



New CMS obtained using xFitter

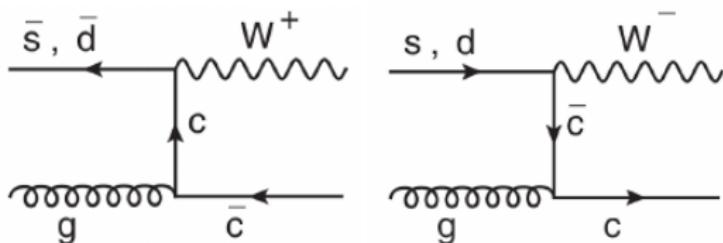
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(Hamburg University)

xFitter Workshop, Minsk
18.03.2019

Overview of new results since March 2018

- “Measurement of associated production of a W boson and a charm quark in proton-proton collisions at $\sqrt{s} = 13 \text{ TeV}$
[SMP-17-014, arXiv:1811.10021, submitted to Eur. Phys. J.]
- “Measurements of normalised multi-differential cross sections for top quark pair production in pp collisions at $\sqrt{s} = 13 \text{ TeV}$ and simultaneous determination of the strong coupling strength, top quark pole mass and parton distribution functions”
[CMS-PAS-TOP-18-004, paper in a few days]
- “Measurement of the $t\bar{t}$ production cross section, the top quark mass, and the strong coupling constant using dilepton events in pp collisions at $\sqrt{s} = 13 \text{ TeV}$
[TOP-17-001, arXiv:1812.10505, submitted to Eur. Phys. J.]
- “Standard Model Physics at the HL-LHC and HE-LHC”
[CERN-LPCC-2018-03, arXiv:1902.04070]

Measurement of associated production of W and c [arXiv:1811.10021]

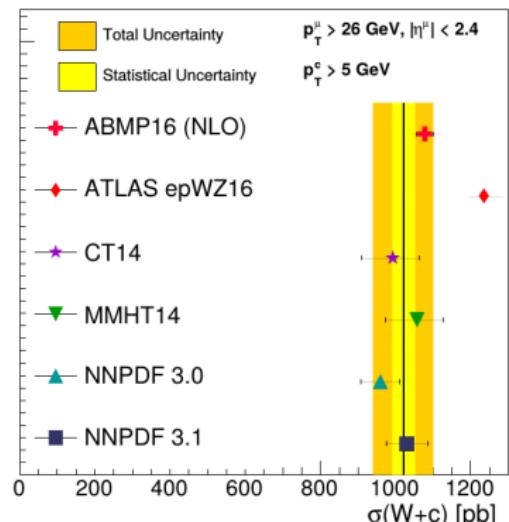


- $W \rightarrow \mu, c \rightarrow D^* \rightarrow D^0 + \pi_{slow} \rightarrow K + \pi + \pi_{slow}$
- $|\eta(\mu)| < 2.4, p_T(c) > 5 \text{ GeV}$
- Measured total cross section and differential cross section as function of $|\eta(\mu)|$
- Results are used to probe strange density in the proton at NLO (xFitter)

Measurement of associated production of W and c [arXiv:1811.10021]

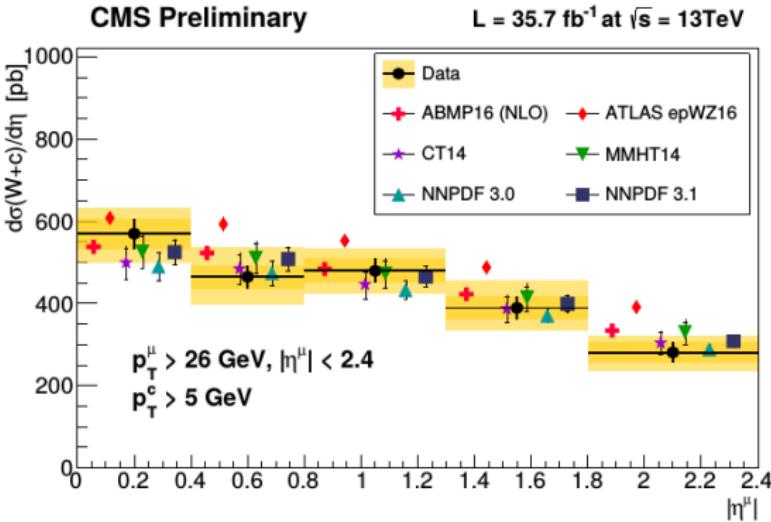
CMS Preliminary

$L = 35.7 \text{ fb}^{-1}$ at $\sqrt{s} = 13 \text{ TeV}$



CMS Preliminary

$L = 35.7 \text{ fb}^{-1}$ at $\sqrt{s} = 13 \text{ TeV}$



- Calculations done with MCFM at NLO ($O(\alpha_s^2)$)
- $\mu_r = \mu_f = M_W$, $m_c = 1.5 \text{ GeV}$
- Scales varied simultaneously by factor 2 (3%)
- Good agreement with theoretical predictions, except using ATLASepWZ16nnlo

Measurement of associated production of W and c [arXiv:1811.10021]

- Study performed using xFitter-2.0.0
- Fitted data:
 - ▶ HERA DIS
 - ▶ CMS W asymmetry at 7 TeV
 - ▶ CMS W asymmetry at 8 TeV
 - ▶ CMS W+c at 7 TeV
 - ▶ CMS W+c at 13 TeV
- PDF uncertainties estimated using standard HERAPDF approach
- Fit uncertainties estimated using HESSE and MC replica methods

$$x u_v(x) = A_{u_v} x^{B_{u_v}} (1-x)^{C_{u_v}} (1+E_{u_v}x^2),$$

$$x d_v(x) = A_{d_v} x^{B_{d_v}} (1-x)^{C_{d_v}},$$

$$x \bar{U}(x) = A_{\bar{U}} x^{B_{\bar{U}}} (1-x)^{C_{\bar{U}}} (1+E_{\bar{U}}x^2),$$

$$x \bar{d}(x) = A_{\bar{d}} x^{B_{\bar{d}}} (1-x)^{C_{\bar{d}}}$$

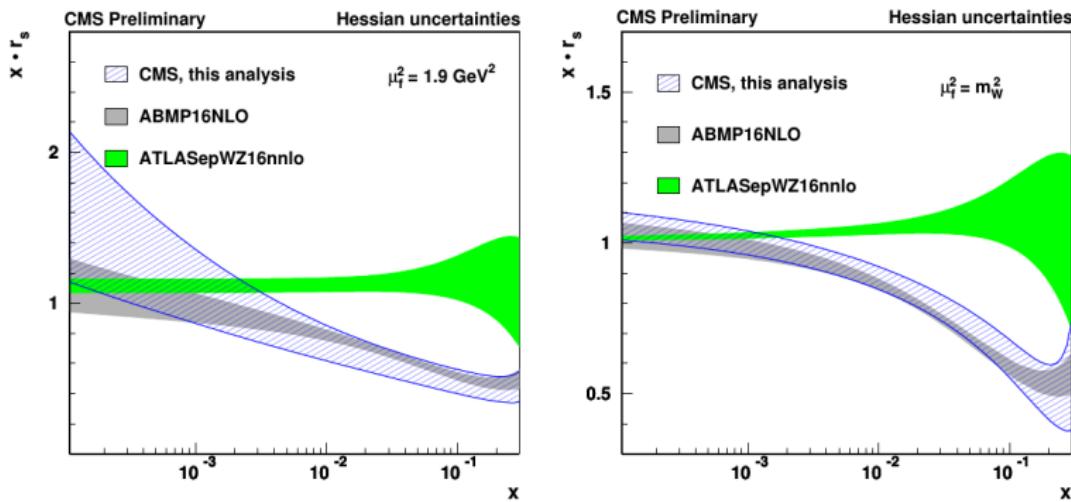
$$x \bar{s}(x) = A_{\bar{s}} x^{B_{\bar{s}}} (1-x)^{C_{\bar{s}}}$$

$$x g(x) = A_g x^{B_g} (1-x)^{C_g}$$

$$\begin{aligned}s(x) &= \bar{s}(x) \\ B_{\bar{U}} &\neq B_{\bar{d}} \neq B_{\bar{s}}\end{aligned}$$

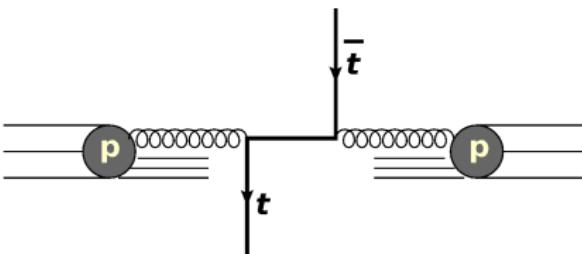
Dataset		χ^2/n_{dp}
HERA I+II charged current	e ⁺ p	43 / 39
HERA I+II charged current	e ⁻ p	57 / 42
HERA I+II neutral current	e ⁻ p	218 / 159
HERA I+II neutral current	e ⁺ p, $E_p = 820$ GeV	69 / 70
HERA I+II neutral current	e ⁺ p, $E_p = 920$ GeV	448 / 377
HERA I+II neutral current	e ⁺ p, $E_p = 460$ GeV	216 / 204
HERA I+II neutral current	e ⁺ p, $E_p = 575$ GeV	220 / 254
CMS W muon charge asymmetry 7 TeV		13 / 11
CMS W muon charge asymmetry 8 TeV		4.2 / 11
W + c 7 TeV		2.2 / 5
W + c 13 TeV		2.1 / 5
Correlated χ^2		87
Total χ^2 / dof		1385 / 1160

Measurement of associated production of W and c [arXiv:1811.10021]

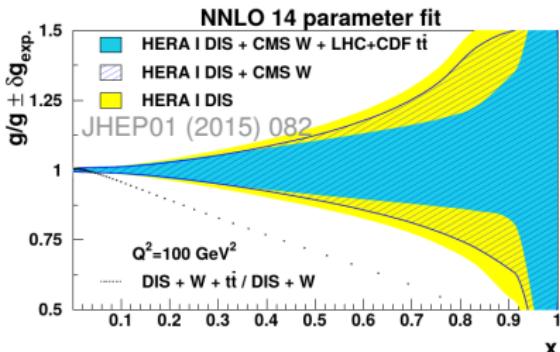


- Determined r_s agree with earlier results obtained in neutrino scattering experiments, but do not support the hypothesis of an enhanced strange quark contribution in the proton quark sea

Why measure $t\bar{t}$ production?



- m_t provides a hard scale ($\alpha_s \approx 0.1$)
⇒ ultimate probe of perturbative QCD
(NLO, aNNLO, NNLO, ...)
- Produced mainly via gg
⇒ constrain gluon PDF at high x
- Production sensitive to α_s and m_t^{pole}
- May provide insight into possible new physics



Why measure multidifferentially?

- differential (1D) $t\bar{t}$ data provide constraints on gluon PDF [JHEP01 (2015) 082]
- 2D $t\bar{t}$ data: stronger PDF constraints [EPJ C77 (2017) 459]
- 3D $[N_{\text{jet}}^{0,1+}, M(t\bar{t}), y(t\bar{t})]$ cross sections constrain α_s , m_t^{pole} , PDFs:
 - ▶ $y(t\bar{t})$ constrains PDFs (boost)
 - ▶ N_{jet} constrains α_s (extra radiation)
 - ▶ $M(t\bar{t})$ constrains m_t^{pole} (threshold)

Measurement of multidifferential $t\bar{t}$ cross sections [CMS-PAS-TOP-18-004]

First time measured 3D cross sections as function of $M(t\bar{t})$, $y(t\bar{t})$, N_{jet} :

- $[N_{\text{jet}}^{0,1+}, M(t\bar{t}), y(t\bar{t})]$
- $[N_{\text{jet}}^{0,1,2+}, M(t\bar{t}), y(t\bar{t})]$

Exploited data for $\alpha_s + m_t + \text{PDF}$ extraction at NLO (highest available order for $t\bar{t} + \text{jets}$):

- sensitivity to PDFs from $M(t\bar{t})$, $y(t\bar{t})$ ($x_{1,2} = (M(t\bar{t})/\sqrt{s}) \exp[\pm y(t\bar{t})]$)
- sensitivity to α_s from N_{jet} and $M(t\bar{t})$, $y(t\bar{t})$ (PDFs)
- sensitivity to m_t from $M(t\bar{t})$ via threshold and cone effects

Data interpretation consists of two parts:

(1) comparison theory vs data using external PDF sets:

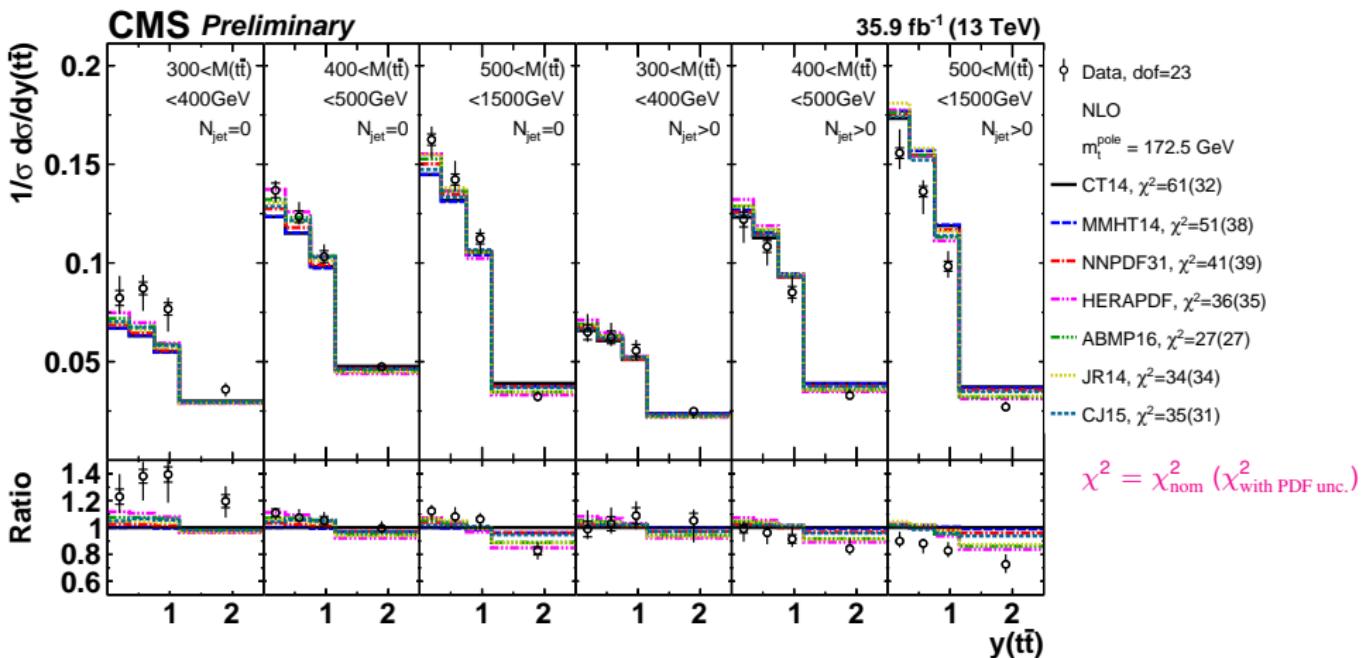
- ▶ extracting α_s keeping m_t^{pole} fixed
- ▶ extracting m_t^{pole} keeping α_s fixed

→ this presents α_s , m_t^{pole} extraction from $t\bar{t}$ data only

(2) simultaneous fit of PDFs, α_s and m_t^{pole} using $t\bar{t}$ and HERA DIS:

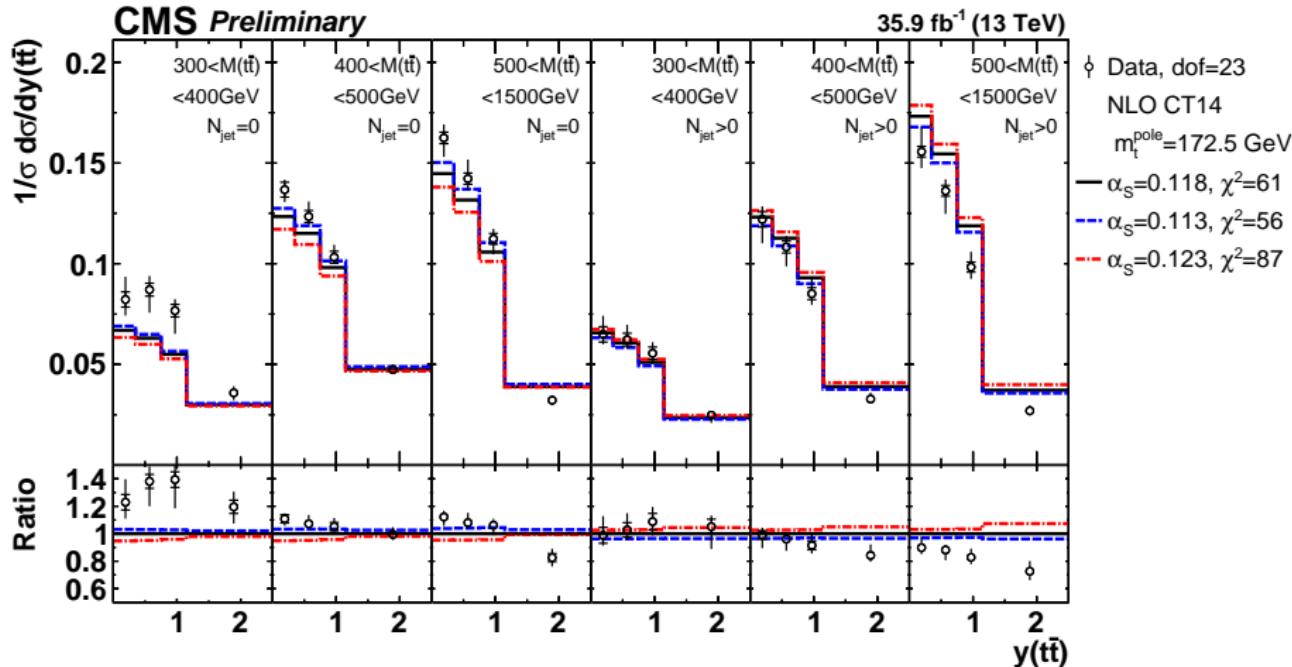
- this presents fully consistent extraction of α_s , m_t^{pole} and PDFs, but using also HERA data
- important as exercise to understand new $t\bar{t}$ data, providing baseline for future global fits

$[N_{\text{jet}}^{0,1+}, M(t\bar{t}), y(t\bar{t})]$ compared to NLO predictions with different PDFs



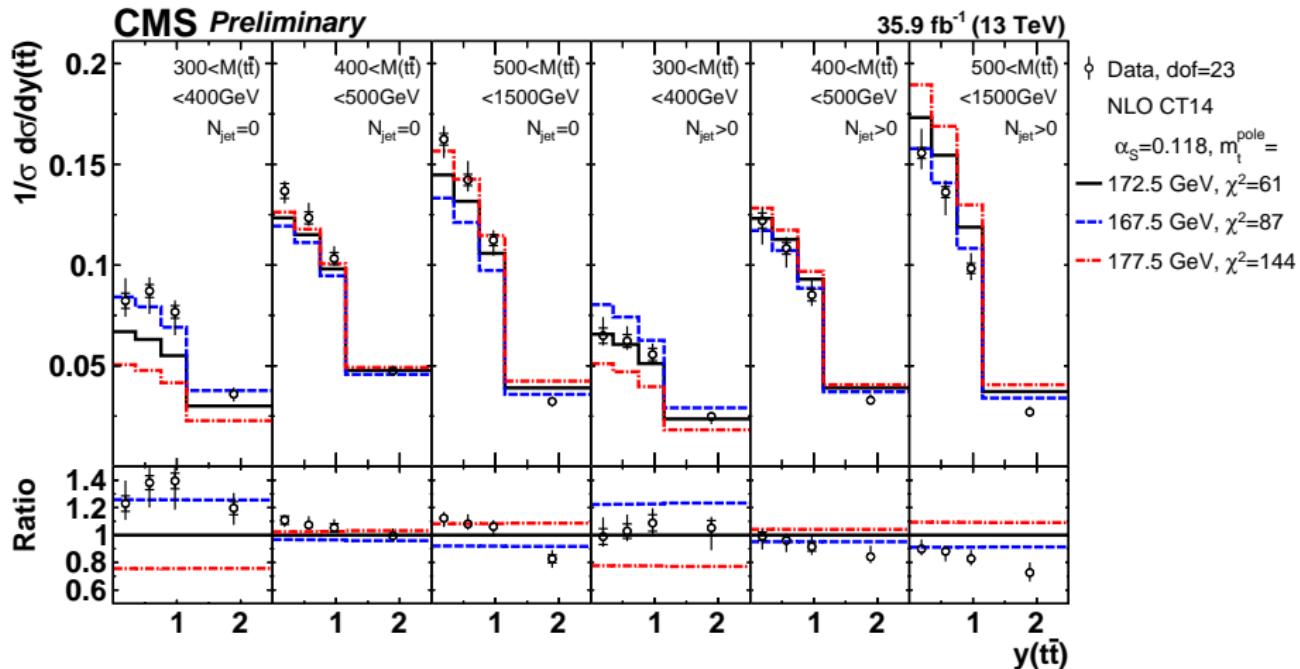
- description depends on PDFs → data are sensitive to PDFs
- all modern PDF sets considered
 - ▶ best description given by ABMP16

$[N_{\text{jet}}^{0,1+}, M(t\bar{t}), y(t\bar{t})]$ compared to NLO predictions with different α_s



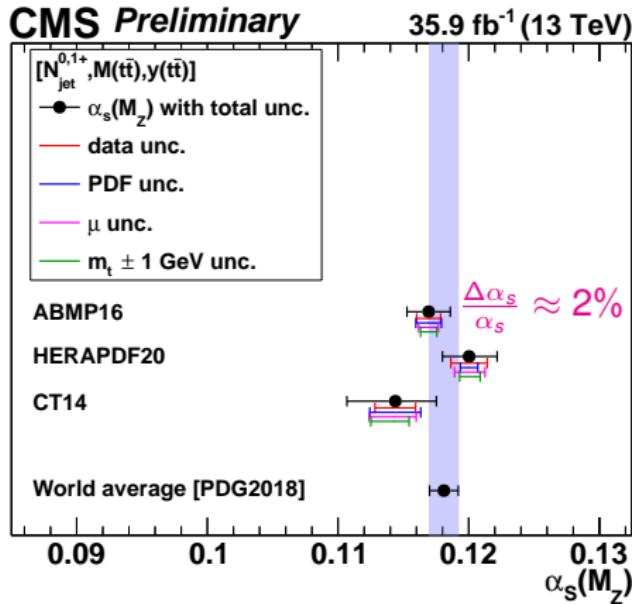
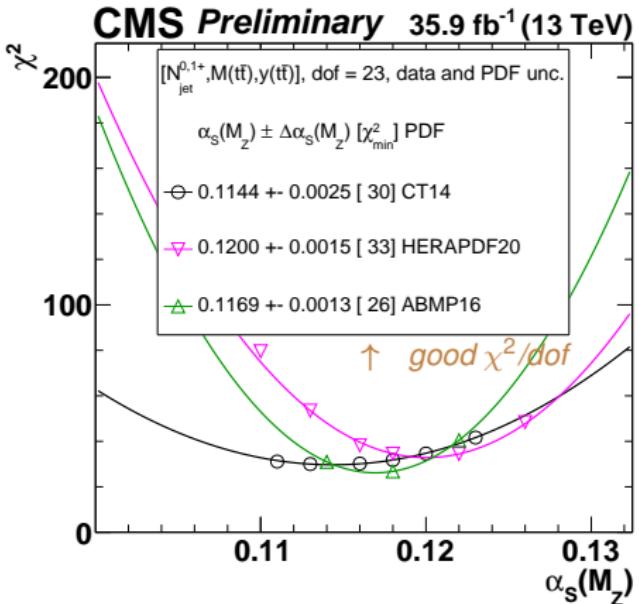
- α_s sensitivity comes from different N_{jet} bins
- further (indirect) sensitivity comes from $[M(t\bar{t}), y(t\bar{t})]$ via sensitivity to PDFs

$[N_{\text{jet}}^{0,1+}, M(t\bar{t}), y(t\bar{t})]$ compared to NLO predictions with different m_t^{pole}



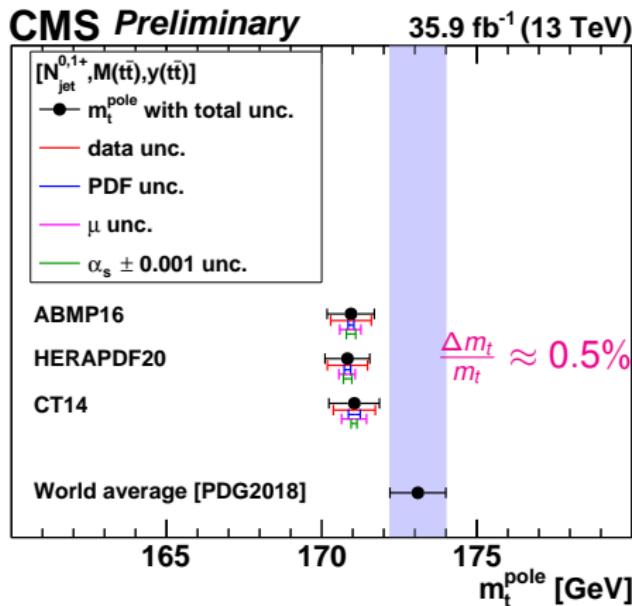
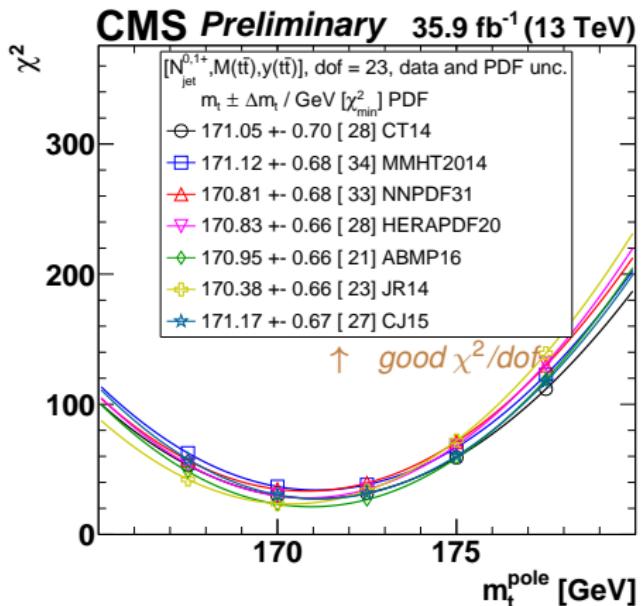
- m_t^{pole} sensitivity comes from $M(t\bar{t})$, mainly 1st bin
- this method differs from extracting m_t^{pole} from total $t\bar{t}$ x-section, and is similar to extracting m_t^{pole} from $t\bar{t}j$ diff. x-section [EPJ C73 (2013) 2438, CMS-PAS-TOP-13-006, JHEP 1510 (2015) 121]
- previous determination using this method: prelim. D0 results [FERMILAB-CONF-16-383-PPD]

Results: extraction of α_s from $[N_{\text{jet}}^{0,1+}, M(t\bar{t}), y(t\bar{t})]$



- used $m_t^{\text{pole}} = 172.5 \text{ GeV}$ in ME for all PDF sets (ABMP16 fitted $m_t^{\text{pole}} = 171.44 \text{ GeV}$)
- precise determination of α_s is possible using these data
- significant dependence on PDF set observed (correlation between g and α_s)

Results: extraction of m_t^{pole} from $[N_{\text{jet}}^{0,1+}, M(t\bar{t}), y(t\bar{t})]$

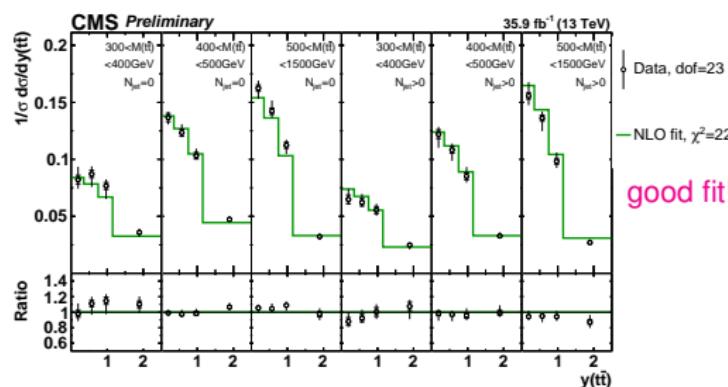


- used α_s from each PDF set ($\alpha_s = 0.118$ in CT and HERAPDF, $\alpha_s = 0.119$ in ABMP)
- precise determination of m_t^{pole} is possible using these data
→ uncertainty smaller than world average
- no significant dependence on PDF set

Simultaneous PDF + α_s + m_t^{pole} fit: results

- followed standard approach: using HERA DIS data only, or HERA + $t\bar{t}$ data to demonstrate added value from $t\bar{t}$ on PDF and α_s determination
- settings follow HERAPDF2.0 fit (very similar to TOP-14-013), use xFitter-2.0.0
- input data: combined HERA DIS [1506.06042] + $t\bar{t}$ (further details in BACKUP)

Data sets	χ^2/dof	
	Nominal fit	+ $[N_{\text{jet}}, y(t\bar{t}), M(t\bar{t})]$
CMS $t\bar{t}$		10/23
HERA CC $e^- p$, $E_p = 920 \text{ GeV}$	55/42	55/42
HERA CC $e^+ p$, $E_p = 920 \text{ GeV}$	38/39	39/39
HERA NC $e^- p$, $E_p = 920 \text{ GeV}$	218/159	217/159
HERA NC $e^+ p$, $E_p = 920 \text{ GeV}$	438/377	448/377
HERA NC $e^+ p$, $E_p = 820 \text{ GeV}$	70/70	71/70
HERA NC $e^+ p$, $E_p = 575 \text{ GeV}$	220/254	222/254
HERA NC $e^+ p$, $E_p = 460 \text{ GeV}$	219/204	220/204
Correlated χ^2	82	90
Log-penalty χ^2	+2	-7
Total χ^2/dof	1341/1130	1364/1151

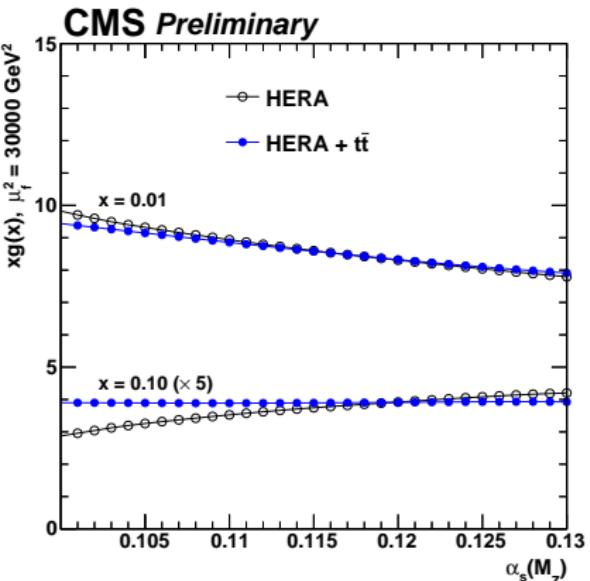
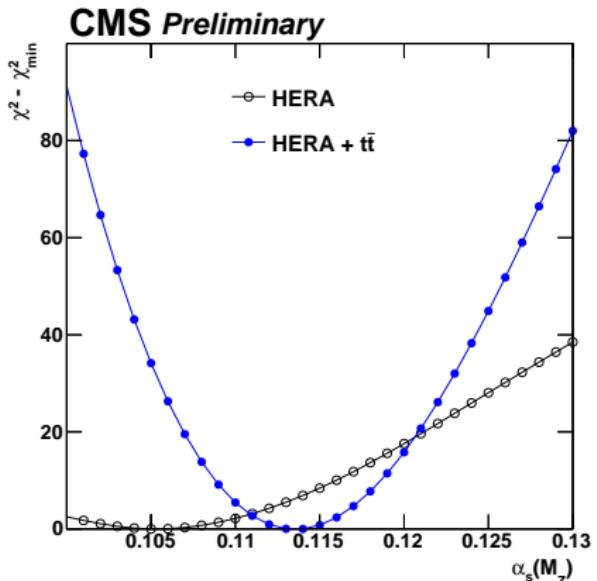


$$\alpha_s(M_Z) = 0.1135 \pm 0.0016(\text{fit})^{+0.0002}_{-0.0004}(\text{mod})^{+0.0008}_{-0.0001}(\text{par})^{+0.0011}_{-0.0005}(\text{scale}) = 0.1135^{+0.0021}_{-0.0017}(\text{total})$$

$$m_t^{\text{pole}} = 170.5 \pm 0.7(\text{fit})^{+0.1}_{-0.1}(\text{mod})^{+0.0}_{-0.1}(\text{par})^{+0.3}_{-0.3}(\text{scale}) \text{ GeV} = 170.5 \pm 0.8(\text{total}) \text{ GeV}$$

→ two SM parameters are simultaneously determined from these data to high precision with only weak correlation between them ($\rho = 0.3$) + constraints on PDFs (next slides)

Simultaneous PDF + α_s + m_t^{pole} fit: correlation between α_s and gluon

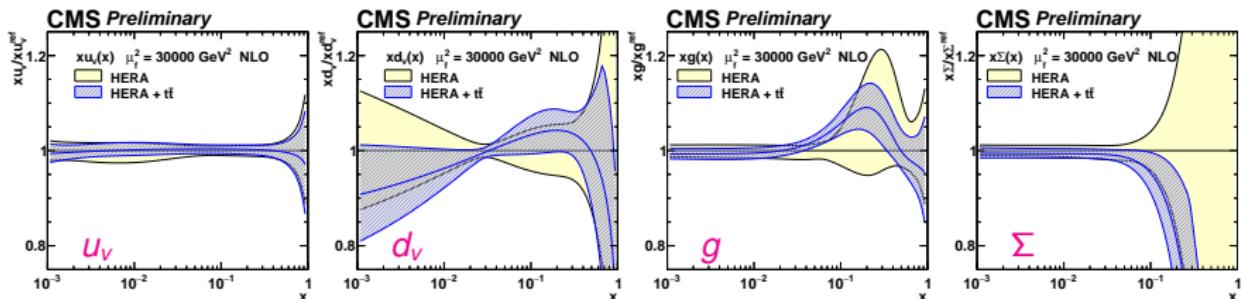


Adding $t\bar{t}$ data:

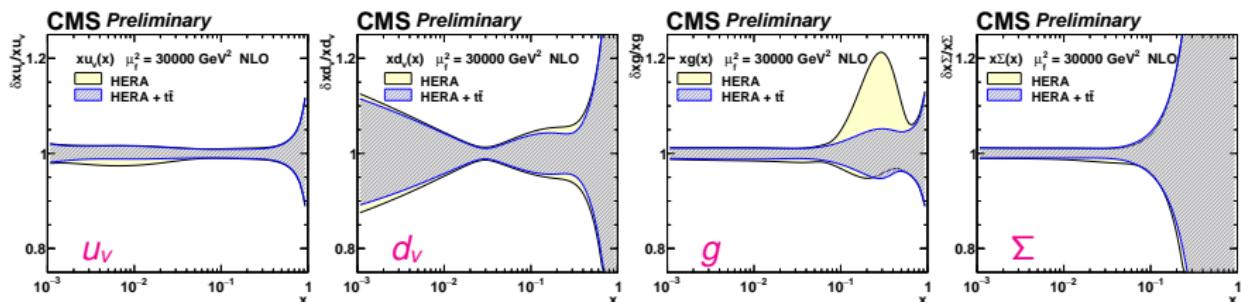
- constrain α_s (left)
- reduce correlation between α_s and gluon (g) (right)
 - weak correlation (α_s, m_t) \rightarrow weak correlation (g, m_t)

Simultaneous PDF + α_s + m_t^{pole} fit: Impact on PDFs

PDFs (α_s in HERA-only fit set to $\alpha_s = 0.1135 \pm 0.0016$)



Relative PDF uncertainties

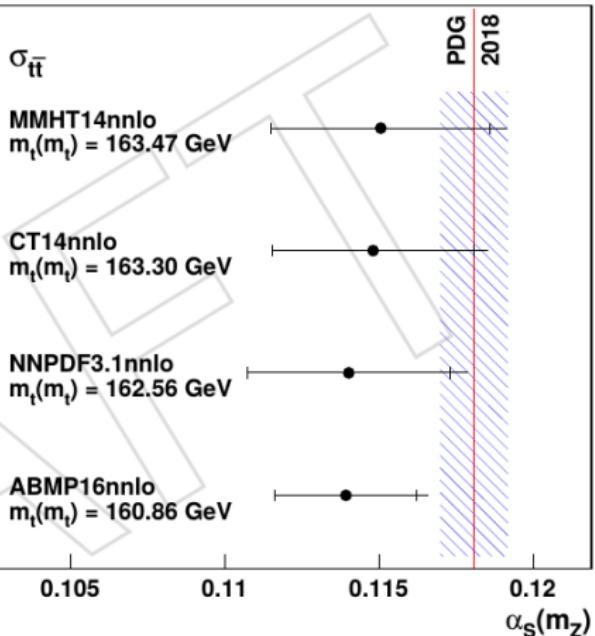


- reduced g uncertainty at high x
- smaller impact on other distributions via correlations in the fit

Extraction of α_s and m_t from total $t\bar{t}$ cross section [arXiv:1812.10505]

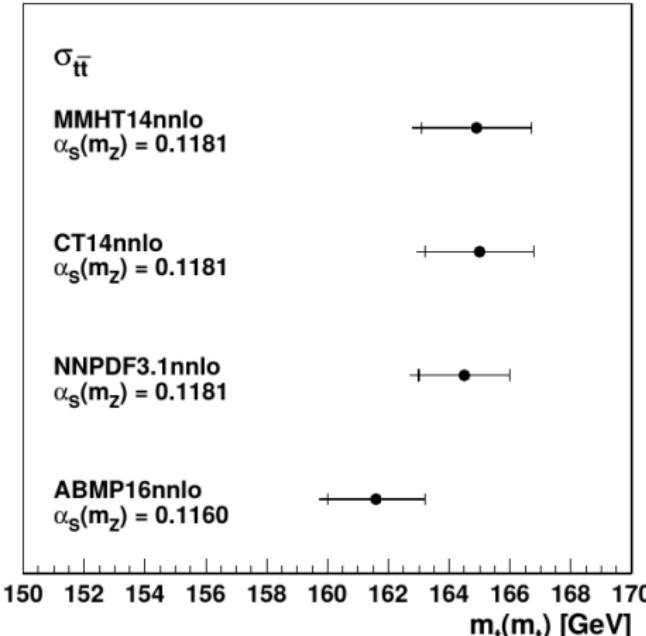
CMS

35.9 fb^{-1} (13 TeV)



CMS

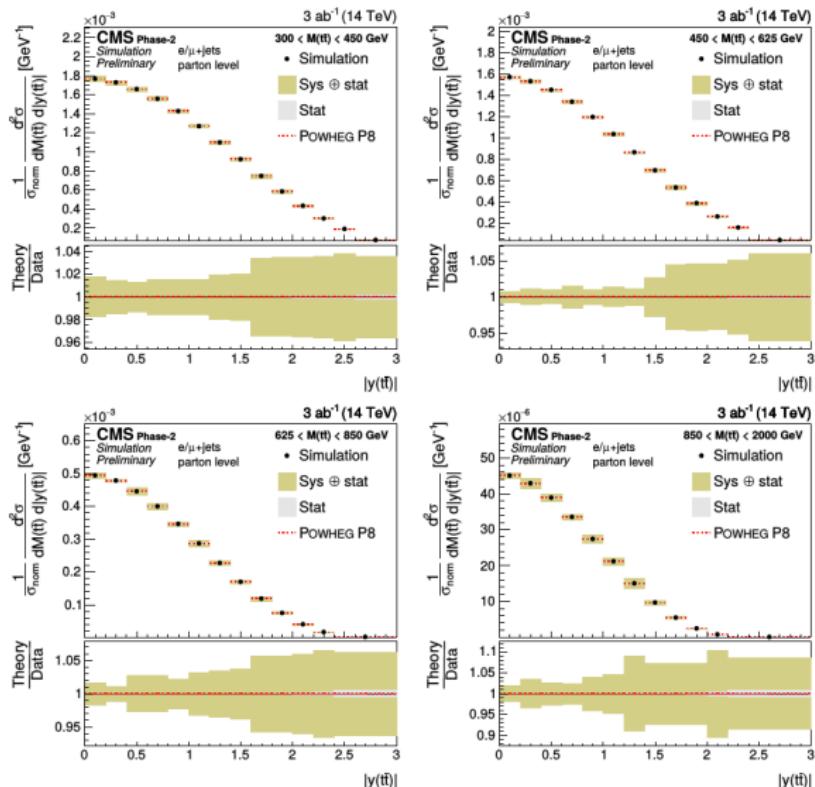
35.9 fb^{-1} (13 TeV)



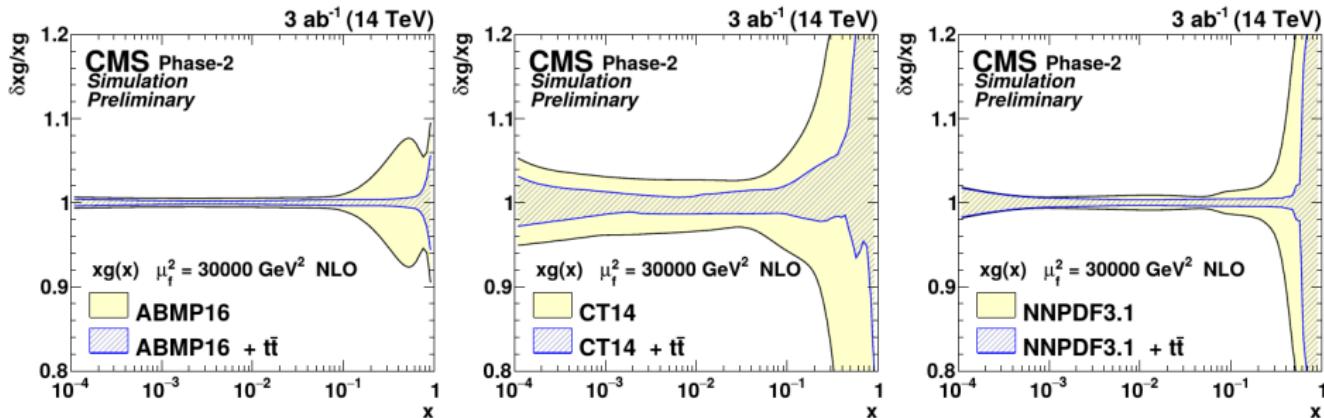
- α_s and $m_t(m_t)$ extracted from the total $t\bar{t}$ cross section at NNLO using different PDF sets
- Theoretical predictions obtained using Hathor interfaced in xFitter
- Furthermore, m_t^{pole} extracted at NNLO+NNLL using Top++

PDF constraints from double-differential $t\bar{t}$ cross sections [1902.04070]

- Presented projection of CMS differential $t\bar{t}$ cross section measurements in $e/\mu+jets$ channel with 3 ab^{-1} at 14 TeV



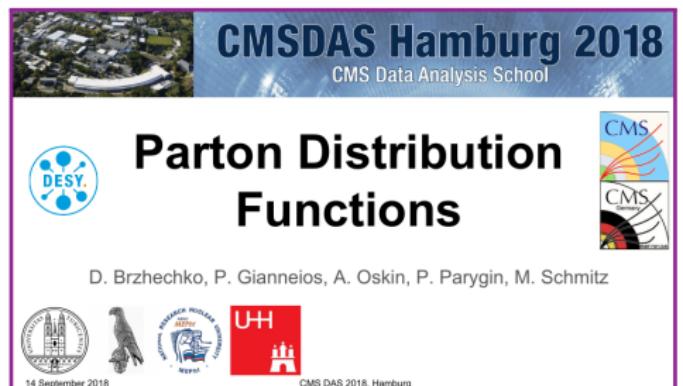
PDF constraints from double-differential $t\bar{t}$ cross sections [1902.04070]



- PDF constraints from differential $t\bar{t}$ cross sections as functions of $M(t\bar{t})$ and $y(t\bar{t})$ are estimated using profiling technique implemented in xFitter
→ strong impact on gluon PDF at high x in any modern PDF set

xFitter at CMS Data Analysis School

- xFitter was presented at CMS Data Analysis School at DESY in September 2018
- The exercises were about getting familiar with PDF fitting using xFitter and studying impact of CMS measurements on PDFs
- The team of young people (new to xFitter) created a “new PDF set” in two days

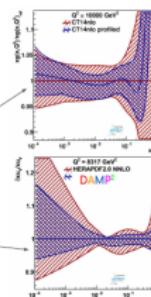


A presentation slide for CMSDAS Hamburg 2018. It features an aerial view of the DESY facility on the left, followed by the text "CMSDAS Hamburg 2018" and "CMS Data Analysis School". Below this, the title "Parton Distribution Functions" is displayed in large bold letters. To the right of the title is the CMS logo. At the bottom, the names D. Brzhechko, P. Gianneios, A. Oskin, P. Parygin, M. Schmitz are listed, along with logos for DESY, UH (University of Hamburg), and other institutions.

14 September 2018 CMS DAS 2018, Hamburg

Conclusions

- Determination of strong coupling depends on PDF sets
 - PDFs are quite important
- Important to know shape and uncertainties
- Important to include as much data as possible
 - Jets improve gluon and allow α_s estimation
 - W and Z data constrain u_v , d_v and sea quarks



The figure consists of two vertically stacked plots. Both plots show the ratio $\alpha_s(Q^2)/\alpha_s(Q_0^2)$ on the y-axis against Q^2 on the x-axis, with logarithmic scales from 10^{-1} to 10^1 . The top plot is for $Q^2 = 10000 \text{ GeV}^2$ and shows a central fit with red and blue shaded regions representing different PDF sets. The bottom plot is for $Q^2 = 6377 \text{ GeV}^2$ and includes additional data points for HERA II (blue triangles) and DAMPE (red triangles). Both plots illustrate how PDF fits change with Q^2 .

14 September 2018 CMS DAS 2018, Hamburg

Summary

- New CMS measurements of $t\bar{t}$ and W+c production facilitate improved determination of proton PDFs
- xFitter as unique open source platform for PDF fitting plays crucial role in data interpretation
- New CMS analyses provide and exploit new developments in xFitter:
 - ▶ 3D $t\bar{t}$ measurement used recent developments in xFitter theory interface
 - ▶ new reaction (KMatrix) was implemented in the context of this analysis
- Future synergy between xFitter team and experimental collaborations is important to fully reveal potential of LHC data

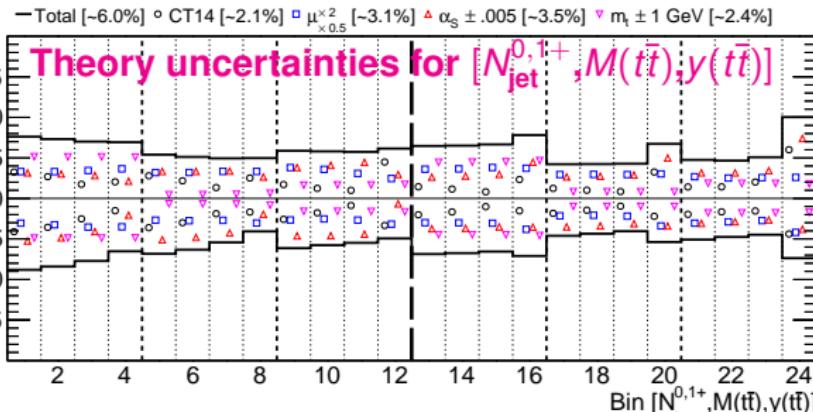
BACKUP

NLO calculations

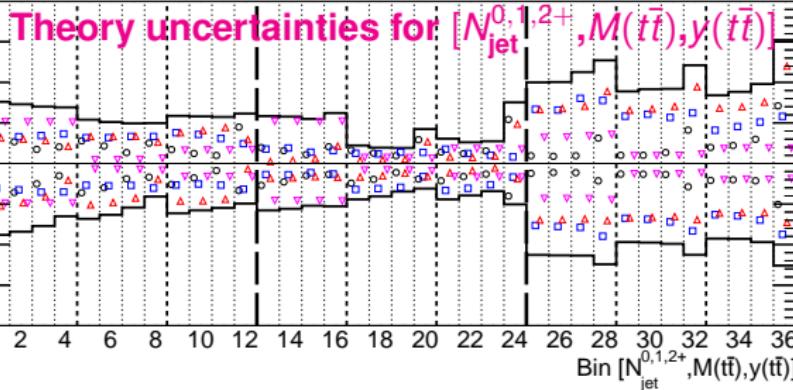
- NLO predictions for inclusive $t\bar{t}$, $t\bar{t} + 1$ jet and $t\bar{t} + 2$ jets are computed and compared to data using MadGraph5_aMC@NLO + aMCfast + ApplGrid + xFitter:
 - ▶ $[N_{\text{jet}}^{0,1+}, M(t\bar{t}), y(t\bar{t})]$ with 2 N_{jet} bins:
 - ★ $\sigma^{\text{NLO}}(N_{\text{jet}} = 0) = \sigma^{\text{NLO}}(t\bar{t}) - \sigma^{\text{NLO}}(t\bar{t} + 1\text{jet})$
 - ★ $\sigma^{\text{NLO}}(N_{\text{jet}} > 0) = \sigma^{\text{NLO}}(t\bar{t} + 1\text{jet})$
 - ▶ $[N_{\text{jet}}^{0,1,2+}, M(t\bar{t}), y(t\bar{t})]$ with 3 N_{jet} bins:
 - ★ $\sigma^{\text{NLO}}(N_{\text{jet}} = 0) = \sigma^{\text{NLO}}(t\bar{t}) - \sigma^{\text{NLO}}(t\bar{t} + 1\text{jet})$
 - ★ $\sigma^{\text{NLO}}(N_{\text{jet}} = 1) = \sigma^{\text{NLO}}(t\bar{t} + 1\text{jet}) - \sigma^{\text{NLO}}(t\bar{t} + 2\text{jets})$
 - ★ $\sigma^{\text{NLO}}(N_{\text{jet}} > 1) = \sigma^{\text{NLO}}(t\bar{t} + 2\text{jets})$
- $\mu_r = \mu_f = H'/2$, $H' = \sum_i m_{T,i}$ where the sum runs over all final-state partons (t, \bar{t} and up to three light partons in the $t\bar{t} + 2$ jets calculations) and $m_T = \sqrt{m^2 + p_T^2}$. Uncertainties:
 - ▶ μ_r, μ_f are varied by factor 2 (6 variations in total)
 - ▶ alternative functional form $\mu_r = \mu_f = H/2$, $H = \sum_i m_{T,i}$ with the sum runs over t and \bar{t}
- $m_t^{\text{pole}} = 172.5 \pm 1$ GeV (sometimes ± 5 GeV for presentation purposes)
- PDFs and α_s from several groups via LHAPDF, $\alpha_s \pm 0.001$ for uncertainties (sometimes ± 0.005 for presentation purposes)
- multiplied with non-perturbative corrections (< 5%) from parton to particle jet level
(BACKUP)

Data and theory uncertainties $[N_{\text{jet}}^{0,1+}, M(t\bar{t}), y(t\bar{t})]$

Uncertainty [%]



Total [-6.0%] ° CT14 [-2.1%] □ $\mu_{\times 0.5}^{x^2}$ [-3.1%] ▲ $\alpha_S \pm .005$ [-3.5%] ▼ $m_t \pm 1 \text{ GeV}$ [-2.4%]



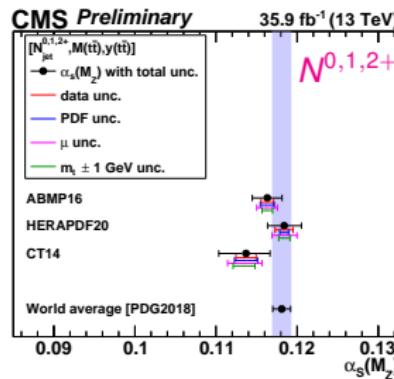
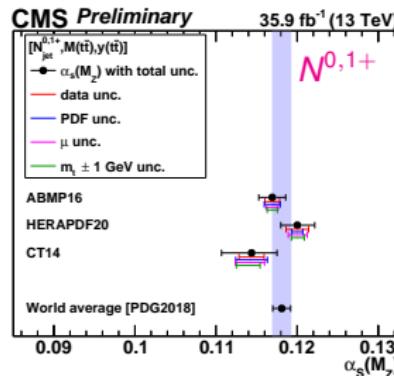
Total [-7.0%] ° CT14 [-2.2%] □ $\mu_{\times 0.5}^{x^2}$ [-3.9%] ▲ $\alpha_S \pm .005$ [-4.0%] ▼ $m_t \pm 1 \text{ GeV}$ [-2.4%]

- Bins are grouped for $y(t\bar{t})$, $M(t\bar{t})$ and N_{jet} (separated by different vertical lines)
- NLO scale uncertainties are comparable to PDF, α_S and m_t uncertainties
→ data can constrain PDF, α_S and m_t
- Scale uncertainties are considerably smaller for $[N_{\text{jet}}^{0,1+}, M(t\bar{t}), y(t\bar{t})]$
→ $[N_{\text{jet}}^{0,1,2+}, M(t\bar{t}), y(t\bar{t})]$ is used for cross check only

Cross checks

Cross checks of α_s and m_t^{pole} extraction (all results in backup):

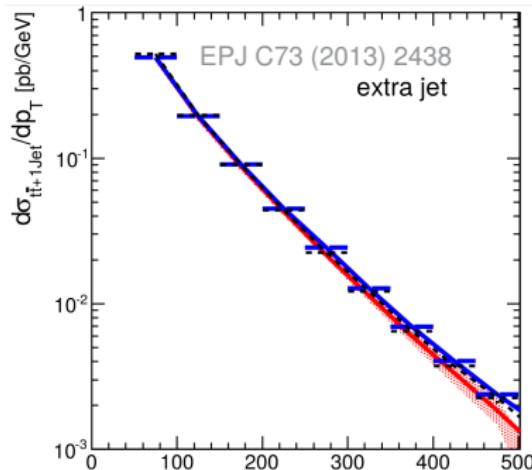
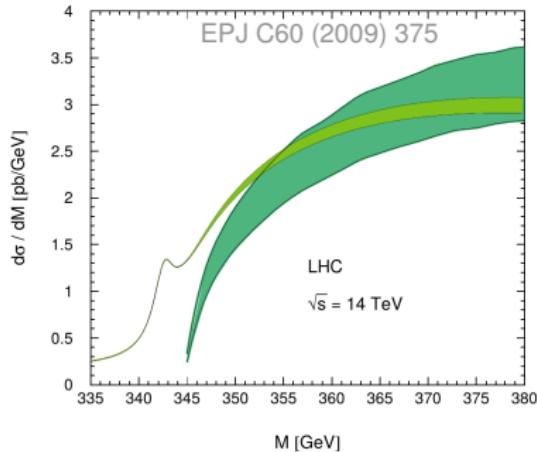
- using $[N_{\text{jet}}^{0,1,2+}, M(t\bar{t}), y(t\bar{t})]$
- using single-differential N_{jet} , $M(t\bar{t})$ or $y(t\bar{t})$ cross sections
- using $[p_T(t\bar{t}), M(t\bar{t}), y(t\bar{t})]$ cross sections with 2 $p_T(t\bar{t})$ bins
- using unnormalised cross sections
- consistent results obtained in all cross checks
- in this analysis, observables ($\frac{1}{\sigma} \frac{d\sigma}{d\ldots}$) have been chosen to have **maximum sensitivity to QCD parameters and minimum experimental and scale uncertainties**



Remarks on limitations in theory calculations

NLO is the only available theory publicly available today, but there are limitations:

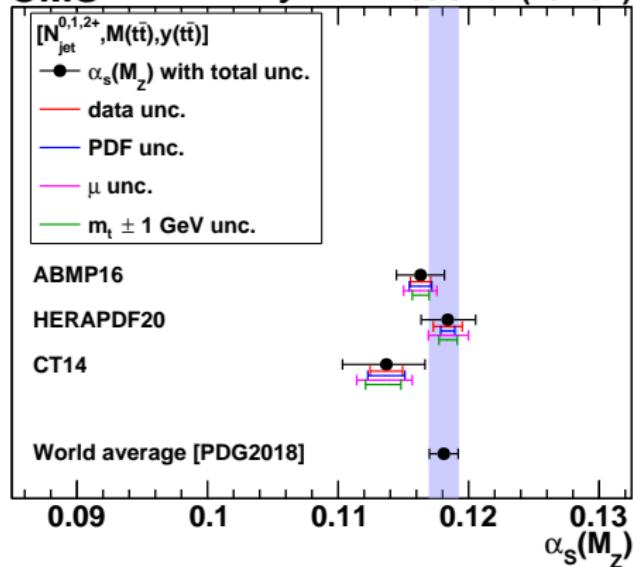
- impact of missing threshold resummation is $\Delta m_t \sim 0.7$ GeV [Eur.Phys.J. C60 (2009) 375]
- impact of missing FSR resummation is $\Delta m_t \sim 0.5$ GeV [Eur. Phys. J. C73 (2013) 2438]
 - ▶ in general, good agreement between NLO and NLO+PS [Fig. 1 in Eur. Phys. J. C73 (2013) 2438]
- EW corrections could be a few % near threshold [Phys. Rev. D91 (2015) 014020] [JHEP10 (2017) 186]
- **most wanted is NNLO QCD**



α_s and m_t^{pole} from $[N_{\text{jet}}, m_{\text{tt}}, y(t\bar{t})]$ with 3 N_{jet} bins

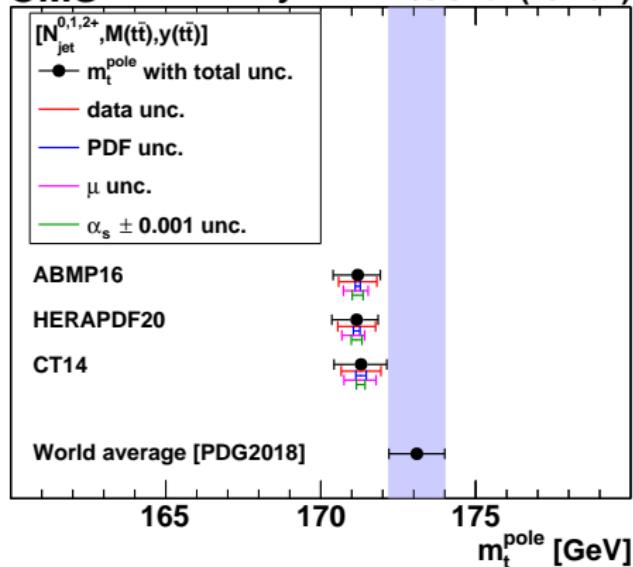
CMS Preliminary

35.9 fb⁻¹ (13 TeV)



CMS Preliminary

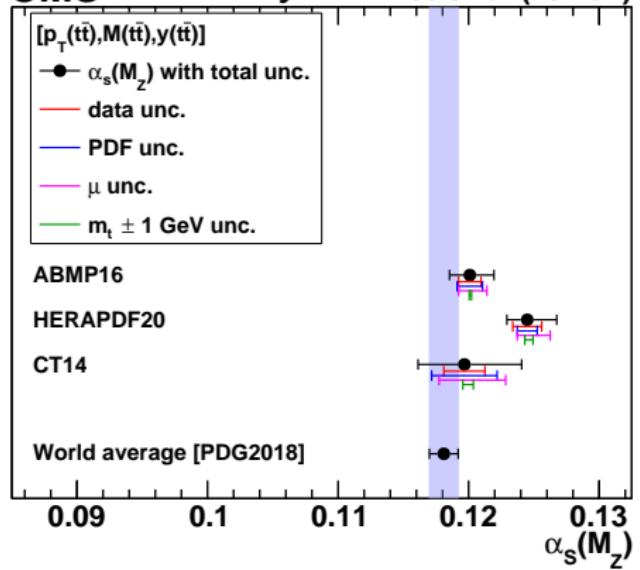
35.9 fb⁻¹ (13 TeV)



α_s and m_t^{pole} from $[p_T(t\bar{t}), m_{t\bar{t}}, y(t\bar{t})]$ with 2 $p_T(t\bar{t})$ bins

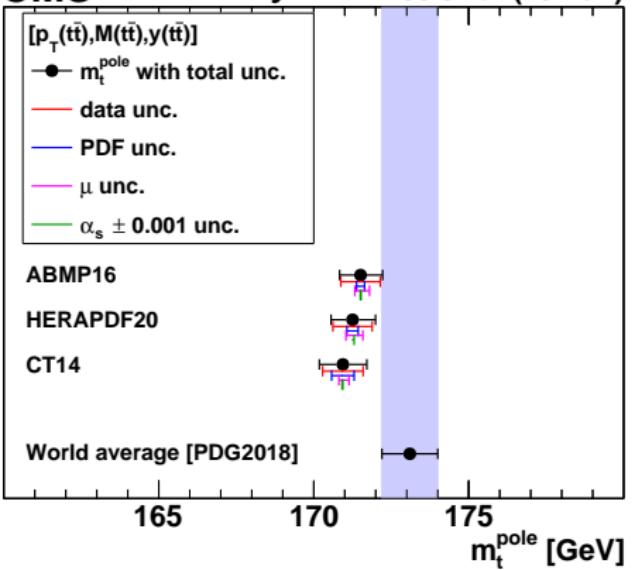
CMS Preliminary

35.9 fb^{-1} (13 TeV)



CMS Preliminary

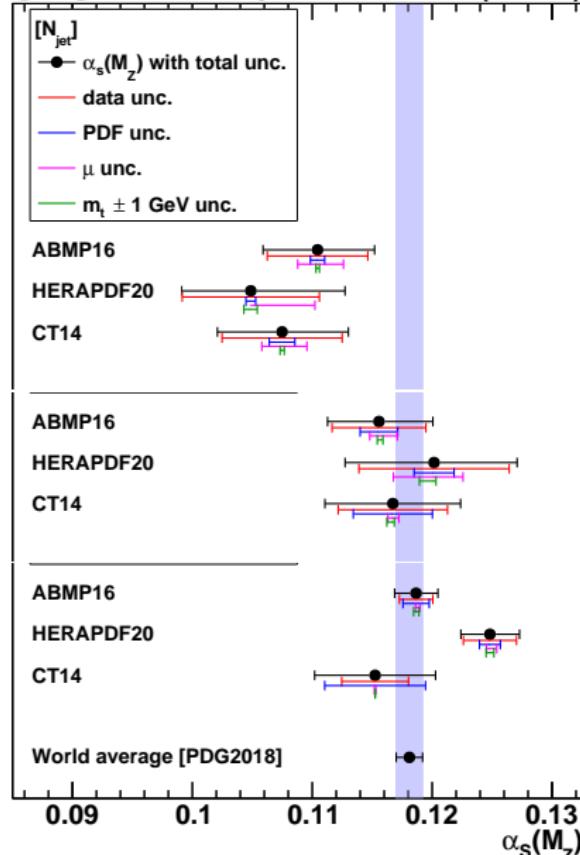
35.9 fb^{-1} (13 TeV)



α_s and m_t^{pole} from single-differential cross sections

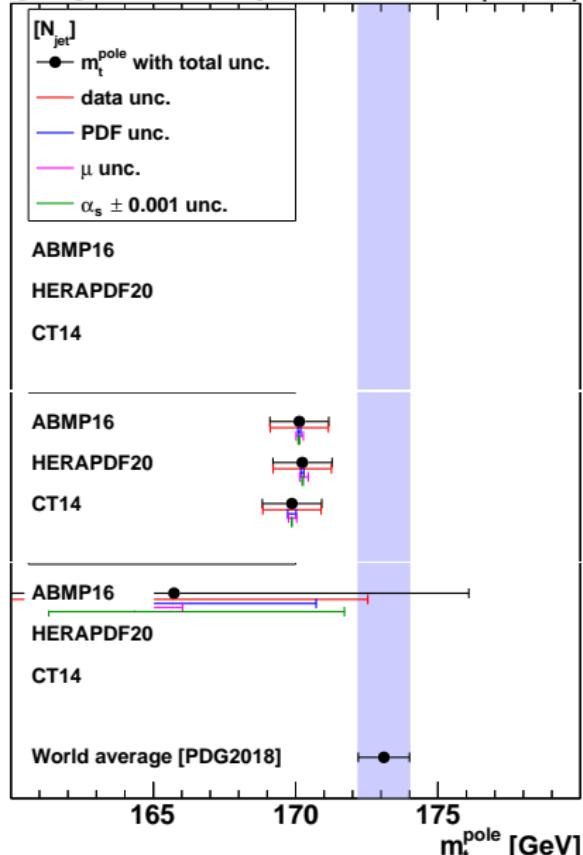
CMS Preliminary

35.9 fb⁻¹ (13 TeV)



CMS Preliminary

35.9 fb⁻¹ (13 TeV)



Simultaneous PDF $+\alpha_s + m_t^{\text{pole}}$ fit: settings

- followed standard approach: using HERA DIS data only, or HERA + $t\bar{t}$ data to demonstrate added value from $t\bar{t}$ on PDF and α_s determination
- settings follow HERAPDF2.0 fit (very similar to TOP-14-013), use xFitter-2.0.0
- input data: combined HERA DIS [1506.06042] + $t\bar{t}$
- RTOPT, $M_c = 1.47 \text{ GeV}$, $M_b = 4.5 \text{ GeV}$, $Q_{\min}^2 = 3.5^{+1.5}_{-1.0} \text{ GeV}^2$
- predictions for $t\bar{t}$ data via MadGraph5_aMC@NLO + aMCfast + ApplGrid,
 $\mu_r = \mu_f = H_t/4$, $H_t = \sqrt{m_t^2 + (p_T(t))^2} + \sqrt{m_{\bar{t}}^2 + (p_T(\bar{t}))^2}$ varied by factor 2
 - dependence on α_s and scales written in ApplGrid tables
 - dependence on m_t^{pole} derived by linear interpolation between tables generated with different values of m_t^{pole} (new feature for xFitter)
 - kinematic range probed by $t\bar{t}$: $x = (M(t\bar{t})/\sqrt{s}) \exp[\pm y(t\bar{t})] \Rightarrow 0.01 \lesssim x \lesssim 0.1$
- 15-parameter form (backup) determined using parametrisation scan (one extra g parameter required by $t\bar{t}$ data) at $Q_0^2 = 1.9 \text{ GeV}^2$, $f_s = 0.4 \pm 0.1$
- DGLAP NLO PDF evolution via QCDNUM-17.01.14
- PDF uncertainties: fit ($\Delta\chi^2 = 1$ via HESSE, cross checked with MC replica method), model and parametrisation; in addition for α_s and m_t^{pole} scale uncertainties for $t\bar{t}$ are considered

Simultaneous PDF, α_s and m_t^{pole} fit: PDF parametrisation

Determined using parametrisation scan:

$$x_g(x) = A_g x^{B_g} (1-x)^{C_g} (1+E_g x^2) - A'_g x^{B'_g} (1-x)^{C'_g},$$

$$x_{u_v}(x) = A_{u_v} x^{B_{u_v}} (1-x)^{C_{u_v}} (1+D_{u_v} x),$$

$$x_{d_v}(x) = A_{d_v} x^{B_{d_v}} (1-x)^{C_{d_v}},$$

$$x\bar{U}(x) = A_{\bar{U}} x^{B_{\bar{U}}} (1-x)^{C_{\bar{U}}} (1+D_{\bar{U}} x),$$

$$x\bar{D}(x) = A_{\bar{D}} x^{B_{\bar{D}}} (1-x)^{C_{\bar{D}}},$$

- additional gluon parameter (E_g) required by new $t\bar{t}$ data
- PDF parametrisation uncertainties given by $A'_g = 0$ (13p) and $E_g = 0$ (14p), and $Q_0^2 = 1.9 \pm 0.3 \text{ GeV}^2$ variation