## Flavor in high-energy cosmic neutrinos: Interpretation and new challenges

Mauricio Bustamante

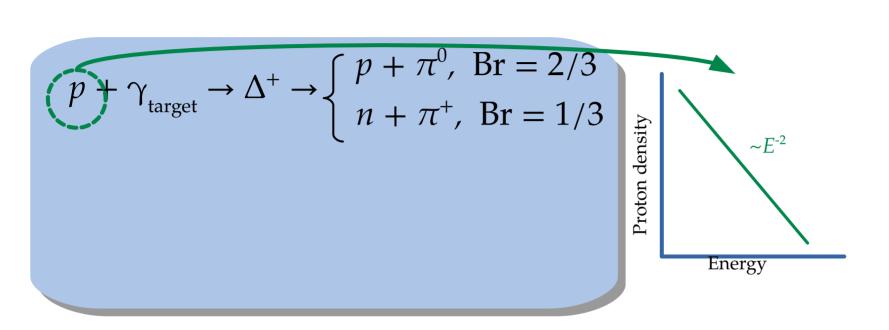
Niels Bohr Institute, University of Copenhagen

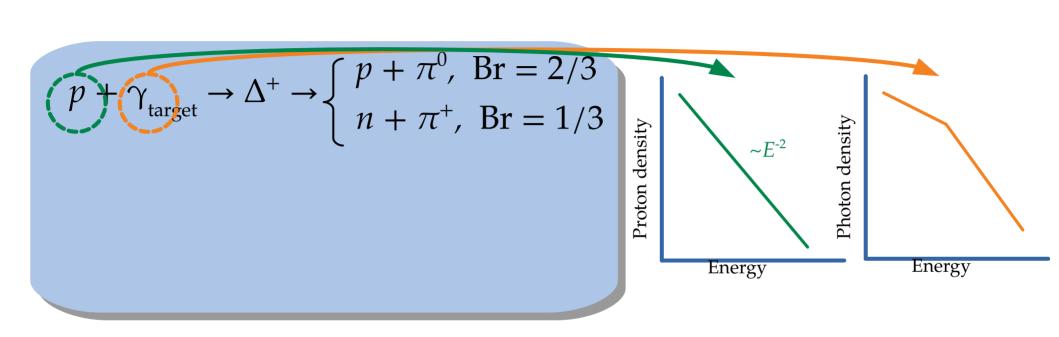


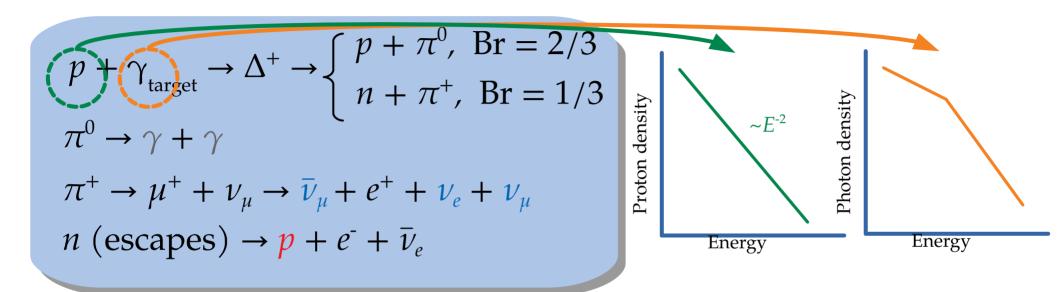
PAHEN Berlin, September 27, 2019



$$p + \gamma_{\text{target}} \rightarrow \Delta^{+} \rightarrow \begin{cases} p + \pi^{0}, \text{ Br} = 2/3\\ n + \pi^{+}, \text{ Br} = 1/3 \end{cases}$$





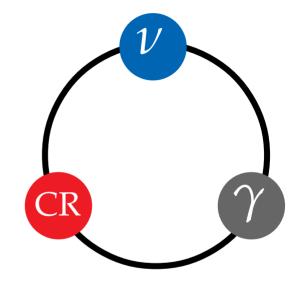


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$$\pi^{0} \rightarrow \gamma + \gamma$$

$$\pi^{+} \rightarrow \mu^{+} + \nu_{\mu} \rightarrow \bar{\nu}_{\mu} + e^{+} + \nu_{e} + \nu_{\mu}$$

$$n \text{ (escapes)} \rightarrow p + e^{-} + \bar{\nu}_{e}$$



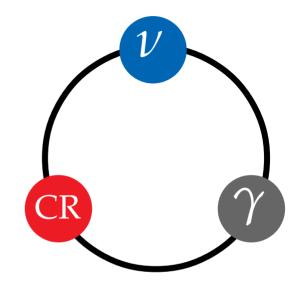
Neutrino energy = Proton energy / 20 Gamma-ray energy = Proton energy / 10

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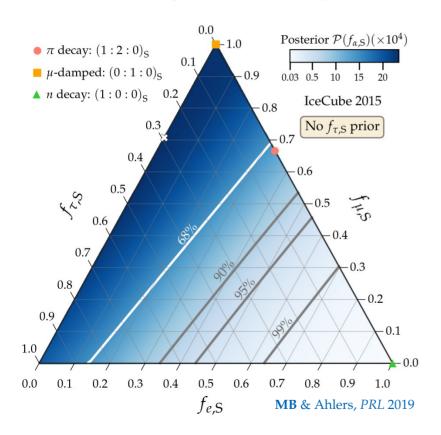


1 PeV 20 PeV

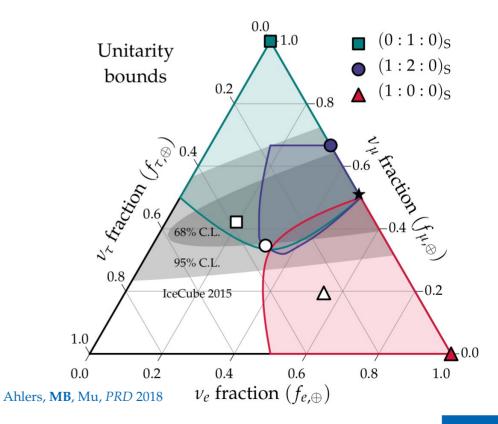
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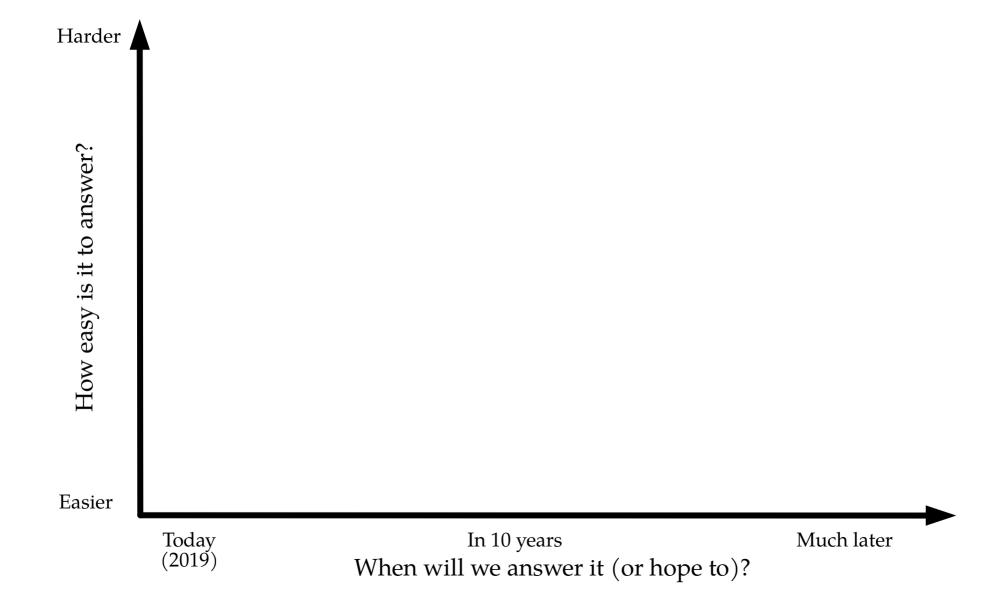
### Flavor is a two-edged sword (one that's increasingly sharper)

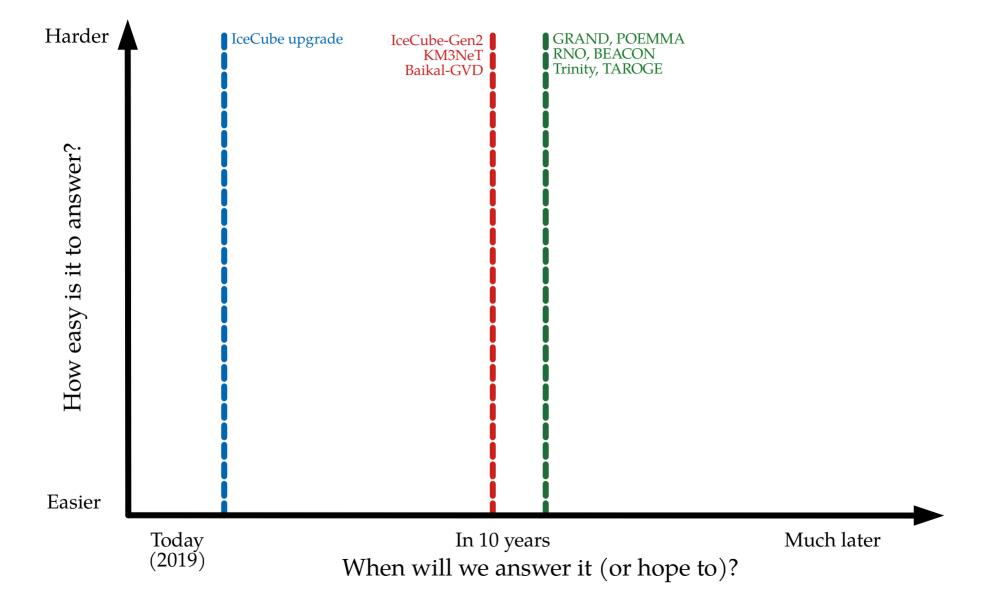
Trusting particle physics and learning about astrophysics

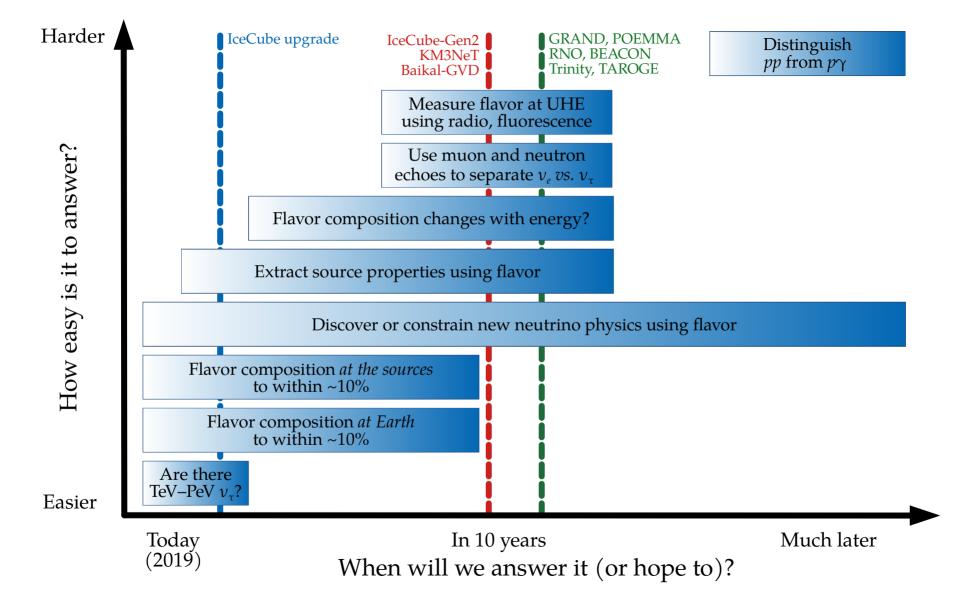


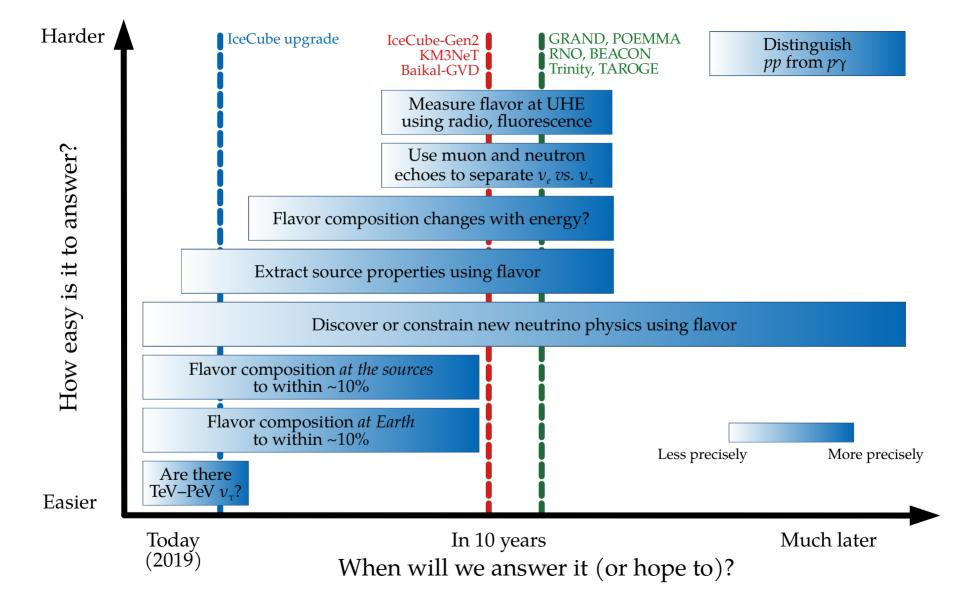
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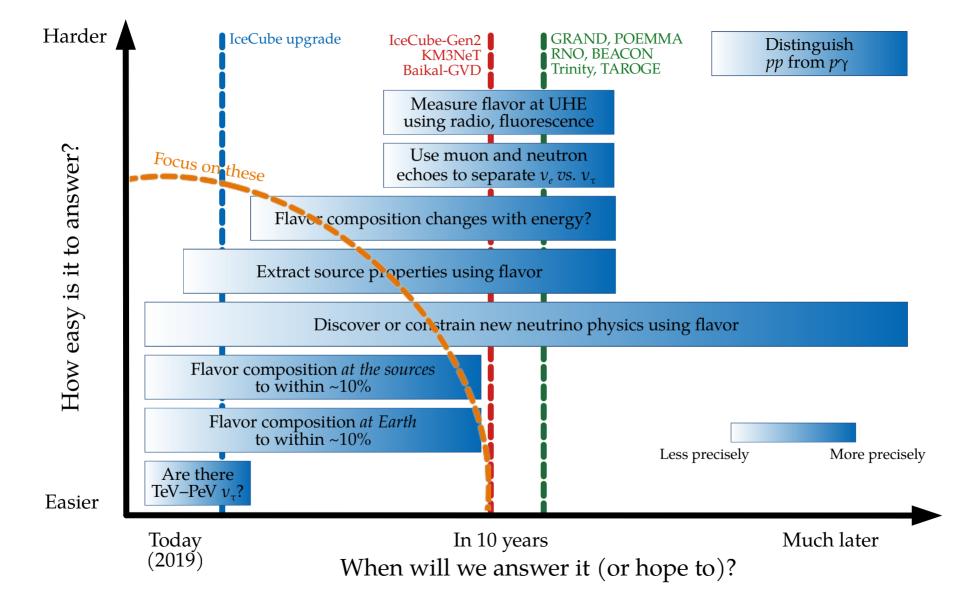






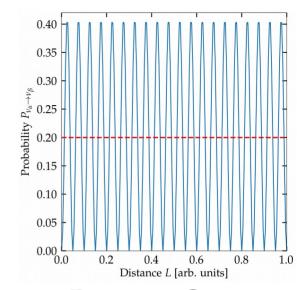






## High-energy neutrinos oscillate fast

$$P_{\nu_{\alpha} \to \nu_{\beta}} = \delta_{\alpha\beta} - 4 \sum_{i>j} \operatorname{Re}(U_{\alpha i}^* U_{\beta i} U_{\alpha j} U_{\beta j}^*) \sin^2\left(\Delta m_{ij}^2 \frac{L}{4E}\right) + 2 \sum_{i>j} \operatorname{Im}(U_{\alpha i}^* U_{\beta i} U_{\alpha j} U_{\beta j}^*) \sin\left(\Delta m_{ij}^2 \frac{L}{2E}\right)$$



Oscillation length for 1-TeV  $\nu$ :  $2\pi \times 2E/\Delta m^2 \sim 0.1$  pc

~ 8% of the way to Proxima Centauri

≪ Distance to Galactic Center (8 kpc)

≪ Distance to Andromeda (1 Mpc)

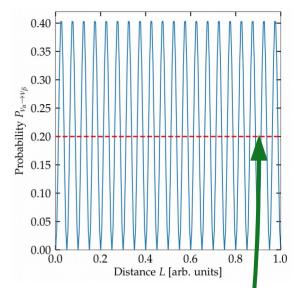
≪ Cosmological distances (few Gpc)

We cannot resolve oscillations, so we use instead the average probability:

$$\langle P_{\nu_{\alpha} \to \nu_{\beta}} \rangle = \sum_{i=1}^{3} |U_{\alpha i}|^{2} |U_{\beta i}|^{2} \qquad \begin{array}{l} \text{Mixing parameters} \\ \text{(NuFit 4.1, normal mass ordering):} \\ \theta_{23} \approx 48^{\circ}, \, \theta_{13} \approx 9^{\circ}, \, \theta_{12} \approx 34^{\circ}, \, \delta \approx 222^{\circ} \end{array}$$

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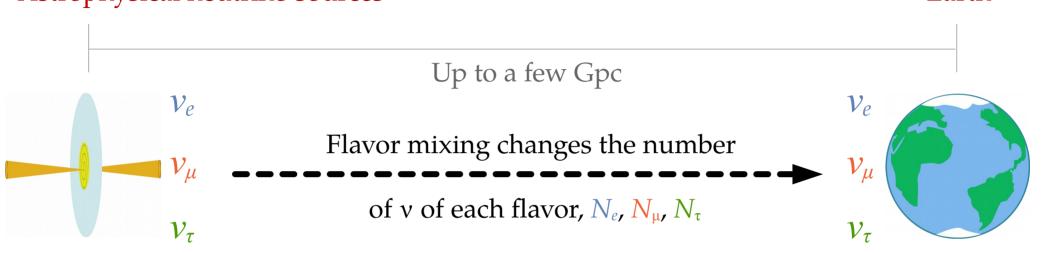
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## Flavor composition basics

Astrophysical neutrino sources

Earth



▶ Different processes yield different ratios of neutrinos of each flavor:

$$(f_{e,S},f_{\mu,S},f_{\tau,S})\equiv(N_{e,S},N_{\mu,S},N_{\tau,S})/N_{\mathrm{tot}}$$

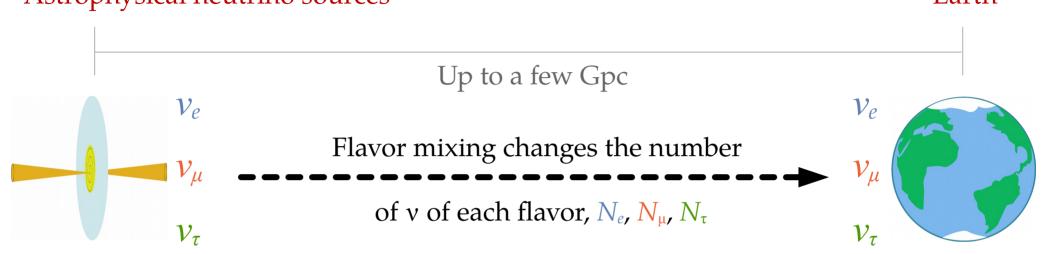
► Flavor ratios at Earth ( $\alpha = e, \mu, \tau$ ):

$$f_{\alpha,\oplus} = \sum_{\beta=e,\mu,\tau} P_{\nu_{\beta}\to\nu_{\alpha}} f_{\beta,S}$$

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Standard oscillations or new physics

## Why are flavor ratios useful?

▶ The normalization of the flux is uncertain – but it cancels out in flavor ratios:

α-flavor ratio at Earth 
$$(f_{\alpha,\oplus}) = \frac{\text{Flux at Earth of } \nu_{\alpha} (\alpha = e, \mu, \tau)}{\text{Sum of fluxes of all flavors}}$$

- ► Ratios remove systematic uncertainties common to all flavors
- ► Flavor ratios are useful in astrophysics and particle physics

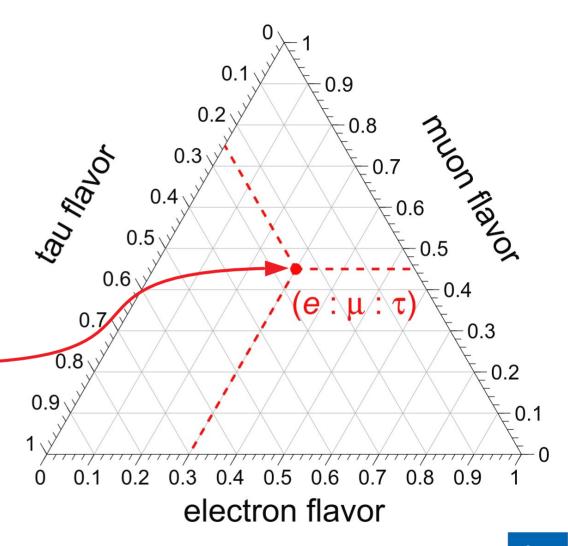
*Note:* Ratios are for  $\nu + \bar{\nu}$ , since neutrino telescopes cannot tell them apart

## Reading a ternary plot

Assumes underlying unitarity – sum of projections on each axis is 1

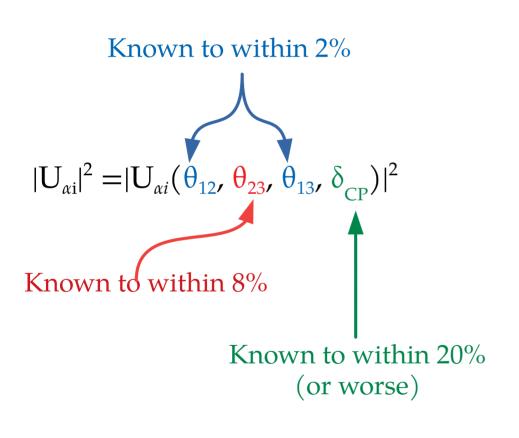
How to read it: Follow the tilt of the tick marks, *e.g.*,

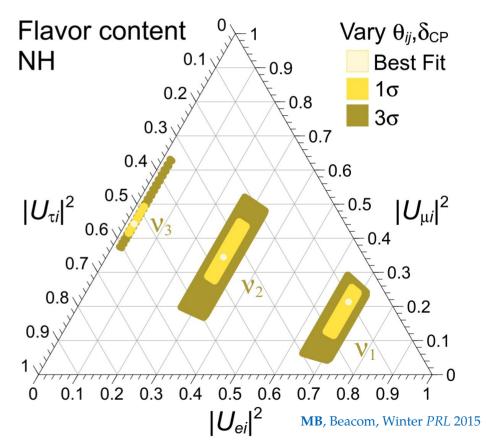
$$(e:\mu:\tau) = (0.30:0.45:0.25)$$



### Flavor content of neutrino mass eigenstates

Flavor content for every allowed combination of mixing parameters –

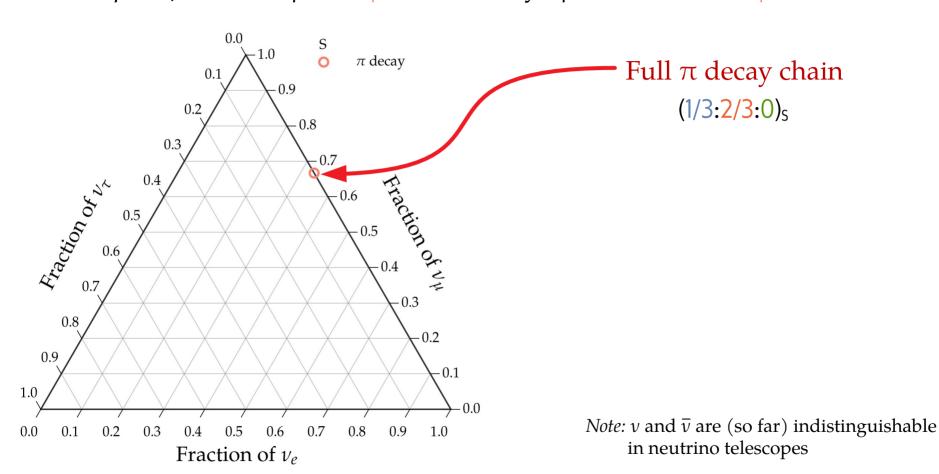


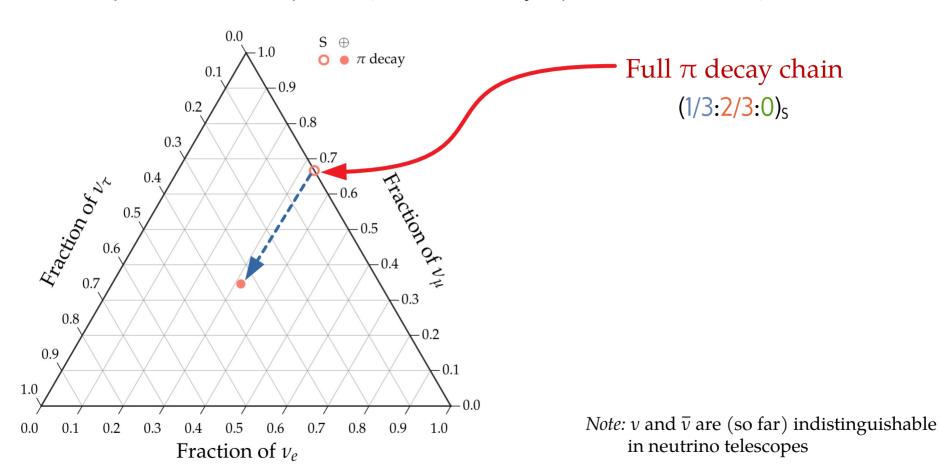


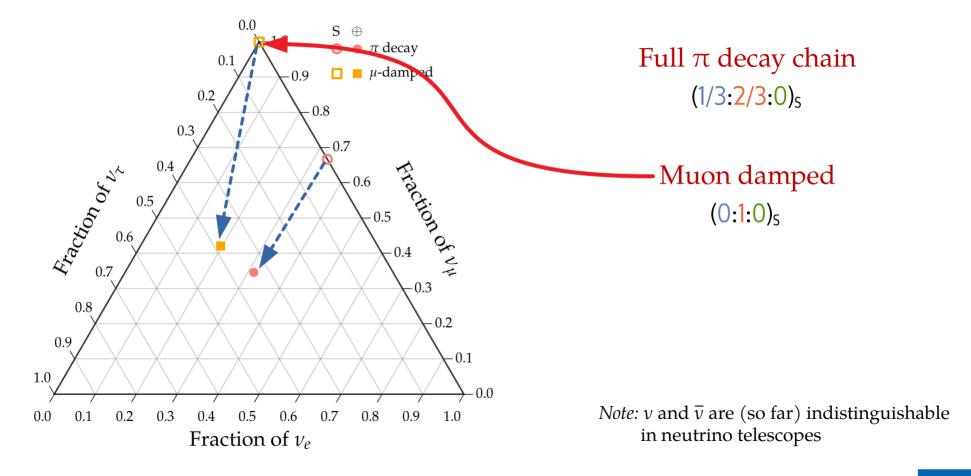
One likely TeV–PeV 
$$\nu$$
 production scenario:  $p + \gamma \rightarrow \pi^+ \rightarrow \mu^+ + \nu_{\mu}$  followed by  $\mu^+ \rightarrow e^+ + \nu_e + \overline{\nu}_{\mu}$ 

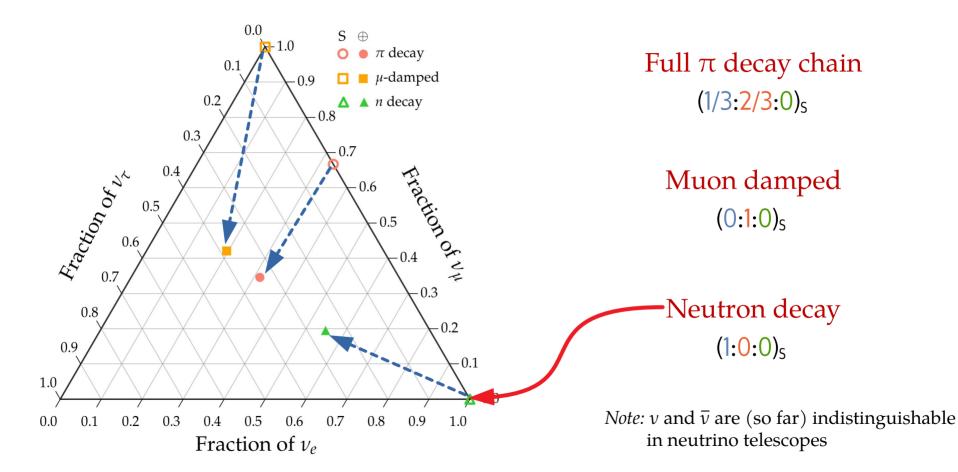
Full  $\pi$  decay chain (1/3:2/3:0)<sub>5</sub>

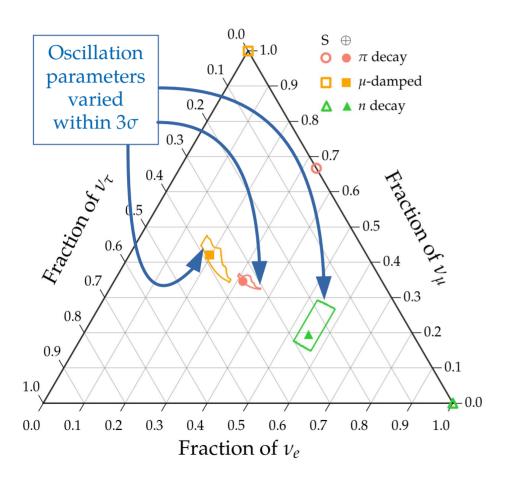
*Note:* v and  $\bar{v}$  are (so far) indistinguishable in neutrino telescopes









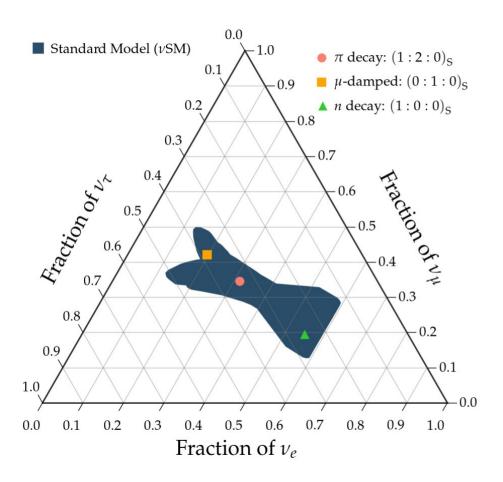


Full  $\pi$  decay chain (1/3:2/3:0)<sub>s</sub>

Muon damped (0:1:0)<sub>s</sub>

Neutron decay (1:0:0)<sub>S</sub>

*Note:* v and  $\bar{v}$  are (so far) indistinguishable in neutrino telescopes



All possible flavor ratios at the sources

+

Vary oscillation parameters within  $3\sigma$ 

*Note:* v and  $\bar{v}$  are (so far) indistinguishable in neutrino telescopes

### How does IceCube see TeV-PeV neutrinos?

#### Deep inelastic neutrino-nucleon scattering

Neutral current (NC)

Charged current (CC)

$$\nu_x + N \rightarrow \nu_x + X$$

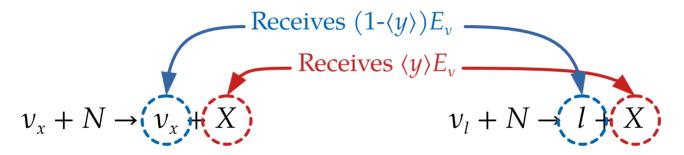
$$v_l + N \rightarrow l + X$$

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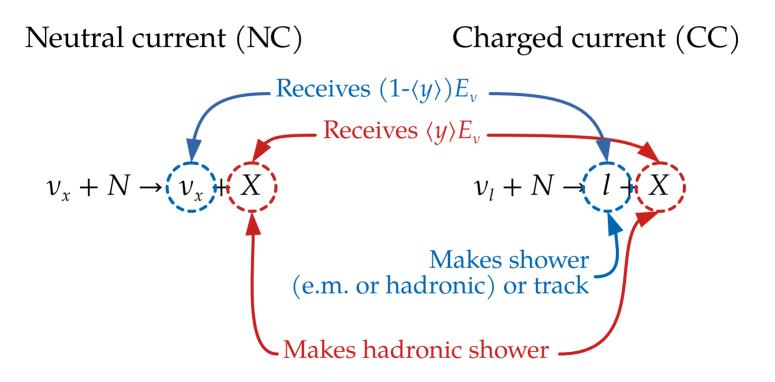
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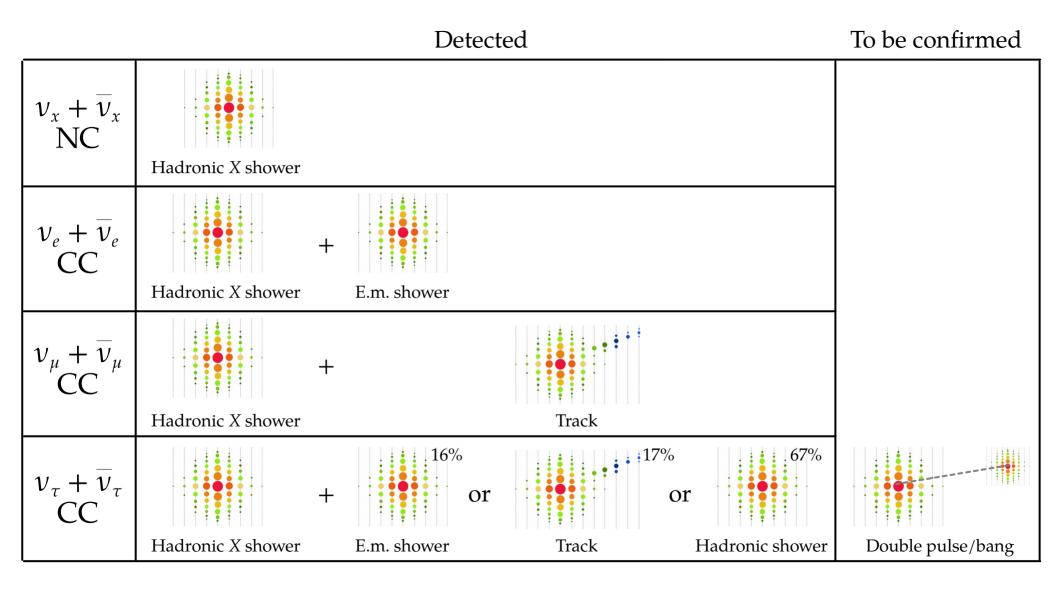


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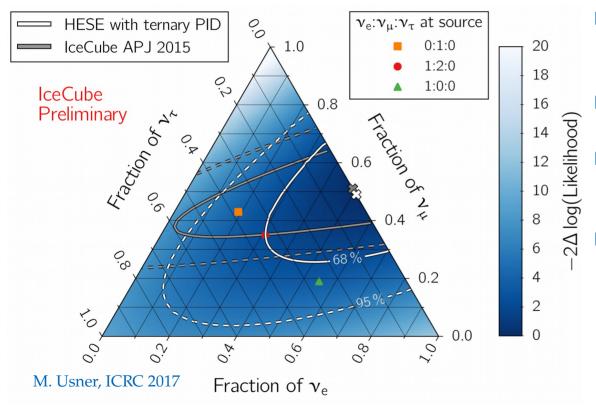
#### Deep inelastic neutrino-nucleon scattering



At TeV–PeV, the average inelasticity  $\langle y \rangle = 0.25-0.30$ 



## IceCube results: Flavor composition

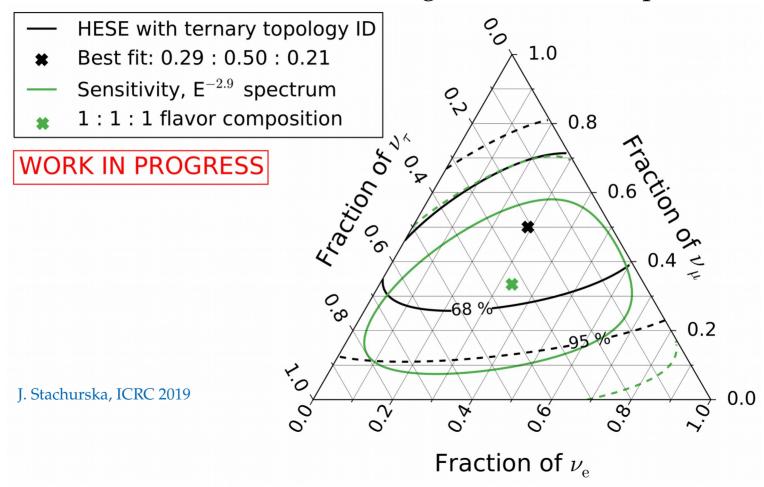


- ► Compare number of tracks  $(v_{\mu})$  vs. showers (all flavors)
- ► Best fit:  $(f_e:f_\mu:f_\tau)_{\oplus} = (0.5:0.5:0)_{\oplus}$
- ► Compatible with standard source compositions
- ► Lots of room for improvement: more statistics, better flavor-tagging

Li, MB, Beacom PRL 2019

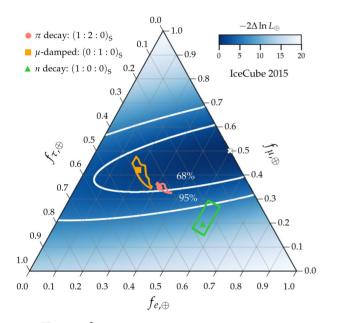
## IceCube results: Flavor composition

There are 2  $\nu_{\tau}$  candidate events which change the flavor composition:



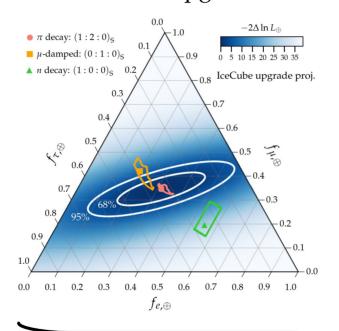
### Flavor composition: now and in the future

#### Today IceCube

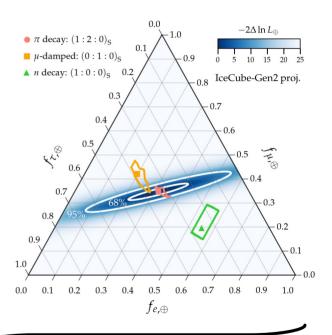


- ► Best fit:  $(f_e:f_u:f_\tau)_{\oplus} = (0.5:0.5:0)_{\oplus}$
- ► Compatible with standard source compositions
- ▶ Hints of one  $\nu_{\tau}$  (not shown)

#### Near future (2022) IceCube upgrade



#### In 10 years (2030s) IceCube-Gen2



Assuming production by the full pion decay chain

Plus possibly better flavor-tagging, *e.g.*, muon and neutron echoes [Li, MB, Beacom *PRL* 2019]

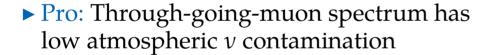
## High-energy cosmic neutrinos made in neutron decays?

 $1. \times 10^{-}$ 

- ▶ Palladino, EPIC 2019
- ▶ Join the two IceCube spectrum fits:

From HESE + through-going muons:  $\Phi \propto E^{-2.5\pm0.1}$ Use it between 30 and 200 TeV

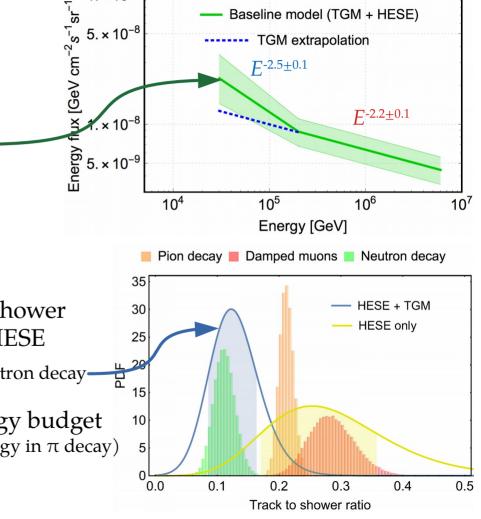
From only through-going muons:  $\Phi \propto E^{-2.2\pm0.1}$ Use it above 200 TeV



▶ Using the broken power law, compute track-to-shower ratio r ( $\sim f_{\nu,\oplus}/f_{e,\oplus}$ ) of astrophysical  $\nu$  in 7.5 yr of HESE

Fit to HESE data favors high content of  $v_e + \overline{v}_e$ , like from neutron decay—

▶ Main problem with this interpretation: the energy budget  $\overline{\nu}_e$  from *n* decay gets 0.1% of the *n* energy (vs. 5% of the *p* energy in  $\pi$  decay)



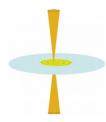
Baseline model (TGM + HESE)

## Inferring the flavor composition at the sources

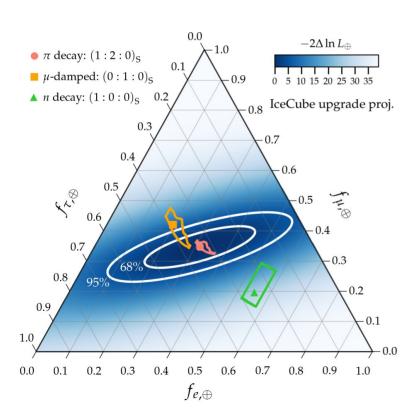
**Measured:** Flavor ratios at Earth



Invert flavor oscillations

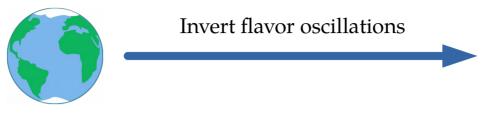


Inferred:
Flavor ratios at astrophysical sources

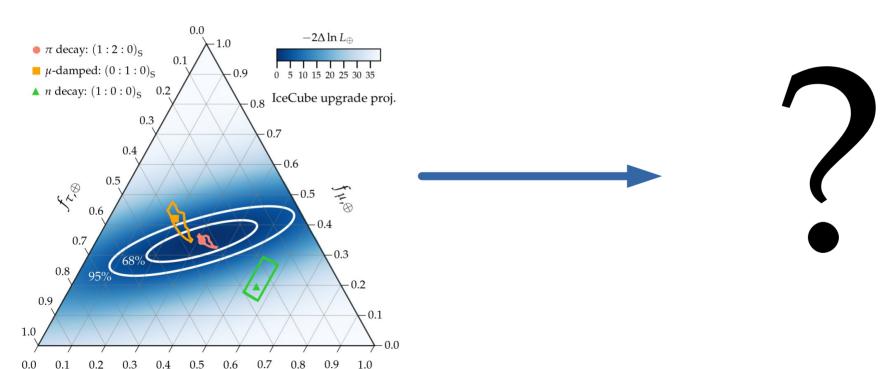




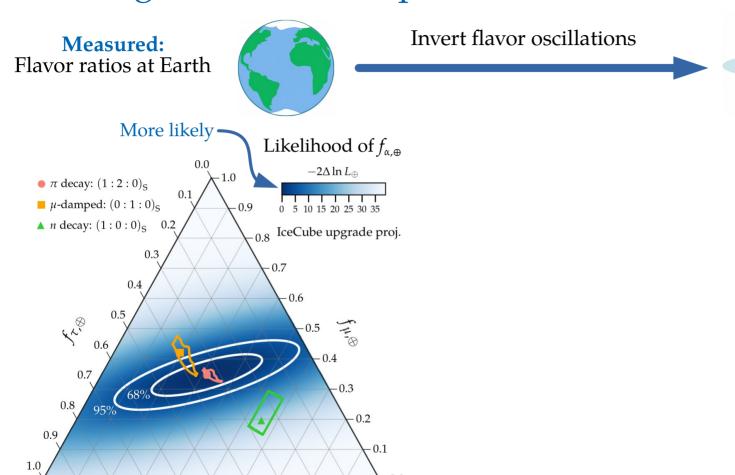
 $f_{e,\oplus}$ 



Inferred:
Flavor ratios at astrophysical sources



**MB** & Ahlers, *PRL* 2019



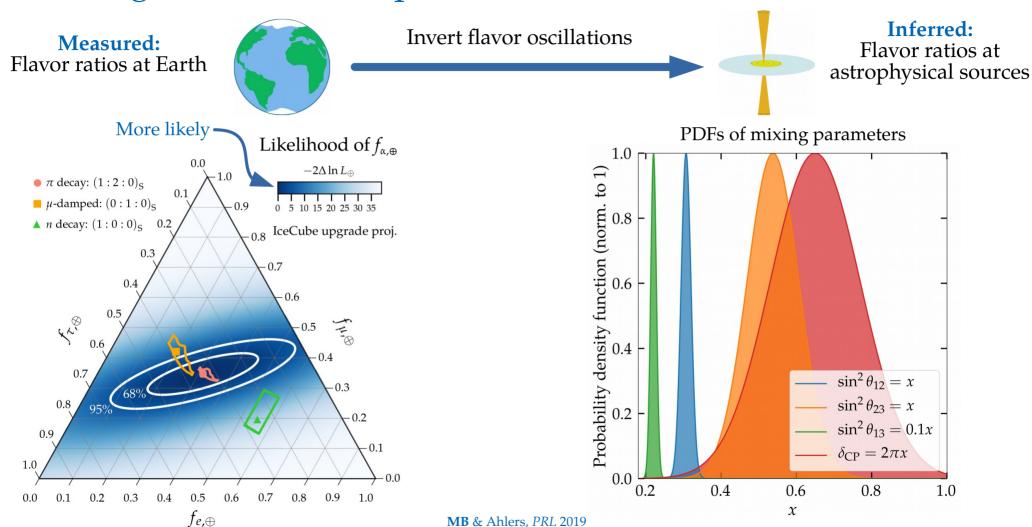
0.8

0.3

0.4

0.5 *fe,*⊕ **Inferred:** 

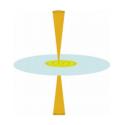
Flavor ratios at astrophysical sources



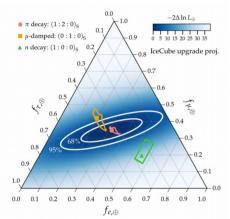
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Inferred:
Flavor ratios at astrophysical sources



Posterior probability density of  $f_{\alpha,S}$  being the flavor ratios at the sources:

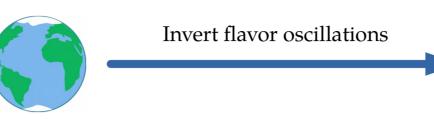
$$\mathcal{P}(f_{\alpha,S}) \equiv \int d\boldsymbol{\theta} \frac{\mathcal{P}(\boldsymbol{\theta})}{\mathcal{N}(\boldsymbol{\theta})} \mathcal{L}_{\oplus} [f_{e,\oplus}(f_{\alpha,S},\boldsymbol{\theta}), f_{\mu,\oplus}(f_{\alpha,S},\boldsymbol{\theta})]$$
$$\boldsymbol{\theta} \equiv (\theta_{12}, \theta_{23}, \theta_{13}, \delta_{\mathrm{CP}})$$

$$\begin{array}{c} \text{1.0} \\ \text{(I o)} \\ \text{(I o$$

Normalization: 
$$\mathcal{N}(oldsymbol{ heta}) \equiv \int\limits_0^1 \mathrm{d}f_{e,\mathrm{S}} \int\limits_0^{1-f_{e,\mathrm{S}}} \mathrm{d}f_{\mu,\mathrm{S}} \,\, \mathcal{L}_\oplus \left[ f_{e,\oplus}(f_{lpha,\mathrm{S}},oldsymbol{ heta}), f_{\mu,\oplus}(f_{lpha,\mathrm{S}},oldsymbol{ heta}) 
ight]$$

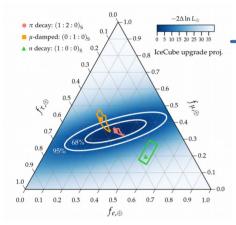
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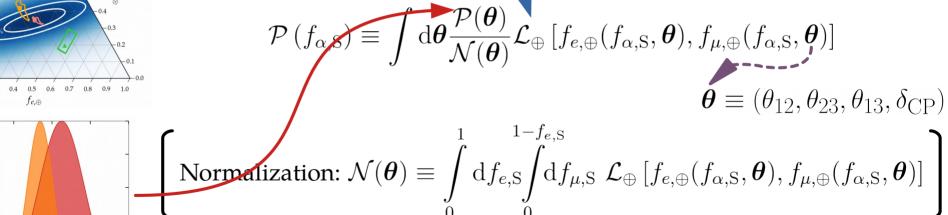
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Flavor ratios at astrophysical sources



Probability density function (norm. to 1) 8.0 8.0 8.0

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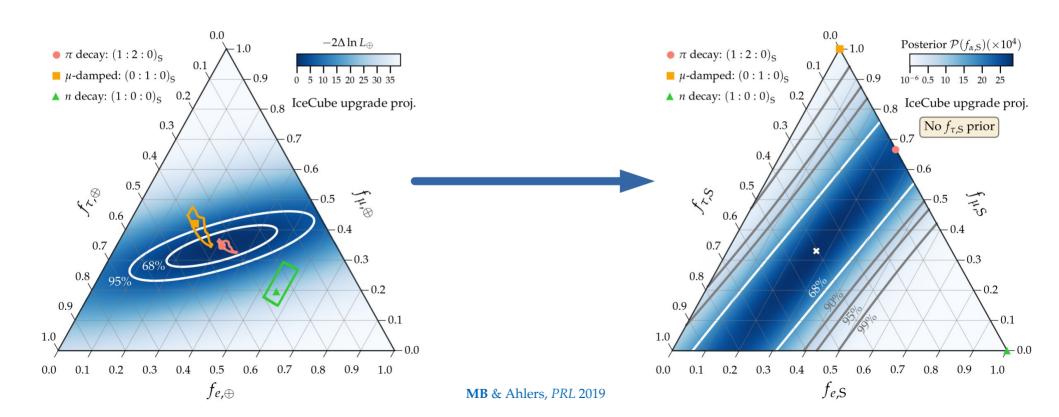


MB & Ahlers, PRL 2019

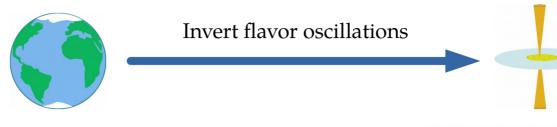


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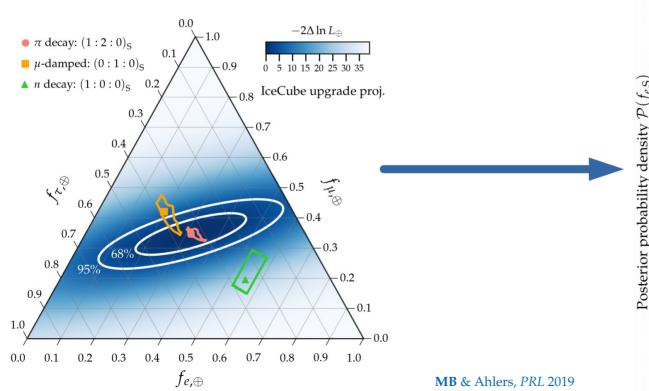


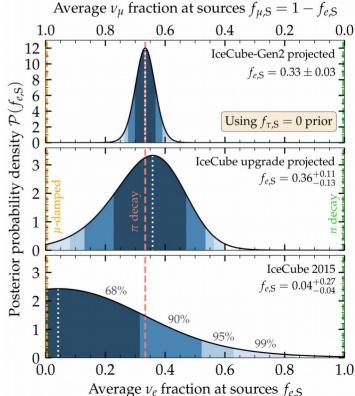




#### **Inferred:**

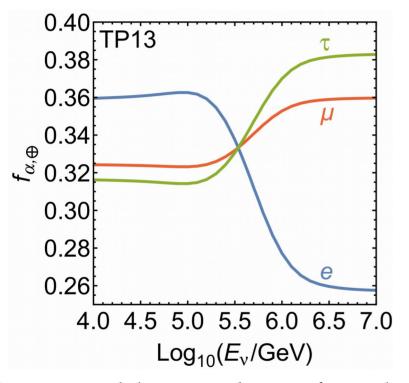
Flavor ratios at astrophysical sources

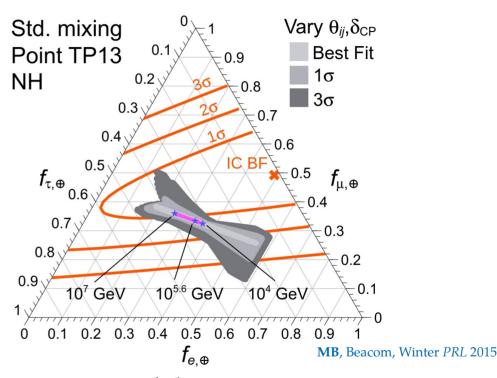




#### Energy dependence of the flavor composition?

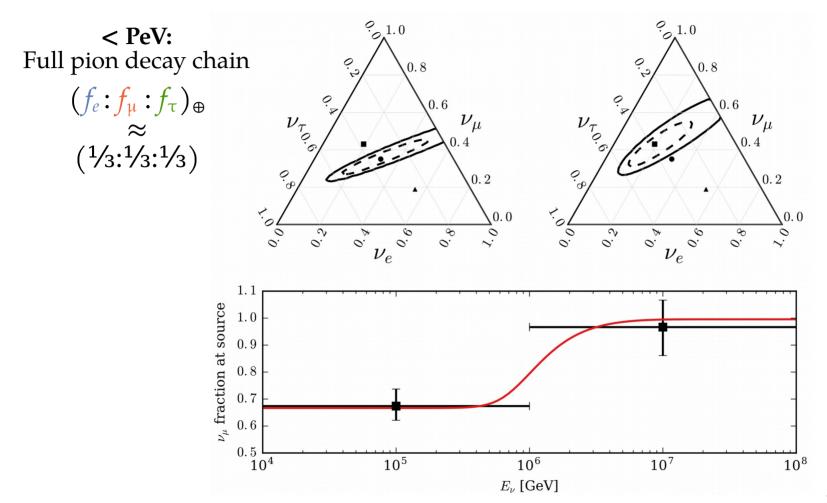
Different neutrino production channels accessible at different energies –





- ► TP13:  $p\gamma$  model, target photons from electron-positron annihilation [Hümmer et al., Astropart. Phys. 2010]
- ► Will be difficult to resolve [Kashti, Waxman, PRL 2005; Lipari, Lusignoli, Meloni, PRD 2007]

#### ... Observable in IceCube-Gen2?



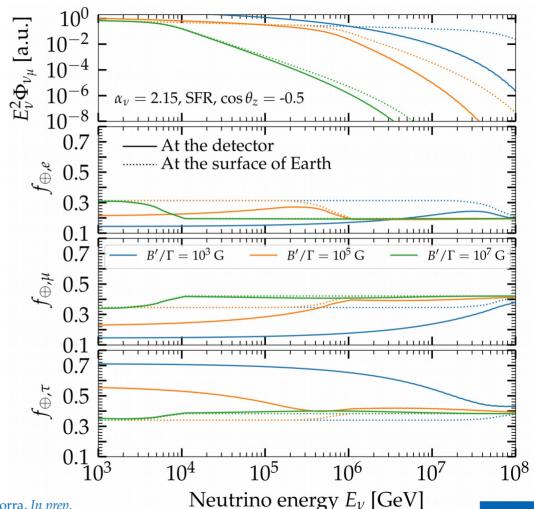
> PeV: Muon damping  $(f_e:f_{\mu}:f_{\tau})_{\oplus}$   $\approx$  (0.2:0.4:0.4)

More detailed studies are required

Borrowed from J. van Santen & M. Kowalski

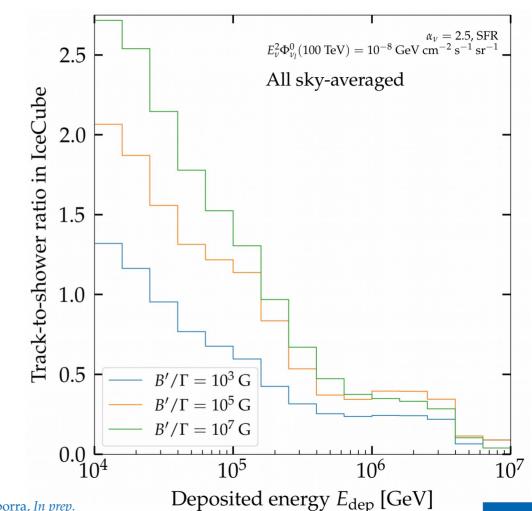
## Extracting source properties using flavor

- ► Goal: Use the flavor composition (and spectrum) of the diffuse  $\nu$  flux to extract the *average* magnetic strength B of the sources
- ► After synchrotron cooling sets in (at an energy  $\sim 1/B$ ):
  - ▶ The spectrum steepens by  $E^{-2}$
  - ▶ The flavor ratios change to  $(0:1:0)_S$
- ► We propagate the fluxes coming from each direction inside the Earth to the detector (with NuSQuIDS):
  - ightharpoonup Charged-current vN interactions deplete the flux
  - ▶ Neutral-current  $\nu N$  interactions pile-up low energy  $\nu$
  - $\triangleright v_{\tau}$  regeneration computed
- ▶ The arrival direction matters!

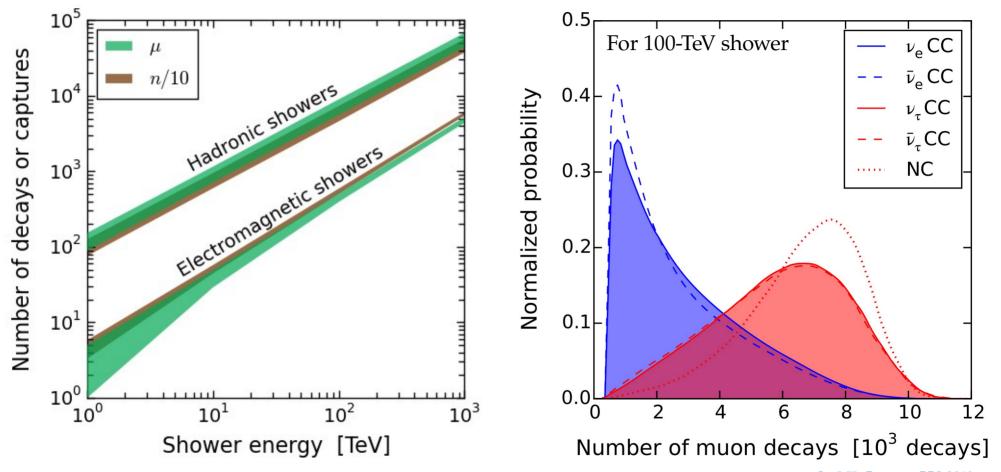


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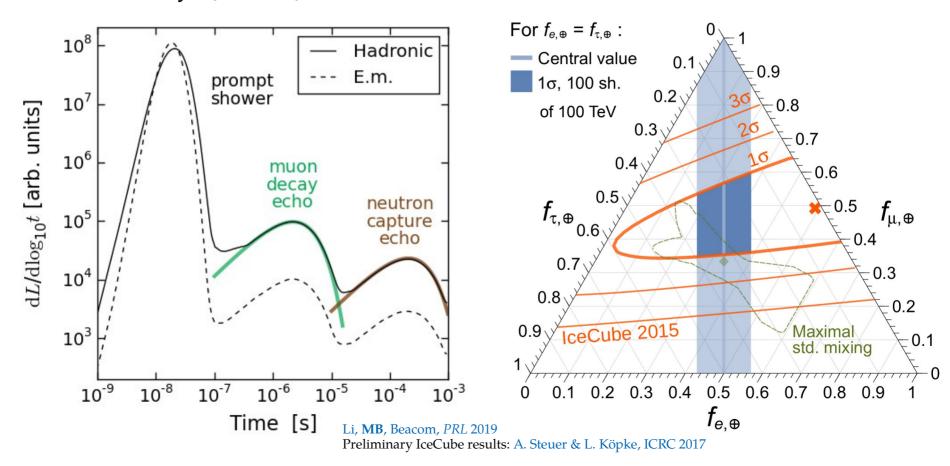
# The low-energy behavior of high-energy showers



Li, MB, Beacom, PRL 2019

#### Improving flavor-tagging using light echoes

Late-time light (*echoes*) from muon decays and neutron captures can separate showers made by  $v_e$  and  $v_\tau$  —

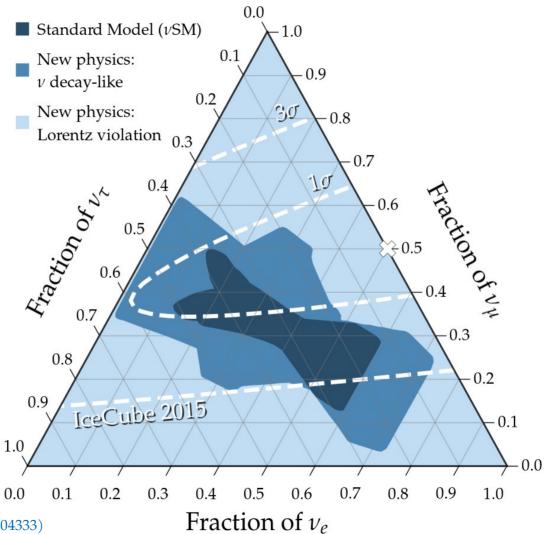


# Improving flavor-tagging using light echoes

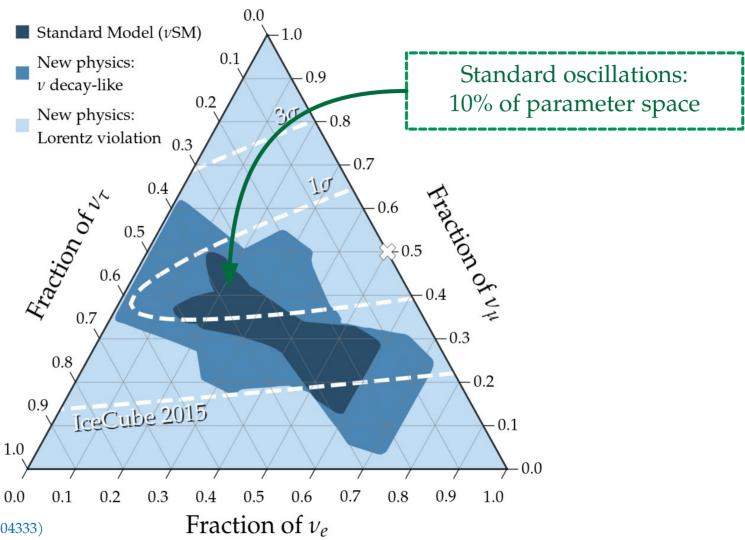
Time [s]

Late-time light (*echoes*) from muon decays and neutron captures can separate

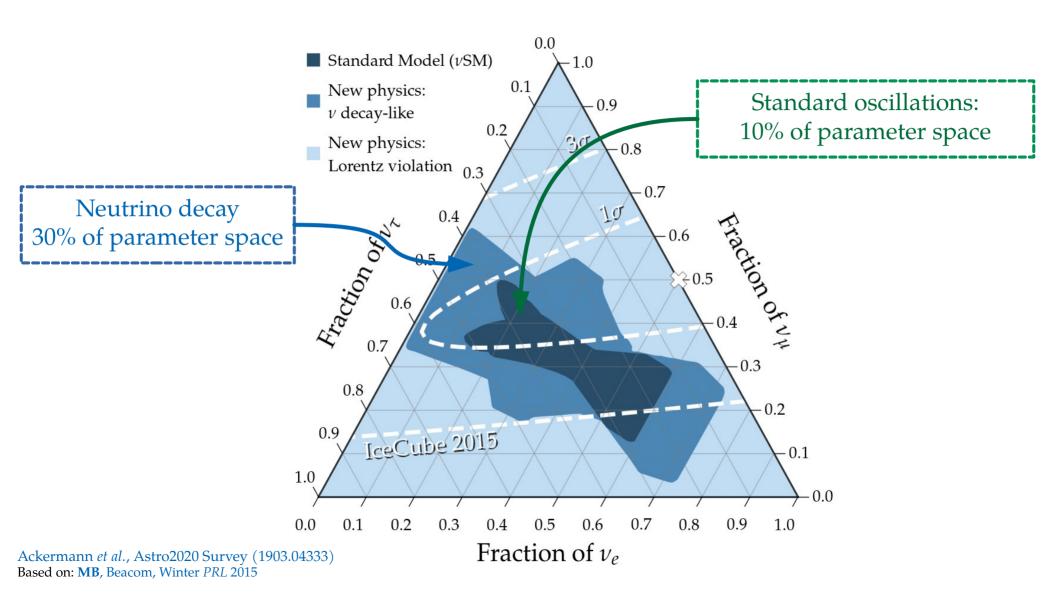
showers made by  $\nu_e$  and  $\nu_{\tau}$  — ~10× improvement over current measurement For  $f_{e,\oplus} = f_{\tau,\oplus}$ : 10<sup>8</sup> Hadronic Central value 0.1 0.9 E.m. prompt  $1\sigma$ , 100 sh. 0.2 shower 10<sup>7</sup> 8.0  $\mathrm{d}L/\mathrm{dlog}_{10}t$  [arb. units] of 100 TeV 0.7 10<sup>6</sup> 0.4 muon 0.6 decay 0.5 echo neutron  $f_{\tau,\oplus}$  $f_{\mu,\,\oplus}$ 10<sup>5</sup> capture echo 0.4 0.7 0.3 10<sup>4</sup> 0.8 0.2 IceCube 2015 0.9 Maximal 10<sup>3</sup> -0.1std. mixing 10-8 10<sup>-7</sup> 10<sup>-6</sup> 10<sup>-5</sup> 10<sup>-9</sup> 10<sup>-4</sup> 10<sup>-3</sup> 0.3 0.4 0.5 0.6 8.0  $f_{\mathrm{e},\oplus}$ 

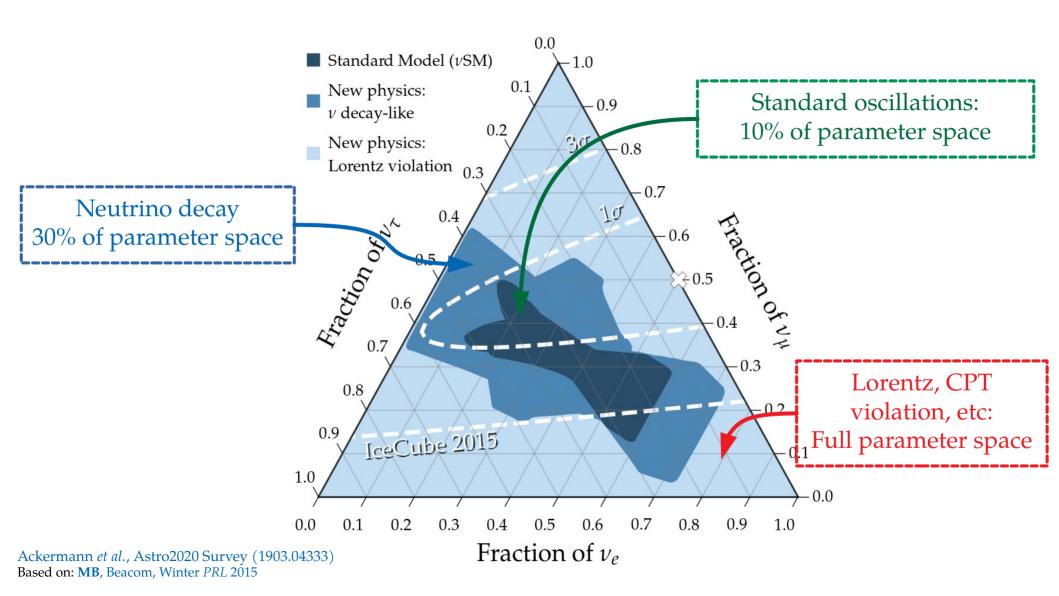


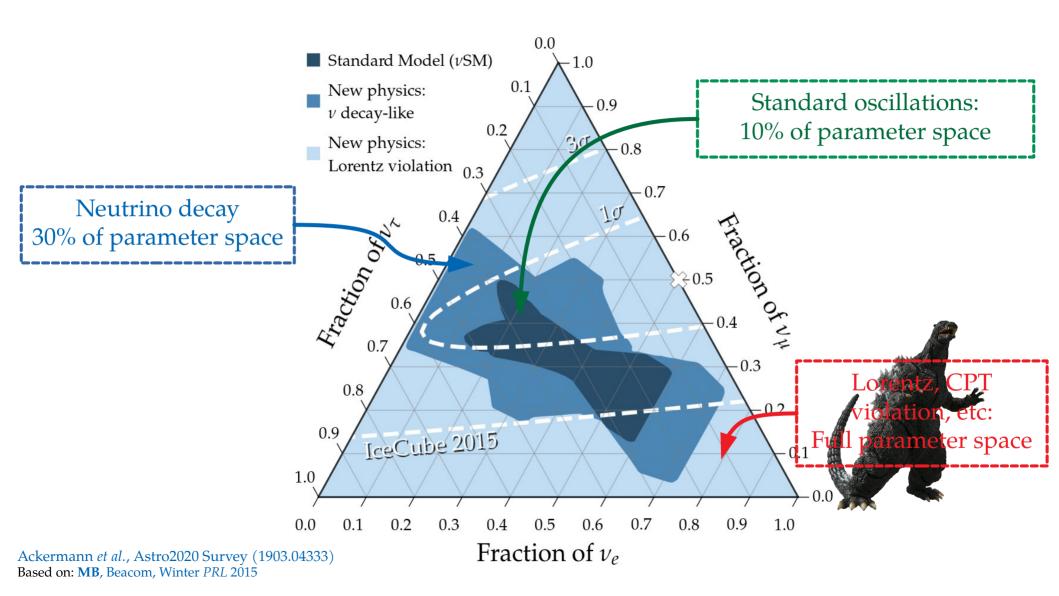
Ackermann *et al.*, Astro2020 Survey (1903.04333) Based on: MB, Beacom, Winter *PRL* 2015



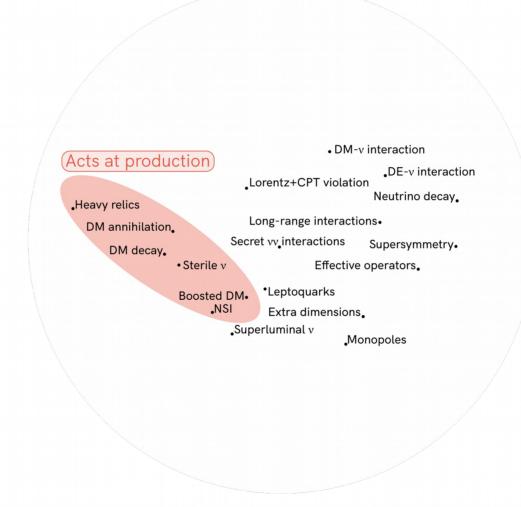
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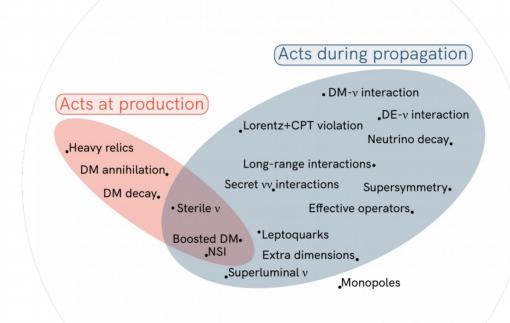


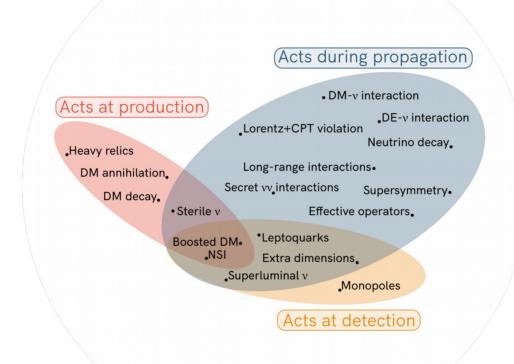


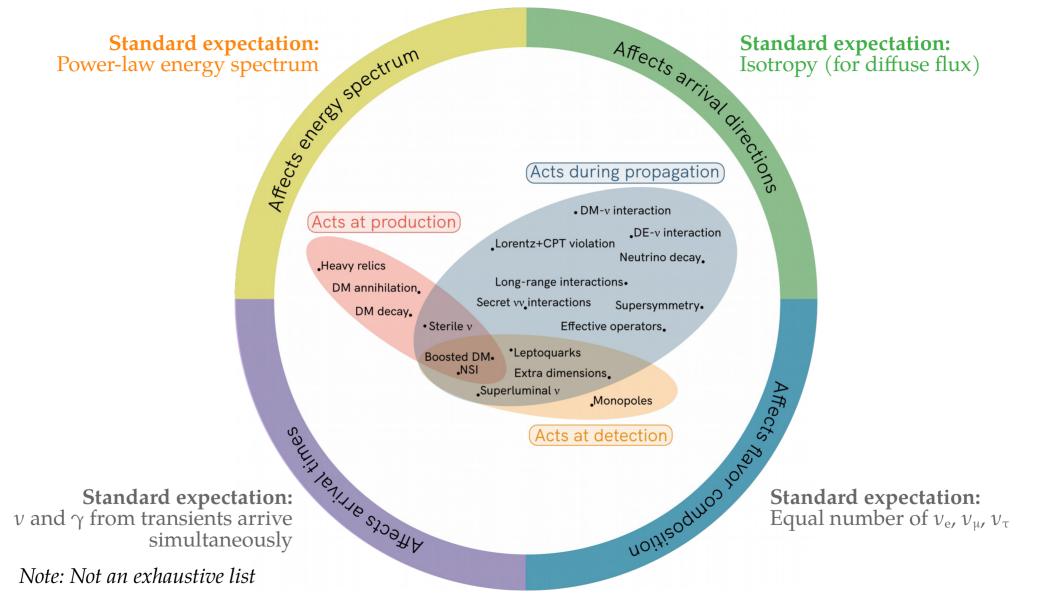


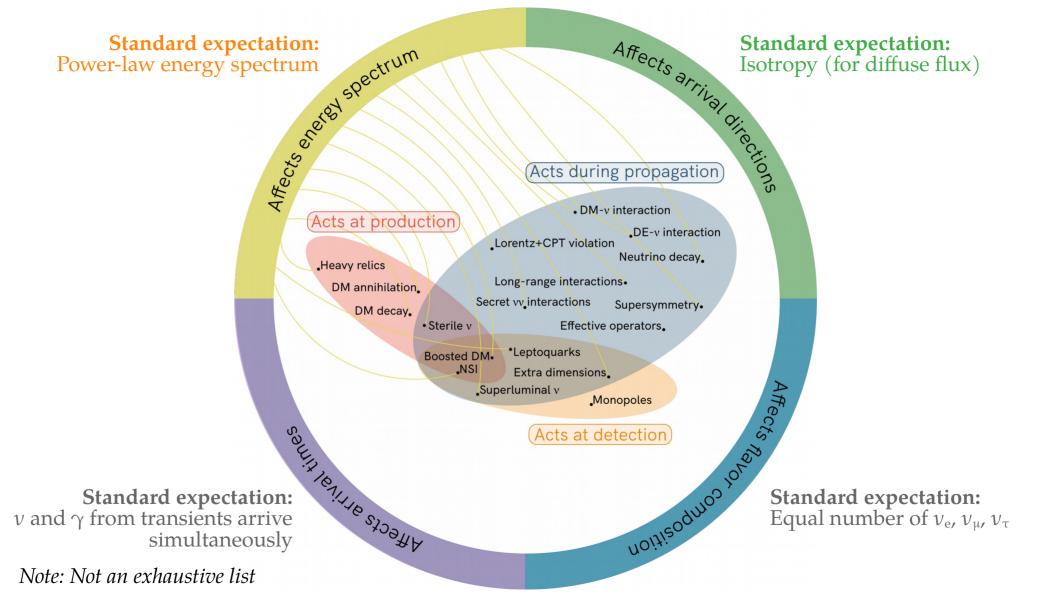


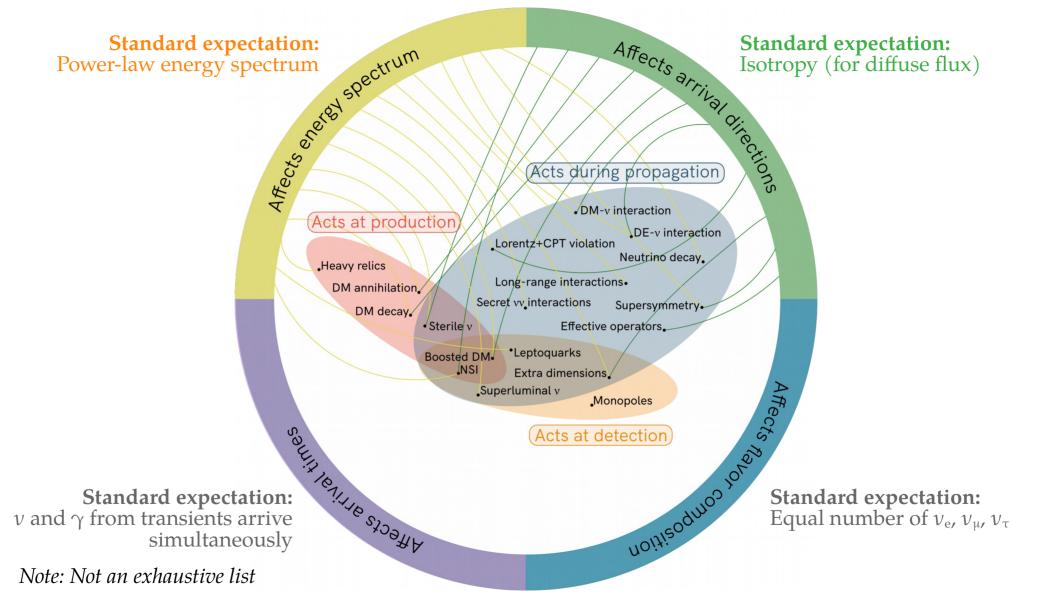


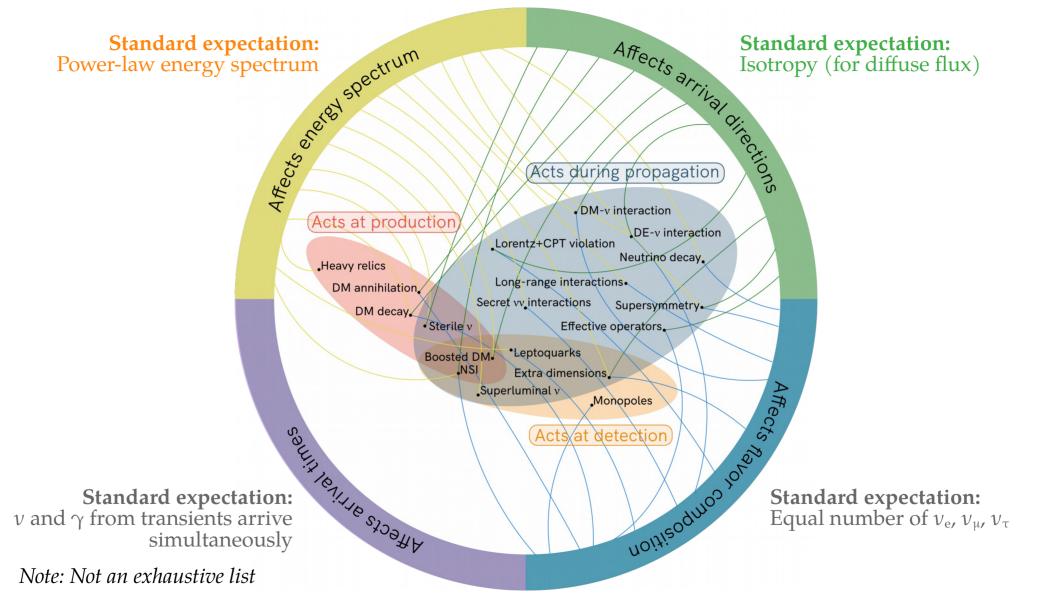


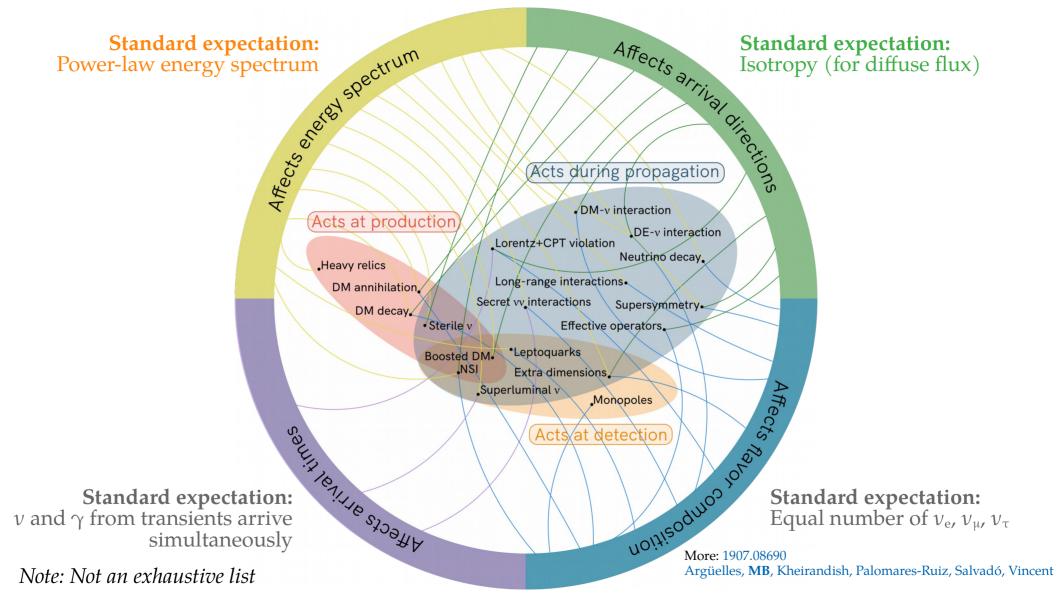


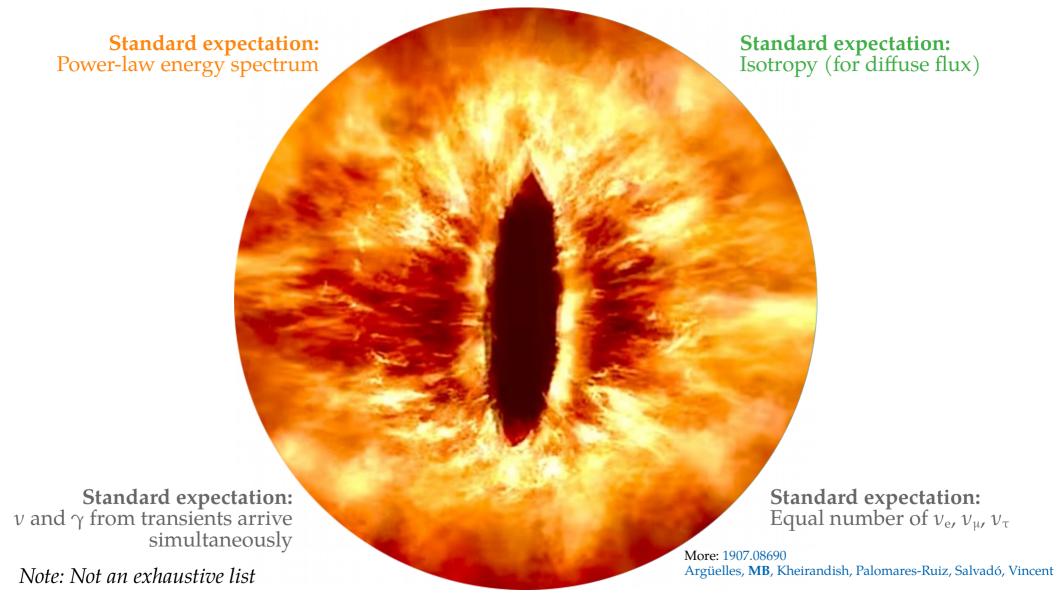


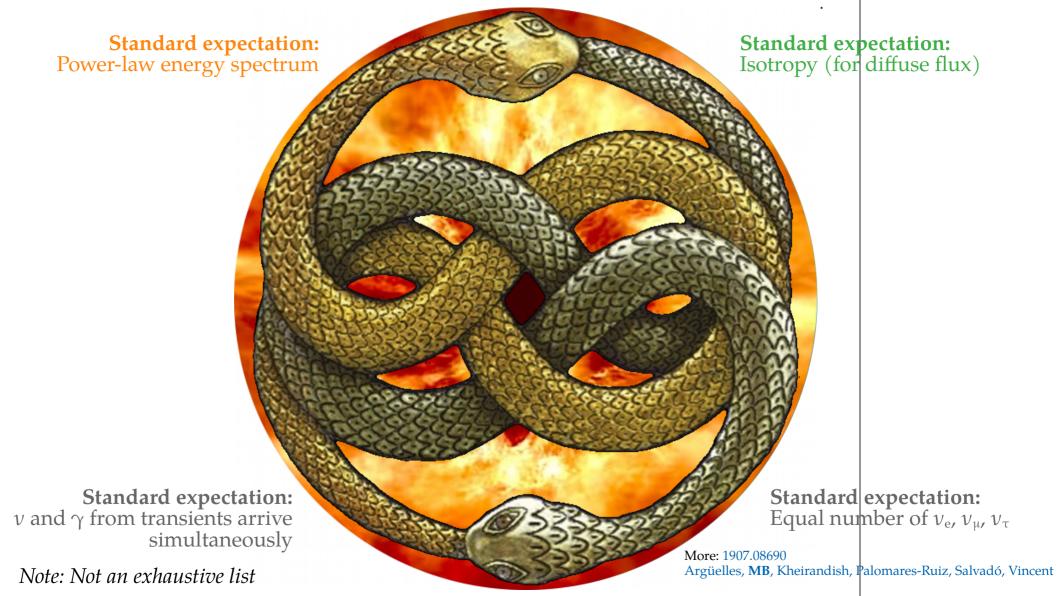






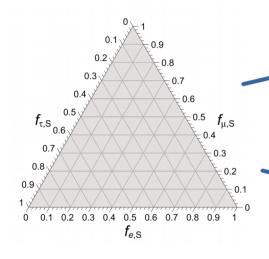


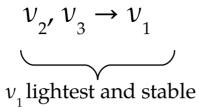




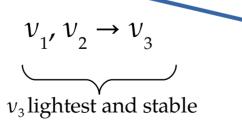
# Measuring the neutrino lifetime

#### Sources

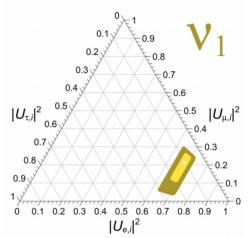




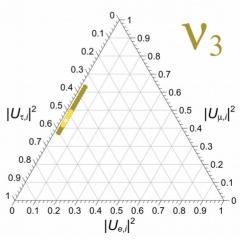
If all unstable neutrinos decay



#### Earth



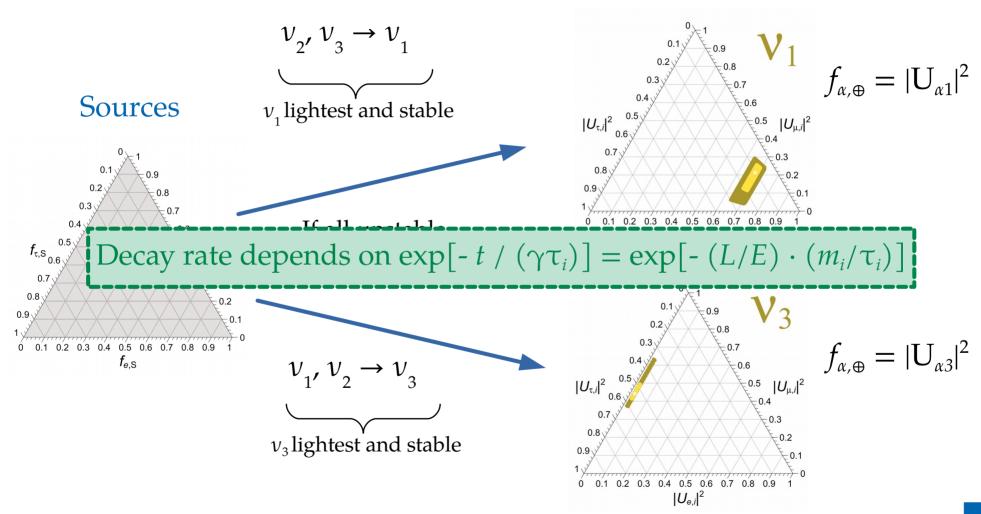
$$f_{\alpha,\oplus} = |\mathbf{U}_{\alpha 1}|^2$$

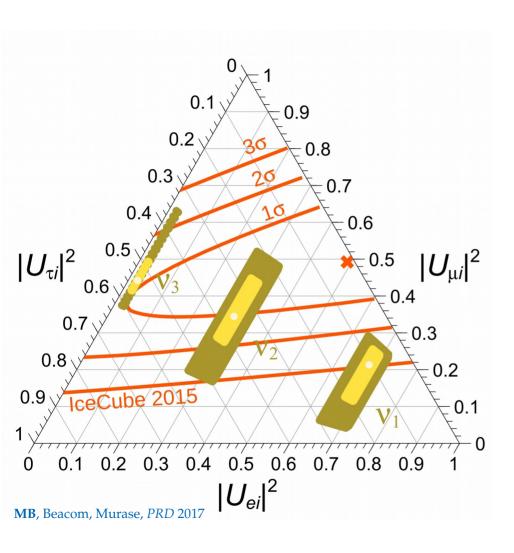


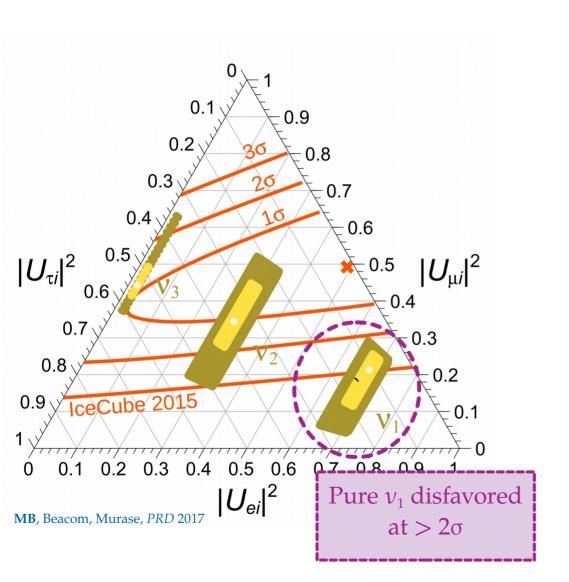
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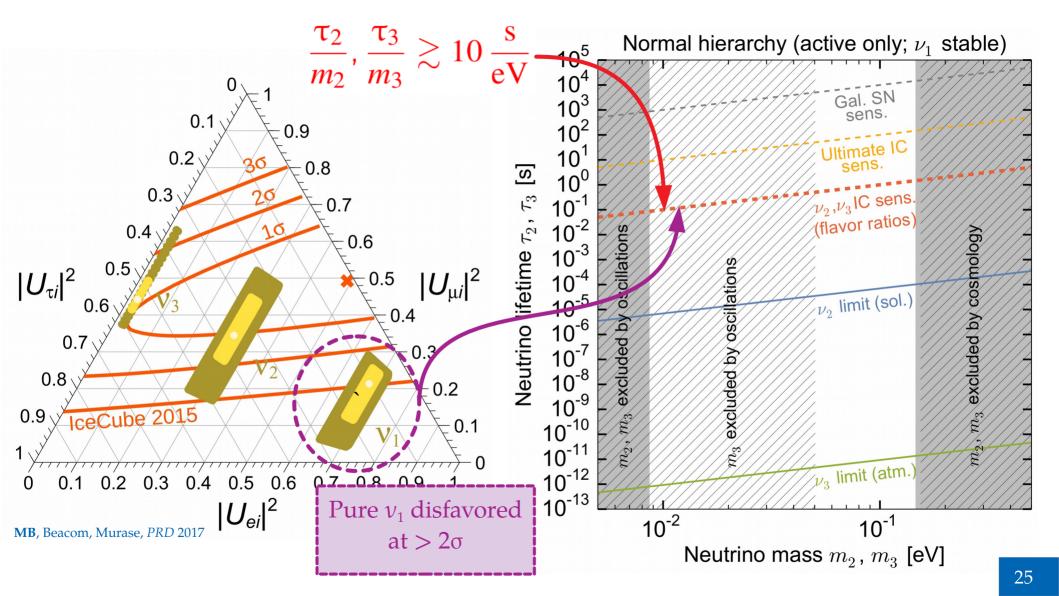
## Measuring the neutrino lifetime

#### Earth









#### What lies beyond? Pick your monster

- ► High-energy effective field theories
  - ► Violation of Lorentz and CPT invariance
    [Barenboim & Quigg, PRD 2003; Kostelecky & Mewes 2004; MB, Gago, Peña-Garay, JHEP 2010]
  - ► Violation of equivalence principle [Gasperini, PRD 1989; Glashow et al., PRD 1997]
  - ► Coupling to a gravitational torsion field [De Sabbata & Gasperini, Nuovo Cim. 1981]
  - ► Renormalization-group-running of mixing parameters [MB, Gago, Jones, JHEP 2011]
  - ► General non-unitary propagation [Ahlers, MB, Mu, PRD 2018]
- ► Active-sterile mixing
  [Aeikens et al., JCAP 2015; Brdar, JCAP 2017; Argüelles et al., 1909.05341]
- ► Flavor-violating physics
  - ► New neutrino-electron interactions [MB & Agarwalla, PRL 2019]
  - ► New vv interactions
    [Ng & Beacom, PRD 2014; Cherry, Friedland, Shoemaker, 1411.1071; Blum, Hook, Murase, 1408.3799]



Toho Company Ltd.

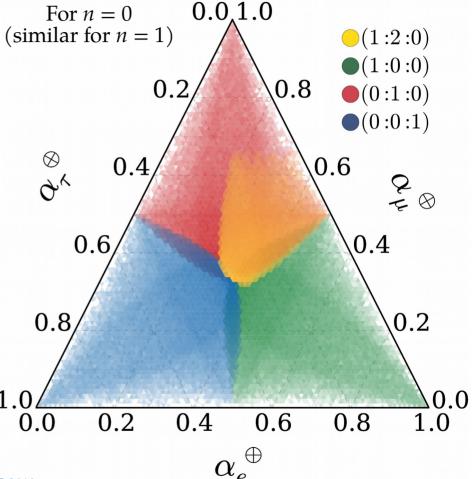
# New physics – High-energy effects

$$H_{
m tot} = H_{
m std} + H_{
m NP}$$
 $H_{
m std} = rac{1}{2E} U_{
m PMNS}^{\dagger} \, {
m diag} \left(0, \Delta m_{21}^2, \Delta m_{31}^2 
ight) \, U_{
m PMNS}$ 

$$H_{\mathsf{NP}} = \sum_{n} \left(\frac{E}{\Lambda_{n}}\right)^{n} U_{n}^{\dagger} \operatorname{diag}\left(O_{n,1}, O_{n,2}, O_{n,3}\right) U_{n}$$

This can populate *all* of the triangle –

- ► Use current atmospheric bounds on  $O_{n,i}$ :  $O_0 < 10^{-23}$  GeV,  $O_1/\Lambda_1 < 10^{-27}$  GeV
- ► Sample the unknown new mixing angles



See also: Rasmusen *et al.*, *PRD* 2017; **MB**, Beacom, Winter *PRL* 2015; **MB**, Gago, Peña-Garay *JCAP* 2010; Bazo, **MB**, Gago, Miranda *IJMPA* 2009; + many others

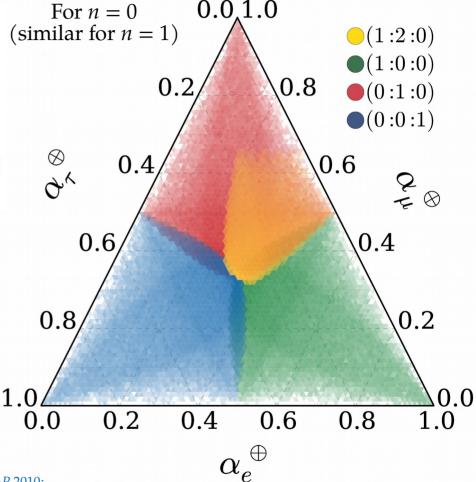
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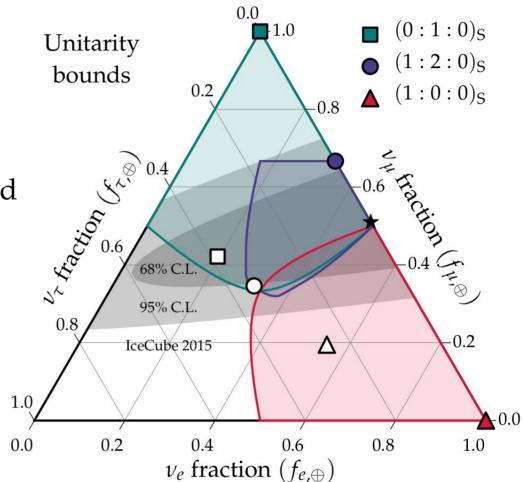


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# Using unitarity to constrain new physics

$$H_{tot} = H_{std} + H_{NP}$$

- New mixing angles unconstrained
- ► Use unitarity  $(U_{NP}U_{NP}^{\dagger} = 1)$  to bound all possible flavor ratios at Earth
- Can be used as prior in new-physics searches in IceCube



Ahlers, **MB**, Mu, *PRD* 2018 See also: Xu, He, Rodejohann, *JCAP* 2014

# Final thoughts

- ► Flavor has a vast potential to test astrophysics and particle physics
- ► We can tap into this potential *already today*
- ▶ Where should we go as a community?
  - ▶ Move beyond the simplest flavor-ratio fits (*i.e.*, include flavor ID,  $\overline{\nu}/\nu$ )
  - ▶ Include the uncertainties in mixing parameters in analyses they matter
  - ightharpoonup Experimental collaborations could provide the likelihood or posterior of  $f_{\alpha,\oplus}$
  - ▶ Muon and neutron echoes in IC-Gen2: characterize afterpulsing in PMTs before deployment
  - ▶ Put serious thought into flavor measurements in non-optical Cherenkov detectors
- ▶ Exciting prospects: larger statistics, better reconstruction, higher energies

# Backup slides

# Flavor-transition probability: the quick and dirty of it

▶ In matrix form: 
$$\begin{pmatrix} \nu_e \\ \nu_{\mu} \\ \nu_{\tau} \end{pmatrix} = \begin{pmatrix} U_{e1}^* & U_{e2}^* & U_{e3}^* \\ U_{\mu 1}^* & U_{\mu 2}^* & U_{\mu 3}^* \\ U_{\tau 1}^* & U_{\tau 2}^* & U_{\tau 3}^* \end{pmatrix} \begin{pmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{pmatrix}$$

▶ Pontecorvo-Maki-Nakagawa-Sakata matrix  $(c_{ij} = \cos \theta_{ij}, s_{ij} = \sin \theta_{ij})$ :

$$U = \begin{pmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{pmatrix} \begin{pmatrix} c_{13} & 0 & s_{13}e^{-i\delta} \\ 0 & 1 & 0 \\ -s_{13}e^{i\delta} & 0 & c_{13} \end{pmatrix} \begin{pmatrix} c_{12} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} e^{i\alpha_1/2} & 0 & 0 \\ 0 & e^{i\alpha_2/2} & 0 \\ 0 & 0 & 1 \end{pmatrix}$$
Atmospheric Cross mixing Solar Majorana CP phases

► Probability for 
$$\nu_{\alpha} \rightarrow \nu_{\beta}$$
:  $P_{\nu_{\alpha} \rightarrow \nu_{\beta}} = \delta_{\alpha\beta} - 4 \sum_{i>j} \operatorname{Re}(U_{\alpha i}^* U_{\beta i} U_{\alpha j} U_{\beta j}^*) \sin^2\left(\Delta m_{ij}^2 \frac{L}{4E}\right) + 2 \sum_{i>j} \operatorname{Im}(U_{\alpha i}^* U_{\beta i} U_{\alpha j} U_{\beta j}^*) \sin\left(\Delta m_{ij}^2 \frac{L}{2E}\right)$ 

# Flavor-transition probability: the quick and dirty of it

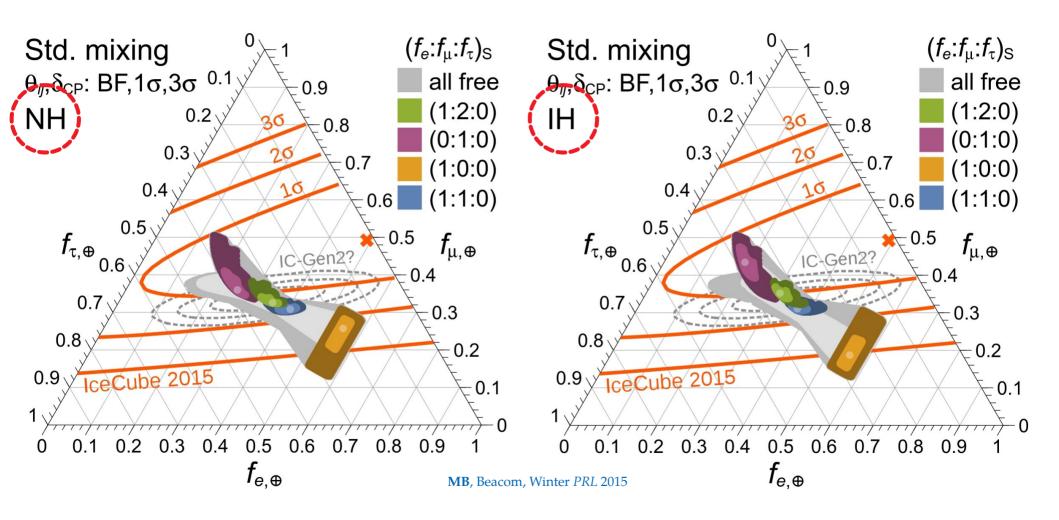
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Flavor composition – a few source choices

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# Fundamental physics with HE cosmic neutrinos

- ▶ Numerous new-physics effects grow as  $\sim \kappa_n \cdot E^n \cdot L$
- ► So we can probe  $\kappa_n \sim 4 \cdot 10^{-47} \, (E/\text{PeV})^{-n} \, (L/\text{Gpc})^{-1} \, \text{PeV}^{1-n}$
- ▶ Improvement over current limits:  $\kappa_0 < 10^{-29}$  PeV,  $\kappa_1 < 10^{-33}$
- ► Fundamental physics can be extracted from four neutrino observables:
  - ► Spectral shape
  - ► Angular distribution
  - ► Flavor composition
  - ► Timing

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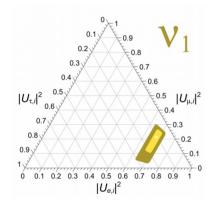
  - ▶ Timing

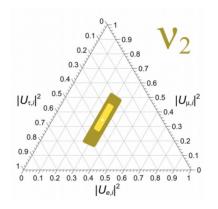
```
    Angular distribution
    Flavor composition
    In spite of poor energy, angular, flavor reconstruction & astrophysical unknowns

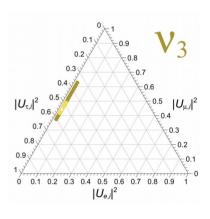
                                                In spite of
```

## Two classes of new physics

- ▶ Neutrinos propagate as an incoherent mix of  $\nu_1$ ,  $\nu_2$ ,  $\nu_3$
- ► Each one has a different flavor content:



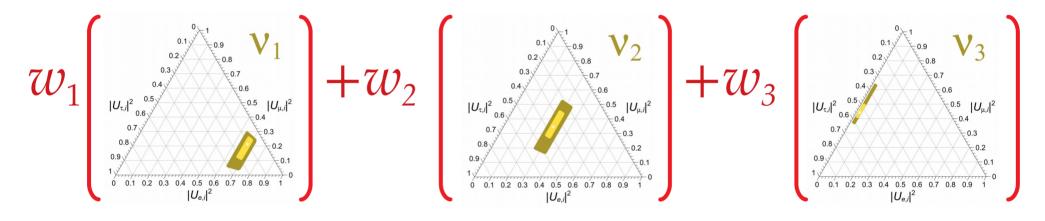




- ► Flavor ratios at Earth are the result of their combination
- ▶ New physics may:
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  - ightharpoonup Redefine the propagation states (*e.g.*, Lorentz-invariance violation)

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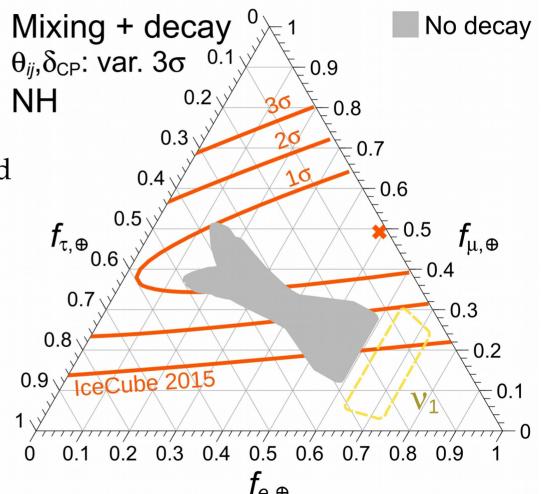


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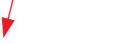
Find the value of D so that decay is complete, *i.e.*,  $f_{\alpha,\oplus} = |U_{\alpha 1}|^2$ , for

- Any value of mixing parameters; and
- ► Any flavor ratios at the sources

(Assume equal lifetimes of  $v_2$ ,  $v_3$ )



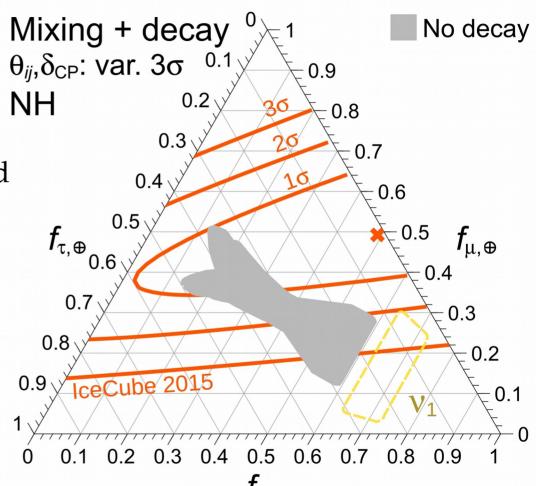
Fraction of  $v_2$ ,  $v_3$  remaining at Earth



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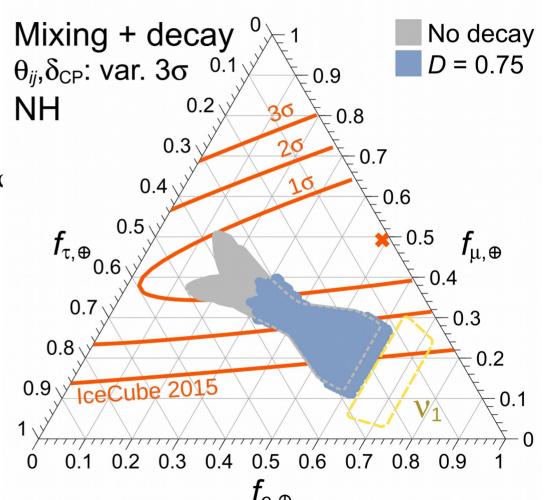
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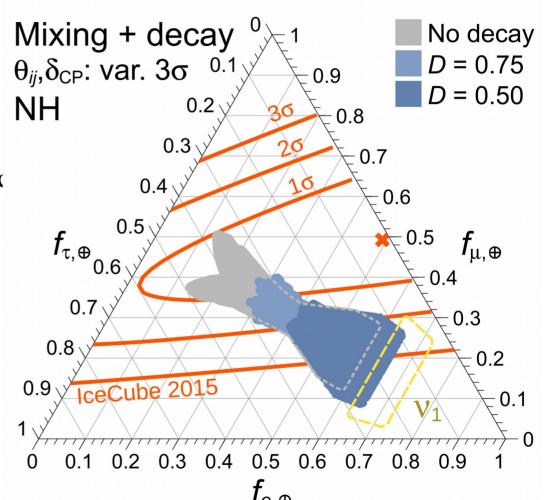
Fraction of  $v_2$ ,  $v_3$  remaining at Earth



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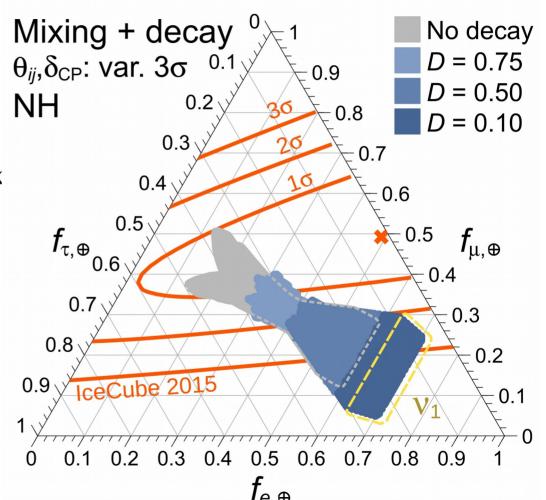
Fraction of  $v_2$ ,  $v_3$  remaining at Earth



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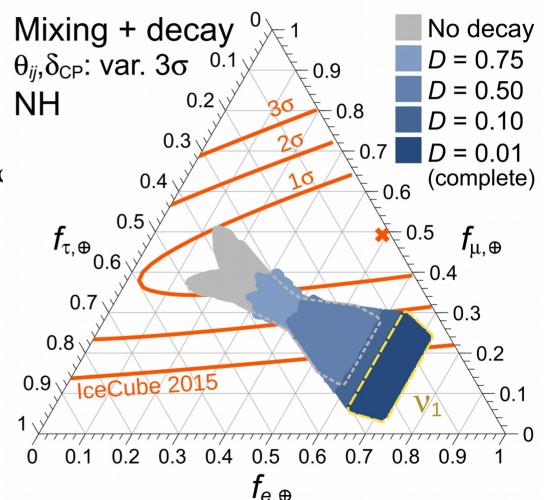
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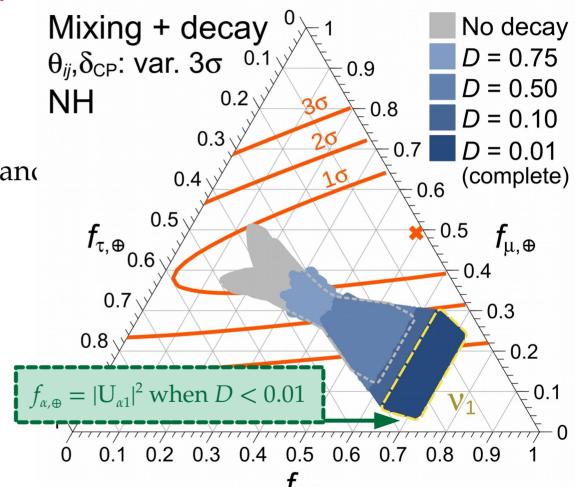
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## Ultra-long-range flavorful interactions

- Simple extension of the SM: Promote the global lepton-number symmetries  $L_e$ - $L_\mu$ ,  $L_e$ - $L_\tau$  to local symmetries
- ► They introduce new interaction between electrons and  $\nu_e$  and  $\nu_\mu$  or  $\nu_\tau$  mediated by a new neutral vector boson (Z'):
  - ► Affects oscillations
  - ▶ If the *Z'* is *very* light, *many* electrons can contribute

## The new potential sourced by an electron

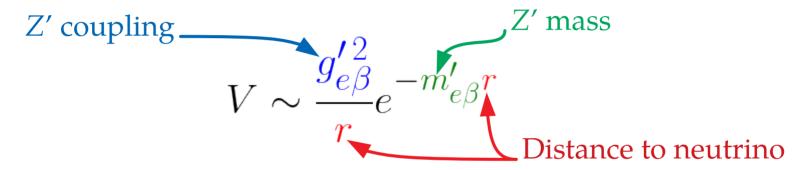
Under the  $L_e$ - $L_\mu$  or  $L_e$ - $L_\tau$  symmetry, an electron sources a Yukawa potential —

$$V \sim \frac{g_{e\beta}^{\prime 2}}{r} e^{-m_{e\beta}^{\prime}r}$$

A neutrino "feels" all the electrons within the interaction range  $\sim (1/m')$ 

## The new potential sourced by an electron

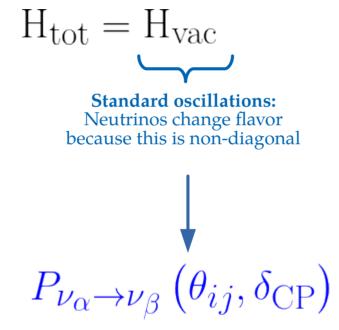
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$$H_{tot} = H_{vac}$$

$$\underline{\text{Standard oscillations:}}$$
Neutrinos change flavor because this is non-diagonal}



$$H_{\text{tot}} = H_{\text{vac}} + \underbrace{V_{e\beta}}_{\text{e}\beta}$$

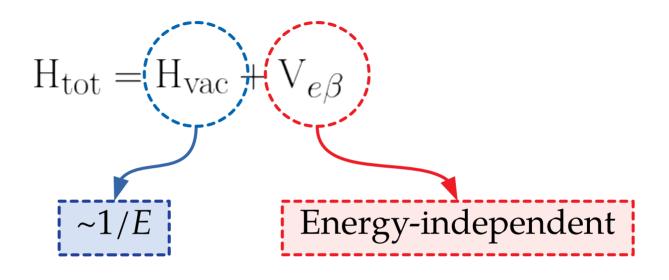
New neutrino-electron interaction: This is diagonal

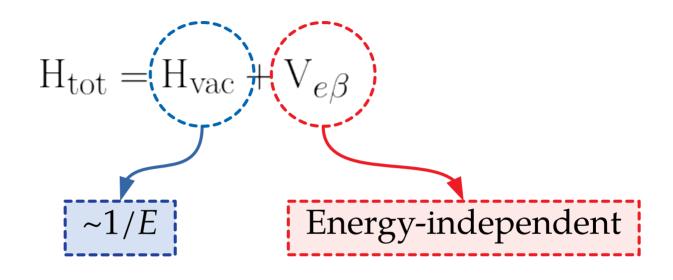
$$H_{\text{tot}} = H_{\text{vac}} + \underbrace{\bigvee_{e\beta}}_{\text{New neutrino-electron interaction:}}_{\text{This is diagonal}} \\ P_{\nu_{\alpha} \rightarrow \nu_{\beta}} \left(\theta_{ij}, \delta_{\text{CP}}, \Delta m_{ij}^2, E_{\nu}, g_{e\mu}', m_{e\mu}'\right)$$

$$H_{\text{tot}} = H_{\text{vac}} + \underbrace{\bigvee_{e\beta}}_{\text{New neutrino-electron interaction:}}_{\text{This is diagonal}} \\ P_{\nu_{\alpha} \rightarrow \nu_{\beta}} \left(\theta_{ij}, \delta_{\text{CP}}, \Delta m_{ij}^2, E_{\nu}, g_{e\mu}', m_{e\mu}'\right)$$

If  $V_{e\beta}$  dominates  $(g' \gg 1, m' \ll 1)$ , oscillations turn off

$$H_{\text{tot}} = H_{\text{vac}} + V_{e\beta}$$



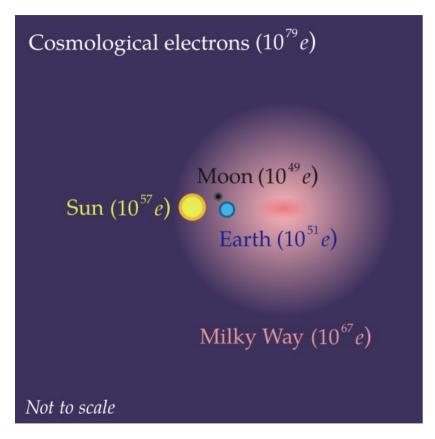


... We can use high-energy astrophysical neutrinos

# The total potential

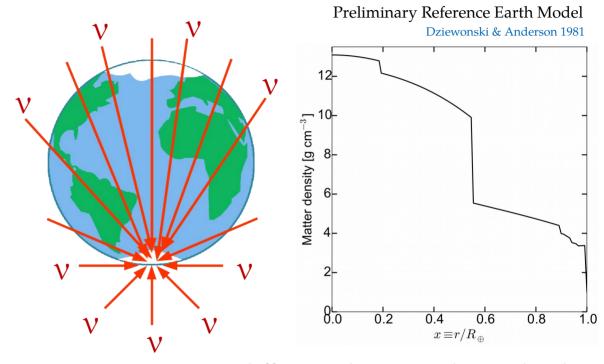
```
Cosmological electrons (10^{79}e)
                      Moon (10^{49}e)
     Sun (10<sup>57</sup>e) 0
                        Earth (10<sup>51</sup>e)
                      Milky Way (10^{67}e)
Not to scale
```

## The total potential



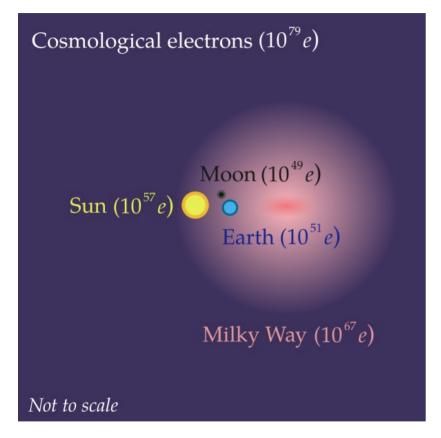
$$V_{e\beta} = V_{e\beta}^{\oplus}$$

#### Earth:

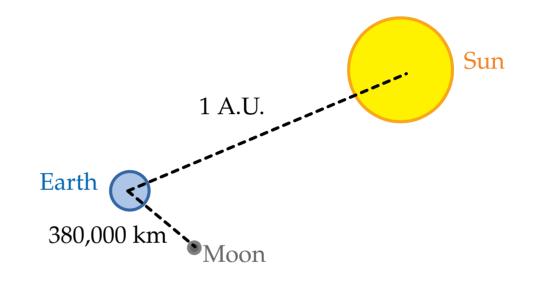


Neutrinos traverse different electron column depths

## The total potential

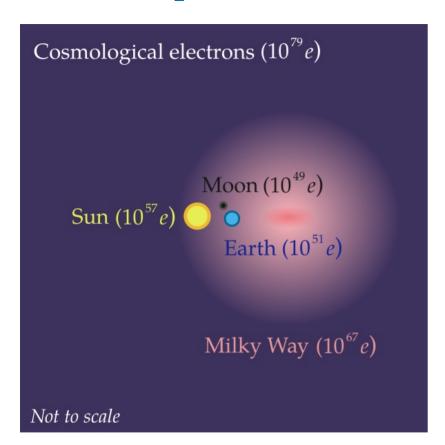


#### Moon and Sun:

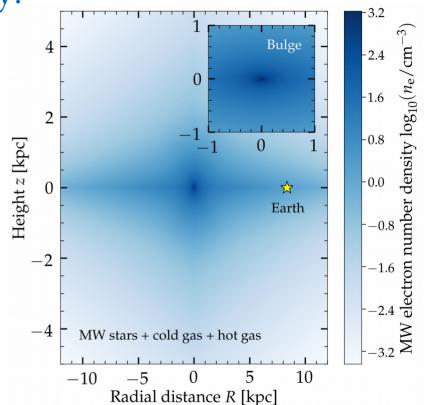


Treated as point sources of electrons

$$V_{e\beta} = V_{e\beta}^{\oplus} + V_{e\beta}^{\text{Moon}} + V_{e\beta}^{\odot}$$

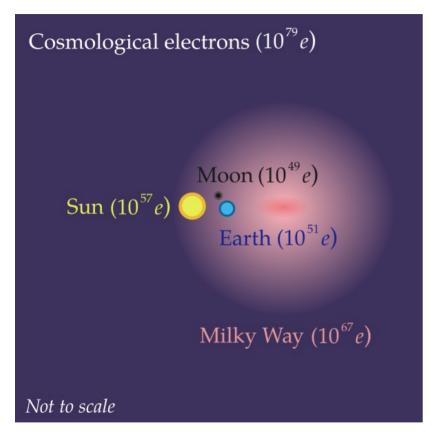


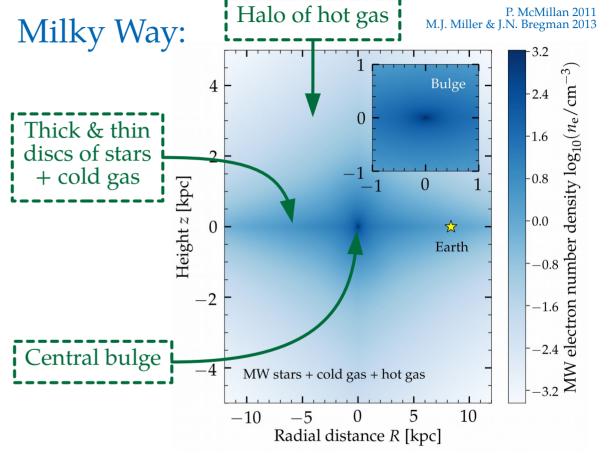
Milky Way:



$$V_{e\beta} = V_{e\beta}^{\oplus} + V_{e\beta}^{\text{Moon}} + V_{e\beta}^{\odot} + V_{e\beta}^{\text{MW}}$$

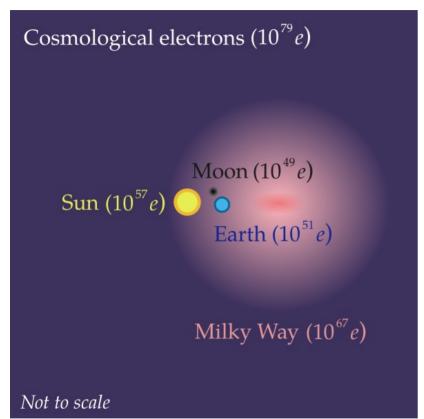
## The total potential

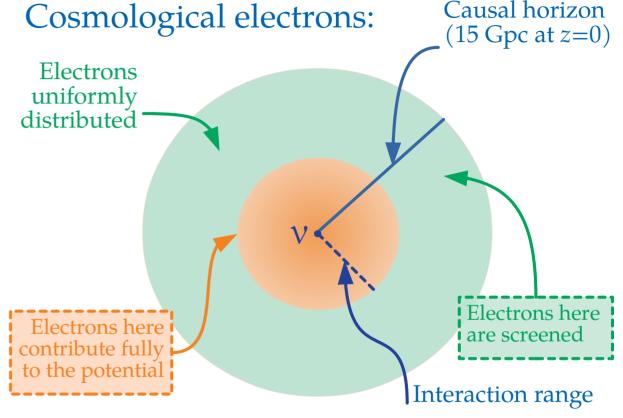




$$V_{e\beta} = V_{e\beta}^{\oplus} + V_{e\beta}^{\text{Moon}} + V_{e\beta}^{\odot} + V_{e\beta}^{\text{MW}}$$

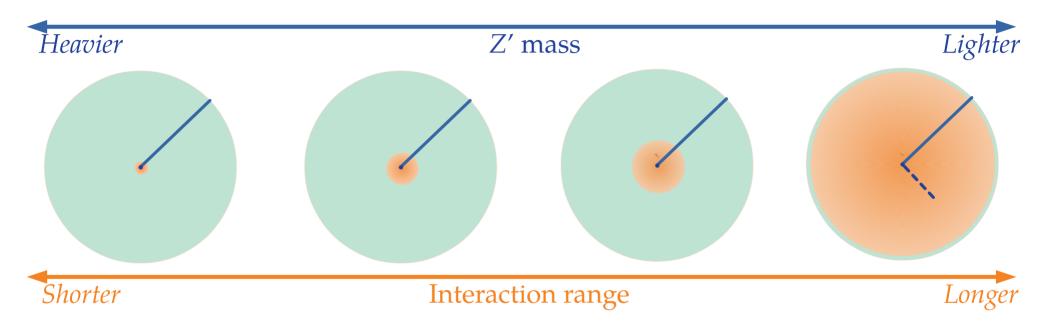
## The total potential





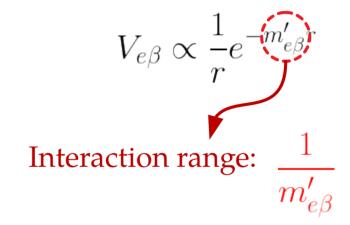
$$V_{e\beta} = V_{e\beta}^{\oplus} + V_{e\beta}^{\text{Moon}} + V_{e\beta}^{\odot} + V_{e\beta}^{\text{MW}} + V_{e\beta}^{\cos}$$

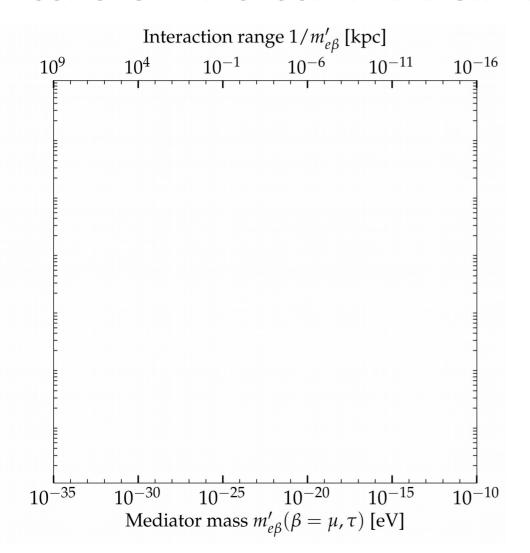
## The total potential

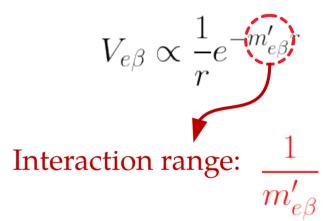


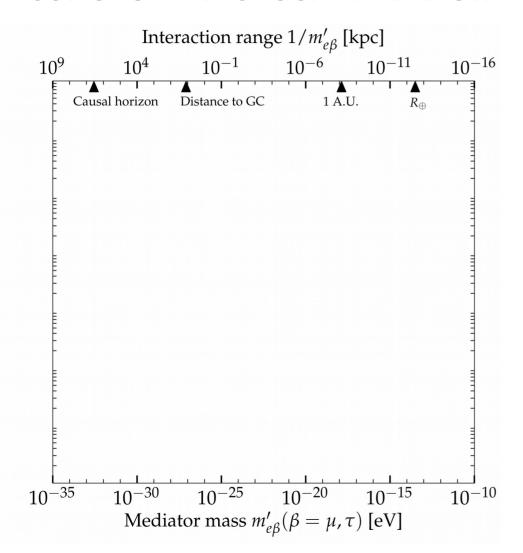
$$V_{e\beta} = V_{e\beta}^{\oplus} + V_{e\beta}^{\text{Moon}} + V_{e\beta}^{\odot} + V_{e\beta}^{\text{MW}} + V_{e\beta}^{\cos}$$

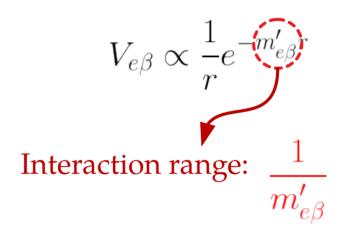
$$V_{e\beta} \propto \frac{1}{r} e^{-m'_{e\beta}r}$$

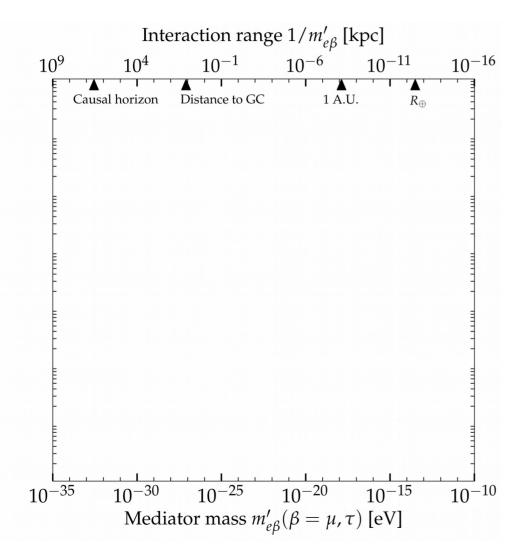




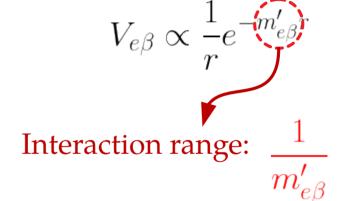




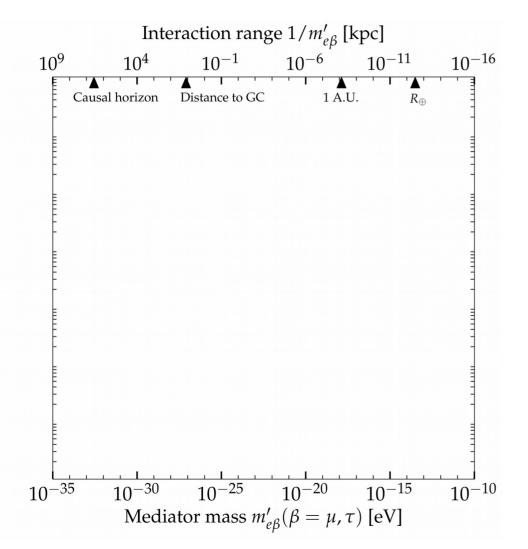


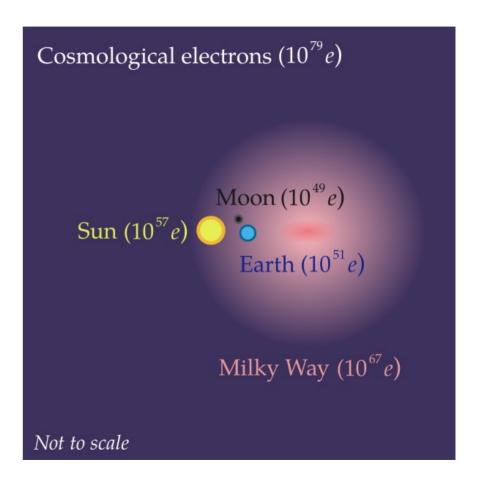


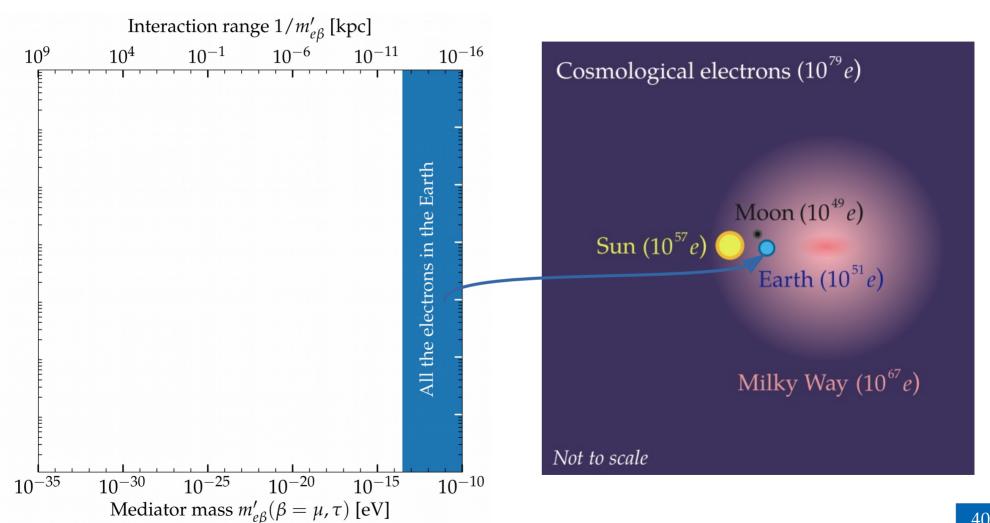
Potential:

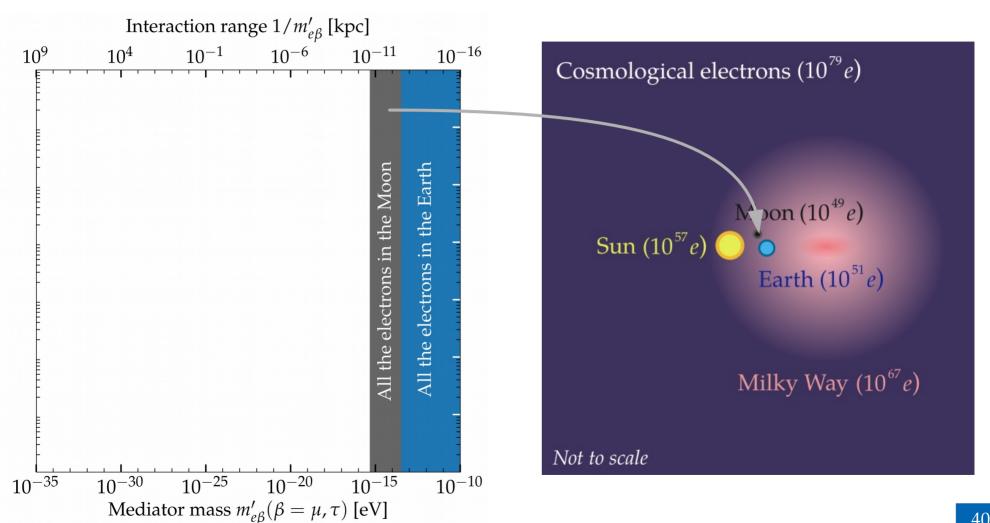


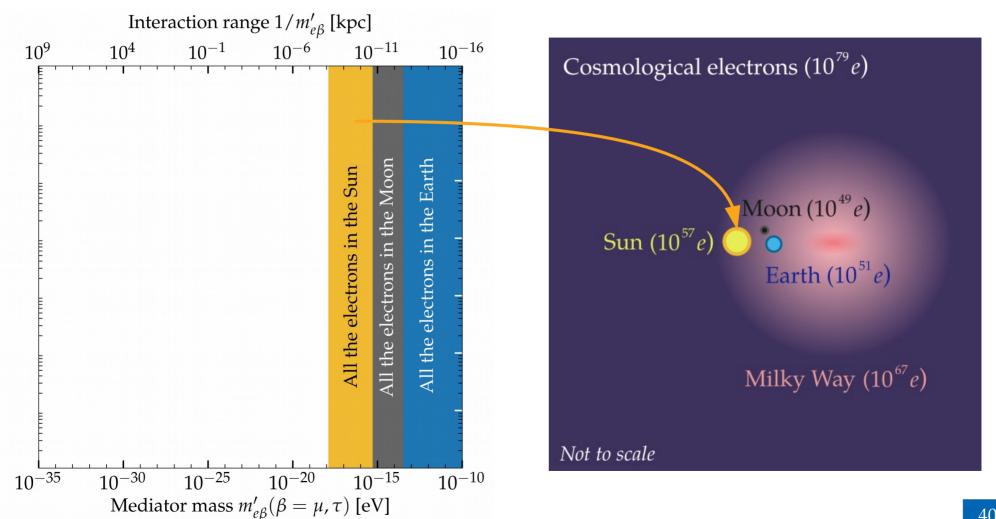
Light mediators ⇒ Long interaction ranges

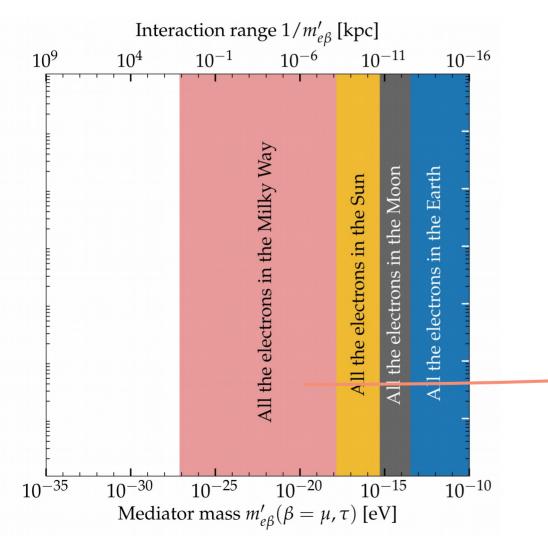


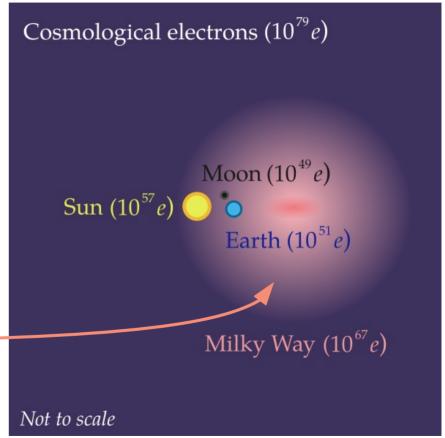


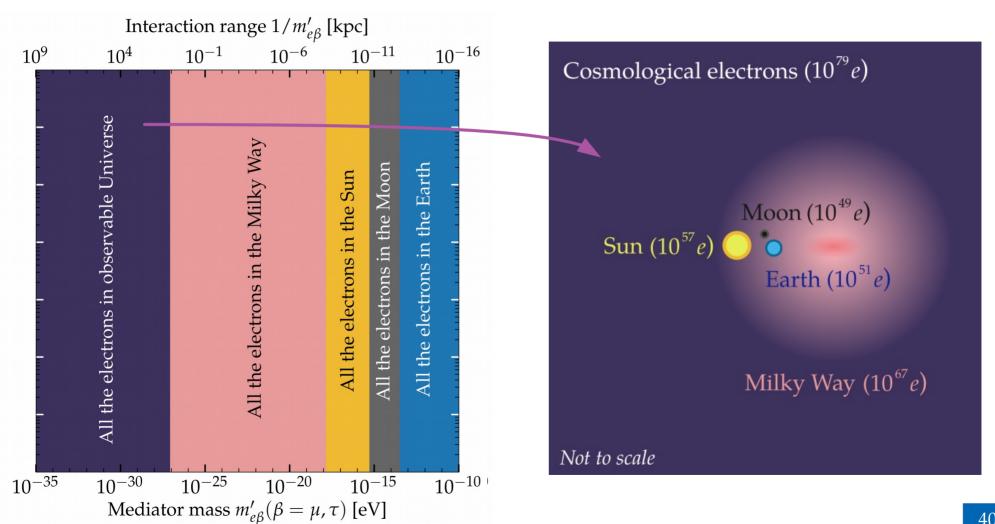


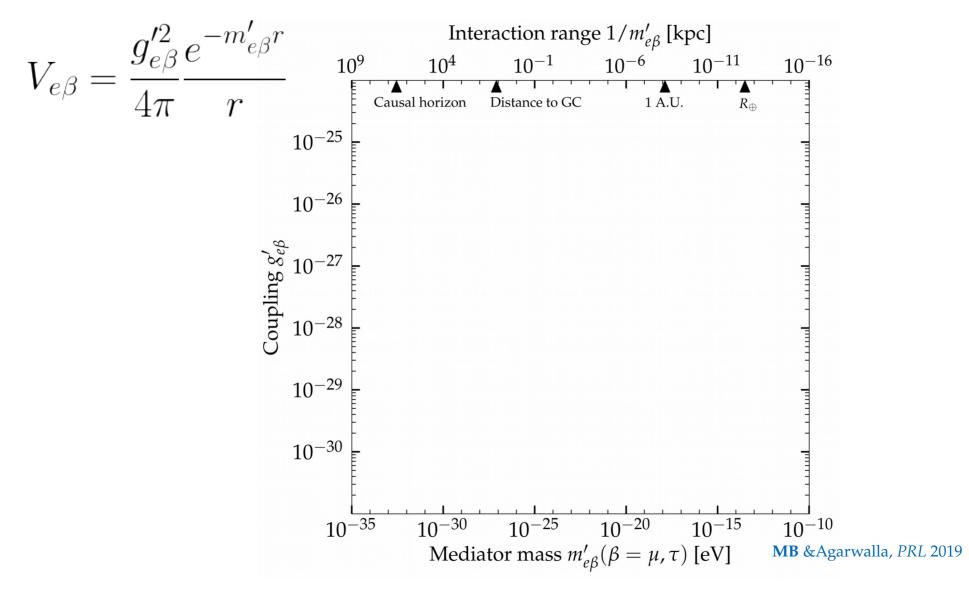


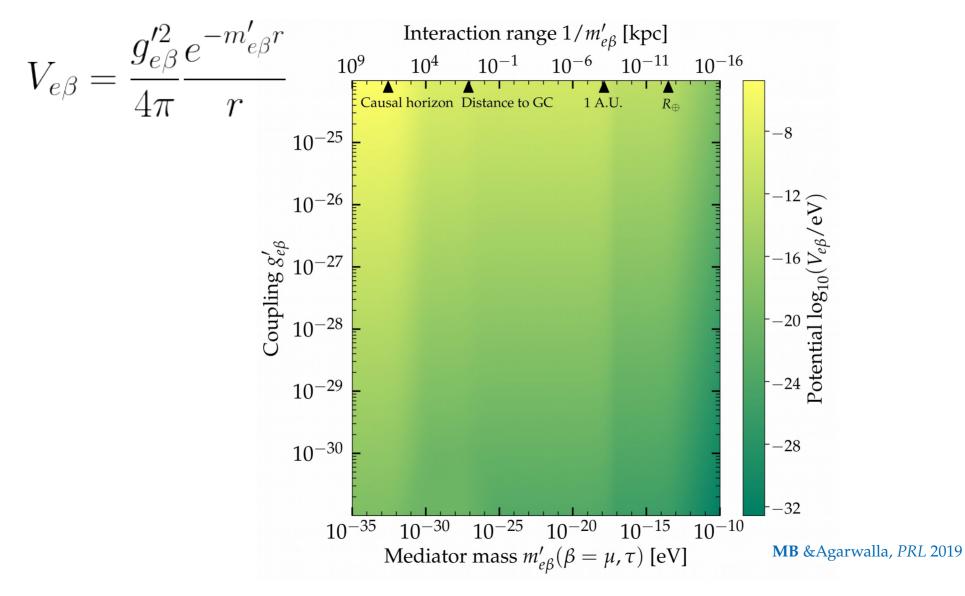


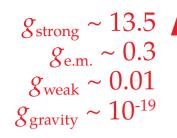


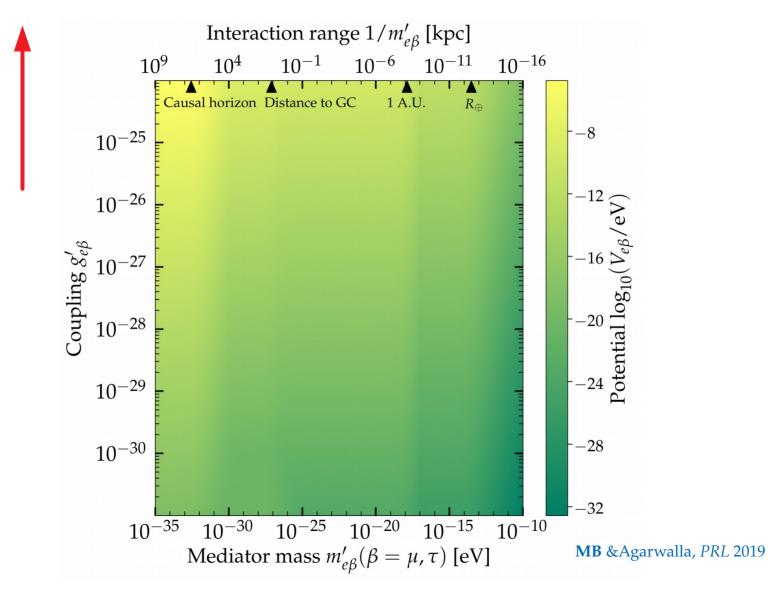


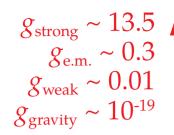


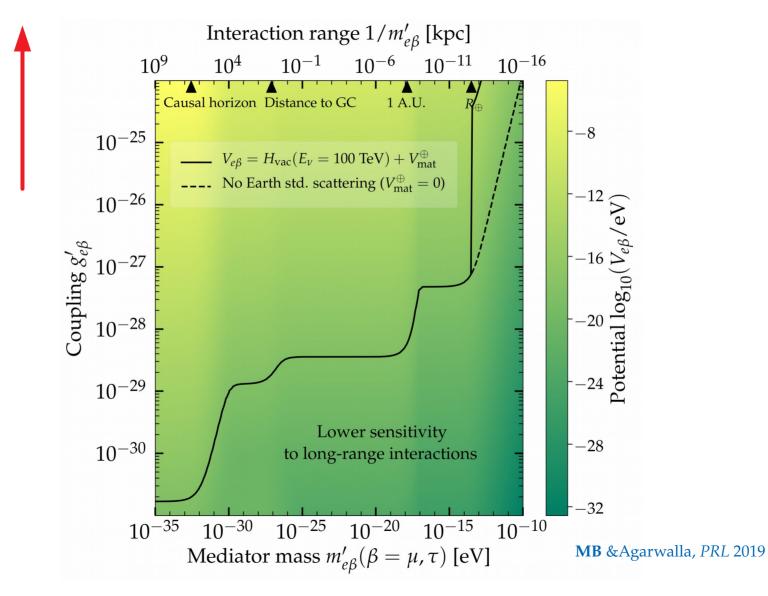


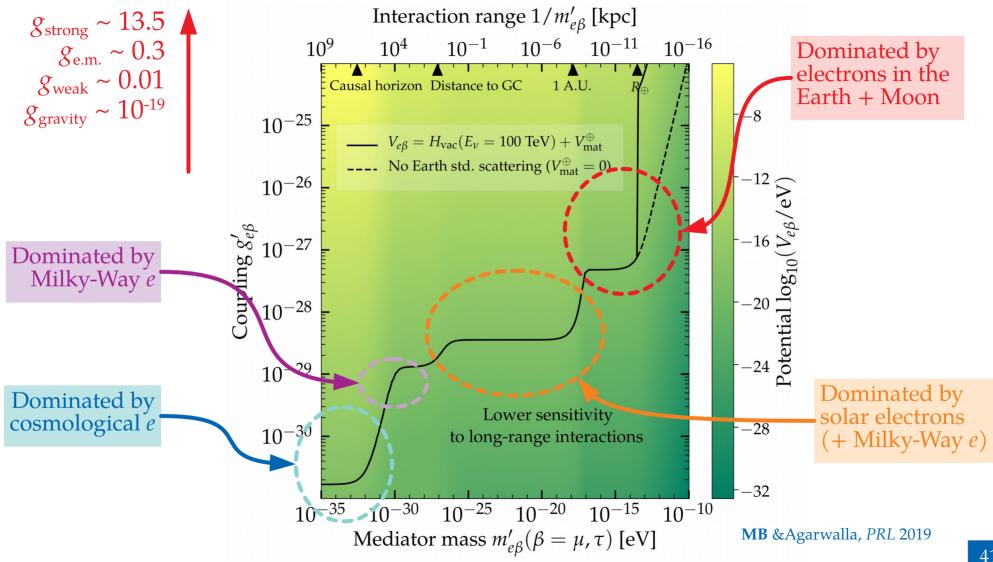


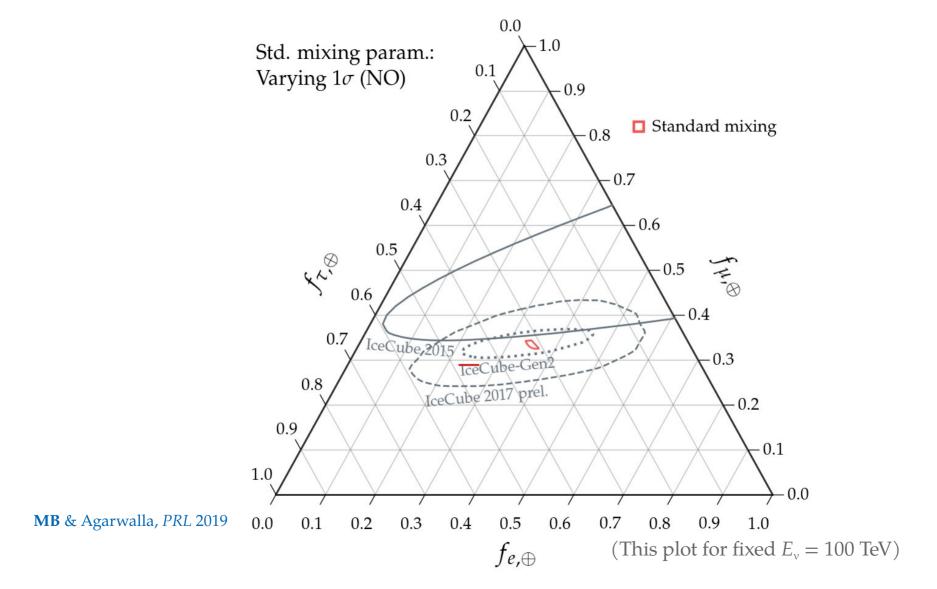


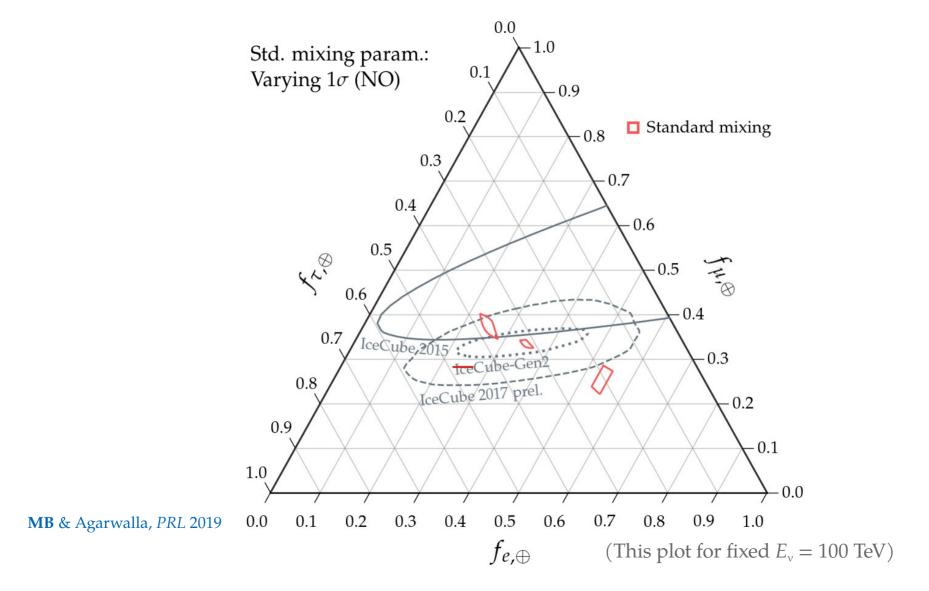


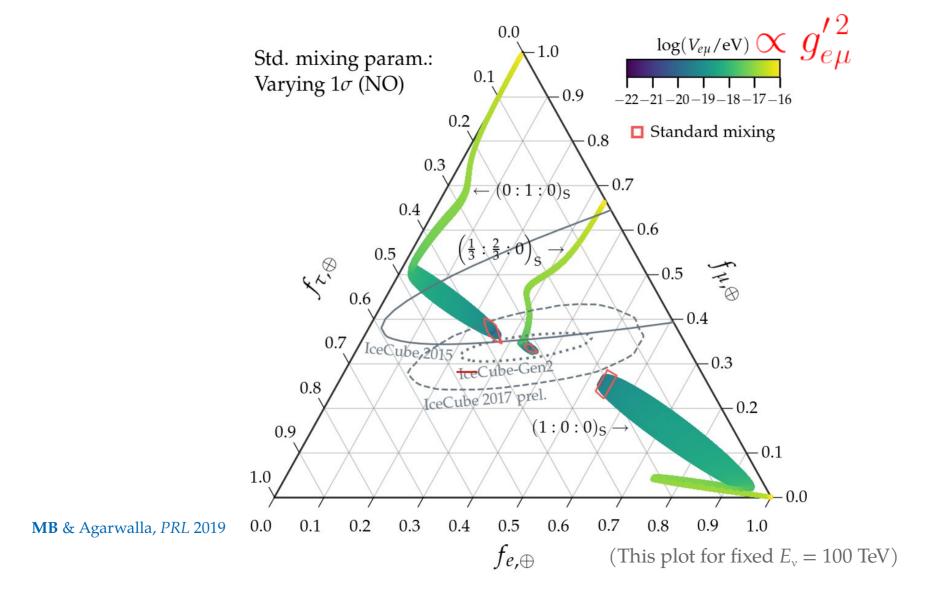


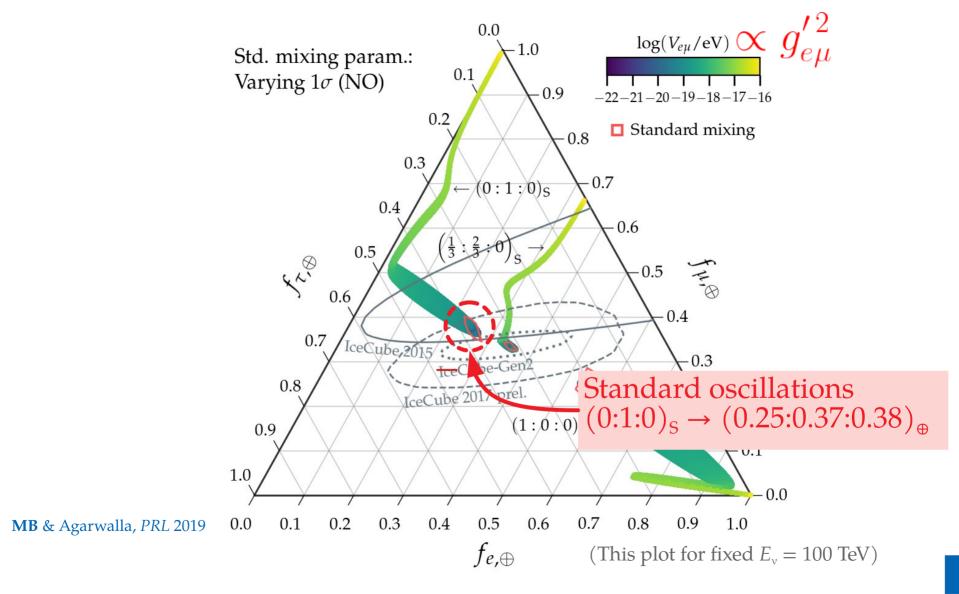


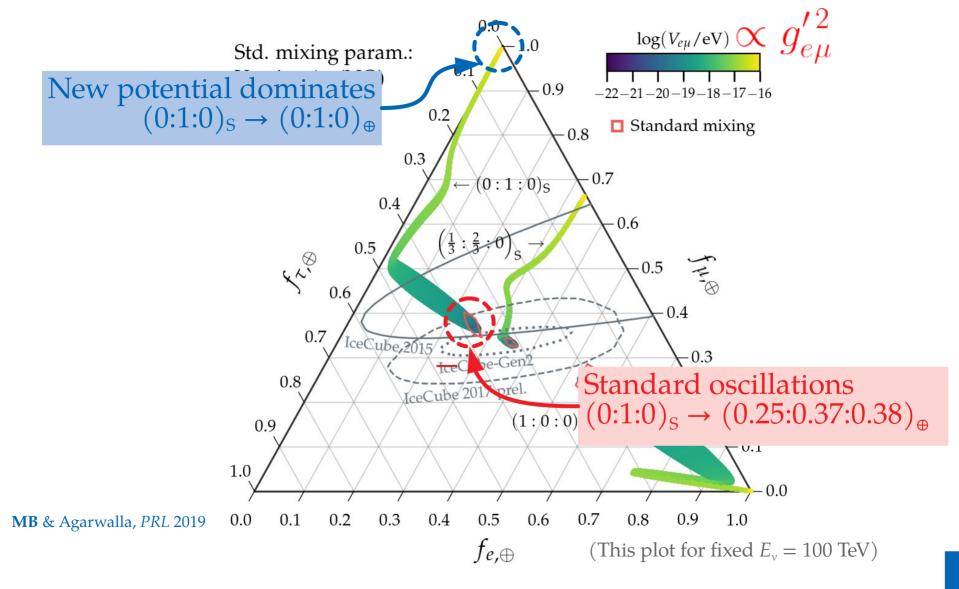


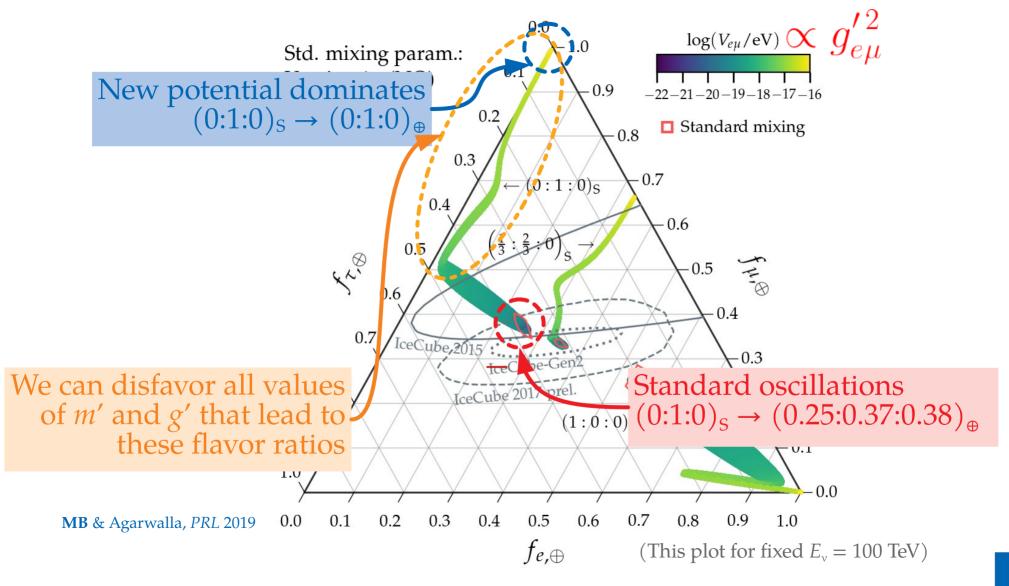


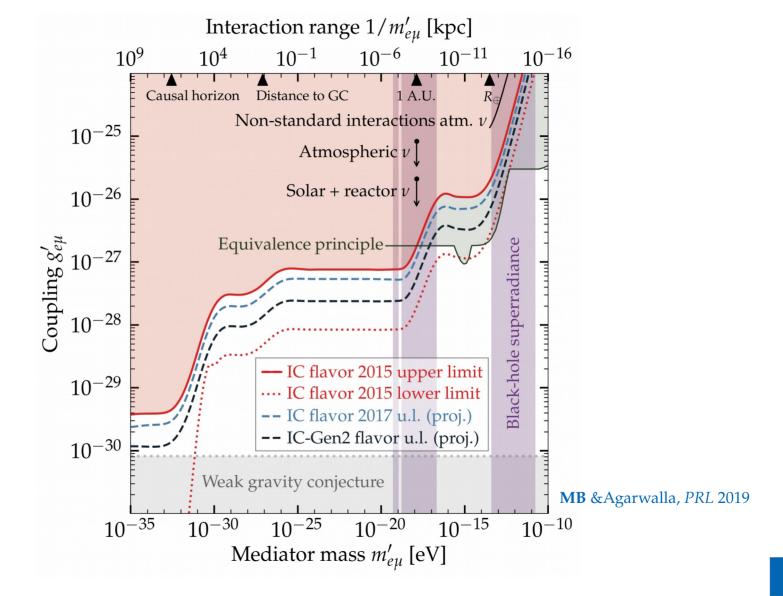








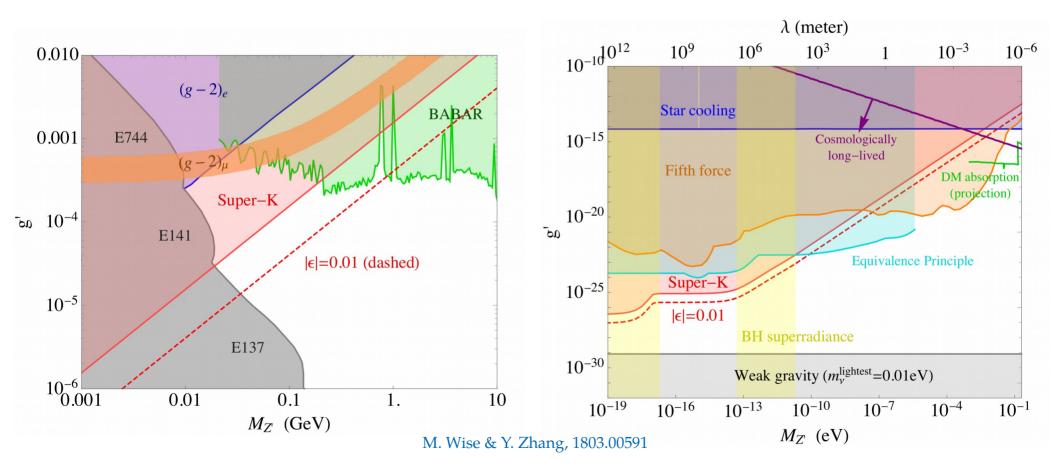




#### Current limits on the Z'

#### MeV-GeV masses

#### Sub-eV masses



## Connecting flavor-ratio predictions to experiment

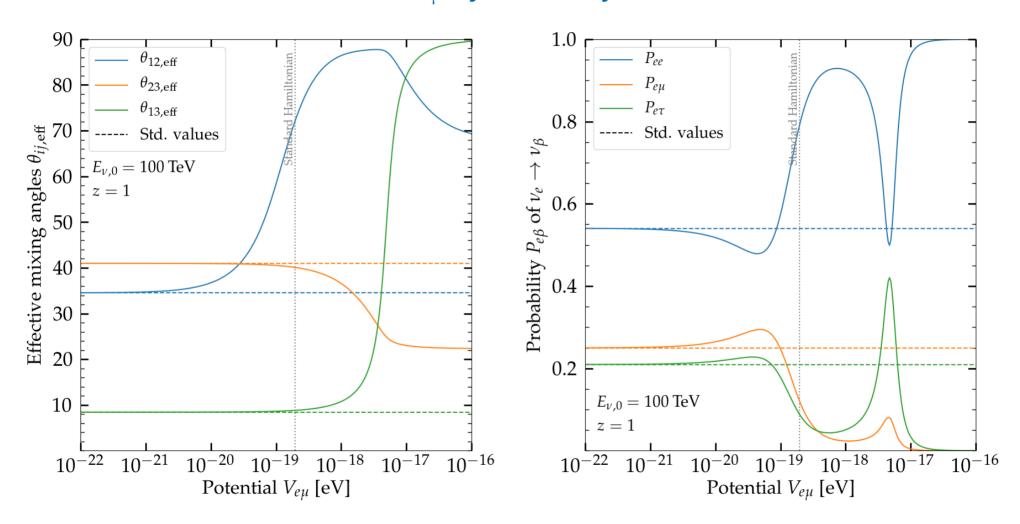
Integrate potential in redshift, weighed by source number density
 → Assume star formation rate

$$\langle V_{e\beta}^{\cos} \rangle \propto \int dz \; 
ho_{
m SFR}(z) \cdot rac{dV_{
m c}}{dz} \cdot V_{e\beta}^{\cos}(z)$$
 Density of cosmological  $e$  grows with  $z$ 

Convolve flavor ratios with observed neutrino energy spectrum  $\rightarrow$  Either  $E^{-2.50}$  (combined analysis) or  $E^{-2.13}$  (through-going muons)

$$\langle \Phi_{\alpha} \rangle \propto \int dE_{\nu} \ f_{\alpha,\oplus}(E_{\nu}) \ E_{\nu}^{-\gamma} \ \Rightarrow \ \langle f_{\alpha,\oplus} \rangle \equiv \frac{\langle \Phi_{\alpha} \rangle}{\sum_{\beta=e,\mu,\tau} \langle \Phi_{\beta} \rangle}$$
 Energy-averaged flux Energy-averaged flavor ratios

# Resonance due to the $L_e$ - $L_\mu$ symmetry



# Resonance due to the $L_e$ - $L_{\mu}$ symmetry (*cont.*)

