



# Constraining the Higgs boson self-coupling from single-Higgs and the combination of single-Higgs and double-Higgs

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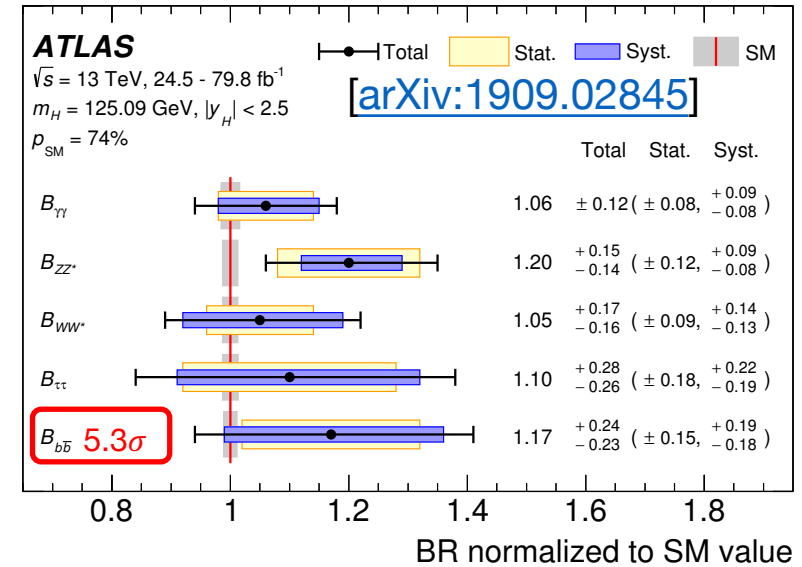
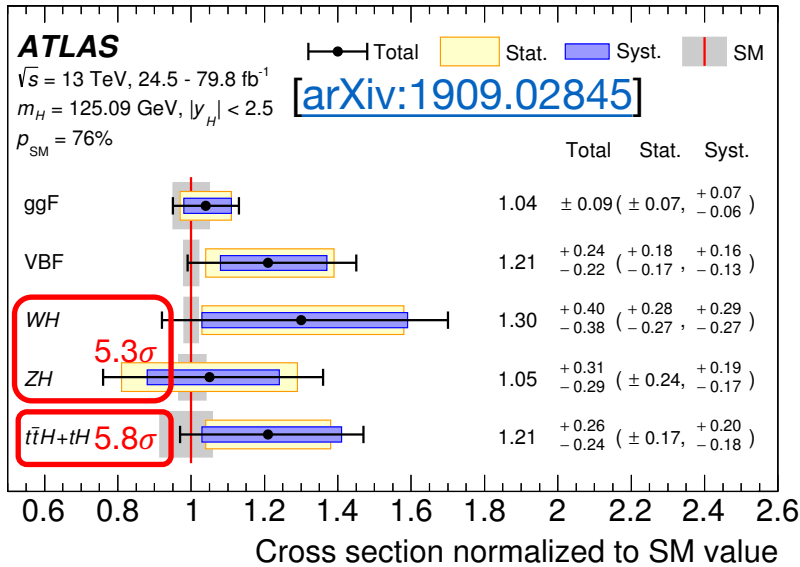
13th Annual Meeting of the Helmholtz Alliance "Physics at the Terascale"

# Outline

- Constraints on the Higgs self-coupling from the **single-Higgs** analyses
- Constraints on the Higgs self-coupling from the **combination** of the single-Higgs and double-Higgs analyses

# Introduction

- During Run2 data taking, the Higgs production processes and decays have been measured with an increasing precision
  - $VH$ ,  $ttH$ ;  $H \rightarrow b\bar{b}$  were discovered during Run2

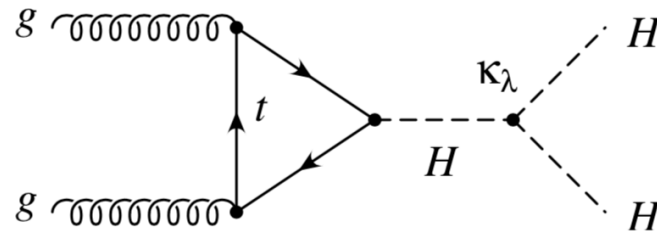


$$V(H) = \frac{m_H^2}{2} H^2 + \lambda_3 v H^3 + \lambda_4 H^4$$

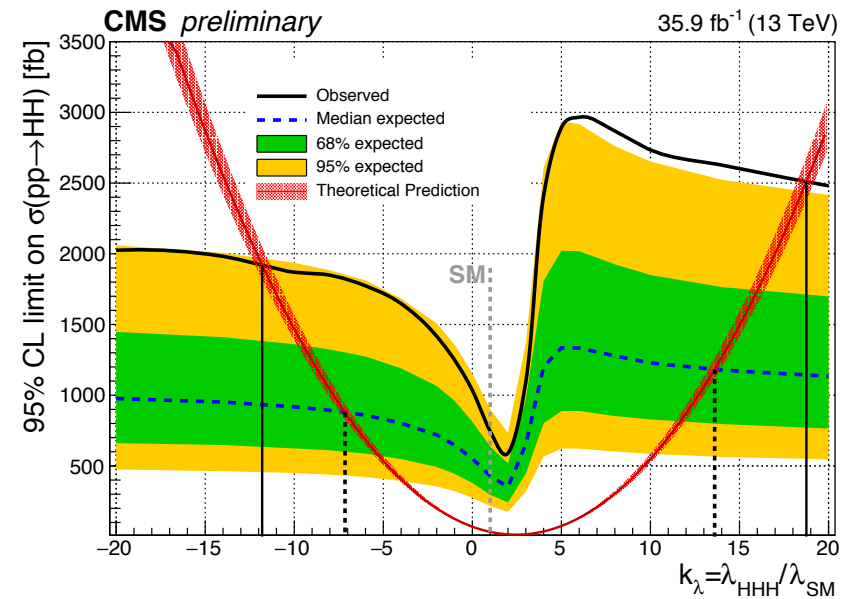
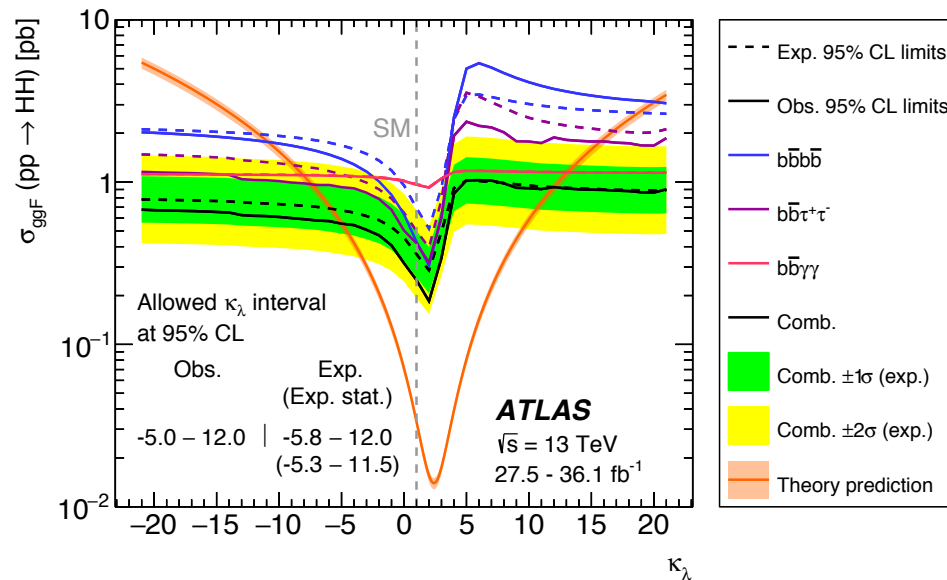
- The properties of the Higgs scalar potential, in particular the Higgs boson self-coupling, are still largely unconstrained

# Latest results in the HH measurement

- The non-resonant HH production processes (ggF) provide a unique chance to probe  $\kappa_\lambda = \lambda_{HHH}/\lambda_{HHH}^{SM}$  with direct measurements



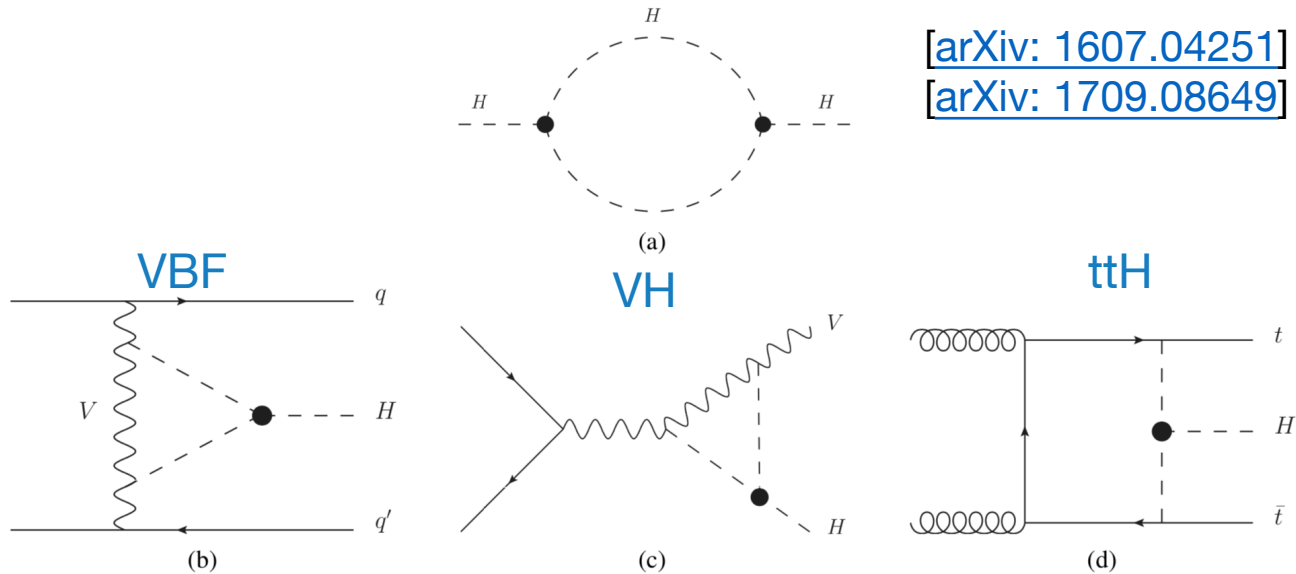
- Constrain the  $\kappa_\lambda$  by estimating the upper limits of the HH production (assuming SM H decay) with CLs approach



95% CL	Obs.	Exp.
ATLAS [ <a href="https://arxiv.org/abs/1906.02025">arXiv:1906.02025</a> ]	[-5.0, 12.0]	[-5.8, 12.0]
CMS [ <a href="https://arxiv.org/abs/1703.03020">CMS-PAS-HIG-17-030</a> ]	[-11.8, 18.8]	[-7.1, 13.6]

# Indirect measurement in the single-H

- **Single Higgs processes** do not depend on  $\lambda_{HHH}$  at LO, while its contributions need to be taken into account for the complete **NLO EWK corrections**
- $\lambda_{HHH}$  contributes via Higgs **self energy loop** corrections and additional diagrams

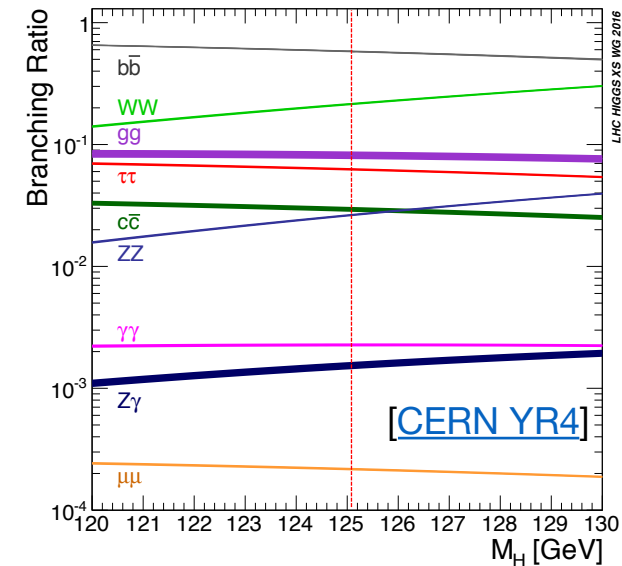


- An **indirect constraint** on  $\lambda_{HHH}$  can be extracted by comparing the single-Higgs measured results and the SM predictions corrected for the  $\lambda_{HHH}$ -dependent NLO EW effects

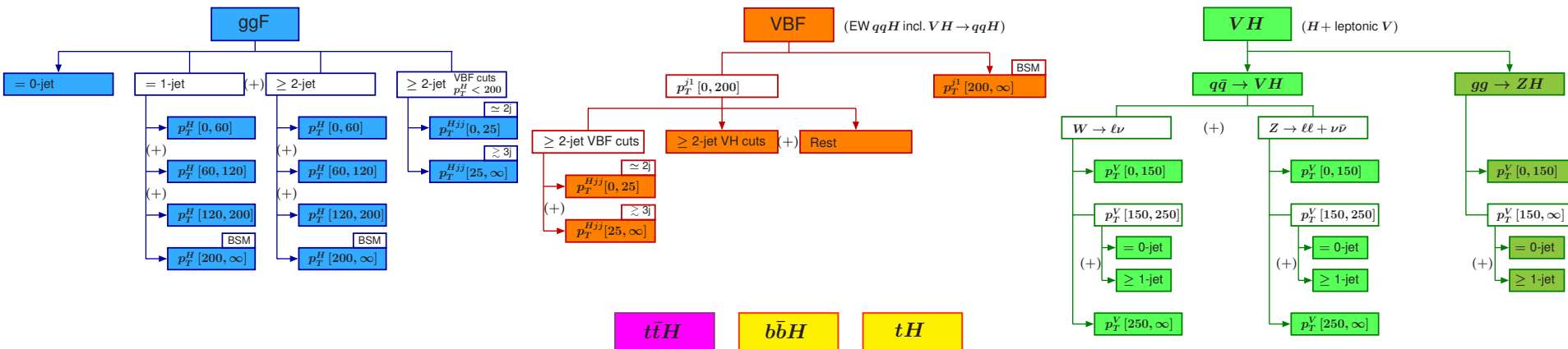
- Signal strength:  $\mu_{if}(\kappa\lambda) = \mu_i(\kappa\lambda) \times \mu_f(\kappa\lambda) \equiv \frac{\sigma_i(\kappa\lambda)}{\sigma_{SM,i}} \times \frac{BR_f(\kappa\lambda)}{BR_{SM,f}}$

# Data and input measurement

Analysis	Integrated luminosity ( $\text{fb}^{-1}$ )
$H \rightarrow \gamma\gamma$ (including $t\bar{t}H, H \rightarrow \gamma\gamma$ )	79.8
$H \rightarrow ZZ^* \rightarrow 4\ell$ (including $t\bar{t}H, H \rightarrow ZZ^* \rightarrow 4\ell$ )	79.8
$H \rightarrow WW^* \rightarrow e\nu\mu\nu$	36.1
$H \rightarrow \tau\tau$	36.1
$VH, H \rightarrow b\bar{b}$	79.8
$t\bar{t}H, H \rightarrow b\bar{b}$ and $t\bar{t}H$ multilepton	36.1



- Higgs couplings measurements separate production processes and kinematic regions using the [simplified template cross section \(STXS\) framework, YR4](#)
- The analysis categories are designed to [maximize the sensitivity to each truth-level region](#) defined within the framework



# Theoretical model: production mode

$$\mu_i(\kappa_\lambda, \kappa_i) = \frac{\sigma^{BSM}}{\sigma^{SM}} = Z_H^{BSM}(\kappa_\lambda) \left[ \kappa_i^2 + \frac{(\kappa_\lambda - 1)C_1^i}{K_{EW}^i} \right]$$

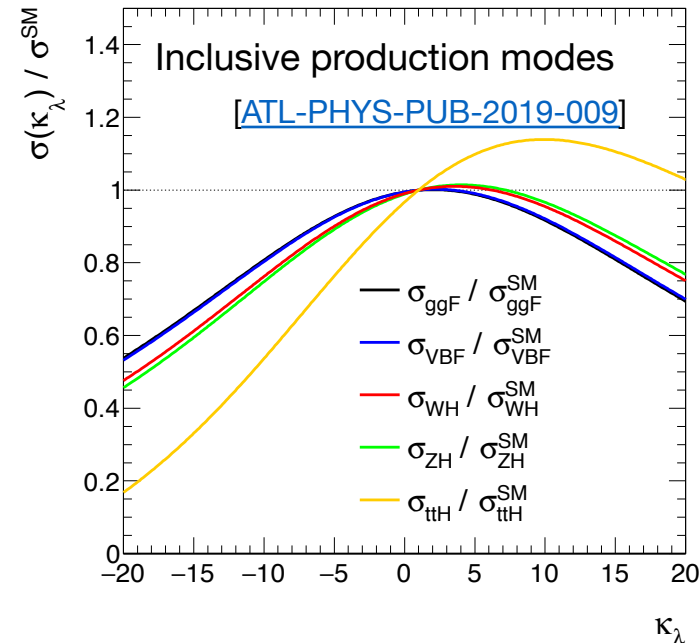
$$Z_H^{BSM}(\kappa_\lambda) = \frac{1}{1 - (\kappa_\lambda^2 - 1)\delta Z_H}, \quad \delta Z_H = -1.536 \times 10^{-3}$$

- $K_{EW}^i = \frac{\sigma_{NLO}^{SM,i}}{\sigma_{LO}^{SM,i}}$ : Complete NLO EW correction for the production
- $C_1^i$ : process and kinematics-dependent linear coefficient that provides the sensitivity of the measurement to  $\kappa_\lambda$
- $\kappa_i^2 = \frac{\sigma_{LO,i}^{BSM}}{\sigma_{LO,i}^{SM}}$ : Modifiers to other Higgs boson couplings in the  $\kappa$ -framework
  - Only  $\kappa_F$  (all fermions) and  $\kappa_V$  (all weak vector bosons) are considered

[arXiv: 1607.04251]

[arXiv: 1709.08649]

production mode	ggF	VBF	ZH	WH	$t\bar{t}H$
<b>inclusive</b> $C_1^i \times 100$	0.66	0.63	1.19	1.03	3.52
$K_{EW}^i$	1.049	0.932	0.947	0.93	1.014
$\kappa_i^2$	$\kappa_F^2$	$\kappa_V^2$	$\kappa_V^2$	$\kappa_V^2$	$\kappa_F^2$



# Theoretical model: decay rate

- Higgs boson decay rates

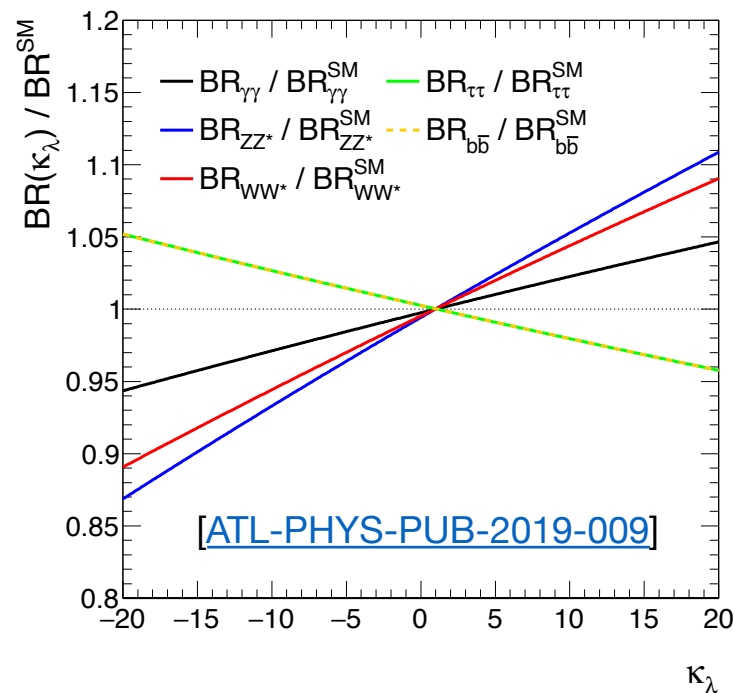
$$\mu_f(\kappa_\lambda, \kappa_f) = \frac{BR_f^{BSM}}{BR_f^{SM}} = \frac{\kappa_f^2 + (\kappa_\lambda - 1)C_1^f}{\sum_j BR_j^{SM} [\kappa_j^2 + (\kappa_\lambda - 1)C_1^j]}$$

- $C_1^f$ : linear coefficient provides the sensitivity to  $\kappa_\lambda$

[arXiv: 1607.04251]

[arXiv: 1709.08649]

decay mode	$H \rightarrow \gamma\gamma$	$H \rightarrow WW^*$	$H \rightarrow ZZ^*$	$H \rightarrow b\bar{b}$	$H \rightarrow \tau\tau$
$C_1^f \times 100$	0.49	0.73	0.82	0	0
$\kappa_f^2$	$1.59\kappa_V^2 + 0.07\kappa_F^2 - 0.67\kappa_V\kappa_F$	$\kappa_V^2$	$\kappa_V^2$	$\kappa_F^2$	$\kappa_F^2$



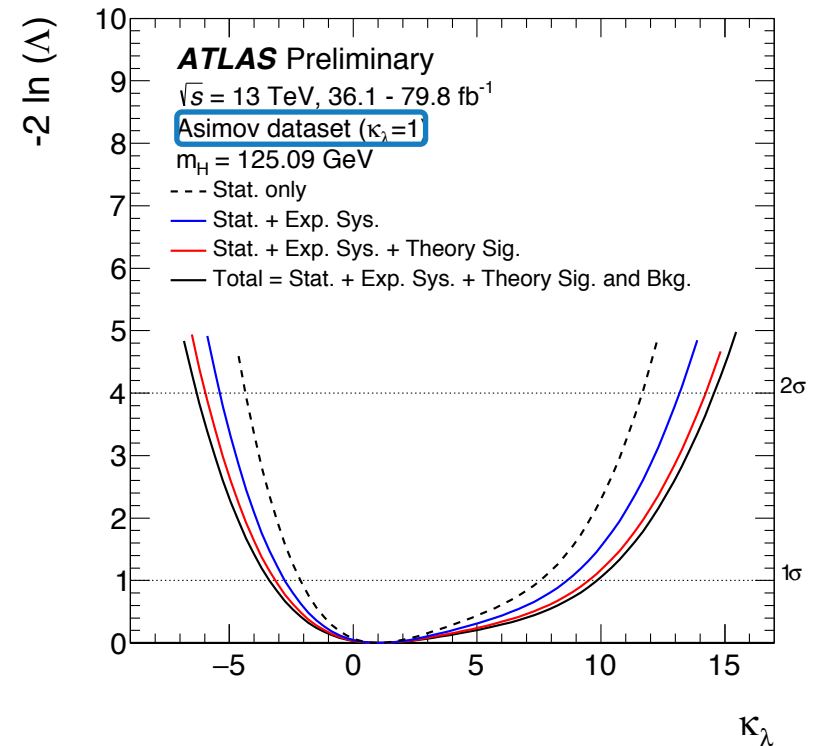
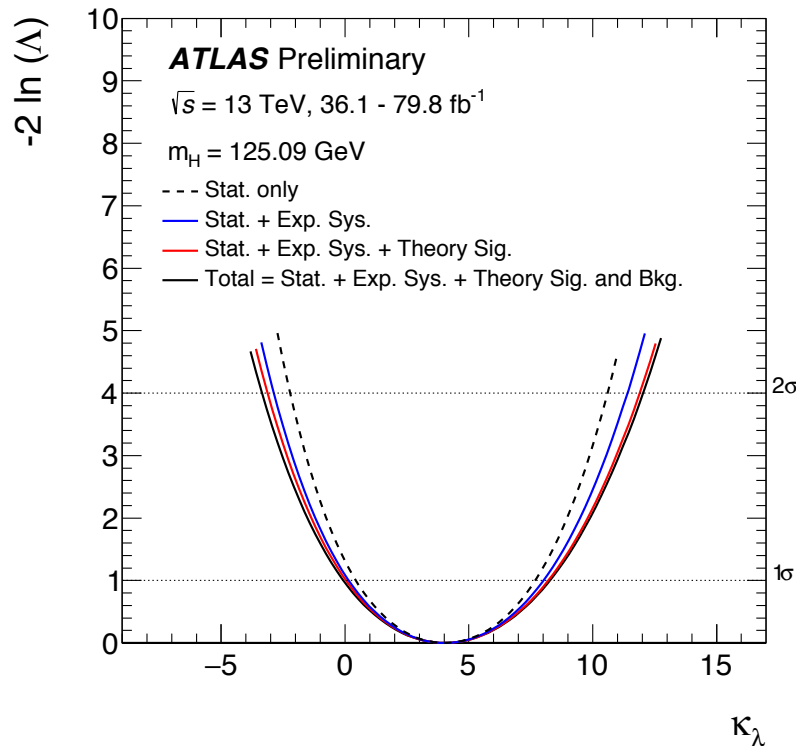


# Kinematic dependence of $\kappa_\lambda$

- A more differential description (i.e STXS w.r.t the inclusive production processes) of the dependence on  $\kappa_\lambda$  can help
  - To reduce the potential bias on the determination of  $\kappa_\lambda$
  - To further increase the sensitivity to  $\kappa_\lambda$
- The dependence is considered by exploiting cross-sections in the STXS stage-1 framework
- The analysis estimated dependence in the VBF, ZH and WH
  - Re-deriving the kinematic dependent coefficients  $C_1^i$  in stage 1 truth bins
- Differential  $\kappa_\lambda$  corrections are not yet available for ggF, because these involve higher order calculations including two loop corrections
- The measurement for the ttH are inclusive so far

# $\kappa_\lambda$ -only results

- A likelihood fit is performed to constrain the Higgs boson self-coupling  $\kappa_\lambda$  in the single-Higgs measurement
  - Theory validity range [arXiv: 1607.04251]:  $-20 < \kappa_\lambda < 20$



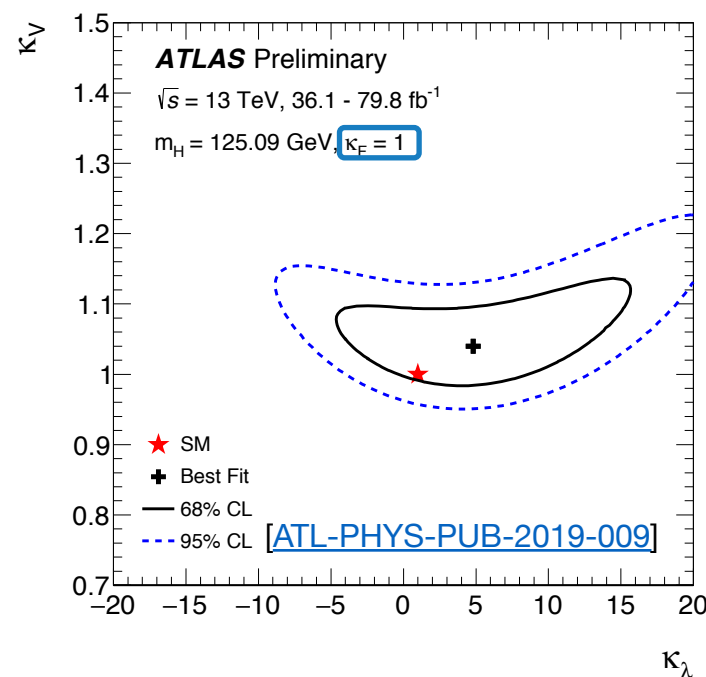
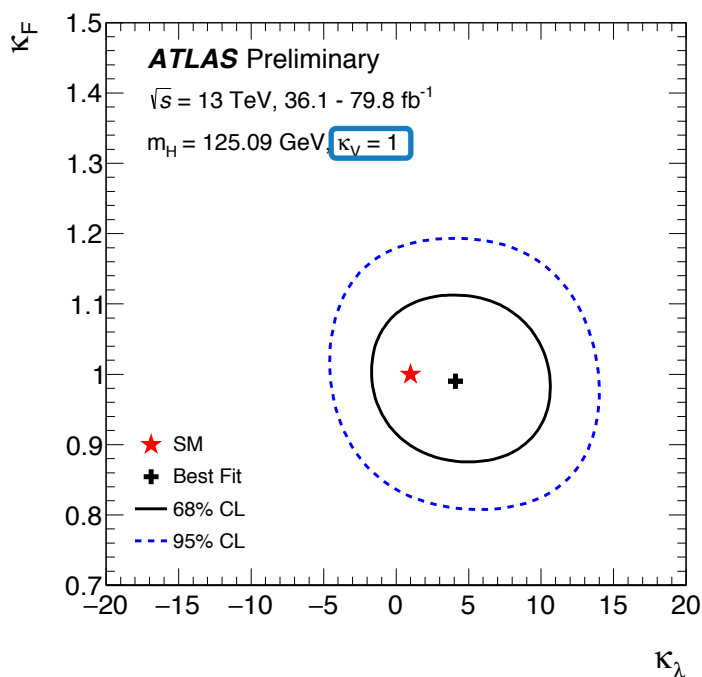
- Best fit:  $\kappa_\lambda = 4.0^{+4.3}_{-4.1} = 4.0^{+3.7}_{-3.6}(\text{stat.})^{+1.6}_{-1.5}(\text{exp.})^{+1.3}_{-0.9}(\text{sig. th.})^{+0.8}_{-0.9}(\text{bkg. th.})$

95% CL	Obs.	Exp.
H [ATL-PHYS-PUB-2019-009], up to 80 /fb	[-3.2, 11.9]	[-6.2, 14.4]
HH [arXiv:1906.02025], up to 36 /fb	[-5.0, 12.0]	[-5.8, 12.0]

- The sensitivity from single-Higgs and double-Higgs is similar

# $\kappa_\lambda$ and $\kappa_F$ , $\kappa_\lambda$ and $\kappa_V$ fits

- A simultaneous fit is performed to  $\kappa_\lambda$  and  $\kappa_F$  ( $\kappa_V = 1$ ),  $\kappa_\lambda$  and  $\kappa_V$  ( $\kappa_F = 1$ )
- These fits target scenarios where new physics could affect only the Yukawa type terms ( $\kappa_V = 1$ ) or only the couplings to vector bosons ( $\kappa_F = 1$ ), in addition to the Higgs boson self-coupling ( $\kappa_\lambda$ )



- The sensitivity to  $\kappa_\lambda$  is not much degraded when determining  $\kappa_F$  at the same time
- While it's degraded by 50% when determining  $\kappa_V$  simultaneously

POIs	Granularity	$\kappa_F^{+1\sigma}_{-1\sigma}$	$\kappa_V^{+1\sigma}_{-1\sigma}$	$\kappa_\lambda^{+1\sigma}_{-1\sigma}$	$\kappa_\lambda$ [95% C.L.]
$\kappa_\lambda$	STXS	1	1	$4.0^{+4.3}_{-4.1}$	[-3.2, 11.9] <b>Obs</b>
				$1.0^{+8.8}_{-4.4}$	[-6.2, 14.4] <b>Exp</b>
$\kappa_\lambda, \kappa_V$	STXS	1	$1.04^{+0.05}_{-0.04}$	$4.8^{+7.4}_{-6.7}$	[-6.7, 18.4]
			$1.00^{+0.05}_{-0.04}$	$1.0^{+9.9}_{-6.1}$	[-9.4, 18.9]
$\kappa_\lambda, \kappa_F$	STXS	$0.99^{+0.08}_{-0.08}$	1	$4.1^{+4.3}_{-4.1}$	[-3.2, 11.9]
		$1.00^{+0.08}_{-0.08}$		$1.0^{+8.8}_{-4.4}$	[-6.3, 14.4]

- Combine **single-Higgs** and **double-Higgs** together to maximize the sensitivity to constrain  $\kappa_\lambda$

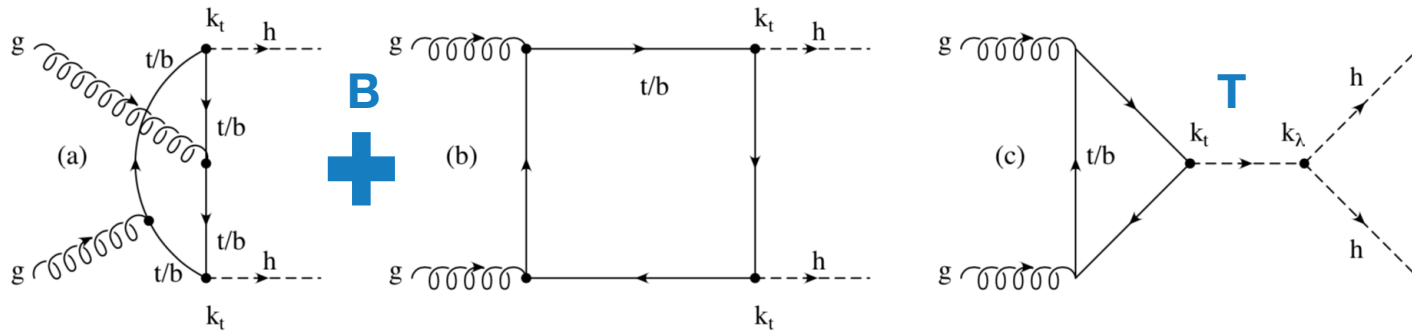
# Data and input measurement

Analysis	Integrated luminosity (fb <sup>-1</sup> )
$H \rightarrow \gamma\gamma$	79.8
$H \rightarrow ZZ^* \rightarrow 4\ell$ (including $t\bar{t}H$ , $H \rightarrow ZZ^* \rightarrow 4\ell$ )	79.8
$H \rightarrow WW^* \rightarrow e\nu\mu\nu$	36.1
$H \rightarrow \tau\tau$	36.1
$VH, H \rightarrow b\bar{b}$	79.8
$t\bar{t}H, H \rightarrow b\bar{b}$ and $t\bar{t}H$ multilepton	36.1
$HH \rightarrow b\bar{b}b\bar{b}$	27.5
$HH \rightarrow b\bar{b}\tau^+\tau^-$	36.1
$HH \rightarrow b\bar{b}\gamma\gamma$	36.1

- Within each of the single-Higgs and the double-Higgs analyses all the categories are orthogonal by definition
- The **single-Higgs** and **double-Higgs** categories are not all orthogonal
  - The overlap has been studied, the  $ttH(\gamma\gamma)$  categories have been removed as they show large overlap with the  $HH \rightarrow b\bar{b}\gamma\gamma$  categories
  - Also the impact on the combined limits of removing  $ttH(\gamma\gamma)$  categories is smaller w.r.t removing  $HH \rightarrow b\bar{b}\gamma\gamma$  categories

# Theory model and interpretation in the double-Higgs

- The double-Higgs production

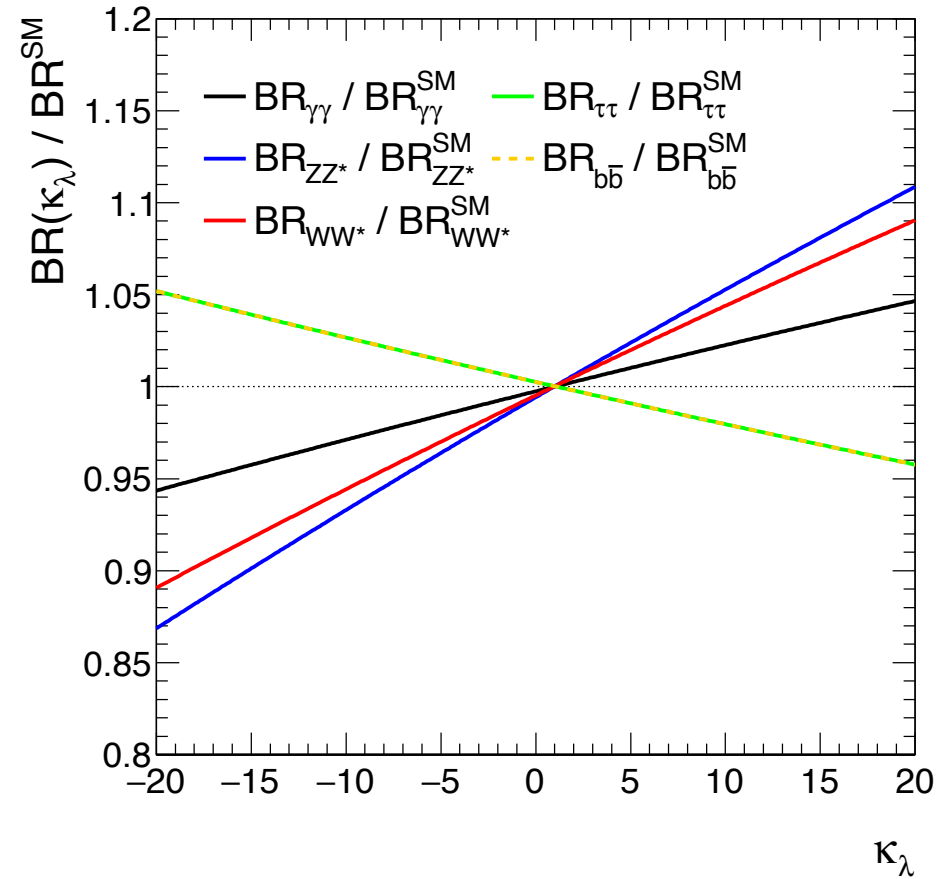
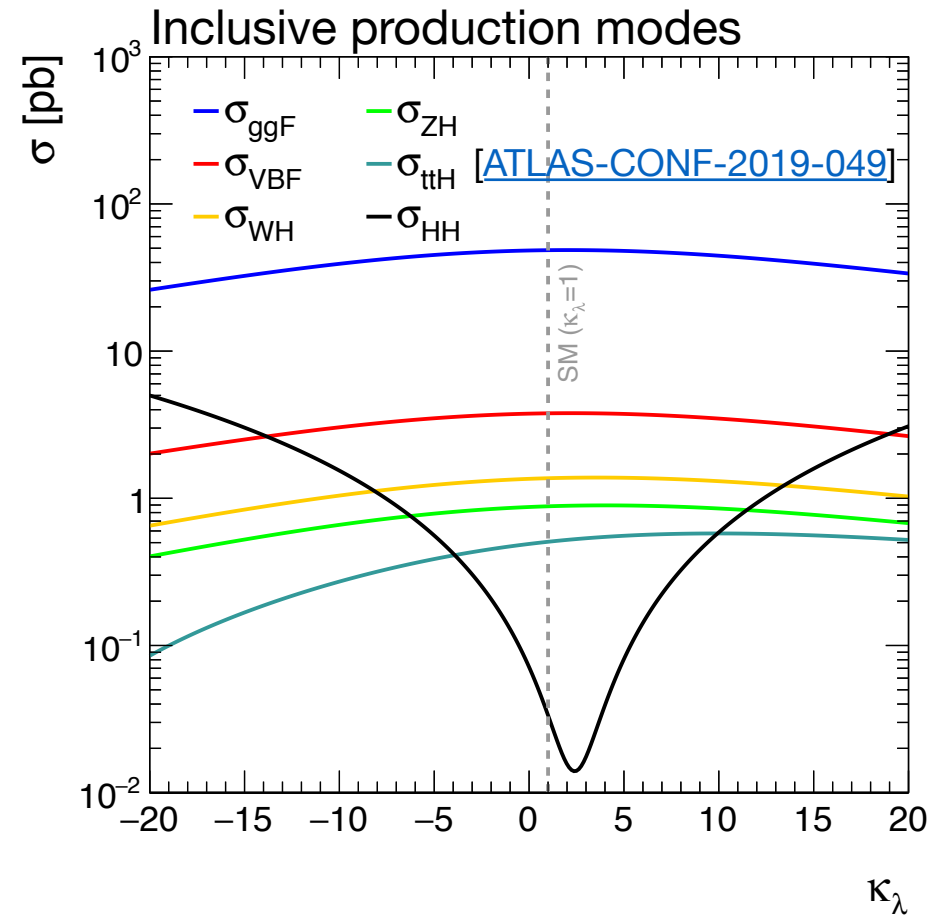


- The amplitude of the HH production can be parameterized as a function of ttH coupling  $\kappa_t = g_{ttH}/g_{ttH}^{SM}$  and HHH coupling  $\kappa_\lambda = g_{HHH}/g_{HHH}^{SM}$ 

$$A(\kappa_t, \kappa_\lambda) = \kappa_t^2 B + \kappa_t \kappa_\lambda T$$
- Omitting the integral on the final phase space and on the PDFs for simplicity
- $\sigma(pp \rightarrow HH) \sim \kappa_t^4 \left[ |B|^2 + \frac{\kappa_\lambda}{\kappa_t} (B^* T + T B^*) + \left( \frac{\kappa_\lambda}{\kappa_t} \right)^2 |T|^2 \right]$
- $\kappa_t^4$  appears in the normalization, the signal acceptance depends only from  $\kappa_\lambda/\kappa_t$
- When estimating  $\sigma(pp \rightarrow HH)$ , global normalization factors ( $\kappa_t^4$ ) don't play a role
  - $\Rightarrow$  HH-only measurement can't measure  $\kappa_\lambda$  and  $\kappa_t$  at the same time,  $\kappa_t$  is fixed to the SM in HH analysis alone

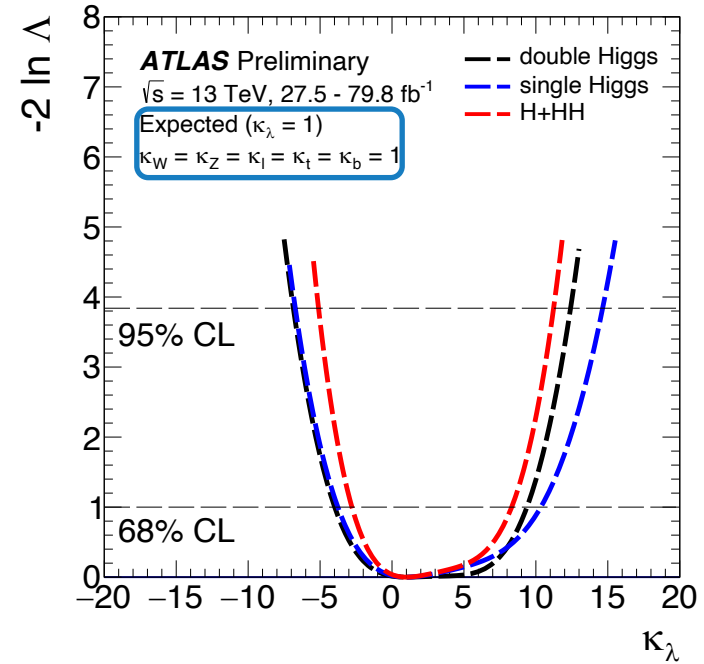
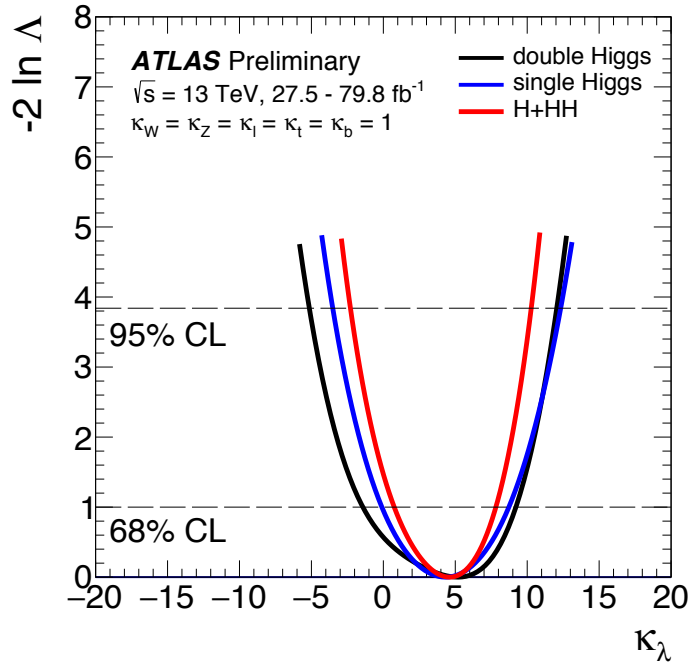
# Theoretical model and parameterization

- Parametrization of **single Higgs** is as before, and is used consistently in **double-Higgs analyses** for **single-Higgs backgrounds** and **Higgs decay branching ratios**



# $\kappa_\lambda$ -only results

- A likelihood fit is performed to constrain  $\kappa_\lambda$  in the combination of single-Higgs and double-Higgs
- All other Higgs boson couplings are fixed to the SM ( $\kappa_t = \kappa_b = \kappa_l = \kappa_W = \kappa_Z = 1$ )



- $\kappa_\lambda = 4.6_{-3.8}^{+3.2} = 4.6_{-3.5}^{+2.9}(\text{stat.})_{-1.2}^{+1.2}(\text{exp.})_{-0.5}^{+0.7}(\text{sig. th.})_{-1.0}^{+0.6}(\text{bkg. th.})$  (obs.)
- $\kappa_\lambda = 1.0_{-3.8}^{+7.3} = 1.0_{-3.0}^{+6.2}(\text{stat.})_{-1.7}^{+3.0}(\text{exp.})_{-1.2}^{+1.8}(\text{sig. th.})_{-1.1}^{+1.7}(\text{bkg. th.})$  (exp.)

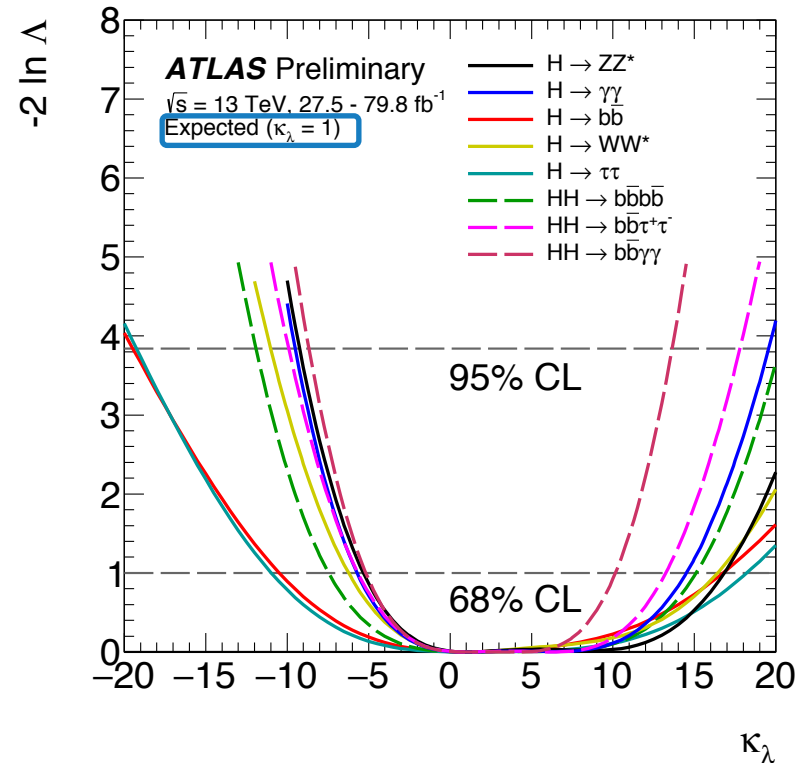
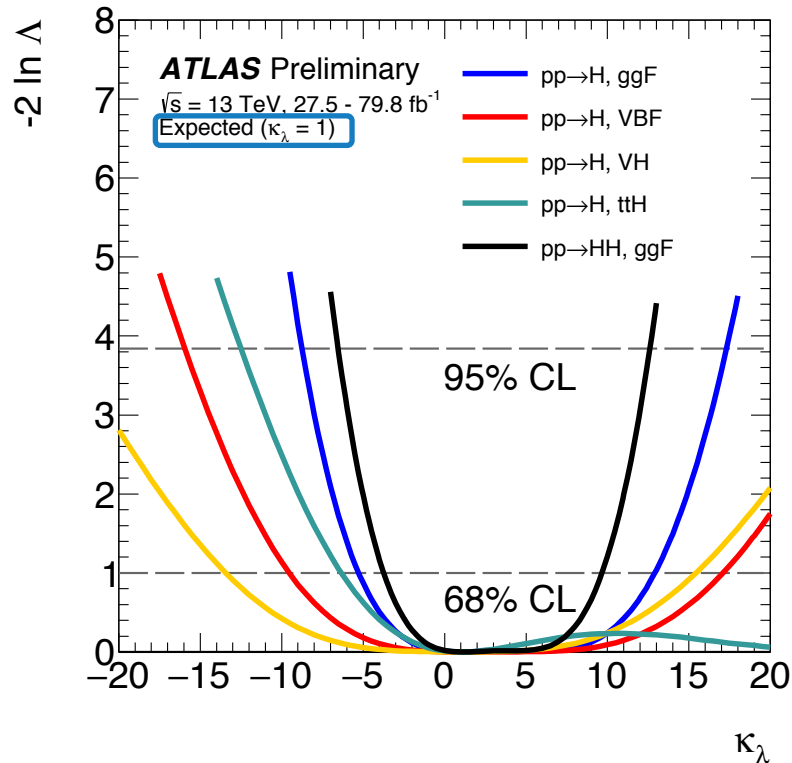
95% CL	Obs.	Exp.
H [ <a href="#">ATL-PHYS-PUB-2019-009</a> ]	[-3.2, 11.9]	[-6.2, 14.4]
HH [ <a href="#">arXiv:1906.02025</a> ]	[-5.0, 12.0]	[-5.8, 12.0]
H+HH [ <a href="#">ATLAS-CONF-2019-049</a> ]	[-2.3, 10.3]	[-5.1, 11.2]

- The combination can better constrain  $\kappa_\lambda$



# Higgs production/decay contributions

- Contributions from the different production and decay modes

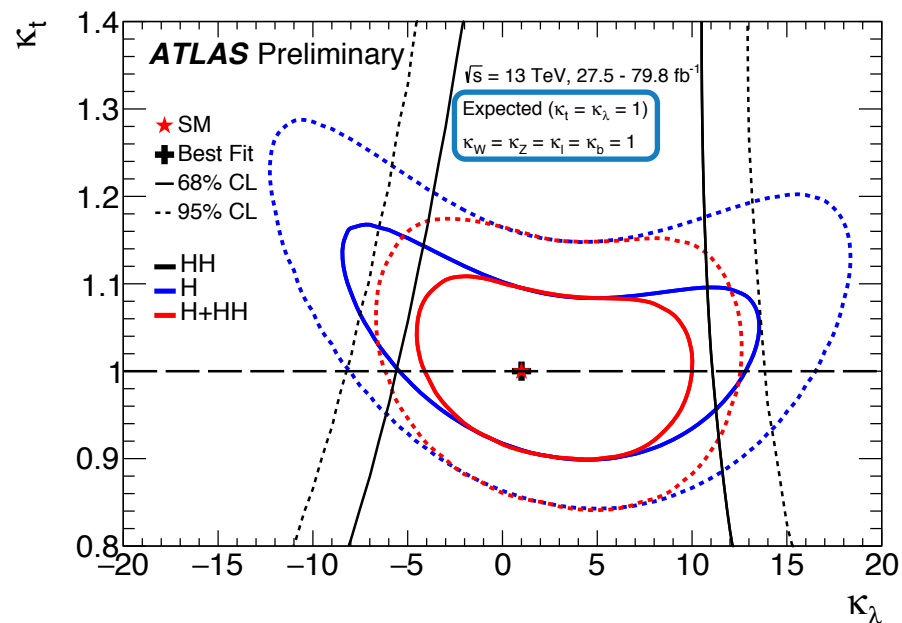
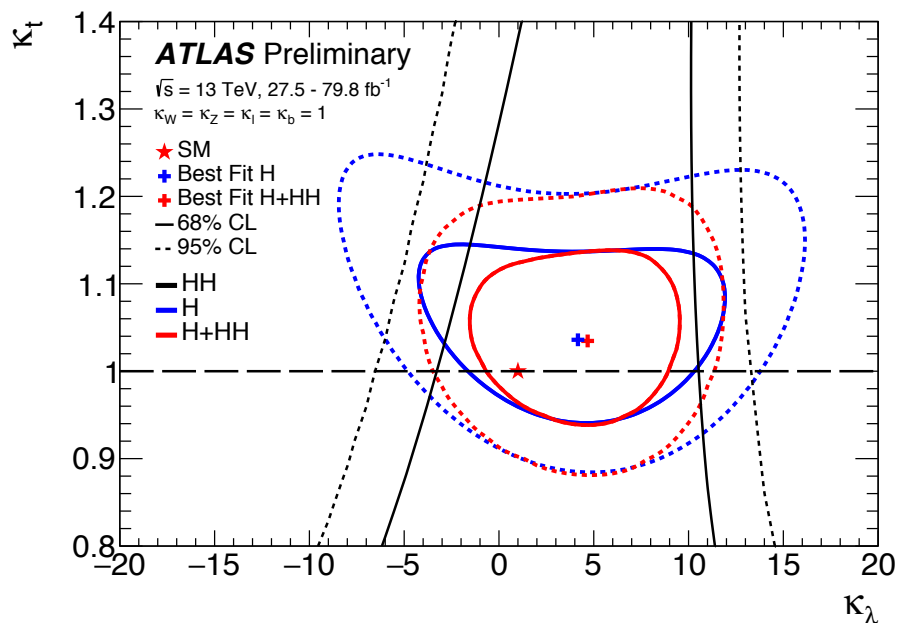


[ATLAS-CONF-2019-049]

- HH production is the most sensitive channel among all Higgs production processes, followed by ggF
- $\text{HH} \rightarrow b\bar{b}\gamma\gamma$ ,  $\text{HH} \rightarrow b\bar{b}\tau\tau$  give dominant contributions in constraining  $\kappa_\lambda$ , followed by  $H \rightarrow \gamma\gamma$

# $\kappa_\lambda - \kappa_t$ measurement

- By fitting together double-Higgs and single-Higgs,  $\kappa_\lambda$  and  $\kappa_t$  can be constrained at the same time

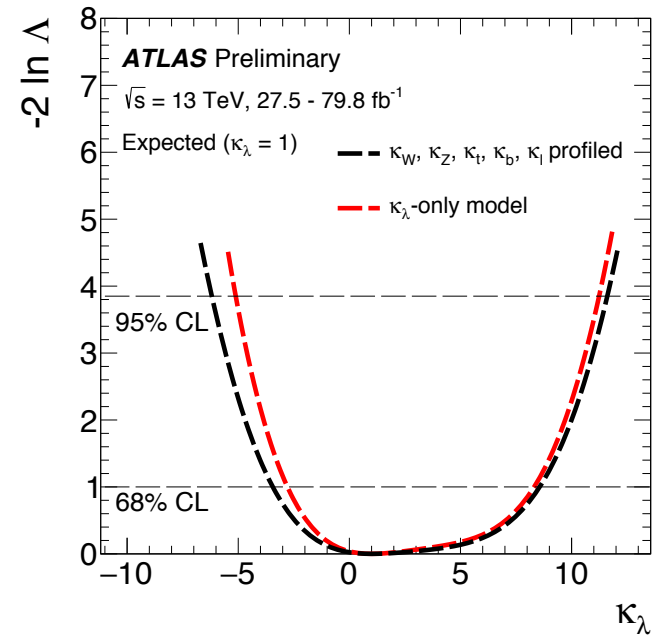
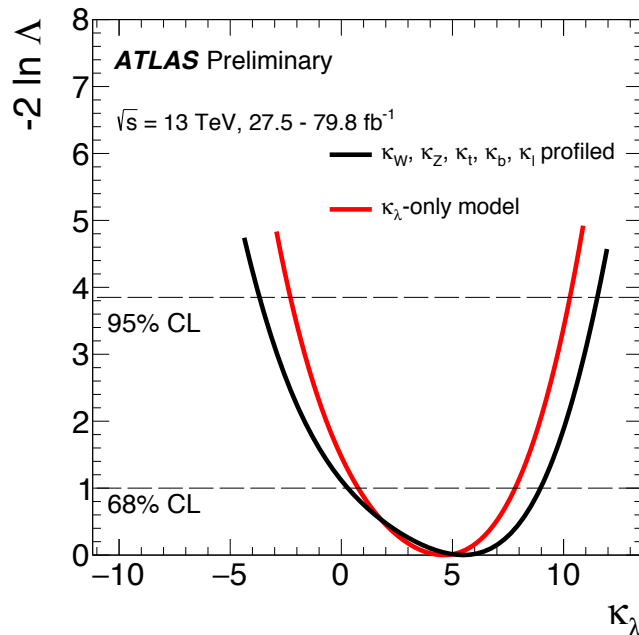


[ATLAS-CONF-2019-049]

- The **double-Higgs analysis alone** doesn't have sensitivity to constrain  $\kappa_\lambda$  and  $\kappa_t$  simultaneously

# Generic model

- To give the most generic measurement, a likelihood fit is performed to constrain simultaneously  $\kappa_\lambda$ ,  $\kappa_W$ ,  $\kappa_Z$ ,  $\kappa_t$ ,  $\kappa_b$  and  $\kappa_l$



[ATLAS-CONF-2019-049]

Model	$\kappa_W^{+1\sigma}_{-1\sigma}$	$\kappa_Z^{+1\sigma}_{-1\sigma}$	$\kappa_t^{+1\sigma}_{-1\sigma}$	$\kappa_b^{+1\sigma}_{-1\sigma}$	$\kappa_l^{+1\sigma}_{-1\sigma}$	$\kappa_\lambda^{+1\sigma}_{-1\sigma}$	$\kappa_\lambda$ [95% CL]	
$\kappa_\lambda$ -only	1	1	1	1	1	$4.6^{+3.2}_{-3.8}$	[-2.3, 10.3]	obs.
						$1.0^{+7.3}_{-3.8}$	[-5.1, 11.2]	exp.
Generic	$1.03^{+0.08}_{-0.08}$	$1.10^{+0.09}_{-0.09}$	$1.00^{+0.12}_{-0.11}$	$1.03^{+0.20}_{-0.18}$	$1.06^{+0.16}_{-0.16}$	$5.5^{+3.5}_{-5.2}$	[-3.7, 11.5]	obs.
	$1.00^{+0.08}_{-0.08}$	$1.00^{+0.08}_{-0.08}$	$1.00^{+0.12}_{-0.12}$	$1.00^{+0.21}_{-0.19}$	$1.00^{+0.16}_{-0.15}$	$1.0^{+7.6}_{-4.5}$	[-6.2, 11.6]	exp.

- Only the **single-Higgs and double-Higgs combination** could give enough sensitivity to exploit the generic model

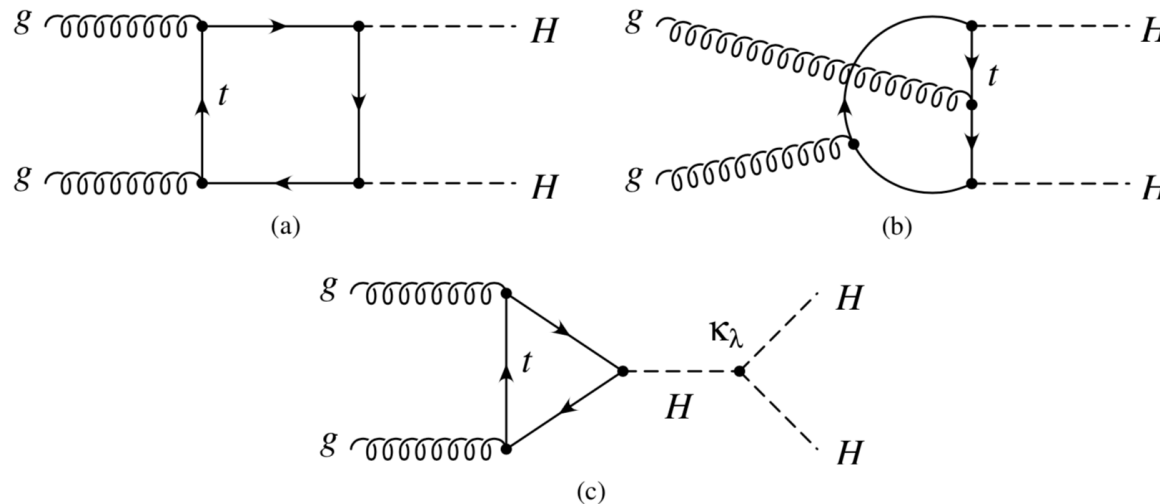
# Summary

- The **HH searches** (up to  $36.1 \text{ fb}^{-1}$ ) provide a unique chance to probe the Higgs self-coupling  $\kappa_\lambda = \lambda_{HHH}/\lambda_{SM}$  with **direct measurements**, the observed 95% CL is  $[-5.0, 12.0]$
- The **single-Higgs** analysis (up to  $80 \text{ fb}^{-1}$ ) shows that **an alternative and complementary approach** to constrain the Higgs self-coupling is feasible
- This approach can provide similar sensitivity w.r.t the double Higgs production, 95% CL:  $[-3.2, 11.9]$ , with other  $\kappa$  parameters fixed to the SM
- Furthermore,  $\kappa_\lambda$  has been constrained exploiting **the combination** of single-Higgs analyses and double-Higgs analyses
- The combination improves **the constraining power** on  $\kappa_\lambda$ , 95% CL:  $[-2.3, 10.3]$ , with other  $\kappa$  parameters fixed to the SM
- The combination can also **investigate other models** to which there is little sensitivity using just single-Higgs or double-Higgs measurements

# Backup

# Introduction about HH measurement

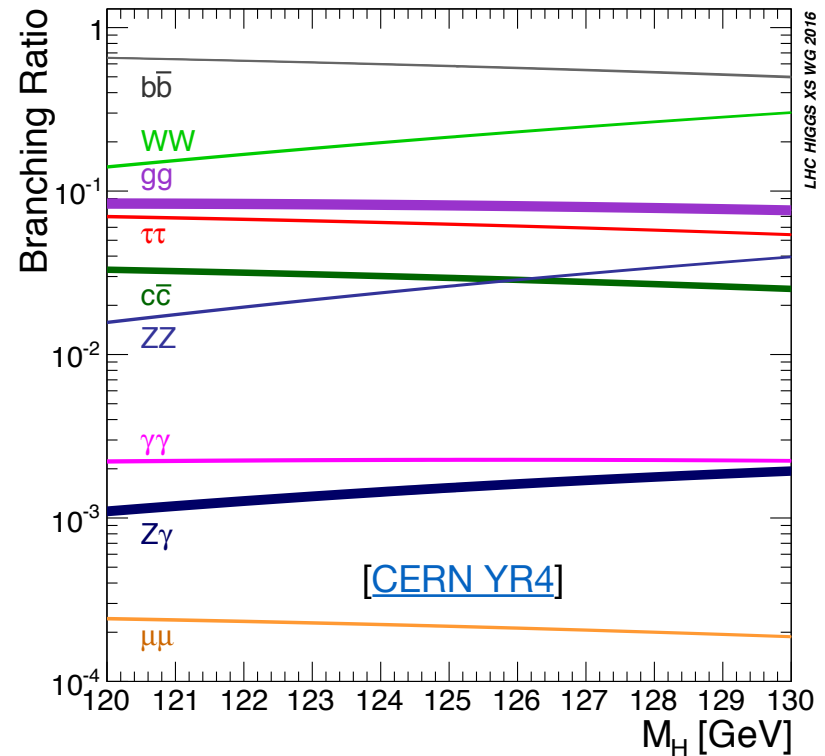
- During Run2 data taking, the Higgs production cross-sections and decays have been measured with an increasing precision
- The properties of the Higgs scalar potential, in particular the **Higgs boson self-coupling**, are still largely unconstrained
- The **non-resonant HH production** processes (ggF)
  - $\sigma^{SM}(pp \rightarrow HH, ggF)$ : 33.41 fb at NLO QCD correction with the full top-quark mass dependence



- The tree-level diagram is sensitive to the **Higgs boson trilinear self-coupling constant**  $\lambda_{HHH}$
- The HH searches provide a unique chance to probe it with **direct measurements**

# Input channels up to $36.1 \text{ fb}^{-1}$

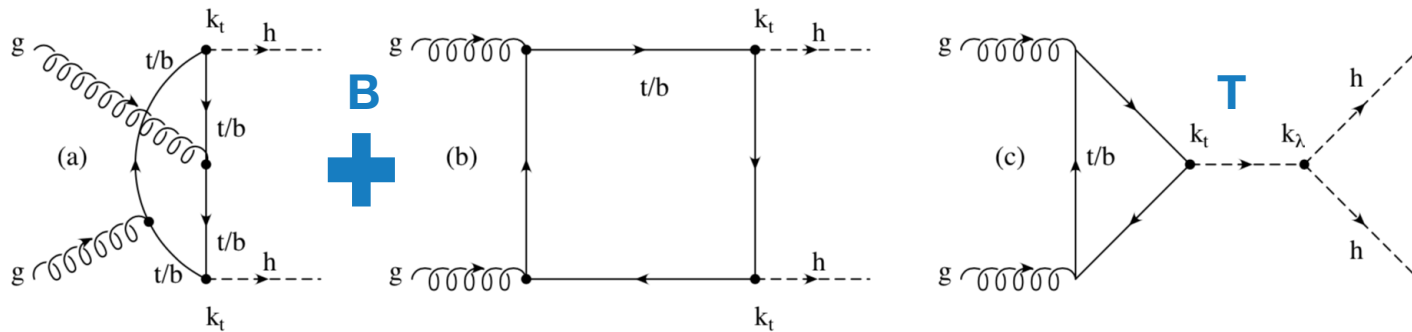
- **$bbbb$** : benefitting from the largest BR of  $H \rightarrow bb$
- **$bb\tau\tau$** : being large decay (BR  $\sim 7.5\%$ ) and with excellent background rejection from  $\tau$  performance
- **$bb\gamma\gamma$** : the best H resolution by  $H \rightarrow \gamma\gamma$



- Channels are either kept statistically orthogonal by event selection or have negligible overlap
- The rest HH channels have negligible contributions

# Theory model and interpretation

- The di-Higgs production



- The amplitude of the HH production can be parameterized as a function of ttH coupling  $k_t = g_{ttH}/g_{ttH}^{SM}$  and HHH coupling  $k_\lambda = g_{HHH}/g_{HHH}^{SM}$

$$A(k_t, k_\lambda) = k_t^2 B + k_t k_\lambda T$$

- Omitting the integral on the final phase space and on the PDFs for simplicity

$$\sigma(pp \rightarrow HH) \sim k_t^4 \left[ |B|^2 + \frac{k_\lambda}{k_t} (B^* T + T B^*) + \left( \frac{k_\lambda}{k_t} \right)^2 |T|^2 \right]$$

- The **signal acceptance** depends only from  $k_\lambda/k_t$

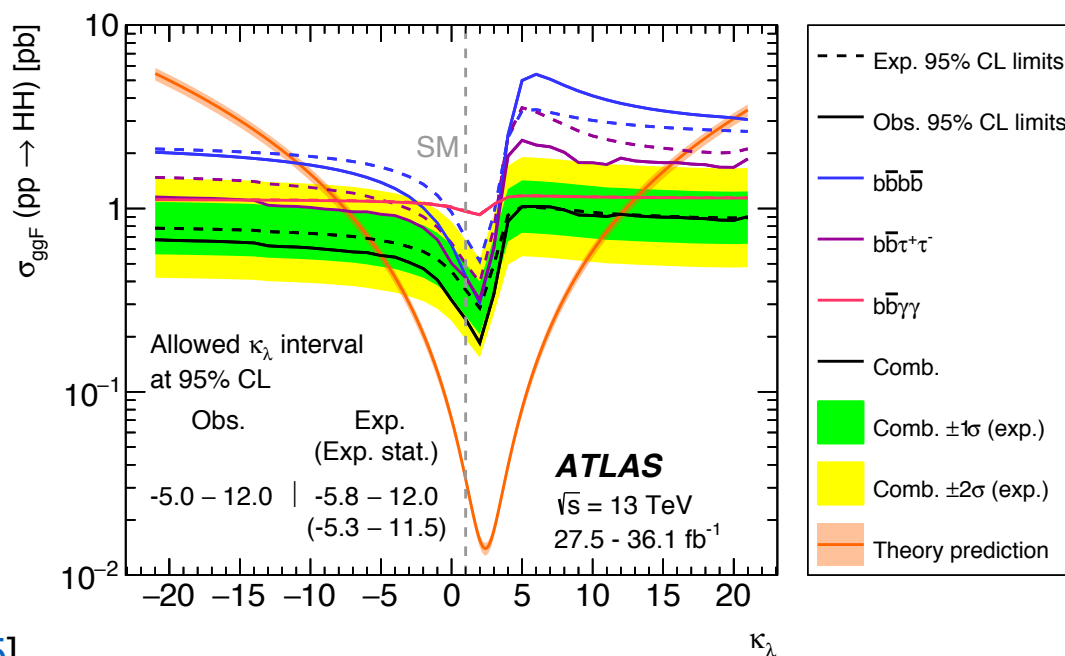
- When estimating upper limits on  $\sigma(pp \rightarrow HH)$  (POI), all global normalization factors ( $k_t^4$ ) don't play a role, the limit can be expressed as a function of  $k_\lambda/k_t$

- $\Rightarrow$  HH-only measurement can't measure  $k_\lambda$  and  $k_t$  at the same time



# Limits on the trilinear Higgs self-coupling

- With each  $k_\lambda$  assumption, estimate the upper limits of the **HH production** (assuming **SM H decay**) with **CLs approach**
- The limit curve is compared to the predicted cross section, from which **the constraint on  $k_\lambda$**  can be determined



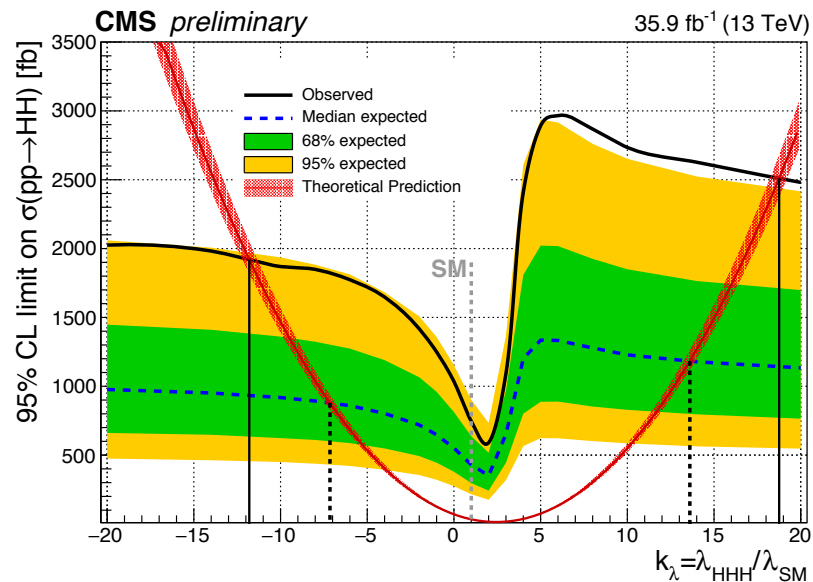
[[arXiv:1906.02025](https://arxiv.org/abs/1906.02025)]

Final state	Allowed $\kappa_\lambda$ interval at 95% CL		
	Obs.	Exp.	Exp. stat.
$b\bar{b}b\bar{b}$	-10.9 — 20.1	-11.6 — 18.8	-9.8 — 16.3
$b\bar{b}\tau^+\tau^-$	-7.4 — 15.7	-8.9 — 16.8	-7.8 — 15.5
$b\bar{b}\gamma\gamma$	-8.1 — 13.1	-8.1 — 13.1	-7.9 — 12.9
Combination	-5.0 — 12.0	-5.8 — 12.0	-5.3 — 11.5

# Combination of HH channels in CMS

- CMS combines Higgs boson pair productions with  $35.9 \text{ fb}^{-1}$  data collected in 2016
- Channel
  - $bb\gamma\gamma$ ,  $bb\tau\tau$ ,  $bbbb$ ,  $bbVV$  (additional channel w.r.t to the ATLAS measurement)
- A HH production scan is performed for different values of the  $k_\lambda$

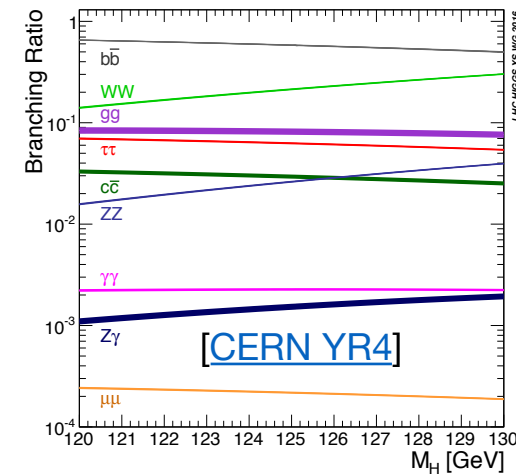
[CMS-PAS-HIG-17-030]



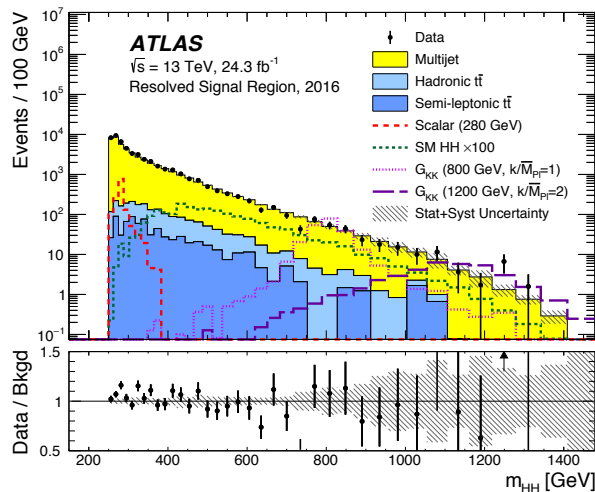
95% CL	Obs.	Exp.
ATLAS [arXiv:1906.02025]	[-5.0, 12.0]	[-5.8, 12.0]
CMS [CMS-PAS-HIG-17-030]	[-11.8, 18.8]	[-7.1, 13.6]

# Input channels up to 36.1 fb<sup>-1</sup>

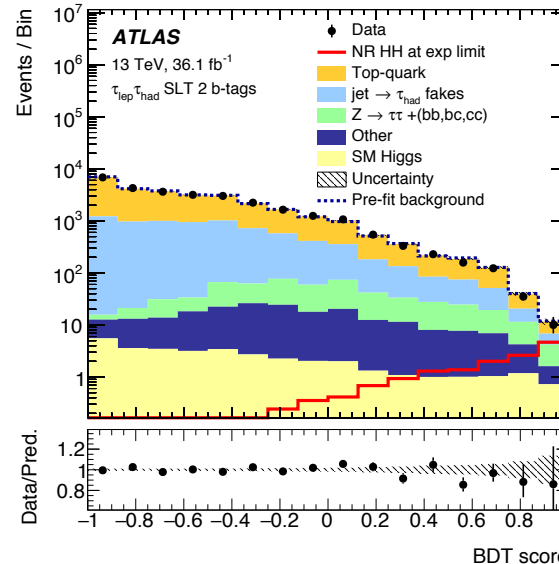
- *bbbb*: benefitting from the largest BR of  $H \rightarrow bb$
- *bb $\tau\tau$* : being large decay (BR  $\sim 7.5\%$ ) and with excellent background rejection from  $\tau$  performance
- *bb $\gamma\gamma$* : the best H resolution by  $H \rightarrow \gamma\gamma$
- The rest HH channels have negligible contributions



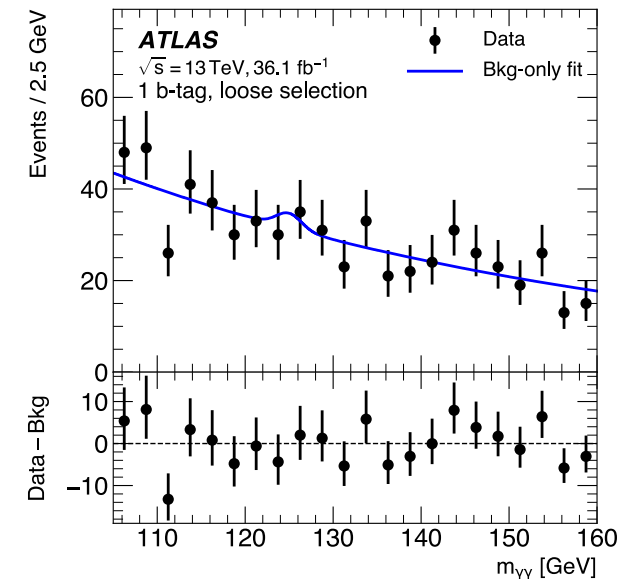
*bbbb*  
[arXiv:1804.06174]



*bb $\tau\tau$*   
[arXiv:1808.00336]



*bb $\gamma\gamma$*   
[arXiv:1807.04873]



- Channels are either kept statistically orthogonal by event selection or are checked to have negligible overlap

# Kinematical parameterization

- The linear combination method

- To avoid simulating a huge amount of events per  $k_\lambda$
- 3 basis amplitudes with certain  $k_\lambda$  LO samples can be linearly combined into an amplitude with any  $k_\lambda$  value

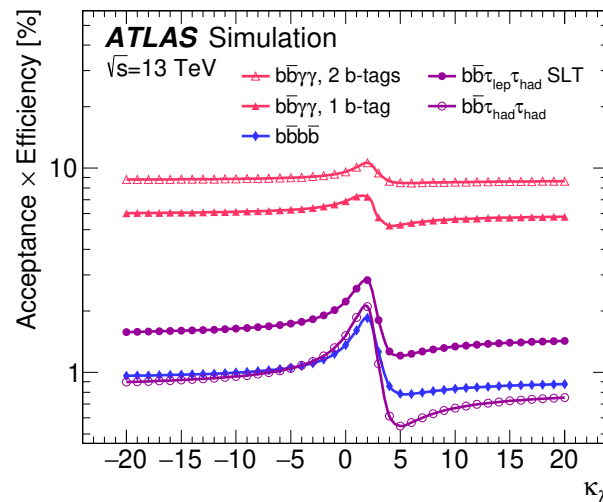
$$|A(k_t, k_\lambda)|^2 = k_t^2 \left[ \left( k_t^2 + \frac{k_\lambda^2}{20} - \frac{399}{380} k_t k_\lambda \right) |A(1,0)|^2 + \left( \frac{40}{38} k_t k_\lambda - \frac{2}{38} k_\lambda^2 \right) |A(1,1)|^2 + \frac{k_\lambda^2 - k_t k_\lambda}{380} |A(1,20)|^2 \right]$$

- $(k_t, k_\lambda) = \{(1,0), (1,1), (1,20)\}$  basis is less prone to statistical fluctuations for almost all  $k_\lambda$  points, due to higher number of events at low  $m_{HH}$ , coming from a softer  $m_{HH}^{k_\lambda=20}$  spectrum

- The  $k_\lambda$ -reweighting method (LO  $\rightarrow$  NLO)

- Ratios of the  $m_{HH}$  distributions for all  $k_\lambda$  values to the SM distribution are computed and then used to reweight the events of NLO SM HH signal samples
- The reweighted NLO signal sample is used to compute the signal acceptance and the kinematic distributions for different values of  $k_\lambda$

[[arXiv:1906.02025](https://arxiv.org/abs/1906.02025)]

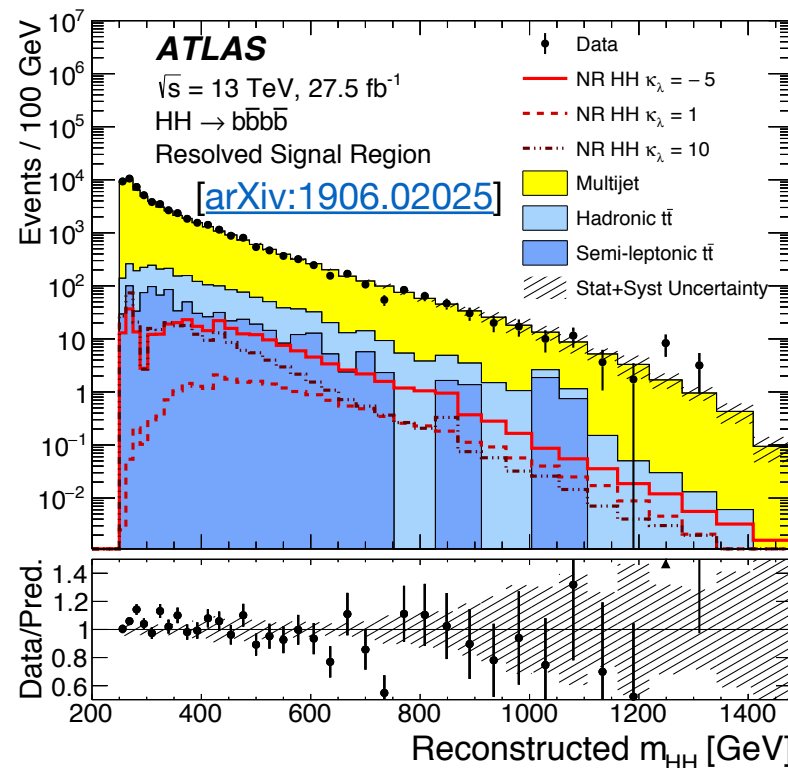


# BDT training strategies

- $k_\lambda = 20$  BDT performs better than the BDT when  $k_\lambda$  deviates from the SM expectation, as it is more sensitive to events in softer  $m_{HH}$  spectrum, while the loss in sensitivity around  $k_\lambda = 1$  is very small
- Thus the  $k_\lambda = 20$  BDT is used for all varied  $k_\lambda$  signals

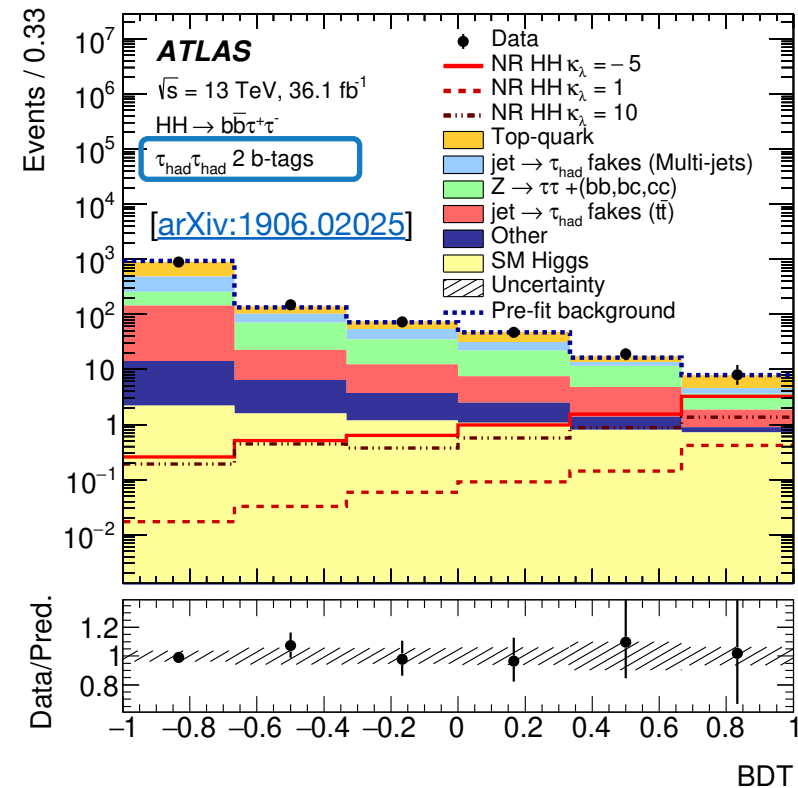
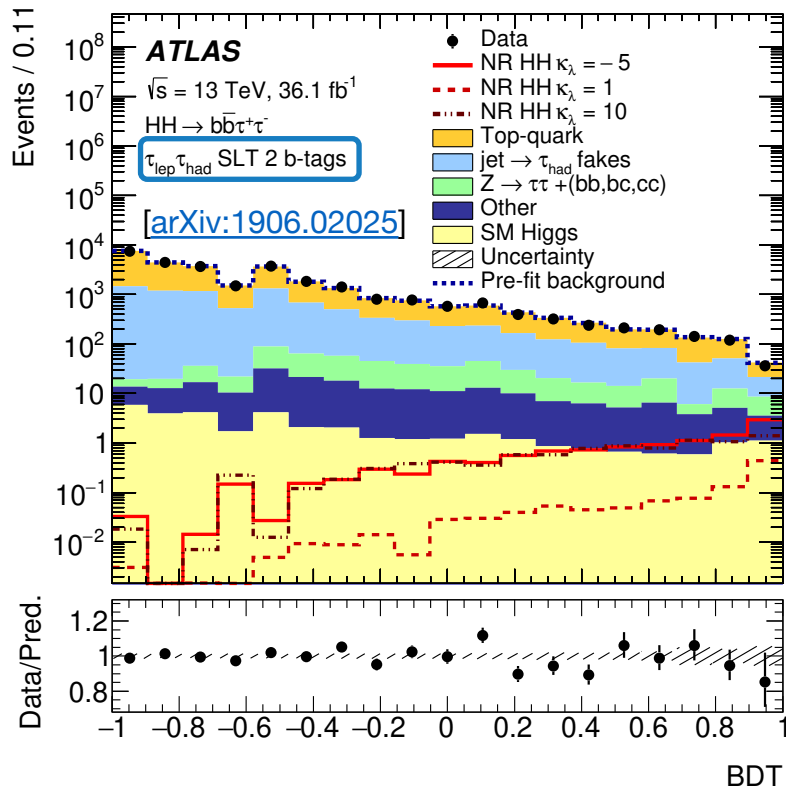
# Interpretation in the bbbb channel

- The **analysis selection** is the same of the non-resonant SM search and the same **final discriminant**, the reconstructed  $m_{HH}$  **distribution**, is used as a fit template [[arXiv:1804.06174](https://arxiv.org/abs/1804.06174)]
- The **signal model** is modified to take into account its dependence from  $k_\lambda$
- The **signal acceptance** varies by a factor 2.5 over the probed range of  $k_\lambda$  : [-20, 20]
- Both effects together determine how the exclusion limits on the **HH production cross-section** vary as a function of  $k_\lambda$



# Interpretation in the $bb\tau\tau$ channel

- Final states with two hadronic tau decays and with one leptonic and one hadronic tau decays are used
- The analysis uses a BDT discriminant trained using the re-weighted NLO signal sample corresponding to  $k_\lambda = 20$ , which shows good sensitivity over the whole range of probed  $k_\lambda$ -values:  $[-20, 20]$
- The sensitivity is also affected by the variation of the signal acceptance of a factor 3 over the probed range of  $k_\lambda$ -values



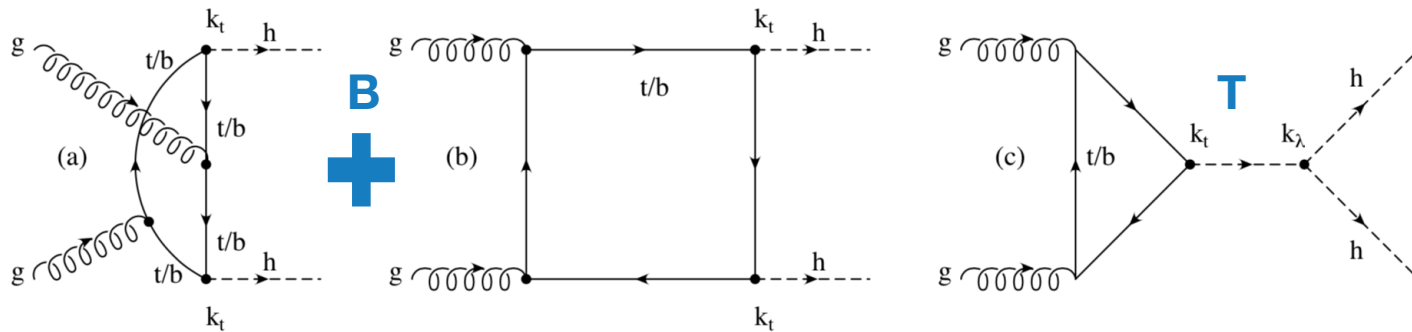
# Interpretation in the $b\bar{b}\gamma\gamma$ channel

- The **kinematic selection** used for the  $k_\lambda$ -scan uses **looser cuts on the  $b$ -jets  $p_T$**  than the selection used to look for the SM HH process [[arXiv:1807.04873](https://arxiv.org/abs/1807.04873)], because the average  $p_T^H$  is lower at large values of  $k_\lambda$
- The statistical analysis is performed using the  **$m_{\gamma\gamma}$  distribution** as the fit template
- The **signal acceptance** varies by about 30% over the probed range of  $k_\lambda$ -values:  $[-20, 20]$
- The **shape of the  $m_{\gamma\gamma}$**  remains independent of  $k_\lambda$ 
  - The  $m_{\gamma\gamma}$  dependence is examined by comparing the generated spectrum in simulation using **different  $k_\lambda$  values**
  - They agree well within statistical uncertainties
  - Furthermore, as the  $m_{\gamma\gamma}$  is modeled with DSCB,  **$\mu_{CB}$  and  $\sigma_{CB}$**  are extracted as a function of  $k_\lambda$
  - Both parameters are flat against  $k_\lambda$  variations in general



# Theory model and interpretation in the double-Higgs

- The di-Higgs production



- The amplitude of the HH production can be parameterized as a function of ttH coupling  $k_t = g_{ttH}/g_{ttH}^{SM}$  and HHH coupling  $k_\lambda = g_{HHH}/g_{HHH}^{SM}$

$$A(k_t, k_\lambda) = k_t^2 B + k_t k_\lambda T$$

- Omitting the integral on the final phase space and on the PDFs for simplicity
- $\sigma(pp \rightarrow HH) \sim k_t^4 \left[ |B|^2 + \frac{k_\lambda}{k_t} (B^* T + T B^*) + \left( \frac{k_\lambda}{k_t} \right)^2 |T|^2 \right] (bb\gamma\gamma)$
- 3 basis amplitudes with certain  $k_\lambda$  samples  $(k_t, k_\lambda) = \{(1,0), (1,1), (1,20)\}$  can be linearly combined into an amplitude with any  $k_\lambda$  value
- $|A(k_t, k_\lambda)|^2 = k_t^2 \left[ \left( k_t^2 + \frac{k_\lambda^2}{20} - \frac{399}{380} k_t k_\lambda \right) |A(1,0)|^2 + \left( \frac{40}{38} k_t k_\lambda - \frac{2}{38} k_\lambda^2 \right) |A(1,1)|^2 + \frac{k_\lambda^2 - k_t k_\lambda}{380} |A(1,20)|^2 \right] (bbbb, bb\tau\tau)$

# Systematic uncertainties

- Experimental systematic uncertainty
  - With the recommendation of CP groups, the uncertainty sources are correlated by sharing the same NP across the channels
- Background uncertainty
  - The uncertainties (modeling and rates) are **not correlated** given different phase space and evaluation methods
- Theoretical uncertainty
  - The uncertainties on **signal acceptances are correlated**
  - They are from renormalization and factorization scales, PS as well as PDF sets

# POI and uncertainties

- POI:  $\sigma(pp \rightarrow HH)$ , assuming SM branching fractions
- Detector systematic uncertainties
  - Jet reconstruction, b-jet tagging, electron, muon and photon reconstruction and identification, as well as the uncertainty of the integrated luminosity are **correlated**
- Theory uncertainties in the signal acceptance
  - QCD scales, PDFs and PS are **correlated**
- Theoretical and modelling systematic uncertainties of the backgrounds are not correlated
  - There is a negligible overlap among these background contributions to the different analyses

- The **predicted HH cross section** is scaled by a factor as a function of  $k_\lambda$ 
  - The factor is calculated by **non-SM-lambda xs over SM-lambda xs** ( $k_\lambda = 1$ ) at NNLO+NNLL from [YR4](#)

# Event kinematic information

- Re-deriving the kinematic dependent coefficients  $C_1^i$

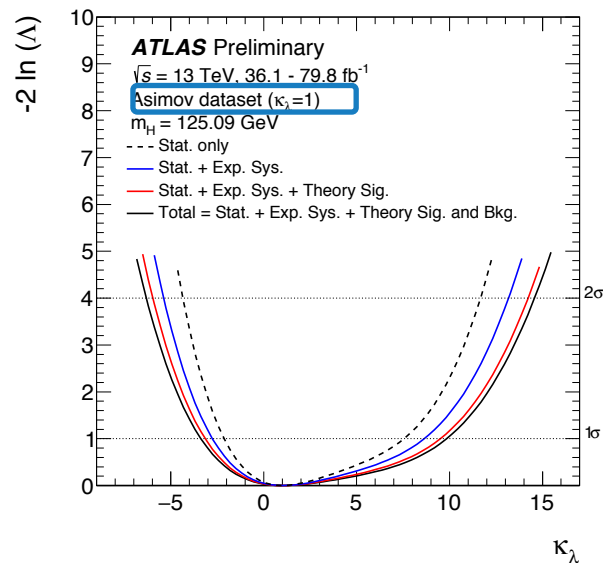
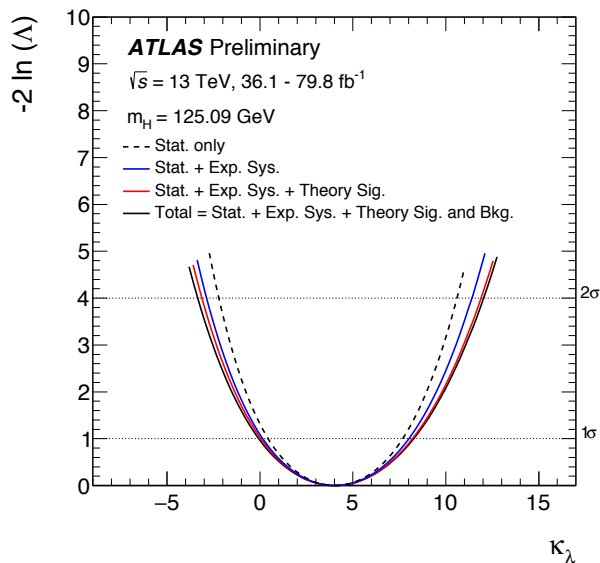
[ATL-PHYS-PUB-2019-009]

STXS region		VBF	WH	ZH
		$C_1^i \times 100$		
VBF + V(had)H	VBF-cuts + $p_T^{j1} < 200$ GeV, $\leq 2j$	0.63	0.91	1.07
	VBF-cuts + $p_T^{j1} < 200$ GeV, $\geq 3j$	0.61	0.85	1.04
	VH-cuts + $p_T^{j1} < 200$ GeV	0.64	0.89	1.10
	no VBF/VH-cuts, $p_T^{j1} < 200$ GeV	0.65	1.13	1.28
	$p_T^{j1} > 200$ GeV	0.39	0.23	0.28
$qq \rightarrow H\ell\nu$	$p_T^V < 150$ GeV		1.15	
	$150 < p_T^V < 250$ GeV, $0j$		0.18	
	$150 < p_T^V < 250$ GeV, $\geq 1j$		0.33	
	$p_T^V > 250$ GeV		0	
$qq \rightarrow H\ell\ell$	$p_T^V < 150$ GeV			1.33
	$150 < p_T^V < 250$ GeV, $0j$			0.20
	$150 < p_T^V < 250$ GeV, $\geq 1j$			0.39
$qq \rightarrow H\nu\nu$	$p_T^V > 250$ GeV			0

- In the phase space where  $K_{EW}^i$  corrections are most significant ( $\sim 15\%$  variations for high  $p_T^H$ ), the sensitivity to the Higgs boson trilinear coupling is minimal
  - It's assumed to be constant to the inclusive values
  - A test has been performed using different  $K_{EW}$  for each STXS bin
  - The fit results with the new  $K_{EW}$  configuration differ by less than percent level w.r.t the nominal results
- The selection efficiency can also depend on  $k_\lambda$ , the effect has been tested using MC samples
  - In general, a negligible dependence is found

# $k_\lambda$ -only results

- A likelihood fit is performed to constrain the Higgs boson self-coupling  $k_\lambda$ 
  - Theory validity range [arXiv: 1607.04251]:  $-20 < k_\lambda < 20$



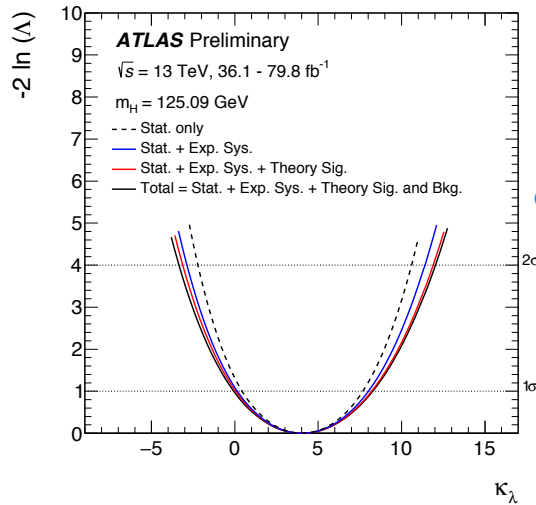
$$k_\lambda = 4.0_{-4.1}^{+4.3} = 4.0_{-3.6}^{+3.7}(\text{stat.})_{-1.5}^{+1.6}(\text{exp.})_{-0.9}^{+1.3}(\text{sig. th.})_{-0.9}^{+0.8}(\text{bkg. th.})$$

95% CL	Obs.	Exp.
H [ATL-PHYS-PUB-2019-009]	[-3.2, 11.9]	[-6.2, 14.4]
HH [arXiv:1906.02025]	[-5.0, 12.0]	[-5.8, 12.0]

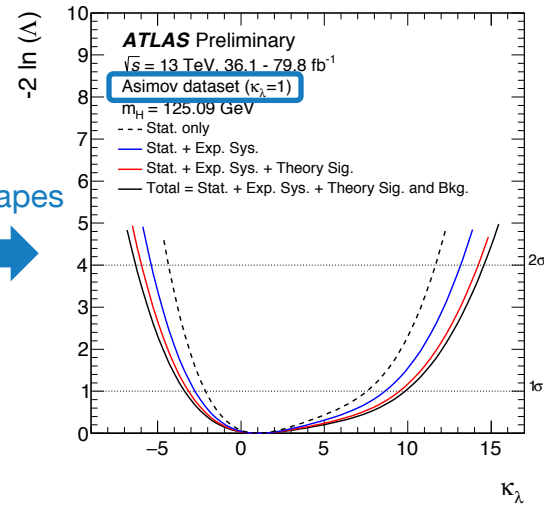
- The impact on the  $k_\lambda$  by using an inclusive cross-section measurement has been studied, where the VBF, WH and ZH are considered as single inclusive bins
- The inclusive fit does not lead to a significant loss in sensitivity to  $k_\lambda$

POIs	Granularity	$\kappa_F^{+1\sigma}_{-1\sigma}$	$\kappa_V^{+1\sigma}_{-1\sigma}$	$\kappa_\lambda^{+1\sigma}_{-1\sigma}$	$\kappa_\lambda$ [95% C.L.]
$\kappa_\lambda$	STXS	1	1	$4.0_{-4.1}^{+4.3}$ $1.0_{-4.4}^{+8.8}$	[-3.2, 11.9] [-6.2, 14.4]
	inclusive	1	1	$4.6_{-4.2}^{+4.3}$ $1.0_{-4.3}^{+9.5}$	[-2.9, 12.5] [-6.1, 15.0]

# Likelihood comparison



different likelihood shapes

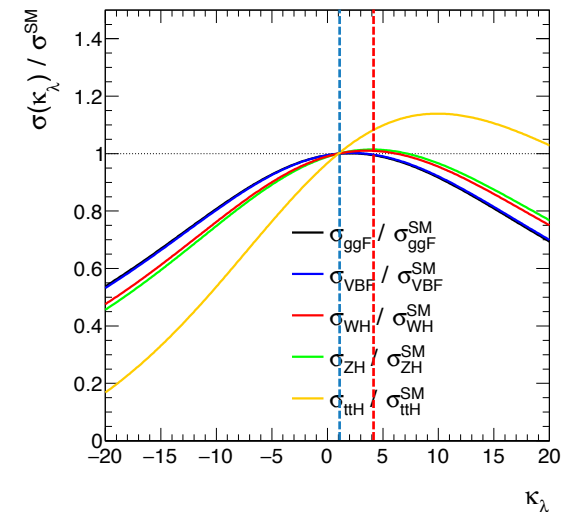


## Explanation

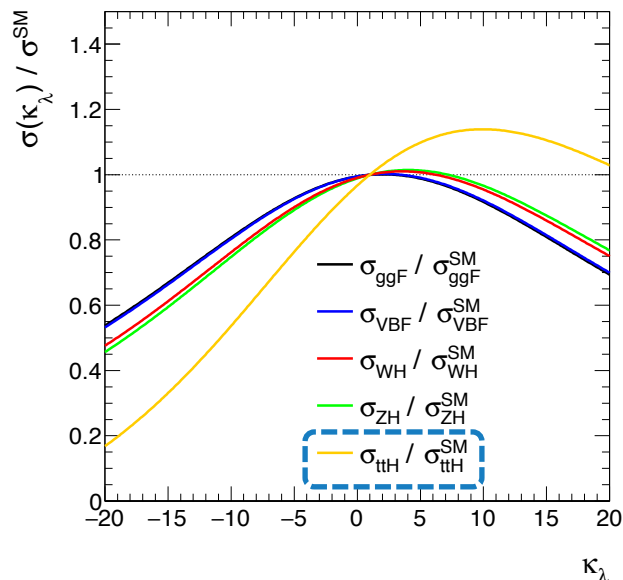
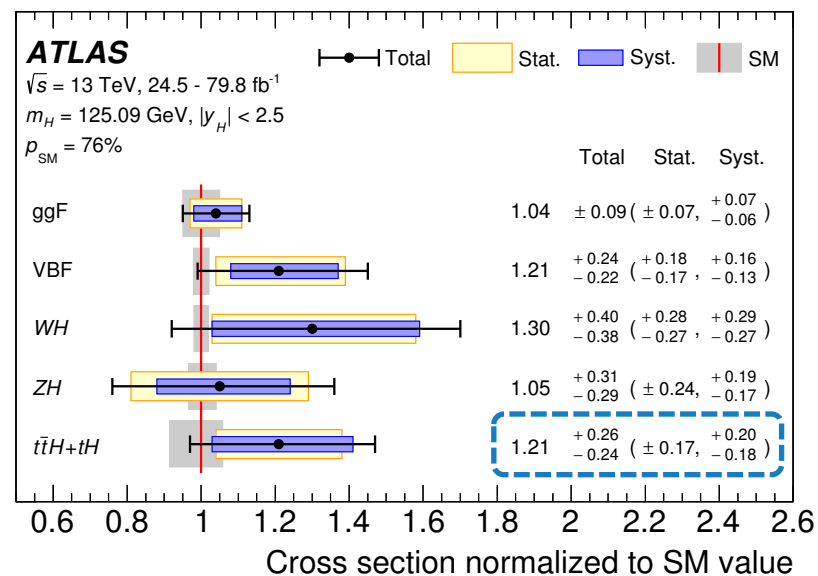
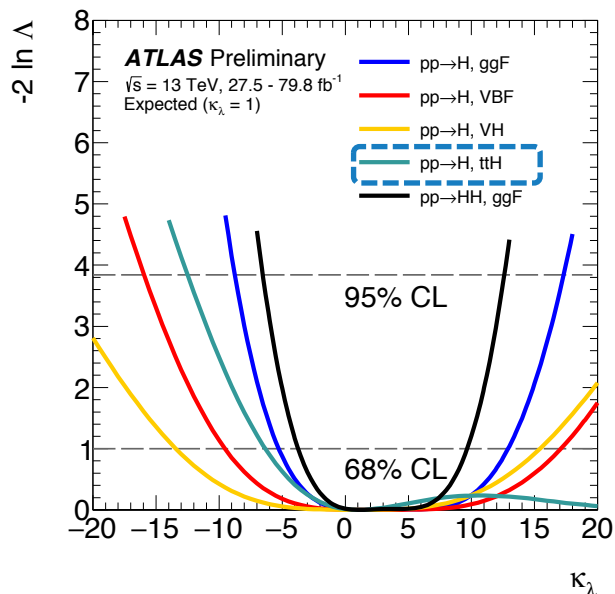
1. The non-linearity of the cross-section dependence from  $k_\lambda$
2. The difference of the best-fit values of  $k_\lambda$

$$\mu_i(k_\lambda, k_i) = \frac{1}{1 - (k_\lambda^2 - 1)\delta Z_H} \left[ k_i^2 + \frac{(k_\lambda - 1)C_1^i}{K_{EW}^i} \right]$$

- The shape is affected by the different behavior of the quadratic and linear  $k_\lambda$  dependent terms
  - If  $k_\lambda < 1$  both terms induce a reduction of the Higgs boson production cross-sections
  - While for  $k_\lambda > 1$  there are larger cancellations that weaken the cross-section dependence



# The observed $\sigma_{ggF}, \sigma_{ttH}$



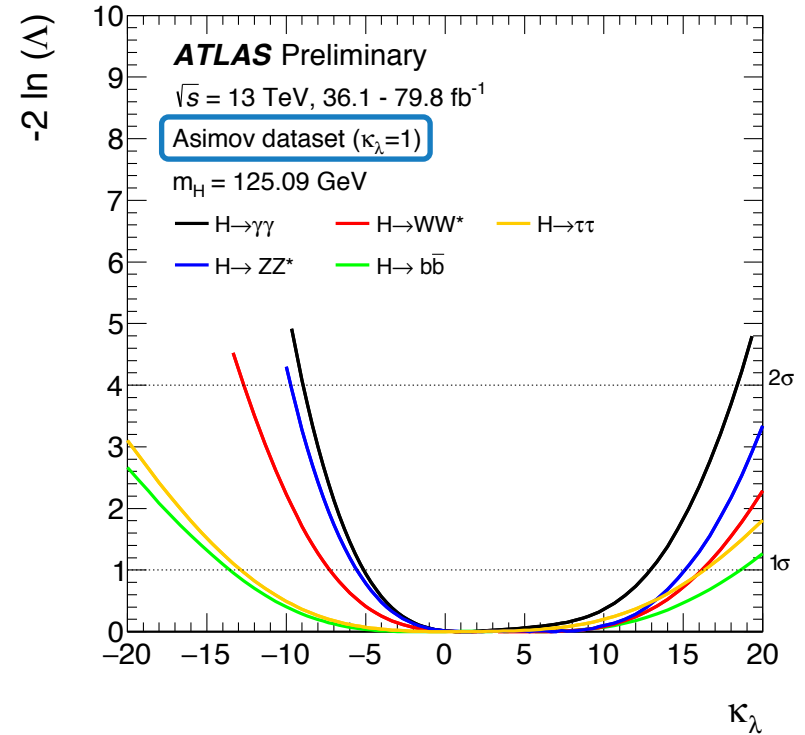
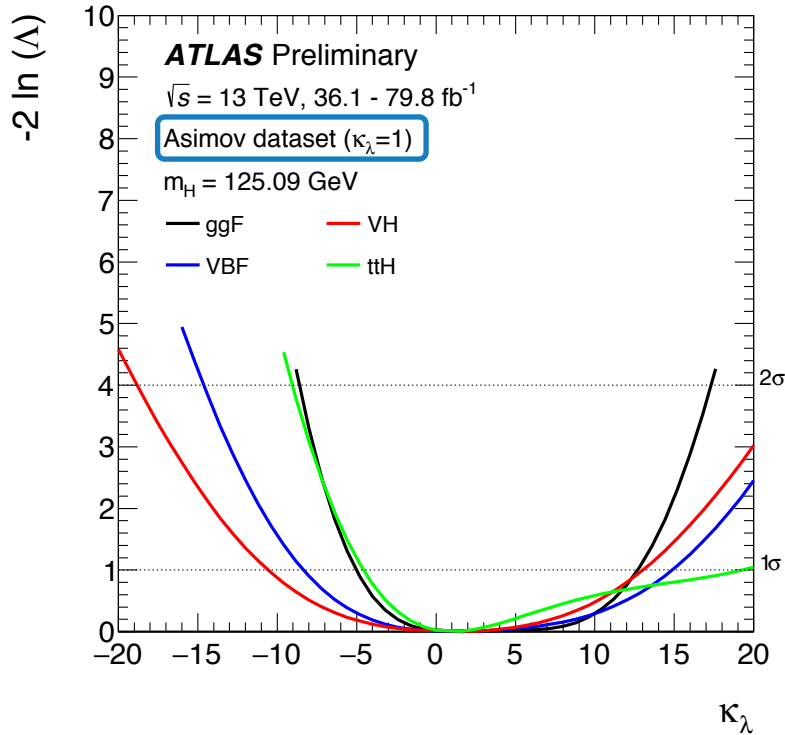
- $ggF, ttH$  are sensitive for measuring  $k_\lambda$
- The measured  $\sigma_{ggF}, \sigma_{ttH+tH}$  is greater SM
- To get higher  $\sigma_{ggF}, \sigma_{ttH}$ ,  $k_\lambda$  has to be greater than the SM



# The sensitivity of different productions and decays

- Moreover, the global likelihood shape depends on combining the different production and decays, which have different sensitivities and significantly different likelihood shapes

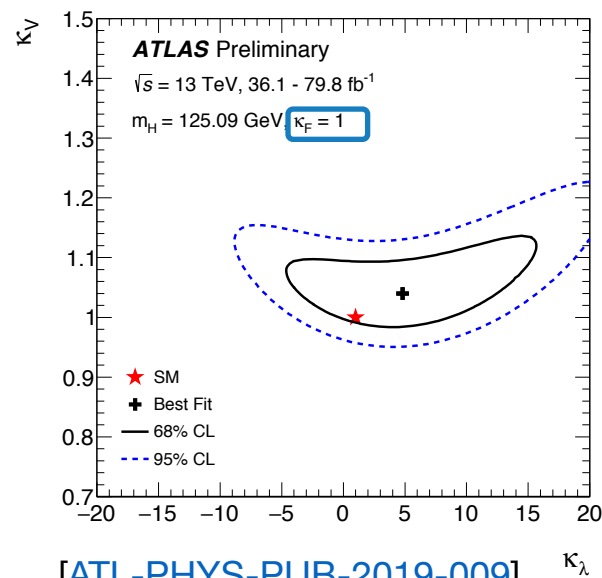
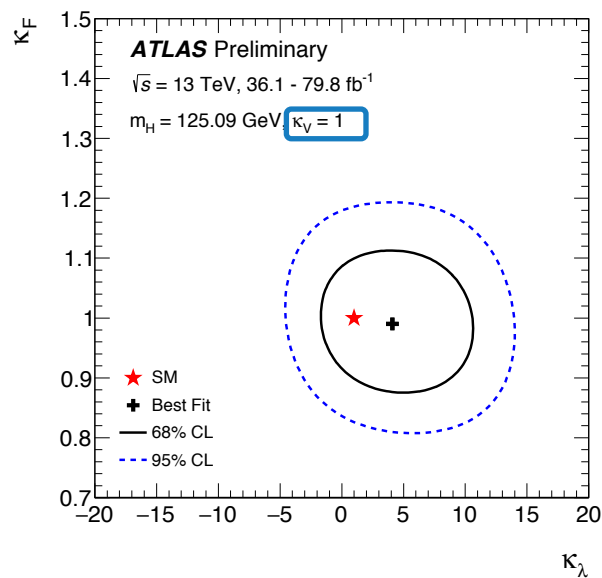
[ATL-PHYS-PUB-2019-009]



- The dominant contributions derive from the di-boson decays  $\gamma\gamma$ ,  $ZZ^*$ ,  $WW^*$  and from the ggF and ttH productions

# $k_\lambda$ and $k_F$ , $k_\lambda$ and $k_V$ fits

- A simultaneous fit is performed to  $k_\lambda$  and  $k_F$  ( $k_V = 1$ ),  $k_\lambda$  and  $k_V$  ( $k_F = 1$ )
- These fits target BSM scenarios where new physics could affect only the Yukawa type terms ( $k_V = 1$ ) or only the couplings to vector bosons ( $k_F = 1$ ), in addition to the Higgs boson self-coupling ( $k_\lambda$ )



[ATL-PHYS-PUB-2019-009]

- The sensitivity to  $k_\lambda$  is not much degraded when determining  $k_F$  at the same time
- While it's degraded by 50% when determining  $k_V$  simultaneously
- An even less constrained fit, by either fitting simultaneously  $k_\lambda$ ,  $k_V$  and  $k_F$ , or fitting simultaneously  $k_\lambda$  and a common coupling modifier ( $k = k_V = k_F$ ), results in nearly no sensitivity to  $k_\lambda$

POIs	Granularity	$k_F^{+1\sigma}_{-1\sigma}$	$k_V^{+1\sigma}_{-1\sigma}$	$k_\lambda^{+1\sigma}_{-1\sigma}$	$k_\lambda$ [95% C.L.]
$k_\lambda$	STXS	1	1	$4.0^{+4.3}_{-4.1}$	[-3.2, 11.9]
				$1.0^{+8.8}_{-4.4}$	[-6.2, 14.4]
$k_\lambda$	inclusive	1	1	$4.6^{+4.3}_{-4.2}$	[-2.9, 12.5]
				$1.0^{+9.5}_{-4.3}$	[-6.1, 15.0]
$k_\lambda, k_V$	STXS	1	$1.04^{+0.05}_{-0.04}$	$4.8^{+7.4}_{-6.7}$	[-6.7, 18.4]
			$1.00^{+0.05}_{-0.04}$	$1.0^{+9.9}_{-6.1}$	[-9.4, 18.9]
$k_\lambda, k_F$	STXS	$0.99^{+0.08}_{-0.08}$	1	$4.1^{+4.3}_{-4.1}$	[-3.2, 11.9]
		$1.00^{+0.08}_{-0.08}$		$1.0^{+8.8}_{-4.4}$	[-6.3, 14.4]

# Multiplicative approach in the Higgs production parameterization

- Additional cross-check about  $k_\lambda$  interpretation in the **Higgs productions**

$$\mu_i(k_\lambda, k_i) = Z_H^{BSM}(k_\lambda) \left[ k_i^2 + \frac{(k_\lambda - 1)C_1^i}{K_{EW}^i} \right]$$

- **Multiplicative approach:**  $k_i$  can also modifies the **loops together with  $k_\lambda$**  to verify the robustness of the nominal approach against **higher-order terms**

$$\mu_i(k_\lambda, k_i) = Z_H^{BSM}(k_\lambda) \left[ k_i^2 + \frac{(k_\lambda k_i^3 - 1)C_1^i}{K_{EW}^i} \right]$$

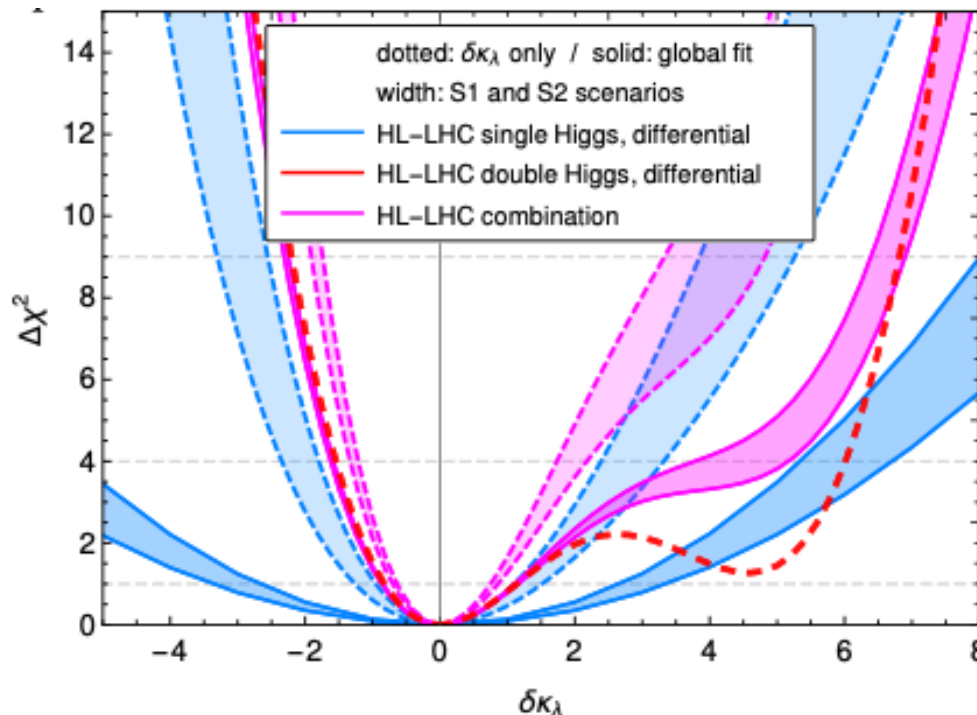
- $k_\lambda$  **measurements** have been performed comparing the **nominal results** and the ones using this **additional configuration**
- **Negligible discrepancies** w.r.t the uncertainty of the nominal measurement have been found

- *bbγγ*: no signal sample is used
- The **analysis acceptance** depends on  $k_\lambda/k_t$  and has been implemented

# Systematic correlations

- The principles for making **systematic uncertainties correlations**
  - Correlate **CP uncertainties** where possible
  - Correlate **theory signal uncertainties** where possible
  - Uncorrelate uncertainties **in different releases**
  - Uncorrelate **background uncertainties** due to different phase spaces in different analyses
  
- Only  $\sim 50$  NPs need to be studied and correlated

- **HH** currently are very limited by statistics also in its systematic uncertainties (eg. bkg systematics), therefore at HL they can gain a lot in sensitivity
- The gain for **SH** is not so enhanced by the increasing of luminosity since at a certain point it becomes limited by systematic uncertainties, that in the HL projection are not so much reduced
- The HL-LHC report that the combination of HH with H brings little additional constraint on the HH constraints alone seems to be a little excessive (especially considering the 2 sigma line)



Higgs Physics at the HL-LHC and HE-LHC: [arXiv:1902.00134](https://arxiv.org/abs/1902.00134)

- Htautau
- [https://gitlab.cern.ch/atlas\\_higgs\\_combination/projects/HiggsCouplingProspectCombSummer2018/blob/master/WS\\_300/Reduced/Htautau/HLLHCred300mu\\_125.root](https://gitlab.cern.ch/atlas_higgs_combination/projects/HiggsCouplingProspectCombSummer2018/blob/master/WS_300/Reduced/Htautau/HLLHCred300mu_125.root)

```

RooProduct::WH125_Htt_yearAll_chanhh_catboostloose_regsig_selCBA_overallNorm_x_sigma_epsilon[ SigXsecOverSM * Mu_VBF_tautau * Mu_VH_tautau *
XS13_WH_tautau * oneover_XS13_WH * oneover_BR_tautau * lumi_1516 * oneover_lumi_1516 *
WH125_Htt_yearAll_chanhh_catboostloose_regsig_selCBA_epsilon ] = 1.00001

```

- All WH, ZH categories have “Mu\_VBF\_tautau \* Mu\_VH\_tautau” handlers
- And there is no WH, ZH POIs (i.e Mu\_WH\_tautau, Mu\_ZH\_tautau)
- Would it possible to remove Mu\_VBF\_tautau and add WH, ZH POIs in it?

```

RooProduct::ttH125_Htt_yearAll_chanhh_catboostloose_regsig_selCBA_overallNorm_x_sigma_epsilon[ SigXsecOverSM * Mu_gg2H_tautau *
Mu_ttH_tautau * XS13_ttH * oneover_XS13_ttH * lumi_1516 * oneover_lumi_1516 * ttH125_Htt_yearAll_chanhh_catboostloose_regsig_selCBA_epsilon
] = 1

```

- All ttH categories have “Mu\_gg2H\_tautau \* Mu\_ttH\_tautau” handlers
- Would it possible take Mu\_gg2H\_tautau out?
- Currently we can only use Mu\_gg2H\_tautau and Mu\_VBF\_tautau in the Htautau workspace