Primary Vertex resolution after applying beamspot constraint

Diwakar

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INFORMATION AVAILABLE IN THE BIG NTUPLES

1. Reconstructed primary vertex
2. Reconstructed primary vertex covariant matrix
3. Beamspot position
4. Beamspot covariant matrix

The idea is to recalculate the primary vertex by using this information by the method of minimising χ^2

RECALCULATING PV BY MINIMISING χ^2

Suppose:

- X(pv) = 3 vector containing PV
- X(bs) = 3 vector containing beamspot position
- V(pv) = 3*3 matrix containing PV covariant matrix (it is symmetric)
- V(bs) = 3*3 matrix containing beamspot covariant matrix (it is also symmetric)

Then χ^2 will be defined as:

$$(x - x(bs))^T V(bs)^{-1} (x - x(bs)) + (x - x(pv))^T V(pv)^{-1} (x - x(pv))$$

The next task is to minimise χ^2 w.r.t. x by taking the derivative of above equation w.r.t. x and putting it equal to 0 (done in next slide). From the resulting equation we will find the value of x for which χ^2 is minimum.

RECALCULATING PV BY MINIMISING χ^2

$$\chi^2 = (x - x(bs))^T V(bs)^{-1} (x - x(bs)) + (x - x(pv))^T V(pv)^{-1} (x - x(pv))$$

x is not a number but a 3 vector or 3*1 matrix.
Now taking derivative w.r.t x and putting it = 0.

$$(x - x(bs))^T V(bs)^{-1} + (x - x(bs))^T (V(bs)^{-1})^T + (x - x(pv))^T V(pv)^{-1} + (x - x(pv))^T (V(pv)^{-1})^T = 0$$

Where we have used the identities:

$$\frac{d(\mathbf{u}^T \mathbf{A} \mathbf{v})}{dx} = \mathbf{u}^T \mathbf{A} \frac{d\mathbf{v}}{dx} + \mathbf{v}^T \mathbf{A}^T \frac{d\mathbf{u}}{dx}$$

$$\frac{d\mathbf{x}^T}{d\mathbf{x}} = \mathbf{I}$$

RECALCULATING PV BY MINIMISING χ^2

$$(x - x(bs))^T V(bs)^{-1} + (x - x(bs))^T (V(bs)^{-1})^T + (x - x(pv))^T V(pv)^{-1} + (x - x(pv))^T (V(pv)^{-1})^T = 0$$

Since V(bs) and V(pv) are symmetric, $V(bs)^{-1}$ and $V(pv)^{-1}$ will also be symmetric, i.e.

$$(V(bs)^{-1})^T = V(bs)^{-1} \quad \text{and} \quad (V(pv)^{-1})^T = V(pv)^{-1}$$

Using this result and rearranging terms in above equation, we will get:

$$x^T = [x(bs)^T\, 2\, V(bs)^{-1} + x(pv)^T\, 2\, V(pv)^{-1}][2\, V(bs)^{-1} + 2\, V(pv)^{-1}]^{-1}$$

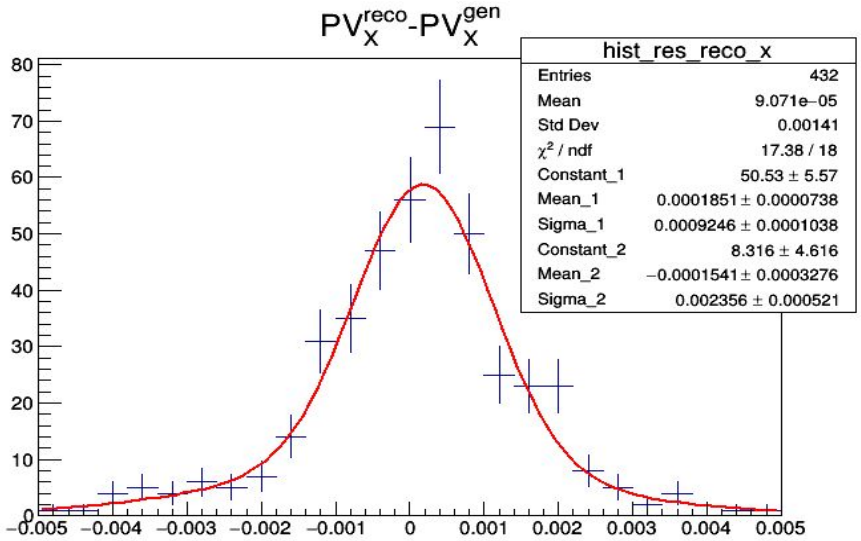
IMPLEMENTATION AND EXECUTION OF CODE

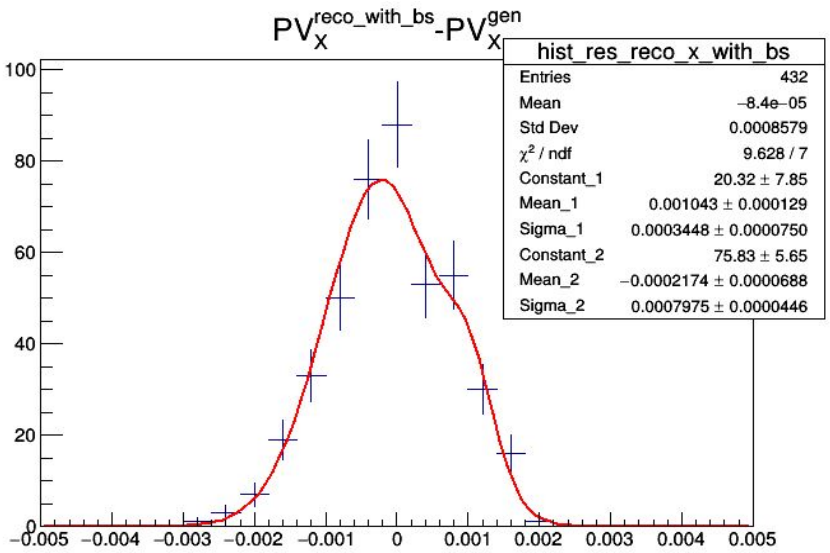
The code was written in SynchNTupleProducer.cpp

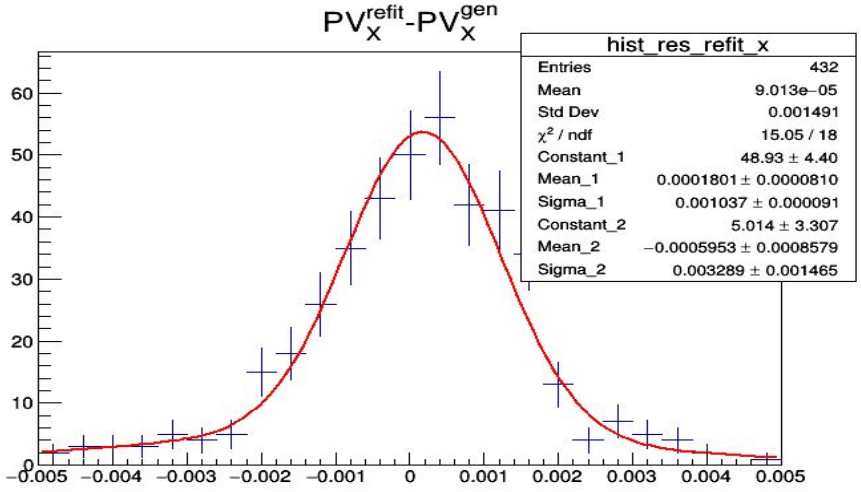
I ran the code for gg->H MC sample.

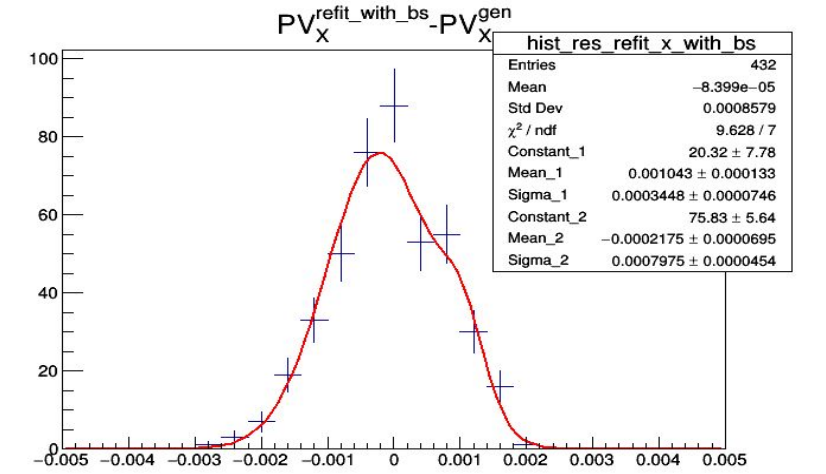
I selected the events in $m\tau_h$ channel for producing SynchNTuples.

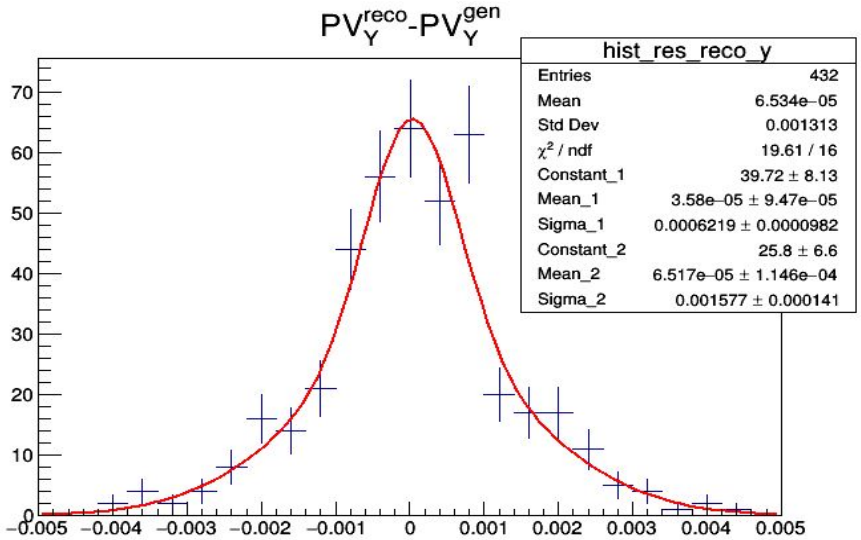
The primary vertex resolution plots are presented in the following slides:

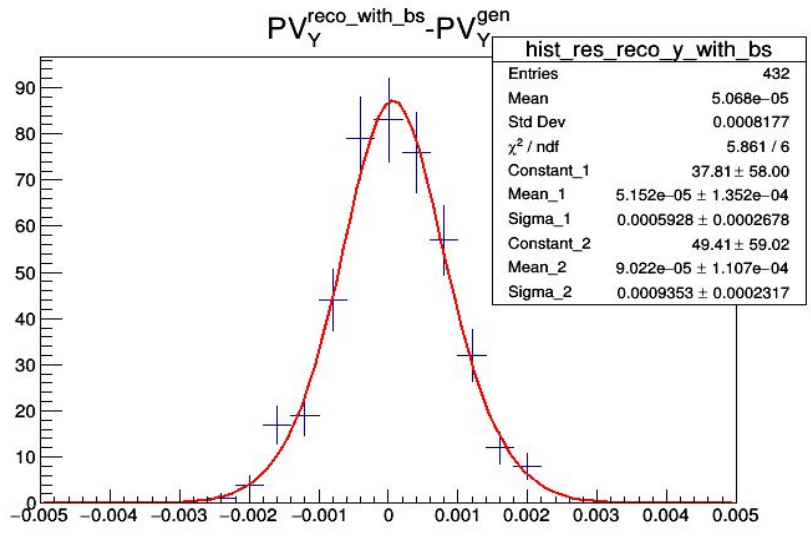

PV_x^{reco}-PV_x^{gen}
hist_res_reco_x
Entries 432
Mean 9.071e−05
Std Dev 0.00141
χ^2 / ndf 17.38 / 18
Constant_1 50.53 ± 5.57
Mean_1 0.0001851 ± 0.0000738
Sigma_1 0.0009246 ± 0.0001038
Constant_2 8.316 ± 4.616
Mean_2 −0.0001541 ± 0.0003276
Sigma_2 0.002356 ± 0.000521

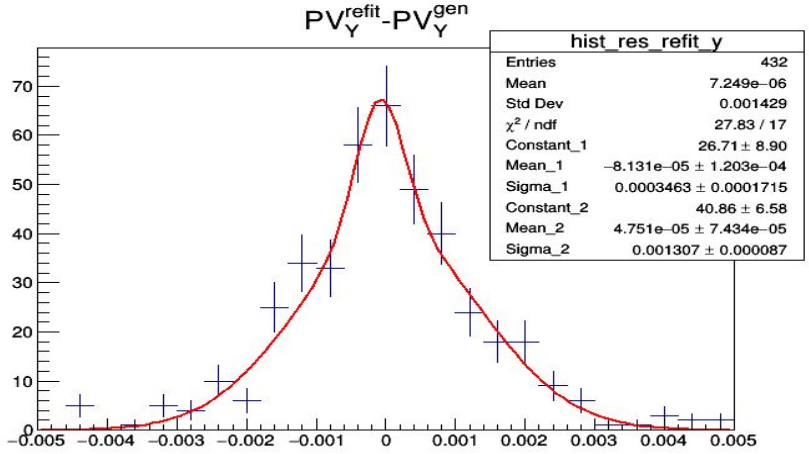

$PV_x^{reco\_with\_bs}$-PV_x^{gen}
hist_res_reco_x_with_bs
Entries 432
Mean −8.4e−05
Std Dev 0.0008579
χ^2 / ndf 9.628 / 7
Constant_1 20.32 ± 7.85
Mean_1 0.001043 ± 0.000129
Sigma_1 0.0003448 ± 0.0000750
Constant_2 75.83 ± 5.65
Mean_2 −0.0002174 ± 0.0000688
Sigma_2 0.0007975 ± 0.0000446

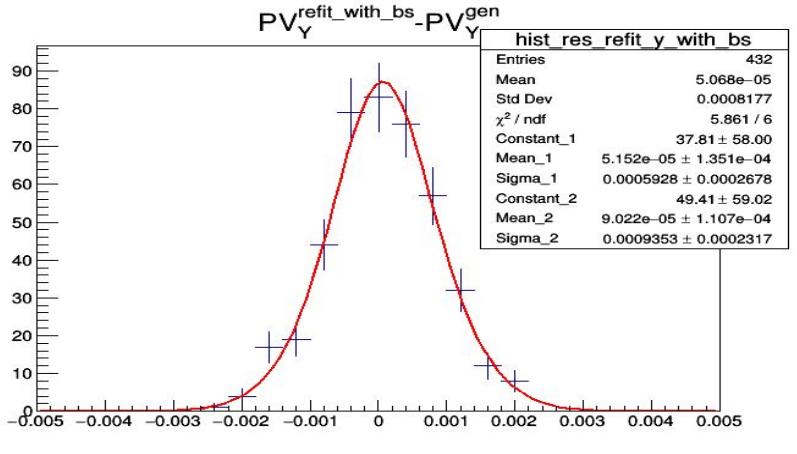

PV_x^{refit}-PV_x^{gen}
hist_res_refit_x
Entries 432
Mean 9.013e−05
Std Dev 0.001491
χ^2 / ndf 15.05 / 18
Constant_1 48.93 ± 4.40
Mean_1 0.0001801 ± 0.0000810
Sigma_1 0.001037 ± 0.000091
Constant_2 5.014 ± 3.307
Mean_2 −0.0005953 ± 0.0008579
Sigma_2 0.003289 ± 0.001465

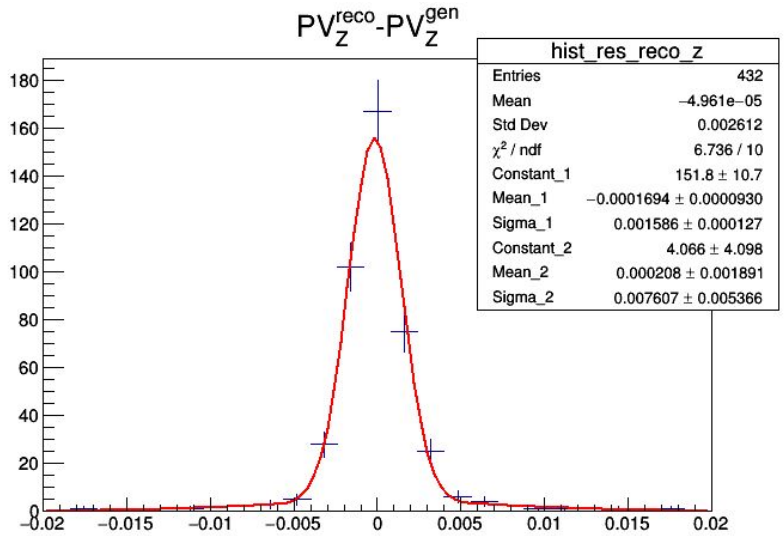

$PV_x^{refit\_with\_bs}$-PV_x^{gen}
hist_res_refit_x_with_bs
Entries 432
Mean −8.399e−05
Std Dev 0.0008579
χ^2 / ndf 9.628 / 7
Constant_1 20.32 ± 7.78
Mean_1 0.001043 ± 0.000133
Sigma_1 0.0003448 ± 0.0000746
Constant_2 75.83 ± 5.64
Mean_2 −0.0002175 ± 0.0000695
Sigma_2 0.0007975 ± 0.0000454

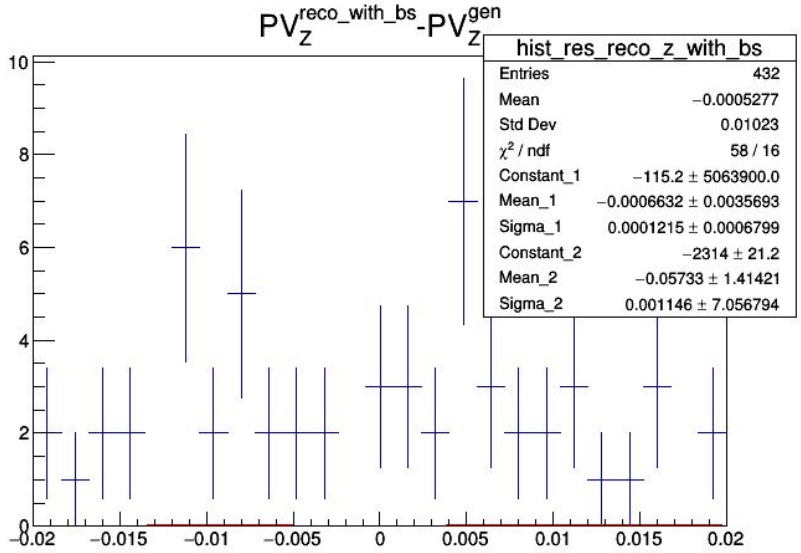

PV_Y^{reco}-PV_Y^{gen}
hist_res_reco_y
Entries 432
Mean 6.534e−05
Std Dev 0.001313
χ² / ndf 19.61 / 16
Constant_1 39.72 ± 8.13
Mean_1 3.58e−05 ± 9.47e−05
Sigma_1 0.0006219 ± 0.0000982
Constant_2 25.8 ± 6.6
Mean_2 6.517e−05 ± 1.146e−04
Sigma_2 0.001577 ± 0.000141

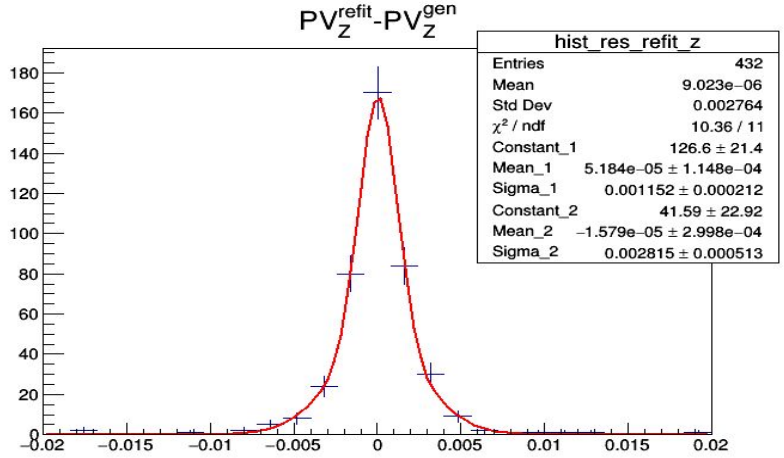

$PV_Y^{reco\_with\_bs}$-PV_Y^{gen}
hist_res_reco_y_with_bs
Entries 432
Mean 5.068e−05
Std Dev 0.0008177
χ² / ndf 5.861 / 6
Constant_1 37.81 ± 58.00
Mean_1 5.152e−05 ± 1.352e−04
Sigma_1 0.0005928 ± 0.0002678
Constant_2 49.41 ± 59.02
Mean_2 9.022e−05 ± 1.107e−04
Sigma_2 0.0009353 ± 0.0002317

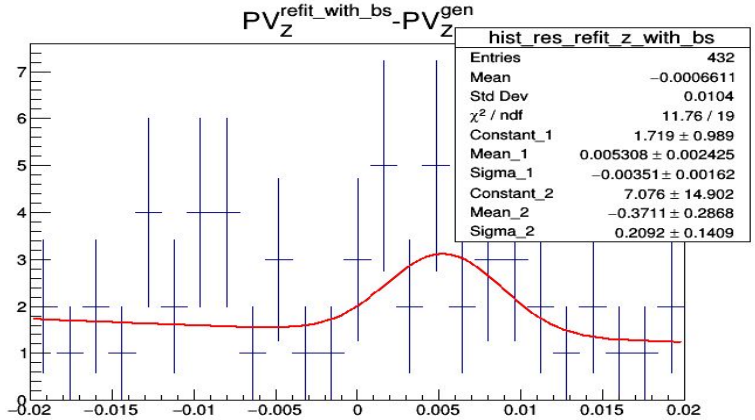

PV_Y^{refit}-PV_Y^{gen}
hist_res_refit_y
Entries 432
Mean 7.249e−06
Std Dev 0.001429
χ² / ndf 27.83 / 17
Constant_1 26.71 ± 8.90
Mean_1 −8.131e−05 ± 1.203e−04
Sigma_1 0.0003463 ± 0.0001715
Constant_2 40.86 ± 6.58
Mean_2 4.751e−05 ± 7.434e−05
Sigma_2 0.001307 ± 0.000087


$PV_Y^{refit\_with\_bs}$-PV_Y^{gen}
hist_res_refit_y_with_bs
Entries 432
Mean 5.068e−05
Std Dev 0.0008177
χ² / ndf 5.861 / 6
Constant_1 37.81 ± 58.00
Mean_1 5.152e−05 ± 1.351e−04
Sigma_1 0.0005928 ± 0.0002678
Constant_2 49.41 ± 59.02
Mean_2 9.022e−05 ± 1.107e−04
Sigma_2 0.0009353 ± 0.0002317


PV_z^{reco}-PV_z^{gen}
hist_res_reco_z
Entries 432
Mean −4.961e−05
Std Dev 0.002612
χ² / ndf 6.736 / 10
Constant_1 151.8 ± 10.7
Mean_1 −0.0001694 ± 0.0000930
Sigma_1 0.001586 ± 0.000127
Constant_2 4.066 ± 4.098
Mean_2 0.000208 ± 0.001891
Sigma_2 0.007607 ± 0.005366


$PV_z^{reco\_with\_bs}$-PV_z^{gen}
hist_res_reco_z_with_bs
Entries 432
Mean −0.0005277
Std Dev 0.01023
χ² / ndf 58 / 16
Constant_1 −115.2 ± 5063900.0
Mean_1 −0.0006632 ± 0.0035693
Sigma_1 0.0001215 ± 0.0006799
Constant_2 −2314 ± 21.2
Mean_2 −0.05733 ± 1.41421
Sigma_2 0.001146 ± 7.056794


PV_z^{refit}-PV_z^{gen}
hist_res_refit_z
Entries 432
Mean 9.023e−06
Std Dev 0.002764
χ² / ndf 10.36 / 11
Constant_1 126.6 ± 21.4
Mean_1 5.184e−05 ± 1.148e−04
Sigma_1 0.001152 ± 0.000212
Constant_2 41.59 ± 22.92
Mean_2 −1.579e−05 ± 2.998e−04
Sigma_2 0.002815 ± 0.000513


$PV_z^{refit\_with\_bs}$-PV_z^{gen}
hist_res_refit_z_with_bs
Entries 432
Mean −0.0006611
Std Dev 0.0104
χ² / ndf 11.76 / 19
Constant_1 1.719 ± 0.989
Mean_1 0.005308 ± 0.002425
Sigma_1 −0.00351 ± 0.00162
Constant_2 7.076 ± 14.902
Mean_2 −0.3711 ± 0.2868
Sigma_2 0.2092 ± 0.1409

CONCLUSIONS

- Beamspot constraint leads to a big improvement in resolution in x and y direction but it miscalculates the z direction totally.
- The effect of refitting is being totally washed out upon applying beamspot constraint in x and y direction.