

Dark Energy

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1. Introduction

Our Cosmological Framework derives from...

Observation:	The Universe is expanding
Principles:	Homogeneous, isotropic
Theory:	General Relativity

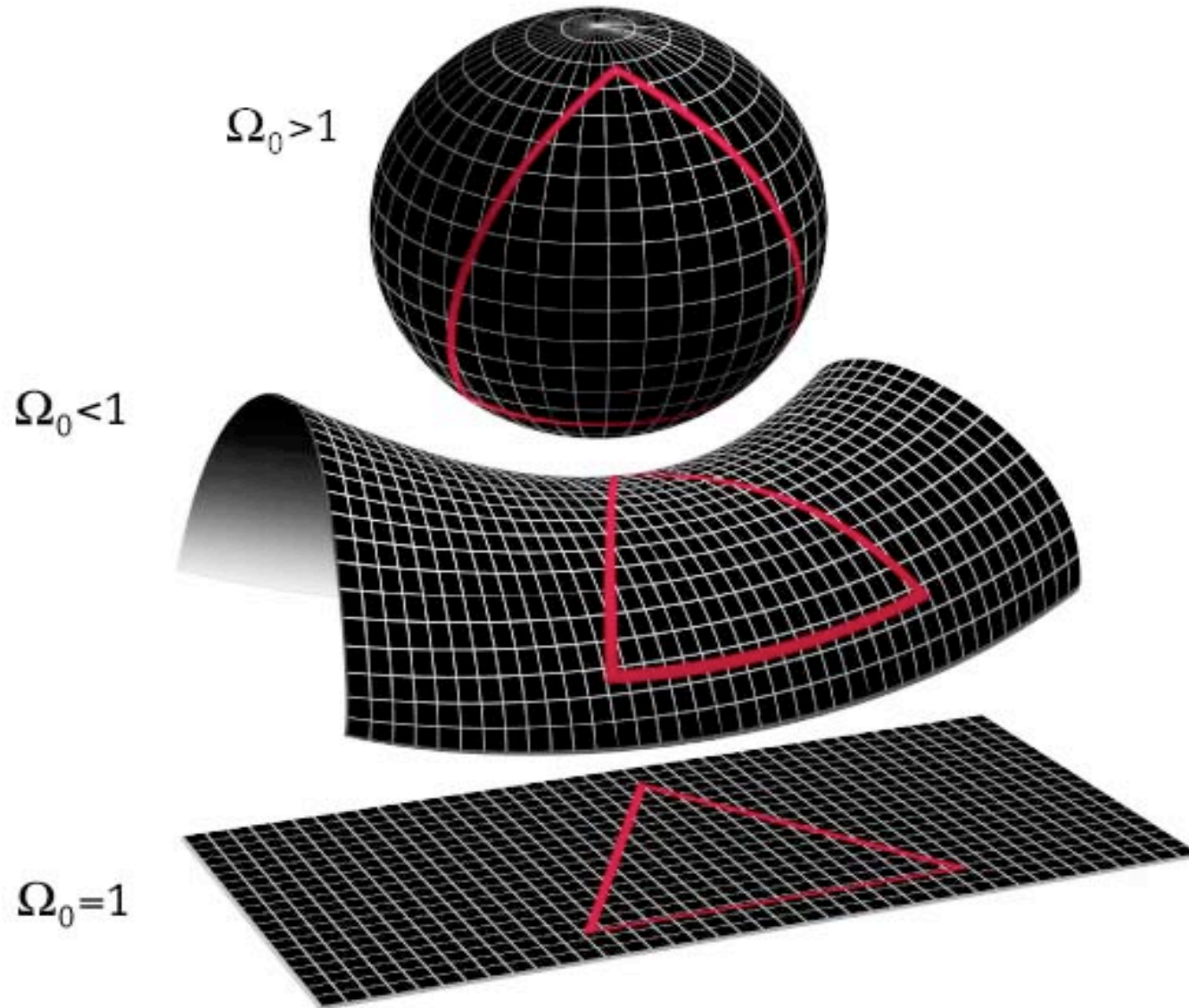
General relativity

Einstein, 1916:
General Relativity



$$\underbrace{-8\pi GT_{\mu\nu}}_{\text{Energy}} = \underbrace{R_{\mu\nu} - \frac{1}{2} g_{\mu\nu} R}_{\text{Curvature}}$$

General Relativity: The Universe can have curvature





I want a **static Universe** -
I'll add a **cosmological constant**

$$\underbrace{-8\pi GT_{\mu\nu}}_{\text{Energy}} = \underbrace{R_{\mu\nu} - \frac{1}{2} g_{\mu\nu} R}_{\text{Curvature}}$$



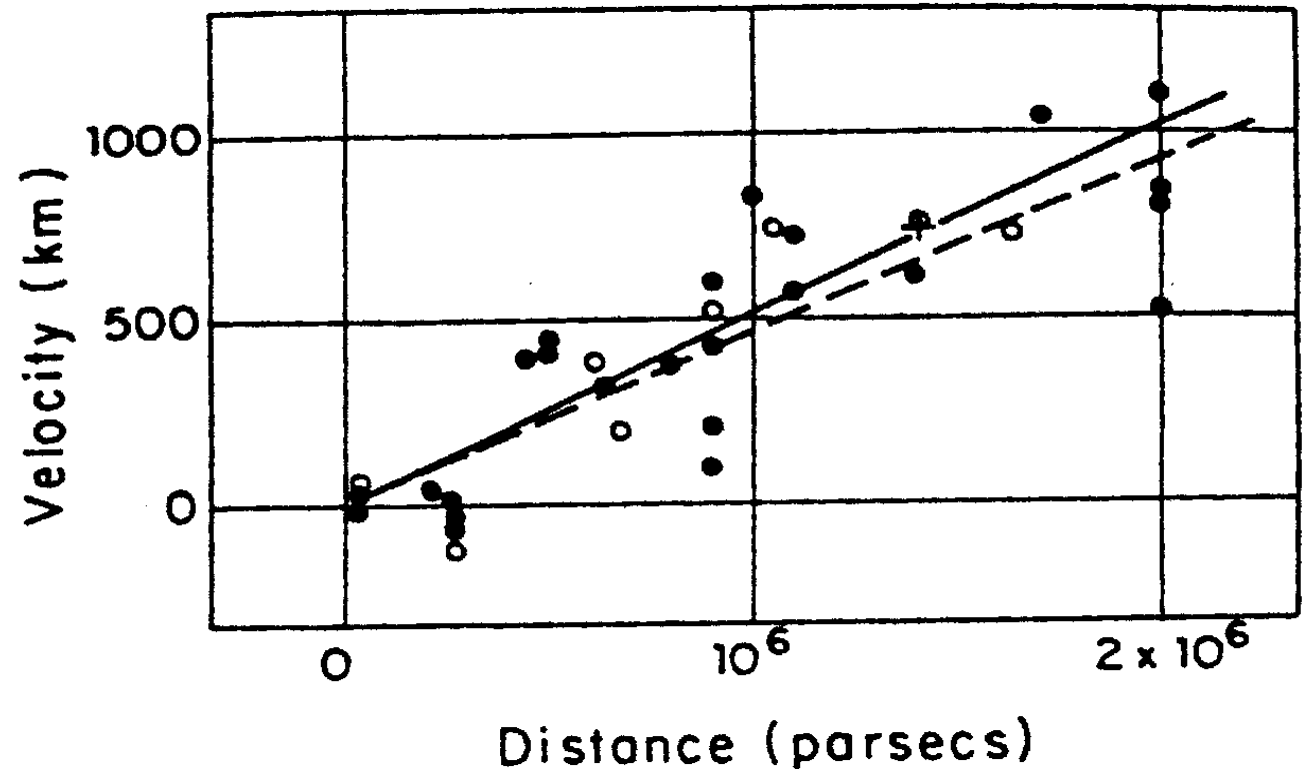
The larger the distance to a Galaxy,
the faster it is flying away from us:
 $\text{velocity} = H_0 \times \text{distance}$

Redshift of
spectral lines:

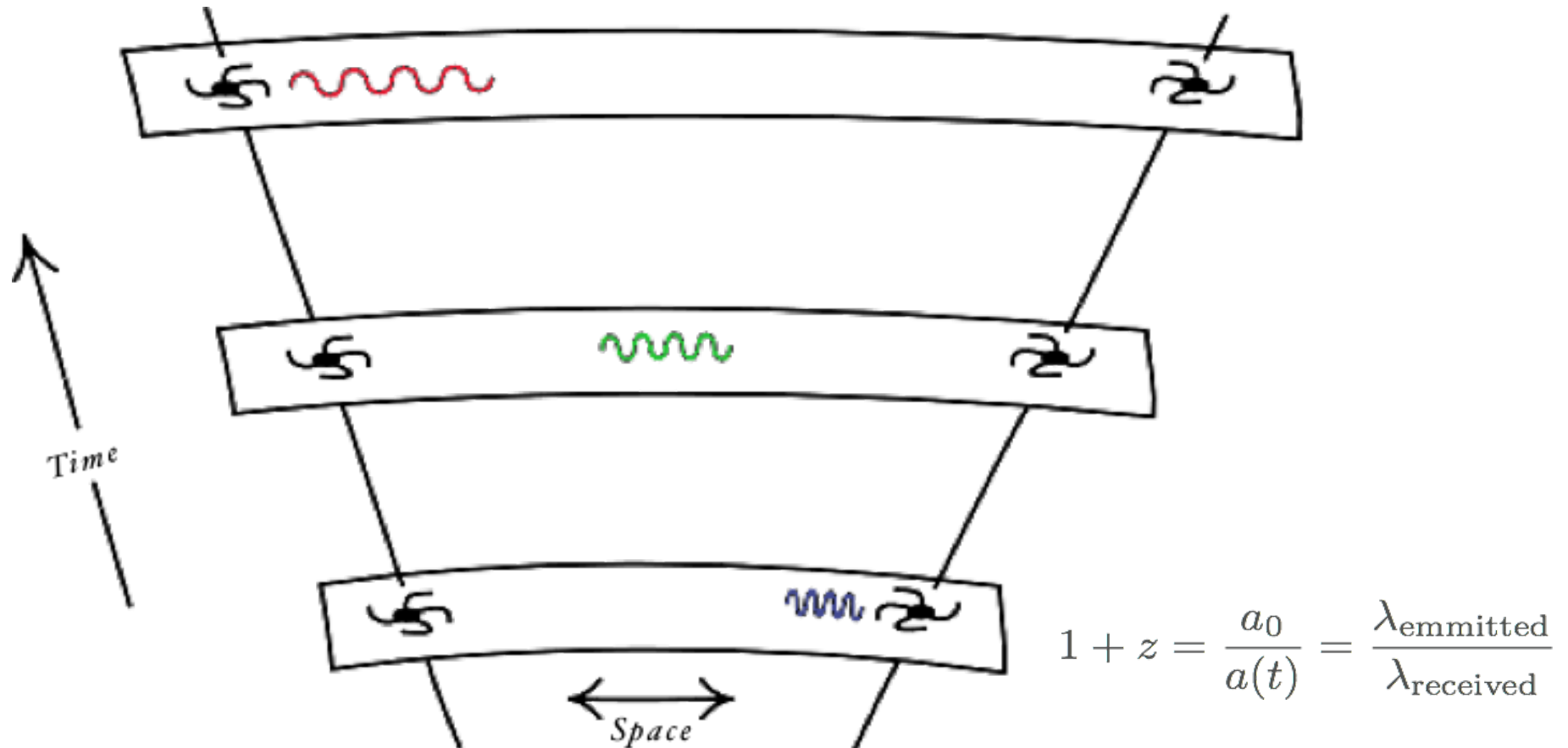
$$z = \frac{\lambda_{\text{obs}} - \lambda_{\text{emit}}}{\lambda_{\text{emit}}}$$

“Doppler effect”

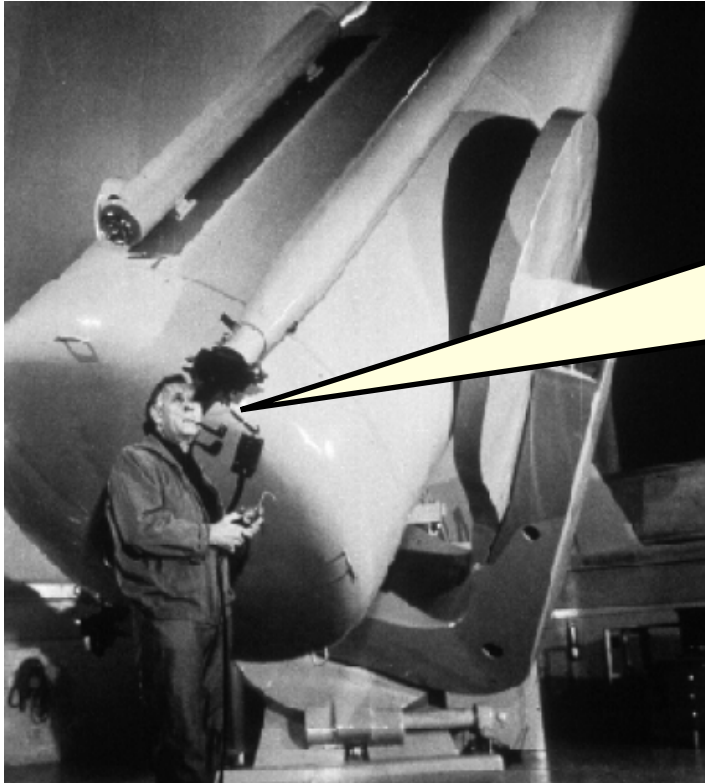
$$v \approx z \cdot (\text{speed of light})$$



Cosmological Redshift



The expansion of the Universe stretches the photon's wavelength

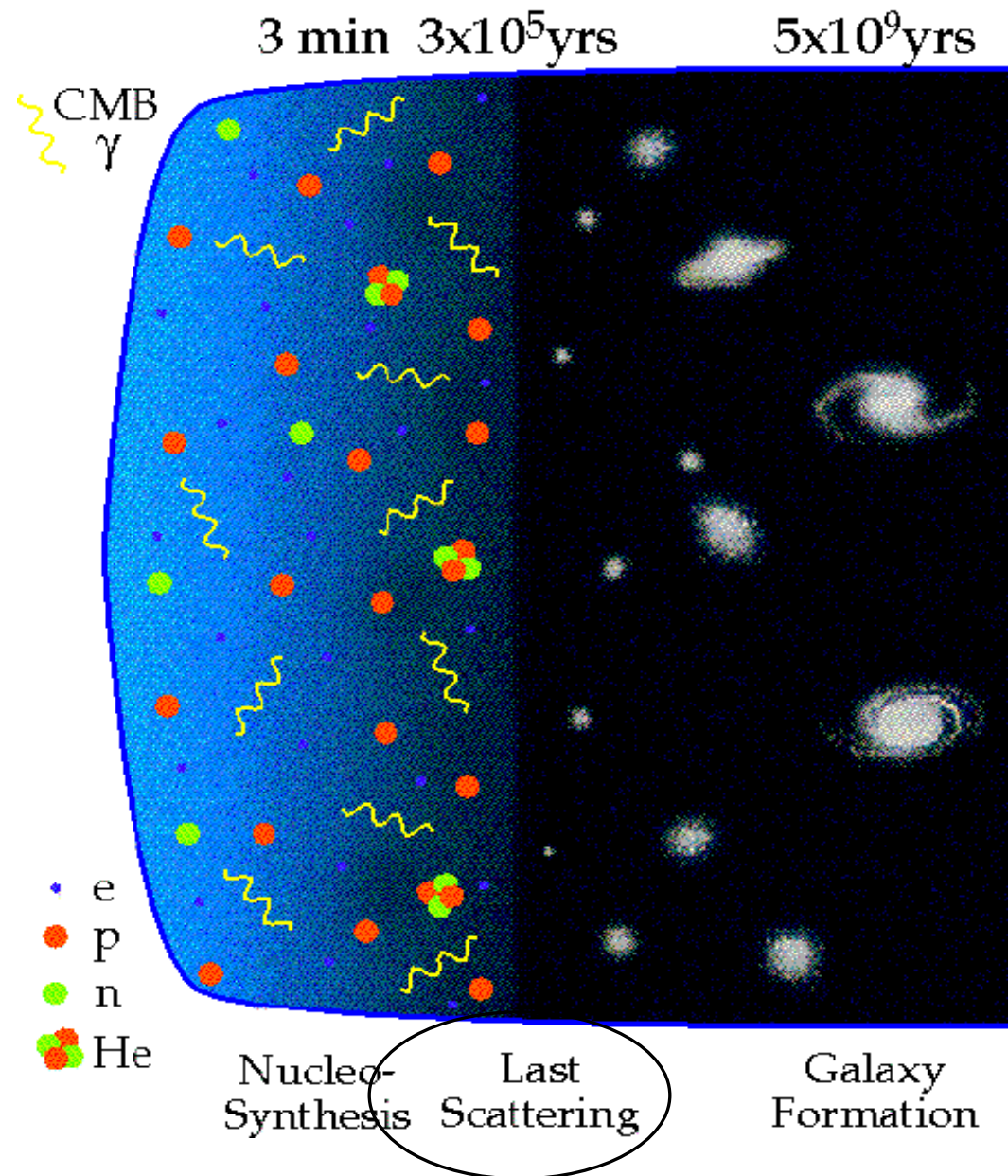


Hubble:
The Universe is expanding!



Einstein (much later):
The cosmological constant was
the biggest Blunder of my life

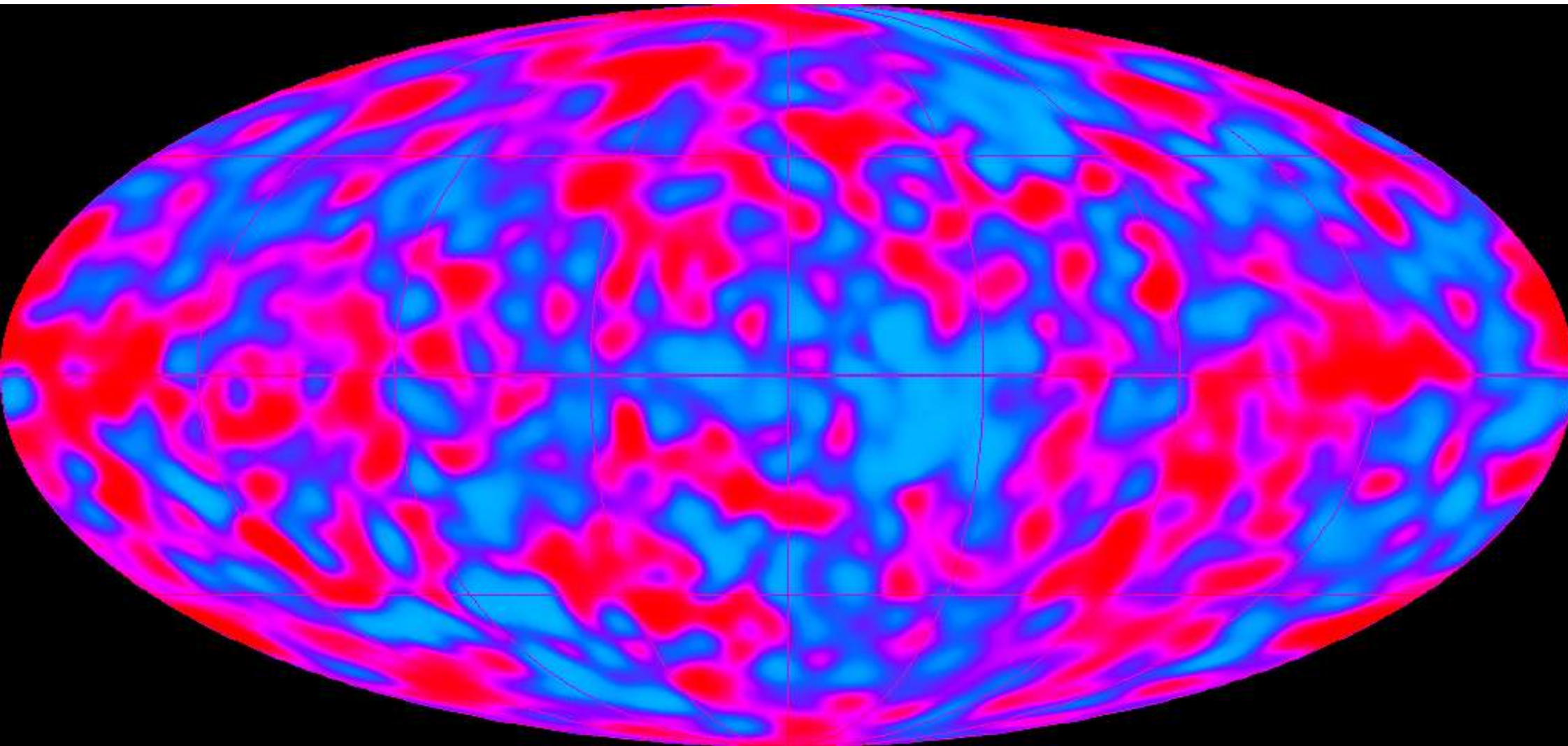
The Big Bang Universe: A very brief History



From W. Hu

The Universe (i.e. CMB) is remarkable isotropic

COBE Map of CMB Fluctuations
2.725 K +/- $\sim 30 \mu\text{K}$ rms, 7° beam



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⇒ Friedman Equation, which governs expansion

$$H^2 \equiv \left(\frac{\dot{R}}{R} \right)^2 = \frac{8\pi G}{3} \rho_M + \frac{\Lambda}{3} - \frac{k}{R^2}$$

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$$\Omega_M + \Omega_\Lambda + \Omega_k = 1$$

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Matter Density

Cosmological Constant/ Dark
Energy

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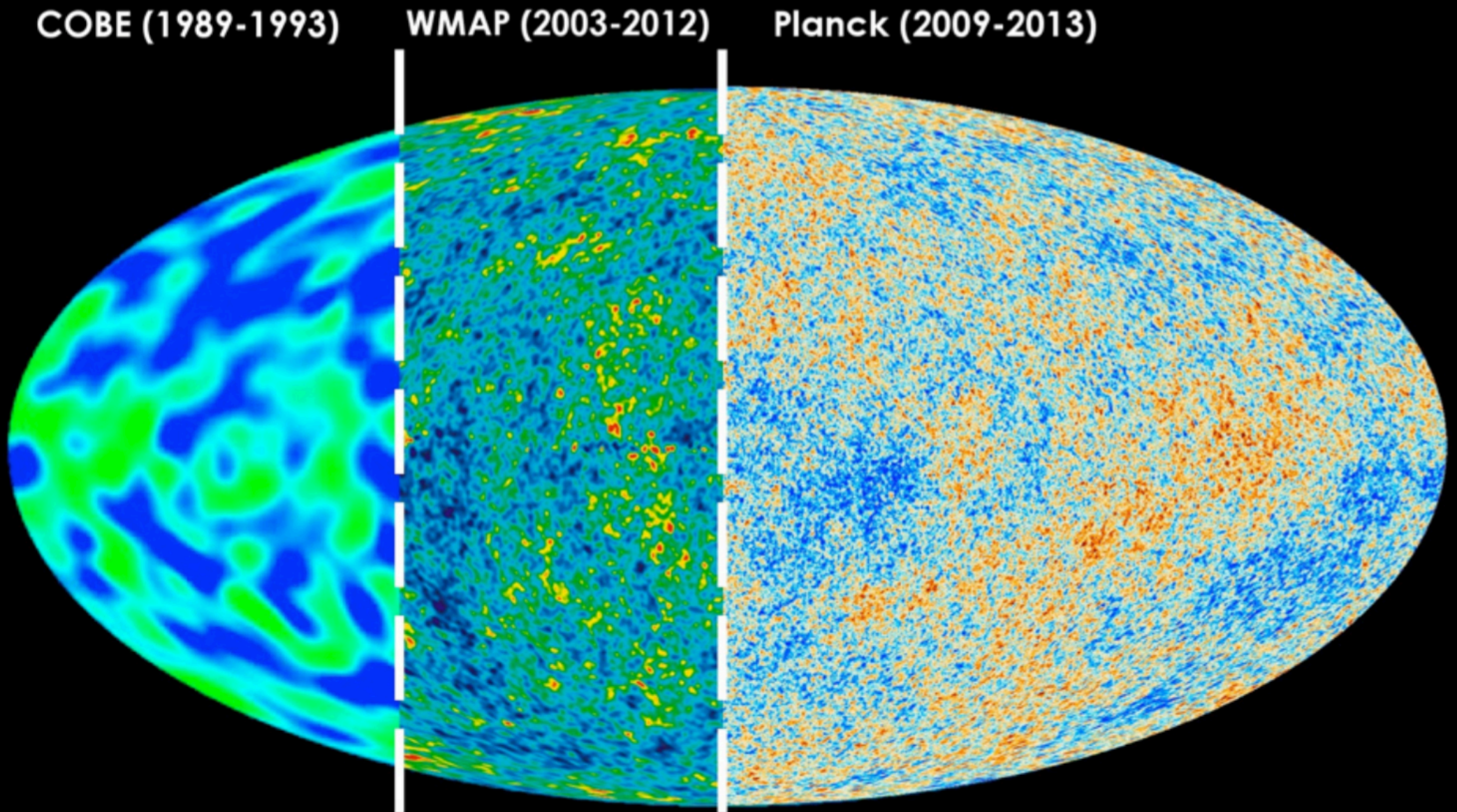
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Matter Density

Cosmological Constant/ Dark
Energy

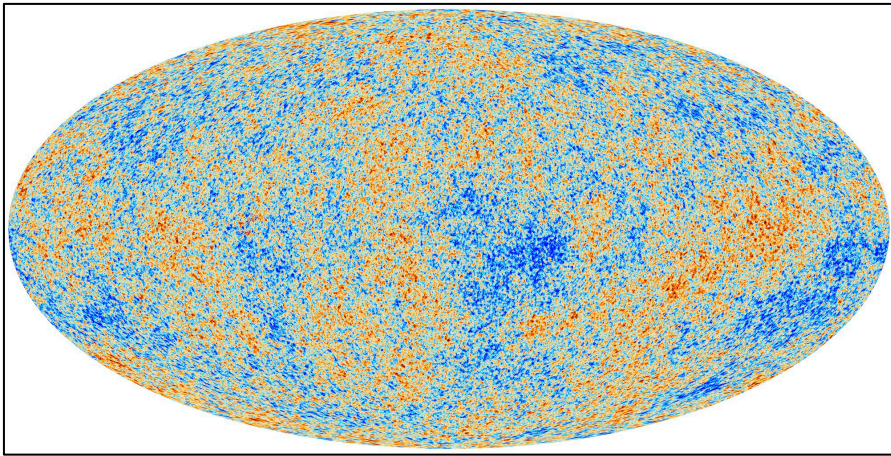
Curvature

Curvature of the Universe & Cosmic Microwave Background (CMB)



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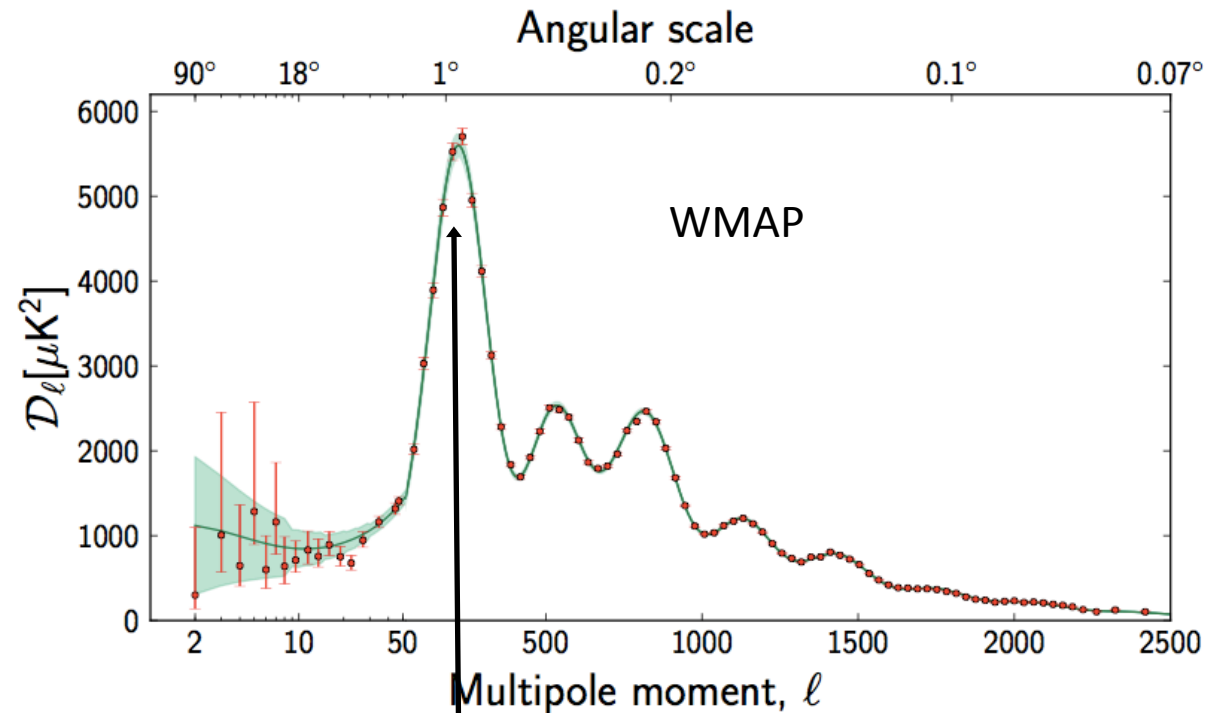
Planck



Representation of temperature map
In Spherical Harmonics:

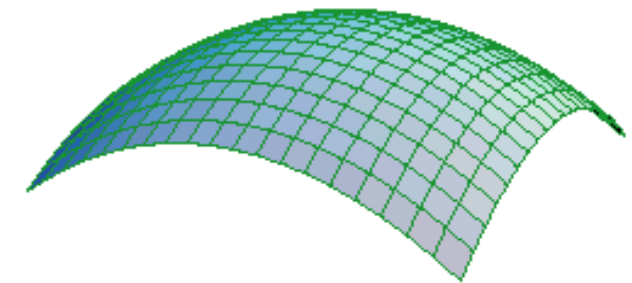
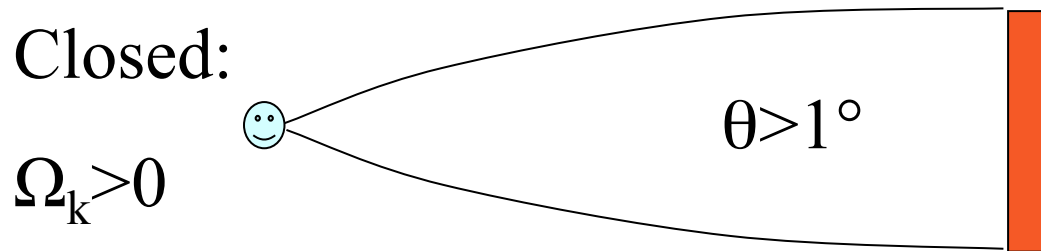
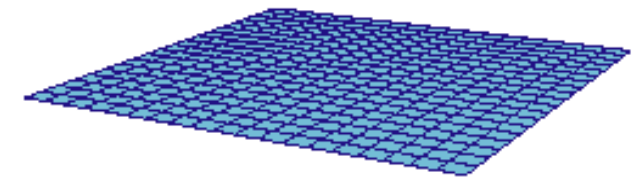
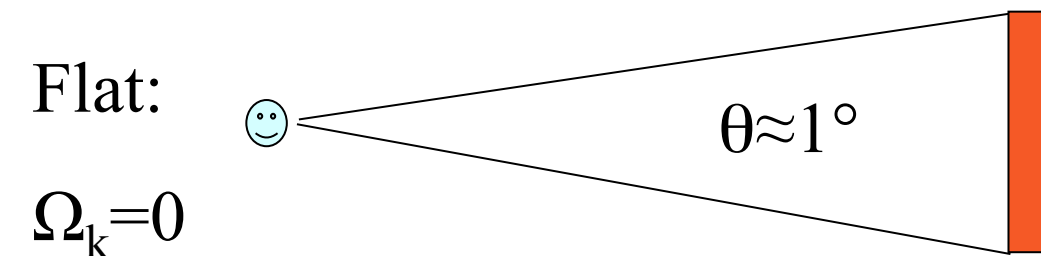
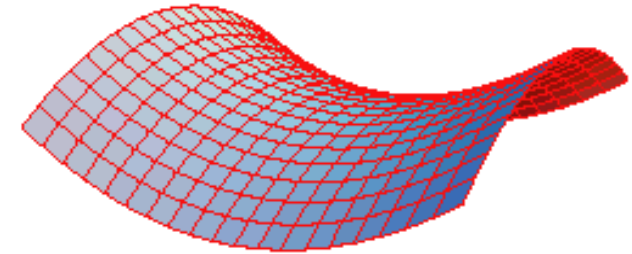
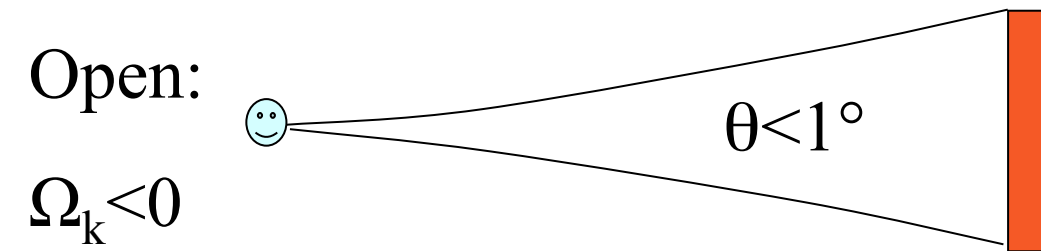
$$\frac{\Delta T}{T} = \sum_{l=2}^{\infty} \sum_{m=-l}^{m=l} a_{lm} Y_{lm}(\theta, \phi)$$

Power spectrum as a function of
angular separation



Resonance length \Leftrightarrow acoustic horizon

Curvature of the Universe & Cosmic Microwave Background (CMB)



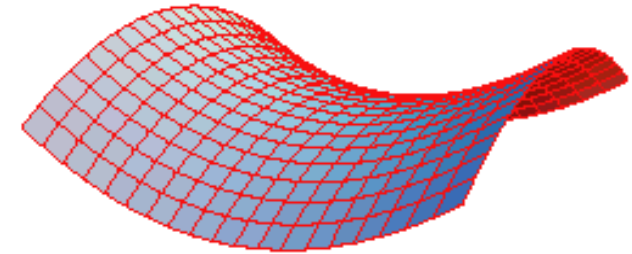
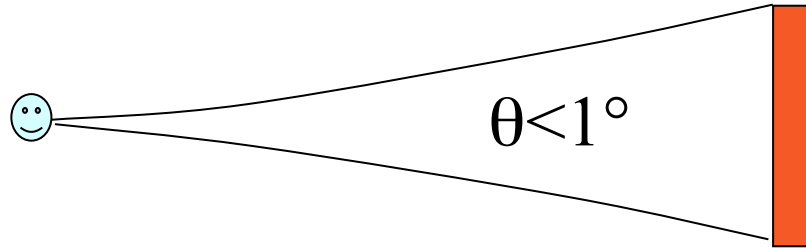
Acoustic horizon $\approx v_s t_{\text{dec}}$

$$\Omega_m + \Omega_\Lambda = 1 - \Omega_k \approx 1$$

Curvature of the Universe & Cosmic Microwave Background (CMB)

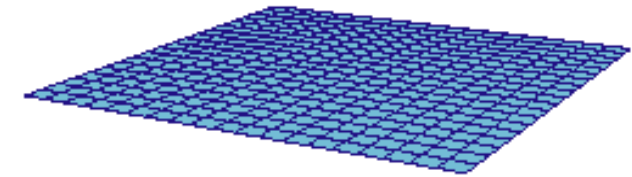
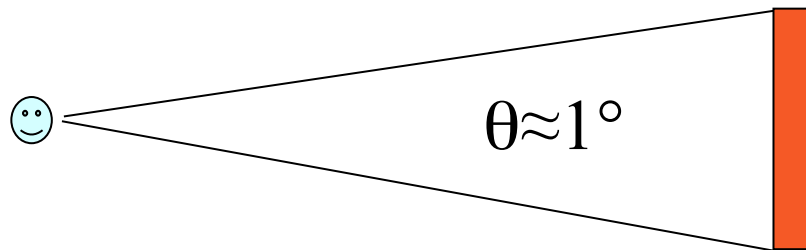
Open:

$$\Omega_k < 0$$



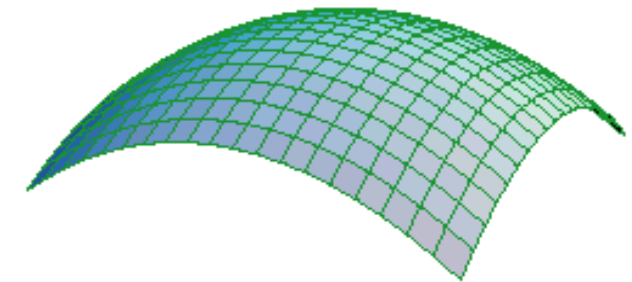
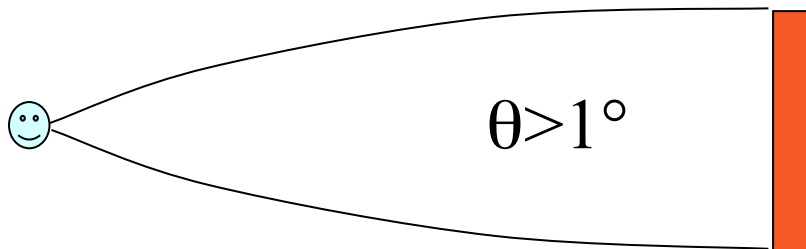
Flat:

$$\Omega_k = 0$$



Closed:

$$\Omega_k > 0$$



Acoustic horizon $\approx v_s t_{\text{dec}}$

$$\Omega_m + \Omega_\Lambda = 1 - \Omega_k \approx 1$$

(Dark) Matter in the Universe



Coma: ~650 galaxies

Galaxy Clusters (F. Zwicky, 1933)

Virial Theorem :

$$E_{\text{kin}} = \frac{1}{2} E_{\text{potential}}$$

Visible matter can not
explain high velocities!

~80% of matter must be **dark**

The cosmological constant Λ

Friedmann, 1922:

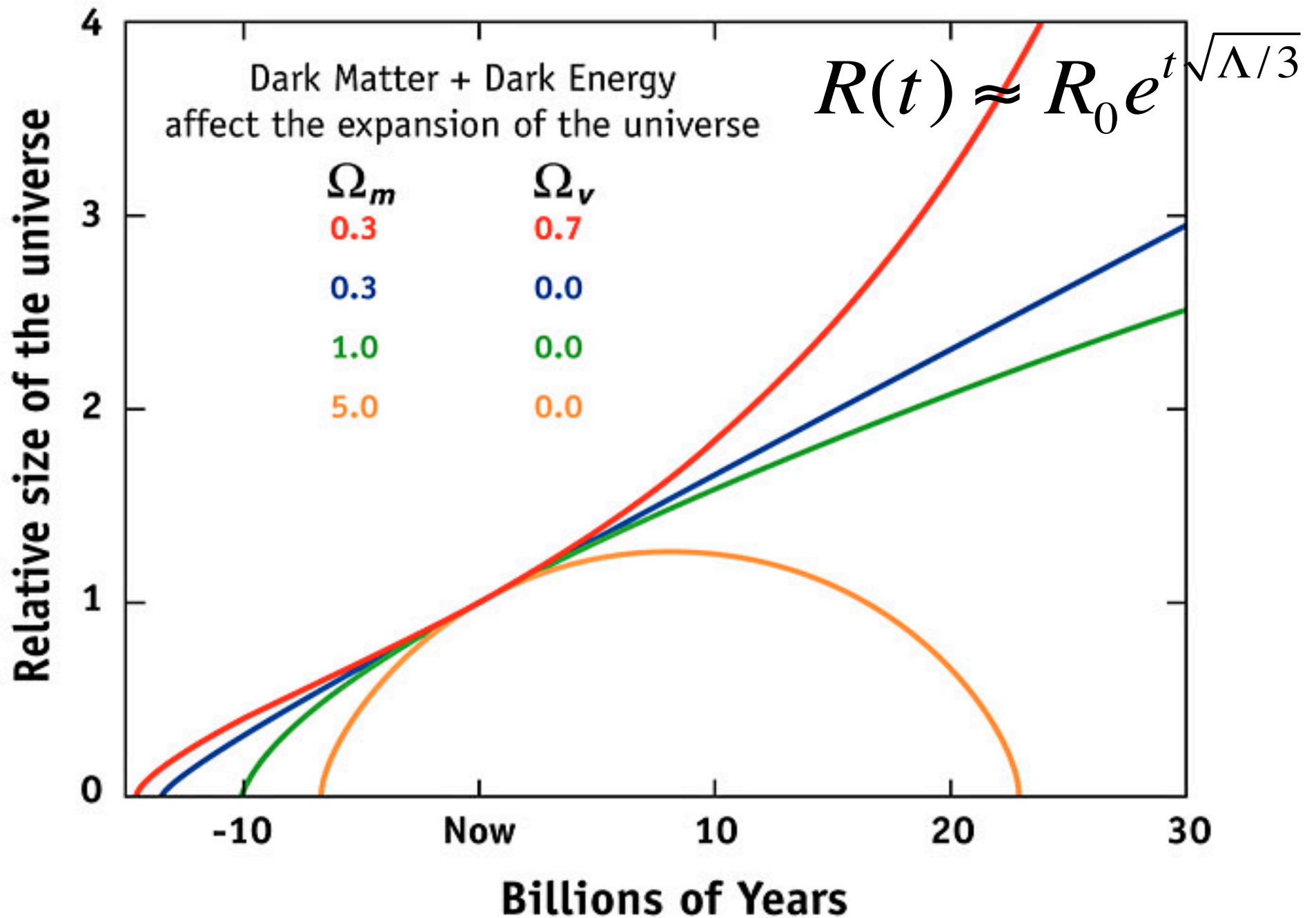


$$\left(\frac{\dot{R}}{R}\right)^2 = \frac{8\pi G}{3}\rho_M + \frac{\Lambda}{3}$$

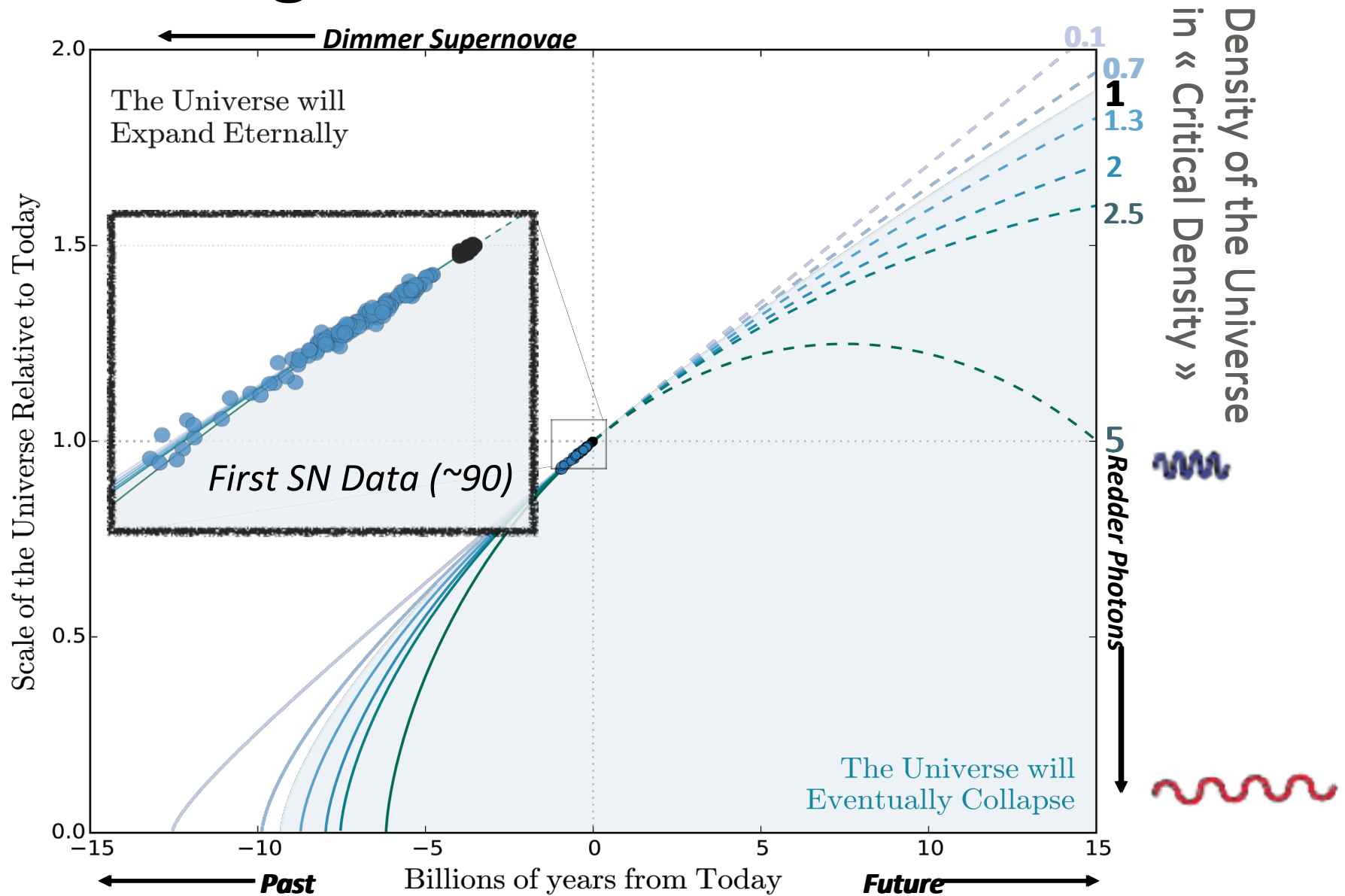
For a Universe without matter, $\rho_M = 0$, the solution is simple :

$$R(t) \propto e^{t\sqrt{\Lambda/3}}$$

The cosmological constant Λ



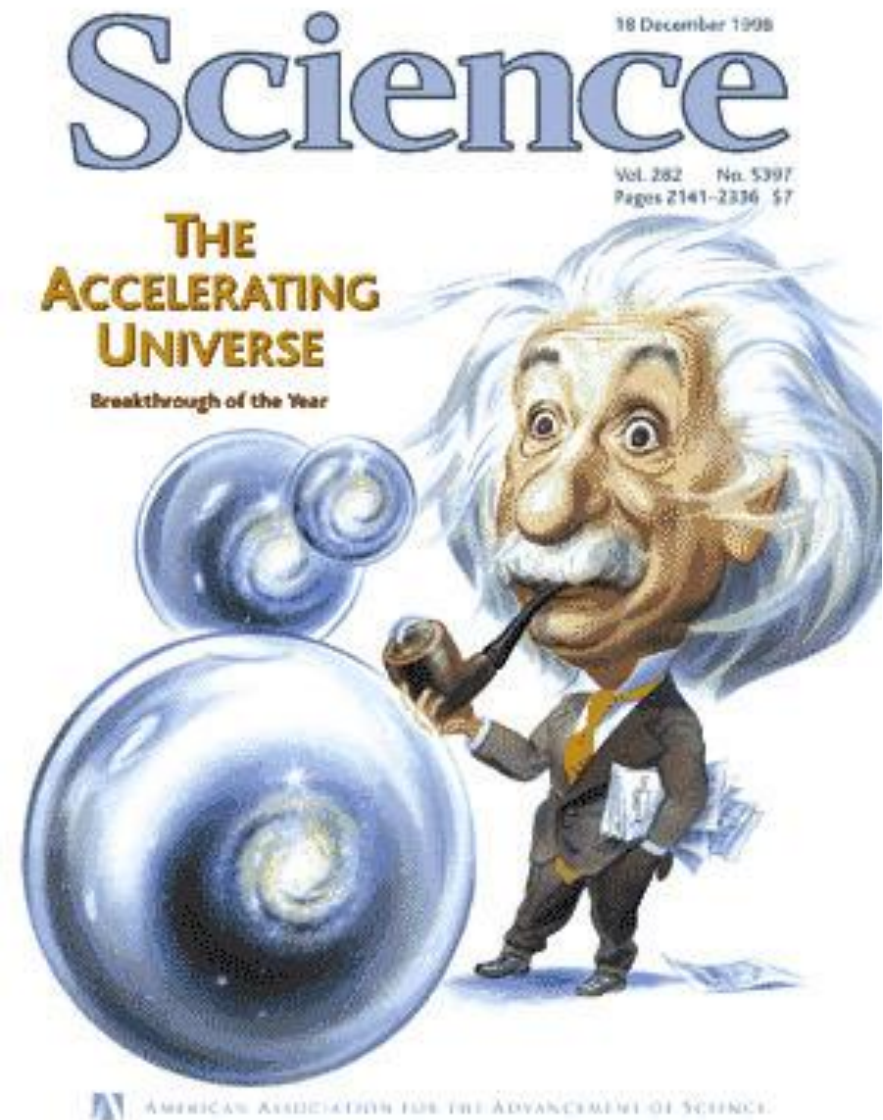
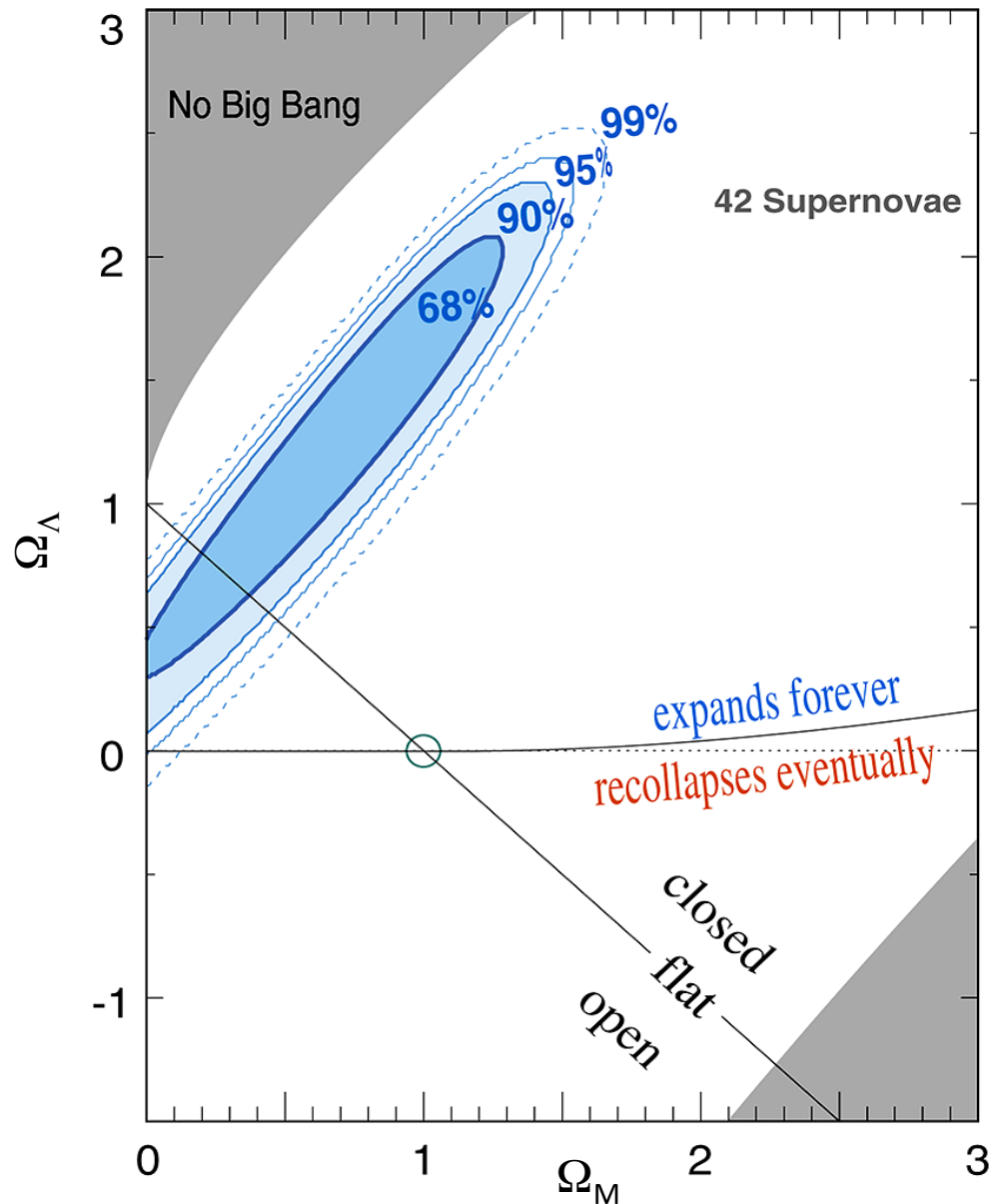
Measuring the Fate of the Universe



Density of the Universe in « Critical Density »



1998: Discovery of Dark Energy



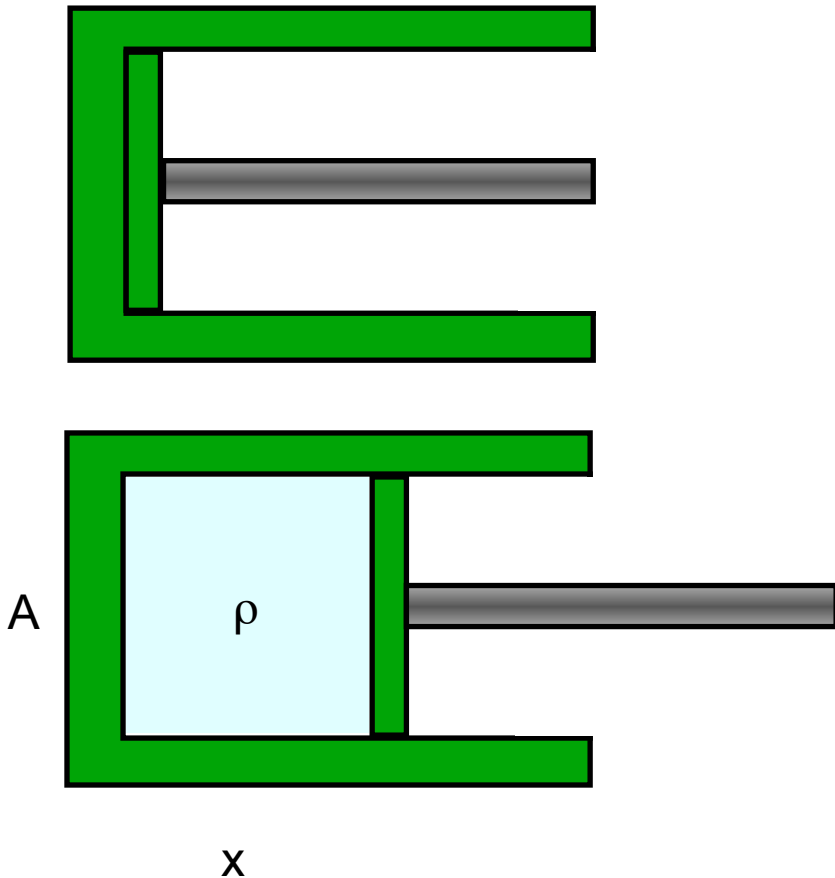
Nobel prize for physics 2011





Vacuum Energy \Leftrightarrow Cosmological Constant?

Zeldovich 1968



Vacuum energy:

Before: $E = 0$

After: $Ax\rho > 0$

Pressure (p) of Vacuum energy follows with assumption of energy conservation:

$$Ax\rho + Ax p = 0 \Rightarrow \mathbf{p = - \rho}$$

Vacuum energy has all the properties of the Cosmological constant Λ , i.e. it has negative pressure.

Fundamental Problems of Vacuum Energy/Cosmological Constant:

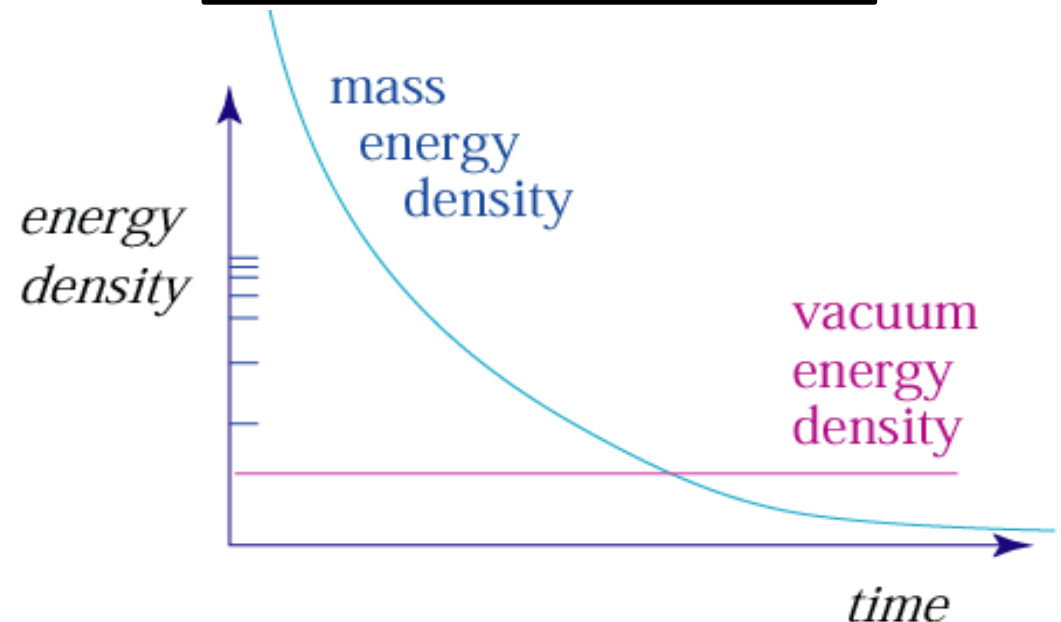
Why so small?

Expectation: $\rho_{\Lambda} \sim (M_{\text{planck}})^4$
 \Rightarrow 120 orders of magnitudes larger than the observed value!

Why now?

Matter: $\rho \propto R^{-3}$
Vacuum Energy: $\rho = \text{constant}$

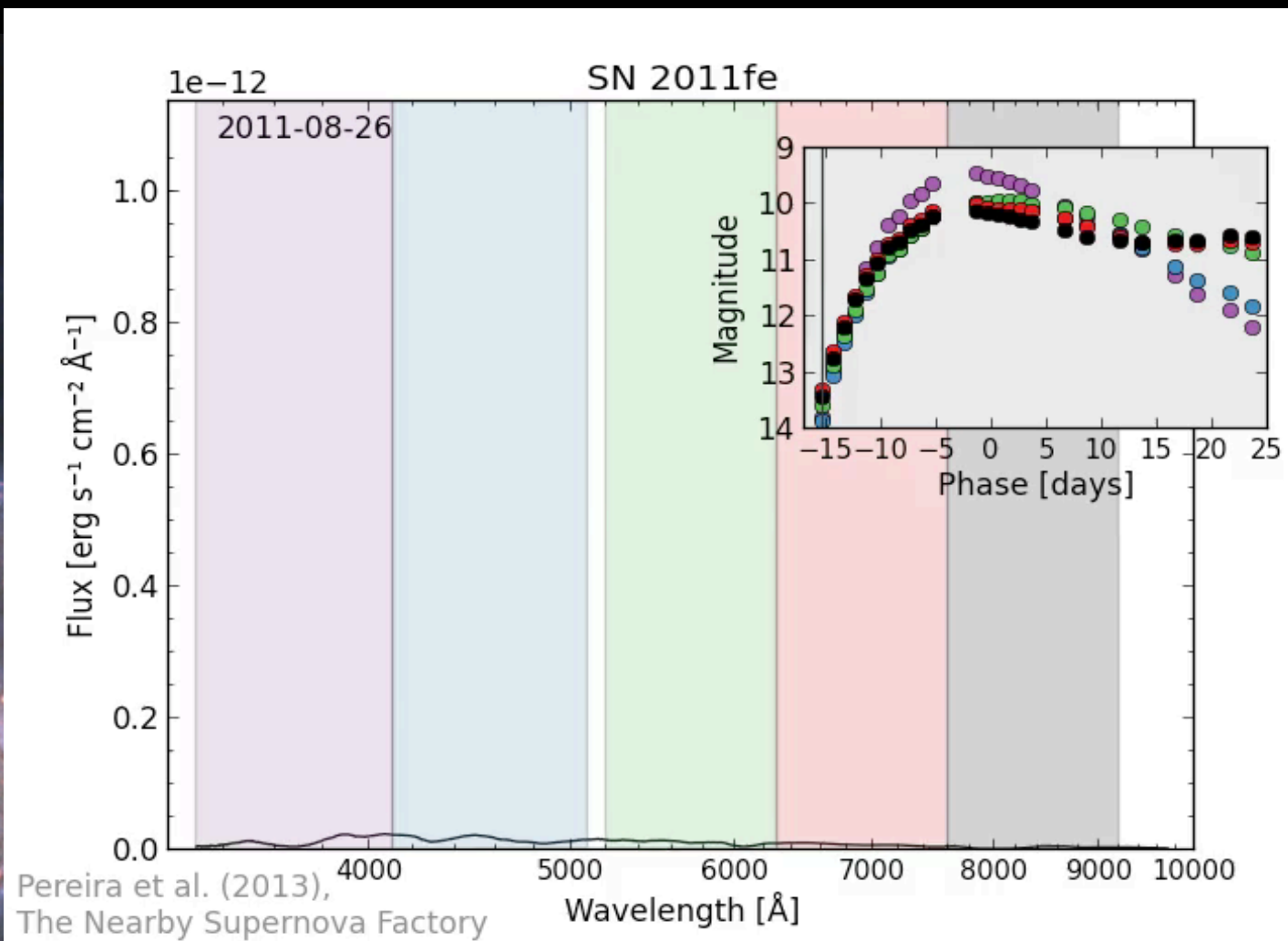
Dark Energy with equation-of-state:
 $p = w\rho$
(p = pressure; ρ = density)
 $\Rightarrow \rho \propto R^{-3(1+w)}$



Observations & Parameters

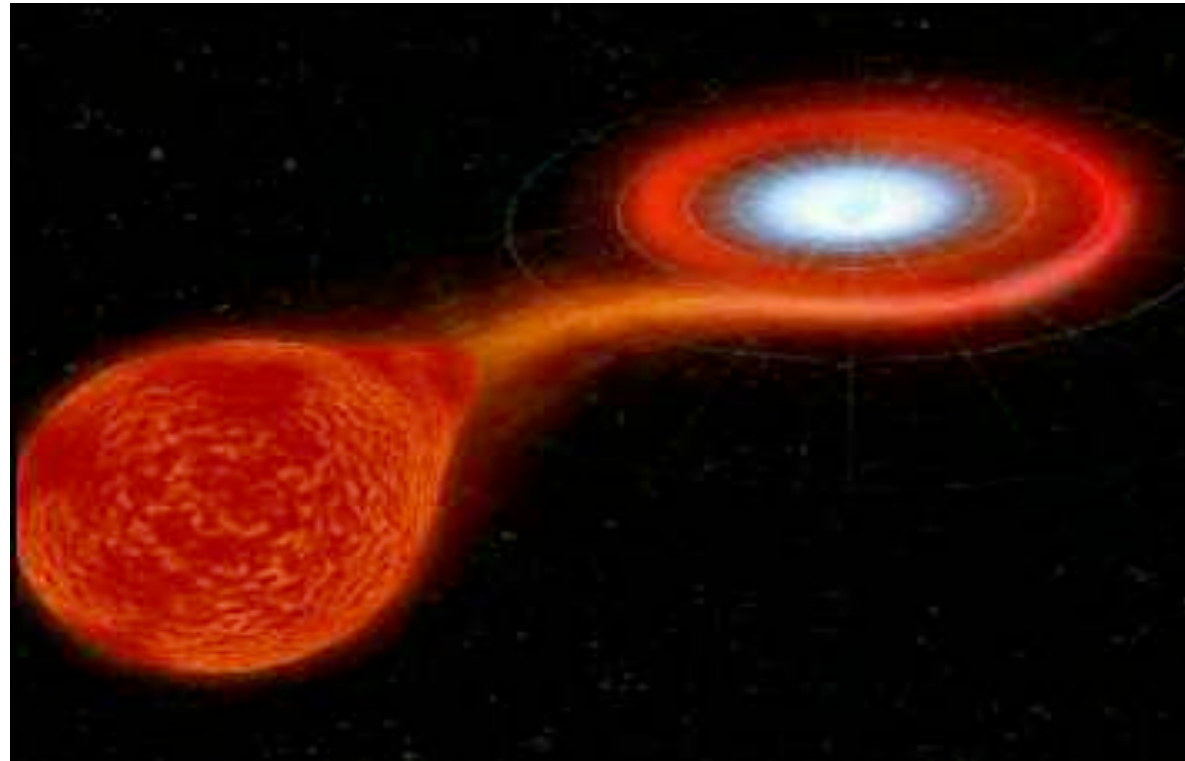


SN 2011fe

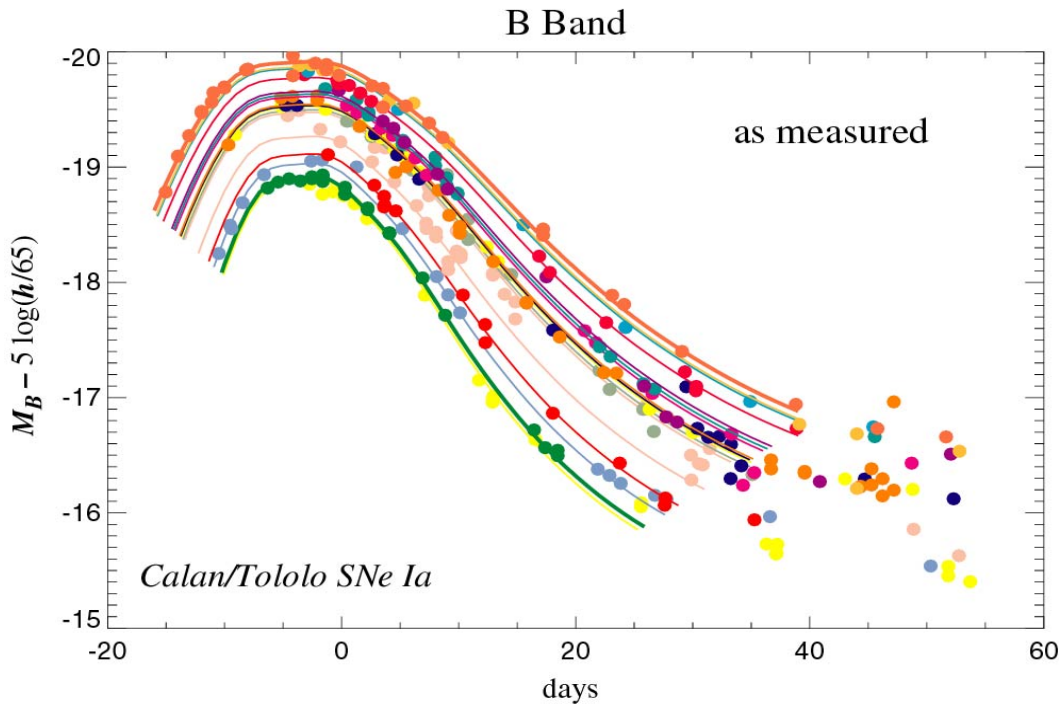


Supernova Type Ia

- ⇒ White dwarf in binary system
- ⇒ Mass transfer up to „critical“ Chandrasekhar mass of $1.4 M_{\odot}$
- ⇒ Thermonuclear explosion
- ⇒ Explosion of similar energies
- ⇒ Visible in cosmic distances



SNe Ia as “standard” Candles



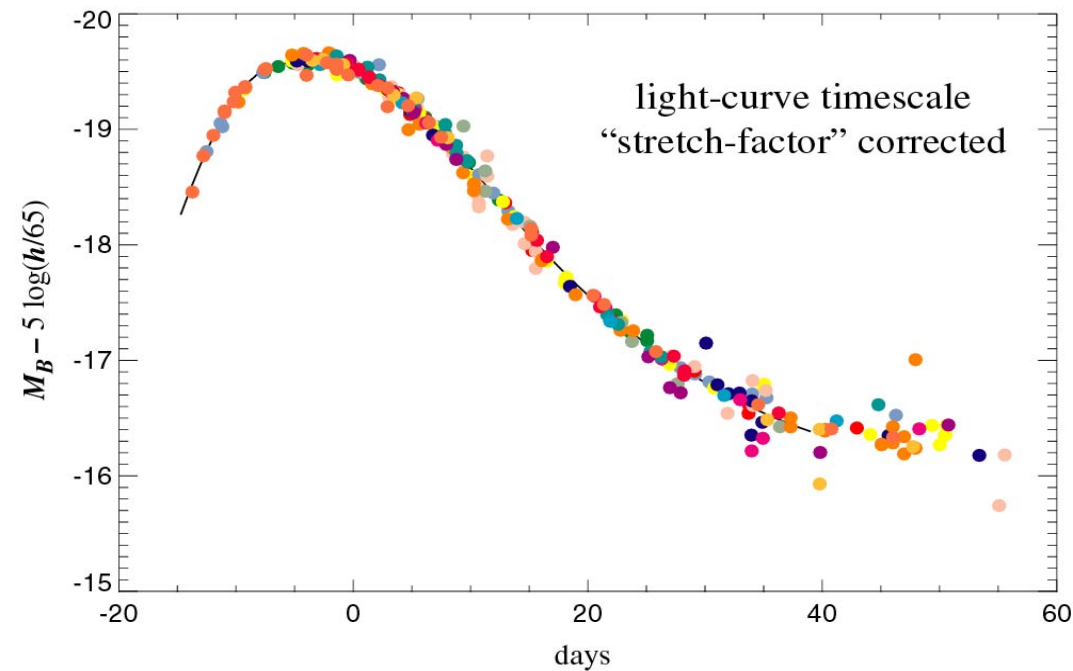
- Nearby supernovae used to study SNe light curve ($z < 0.1$)
- Intrinsically brighter SNe have wider lightcurves.

Stretching the timescale:

$$t' = s \times t$$

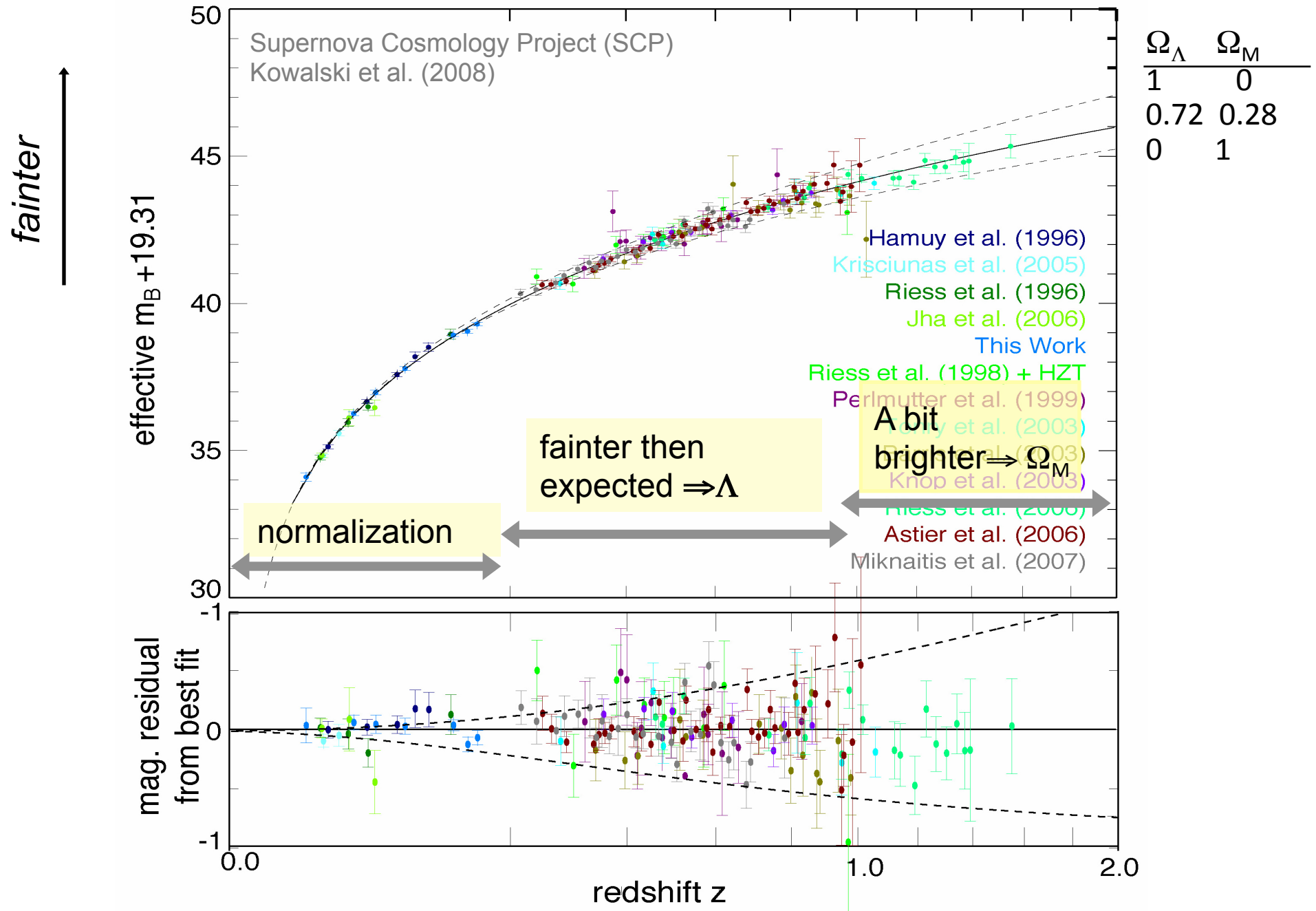
Correcting the brightness

$$M' = M + \alpha (s - 1)$$

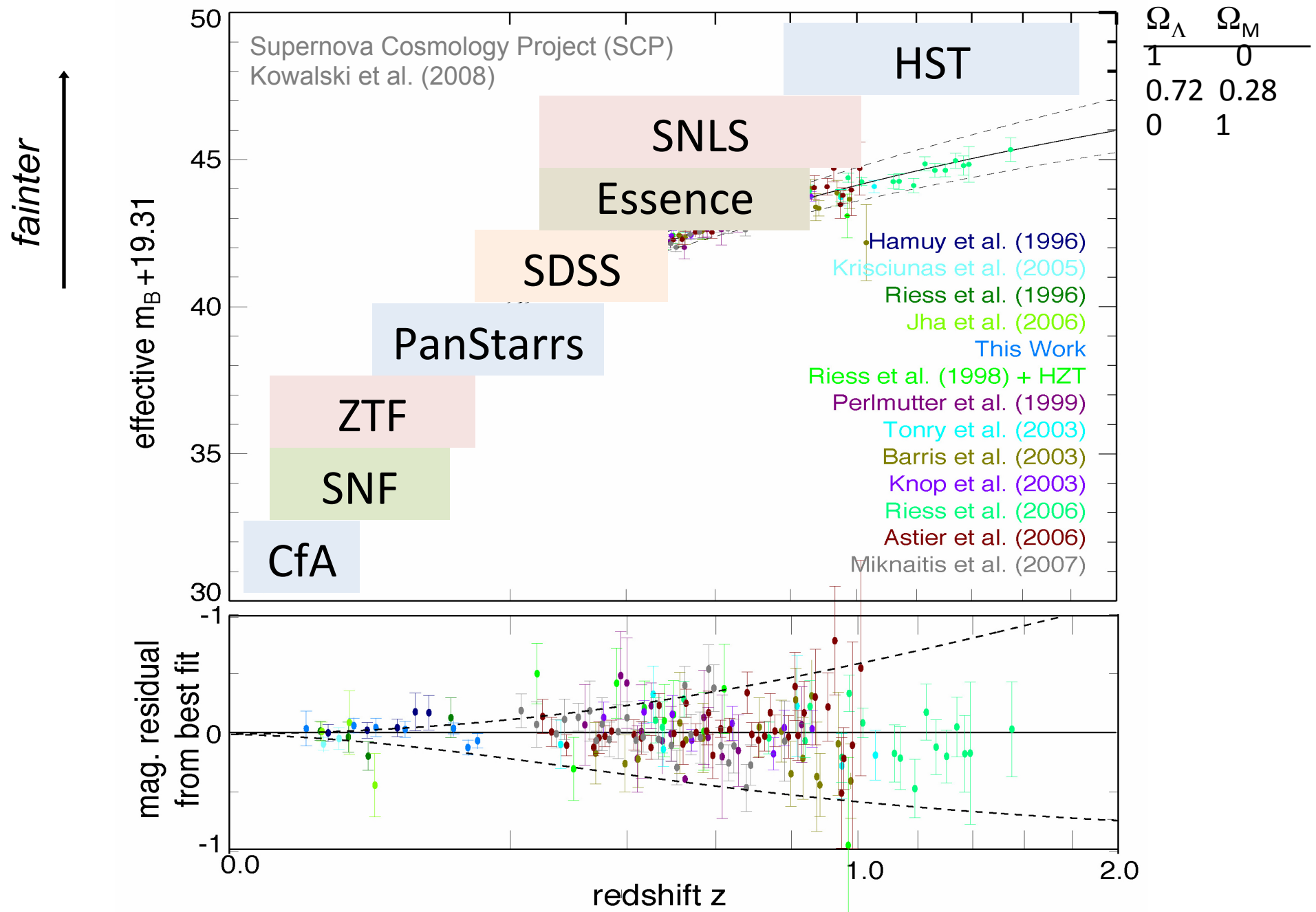


Kim, *et al.* (1997)

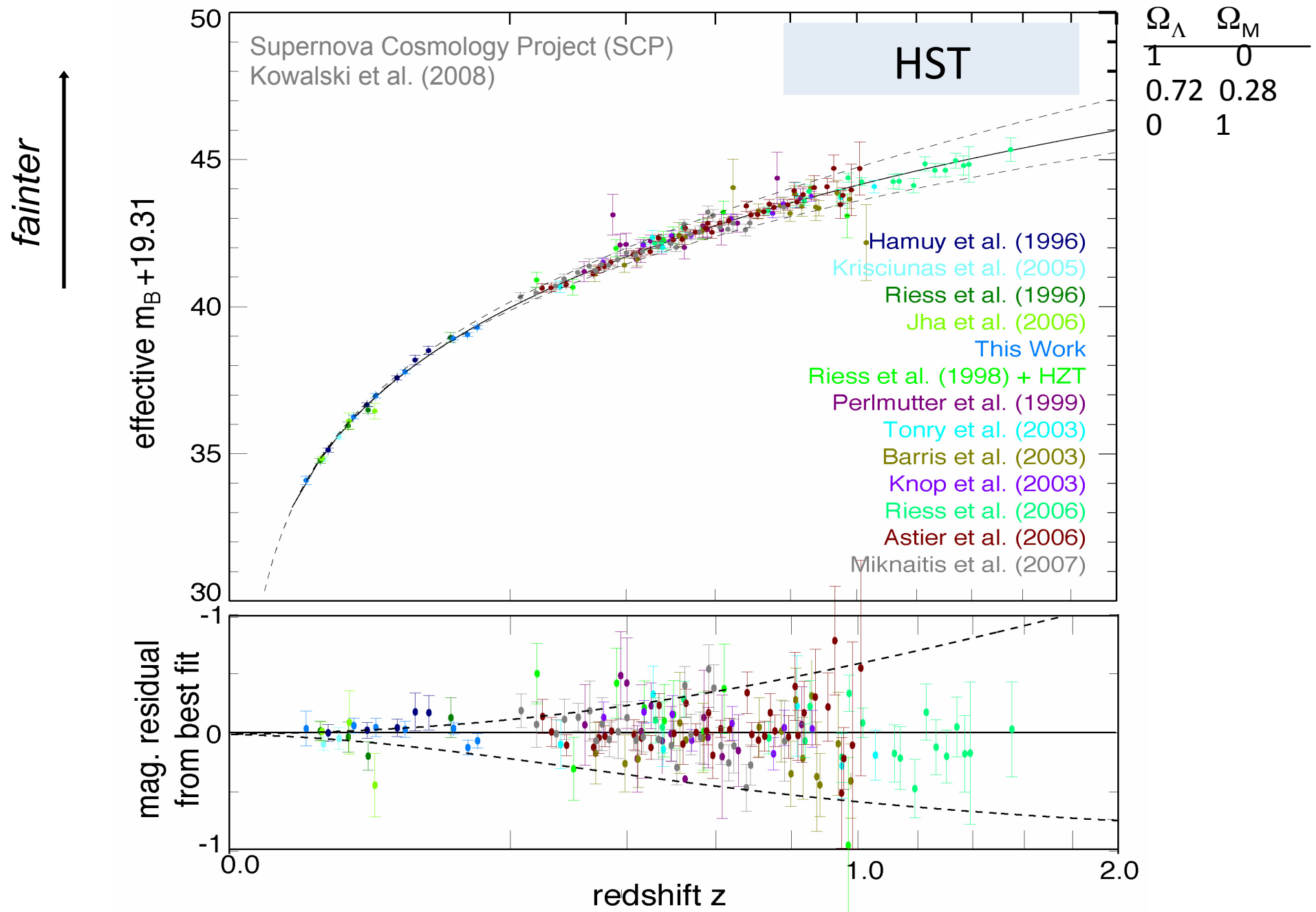
SNe Ia Hubble Diagram



SNe Ia Hubble Diagram

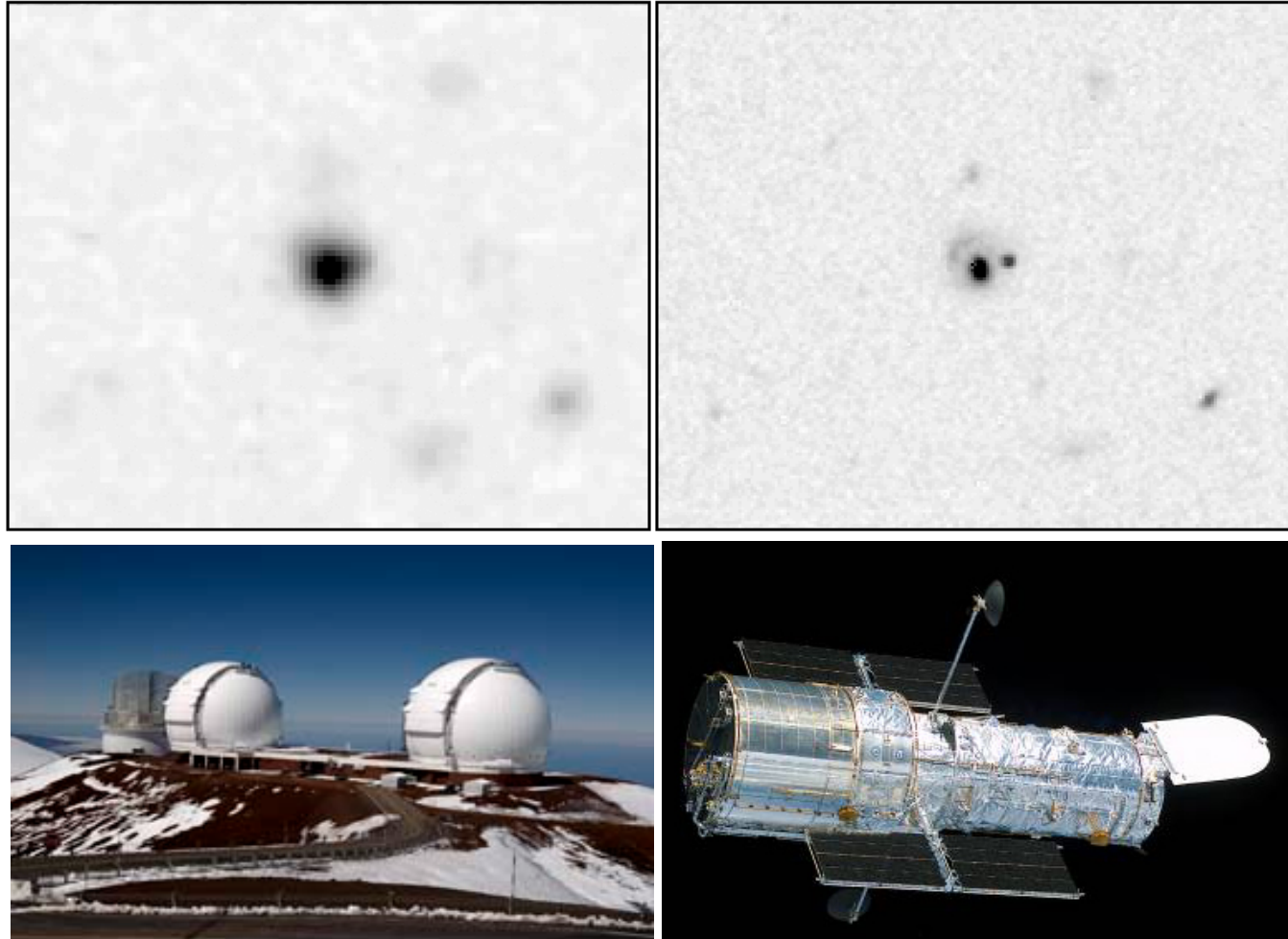


SNe Ia Hubble Diagram



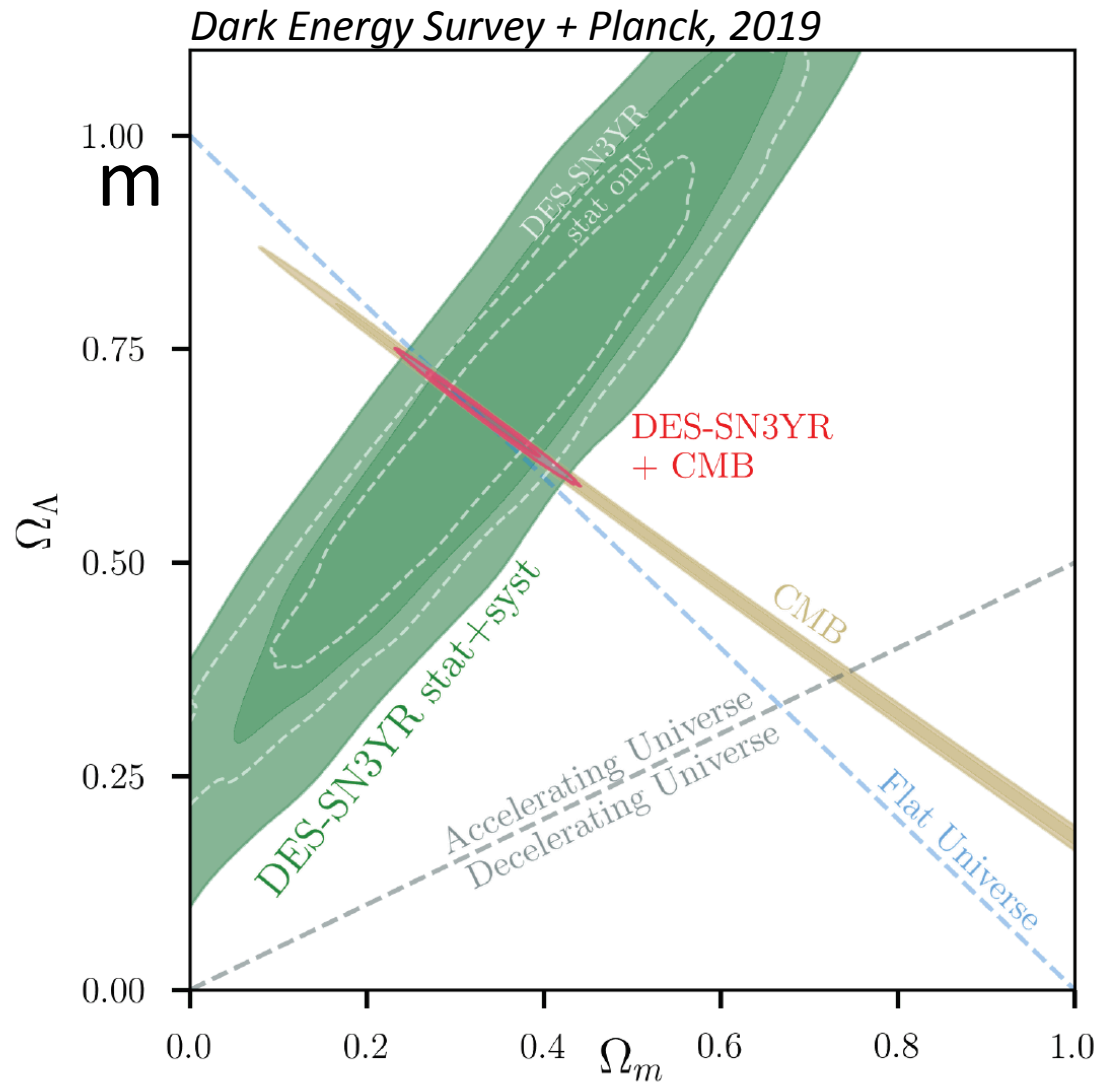
SNe at large Redshifts ($z > 1$)

SN 1997cj



Twin Keck telescopes on Mauna Kea.

Cosmological parameters



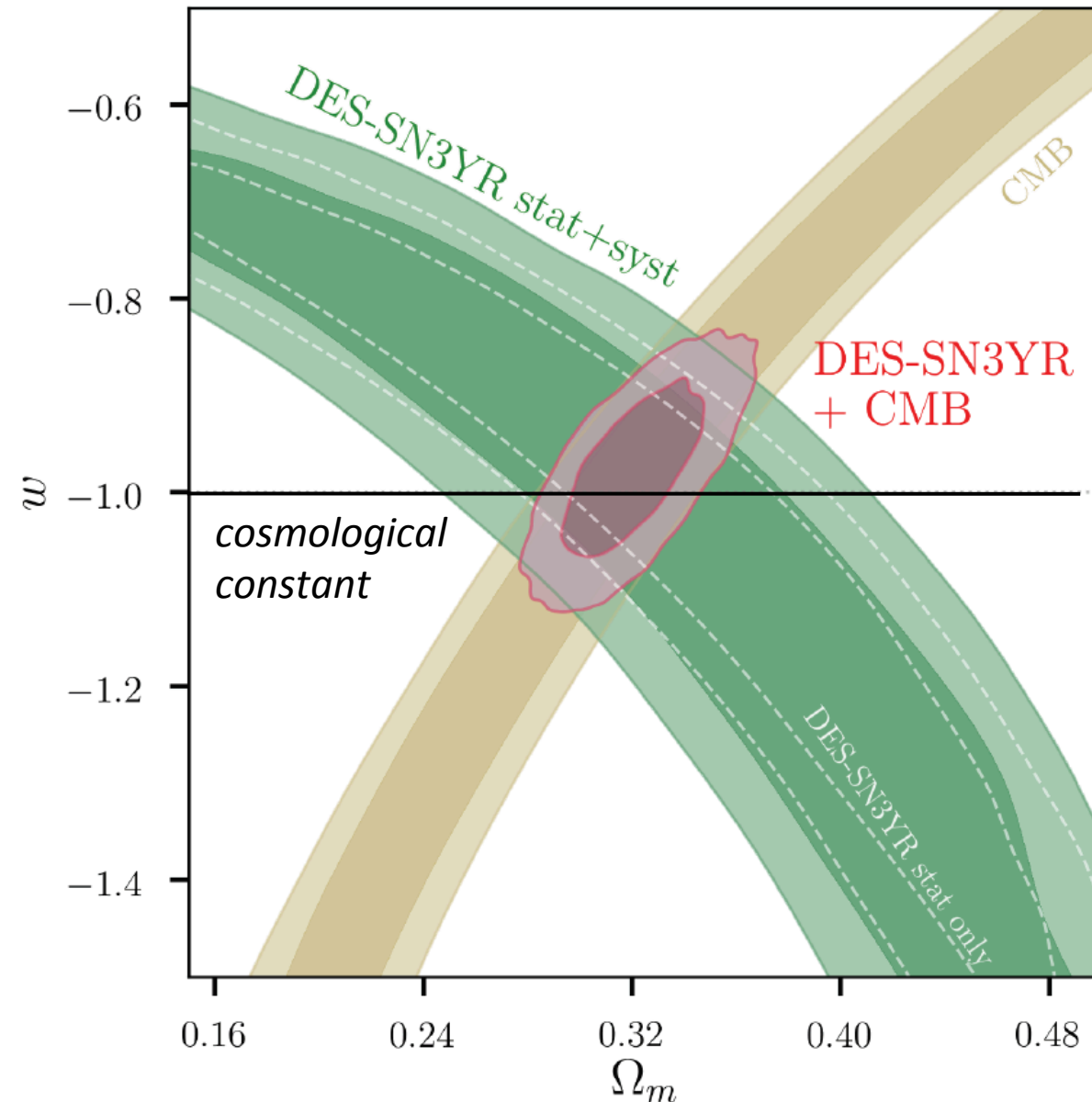
$$\Omega_\Lambda = 0.690 \pm 0.008$$

$$\Omega_M = 0.308 \pm 0.008$$

Universe dominated by DE
Universe flat to within $\sim 0.5\%$

Cosmological Parameters

Dark Energy Survey + Planck, 2019



Equation of state: $p=w\rho$

Constant w :

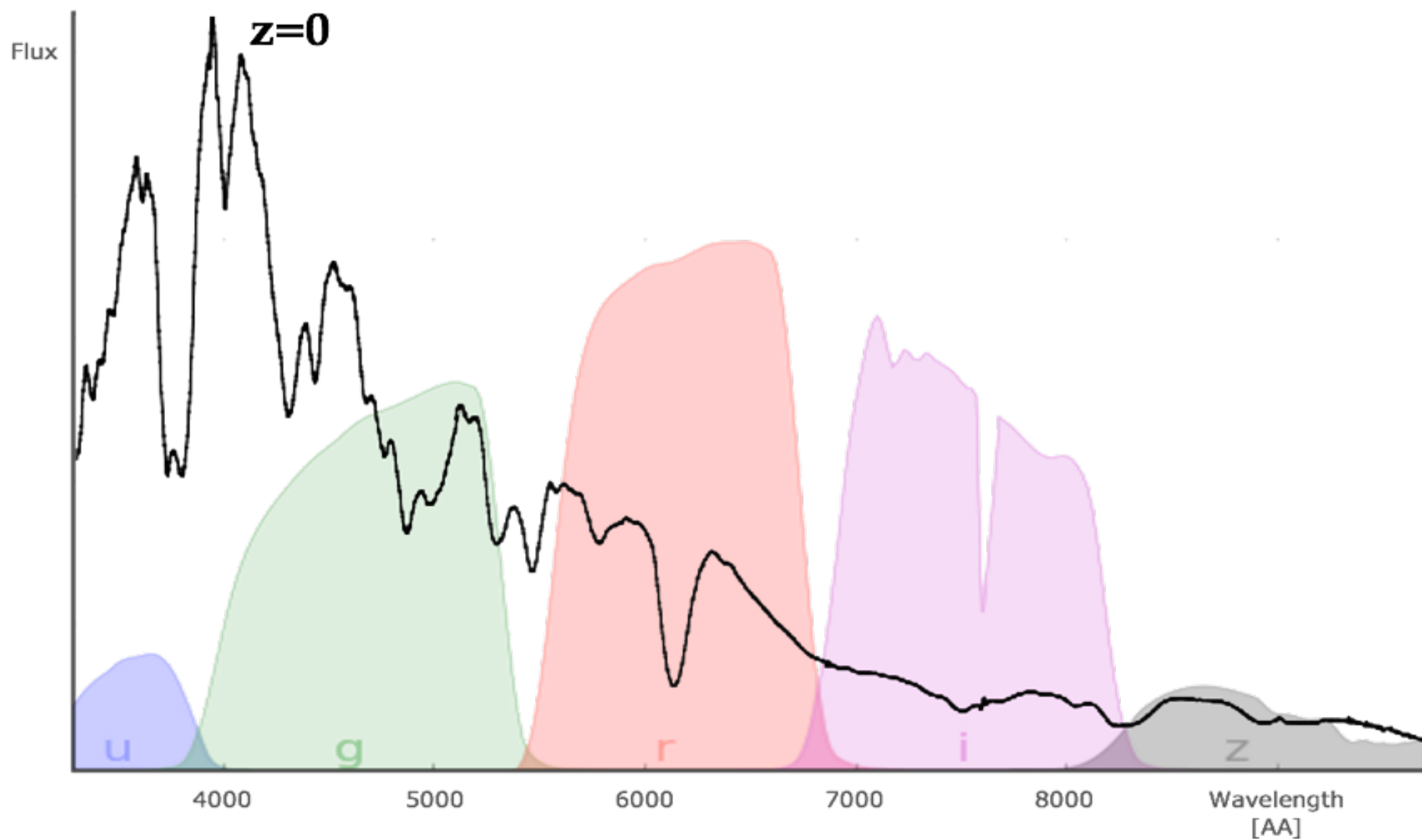
$$w = -0.978 \pm 0.059$$

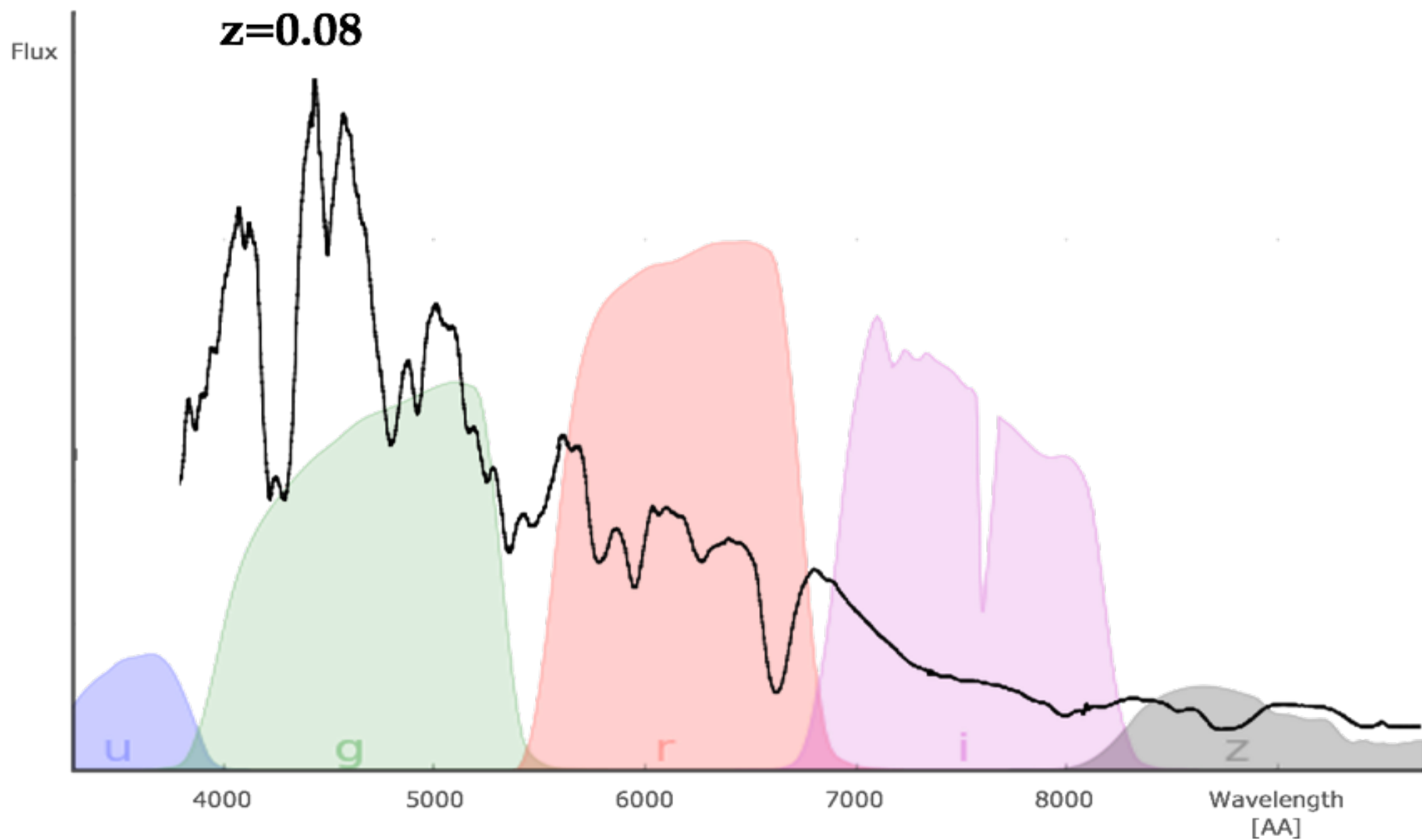
A bit of dirty laundry

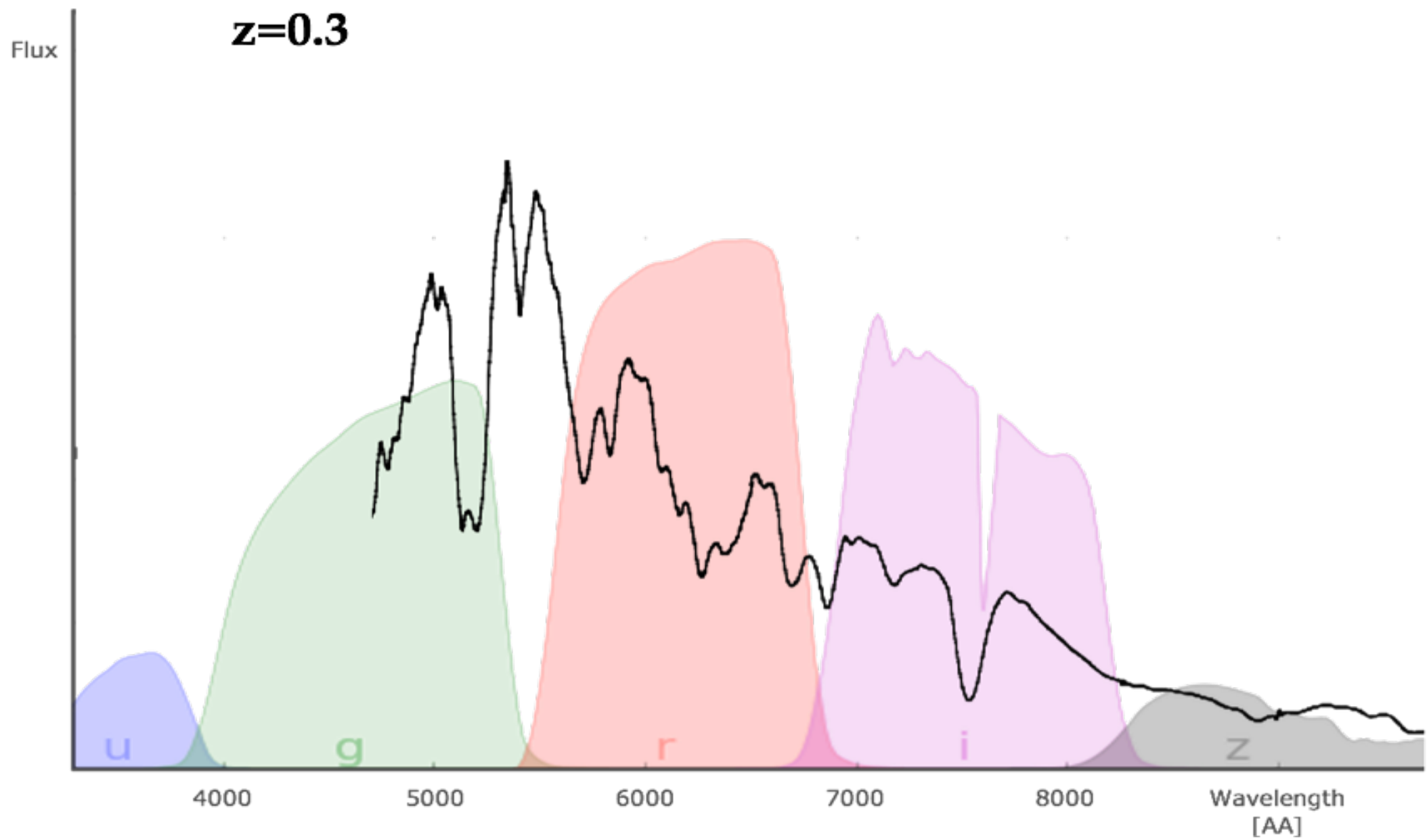
Dark Energy Equation-of-State parameter:

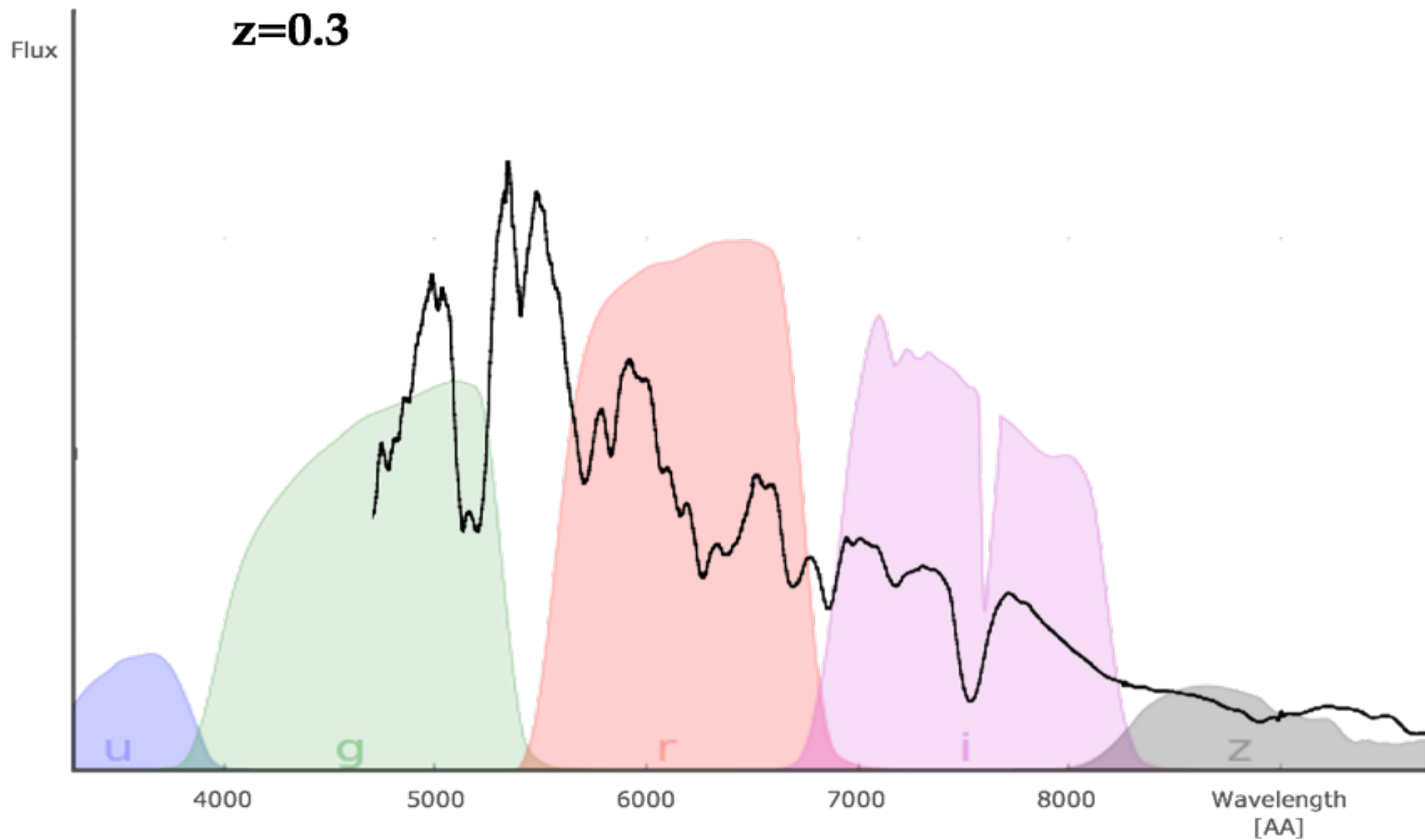
$$w = -0.978 \pm 0.042 \text{ (stat)} \pm 0.042 \text{ (sys)}$$

Dark Energy Survey, 2019









The problem of Flux calibration

Bohlin & Gordon 2014

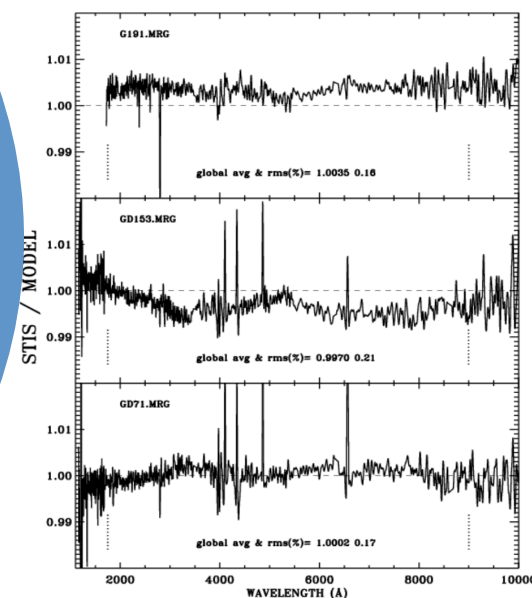
Model

White dwarf NLTE
atmosphere models

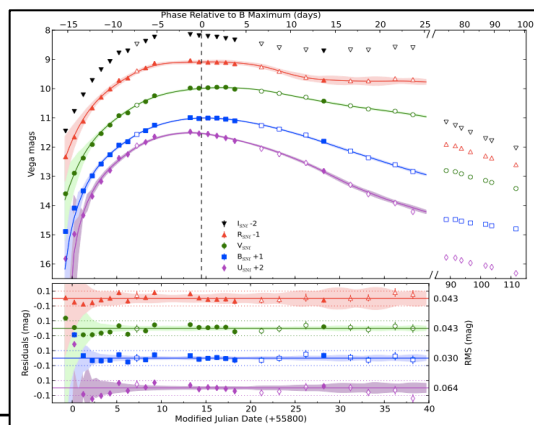


Primary standards

STIS Observation of WDs:
G191B2B, GD153, GD71



Science objects SNe, WDs,...

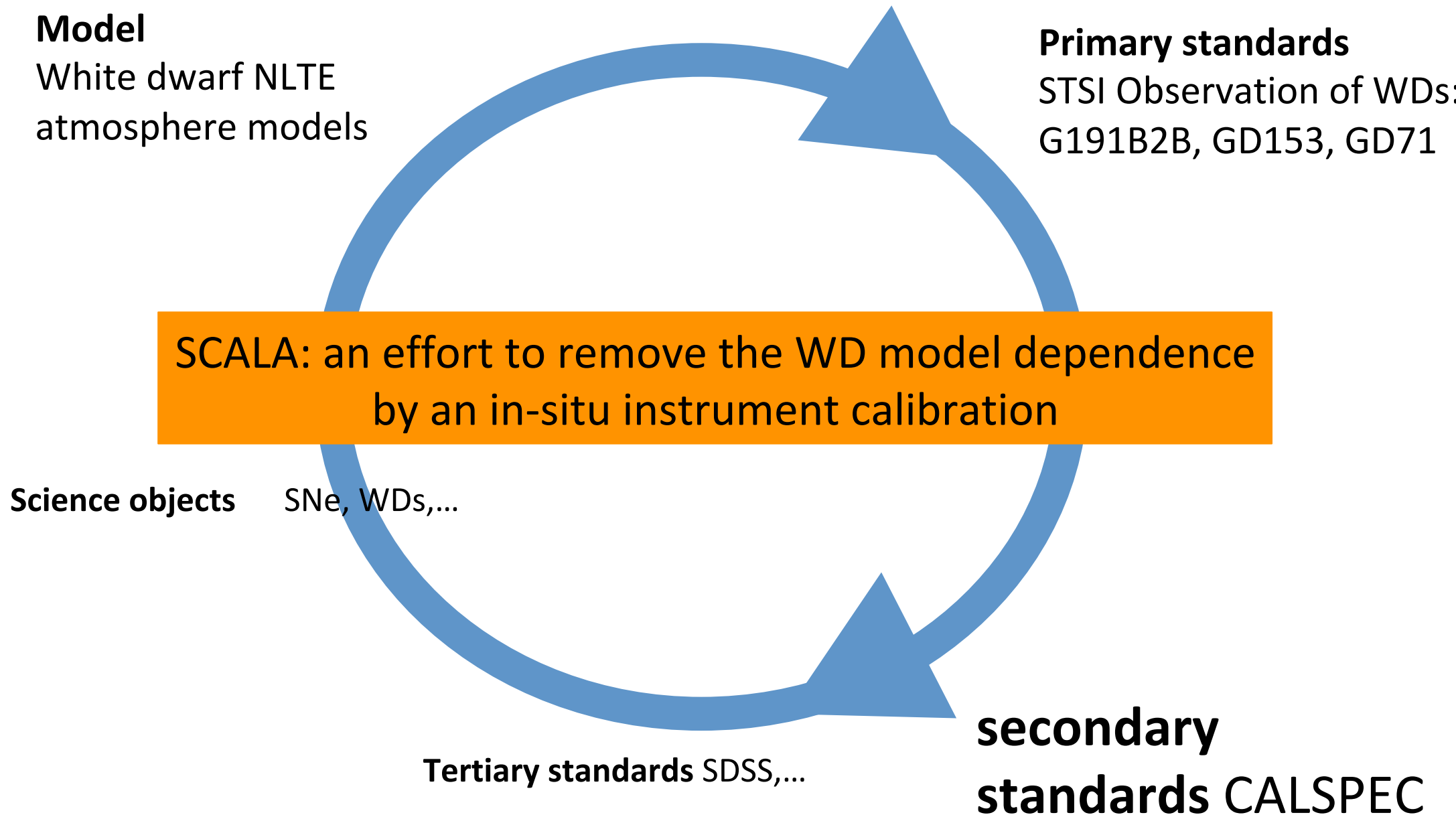


Tertiary standards SDSS,...

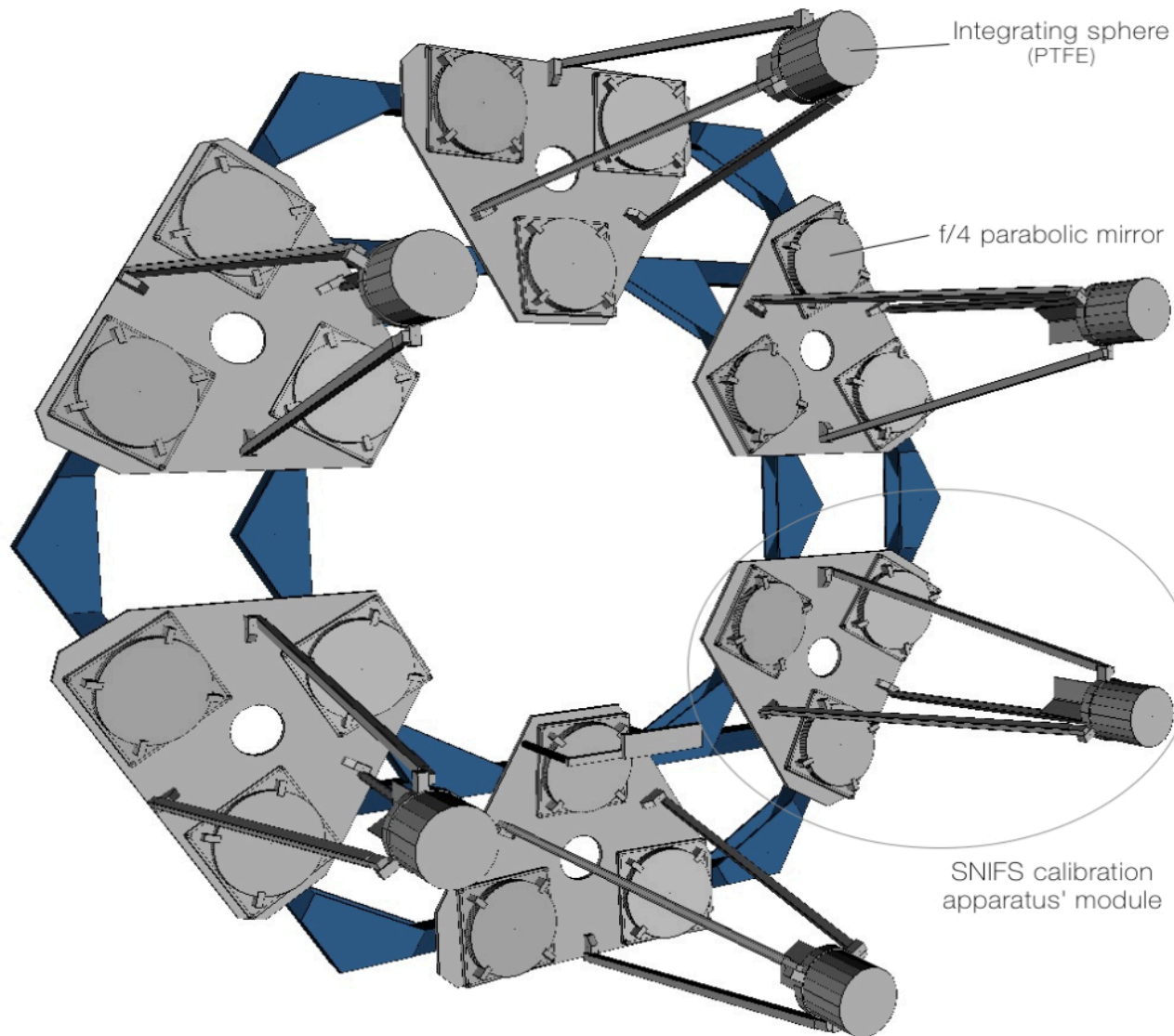
secondary
standards CALSPEC

The problem of Flux calibration

Bohlin & Gordon 2014



SNIFS Calibration Apparatus (SCALA)

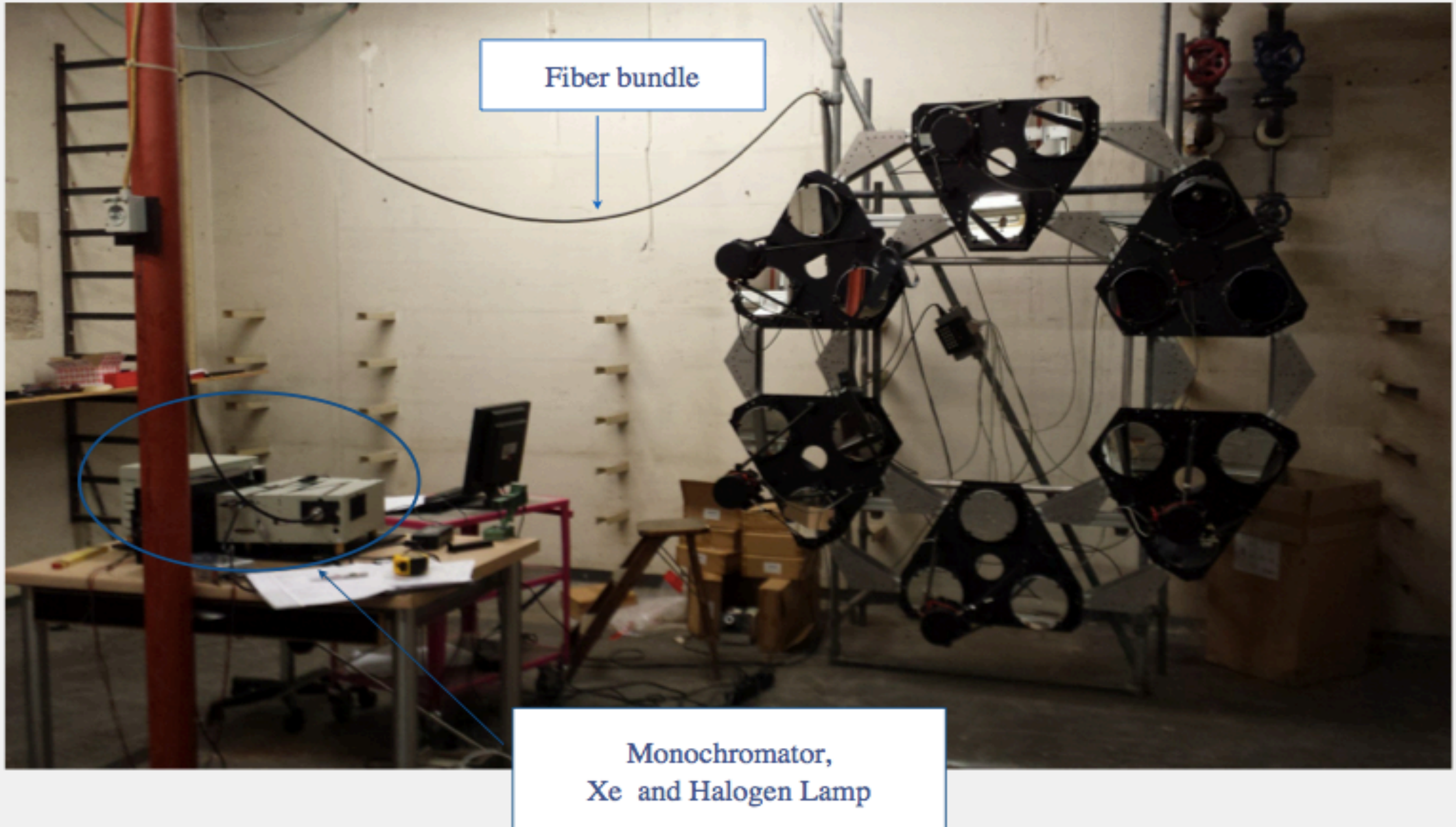


- Tunable wavelength
- Mirrors illuminated by integrating spheres
- 1 degree wide, flat beams
- Photon flux monitored through calibrated PDs.

“artificial planet”

SNIFS Calibration Apparatus (SCALA)

⇒ Flux calibration of instrument with artificial light source



SNIFS Calibration Apparatus (SCALA)



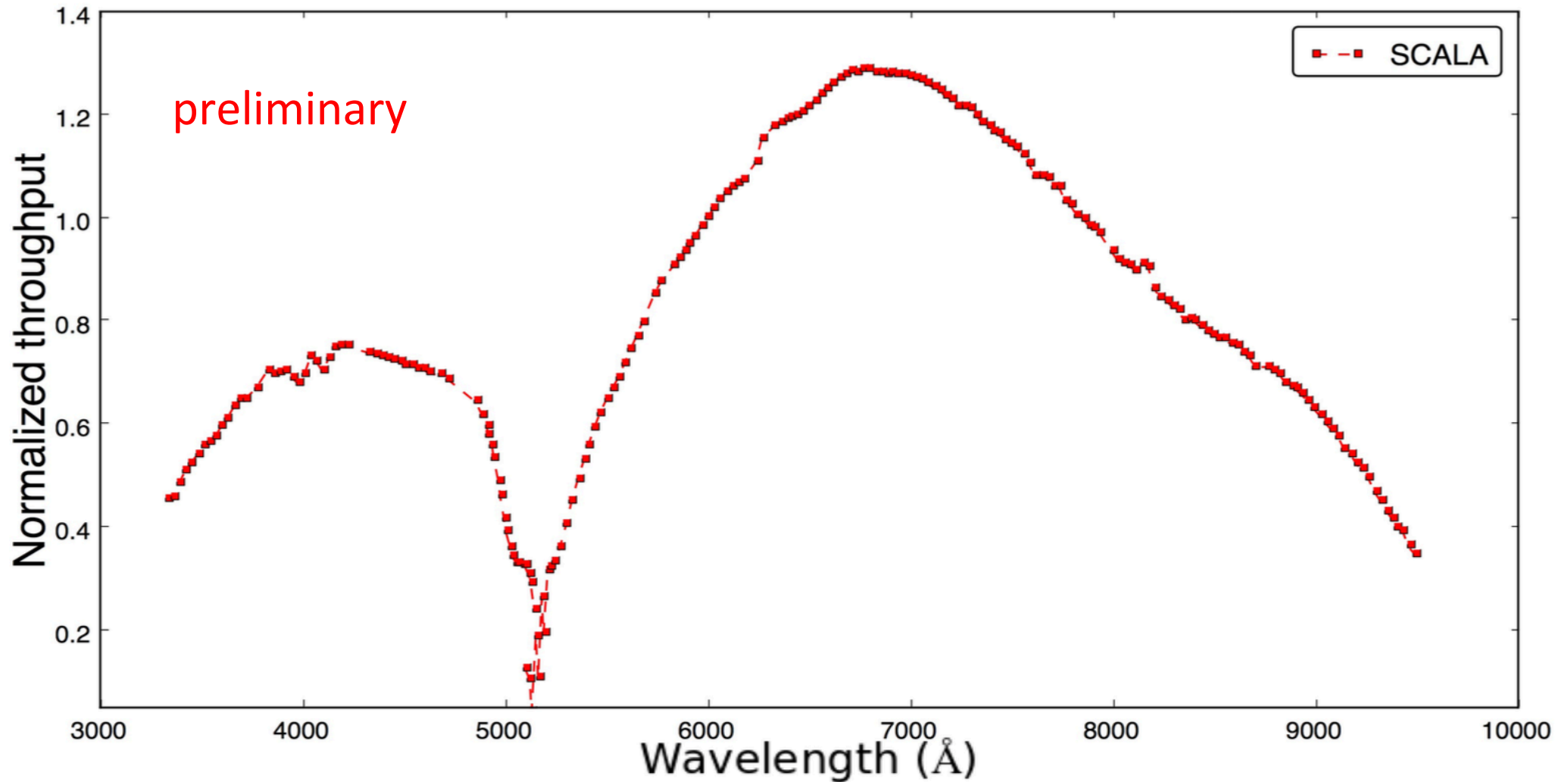
Tunable and flux calibrated
monochromatic flatfield

SNIFS Calibration Apparatus (SCALA)



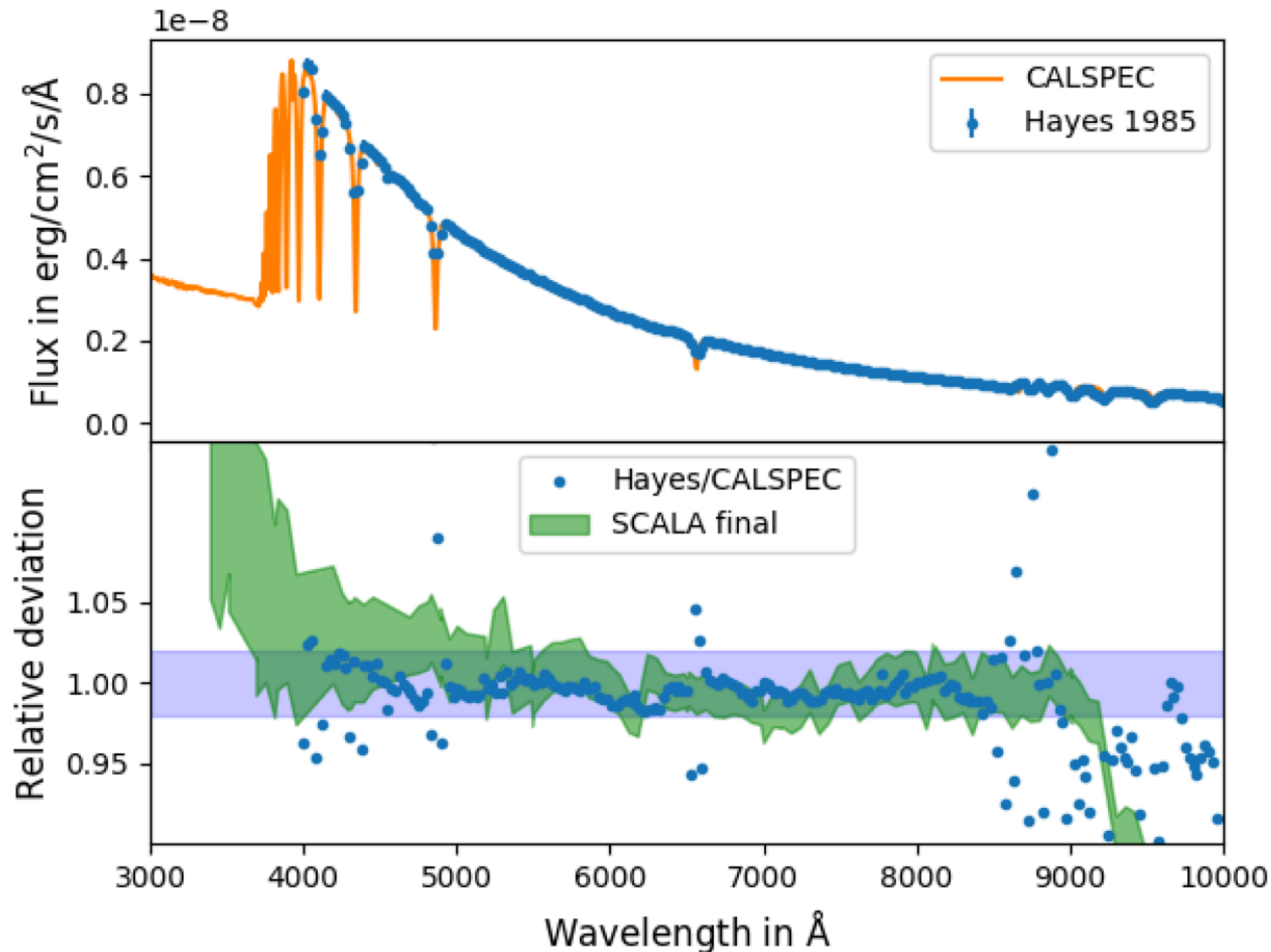
Tunable and flux calibrated
monochromatic flatfield

SNIFS throughput



→ allows to provide bottom up-calibration of standard star network

SNIFS vs Standard stars: $\sim 1\%$ agreement

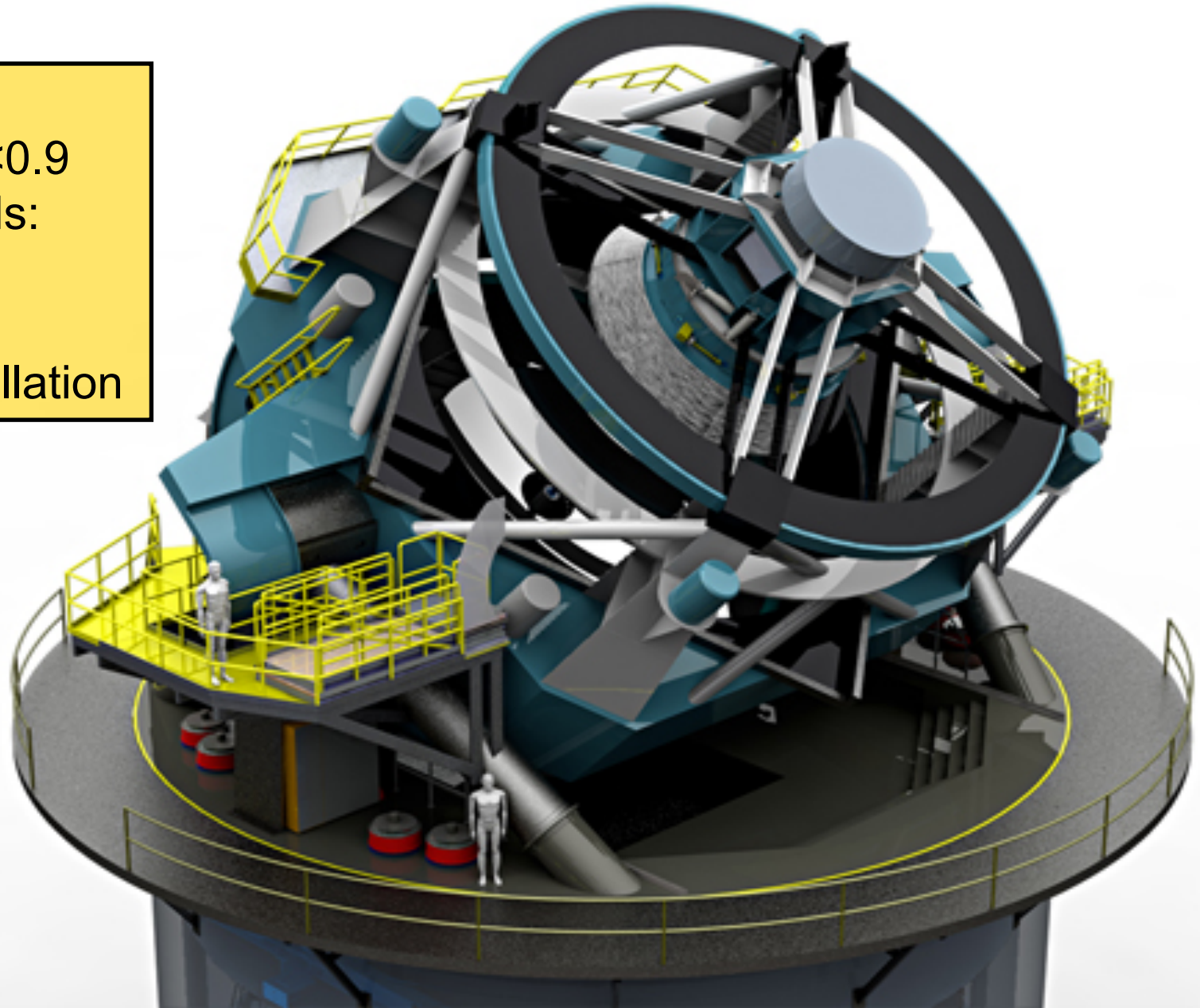


Outlook

The Large Synoptic Survey Telescope

Starting 2022:
~ 10^5 SNe / yr @ $0.1 < z < 0.9$
Other important methods:
✓ Weak lensing
✓ Cluster rates
✓ Baryon acoustic oscillation

8.4 m diameter
9.6 sq.deg FOV
 3.2×10^9 pixels
15 s exposures

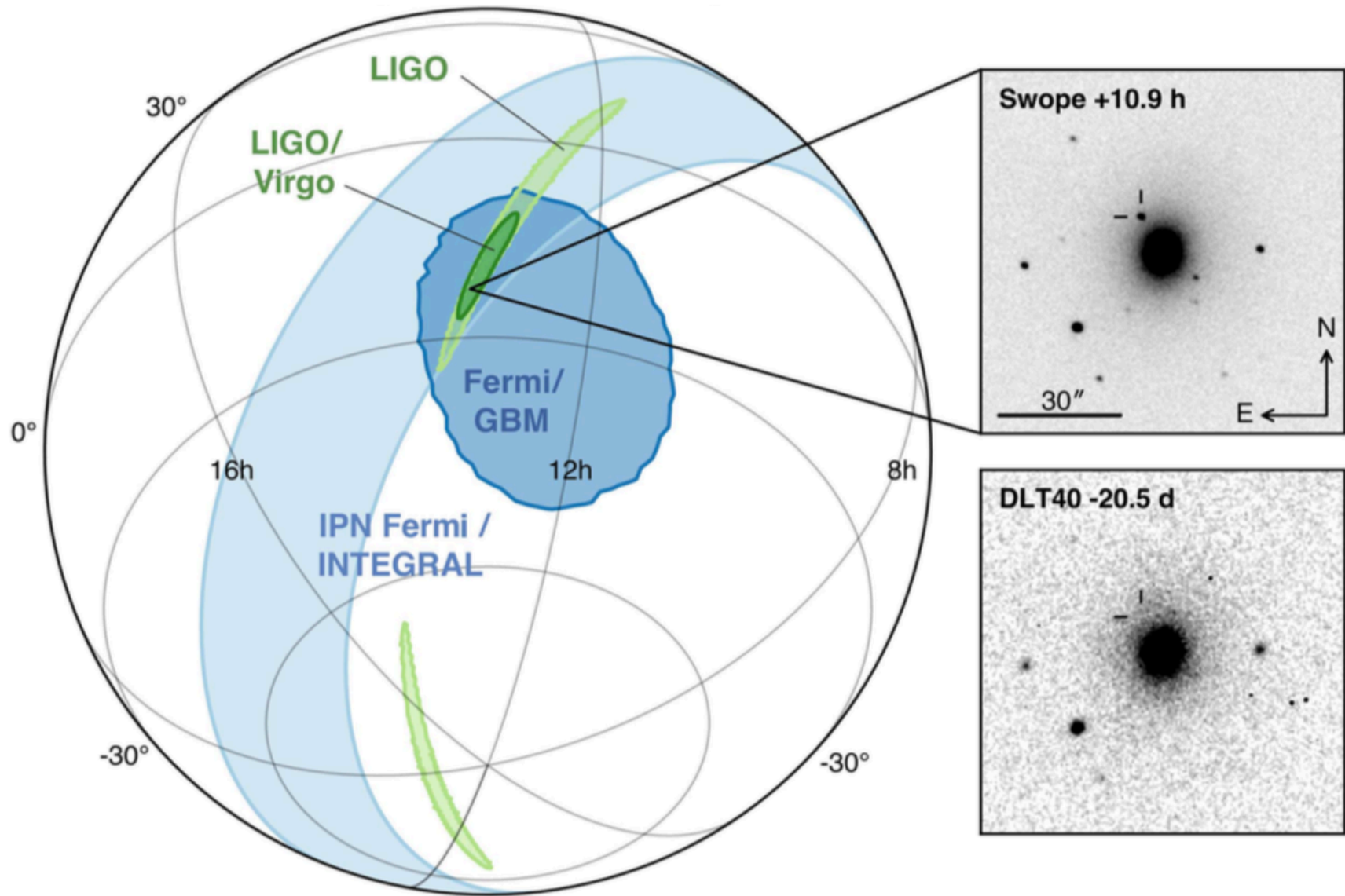


Multi-messenger cosmology: Hubble constant

“I report here how gravitational wave observations can be used to determine the Hubble constant, H_0 . [...] **The signal is easily identified** and contains enough information to determine the **absolute distance to the binary**, independently of any assumptions about the masses of the stars. Ten events out to 100 Mpc may suffice to measure the Hubble constant to 3% accuracy.”

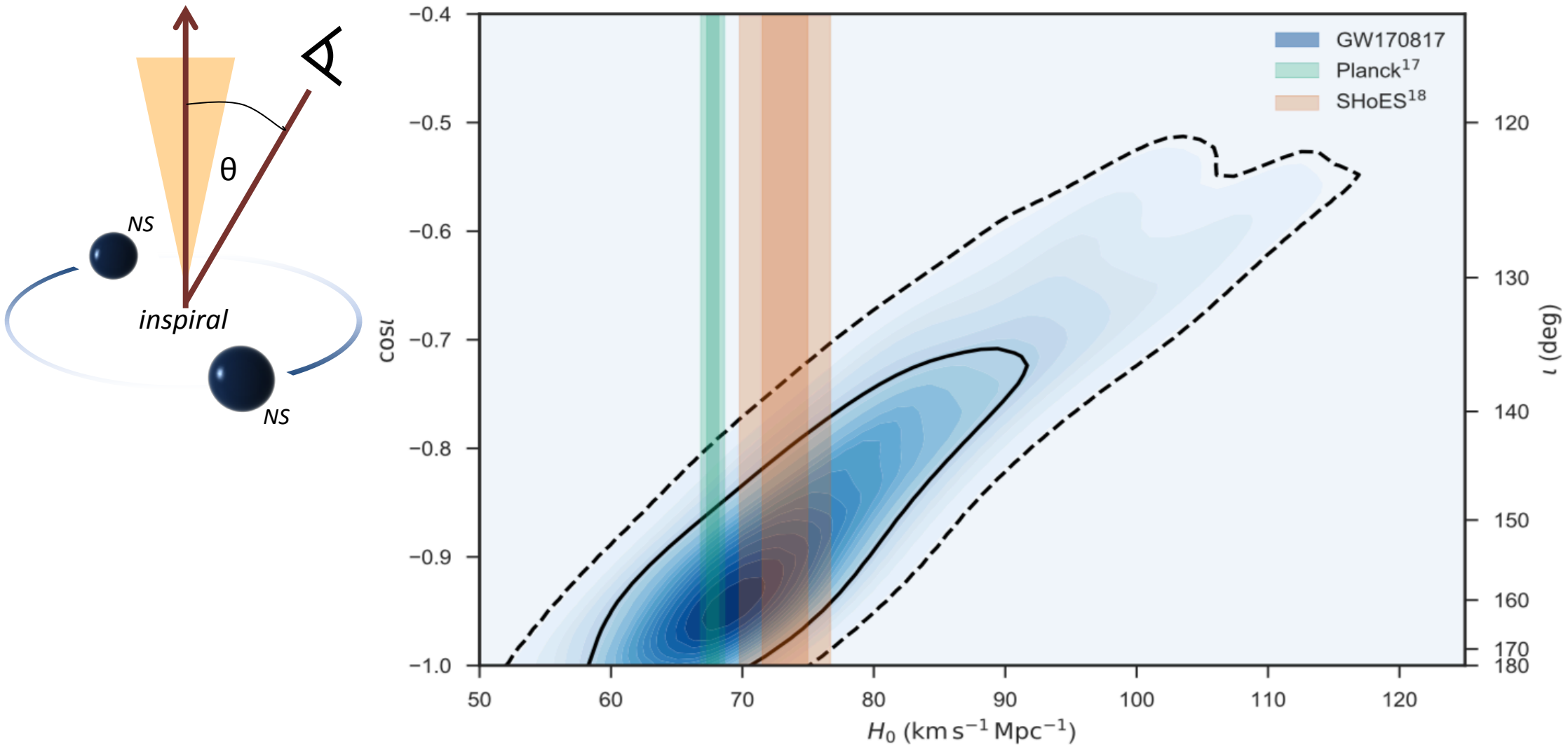
- *Bernard Schutz, Nature 1986*

Multi-messenger cosmology: Hubble constant

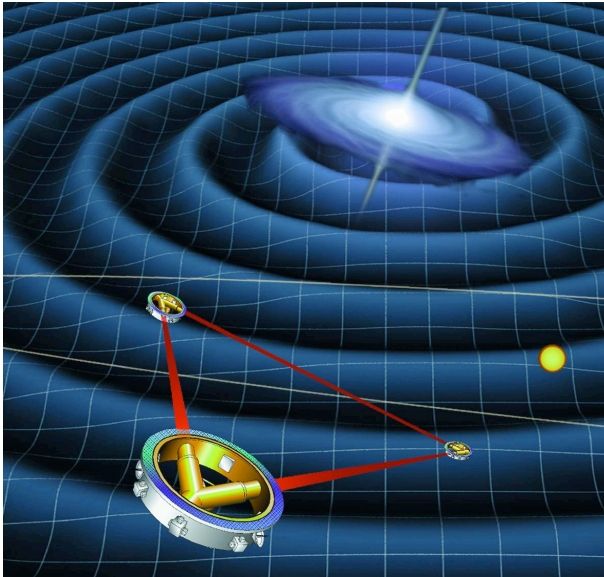


Multi-messenger cosmology: Hubble constant

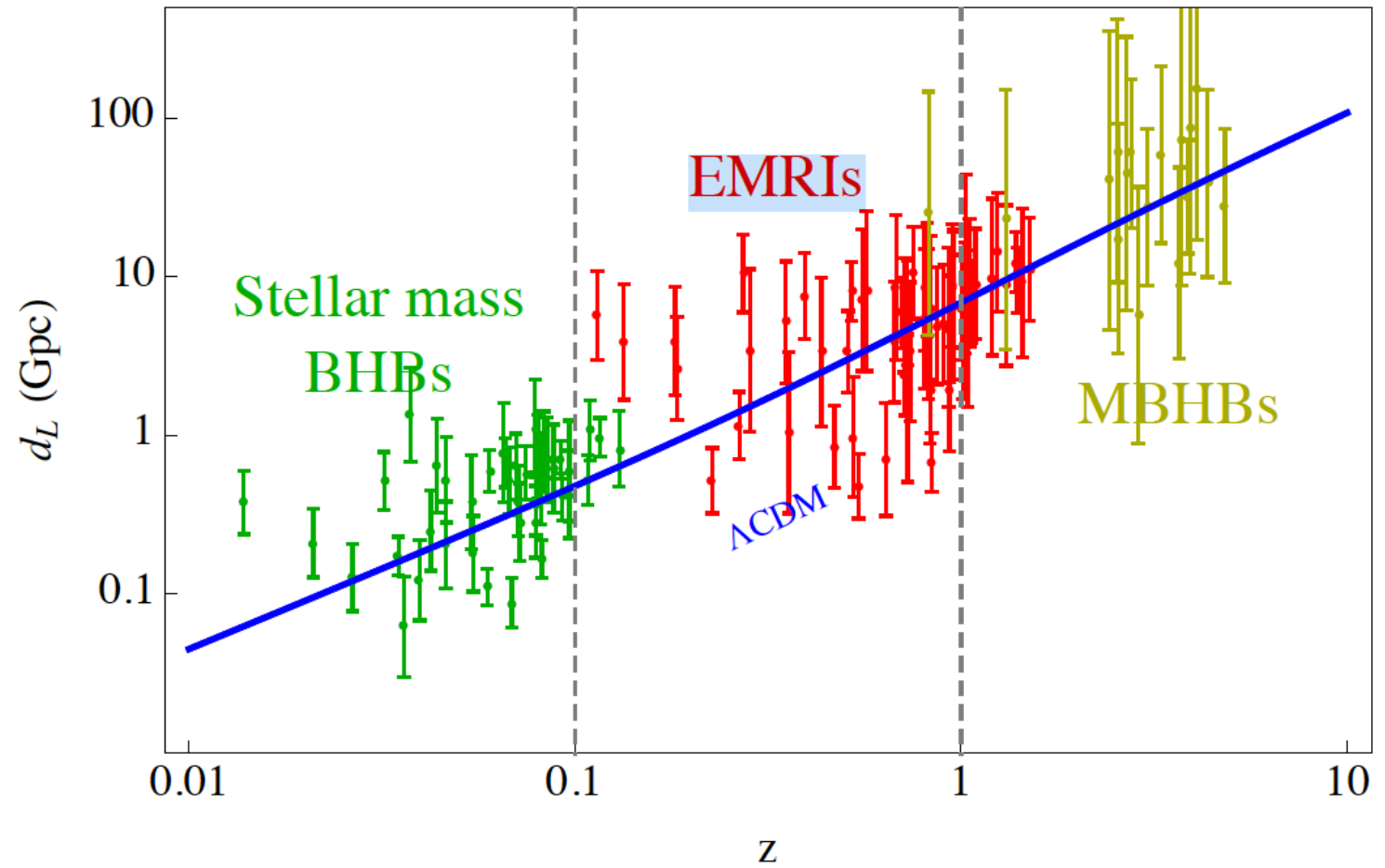
$$H_0 = 70^{+12}_{-8} \text{ km s}^{-1} \text{ Mpc}^{-1}$$



GW 2030+



Example of possible LISA cosmological data



Summary

- Cosmology today is about precision
- Multiple probes for highest sensitivity
- Λ CDM looks strong so far – despite interpretational problems with dark energy
- Many new surveys committed, hence much progress expected!