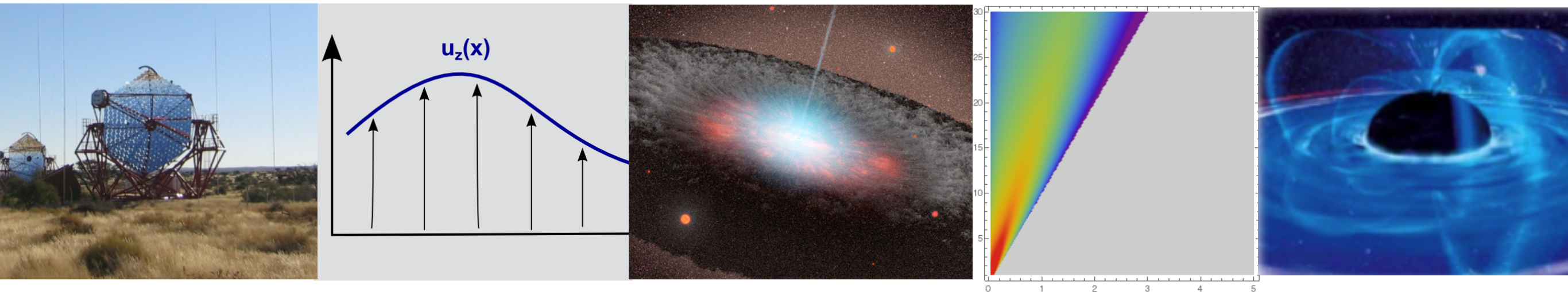


Cosmic (Particle) Accelerators II

- Sources & Mechanisms -

Frank M. Rieger
ISAPP School
Heidelberg, May 28, 2019



ITA Univ. Heidelberg

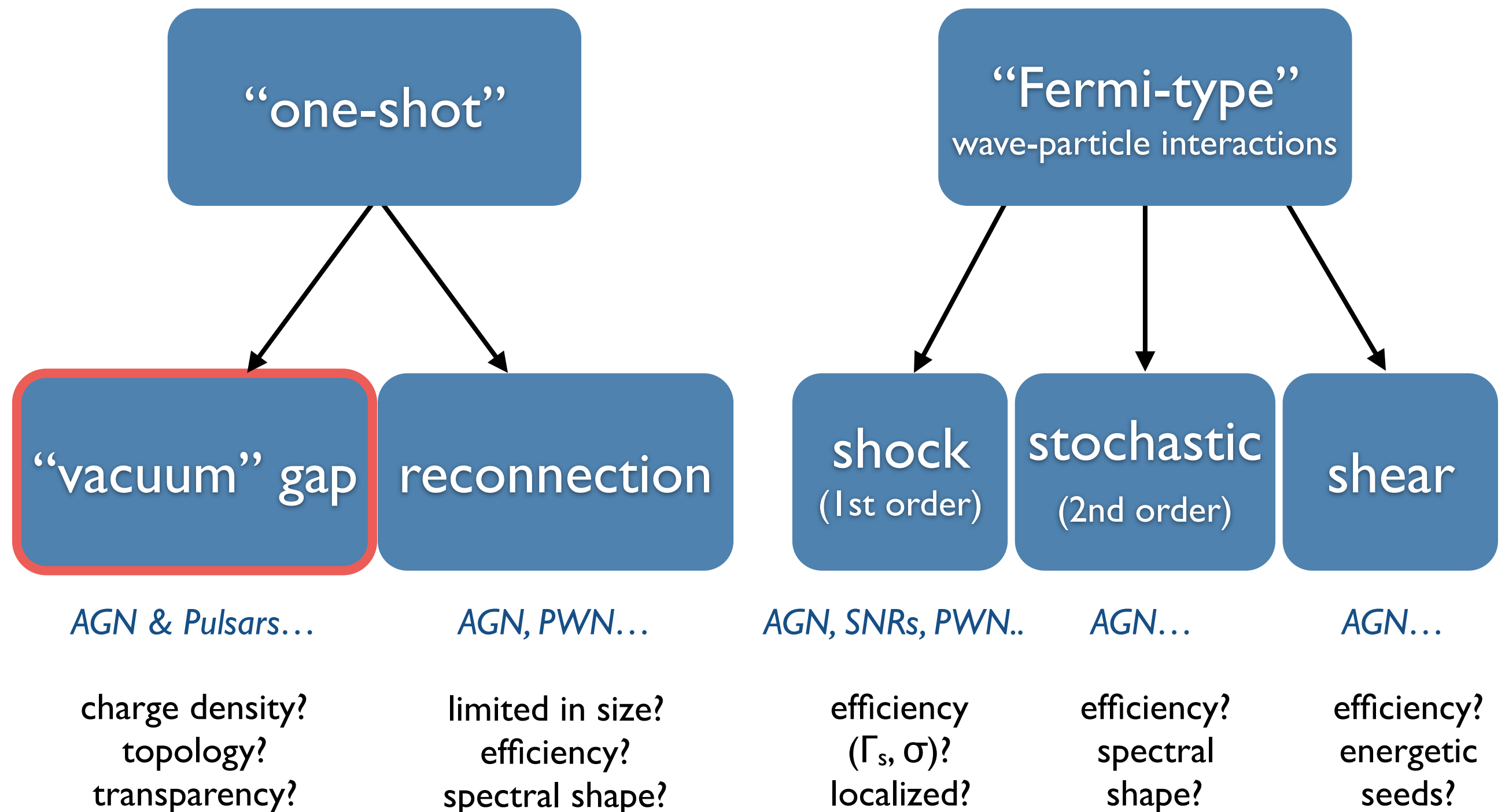


**Max Planck Institut
für Kernphysik**
Heidelberg, Germany

Outline

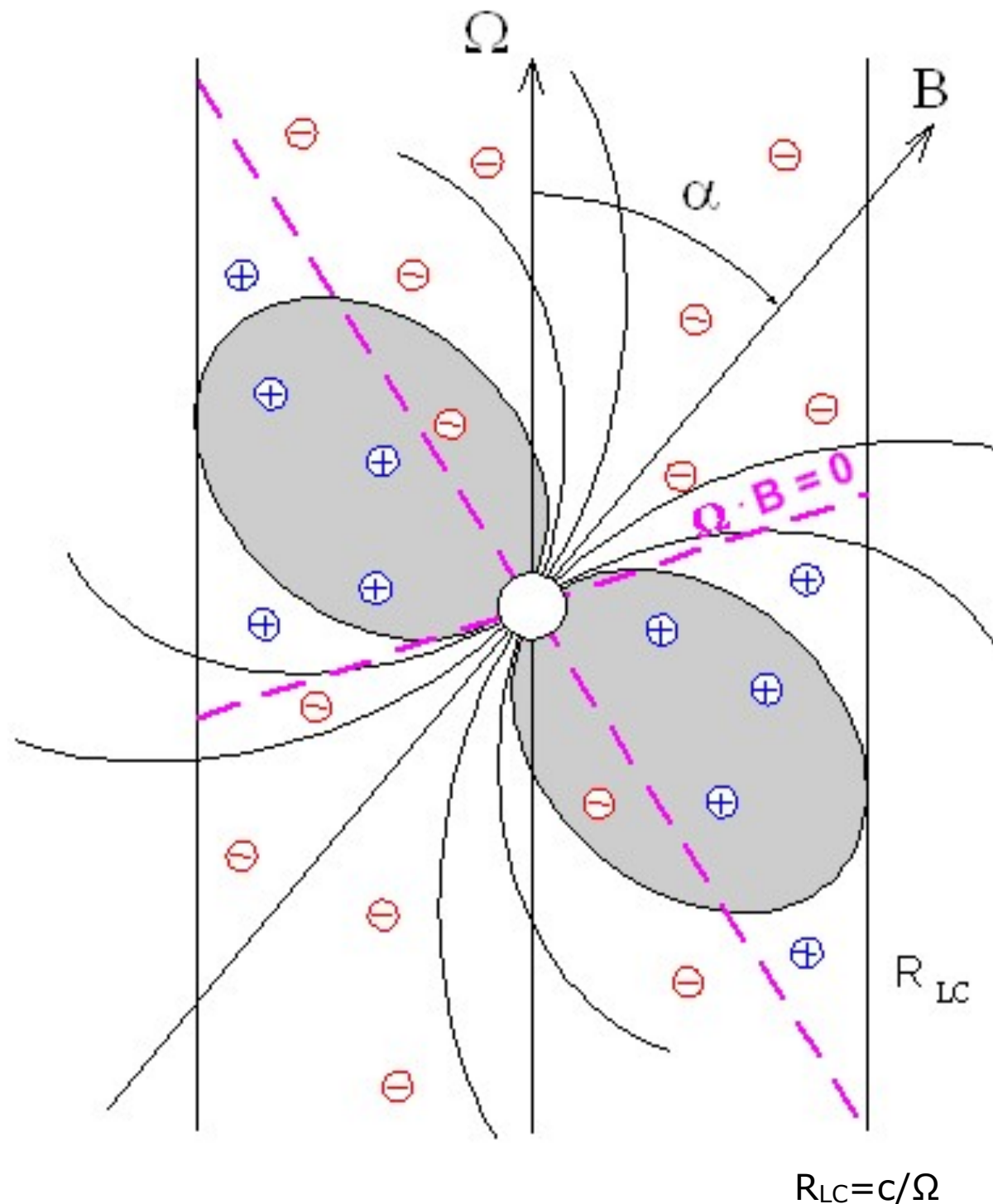
- Particle Acceleration Mechanisms
- *Gap-type particle acceleration* (pulsars, black holes)
 - ▶ concept & relevance
- *Fermi-type particle acceleration*
 - ▶ stochastic 2nd order Fermi
 - ▶ shock acceleration - 1st order Fermi (SNR)
 - ▶ shear acceleration (AGN)
- Conclusions

Possible Acceleration Processes & Sites (*not exhaustive*)



The Occurrence of Gaps in Pulsar Magnetospheres I

Goldreich & Julian 1969



- in vacuum: $e E_{||} \gg F_{\text{grav}}$ at surface
 - vacuum conditions cannot exist

- if enough charges, force-free conditions possible:

$$\vec{E} = -(\vec{v} \times \vec{B})/c = -([\vec{\Omega} \times \vec{r}] \times \vec{B})/c$$

- Goldreich-Julian charge density:

$$\rho_{GJ} = \frac{\vec{\nabla} \cdot \vec{E}}{4\pi} \simeq -\frac{\vec{\Omega} \cdot \vec{B}}{2\pi c}$$

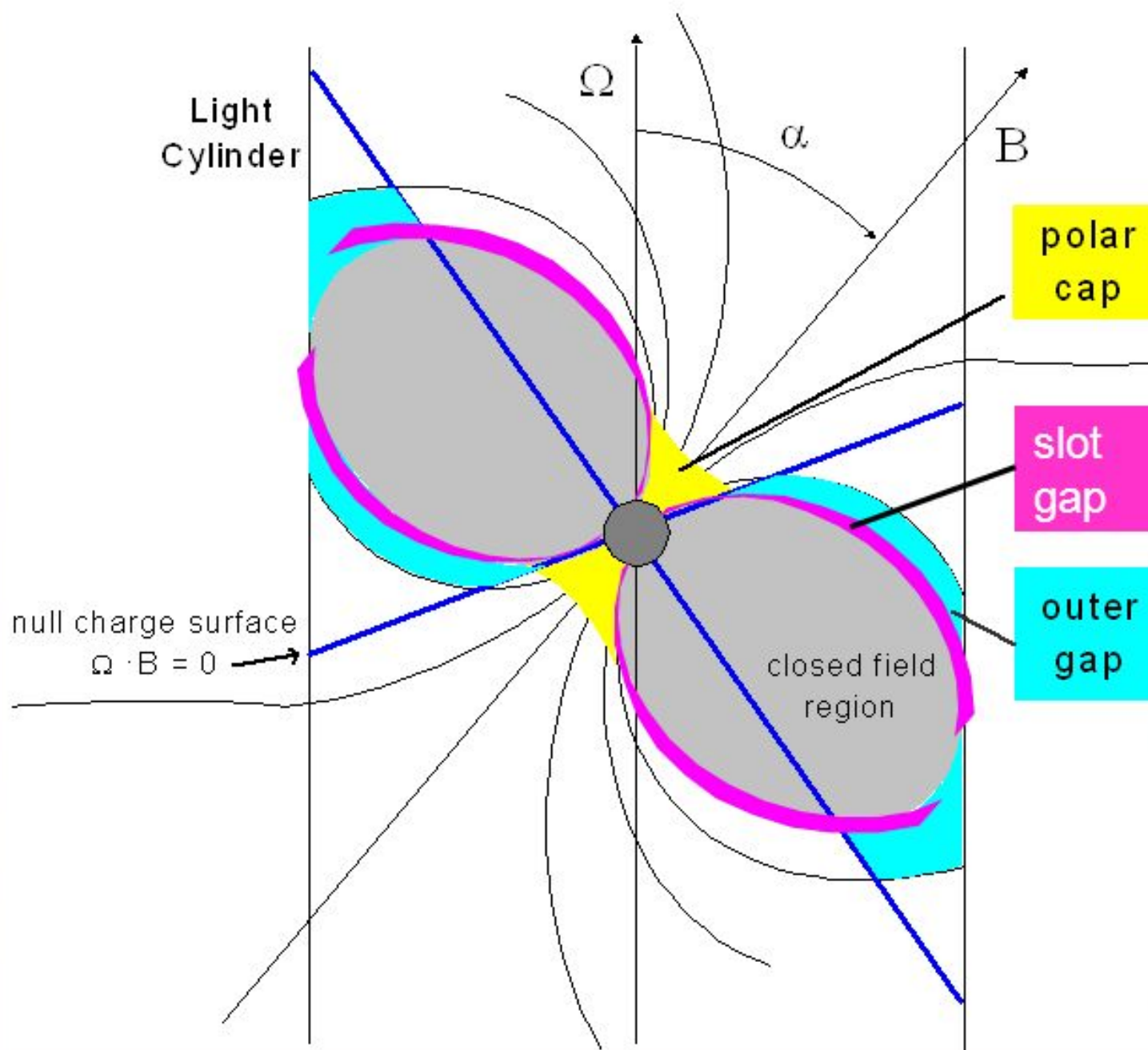
- co-rotating dipole magnetic field defines null charge surface

$$\begin{aligned} \vec{B} &\propto (2 \cos \theta \vec{e}_r + \sin \theta \vec{e}_\theta) / r^3 \\ \Rightarrow \rho_{GJ}(r) &\propto (\sin^2 \theta - 2 \cos^2 \theta) / r^3 \end{aligned}$$

- **no particle acceleration ($E_{||} = 0$)**

The Occurrence of Gaps in Pulsar Magnetospheres II

Possible sites of particle acceleration



(Credits: A. Harding)

- ideal MHD in most of magnetosphere: $\vec{E} \cdot \vec{B} = 0$

- deficient charge supply:

$$\vec{E} \cdot \vec{B} \neq 0$$

\Rightarrow particle acceleration

- Solve Gauss' law:

$$\vec{\nabla} \cdot \vec{E} = 4\pi(\rho - \rho_{GJ})$$

(e.g., Ruderman & Sutherland 1975; Cheng et al. 1985; Muslimov & Harding 2003)

The Occurrence of Gaps in BH Magnetospheres

► Null surface in Kerr Geometry ($r \sim r_g \equiv GM/c^2$)

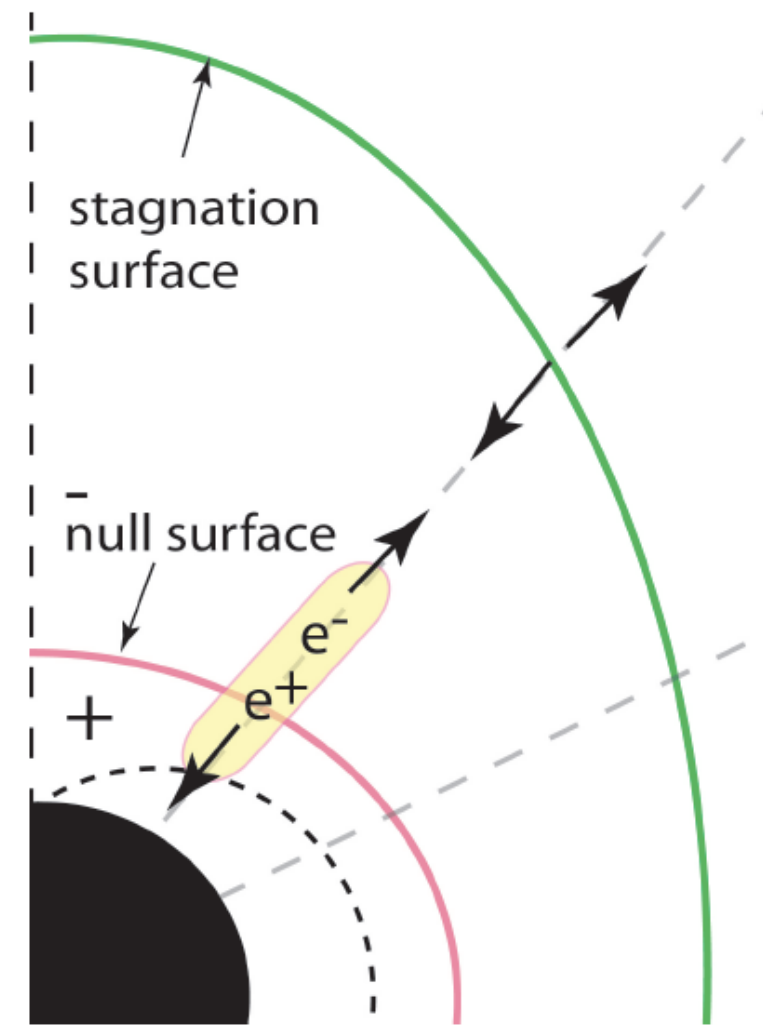
for force-free magnetosphere, vanishing of poloidal electric field $\mathbf{E}_p \propto (\Omega^F - \omega) \nabla \Psi = 0$, ω = Lense-Thirring

$\Rightarrow \rho_{GJ}$ changes sign, “gap” may easily develop

► Stagnation surface ($r \sim \text{few } r_g$)

Inward flow of plasma below due to gravitation field
outward motion above

\Rightarrow charges need to be continuously replenished

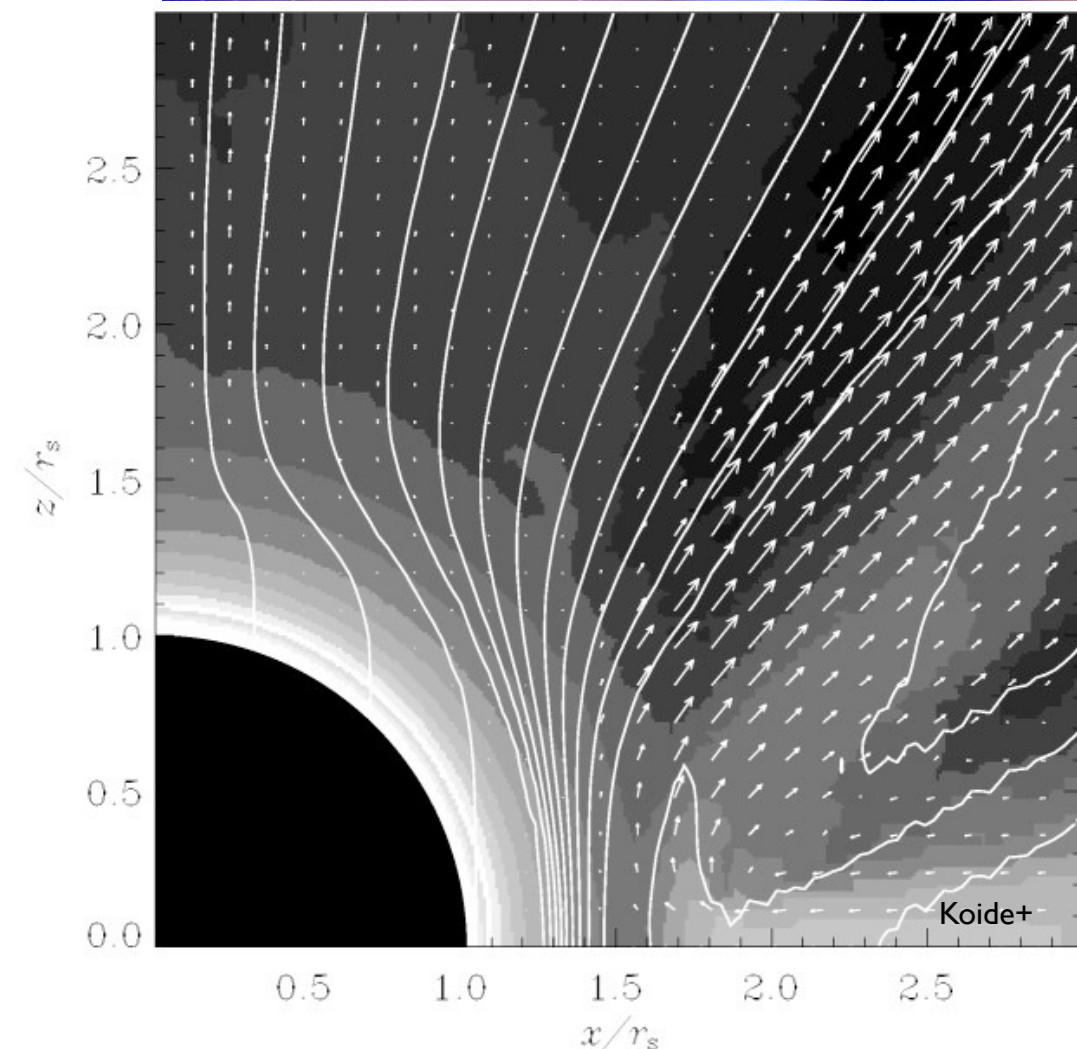


Levinson & Segev 2017

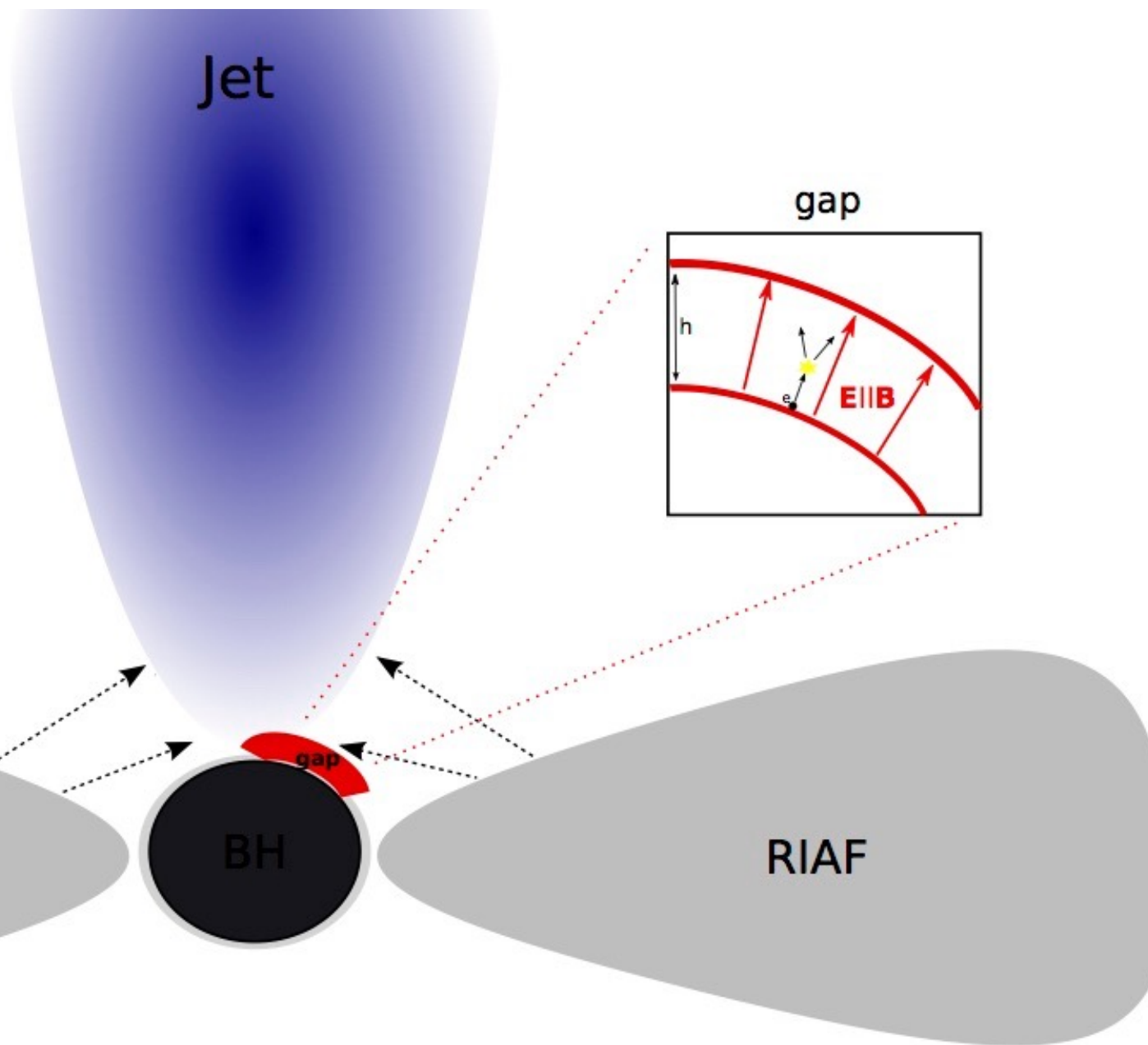
(e.g., Blandford & Znajek 1977; Beskin et al. 1992, Hirotani & Okamoto 1998)

The Conceptual Relevance of BH Gaps

- *BH-driven jets (Blandford-Znajek)*
 - ▶ *Self-consistency*: Plasma source needed to ensure force-free MHD
- *Non-thermal Particle Acceleration*
 - ▶ *Implication*: efficient (direct) acceleration of electrons & positrons
- *Radiation & Pair Cascade.....*
 - ▶ *Features*: expect γ -ray production,
 - ▶ $\gamma\gamma$ -absorption triggers **pair cascade**
 - ▶ generating charge multiplicity
 - ▶ ensuring electric field screening (closure)



Gamma-Ray Emission from AGN Magnetospheres



- *Direct electric field acceleration:*

Rate of energy gain for electron:

$$d\gamma/dt \propto e \Delta\phi_{\text{gap}} \cdot (c/h)$$

- *Curvature & Inverse Compton:*

HE γ -rays via curvature: $\nu \sim (0.2c) (\gamma^3/R_c)$

VHE γ -rays via IC: $h\nu \lesssim \gamma m_e c^2$

- *Accretion environment (RIAF):*

Radiatively inefficient needed to facilitate escape of VHE photons

- *Maximum Gap luminosity:*

$$L_{\text{gap}} \propto n_{\text{GJ}} (\text{Volume}) (d\gamma/dt)$$

Characterizing the Magnetospheric Potential

$$\frac{dE_{||}}{dh} = 4\pi (\rho_e - \rho_{GJ}) \quad \text{''Gauss' law''}$$

Possible boundary conditions in the pulsar case :

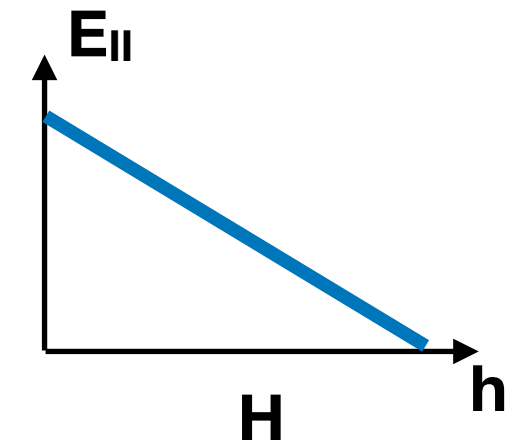
- “*non-free escape*” (Ruderman): $E_{||}(h=0) \neq 0$, $E_{||}(h=H)=0$, $\rho_e \ll \rho_{GJ}$:
- “*free escape*” (Arons): $E_{||}(h=0)=0$, $E_{||}(h=H)=0$, $\rho_e \sim \rho_{GJ}$ ($\rho_e \neq \rho_{GJ} \equiv \Omega B \cos\theta_b$) :

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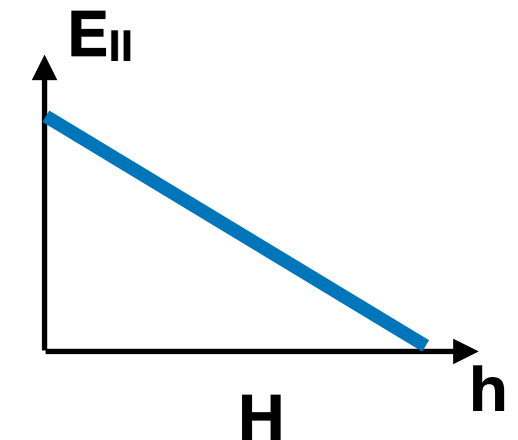
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$$\frac{dE_{||}}{dh} \simeq -4\pi \rho_{GJ} \Rightarrow E_{||}(h) = -4\pi \rho_{GJ} h + \text{const}$$

$$E_{||}(h = H) = 0 \Rightarrow \text{const} = 4\pi \rho_{GJ} H$$

Thus : $E_{||}(h) = E_0 \frac{(H - h)}{H}$, where $E_0 = 4\pi \rho_{GJ} H$



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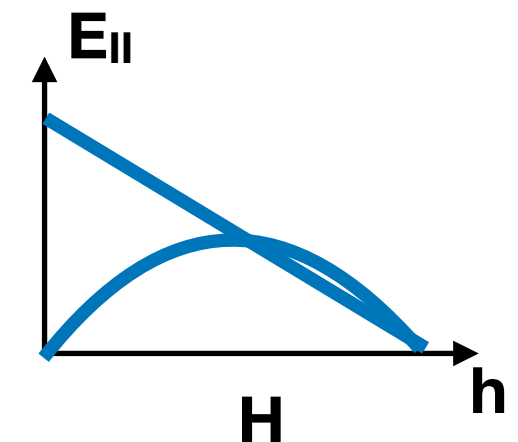
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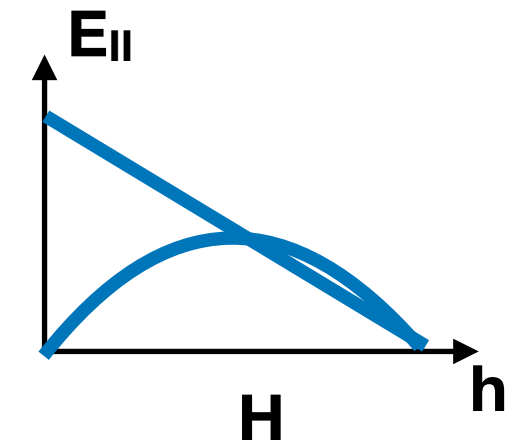
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$$\frac{dE_{||}}{dh} \simeq 4\pi \frac{d(\rho - \rho_{GJ})}{dh} \Big|_{h=H/2} (h - H/2)$$

$$\Rightarrow E_{||}(h) = -E_A \frac{h(H-h)}{H^2} \quad \text{with} \quad E_A = 2\pi \frac{d(\rho - \rho_{GJ})}{dh} H^2$$

Magnetospheric Potential & Jet Power in AGN - *Differences*

Solving Gauss' laws depending on different boundaries

$$\frac{dE_{||}}{dh} = 4\pi (\rho_e - \rho_{GJ}) \quad \text{"Gauss' law"}$$

highly under-dense: $\rho_e \ll \rho_{GJ}$

► Gap potential:

$$\Delta\phi_{\text{gap}} \sim a_{\text{spin}} r_g B (\mathbf{H}/r_g)^2$$

► Constraining losses:

► Curvature, IC...

► Jet power:

$$L_{\text{VHE}} \sim L_{\text{jet}} \times (\mathbf{H}/r_g)^2 \dots$$

e.g., Blandford & Znajek 1982,
Levinson 2000
Levinson & FR 2011

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Katsoulakos & FR 2018

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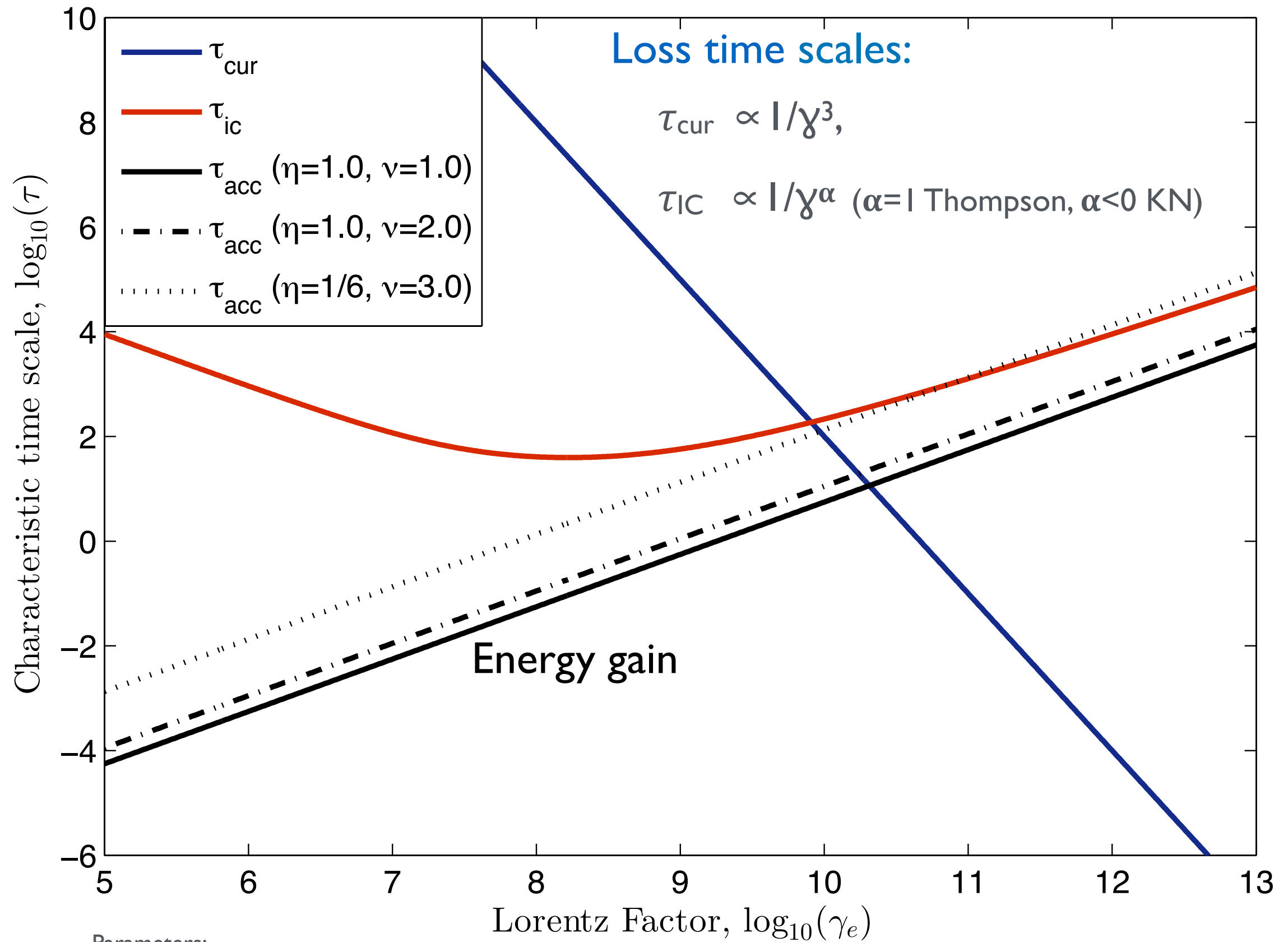
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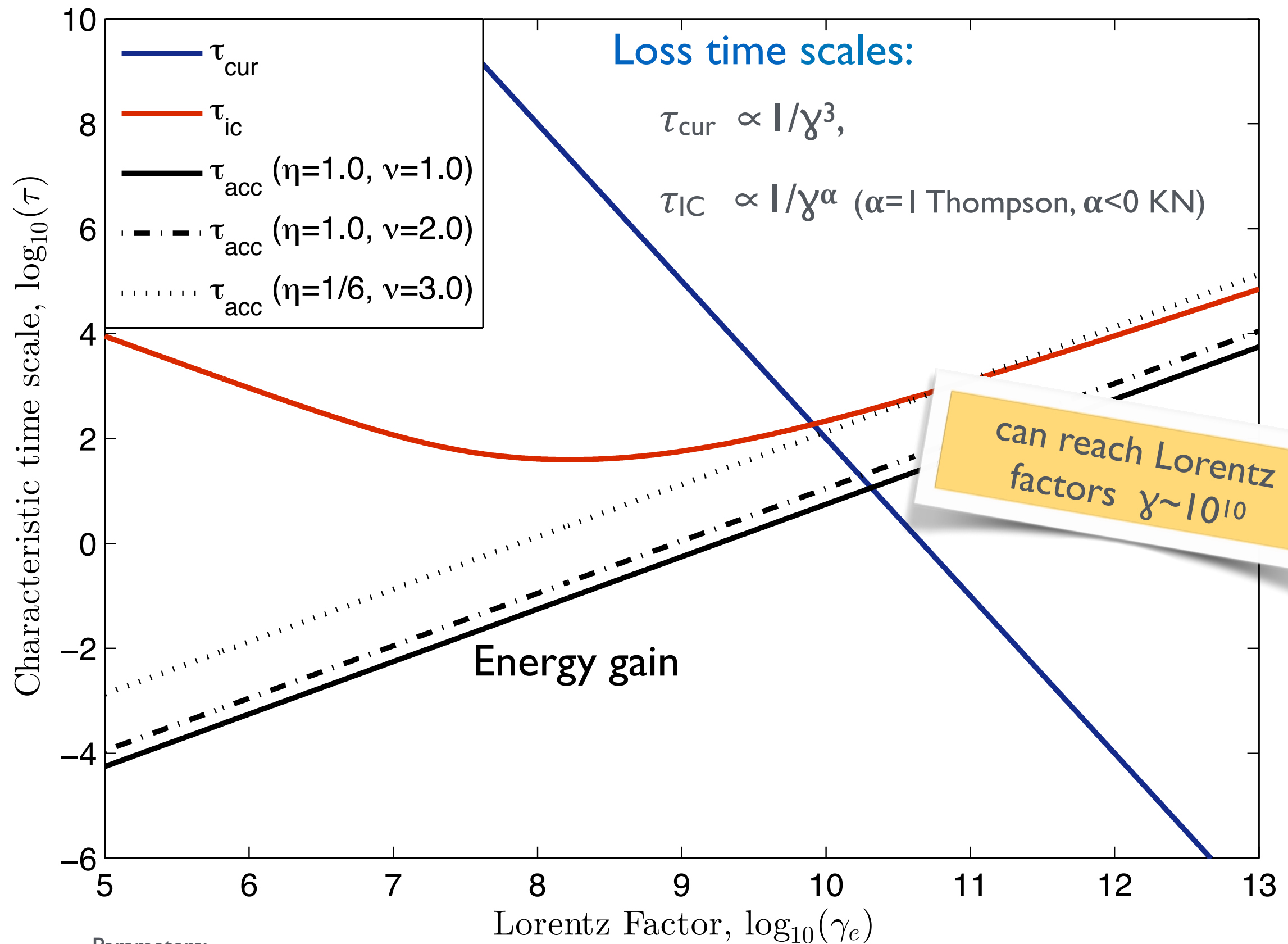
e.g., Hirotani & Pu 2016
Katsoulakos & FR 2018

Jet power constraints
can become relevant

Timescales (example)



Timescales (example)



Example: Phenomenological Relevance of Gaps in AGN

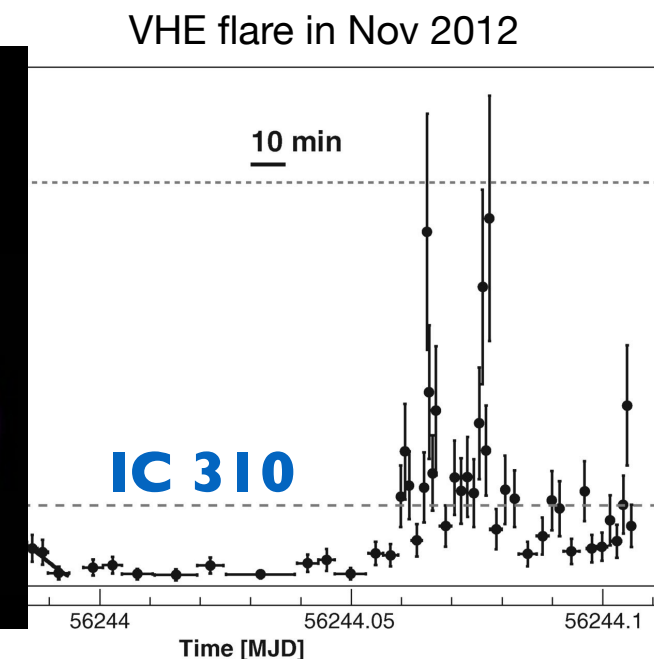
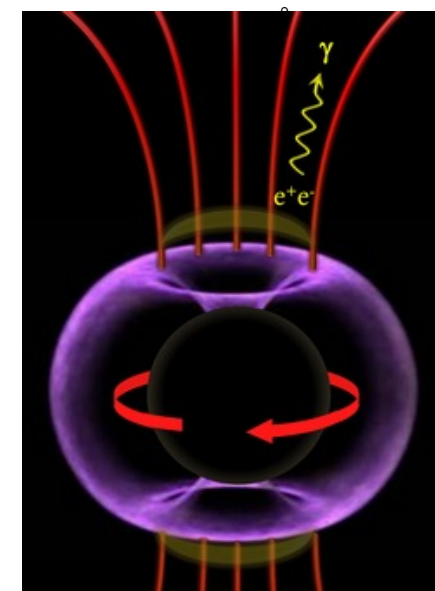
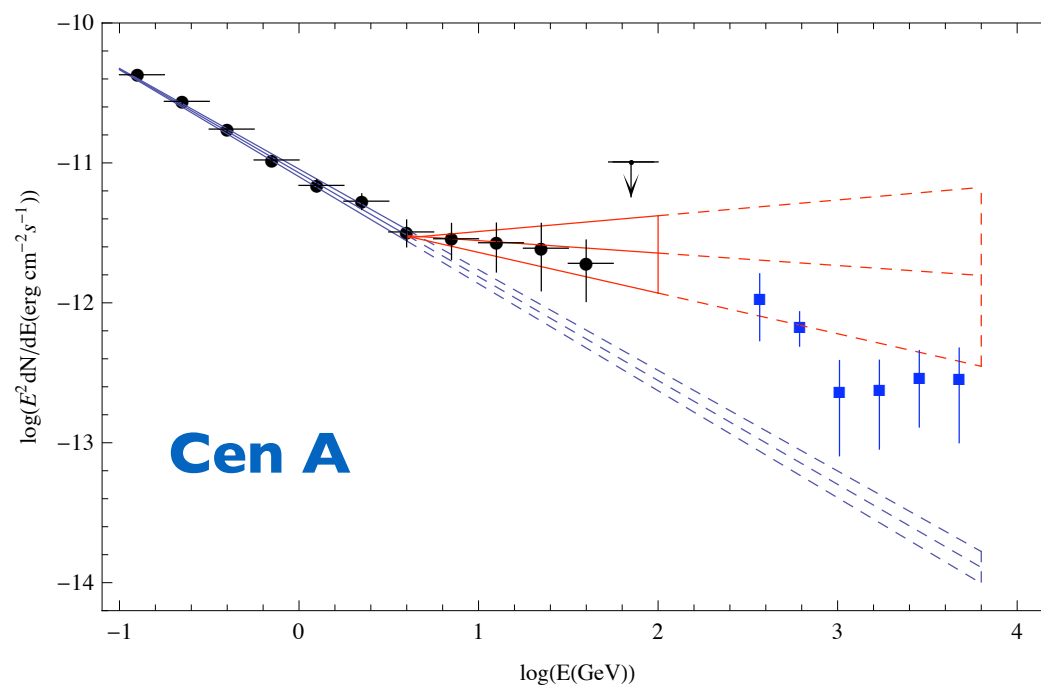
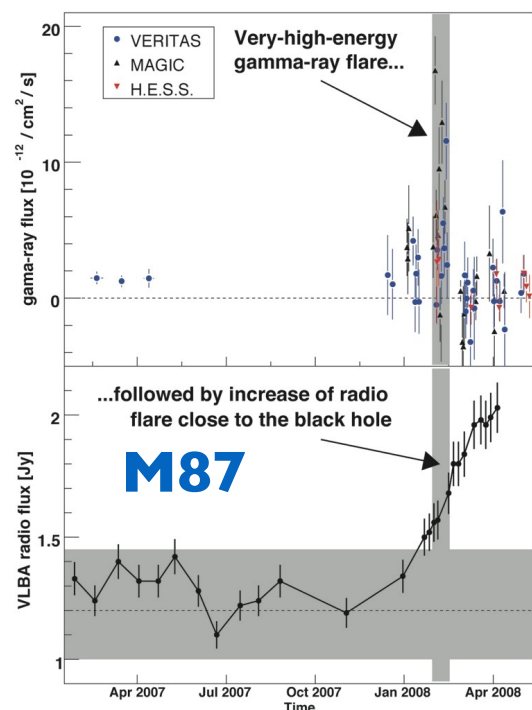
► Gamma-Ray Emission from *Radio Galaxies*:

misaligned jets: moderate Doppler boosting of jet emission only

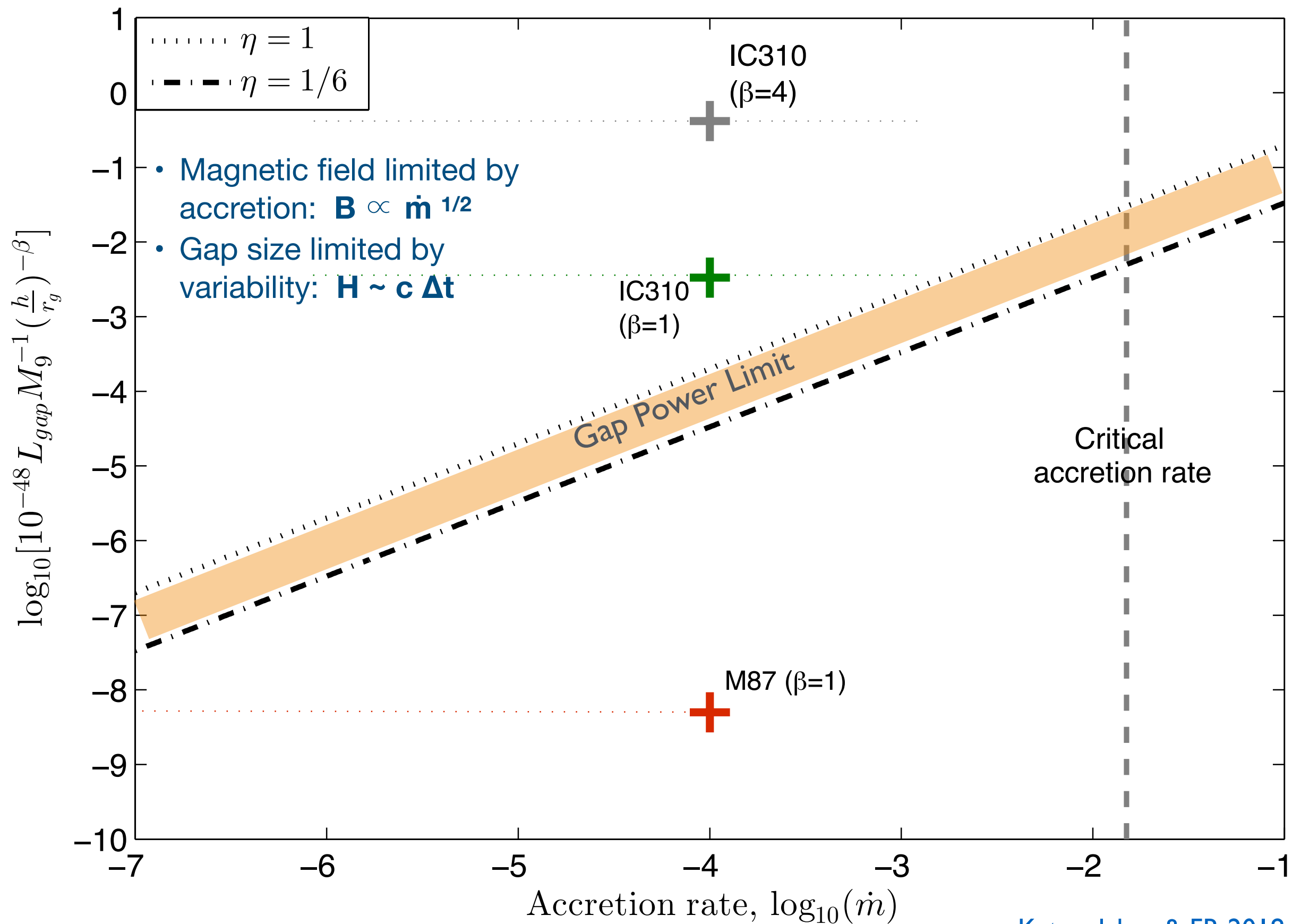
⇒ *gap IC & curvature emission may show up at hard HE-VHE gamma-rays*

► Possibly related to observable AGN features in:

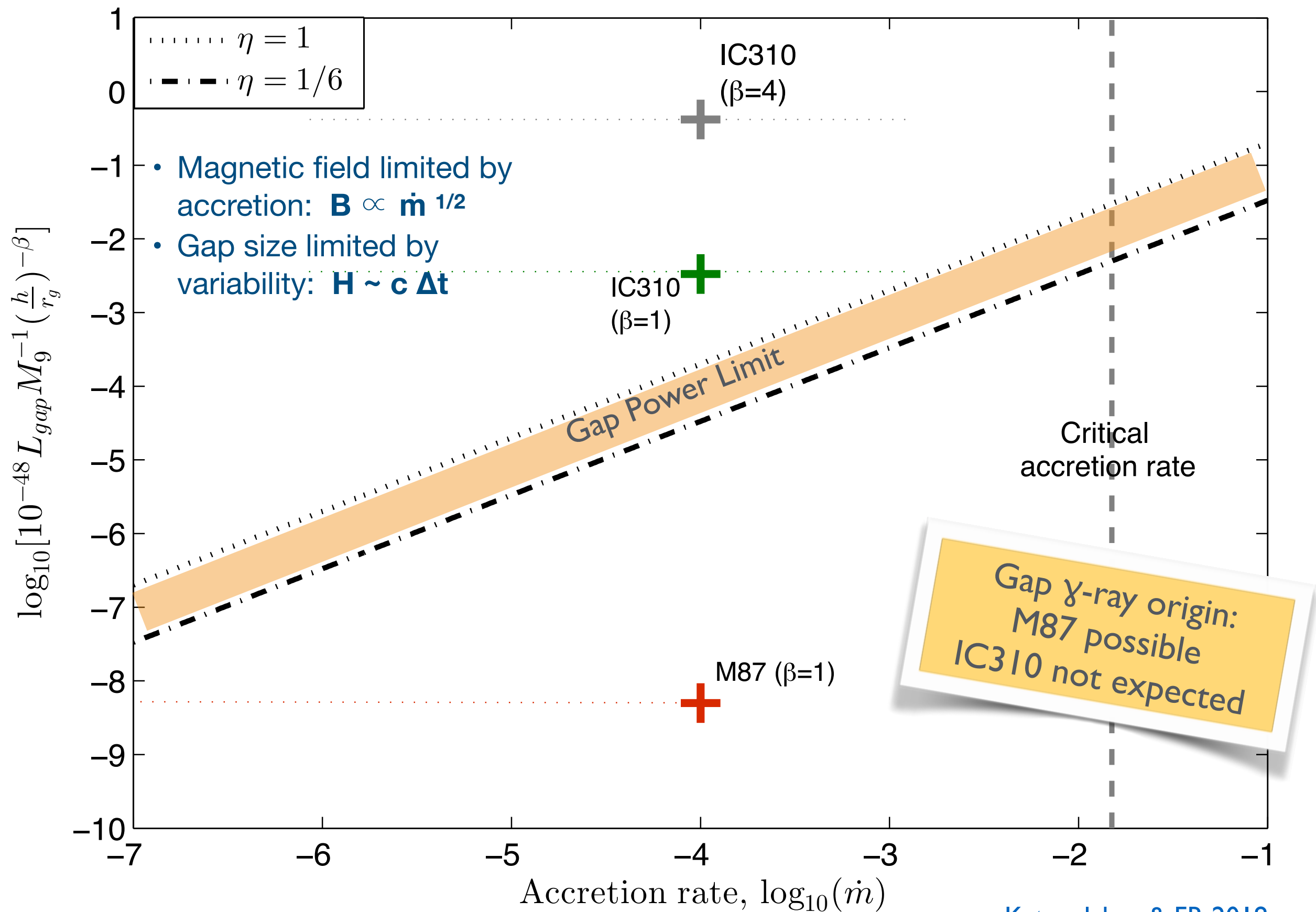
- **M87** (d ~ 17 Mpc): day-scale VHE variability, radio-VHE outburst correlation...
- **Cen A** (d ~ 4 Mpc): spectral hardening of core emission above ~5 GeV...
- **IC 310** (d ~ 80 Mpc): rapid (5 min) VHE variability, huge power ($L_\gamma \sim 10^{44}$ erg/sec)



Example: Maximum Gap Power Constraints



Example: Maximum Gap Power Constraints



Preference for Outer Gap Acceleration in Pulsars ?

- **Polar Cap Acceleration:**

- ▶ absorption via magnetic pair creation,
super-exponential cut-off in gamma-ray emission

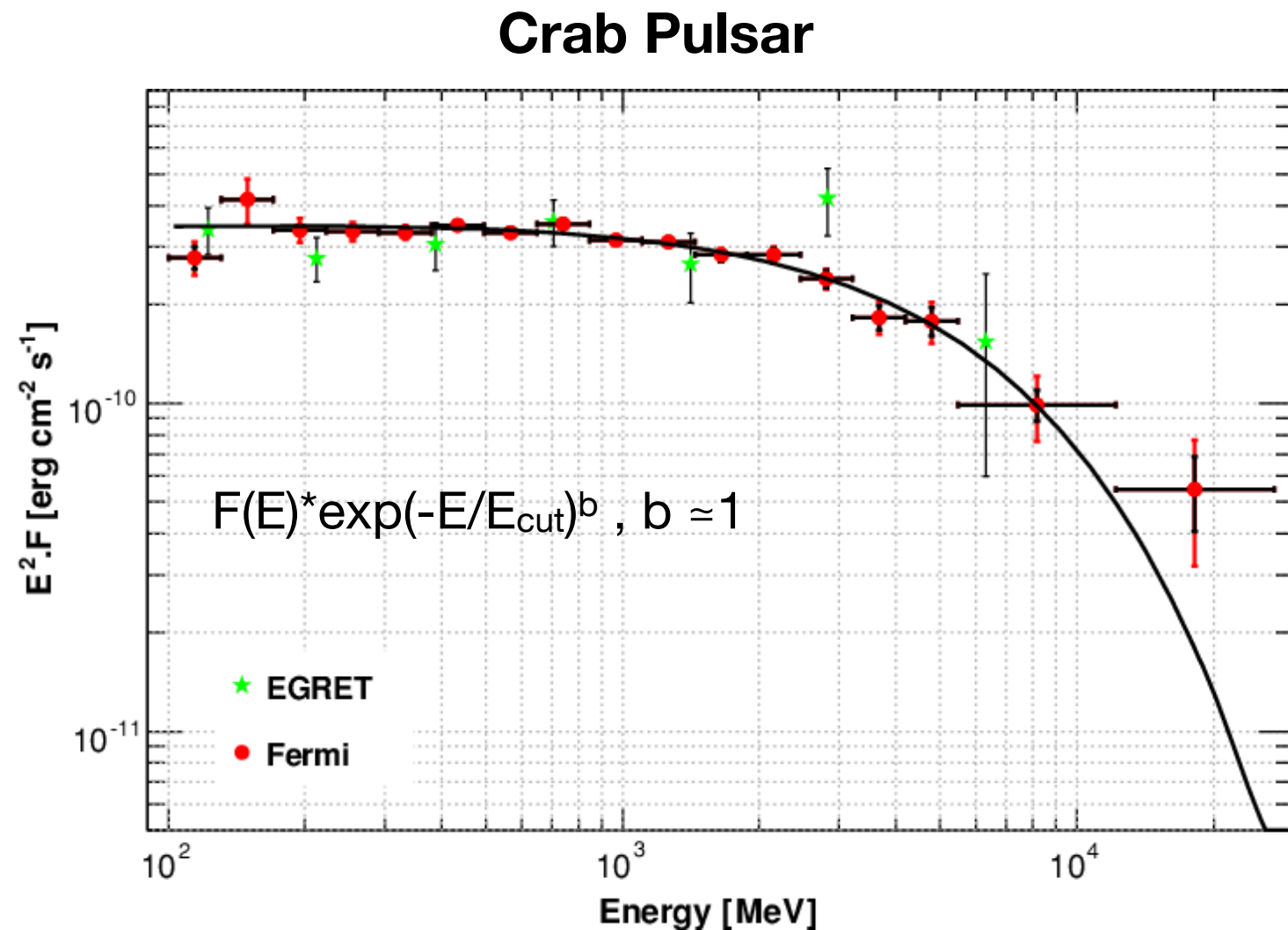
- **Outer Gap Acceleration:**

- ▶ curvature radiation, **exponential cut-off** in gamma-ray emission

- Fermi-LAT HE observations:

- ▶ **super-exponential cutoff excluded**
- ▶ brightest pulsars (Crab, Vela) : even show sub-exponential cut-off
 - ➡ superposition (states & sites) ?
- ▶ cut-offs in narrow band $E_{\text{cut}} \sim 1\text{-}5 \text{ GeV}$
- ▶ compatible with curvature radiation

- origin of TeV (IC)?

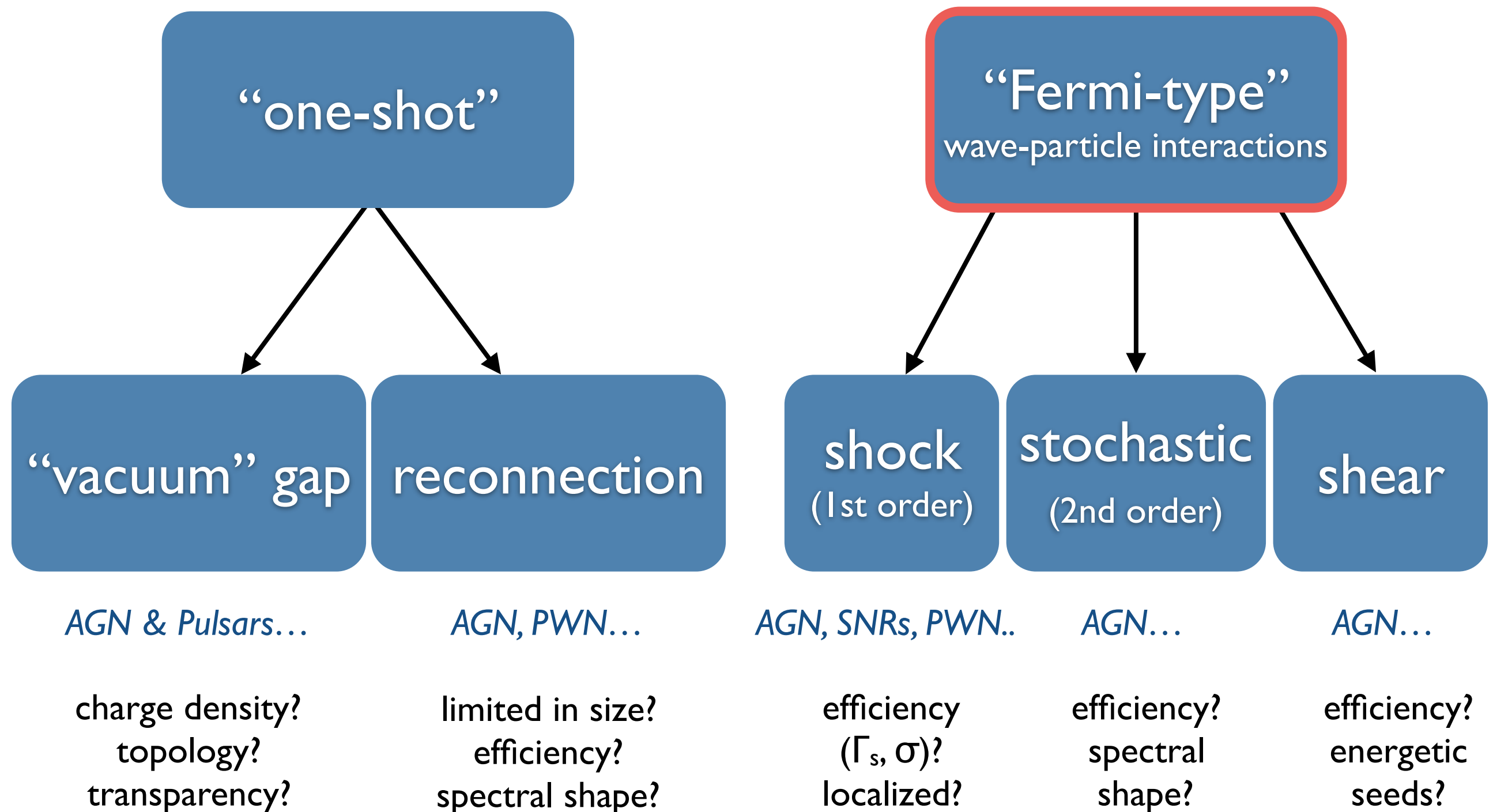


Phase-averaged spectrum, $E_{\text{cut}} \sim 5 \text{ GeV}$

Gap-type Particle Acceleration - Summary

- **gaps** (“unscreened parallel electric fields”) are to be expected in the magnetospheres of **pulsars**, and may occur around **supermassive black holes**
- **most efficient** (“direct - one-shot”) particle acceleration mechanism
 - ▶ energy gain $dE/dt \simeq e \Phi (c/H)$
 - ▶ acceleration timescales can be as short as $t_{acc} \sim \gamma m c / (eB)$
- unavoidable max. cutoff due to curvature radiation
 - ▶ **pulsars** : $\gamma_{max} \sim 10^{7-8} (e^+e^-)$
 - ▶ **AGN** : $\gamma_{max} \sim 10^{10} (e, p)$
- Development of pair cascade may limit size of gap & lead to closure

Possible Acceleration Processes & Sites (*not exhaustive*)



Fermi-type Particle Acceleration

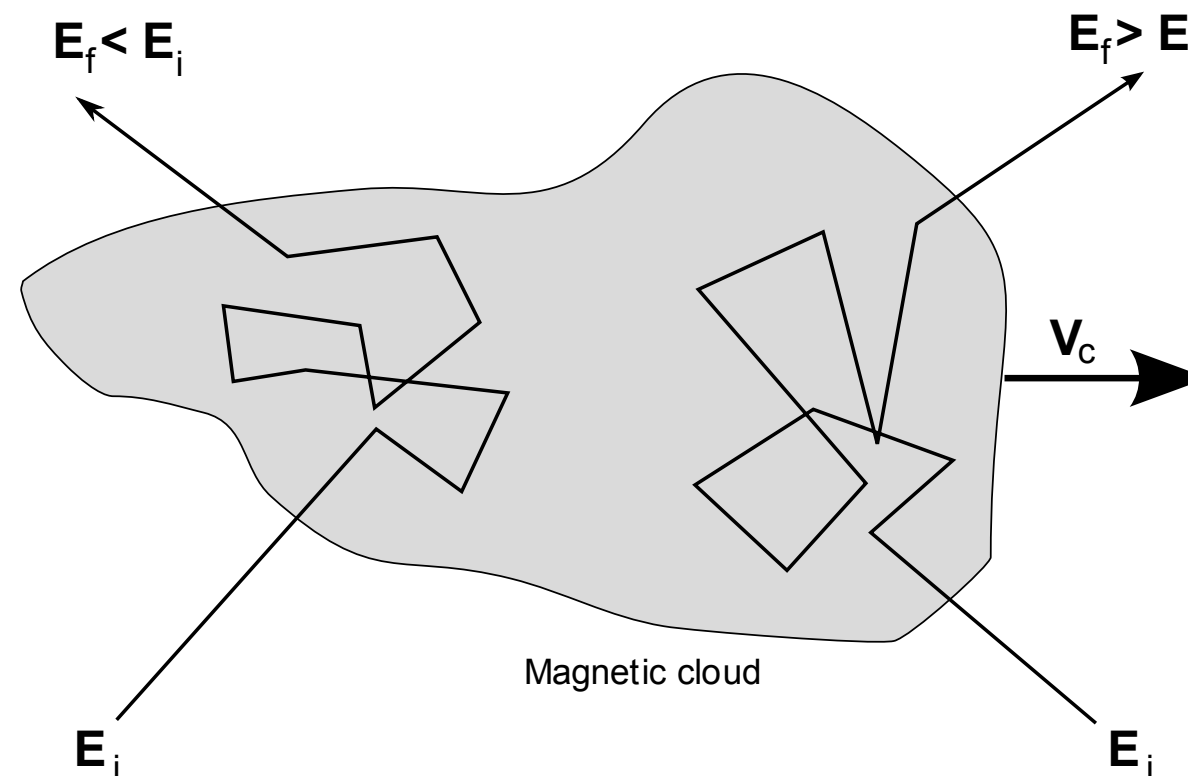
Kinematic effect resulting from scattering off magnetic inhomogeneities

Fermi, Phys. Rev. 75, 578 [1949]

⇒ energy gain as results of multiple scatterings (stochastic process)

Ingredients: in frame of scattering centre

- ▶ momentum magnitude conserved
- ▶ particle direction randomised



Fermi Acceleration - energy change in elastic scattering event I

Energy change ΔE for particle with initial E_i and \vec{p}_i interacting with massive cloud of speed \vec{V}_c :

- **Elastic Scattering:** In cloud frame K' , particle energy is conserved, momentum direction parallel to \vec{V}_c reversed (noting $p_{\parallel} = \vec{p} \cdot \vec{V}_c / V_c = p \cos \theta \simeq \frac{E}{c} v \cos \theta$)
- Lorentz-Transformation to cloud frame K' (cf. time and space trafo):

$$\begin{aligned} E'_i &= \gamma_c (E_i - \vec{p}_i \cdot \vec{V}_c) = \gamma_c (E_i - p_{i,\parallel} V_c) \\ p'_{i,\parallel} &= \gamma_c \left(p_{i,\parallel} - \frac{V_c}{c^2} E_i \right) \end{aligned}$$

- Elastic scattering in frame K' implies:

$$\begin{aligned} E'_f &= E'_i \\ p'_{f,\parallel} &= -p'_{i,\parallel} \end{aligned}$$

- Transforming back to lab. frame K :

$$\begin{aligned} E_f &= \gamma_c (E'_f + p'_{f,\parallel} V_c) = \gamma_c (E'_i - p'_{i,\parallel} V_c) \\ &= \gamma_c^2 \left([E_i - p_{i,\parallel} V_c] - \left[p_{i,\parallel} - \frac{V_c}{c^2} E_i \right] V_c \right) = \gamma_c^2 \left(\left[1 + \frac{V_c^2}{c^2} \right] E_i - 2p_{i,\parallel} V_c \right) \end{aligned}$$

Fermi Acceleration - energy change in elastic scattering event II

- Energy change ΔE :

$$\begin{aligned}\Delta E &= E_f - E_i = \gamma_c^2 \left(\left[1 + \frac{V_c^2}{c^2} \right] E_i - 2p_{i,\parallel} V_c \right) - E_i \\ &= (\gamma_c^2 - 1) E_i + \gamma_c^2 \left(\frac{V_c^2}{c^2} E_i - 2p_{i,\parallel} V_c \right) \\ &= 2\gamma_c^2 \left(\frac{V_c^2}{c^2} E_i - p_{i,\parallel} V_c \right)\end{aligned}$$

noting that $(\gamma_c^2 - 1) = \gamma_c^2 \beta_c^2$.

_Characteristic energy change per scattering (non-relativistic V_c):

$$\Delta E = E_f - E_i = 2 (E_i V_c^2 / c^2 - \vec{p}_i \cdot \vec{V}_c)$$

➡ energy gain for **head-on** ($\vec{p} \cdot \vec{V}_c < 0$), loss for **following** collision ($\vec{p} \cdot \vec{V}_c > 0$)

► **stochastic**: average energy gain 2nd order: $\langle \Delta E \rangle \sim (V_c / c)^2 E$

Fermi Acceleration - energy change in elastic scattering event II

- Energy change ΔE :

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➔ energy gain for *head-on* ($\vec{p} \cdot \vec{V}_c < 0$), loss for *following* collision

can we do
better?

► **stochastic:** average energy gain 2nd order: $\langle \Delta E \rangle \sim (V_c / c)^2 E$

Fermi Acceleration @ shocks

Shock=discontinuity moving through medium at speed larger than speed of sound (upstream)”

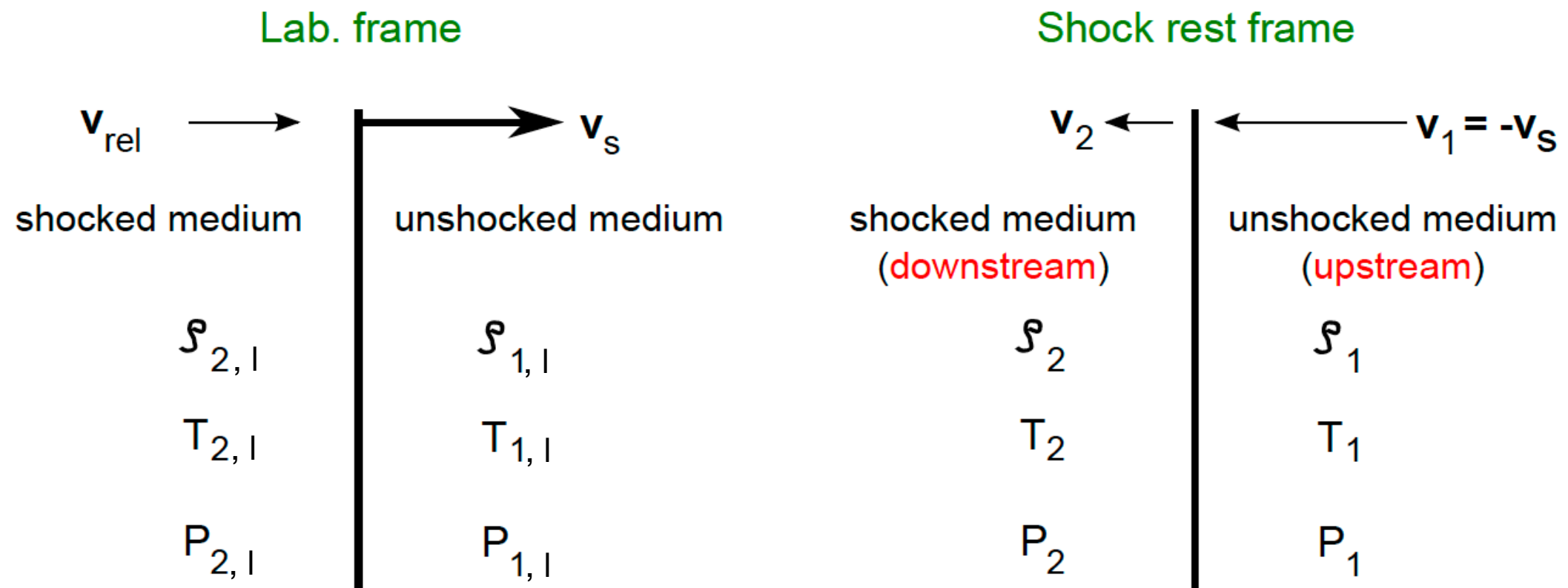


Figure 5: Non-relativistic shock wave in the reference frame of the un-shocked medium, $v_1 = 0$ (lab.frame, left) and in reference frame where the surface of the discontinuity is at rest, $v_s = 0$ (shock rest frame, right). The shock advances into the un-shocked medium at speed v_s . In rest frame of the shock, upstream medium approaches it at speed $v_1 = -v_s$. The shocked fluid moves away from the shock front at speed $v_2 = \rho_1 v_1 / \rho_2$. The shocked fluid thus approaches the un-shocked fluid at speed $v_{rel} = v_1 - v_2$.

Fermi Acceleration @ shocks

_For particles crossing the shock, scattering is always head-on:

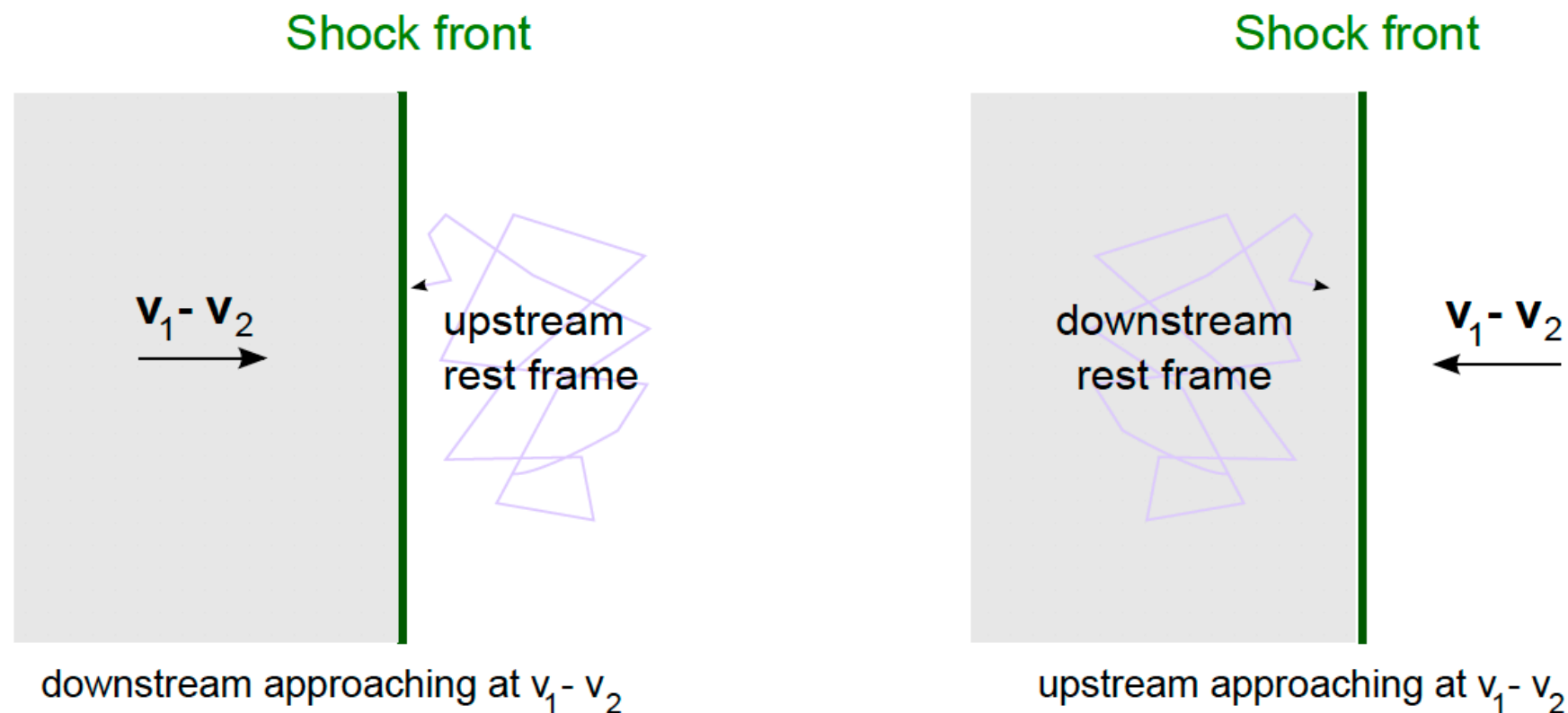


Figure 6: Diffusive shock acceleration: Energetic particles get isotropized in the downstream and upstream rest frame, respectively, by scattering off waves quasi-embedded in the background plasma (2nd order Fermi effects assumed being negligible). The situation is symmetrical: On each crossing of the shock front, they essentially experience head-on collisions with $\delta v = |v_1 - v_2|$, leading to 1st order Fermi acceleration.

► **shock:** spatial diffusion, gain on crossing is 1st order: $\langle \Delta E \rangle \sim (\Delta v / c) E$

Fermi Acceleration Timescales

— **Acceleration timescale** \sim particle energy / (rate of energy change):

$$t_{\text{acc}} = \frac{E}{(dE/dt)} \simeq \frac{E}{\Delta E} \times \tau$$

► **stochastic:** $\tau = \lambda / c$ “mean scattering time” (λ = mean free path):

$$t_{\text{acc}} = \frac{E}{(dE/dt)} \simeq \frac{E}{\Delta E} \times \tau \sim \left(\frac{c}{V_A} \right)^2 \frac{\lambda}{c} \propto \frac{\lambda}{V_A^2}$$

► **shock:** *spatial* diffusion process $\tau = t_c \sim \kappa / (V_s c)$ “crossing time”

(residence time t_c = diffusion length / c , with diffusion length $l \sim \sqrt{\kappa t}$, and $t \sim l / V_s$)

$$t_{\text{acc}} = \frac{E}{(dE/dt)} \simeq \frac{E}{\Delta E} \times t_c \sim \left(\frac{c}{V_s} \right) \frac{\kappa}{V_s c} \sim \frac{\kappa}{V_s^2} \propto \frac{\lambda}{V_s^2}$$

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also second
order in shock
speed !

Fermi Acceleration @ shear flows

_Gradual shear flow with frozen-in scattering centres: *non-relativistic*
 $\vec{u} = u_z(x) \vec{e}_z$

► like 2nd Fermi, stochastic process with average gain:

$$\frac{\langle \Delta E \rangle}{E} \propto \left(\frac{V}{c} \right)^2 = \frac{1}{c^2} \left(\frac{\partial u_x}{\partial x} \right)^2 \lambda^2$$

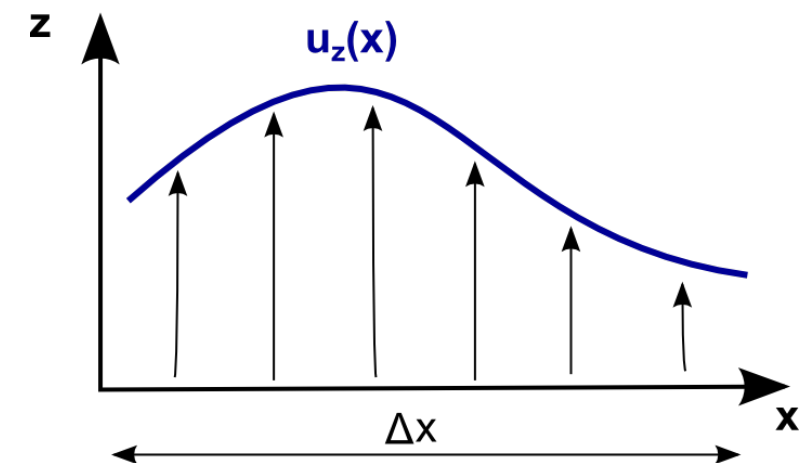
using characteristic *effective velocity*:

$$V = \Delta u = \left(\frac{\partial u_z}{\partial x} \right) \lambda, \text{ where } \lambda = \text{particle mean free path}$$

► leads to

$$t_{\text{acc}} = \frac{E}{(dE/dt)} \simeq \frac{E}{\Delta E} \times \tau \sim \left(\frac{c}{[\partial u_z / \partial x] \lambda} \right)^2 \frac{\lambda}{c} \propto \frac{1}{\lambda}$$

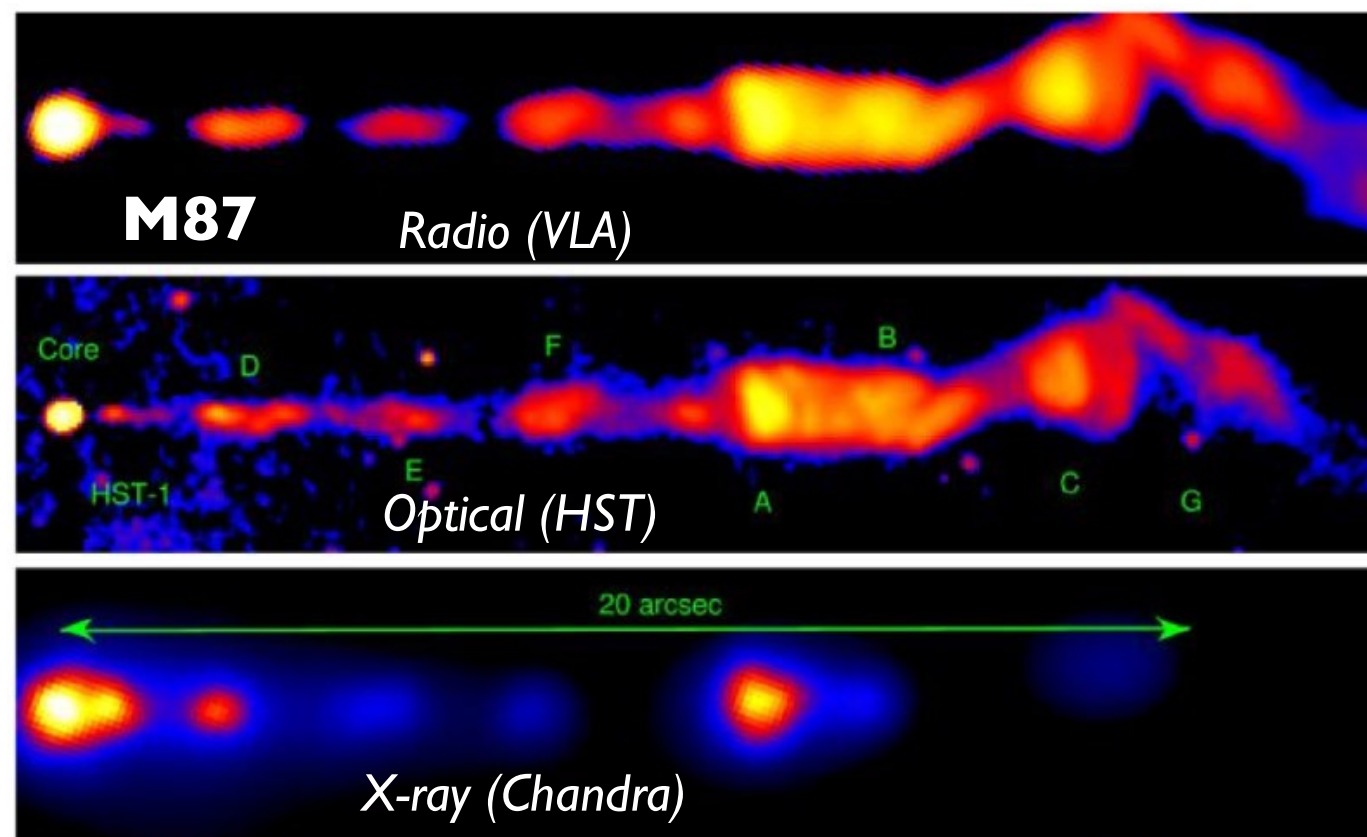
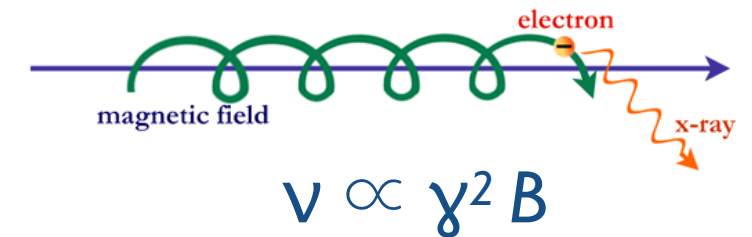
- seed from acceleration @ shock or stochastic....
- easier for protons....



Example: Stochastic & shear acceleration in large-scale AGN jets I

Emission from large-scale jets

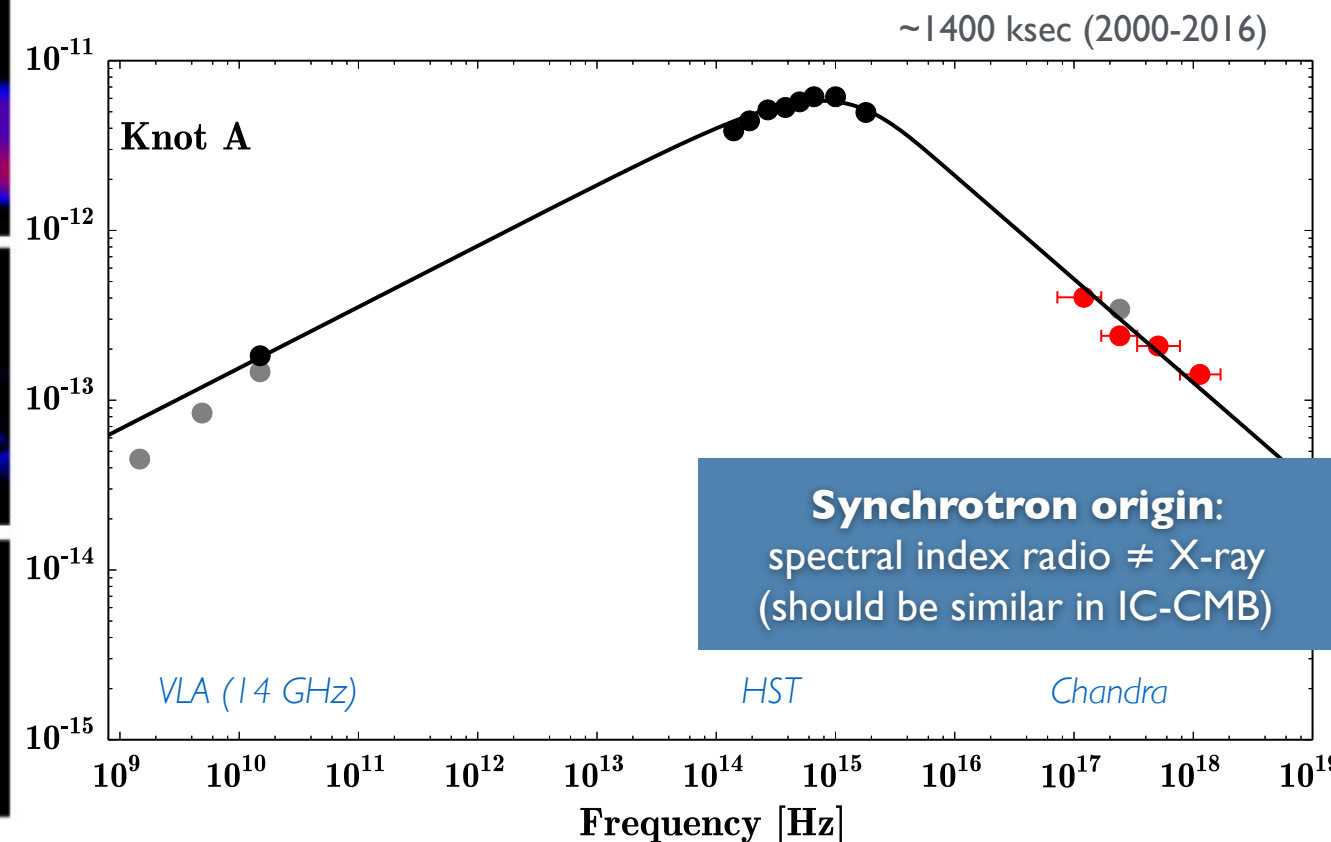
- ▶ extended X-ray electron synchrotron emission
- ▶ electron Lorentz factors $\gamma \sim 10^8$
- ▶ short cooling timescale $t_{\text{cool}} \propto 1/\gamma$; cooling length $c t_{\text{cool}} \ll \text{kpc}$
- ▶ distributed acceleration mechanism required (Sun, Yang, FR+ 2018 for M87)



1 arcsec ~ 0.1 kpc (0.081 kpc)

Marshall+ 2002

Relativistic particles
throughout whole jet

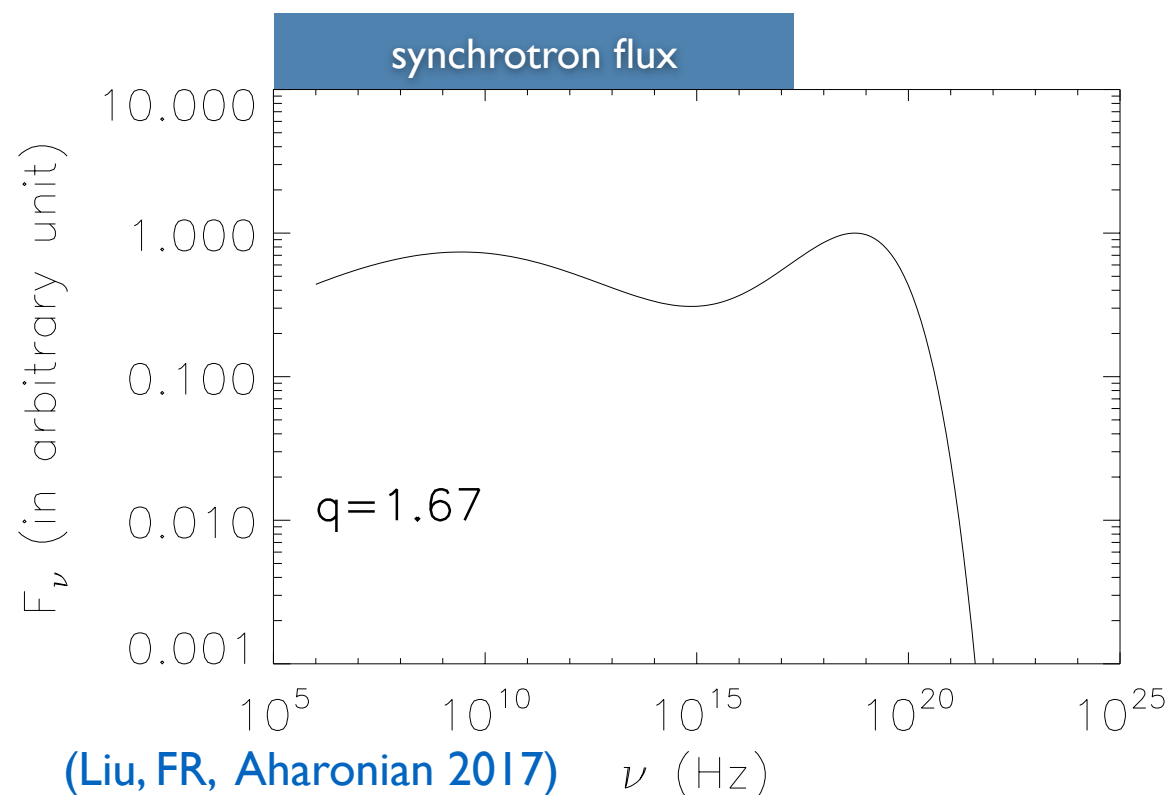
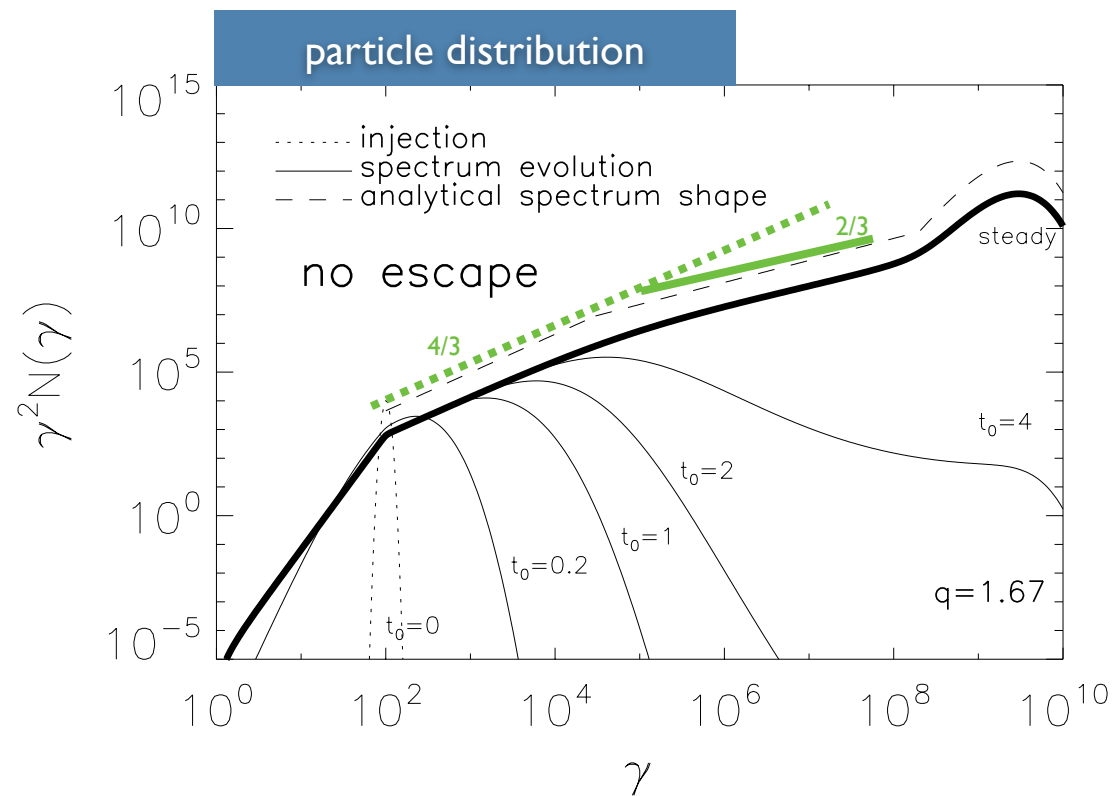


SED can be fitted by broken power-law

($B = 3 \times 10^{-4}$ G, $\gamma_b \sim 10^6$, $\gamma_{\text{max}} \sim 10^8$, $P_{\text{jet}} \sim 10^{43}$ erg/s, $\Delta\alpha \sim 2$)

Example: Stochastic & shear acceleration in large-scale AGN jets II

Radiative-loss-limited acceleration in mildly relativistic flows



Ansatz: Fokker-Planck equation for $f(t,p)$ including stochastic, shear and synchrotron for cylindrical jet.

► from 2nd Fermi ($t_{\text{acc}} \propto \lambda$) to shear ($t_{\text{acc}} \propto l / \lambda$)...

► electron acceleration up to $\gamma \sim 10^9$ possible

► formation of **multi-component particle distribution**

Parameters: $B = 3 \mu\text{G}$, $v_{j,\text{max}} \sim 0.4c$, $r_j \sim 30 \text{ pc}$, $\beta_A \sim 0.007$, $\Delta r \sim r_j/10$, mean free path $\lambda = \xi^{-1} r_g (r_g/\Lambda_{\text{max}})^{1-q} \propto \gamma^{2-q}$, $q=5/3$ (Kolmogorov), $\xi=0.1$

Fermi Acceleration Timescales - Summary

_"1st order" Fermi - standard shock (non-relativistic):

with shock crossing time $t_c \sim \kappa / (u_s c)$, where $\kappa \sim \lambda c$

$$t_{\text{acc}} \sim \left(\frac{c}{V_s} \right) \frac{\kappa}{V_s c} \sim \frac{\kappa}{V_s^2} \propto \frac{\lambda}{V_s^2}$$

_"2nd order" Fermi (stochastic):

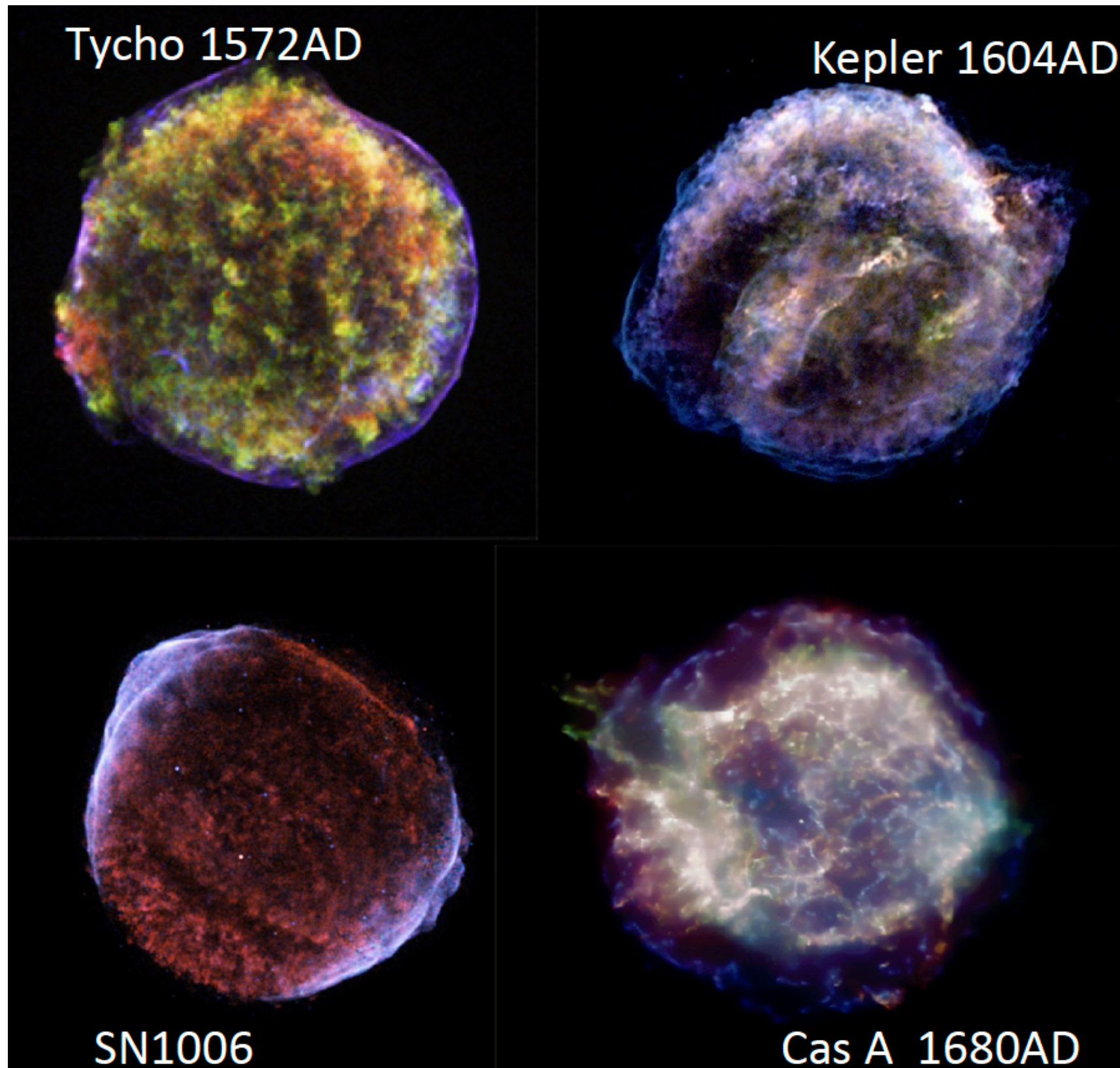
with scattering time $\tau \sim \lambda/c$

$$t_{\text{acc}} \sim \left(\frac{c}{V_A} \right)^2 \frac{\lambda}{c} \propto \frac{\lambda}{V_A^2}$$

_Shear - **gradual** (non-relativistic):

$$t_{\text{acc}} \sim \left(\frac{c}{[\partial u_z / \partial x] \lambda} \right)^2 \frac{\lambda}{c} \propto \frac{1}{\lambda}$$

Example: Shocks in SNRs - historical shell SNR



Mixture of line radiation (hot plasma) & synchrotron continuum (relativistic electrons).

For electron synchrotron in (amplified) magnetic field of ~ 0.1 - 1 mG:

- radio (GHz): $\gamma_e \sim 10^{3-4}$
- X-rays (keV): $\gamma_e \sim 10^{7-8}$

(but: *degeneracy in B & γ*)

Example: Efficient Cosmic Ray (PeV) Acceleration @ SNR shocks ?

- Acceleration timescale:

$$t_{\text{acc}} \simeq \frac{8 \kappa}{V_s^2} = \frac{8 \lambda c}{3 V_s^2}$$

- with spatial diffusion coefficient:

$$\kappa = \lambda c / 3$$

SNR radius
↓

$$t_{\text{acc}} \leq t_{\text{age}} \simeq R / V_s \text{ implies: } \lambda \leq \frac{3}{8} \frac{V_s}{c} R$$

- smallest possible mean free path: $\lambda \approx r_{\text{gyro}} = E / (e B)$

⇒ Limit on maximum CR energy: $E_{\text{max}} \leq \frac{3}{8} \frac{V_s}{c} R e B$

- typical for young SNR:

ISM mag field: few μG

$$V_s = c / 50$$

$$R \sim 10^{19} \text{ cm}$$

$$E_{\text{max}} \lesssim 10^{14} (B / 5 \mu\text{G}) \text{ eV}$$

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(Lagage & Cesarsky 1983)

but limitations due to self-regulated CR escape implying
 $E_{\text{max}} < 1 \text{ PeV}$ for Tycho, Cas A, Kepler (e.g., Bell+ 2013)

Some Issues Concerning Fermi-type Particle Acceleration

- **Stochastic particle acceleration:**

- ▶ generates **no unique power-law** particle distribution, e.g., index depends on ratio of $t_{\text{acc}}/t_{\text{escape}}$; if synchrotron-loss limited, relativistic Maxwellian distributions may occur...
- ▶ **slow process** unless the scattering center speed is high (Alfven speed; AGN jets)...

- **Shock acceleration:**

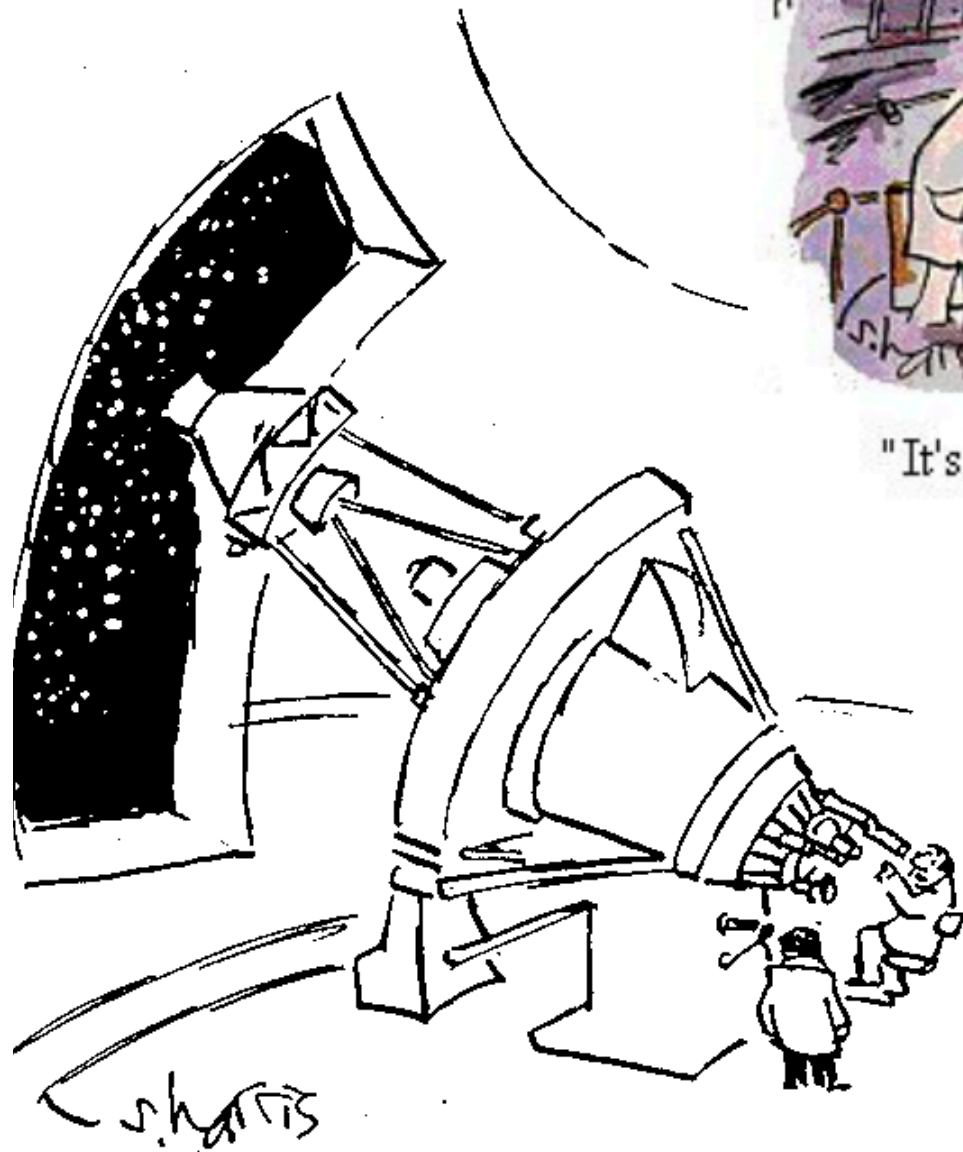
- ▶ **highly relativistic shocks** (PWN, GRBs etc) are **not** expected to be **efficient** accelerators (e.g., isotropization upstream not guaranteed; relativistic shocks are generically quasi-perpendicular as $B_{\perp} = 3 \Gamma_s B_{\perp}' \dots$)
- ▶ no longer a unique power law...

- **Shear acceleration:**

- ▶ **only efficient in relativistic shear flows**
- ▶ particle transport across flow still to be understood
- ▶ destruction of flow (KH/shear instabilities)?

(e.g., Sironi+ 2013, Lemoine & Pelletier 2017; Bell+ 2018, Webb+ 2018, FR 2019)

The END

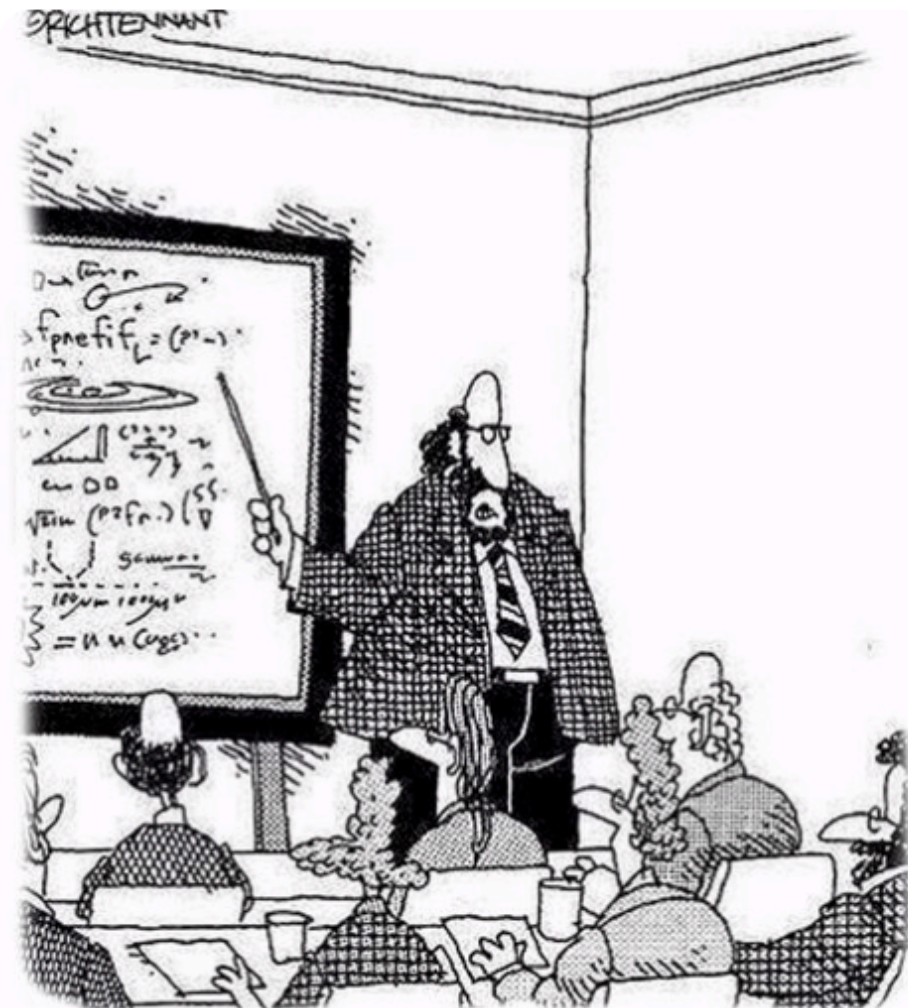


"Actually they all look alike to me."



"It's black, and it looks like a hole.
I'd say it's a black hole."

Thank you!



"Along with 'Antimatter,' and 'Dark Matter,'
we've recently discovered the existence of
'Doesn't Matter,' which appears to have no
effect on the universe whatsoever."