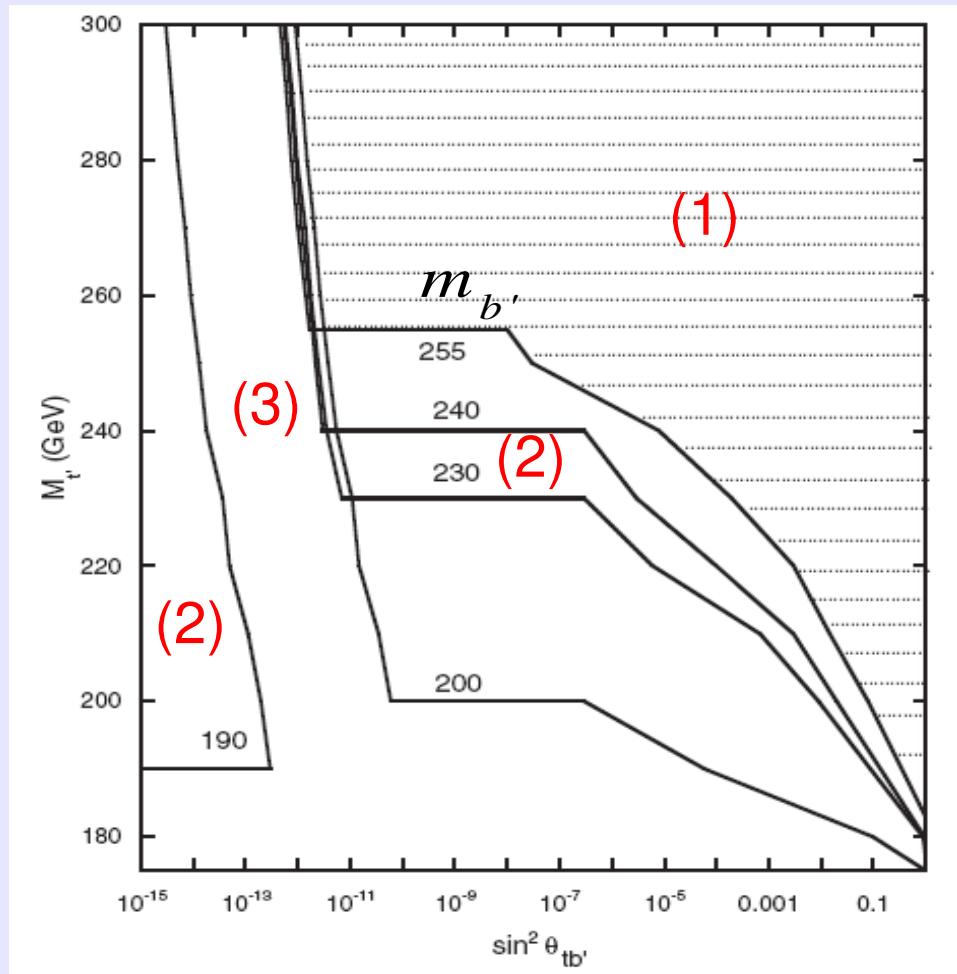


- (1) Region where CDF limit applies
- (2) Region where a smaller mass limit is obtained requiring $\text{BF}(t' \rightarrow W+q)$ still being dominant
- (3) lifetime region: no mass limit

2.5 TEVATRON constraints: assumptions

CDF (1.06 fb⁻¹), PRD 76, 072006 (2007): $p \bar{p} \rightarrow b' \bar{b}', b' (d_4) \rightarrow b + Z$
 $m_{b'} > 268 \text{ GeV @ 95\% CL}$

Hung & Sher, PRD77, 037302 (2008):

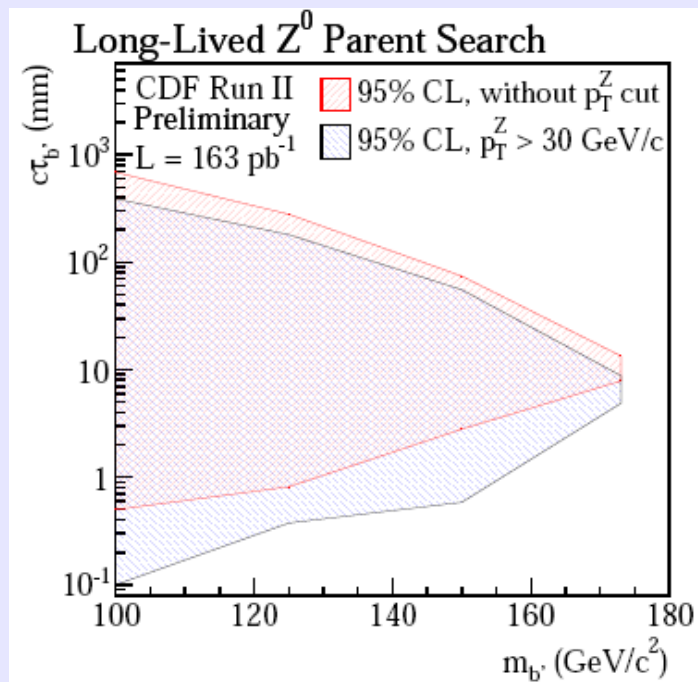
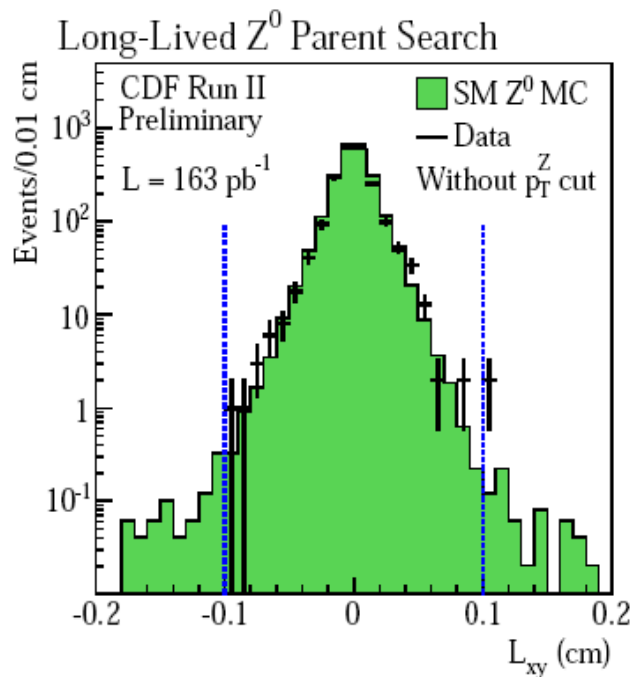
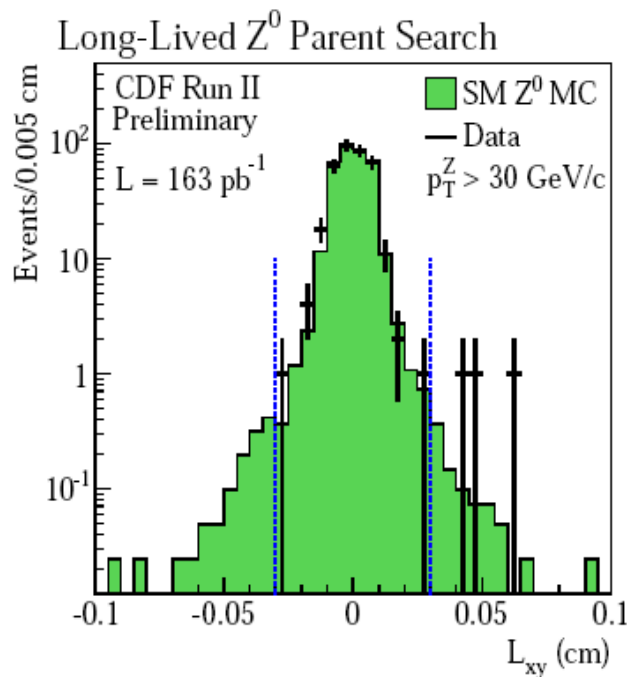


$\text{BF}(b' \rightarrow Z + b) = 100\%$ for
 $m_{b'} > 255 \text{ GeV}$ never met:

$b' \rightarrow W + t$ threshold opens

2.5 TEVATRON constraints: long-lived b'

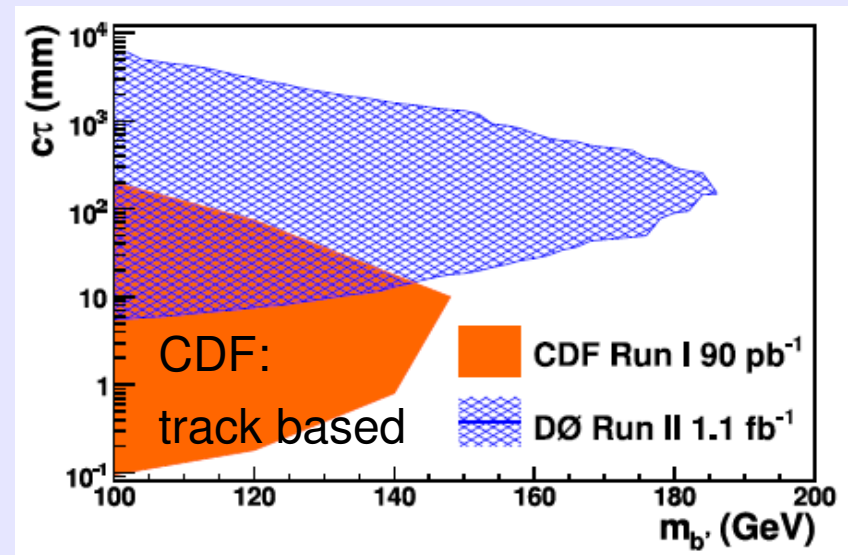
CDF note 7244 (163 pb⁻¹): $b' \rightarrow Z + b$



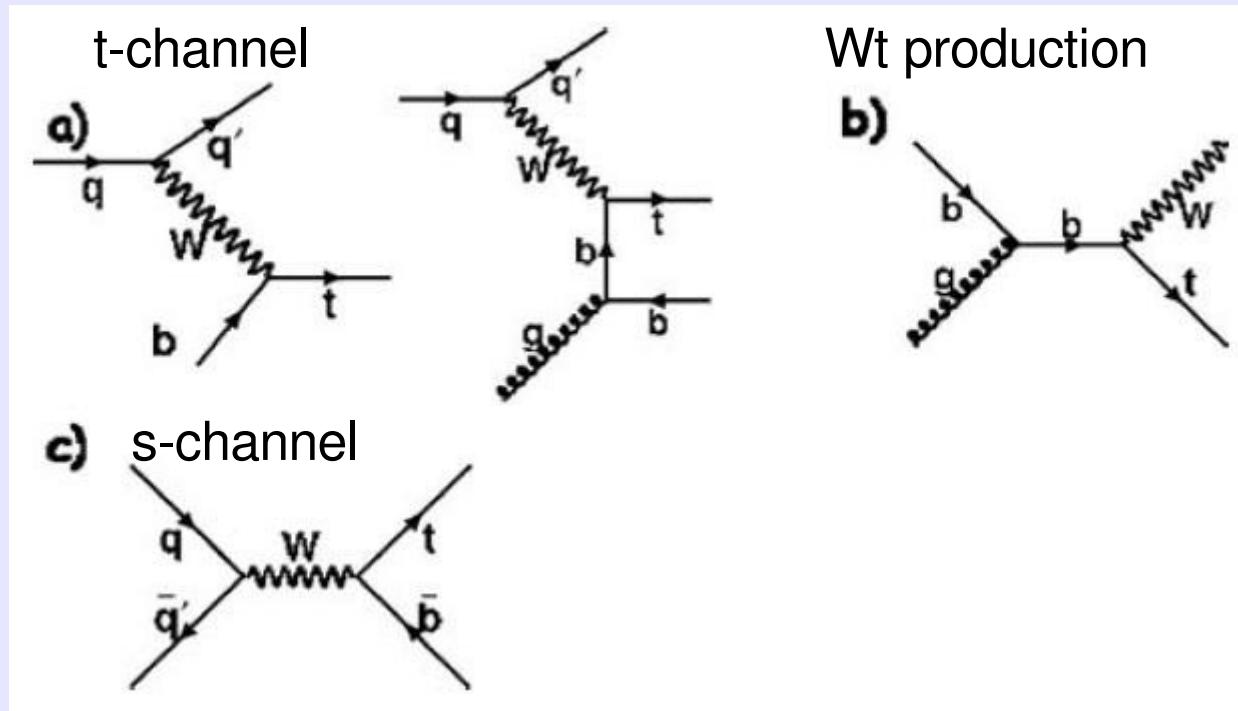
D0, PRL 101, 111802 (2008) with 1.1 fb⁻¹

$b' \rightarrow Z + b$

Search channel: $Z \rightarrow e^+ e^- + X$



3.1 Effects of a 4th generation on Single Top production



Gives direct info on $|V_{tb}|$

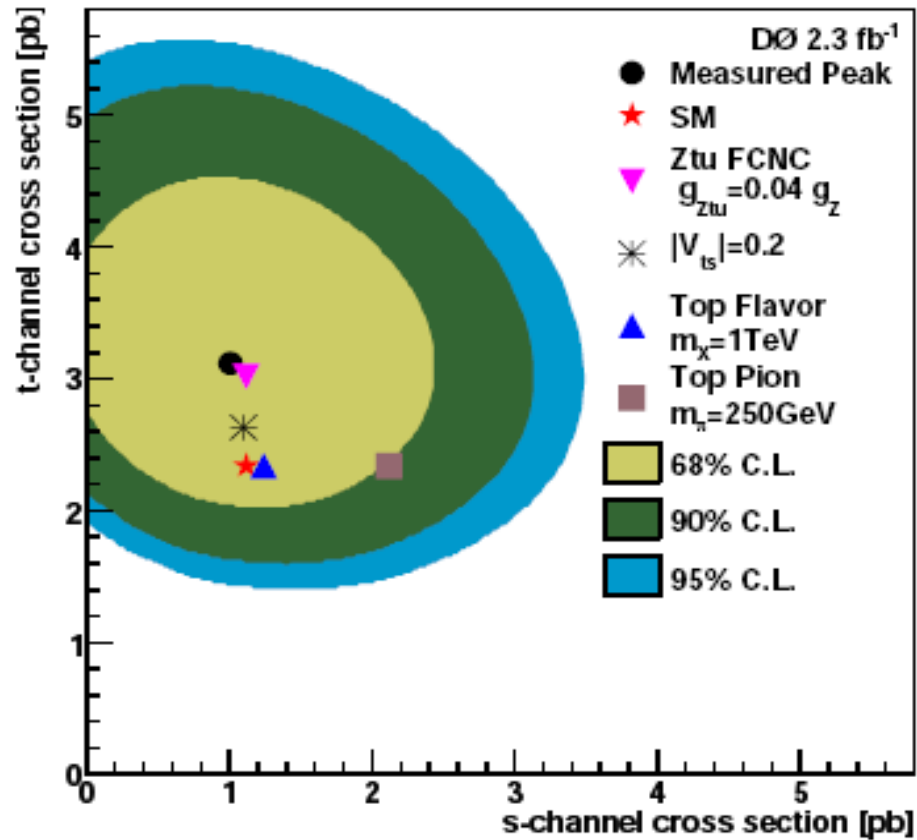
If $\sigma_{\text{meas}} \neq \sigma_{\text{theo}}$:

$|V_{tb}| < 1$ ($\Rightarrow$ 4th gen.)

or other NP

	t -channel	Wt production	s -channel
TEVATRON($\sqrt{s} = 1.8$ TeV, $p\bar{p}$)	1.98 ± 0.30 pb [149, 161]	≈ 0 pb	0.88 ± 0.14 pb [149, 161]
LHC ($\sqrt{s} = 14$ TeV, pp)	245 ± 27 pb [161, 162]	$62.2^{+16.6}_{-3.7}$ pb [145]	10.2 ± 0.7 pb [144, 161]

3.1 Effects of a 4th generation on Single Top production

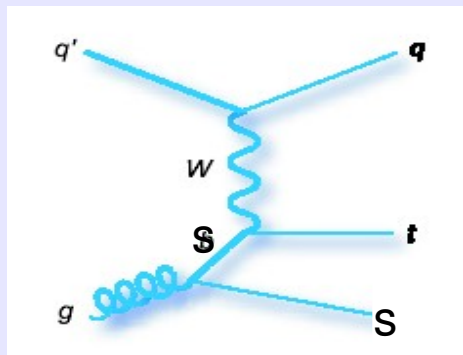


$$\sigma_{\text{SingleTop}} \sim |V_{tb}|^2 \text{ in } N_{\text{gen}}=3\text{-SM}$$

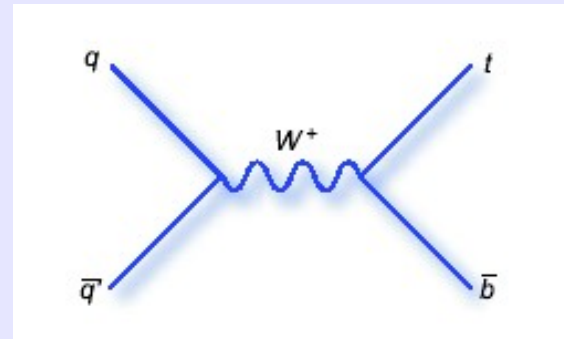
Nonetheless, it is possible to have:

$$\sigma_{\text{SingleTop}}(N_{\text{gen}}=4) > \sigma_{\text{SingleTop}}(N_{\text{gen}}=3)$$

although $|V_{tb}| < 1$ if e.g. $|V_{ts}|$ is sizeable

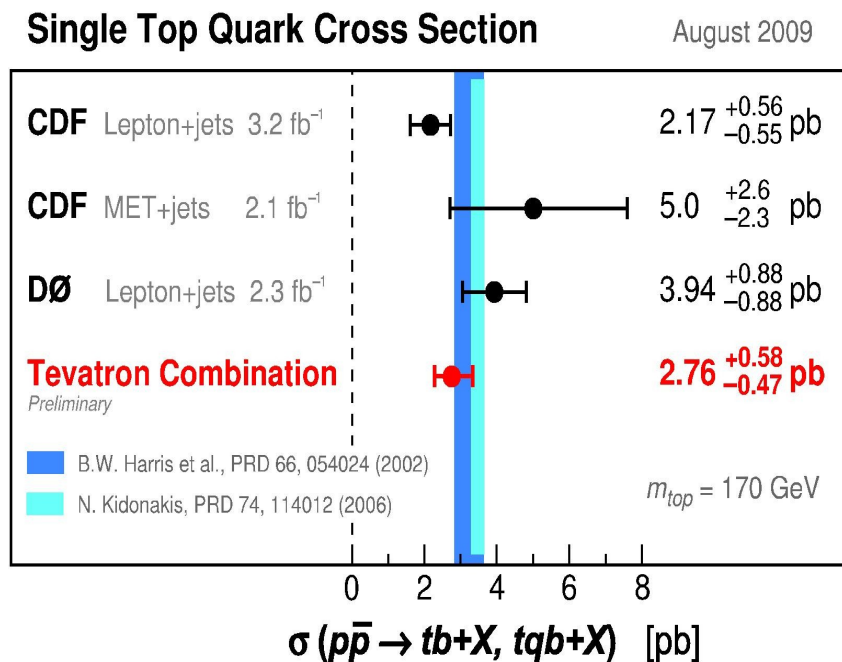


t-channel enhanced
PDF(s) >> PDF(b)



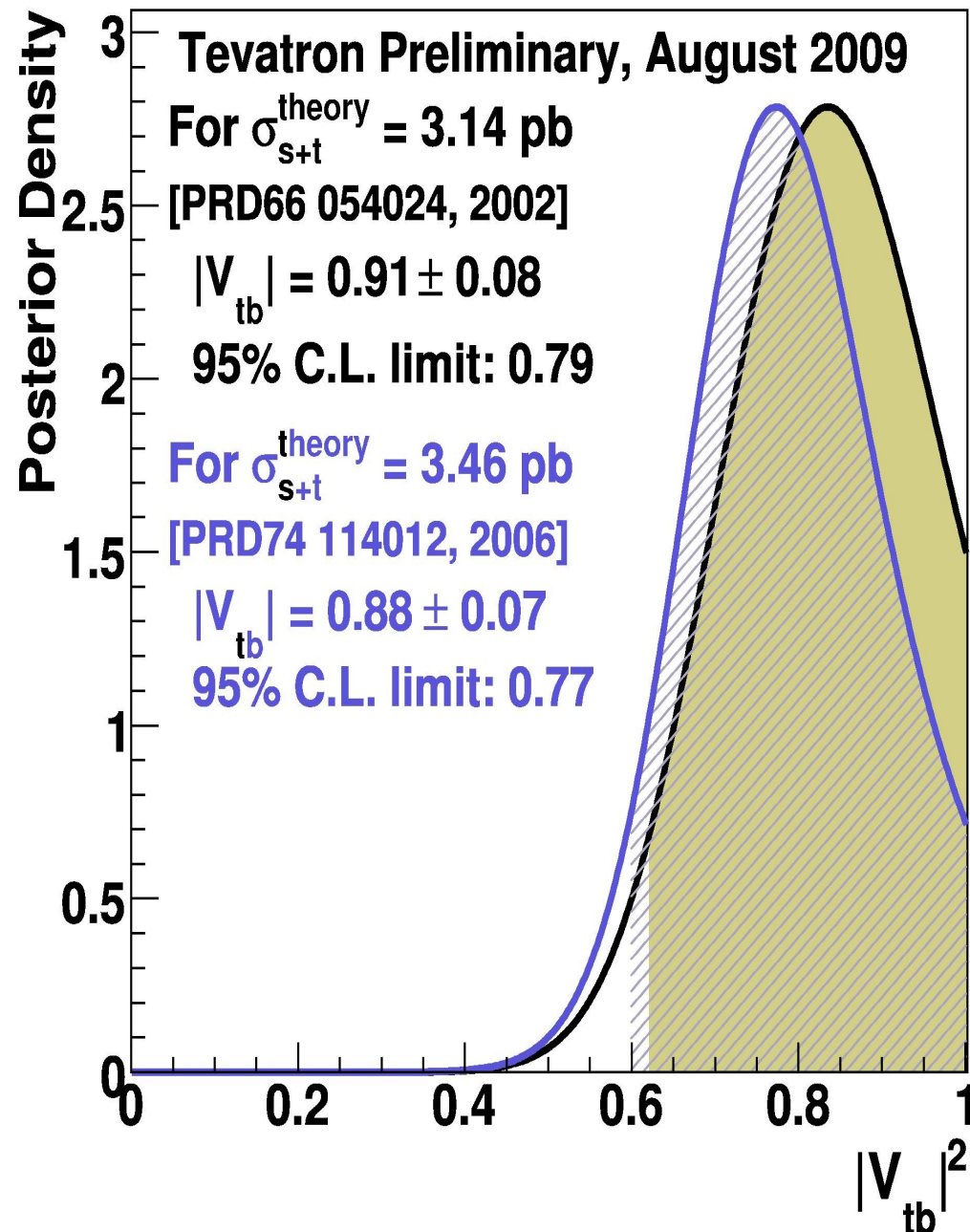
s-channel suppressed: $|V_{tb}| < 1$

3.1 Effects of a 4th generation on Single Top production



D0: 0903.0850 [hep-ex]

CDF: 0903.0885 [hep-ex]



3.1 Effects of a 4th generation on Single Top production

- Final remark: Cross section measurement, respectively, extraction of $|V_{tb}|$ assumes $t \rightarrow Wb$ to be dominant ($\rightarrow$ b-tagging)

- Relevant branching ratio:
$$R = \frac{\Gamma(t \rightarrow W + b)}{\Gamma(t \rightarrow W + q)} = \frac{|V_{tb}|^2}{|V_{td}|^2 + |V_{ts}|^2 + |V_{tb}|^2}$$

determined in $t\bar{t}$ events by measuring 0, 1, ≥ 2 tagged b-jet rates

BF($t \rightarrow Wb$) dominant fulfilled in $N_{\text{gen}}=3$ -SM: $|V_{tb}| = 0.999142^{+0.000021}_{-0.000014}$ (CKMfitter)

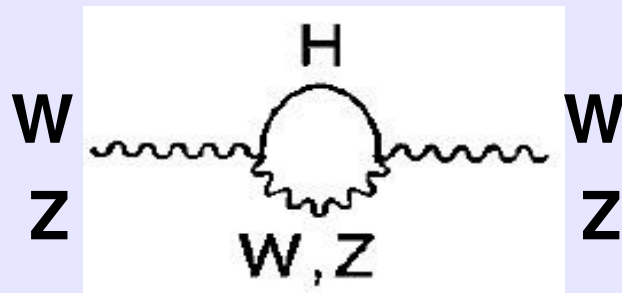
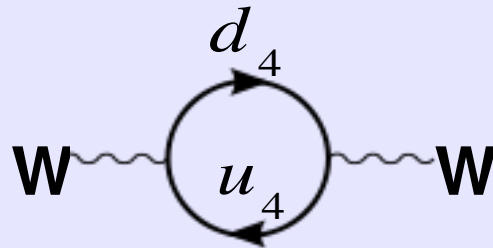
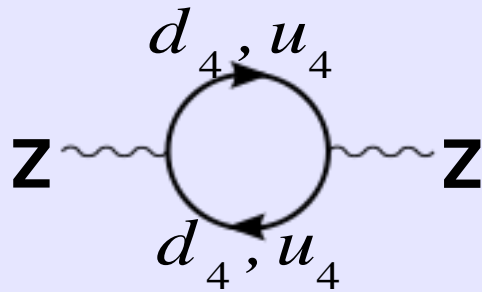
- However, best measurement by D0: $R = 0.97^{+0.09}_{+0.08}$

- Most often not taken into account $\Rightarrow$ Single top: $|V_{tb}| \frac{|V_{tb}|}{\sqrt{|V_{td}|^2 + |V_{ts}|^2 + |V_{tb}|^2}}$

It's even more involved (pdf effect!) $\rightarrow$ see F. Maltoni's talk

4. Mass splitting within a 4. Generation

Self-energy diagrams:



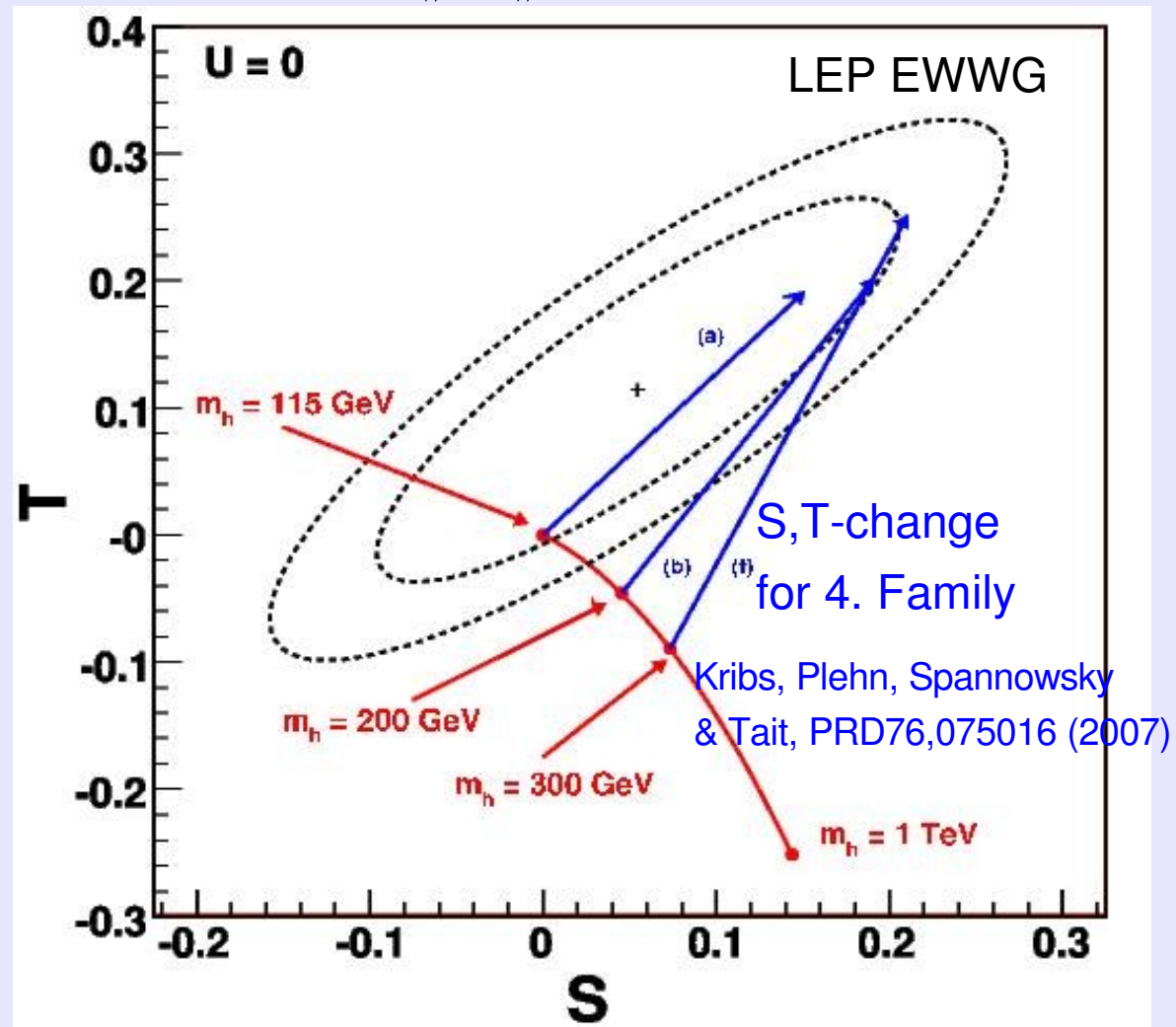
Four Generations:

$M_{\text{Higgs}} \sim 600 \text{ GeV}$ possible

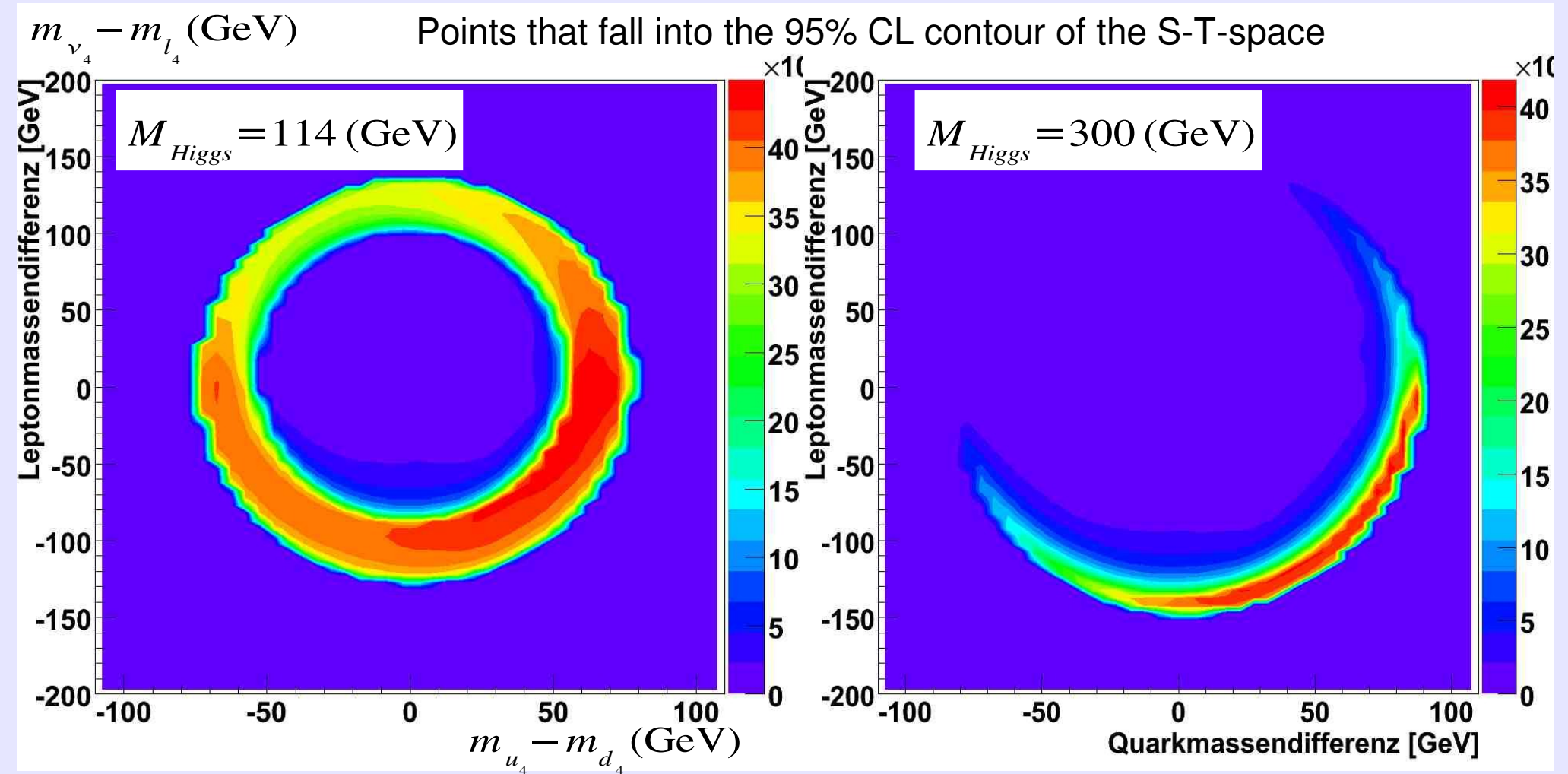
$$S = \frac{1}{6\pi} \left(1 - 2Y \ln \frac{m_{l_4}^2}{m_{\nu_4}^2} \right) + \frac{N_c}{6\pi} \left(1 - 2Y \ln \frac{m_{u_4}^2}{m_{d_4}^2} \right)$$

$$Y = 1/6 (\text{quarks}), -1/2 (\text{leptons})$$

$$T = \frac{1}{12\pi \sin^2 \theta_W M_W^2} \left(N_c \left| m_{u_4}^2 - m_{d_4}^2 \right| + \left| m_{l_4}^2 - m_{\nu_4}^2 \right| \right)$$



4. Mass splitting within a 4. Generation



- $m(u_4) > m(d_4)$ preferred but opposite not excluded, $m(u_4) - m(d_4) > M_W$ not excluded
- $m(l_4) > m(\nu_4)$ preferred but opposite not excluded

(Study done by HUB bachelor students based on code from Kribs et al.

Thanks for the support provided by T. Plehn and M. Spannowsky)

5. What do we know about the CKM & PMNS matrix elements?

- Recent discussion of constraints on 4x4 CKM- & PMNS-elements:

1. Kribs et al., PRD76, 075016, 2007 ---> See talk by T. Plehn

CKM: CKM-Treelevel + W-decays + D-mixing

PMNS: $\mu \rightarrow e\gamma$, $\mu \rightarrow e$ conversion

2. Bobrowski et al., PRD79, 113006, 2009

CKM-Treelevel + K-, D-, B-mixing & $b \rightarrow s\gamma$ ---> See talk by A. Lenz

3. Chanowitz, PRD79, 113008 (2009)

e.w. precision fit: taking into account CKM elements in T

Caveat: All studies here assume lepton universality and, implicitly,

$U_{E4}=1$ in all observables and also in the e.w. precision fit.

In presence of a 4th generation: maybe not justified

5.1 Mixing in quark sector

Directly measured
matrix elements:

at $\sim 2\sigma$

$$|V_{CKM}^{4 \times 4}| = \begin{pmatrix} 0.97418 & 0.2246 & 0.0039 & < 0.038 \\ 0.22 & > 0.84 & 0.041 & < 0.51 \\ < 0.06 & < 0.26 & > 0.78 & < 0.62 \\ < 0.105 & < 0.51 & < 0.62 & > 0.74 \end{pmatrix} \quad \text{my numbers}$$

- Limiting factors:

$$* |V_{tb}| \text{ from single top} + R = \frac{\Gamma(t \rightarrow W + b)}{\Gamma(t \rightarrow W + q)} = \frac{|V_{tb}|^2}{|V_{td}|^2 + |V_{ts}|^2 + |V_{tb}|^2} \quad \text{not well constrained yet}$$

(Please note: $|V_{tb}|$ constraint does not take into account R info)

- * $|V_{cs}|$ from semileptonic D-decays: still large theoretical error

(form factor, decay constant)

5.1 Mixing in quark sector

Directly measured
matrix elements:

$$|V_{CKM}^{4 \times 4}| = \begin{pmatrix} 0.97418 & 0.2246 & 0.0039 & < 0.038 \\ 0.22 & > 0.84 & 0.041 & < 0.51 \\ < 0.06 & < 0.26 & > 0.78 & < 0.62 \\ < 0.105 & < 0.51 & < 0.62 & > 0.74 \end{pmatrix} \quad \text{my numbers}$$

- Constraints discussed by Kribs et al. (my numbers):

* $|V_{tb}|$

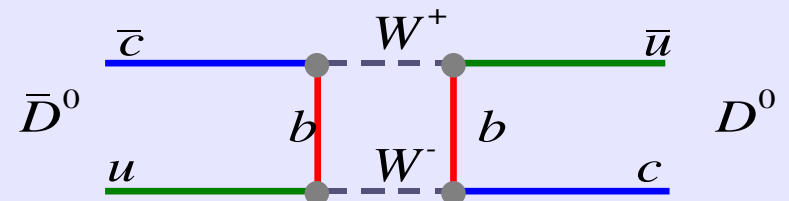
* $\Gamma(W \rightarrow \text{had})$

$$|V_{CKM}^{4 \times 4}| = \begin{pmatrix} 0.97418 & 0.2246 & 0.0039 & < 0.038 \\ 0.22 & 0.97 & 0.041 & < 0.2 \\ < 0.04 & < 0.125 & > 0.78 & < 0.62 \\ < 0.07 & < 0.20 & < 0.62 & > 0.78 \end{pmatrix}$$

* D-mixing (Golowich et al., PRD76:095009, 2007) $\rightarrow |V_{ud_4} V_{cd_4}^*| < 0.002$

Limit depends on d_4 mass (200 GeV used)

See talk by A. Lenz concerning
uncertainties in predicting D-mixing



5.2 Constraint from W-decays

* BF(W→had) used by Kribs et al. calculated from measured BF(W → l ν) !

$$W^+ \begin{array}{l} \swarrow \\ l^+ u \quad c \\ \searrow \\ \nu_l \quad \bar{d}' \quad \bar{s}' \end{array} \quad \frac{\Gamma(W \rightarrow l \nu)}{\Gamma(W \rightarrow All)} \approx \frac{1}{3 + 3 \sum_{i=u,c} \sum_{j=d,s,b} |V_{ij}|^2 (1 + \alpha_s(M_W)/\pi)}$$

* Unitarity check in the first place

* N_{gen} > 3: Strengthen constraint on |V_{cs}| and, consequently, on |V_{ts}|, |V_{t's}| and |V_{cb}| !

* Consistent with 3x3-Unitarity: $\sum_{j=d,s,b} |V_{uj}|^2 + \sum_{j=d,s,b} |V_{cj}|^2 = 2.002 \pm 0.027$

* However: formula assumes lepton universality

N_{gen} = 4: lepton universality possibly violated

and |U_{l4}| > 0 possible for l = e, μ, τ

$$BF(W \rightarrow e \nu) = 0.1075 \pm 0.0013$$

$$BF(W \rightarrow \mu \nu) = 0.1057 \pm 0.0015$$

$$BF(W \rightarrow \tau \nu) = 0.1125 \pm 0.0020$$

$$\frac{\Gamma(W \rightarrow l \nu)}{\Gamma(W \rightarrow All)} \approx \frac{\sum_{k=1,2,3} |U_{lk}|^2}{\sum_{l=e,\mu,\tau} \sum_{k=1,2,3} |U_{lk}|^2 + 3 \sum_{i=u,c} \sum_{j=d,s,b} |V_{ij}|^2 (1 + \alpha_s(M_W)/\pi)}$$

5.3 Mixing in lepton sector: τ - and μ -decays

Constraints on 4th generation from τ mass & (leptonic) BF's:

* Dova, (Swain & Taylor), NP Proc.Suppl.76:133,1999; (hep-ph/9712383; PRD55:1,1997)

1) Since then: Significant improvements in m_τ & BF measurements

2) Assumption: Only significant mixing between 3rd and 4th family

W/o this assumption:

$$\Gamma(\tau^- \rightarrow l^- \bar{\nu}_l \nu_\tau) \propto G_F^2 \sum_{i=1,2,3} |U_{\tau i}|^2 \sum_{k=1,2,3} |U_{lk}|^2 \quad l=e/\mu$$

$$\Gamma(\tau^- \rightarrow h \nu_\tau) \propto G_F^2 f_h^2 |V_{uj}|^2 \sum_{i=1,2,3} |U_{\tau i}|^2 \quad j=d(\pi)/s(K)$$

$$\Gamma(h^- \rightarrow \mu^- \nu_\mu) \propto G_F^2 f_h^2 |V_{uj}|^2 \sum_{i=1,2,3} |U_{\mu i}|^2 \quad j=d(\pi)/s(K)$$

$$\Gamma(\mu^- \rightarrow e^- \bar{\nu}_e \nu_\mu) \propto G_F^2 \sum_{i=1,2,3} |U_{\mu i}|^2 \sum_{k=1,2,3} |U_{ek}|^2$$

=> No strong constraint any more on G_F => CKM & e.w. precision fit?!

5.4 Combining CKM, PMNS and e.w. precision fit

- $|V_{ud}| = 0.97418 \pm 0.00026$ (superallowed β -decays)

With 4th generation: $\Gamma(\beta\text{-decay}) \propto G_F^2 |V_{ud}|^2 \sum_{k=1,2,3} |U_{ek}|^2$

$$\Gamma(\mu^- \rightarrow e^- \bar{\nu}_e \nu_\mu) \propto G_F^2 \sum_{i=1,2,3} |U_{\mu i}|^2 \sum_{k=1,2,3} |U_{ek}|^2$$

- $|V_{us}|$: 1. Consider separate averages for K_{e3} & $K_{\mu 3} \rightarrow \sum_{i=1,2,3} |U_{\mu i}|^2 / \sum_{k=1,2,3} |U_{ek}|^2$
 2. $K_{\mu 2}/\pi_{\mu 2}$: dependency on lepton sector cancels $\rightarrow |V_{us}|^2 / |V_{ud}|^2$

- Single top and R not affected!

- Possibility to determine G_F by avoiding this problem in leading order:

$$\Gamma(Z \rightarrow l^+ l^-) \propto G_F^2 (3\text{-gen. SM} + \text{Loop Contr. from 4th family})$$

=> Need to combine CKM-, PMNS- and e.w precision fit

Work started @ HU Berlin (A. Menzel & H. Lacker) within CKMfitter

5.5 Theoretical prejudice: U_{E4} how close to 1 ?

Consider e.g. mixing angle θ between 3rd and 4th generation:

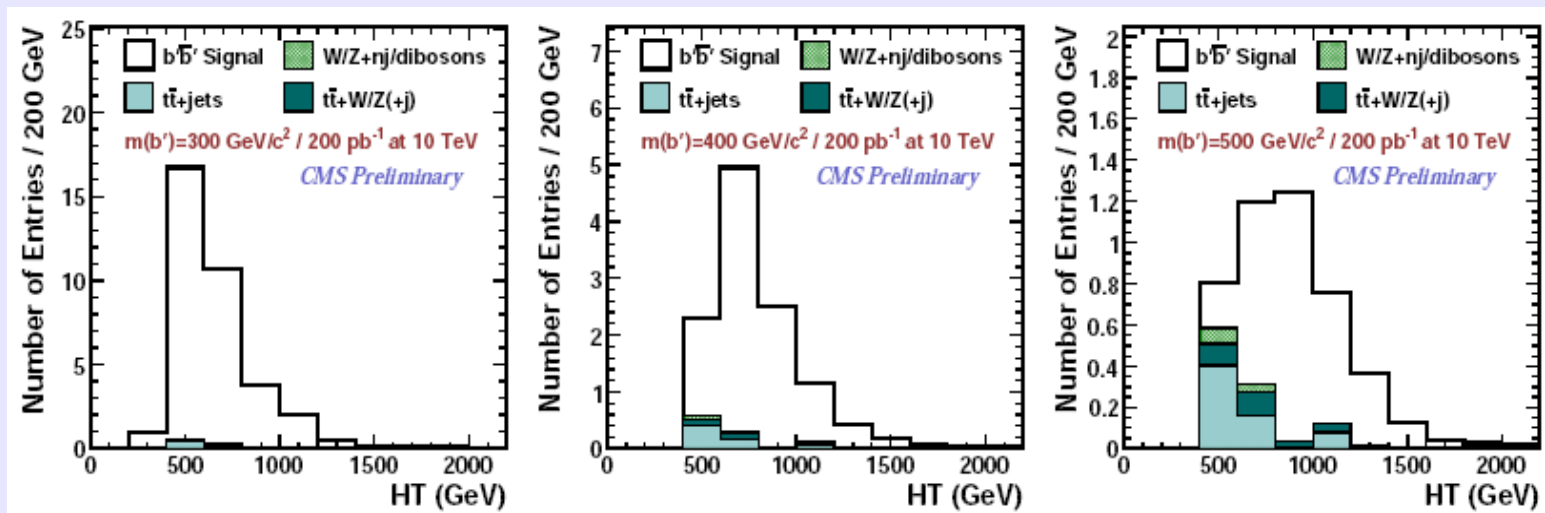
- **Seesaw models** $\rightarrow \sin \theta = \sqrt{m_\tau / m_E} \approx 0.13$
- **Mixing only in neutrino mass matrix** $\rightarrow \sin \theta = \sqrt{m_{\nu_3} / m_{\nu_4}} \approx 5 \times 10^{-6}$
- **Global or discrete family symmetries realized that are broken** $\rightarrow \sin \theta = m_W / m_{Planck} \approx 10^{-17}$
unbroken $\rightarrow \sin \theta = 0$
by Planck scale effects
- **Flavor democracy** $\rightarrow U_{l_4 i} \approx 10^{-5} - 10^{-4}$ ($V_{t'q} \approx 10^{-4} - 10^{-3}$, $V_{qb'} \approx 10^{-4} - 10^{-3}$)
- **Benchmark: $|U_{\mu 4}| \sim 0.023$ corresponds to a $|V_{ud}|$ change of 1σ**

(possible for $\sin \theta_{24} = \sqrt{m_\mu / m_E} \approx 0.03$)

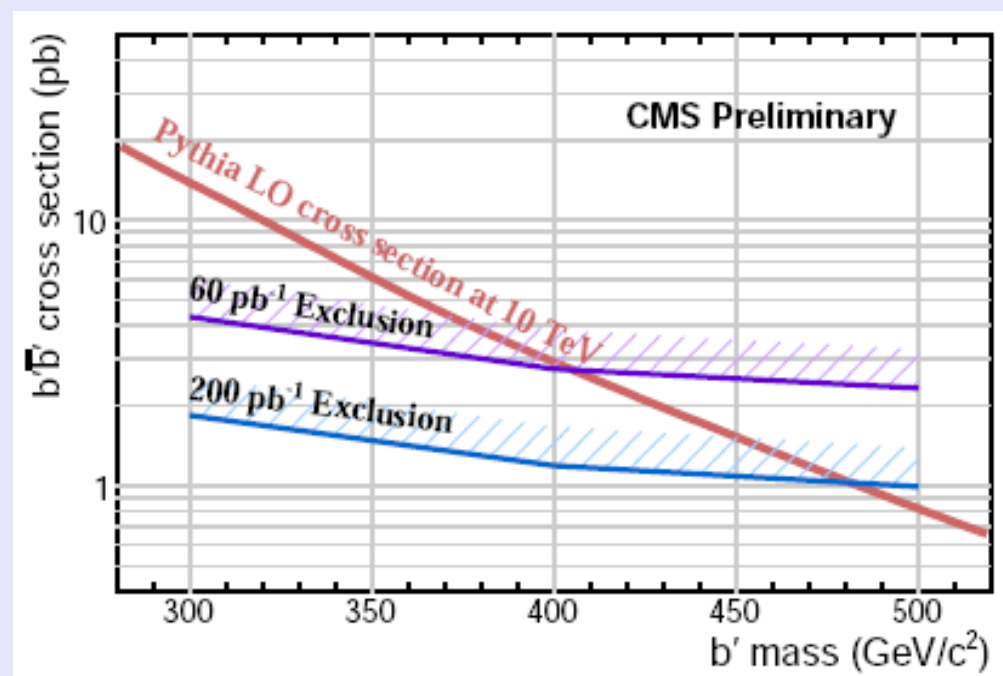
Scenario already excluded? $\frac{g_\tau}{g_\mu} = 0.9976 \pm 0.0022 \stackrel{?}{=} \frac{\cos \theta_{34}}{\cos \theta_{24}} \approx 0.9911$

6.1 Search strategies @ LHC: same-sign dileptons

CMS, PAS EXO-09-012 (200 pb⁻¹, 10 TeV)



Same-sign
dileptons ($N_{\text{jet}} > 3$)
+ trileptons ($N_{\text{jet}} > 1$)



Ideal for searches with early data

Caveat: usual assumptions

Also studied by ATLAS groups
HU Berlin, UCI & SLAC

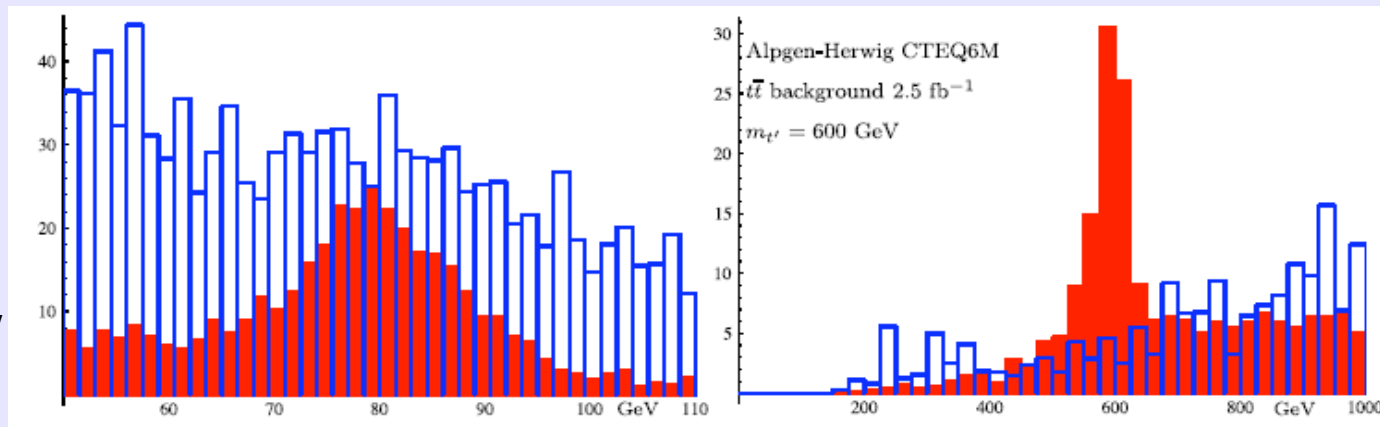
6.2 Search strategies @ LHC: $t' \rightarrow W+q$

- BG: $t\bar{t}$ +jets

Idea: W from t' (b') decays have large boost for high t' (b') masses
jets from hadr. W-decays tend to merge => look for single jet invariant mass

B. Holdom
JHEP 0708,
069 (2007);

Skiba, Tucker-
Smith, hep-ph/
0701247



Understanding
of high- p_T top's?

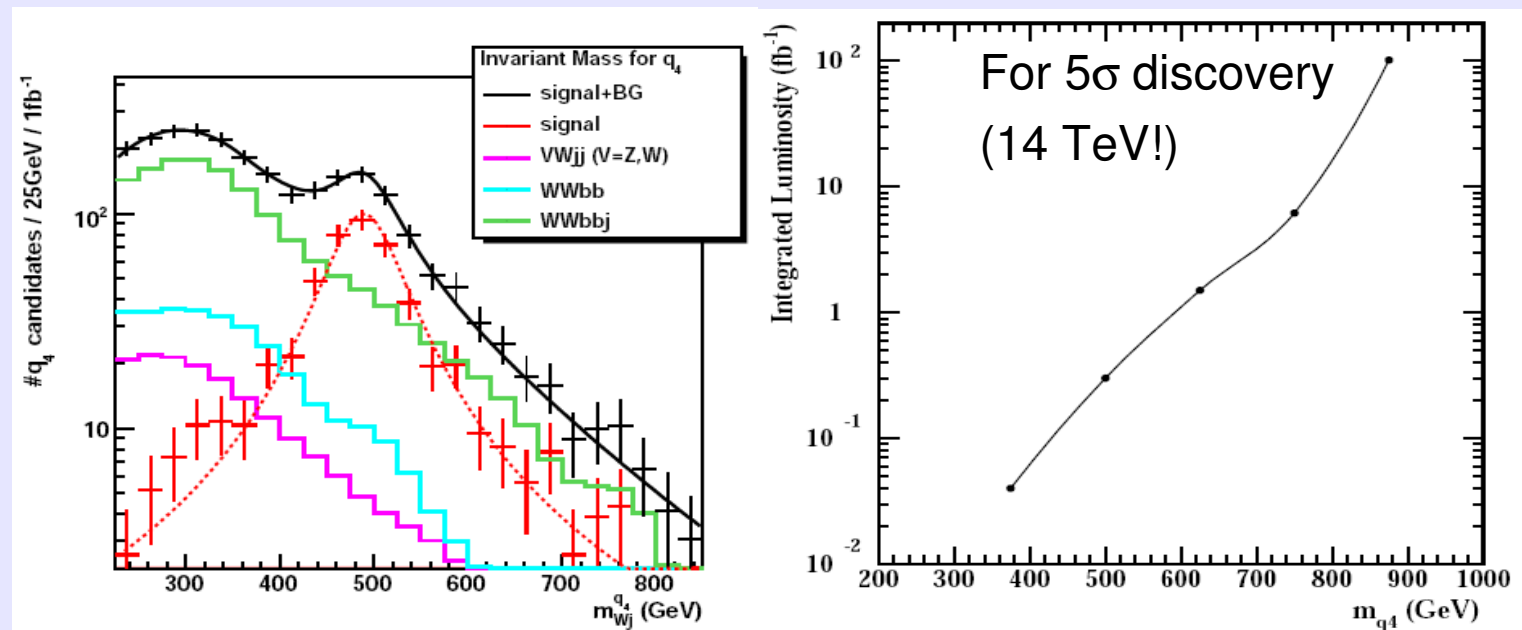
Özcan, Sultansoy and Ünel (ATLAS) EPJ C57, 621 (2008):

Assumption:

primarily mixing with first
two families => $b' \rightarrow W+q$

If not: $t' \rightarrow W+b$

Problem: $BF(t' \rightarrow W+b)$
might be small



7. Summary

1. A 4th generation has several attractive theoretical features:
special role in EWSB, baryogenesis, unification w/o SUSY, ...
2. E.w. prec. fit prefers: small Δm ($\Delta m > m_W$ not excluded)
 $m(u_4) > m(d_4)$, $m(l_4) > m(\nu_4)$ (opposite not excluded)
3. * 3x3 unitarity in lepton sector assumed in all analyses (CKM, ...) so far
* Combined analysis of CKM-, PMNS-, & e.w. precision fit required
4. Current limits depend on assumptions concerning τ /BF's!
=> Correct constraints: functions on masses & mixing angles
5. LHC: * excellent place for discovery 4th ($M \leq 1$ TeV $\rightarrow$ partial wave unitarity)
Complementary search scenarios: $b'(t') \rightarrow W + q(b) \leftrightarrow b' \rightarrow W + t$
* BG-suppression with single jet invariant mass ($\rightarrow$ boosted W's)
(also interesting for other channels)
* Heavy quark with long lifetime searches need more attention