

# Bounds on trilinear couplings in the baryon triality mSUGRA model from neutrino masses

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# Overview

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# Introduction

- neutrino oscillation data indicates that neutrinos are massive
- neutrinos contribute to hot dark matter
- "**Cosmological bound**": WMAP and LSS data combined<sup>1</sup> yield at 99.9% C.L.

$$\sum_i m_{\nu_i} < 0.40 \text{ eV}$$

- in the  $B_3$  mSUGRA model, neutrino masses are generated via lepton number violating (LNV) parameters  
 ⇒ cosmological bound can be used to restrict LNV parameters

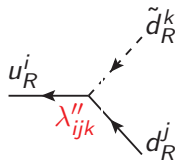
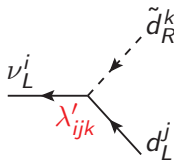
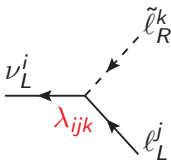
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<sup>1</sup>M. Cirellia and A. Strumia, Cosmology of neutrinos and extra light particles after WMAP3, astro-ph/0607086

# Baryon triality mSUGRA model

Full gauge invariant and renormalizable superpotential:

$$W = W_{MSSM} + \frac{1}{2} \lambda_{ijk} L_i L_j \bar{E}_k + \lambda'_{ijk} L_i Q_j \bar{D}_k - \kappa_i L_i H_u + \frac{1}{2} \lambda''_{ijk} \bar{U}_i \bar{D}_j \bar{D}_k$$



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- MSSM: R-Parity forbids all additional terms to prevent rapid proton decay
- but: R-Parity still allows dimension-five operators leading to proton decay
- **Baryon Triality** ( $B_3$ )
  - forbids BNV terms:  $\lambda'' + \text{dim.-5 operators}$
  - allows LNV terms:  $\lambda, \lambda', \kappa$
- ⇒ proton stability ensured
- further motivation: LNV in leptogenesis, majorana mass terms

# mSUGRA model

- SUSY cannot be an exact symmetry
- after soft SUSY breaking, there are  $\sim 200$  free parameters in a generic  $B_3$  SSM
- **Minimal Supergravity:** SUSY breaking takes place in a "hidden sector" which couples to the observable sector only via gravitational interactions.
- 5 free  $R_P$  conserving parameters

$$M_0, M_{1/2}, A_0, \tan \beta, \text{sgn} \mu$$

$\Rightarrow$  additionally, LNV parameters

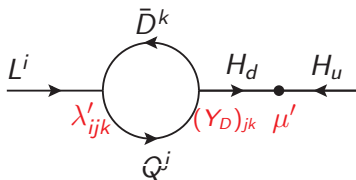
## $B_3$ mSUGRA model

- $\lambda$ ,  $\lambda'$  and  $\kappa$  constitute 39 additional parameters.
- all  $\kappa_i$  can be rotated away at the GUT scale

$$W \supset \mu H_u H_d + \kappa_i H_u L_i$$

$$\begin{pmatrix} \mu \\ \kappa_i \end{pmatrix} \rightarrow \begin{pmatrix} \mu' \\ 0 \end{pmatrix} \quad \text{for} \quad \begin{pmatrix} H_d \\ L_i \end{pmatrix} \rightarrow \begin{pmatrix} \mathcal{L}_0 \\ \mathcal{L}_i \end{pmatrix} = \mathcal{O}_{4 \times 4} \begin{pmatrix} H_d \\ L_i \end{pmatrix}$$

- running from  $M_{\text{GUT}}$  to  $M_Z$ , non-zero  $\kappa_i$  will be generated



## $B_3$ mSUGRA model

- $\lambda, \lambda'$  constitute 36 new parameters.
- makes sense assuming a strong hierarchy, analogously to the case of higgs yukawa couplings
- we select one (dominant) LNV coupling  $\Lambda \in (\lambda_{ijk}, \lambda'_{ijk})$   
 $\Rightarrow$  6 free parameters in total

$$\Lambda, M_0, M_{1/2}, A_0, \tan \beta, \text{sgn} \mu$$

- fix these at the GUT scale, use RGEs to calculate mass spectrum and couplings at  $M_Z$   
 $\Rightarrow$  SOFTSUSY-3.0.12<sup>2</sup> + routines for  $\nu$  masses & bounds

<sup>2</sup>B. C. Allanach, "SOFTSUSY: A C++ program for calculating supersymmetric spectra," hep-ph/0104145.



# Neutrino masses at tree level

- In the  $B_3$  mSUGRA model, neutrinos mix with neutralinos

$$\mathcal{L} = -\frac{1}{2} \begin{pmatrix} -i\tilde{B} & -i\tilde{\mathcal{W}}^3 & \tilde{h}_u^0 & \tilde{h}_d^0 & \nu_i \end{pmatrix} \mathcal{M}_N \begin{pmatrix} -i\tilde{B} \\ -i\tilde{\mathcal{W}}^3 \\ \tilde{h}_u^0 \\ \tilde{h}_d^0 \\ \nu_j \end{pmatrix},$$

$$\mathcal{M}_N = \begin{pmatrix} \mathcal{M}_{\chi^0} & m^T \\ m & 0 \end{pmatrix}$$

⇒ analogous to standard seesaw mechanism

- effective neutrino mass matrix

$$\mathcal{M}_{\text{eff}}^\nu = -m \mathcal{M}_{\chi^0}^{-1} m^T$$

- just one non-zero eigenvalue  $m_\nu^{\text{tree}} \sim -\sum_{i=1}^3 \left( \frac{v_d}{\mu} \kappa_i - v_i \right)^2$ .

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$\Rightarrow$  analogous to standard seesaw mechanism

- effective neutrino mass matrix

$$\mathcal{M}_{\text{eff}}^\nu = -m \mathcal{M}_{\chi^0}^{-1} m^T + m_\nu^{\text{loops}}$$

- just one non-zero eigenvalue  $m_\nu^{\text{tree}} \sim -\sum_{i=1}^3 (v_i - v_d \frac{\kappa_i}{\mu})^2$ .

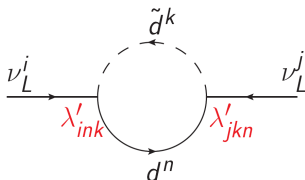
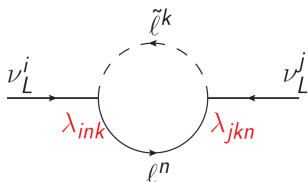
# Loop contributions to neutrino masses

- usually,

$$\frac{m_\nu^{\text{loops}}}{m_\nu^{\text{tree}}} \sim \mathcal{O}(10^{-2})$$

- but there are regions of parameter space where  $m_\nu^{\text{tree}} \rightarrow 0$   
 $\Rightarrow$  loops become dominant!
- important contributions that are not aligned to tree level mass:

$\lambda\lambda$ - and  $\lambda'\lambda'$ -loops



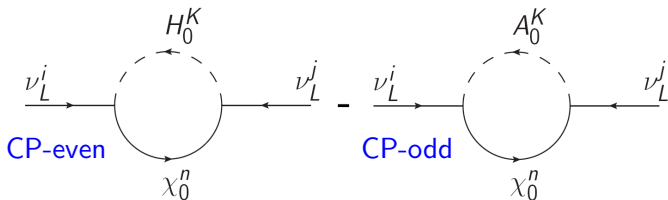
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## Neutral Scalar - Neutralino loops



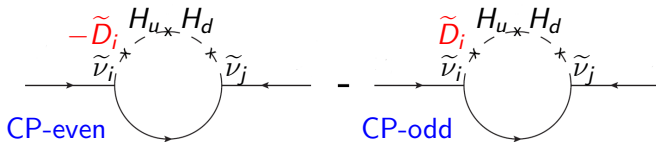
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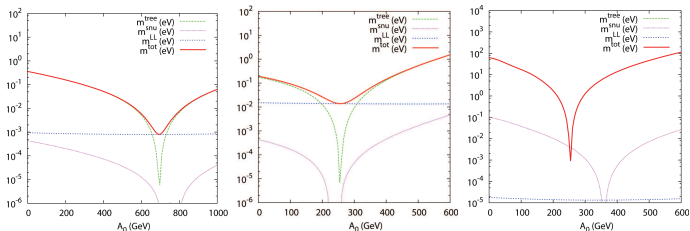
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- but there are regions of parameter space where  $m_\nu^{\text{tree}} \rightarrow 0$   
 $\Rightarrow$  loops become dominant!
- important contributions that are not aligned to the tree level mass:

Neutral Scalar - Neutralino loops  $\sim \Delta m_\nu^2$



# mSUGRA dependence of the neutrino mass contributions



- (a)  $\lambda'_{233} = 10^{-5}$ ,  $M_{1/2} = 300$  GeV,  $M_0 = 500$  GeV,  $\tan \beta = 20$ ,  $\text{sgn}\mu = +1$   
 (b)  $\lambda_{211} = 0.2$ ,  $M_{1/2} = 600$  GeV,  $M_0 = 0$  GeV,  $\tan \beta = 15$ ,  $\text{sgn}\mu = +1$   
 (c)  $\lambda_{211} = 0.001$ ,  $M_{1/2} = 100$  GeV,  $M_0 = 0$  GeV,  $\tan \beta = 10$ ,  $\text{sgn}\mu = +1$

- RGEs tell us that  $\nu$  mass always displays this minimum, for

$$A_0 \approx 2M_{1/2} \quad (\text{case } \Lambda \in \lambda')$$

$$A_0 \approx 1/2M_{1/2} \quad (\text{case } \Lambda \in \lambda)$$

- shifted to higher values of  $A_0$  for  $\tan \beta \lesssim 10$
- for all contributions,  $m_\nu \propto \Lambda^2$

## Upper bounds on the LNV coupling

- neutrino mass minimum yields bounds that are 1-2 orders of magnitude weaker than in previous studies
- Upper bounds on  $\lambda'_{ijk}$  at  $M_{\text{GUT}}$  for SPS1a-like parameters<sup>3</sup>:

$A_0$ (GeV)	Up mixing			Down mixing		
	-100	500	550	-100	500	550
$\lambda'_{i11}$	$2 \times 10^{-3}$	$3 \times 10^{-2}$	$1 \times 10^{-1}$	$1 \times 10^{-3}$	$1 \times 10^{-2}$	$7 \times 10^{-2}$
$\lambda'_{i22}$	$1 \times 10^{-4}$	$1 \times 10^{-3}$	$7 \times 10^{-3}$	$1 \times 10^{-4}$	$1 \times 10^{-3}$	$6 \times 10^{-3}$
$\lambda'_{i33}$	$3 \times 10^{-6}$	$3 \times 10^{-5}$	$2 \times 10^{-4}$	$3 \times 10^{-6}$	$3 \times 10^{-5}$	$2 \times 10^{-4}$
$\lambda'_{i21}, \lambda'_{i12}$	-	-	-	$5 \times 10^{-4}$	$7 \times 10^{-3}$	$4 \times 10^{-2}$
$\lambda'_{i32}, \lambda'_{i23}$	$2 \times 10^{-2}$	$4 \times 10^{-1}$	-	$8 \times 10^{-5}$	$9 \times 10^{-4}$	$4 \times 10^{-3}$
$\lambda'_{i31}, \lambda'_{i13}$	$-, 2 \times 10^{-2}$	$-, 6 \times 10^{-2}$	$-, 2 \times 10^{-1}$	$9 \times 10^{-4}$	$9 \times 10^{-3}$	$4 \times 10^{-2}$

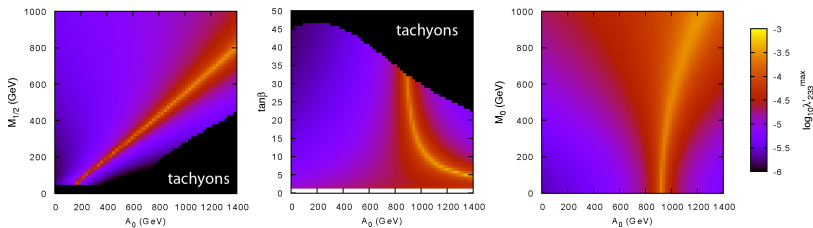
- usually strongest bounds on LNV couplings are from  $\nu$  masses
- in vicinity of minimum, other bounds become comparable, e.g.

$$\lambda'_{211} < 0.06 \text{ from } \Gamma(\pi^- \rightarrow \ell^- \bar{\nu}_\ell)^4$$

<sup>3</sup>  $A_0 = -100$  GeV column from B. C. Allanach et al., "The RPV mSUGRA model," hep-ph/0309196.

<sup>4</sup> Y. Kao and T. Takeuchi, "Single-Coupling Bounds on R-parity violating SUSY, an update," arXiv:0910.4980.

## Two dimensional scans

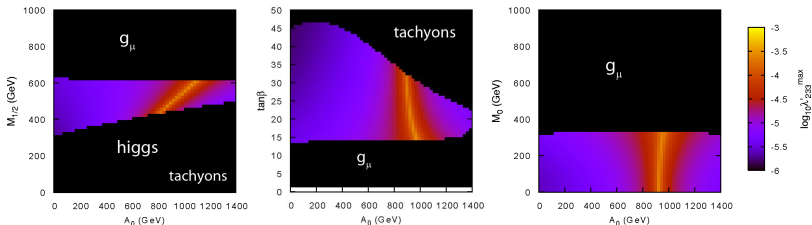


Upper bounds on  $\Lambda \in \lambda'_{233}$  around  $M_{1/2} = 500$  GeV,  $M_0 = 100$  GeV,  $\tan \beta = 20$ ,  $\text{sgn} \mu = +1$

- approx 2 orders of magnitude variation in bounds
- excluded regions due to tachyons



## Other bounds on $B_3$ mSUGRA parameter space



Upper bounds on  $\Lambda \in \chi'_{233}$  around  $M_{1/2} = 500$  GeV,  $M_0 = 100$  GeV,  $\tan \beta = 20$ ,  $\text{sgn} \mu = +1$

- including bounds from
  - LEP2 (higgs)
  - tachyons
  - anomalous magnetic moment of the muon (" $g_\mu$ ")<sup>5</sup>
  - $\text{BR}(b \rightarrow s\gamma)$ <sup>5</sup>
  - $\text{BR}(B_s \rightarrow \mu^+ \mu^-)$ <sup>5</sup>
- still sizeable regions with weaker bounds

<sup>5</sup> using micrOMEGAs2.2 by G. Belanger et al.

## Summary

- there are extended regions of parameter space where bounds on LNV coupling become one to two orders of magnitude weaker than previously considered, up to  $\Lambda \sim \mathcal{O}(0.1)$
- in these regions, loop contributions to neutrino mass from  $\lambda\lambda$ - ( $\lambda'\lambda'$ -) and sneutrino-antisneutrino mixing loops are important
- large LNV couplings give new LSP candidates (e.g. sneutrino,  $\tilde{e}_R$ ) and can lead to resonant single slepton production at the LHC
- to explain neutrino oscillation data ( $\rightarrow$  neutrino mass hierarchy), we need additionally to dominant LNV coupling at least one more small coupling

## Appendix (LHC phenomenology)

- for large LNV couplings, resonant single slepton production possible at the LHC e.g.

$$u_j \bar{d}_k \rightarrow \tilde{\ell}_i^+ \rightarrow \ell_i^+ \tilde{\chi}_m^0$$

- promising like-sign dilepton signature for  $\lambda' = \mathcal{O}(10^{-2})$ , e.g. neutralino LSP scenario with  $\lambda'_{211} = 0.01^6$

$$\begin{aligned} \tilde{\mu}^+ &\rightarrow \mu^+ \tilde{\chi}_1^0 \\ &\stackrel{\lambda'}{\hookrightarrow} \mu^+ \bar{u} d \end{aligned}$$

- current bound from hadron collider resonant production:

$$\lambda'_{211}|_{M_{GUT}} < 0.059$$

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<sup>6</sup>S. Grab et al., "Supersymmetric NLO QCD corrections to resonant slepton production and signals at the Tevatron and the LHC," hep-ph/0611195

## Appendix (LHC phenomenology)

- new LSP candidates beyond  $\chi_1^0, \tilde{\tau}_1$  if  $\Lambda = \mathcal{O}(0.1)$
- e.g. sneutrino LSP for  $\lambda'_{ijk} > 0.05$  possible<sup>7</sup>
- will dominantly decay into two jets via  $\lambda'_{ijk} (\tilde{\nu}_i \rightarrow \bar{d}_j d_k)$
- other possible LSPs:  $\tilde{e}_R$  (for  $\lambda_{121}, \lambda_{131}, \lambda_{231}$ ),  $\tilde{\mu}_R$  (for  $\lambda_{132}$ )<sup>8</sup>
- for these values of  $\Lambda$ , direct and dominating  $B_3$  decays of heavy sparticles

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<sup>7</sup> M. A. Bernhardt et al., "Sneutrino as Lightest Supersymmetric Particle in  $B_3$  mSUGRA Models and Signals at the LHC," arXiv:0810.3423

<sup>8</sup> H. K. Dreiner et al., "All Possible LSPs in R-Parity Violating mSUGRA Models," arXiv:0909.5407 