

Report on Tracking Efficiency

Pisa, 2 November 2018

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Outline

- Reminder about Tracking efficiency strategy
- Efficiency estimator Vs. efficiency
- Summary

Measurement Strategy

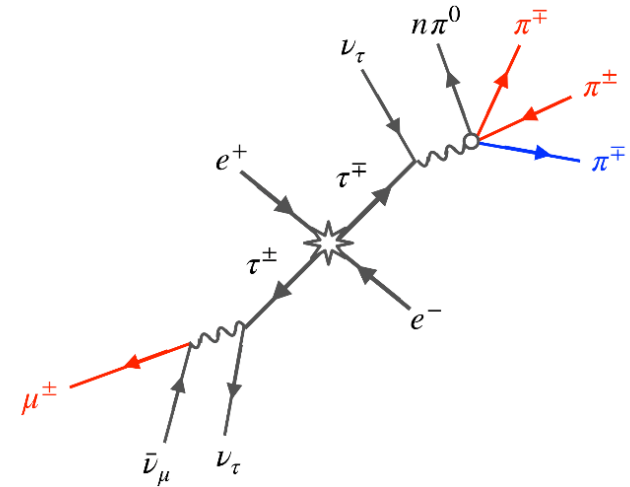
Strategy: exploit charge conservation and kinematic constraints on simple (= with a well recognizable topology) τ -pairs events to deduce the existence of a track.

Reference: “Track finding efficiency in BaBar” <https://arxiv.org/abs/1207.2849>

BaBar strategy was based on *Tau31 events selection*:

- Tracking efficiency, including the detector acceptance, is computed as:
 - $\epsilon \times A = N_4 / (N_3 + N_4)$
 - N_4 = Tau31 events where the 4th track has been found
 - N_3 = Tau31 as reconstructed in the 1+2 selection (further details in the next slide) where the 4th is not found.
- MC-data difference in tracking efficiency is then given by:
 - $\Delta = 1 - \epsilon_{MC} / \epsilon_{data}$
 - With ϵ the tracking efficiency evaluated respectively on MC/data, including the detector acceptance A .

Measurement Strategy: problem with $\varepsilon \times A$ definition



Tag & probe method:

- select events reconstructing one isolated track (consistent with a muon/electron hypothesis \rightarrow *tag side*) + two “good” tracks on the hadronic side (*probe side*)
- Charge conservation implies the 4th track:
 - **FOUND** \rightarrow **N4 ++**
 - **NOT FOUND** \rightarrow **N3 ++**
 - Compute $N4/(N3+N4) = \varepsilon \times A$

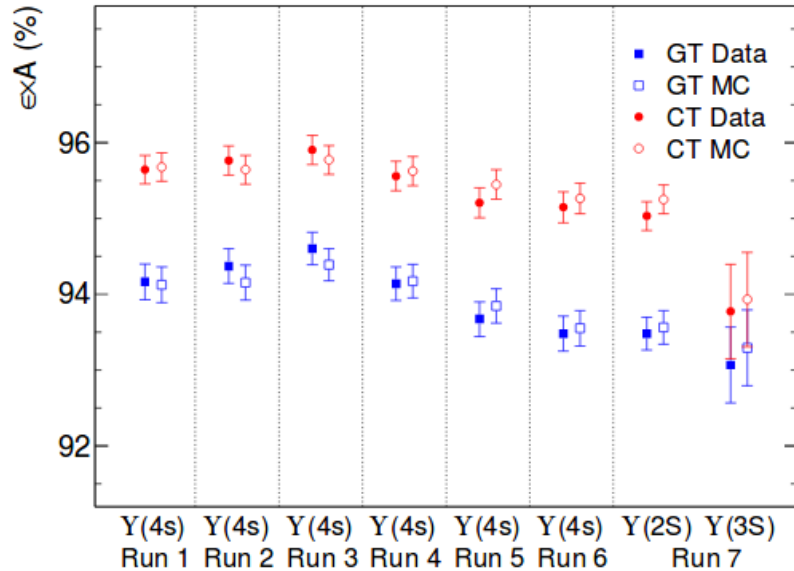
Let's call ε the efficiency to find a track and assume we always have one track on the tag side:

- **N4 = $\varepsilon^3 N \text{ BR}$** (*all 3 tracks on the probe side reconstructed*)
- **N3 = $3 \varepsilon^2 (1-\varepsilon) N \text{ BR}$** (*only 2 out of 3 probe tracks reconstructed \rightarrow binomial variable*)

Measurement Strategy: problem with ϵ_{xA} definition

(II)

<https://arxiv.org/pdf/1207.2849.pdf>



$$\epsilon_{BABAR} \simeq 3\epsilon - 2$$

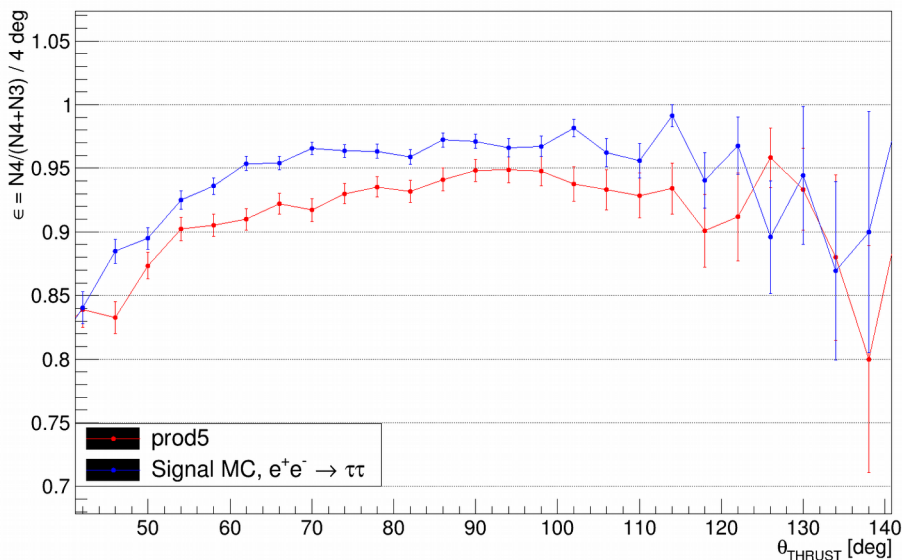
$$\epsilon_{xA} = N4/(N3+N4) = \epsilon_{BABAR}$$

$$\epsilon_{BABAR} = \frac{\epsilon^3}{\epsilon^3 + 3\epsilon^2(1-\epsilon)} = \frac{\epsilon}{3-2\epsilon} = \frac{1-\delta}{1+2\delta} \simeq 1 - 3\delta + o(\delta^2)$$

With δ the probability to loose one track: inefficiency = $1-\epsilon$, and ϵ the real track finding efficiency.

Measurement Strategy: problem with $\epsilon \times A$ definition (III)

Efficiency Vs. θ_{THRUST}



$$\epsilon_{BABAR} \simeq 3\epsilon - 2$$

$$\epsilon_{BelleII} \simeq 2\epsilon - 1$$

$$\epsilon \times A = N4 / (N3 + N4) = \epsilon_{BABAR}$$

$$\epsilon_{BABAR} = \frac{\epsilon^3}{\epsilon^3 + 3\epsilon^2(1-\epsilon)} = \frac{\epsilon}{3-2\epsilon} = \frac{1-\delta}{1+2\delta} \simeq 1 - 3\delta + o(\delta^2)$$

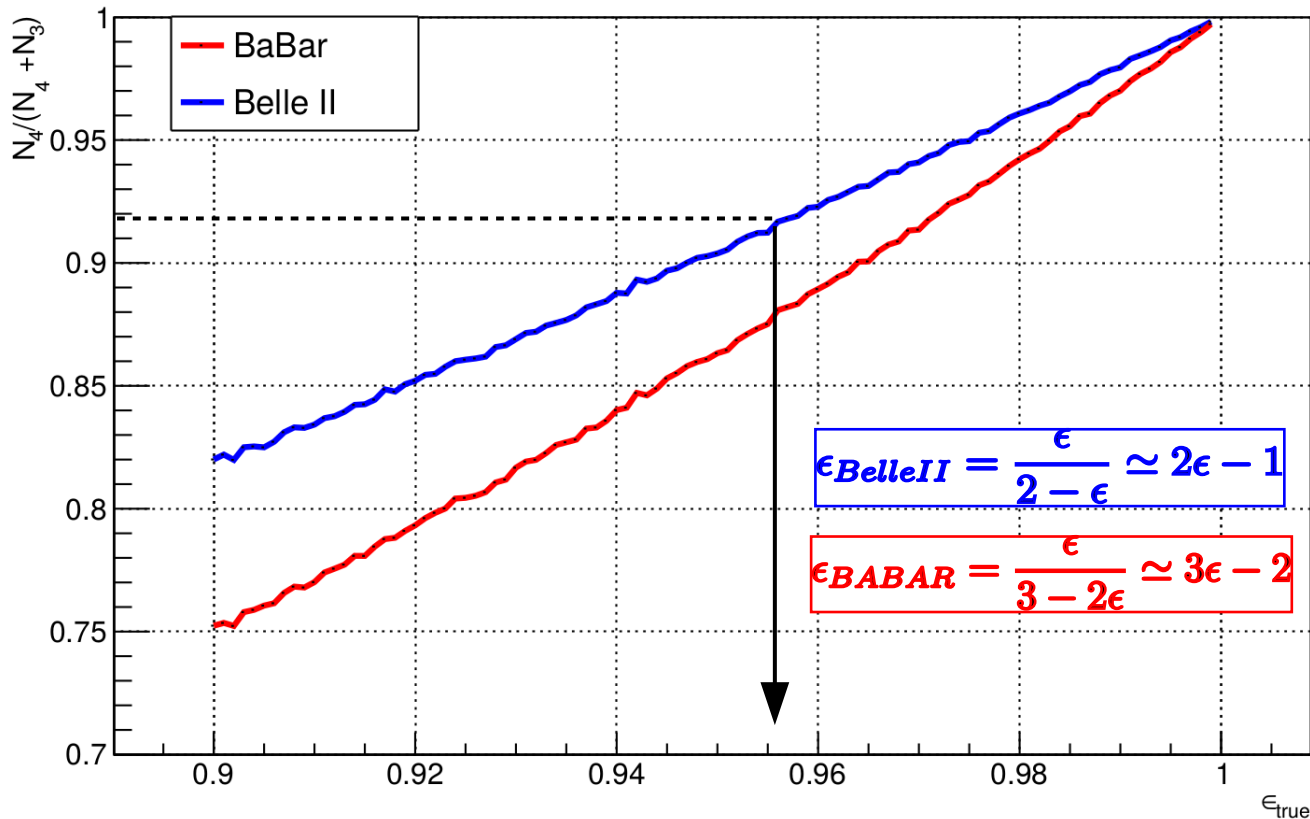
With δ the probability to loose one track: inefficiency = $1-\epsilon$, and ϵ the real track finding efficiency.

For the Belle II case:

- currently we reconstruct only the “opposite” sign case, so $N3 = 2\epsilon^2$ ($1-\epsilon$)N BR (2 remaining tracks with *same sign* out of the 3 \rightarrow event not reconstructed)

$$\epsilon_{BelleII} = \frac{\epsilon^3}{\epsilon^3 + 2\epsilon^2(1-\epsilon)} = \frac{\epsilon}{2-\epsilon} = \frac{1-\delta}{1+\delta} \simeq 1 - 2\delta + o(\delta^2)$$

Toy MC: $N_4/(N_3+N_4)$ Vs ϵ



- 100k events generated for each points in the range $0.9 < \epsilon_{\text{true}} < 1$, step size=0.001
- Each of the 3 prongs(probe side) is a random variable uniformly distributed in $[0,1]$ and if ...
 - ... $< \epsilon_{\text{true}} \rightarrow$ detected
 - ... $> \epsilon_{\text{true}} \rightarrow$ undetected
- Define N_3 and N_4 favorable cases and compute the estimator $N_4/(N_3+N_4)$ for each given ϵ_{true}
- Measured efficiency around $\sim 92\%$ should correspond to $\sim 95.5\%$ real finding efficiency per track

Summary

- $N_4/(N_3+N_4)$ underestimates the real efficiency
- The discrepancy between data and MC is also affected and should be corrected
- Investigate corrections (if) applied by BaBar