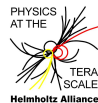


Quantum Chromodynamics

... at the LHC and elsewhere ...

Thomas Schörner-Sadenius



Introductory School to Terascale Physics
DESY Hamburg, 10 March 2010



OUTLINE

- > Basics of Quantum Chromodynamics (QCD)
 - Particles, interactions, Feynman diagrams
 - A bit of history, and some salient features
- > Parton Distribution Functions (veeeery briefly)
 - Factorisation, and QCD processes at the LHC (hadron colliders)
- > Particle production
 - Spectra, multiplicities, identified particles, etc.
- > Jets as probes of hard interactions
 - Jet algorithms
 - Measurements in ee, at HERA, Tevatron and LHC
 - Extractions of α_s
- > The Underlying Event
 - ... just one slide

THE PATH TO QCD – HISTORY (1)

> Early classifications of particles (`particle zoo')

- Based on charge, spin, isospin (Heisenberg et al.: SU(2)-based theories, grouping for example proton and neutron together ...)
- `Invention' of `quarks' as building blocks of hadrons by Gell-Man, Zweig: up, down (strange), ...

> Parallel: scattering experiments on nuclear/proton substructure:

- Evidence for proton substructure: Partons (Bjorken / Feynman).

→ Invention of the `Quark-Parton Model'

Proton consists of pointlike partons/quarks which carry fractional electric charge and a fraction x of the proton's momentum!

> Problems!!!!

- The Δ^{++} : spin-3/2 particle built from 3 identical up quarks with parallel spins????
- Scaling violations in deep-inelastic scattering experiments!!!
- How do electrically charged particles hold together in the proton????
- Where is the rest of the proton momentum – if not in the quarks????

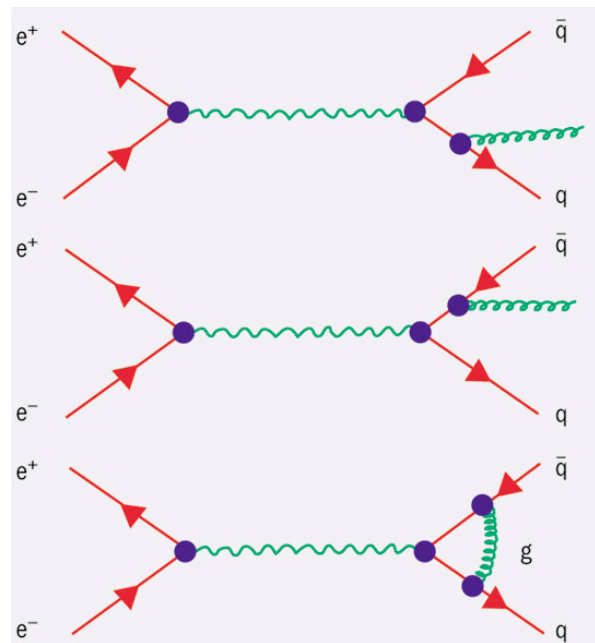
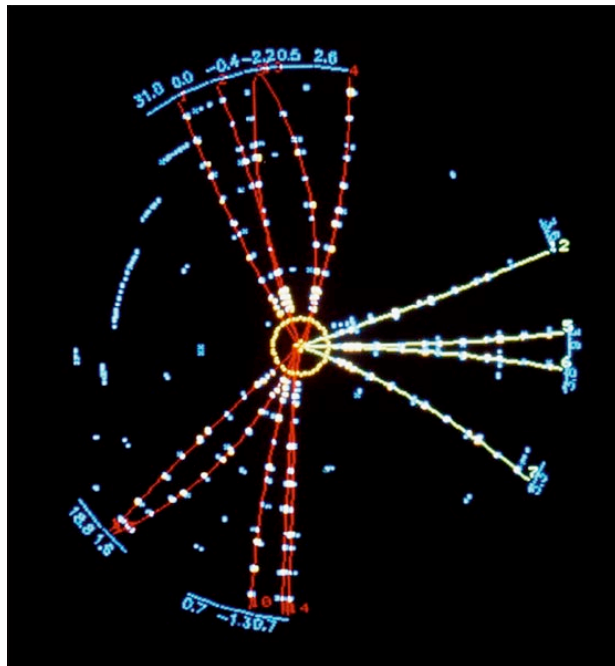
THE PATH TO QCD – HISTORY (2)

➤ Solutions: QCD

- A gauge theory along the lines of what was established for electro-weak interactions!
- Introduction of a new degree of freedom: colour!

➤ Experimental evidence: Discovery of gluons (here at PETRA / DESY!)

- $e^+e^- \rightarrow q\bar{q}g$ events at the PETRA collider 1979!



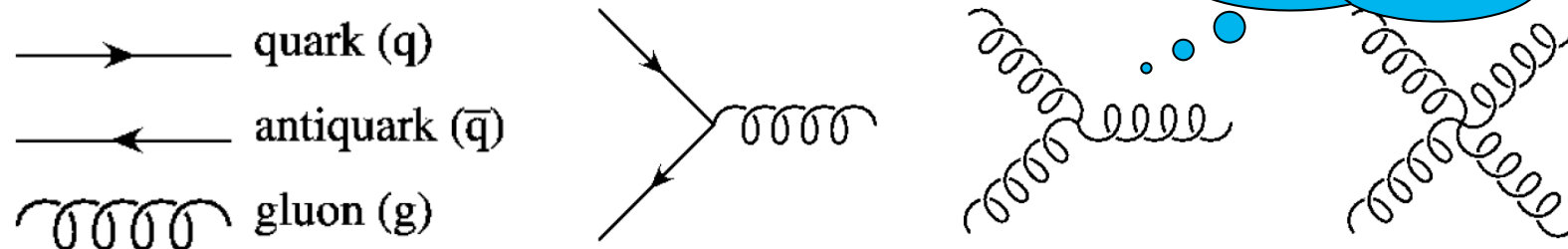
“... at a rate consistent with gluon radiation and a value of the strong coupling of about 0.15 ...”

BASICS OF QCD

> Quantum Chromodynamics (QCD) – the theory of strong interactions

- Non-abelian gauge field theory based on an $SU(3)_C$ symmetry.
- QCD describes interactions between coloured particles: quarks and gluons.
- Developed in the 1970es by Fritzsche, Gell-Mann, Leutwyler, Gross, Weinberg, etc. (see a bit on history later).

> Interactions in QCD



> We have three colour charges ('red', 'blue', 'green') and coloured gauge bosons

- This leads to $8(+1)$ gauge bosons (gluons) – in contrast to QED (1 neutral photon)
- ... and also to other remarkable features (next slides).

SALIENT FEATURES OF QCD (1)

> Asymptotic Freedom (NP2004 – Gross, Wilzcek, Politzer)

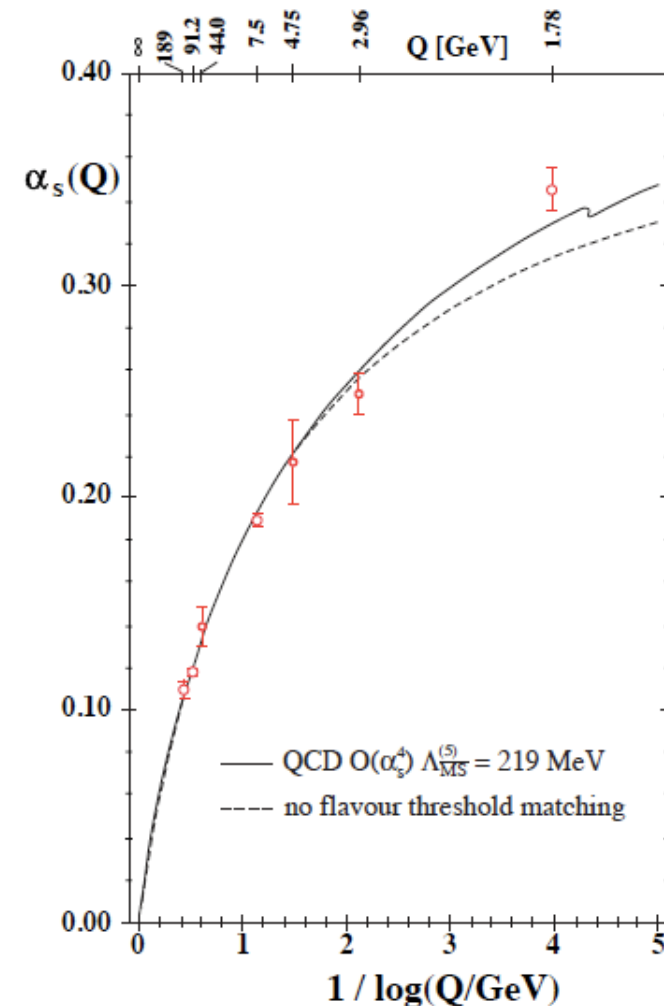
- Relevant parameter: Coupling strength between coloured particles: α_s !

$$\alpha_s(\mu) = \frac{\alpha_s(M_Z)}{1 + \alpha_s(M_Z) \cdot b \cdot \ln(\mu^2 / M_Z^2)}$$

- At large energies / small distances, quarks are 'free' inside the proton / hadron.

> Confinement:

- At large distances / small energies, the coupling increases and diverges.
- There are no free quarks!
- Solution of confinement is one of the Millenium Prize problems (Clay Mathematics Institute).



SALIENT FEATURES OF QCD (2)

> How to tackle QCD?

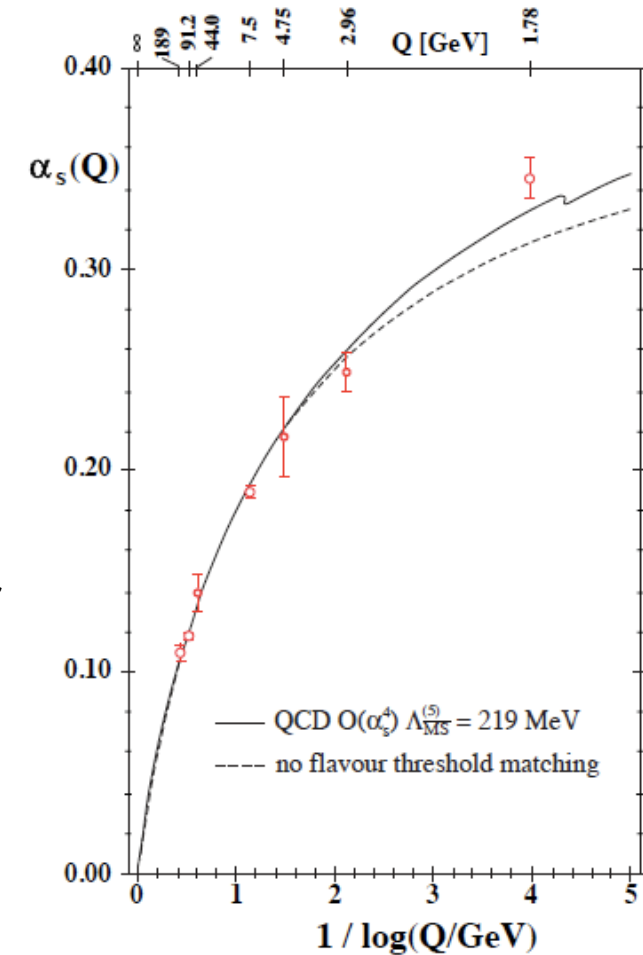
- Perturbative QCD: At high energies, the coupling is small and cross sections can be evaluated as power series in α_s :

$$\sigma = C_0 + \alpha_s \cdot C_1 + \alpha_s^2 \cdot C_2 \dots = \sum_{n=0}^{\infty} \alpha_s^n \cdot C_n$$

The coefficients can typically be evaluated to some (small) order: LO, NLO, NNLO
In addition methods to sum up other large contributing terms (large logs).

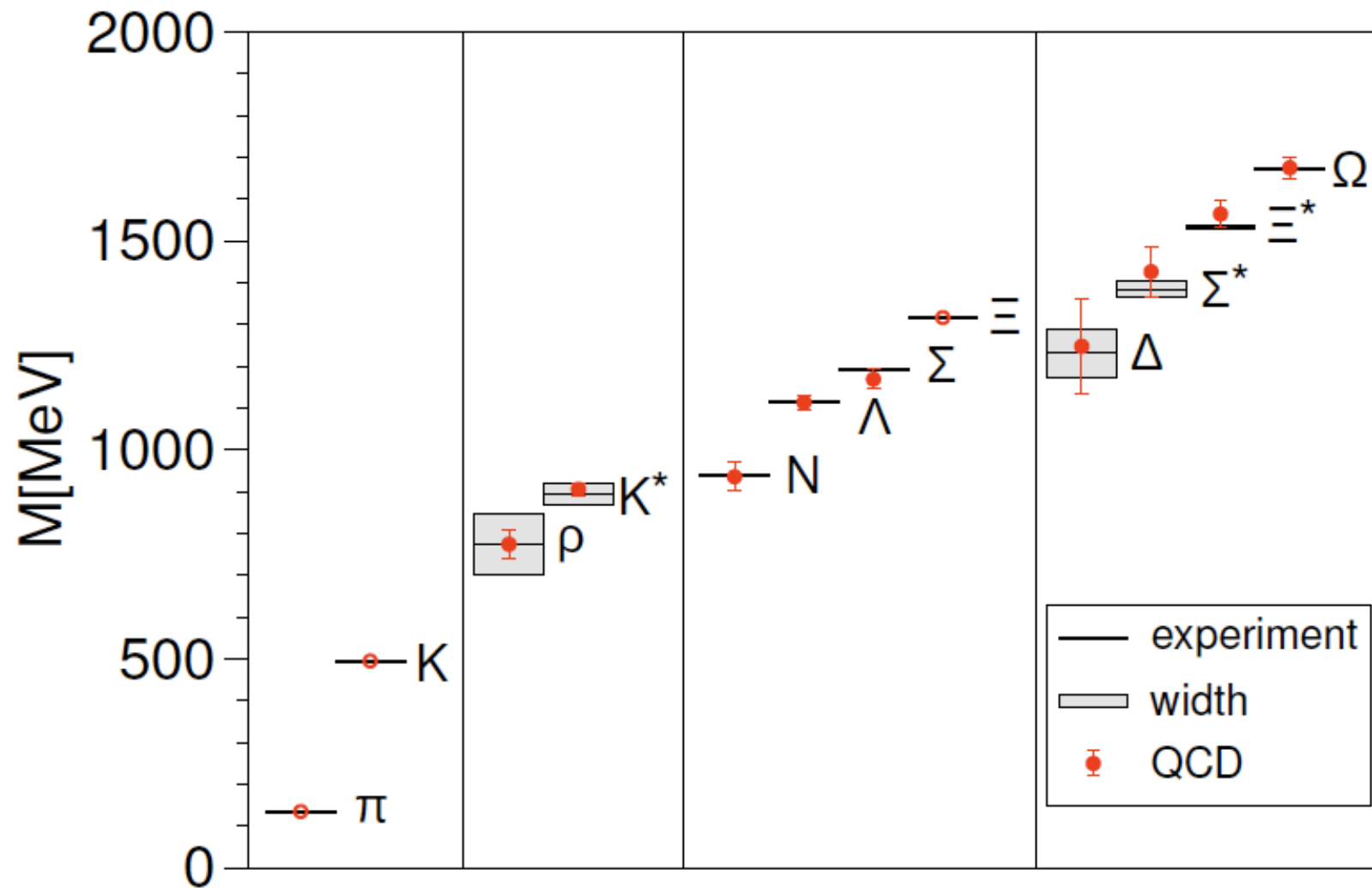
- Lattice QCD: can give particle spectra, indications for the value of the coupling, ...
- Effective theories
- 1/N expansions
- ...

$$\alpha_s(\mu) = \frac{\alpha_s(M_Z)}{1 + \alpha_s(M_Z) \cdot b \cdot \ln(\mu^2/M_Z^2)}$$

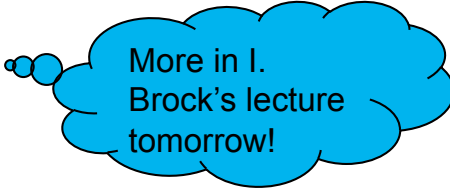


SALIENT FEATURES OF QCD (2)

> Hadron spectroscopy in lattice QCD



PARTON DISTRIBUTION FUNCTIONS



More in I.
Brock's lecture
tomorrow!

> We are talking about proton-proton collisions ...

- ... so we better know what the proton is (in terms of colliding constituents / partons / quarks+gluons).
- Description in terms of parton distribution functions (PDFs): probability to find a quark / gluon of type a with momentum fraction x in the proton when probed at a scale Q !

$$f_{a/p}(x, Q) \quad a = u, \bar{u}, d, \dots, g$$

> Why does $f_{a/p}$ depend on Q (dependence on x should be clear)?

- Virtual processes in the hadron: See more of the inner life when increasing the resolution (the scale / the energy, decreasing the distance, get closer) → change of probabilities to find quarks with certain properties (next slide).

> ... the bad thing about PDFs:

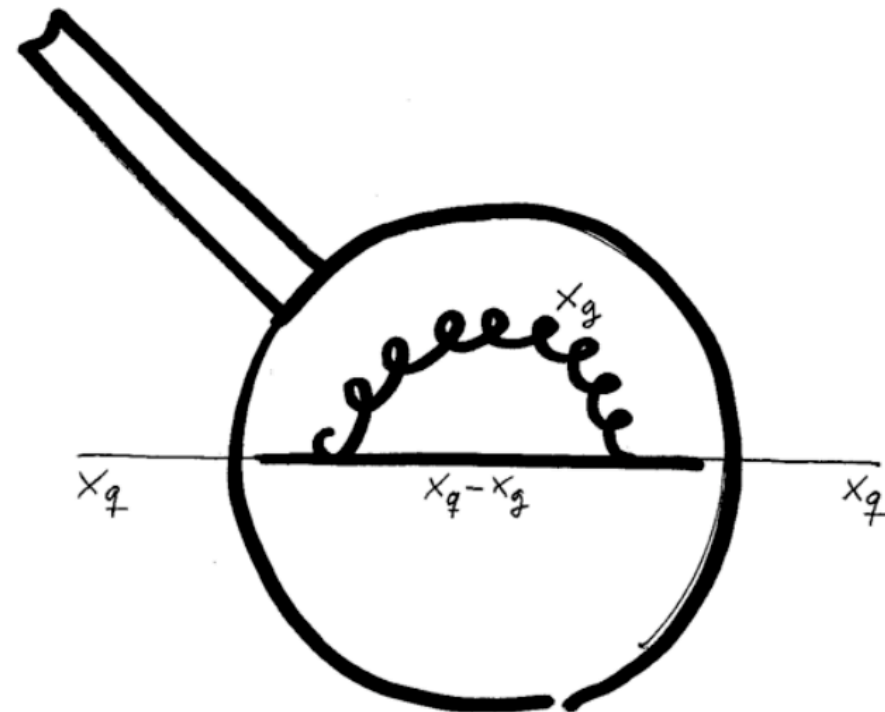
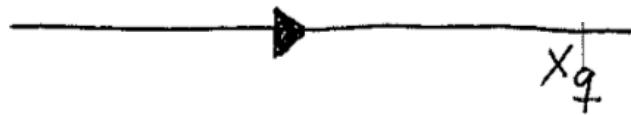
- They cannot be calculated from first principles ...
- ... but have to be determined using experimental data and involved mathematical tools (DGLAP evolution, not covered here).

PARTON DISTRIBUTION FUNCTIONS

More in I.
Brock's lecture
tomorrow!

> Why does $f_{a/p}$ depend on Q ?

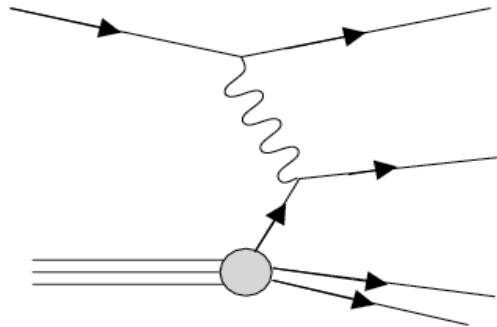
- Virtual processes in the hadron: See more of the inner life when increasing the resolution (the scale / the energy, decreasing the distance, get closer) $\rightarrow$ change of probabilities to find quarks with certain properties.



PARTON DISTRIBUTION FUNCTIONS

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Brock's lecture
tomorrow!

- > Extractions rely mainly on deep-inelastic scattering data (HERA)
 - Structure function F_2 : Related to ep cross section σ_{ep} and parton densities f_i !



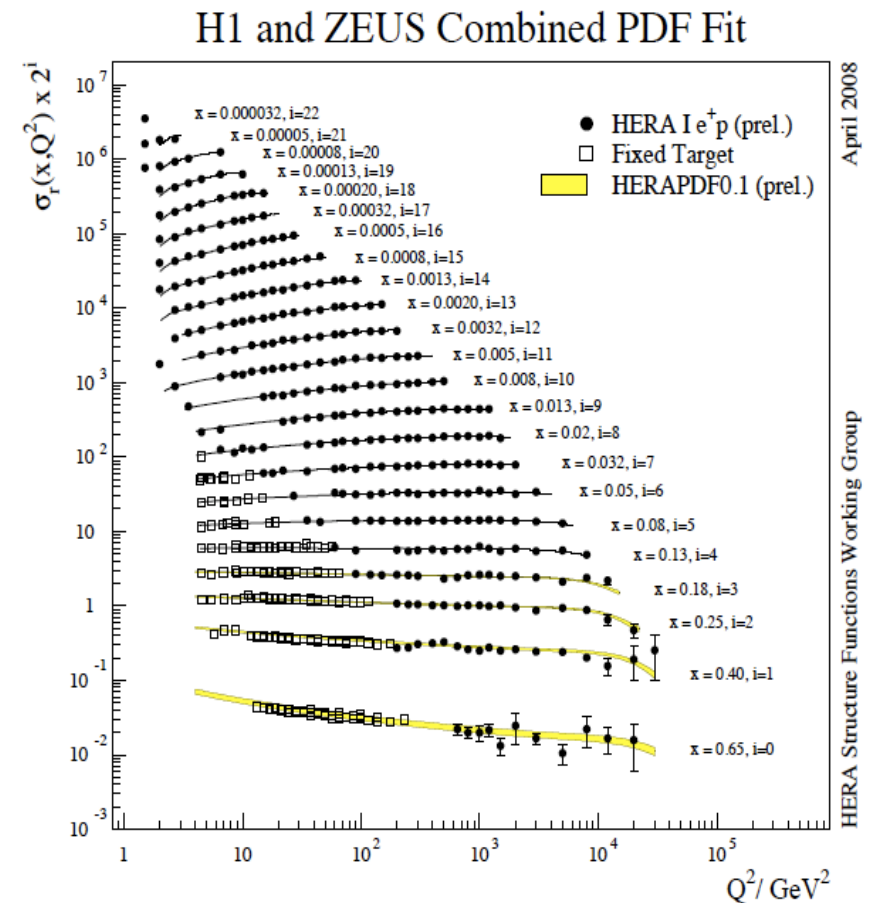
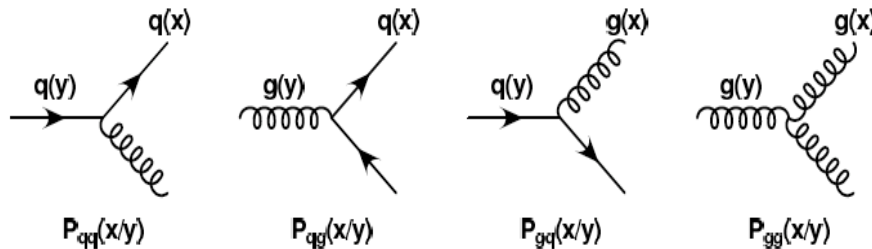
$$\sigma_{ep} \propto F_2(x, Q^2)$$

$$\approx x \sum_{i=q, \bar{q}} f_i(x, Q^2) \cdot q_i^2$$

- > QCD predicts behaviour of $F_2(Q^2)$

$$\frac{\partial F_2(x, Q^2)}{\partial \ln Q^2} \propto -\alpha_S P_{qq} F_2 + \alpha_S P_{qg} g$$

- Use to extract PDF f_i and α_S .



PARTON DISTRIBUTION FUNCTIONS

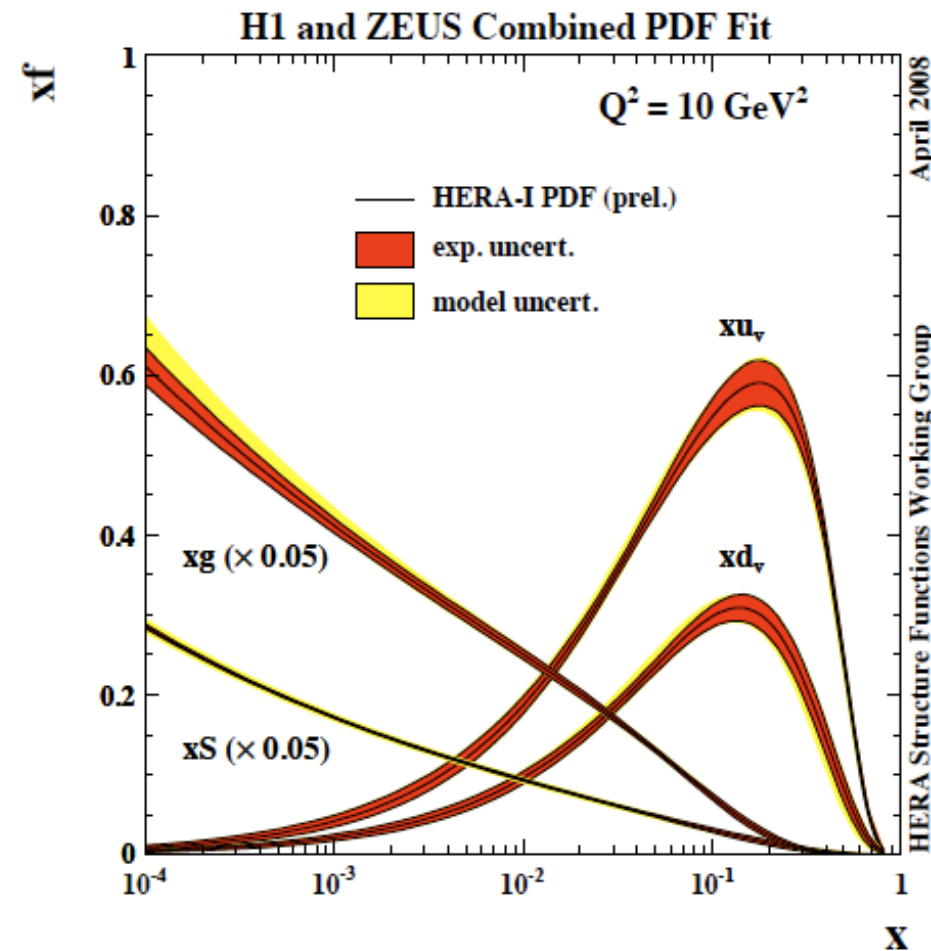
More in I.
Brock's lecture!

- > Current state-of-the art: PDF efforts from different groups like CTEQ, MSTW, HERA, etc. (and hopes to improve with LHC data):

$$f_{a/p}(x, Q) \quad a = u, \bar{u}, d, \dots, g$$

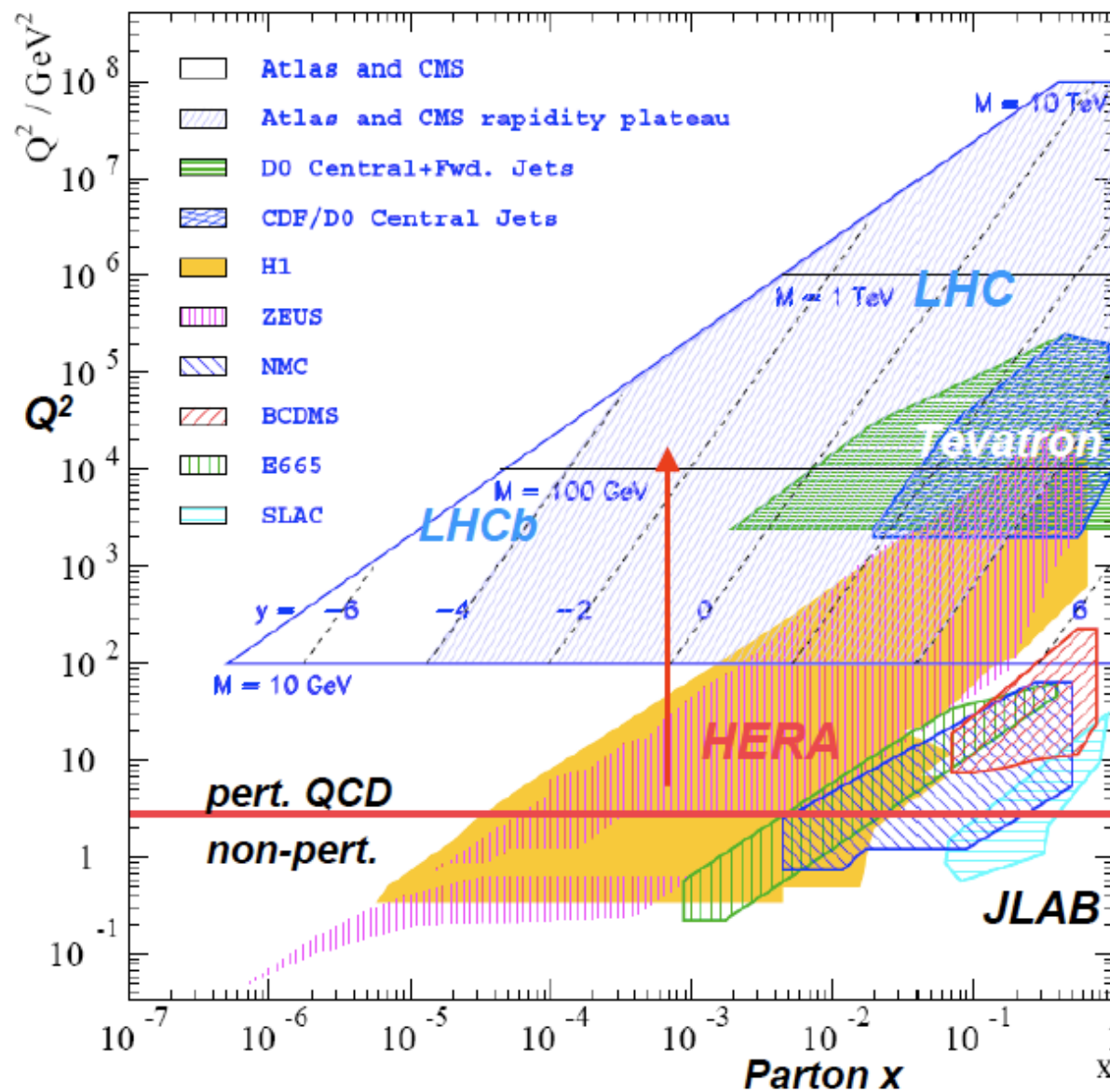
- > Use existing libraries to access given PDF sets for usage in your analysis

- LHAPDF
- OOPDF
- ...
- Interfaced to experiment-specific software!



PARTON DISTRIBUTION FUNCTIONS

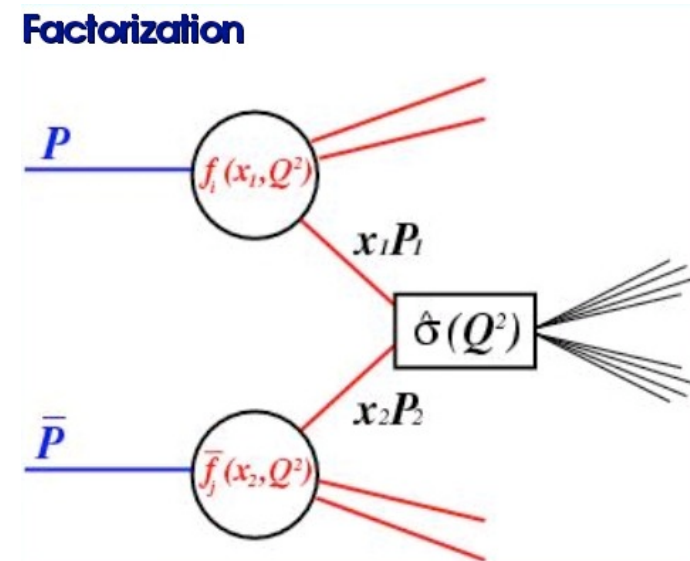
More in I.
Brock's lecture!



PDFs AND FACTORISATION

- > How to get from the PDFs to the physics? Convolution of PDFs with matrix elements describing the underlying scattering process.

$$\begin{aligned}\sigma &= \sum_{a=q,\bar{q},g} f_{a/p}(x_a, Q) \otimes \hat{\sigma}_{ab} \otimes f_{b/p}(x_b, Q) \\ &= \sum_n \sum_{a,b=q,\bar{q},g} f_{a/p} \otimes \hat{\sigma}_{ab,n} \otimes f_{b/p} \\ &= \sum_n \alpha_S^n \cdot \sum_{a,b=q,\bar{q},g} f_{a/p} \otimes C_{ab,n} \otimes f_{b/p}\end{aligned}$$



- > So the problem reduces to having the PDFs and calculating, using pQCD, the matrix elements or coefficients C_n .
 - ➔ Although that statement is a bit over-simplifying ... see next slides!

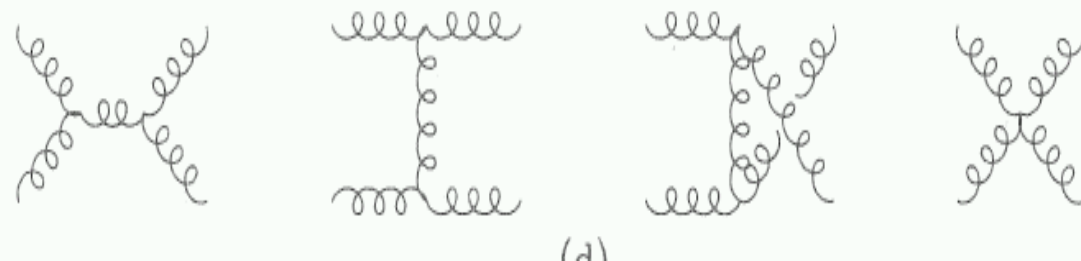
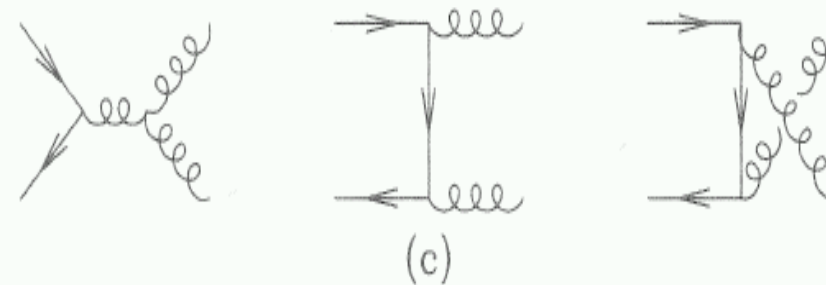
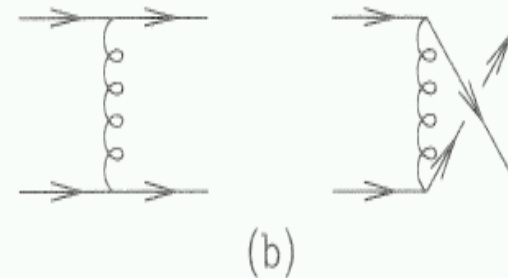
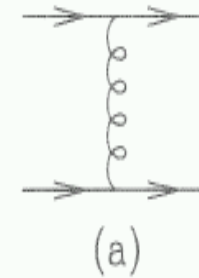
PDFs AND FACTORISATION

> Processes to be considered in QCD events in hadron-hadron collisions!

- ... just a few examples ...

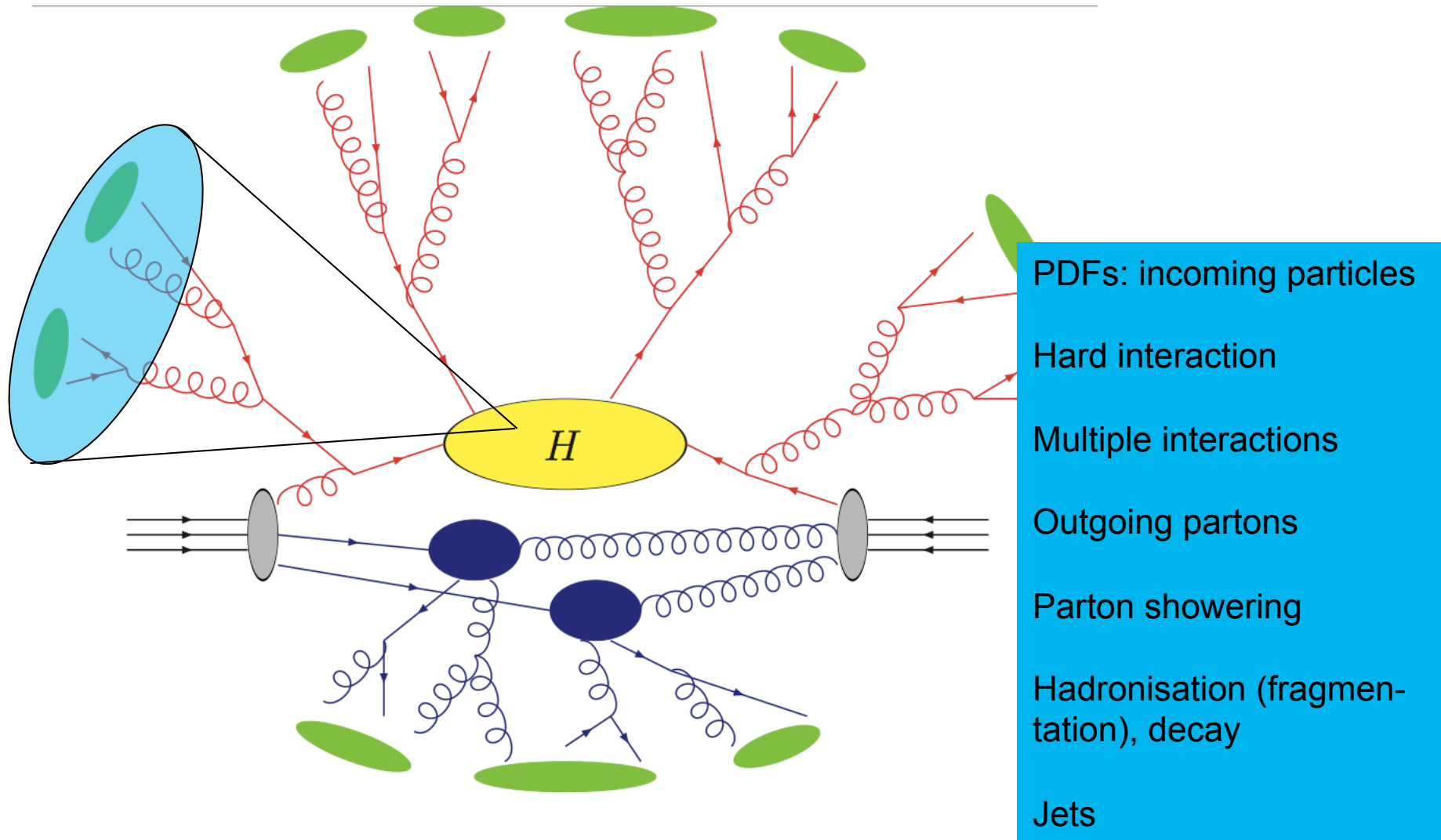
> Important: different final states and different physics questions.

- **Particle production** from “showering” and “fragmentation” of outgoing quarks and gluons.
- **Jets** as “fingerprints” of outgoing quarks and gluons.
- Cross-sections / rates of these processes → background for searches and new physics (QCD as “bread-and-butter physics”)



PDFs AND FACTORISATION

> ... there's more to events in hadron-hadron collisions!

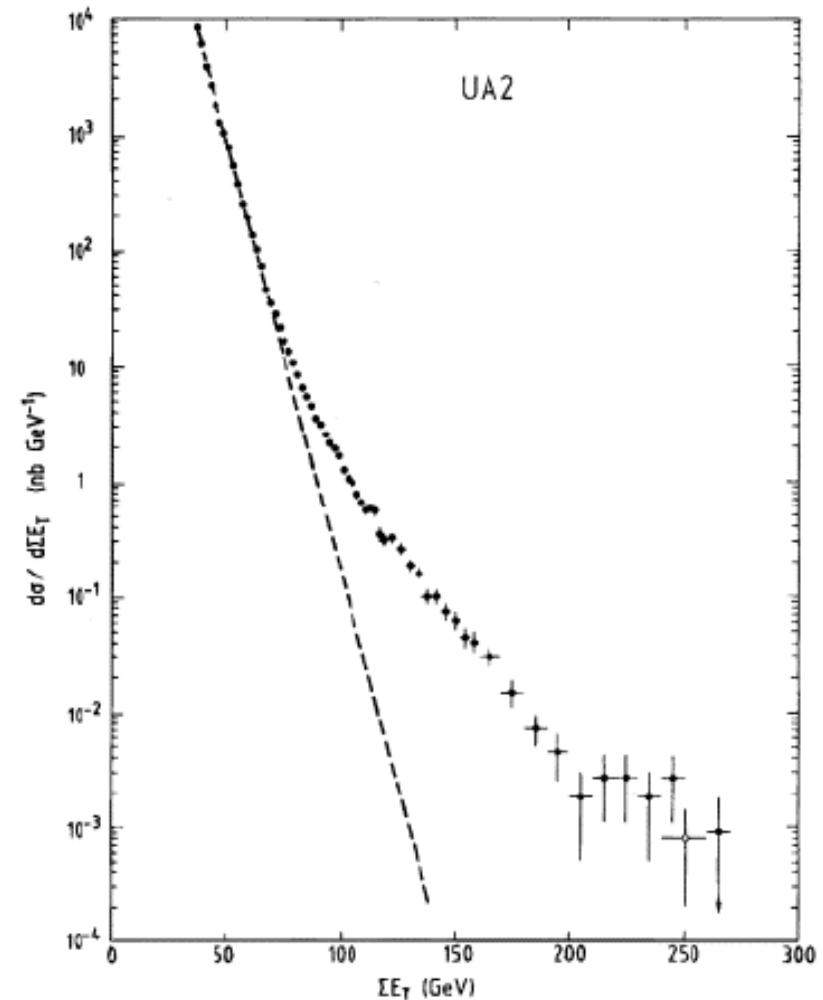
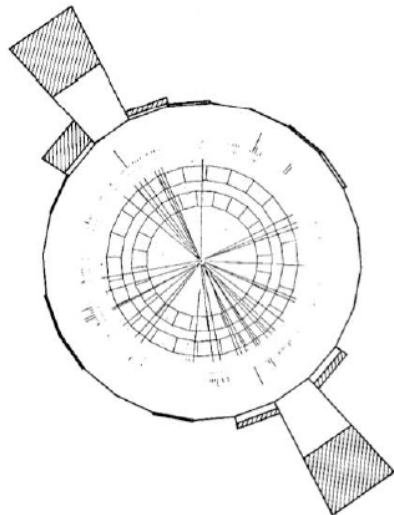




PARTICLE PRODUCTION: HISTORY

➤ In the 1960es, 70es observables describing events were measured in hadron collisions – for example total transverse energy (here UA2 at SppS).

- Low E_T : exponential fall-off, higher E_T : power law: E_T^{-n} .
- Indication for hard proton constituents!
- Furthermore: “jet-like” structures observed: indication of hard $2 \rightarrow 2$ scattering, with final-state clustered around initial partons.



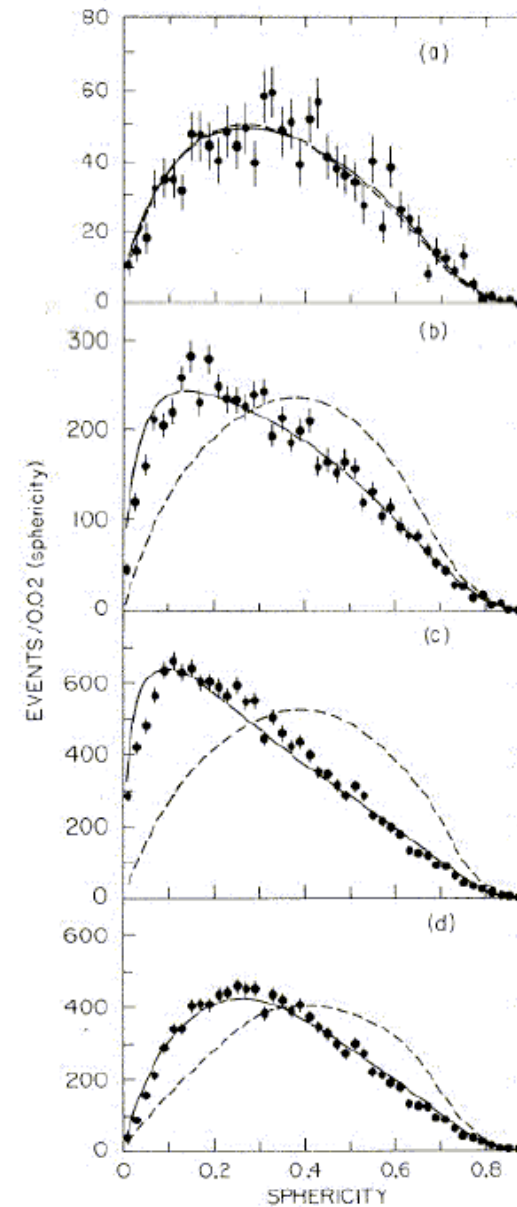
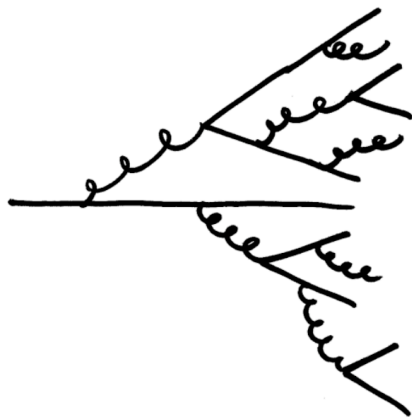
PARTICLE PRODUCTION: HISTORY

➤ Question: Are particles produced spherically symmetrically (in transverse plane) or is there a structure?

- Studied in hadron-hadron / ee collisions.
- Example: Sphericity S (Mark-I at SPEAR):

$$S = \frac{3 (\sum_i p_{T,i}^2)}{2 (\sum_i \vec{p}_i^2)},$$

- Evidence for jet-like structure
→ fragmentation / showering models.

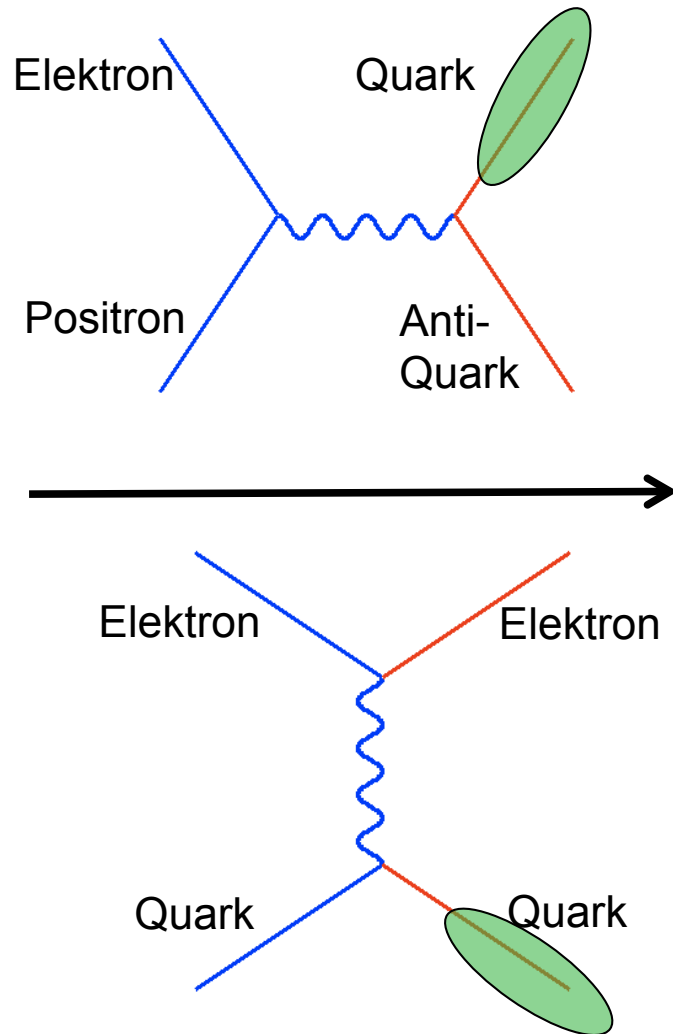


PARTICLE PRODUCTION

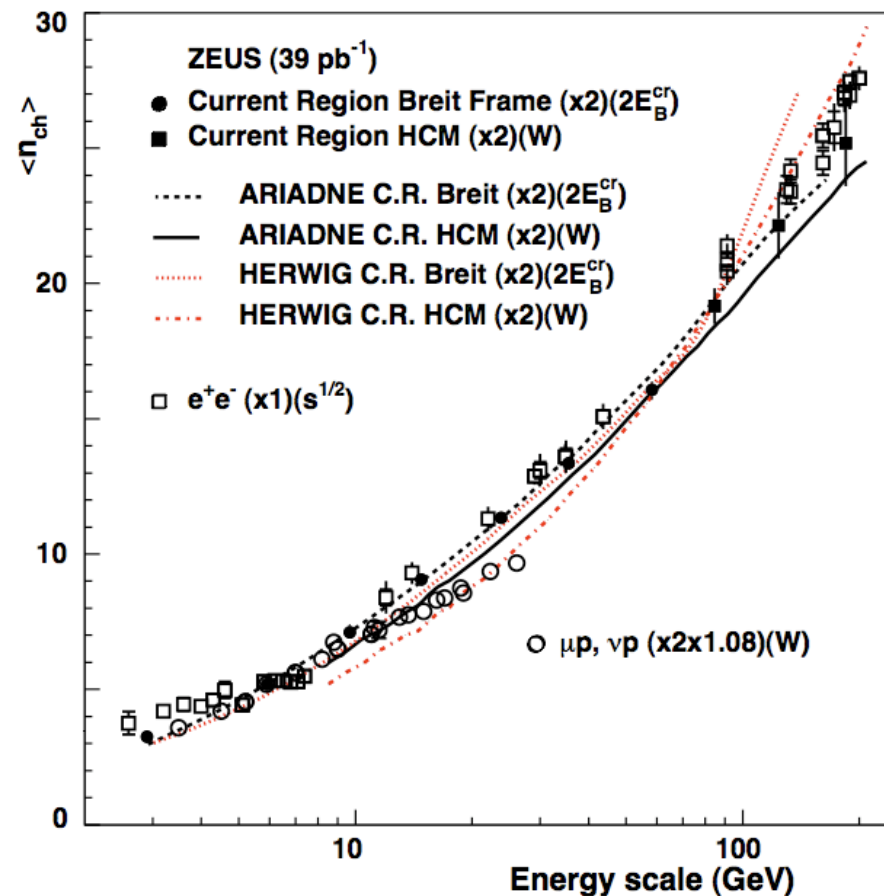
- > In the processes of parton showering and fragmentation of the final-state quarks, numerous stable particles (pions, protons, ...) are produced.
 - Measure the number of charged particles as functions of transverse momentum p_T and pseudorapidity η and test models.
 - Measure energy dependence of average transverse momentum and average charged particle multiplicity.
 - Measure individual particles, for example K , Λ , J/Ψ , and ratios of these.
 - Measure ...
 - > Note that it is especially interesting to measure the same distributions at different centre-of-mass energies and at different machines in order to
 - Be able to compare / verify different measurements and
 - To learn about the behaviour of distributions and average values with energy.
 - To adjust (“tune”) the models we have.
- ➔ Compare experimental results from ISR, SppS, LHC, RHIC, Tevatron

PARTICLE PRODUCTION

> ... energy dependence of charged hadron multiplicity:



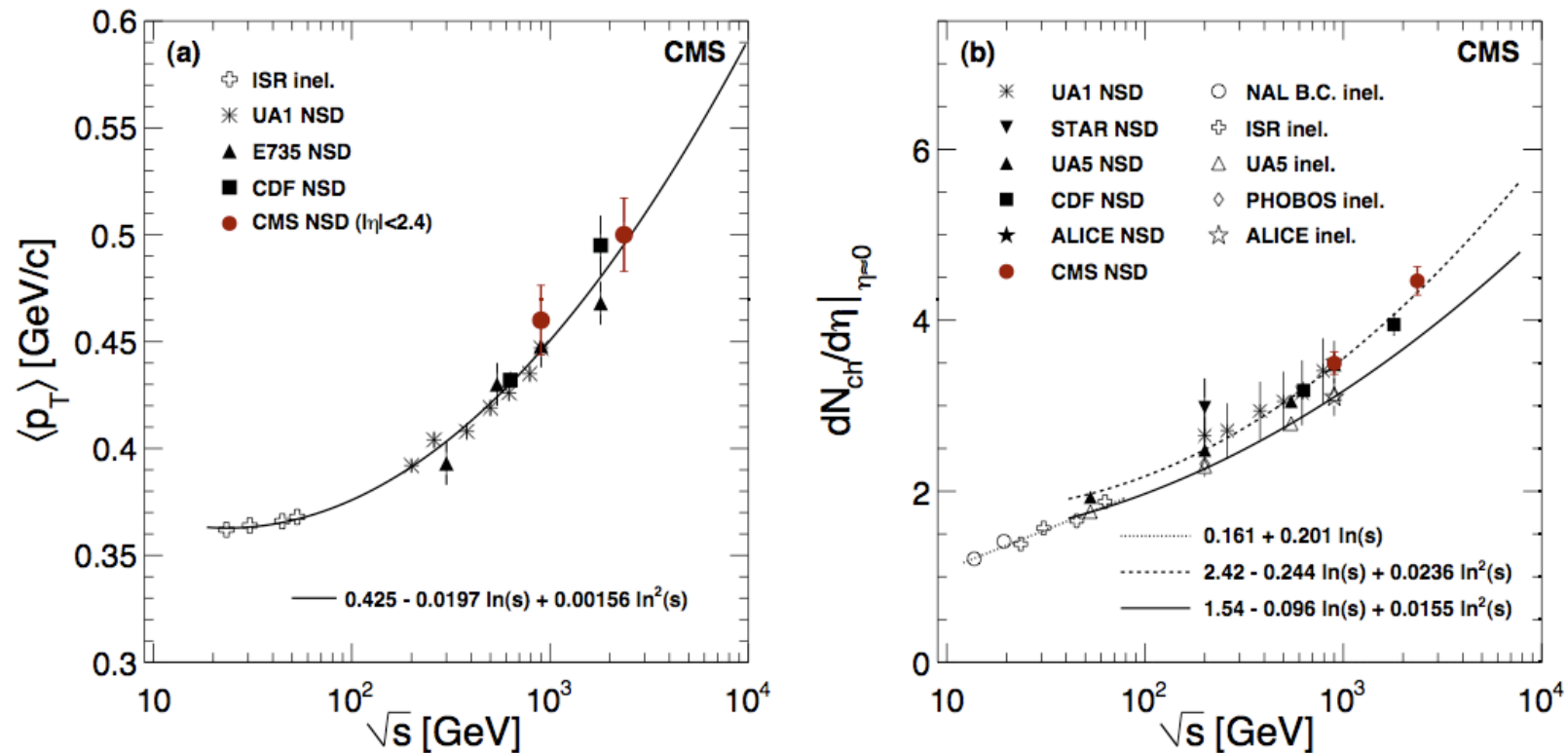
ZEUS



Fragmentation is ~ universal!

PARTICLE PRODUCTION

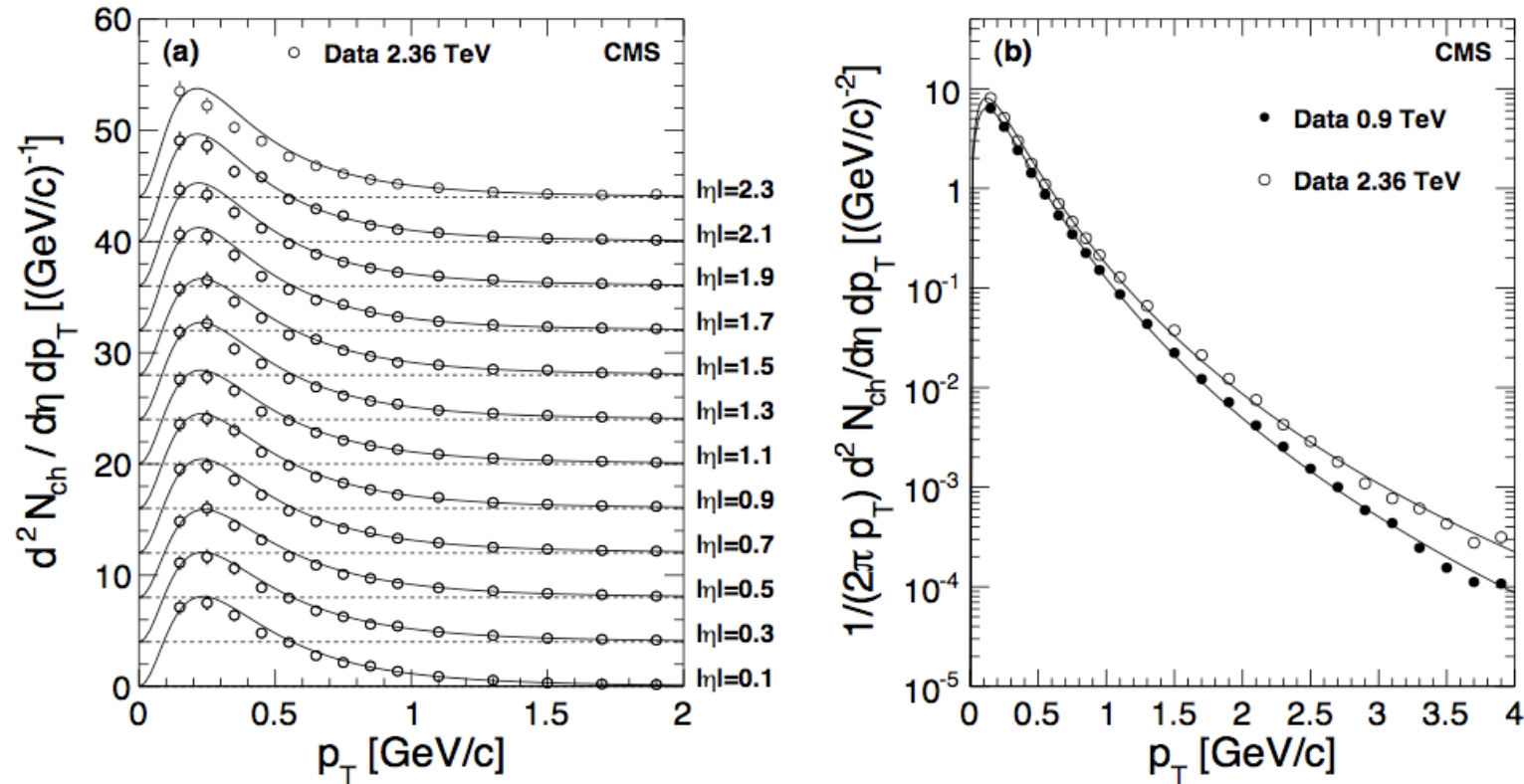
> ... recent results from CMS, and some comparisons.



CMS result fits in nicely with simple parametrisation of behaviour with CMS energy!

PARTICLE PRODUCTION

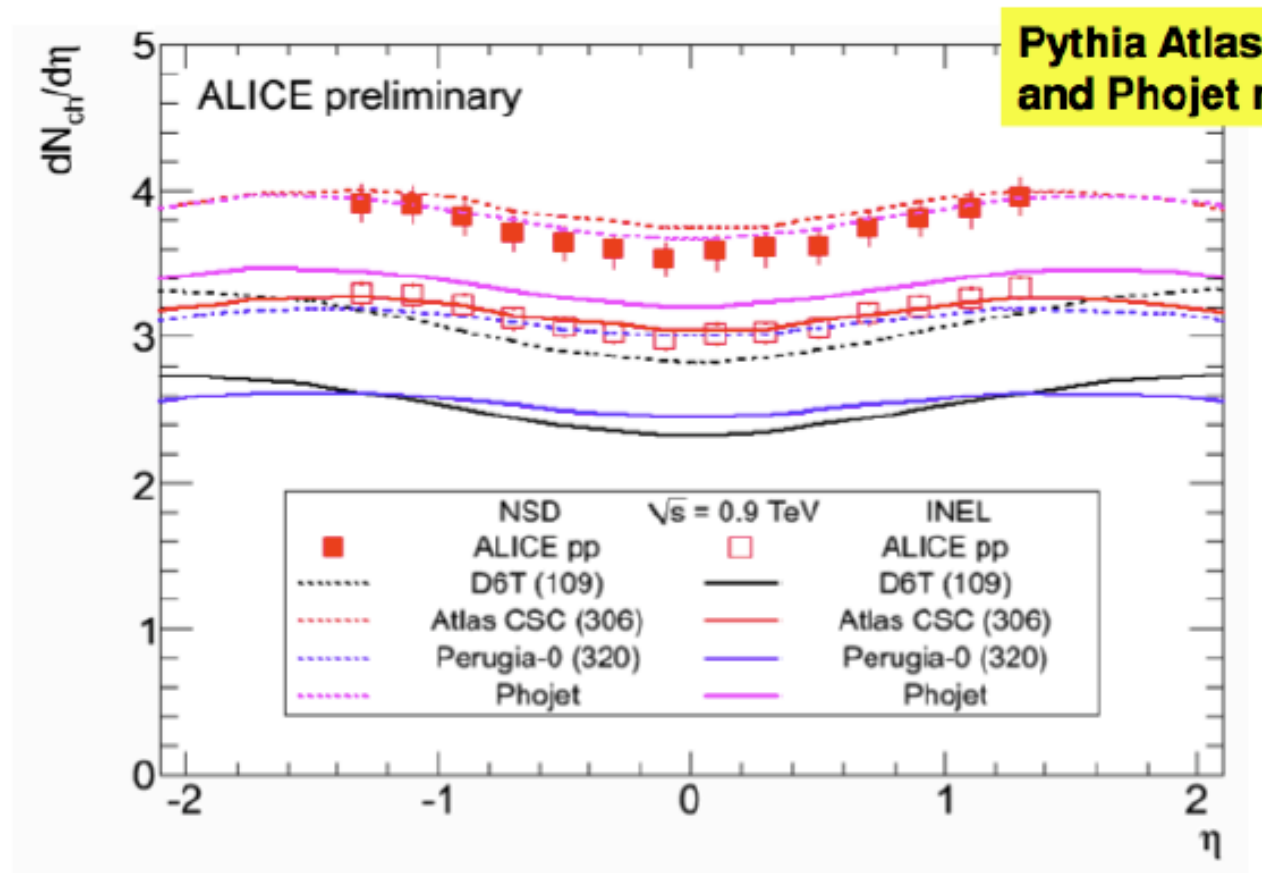
> ... recent results from CMS, and some comparisons.



$$E \frac{d^3 N_{ch}}{dp^3} = \frac{1}{2\pi p_T} \frac{E}{p} \frac{d^2 N_{ch}}{d\eta dp_T} = C(n, T, m) \frac{dN_{ch}}{dy} \left(1 + \frac{E_T}{nT} \right)^{-n},$$

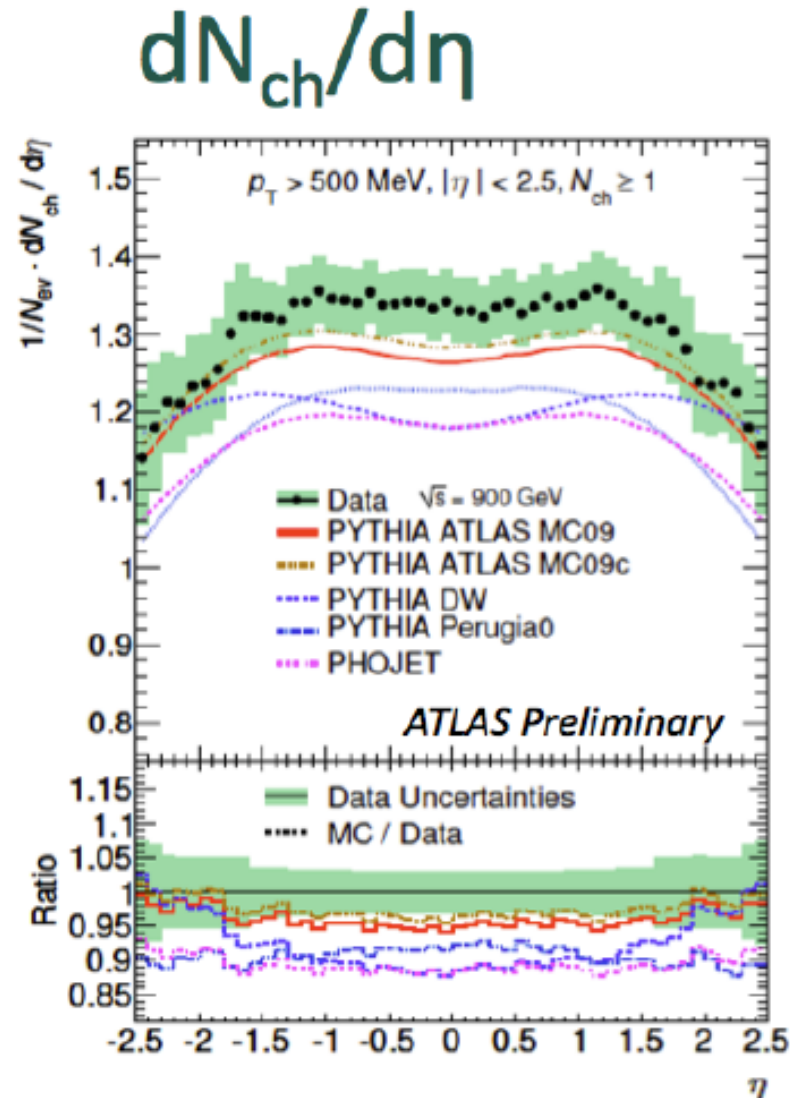
PARTICLE PRODUCTION

- > ... recent results from LHC, and some comparisons.



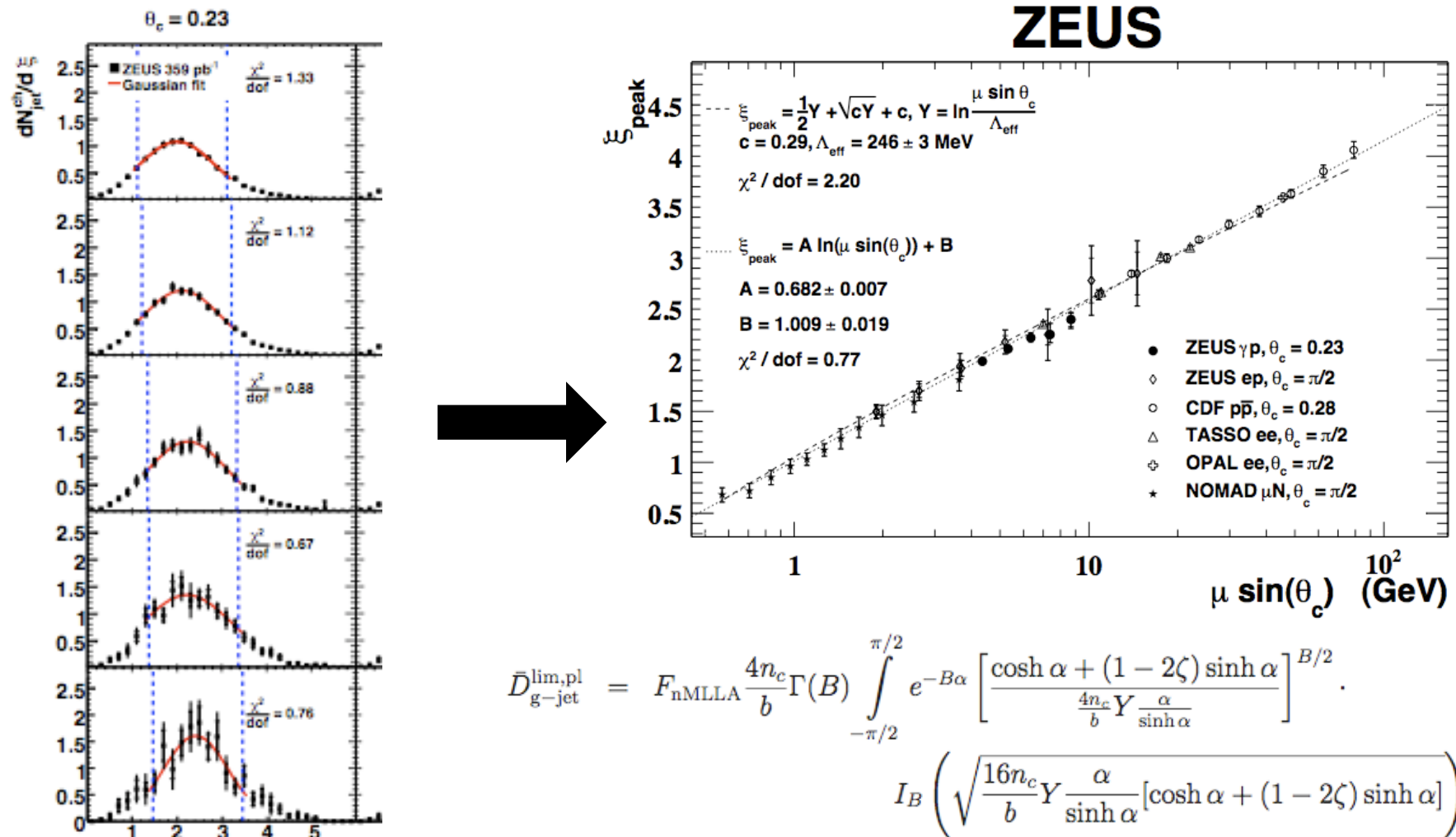
PARTICLE PRODUCTION

- > ... recent results from LHC, and some comparisons.



PARTICLE PRODUCTION

> ... Mean energy fraction of particles in jets as function of opening angle!



Nice agreement between results from different machines !

JET PHYSICS

- > ... there's more to events in hadron-hadron collisions ...
 - ... than “just” produced particles!
- > Already mentioned: “Jets” structures underlying the distribution of the produced particles (example from UA2)
 - Two back-to-back “jets” (word inherited from cosmic-ray experiments)???
 - Polar-angular distribution of jets following

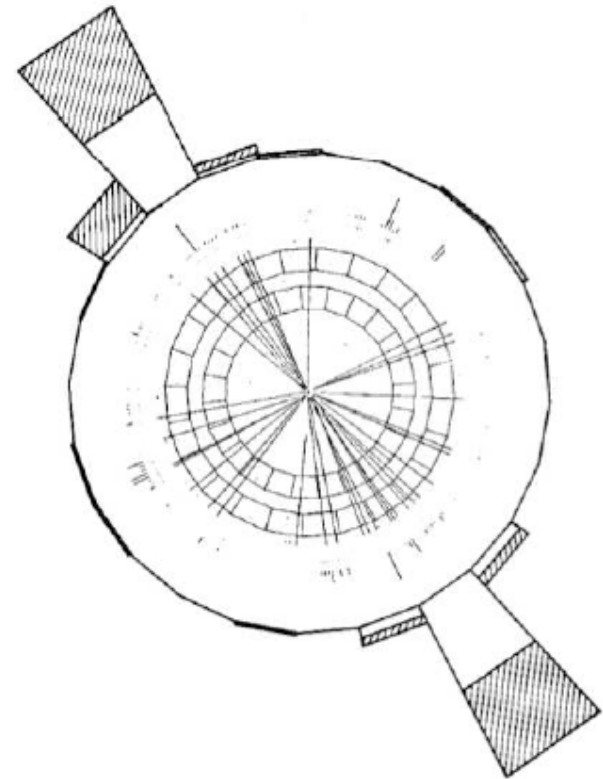
$$1 + \alpha \cos^2 \theta$$

→ 2→2 scattering with spin-1/2 particles?

- > In parallel: jet structures in e^+e^- collisions at different experiments; identification as

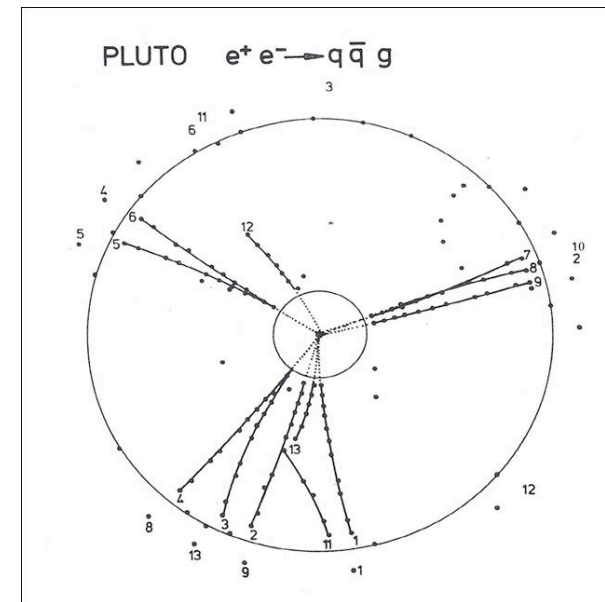
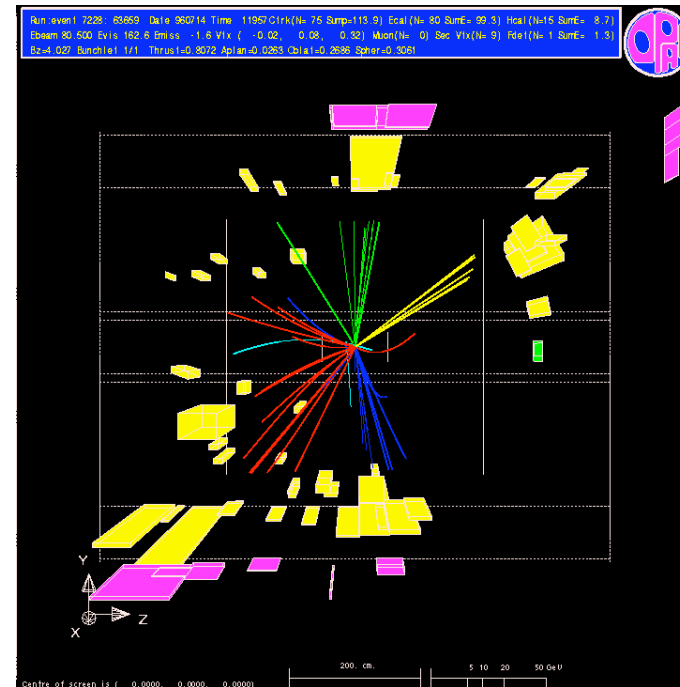
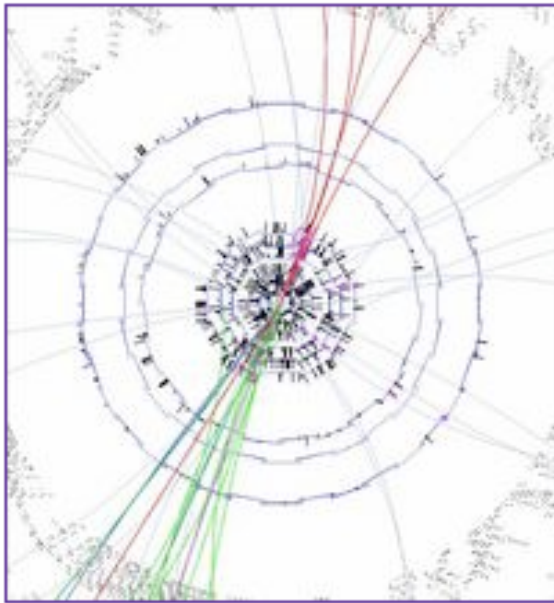
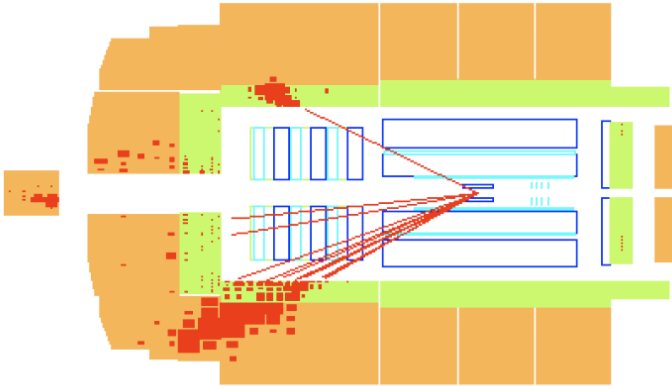
$$e^+e^- \rightarrow q\bar{q}$$

- > Historically not a trivial story to identify the partons in the proton with the results of ee !



JET PHYSICS

> ... at different experiments:



JET PHYSICS

> ... at different experiments:



JET PHYSICS: BASICS

> Jets: two-fold purpose in high-energy physics

- Tool for studying (hard QCD) interactions
- Object of study in itself: Fragmentation etc.

> Jets – although clearly visible to the naked, untrained eye – are neither a simple nor a well-defined concept!

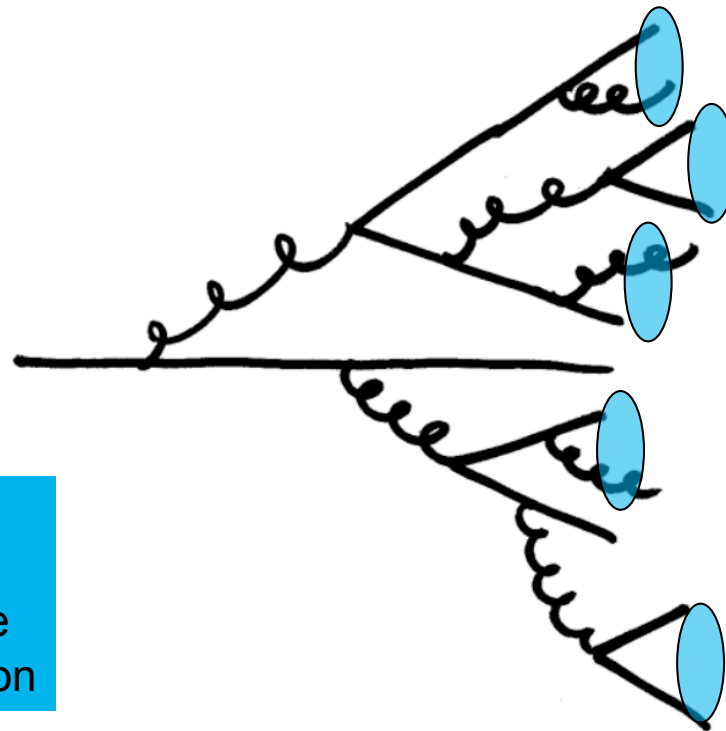
- A jet algorithm is a mathematical prescription for clustering the objects of the final state (if possible both in the experiment and for theoretical predictions and models).
- Different classes of algorithms, different fields of applications (hadron colliders, lepton colliders, HERA, ...), different physics questions → jet physics is a science in itself!
- Jet algorithms shall fulfill a number of requirements (without completeness): theoretically safe, easy to handle, small hadronisation corrections, unbiased, ...

> Currently two classes of algorithms used: cluster algorithms and cone-based algorithms

- Historically, the Tevatron experiments tended to cone-based algorithms, e⁺e⁻ and HERA to clustering algorithms;
- At LHC, both collaborations study a multitude of different algorithms.

JET PHYSICS: ALGORITHMS

- > Cone algorithms: Aim at minimising the relative transverse momentum in cones of fixed sizes (directions of largest energy flow in the event).
- > Clustering algorithms: “Resumming” the parton showering / fragmentation process, using some distance criterion:



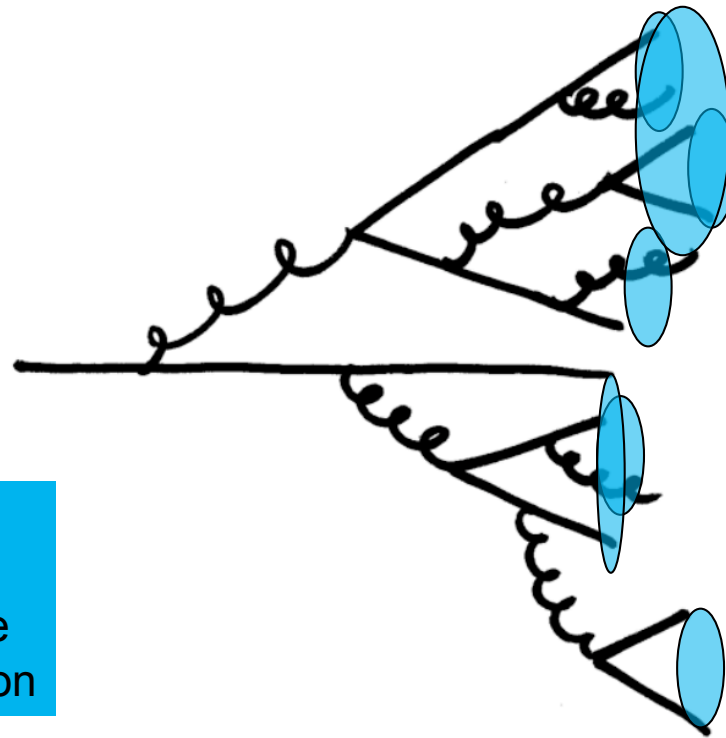
All particles clustered to a number of jets !!!

Possible criteria:

- invariant mass
- distance in angle
- some combination

JET PHYSICS: ALGORITHMS

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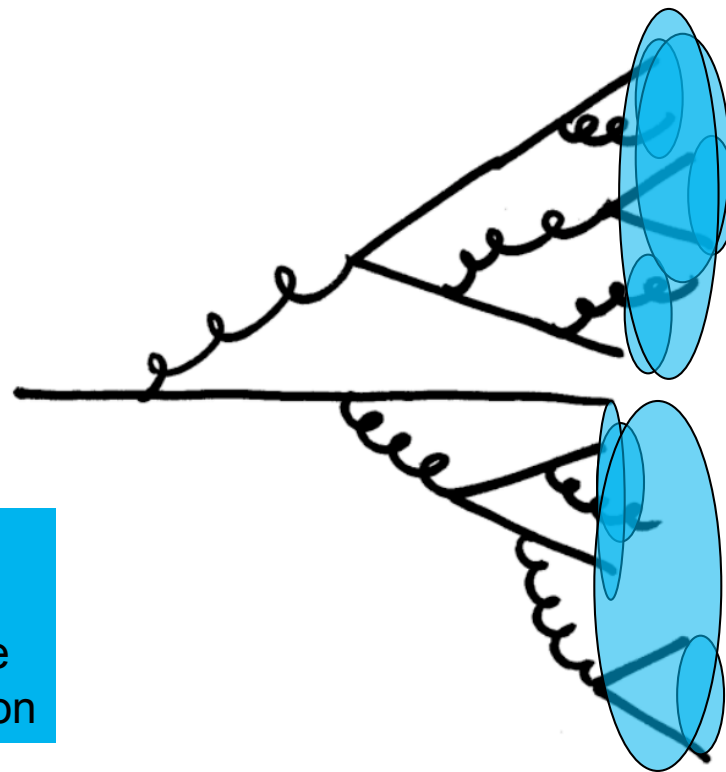
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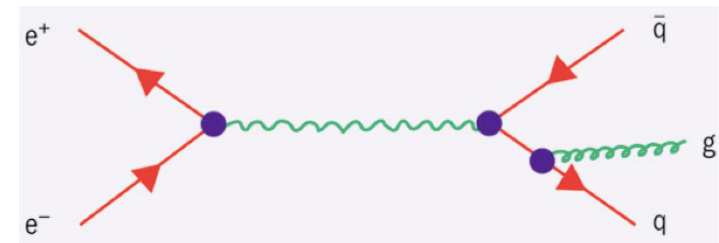
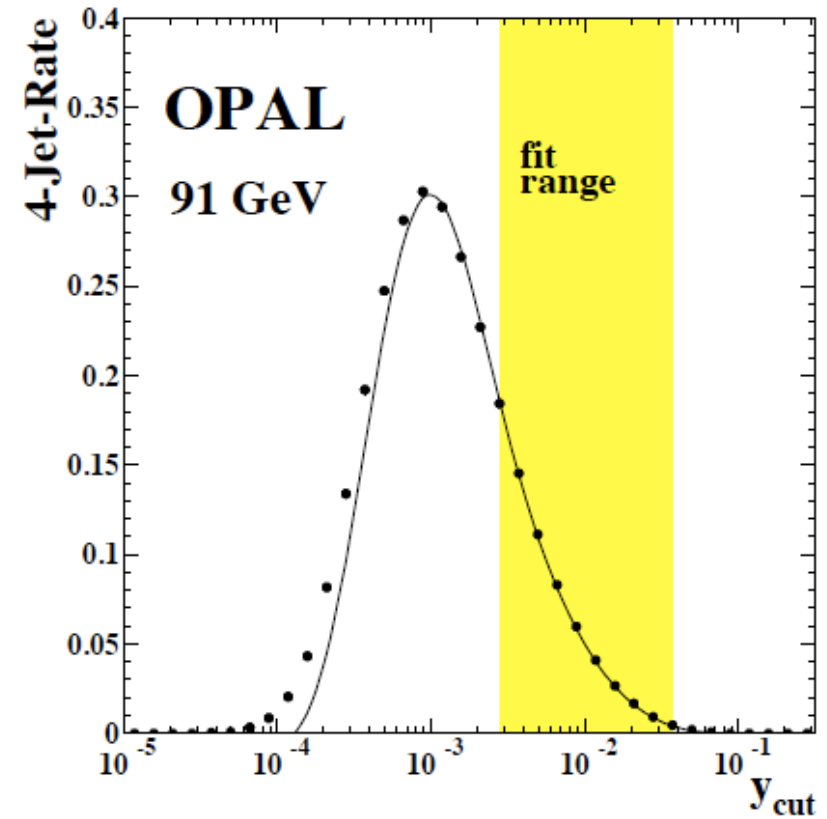
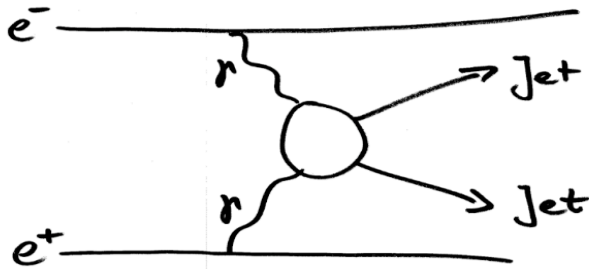
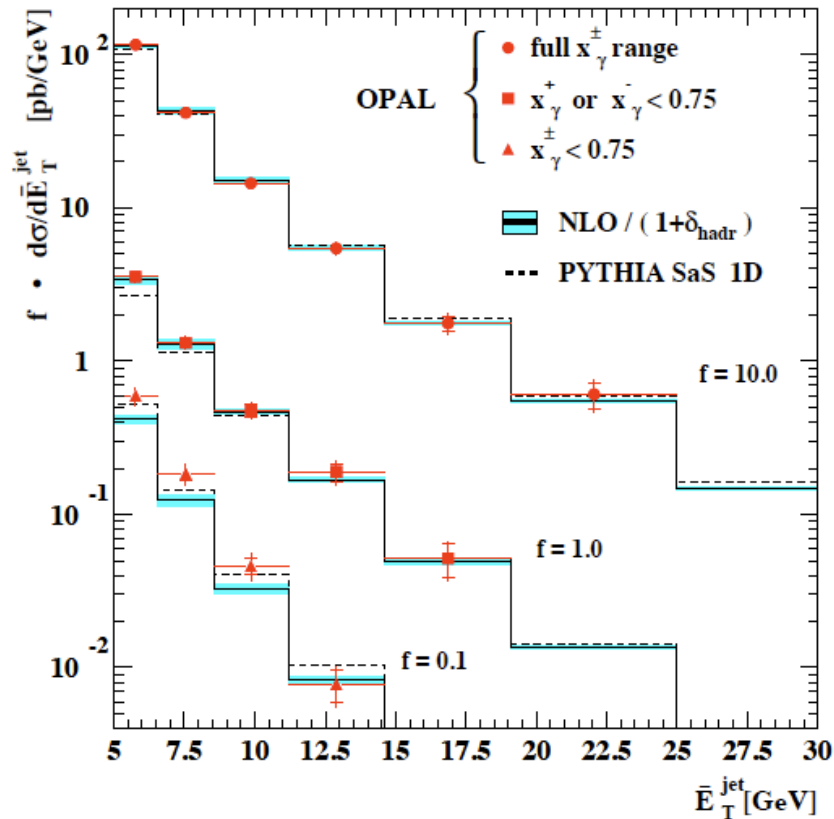
All particles clustered to a number of jets !!!

Possible criteria:

- invariant mass
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JET PHYSICS: RESULTS FROM LEP

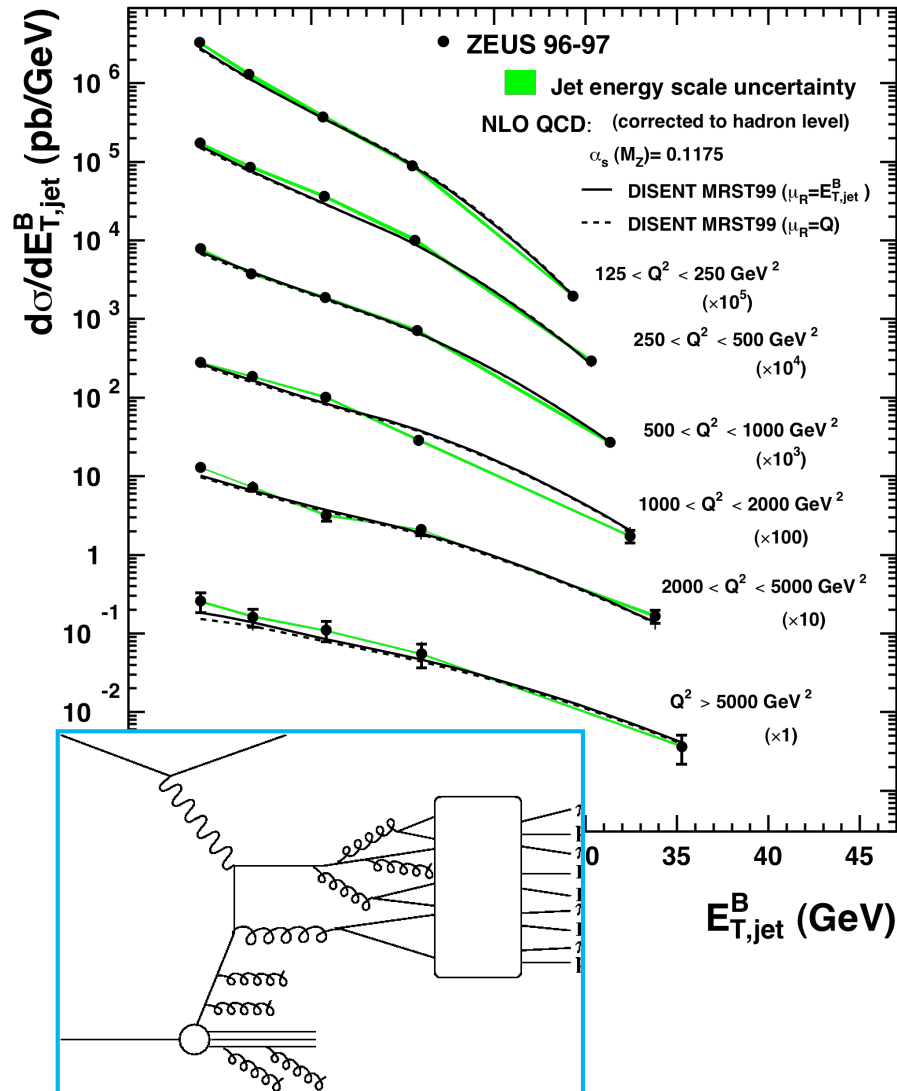
➤ In $ee \rightarrow qq(q,q)$ or in $\gamma\gamma$ collisions:



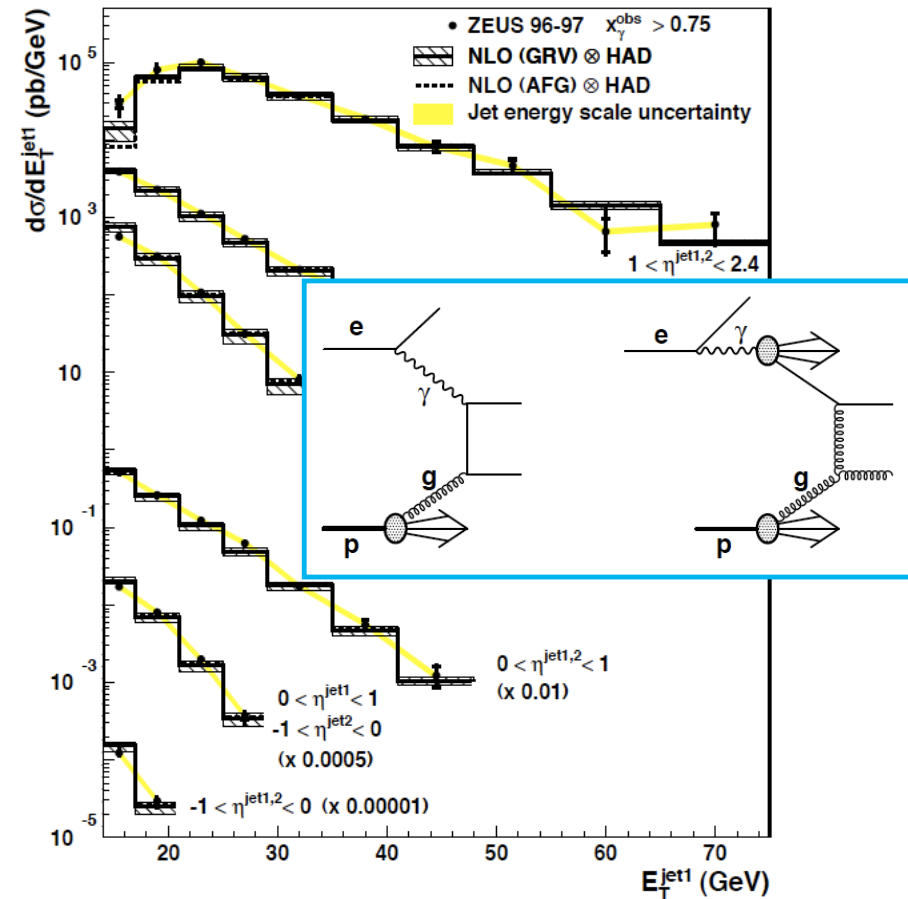
JET PHYSICS: RESULTS FROM HERA (1)

➤ In photoproduction, in deep-inelastic scattering, in diffraction

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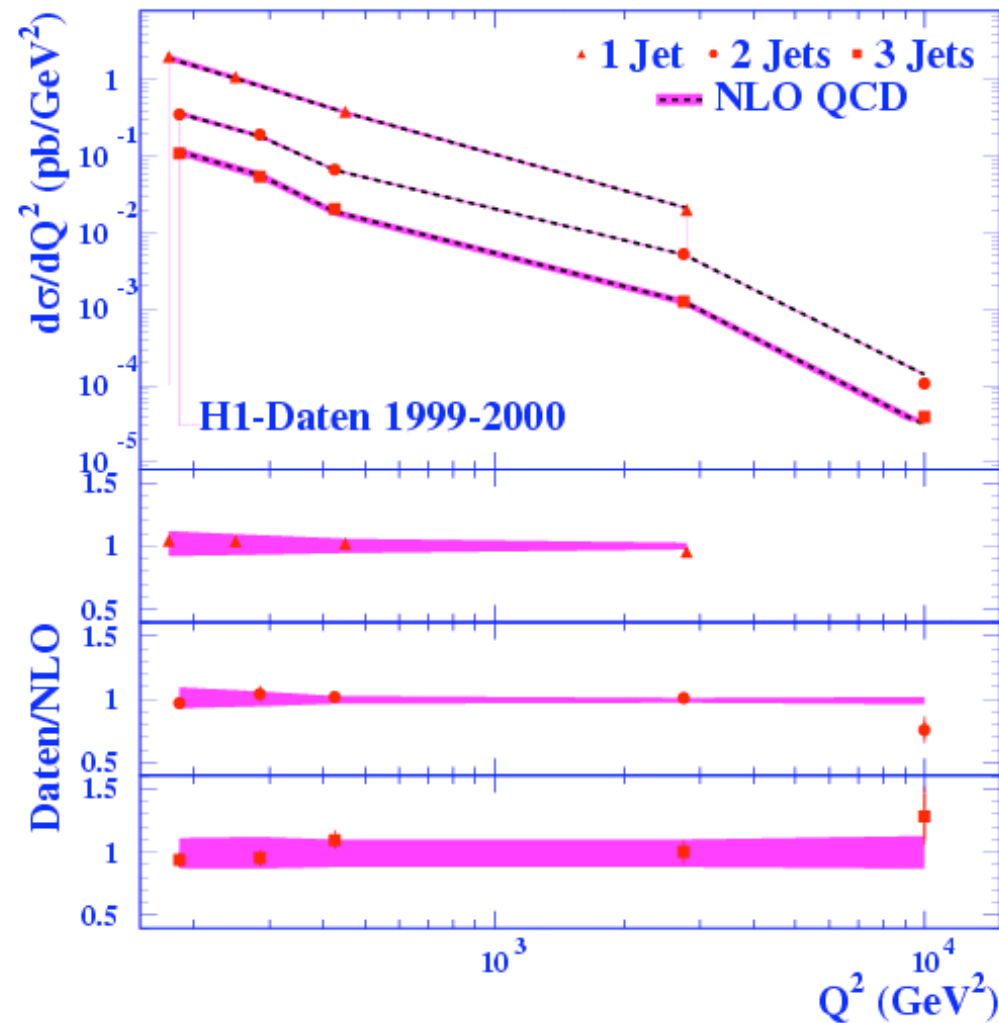
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QCD at NLO works beautifully in most phase-space regions !!!

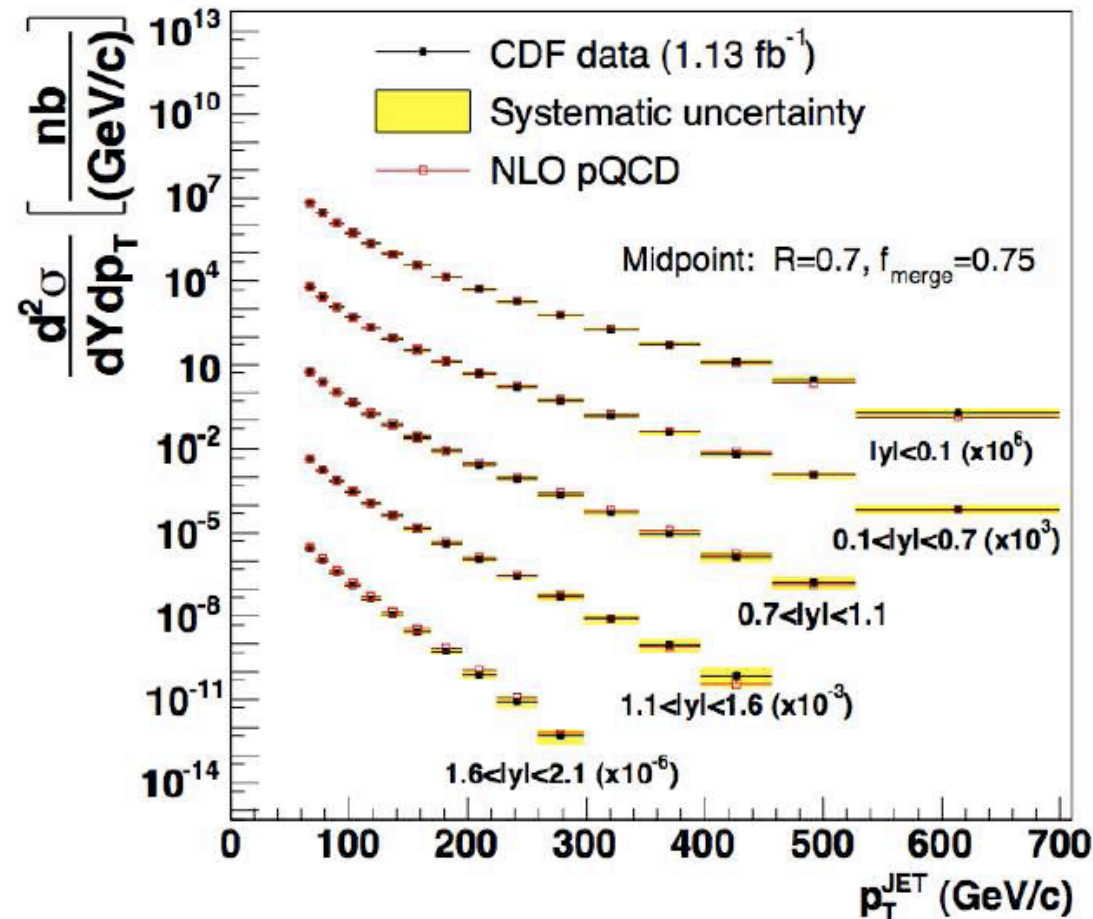
JET PHYSICS: RESULTS FROM HERA (2)

➤ Comparison of 1,2,3 jet production!



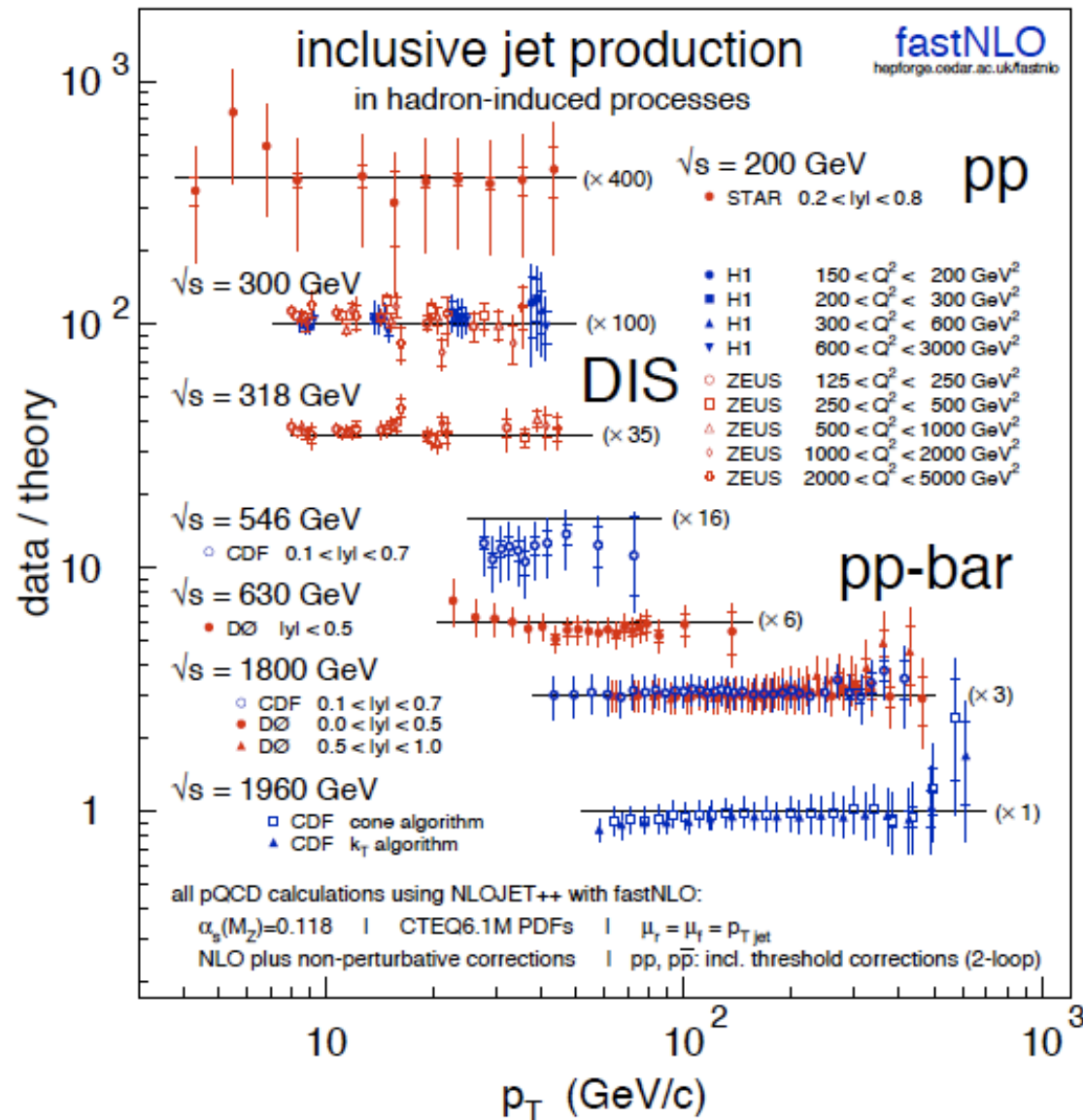
JET PHYSICS: RESULTS FROM TEVATRON

- Measuring jets up to energies of 600 GeV!!!!



- Nice description by NLO QCD calculations! In contrast to HERA, often experimentally limited.

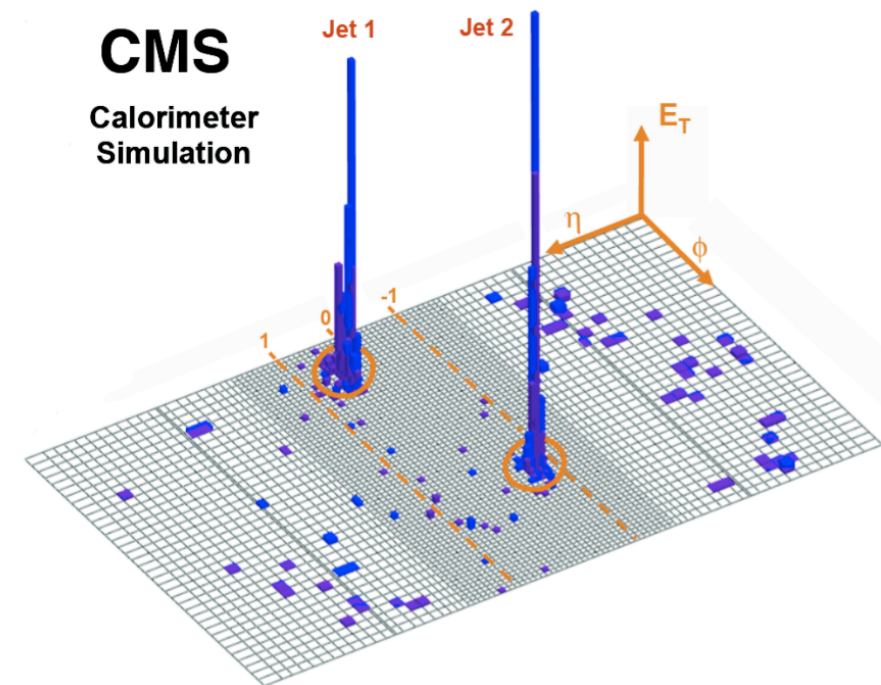
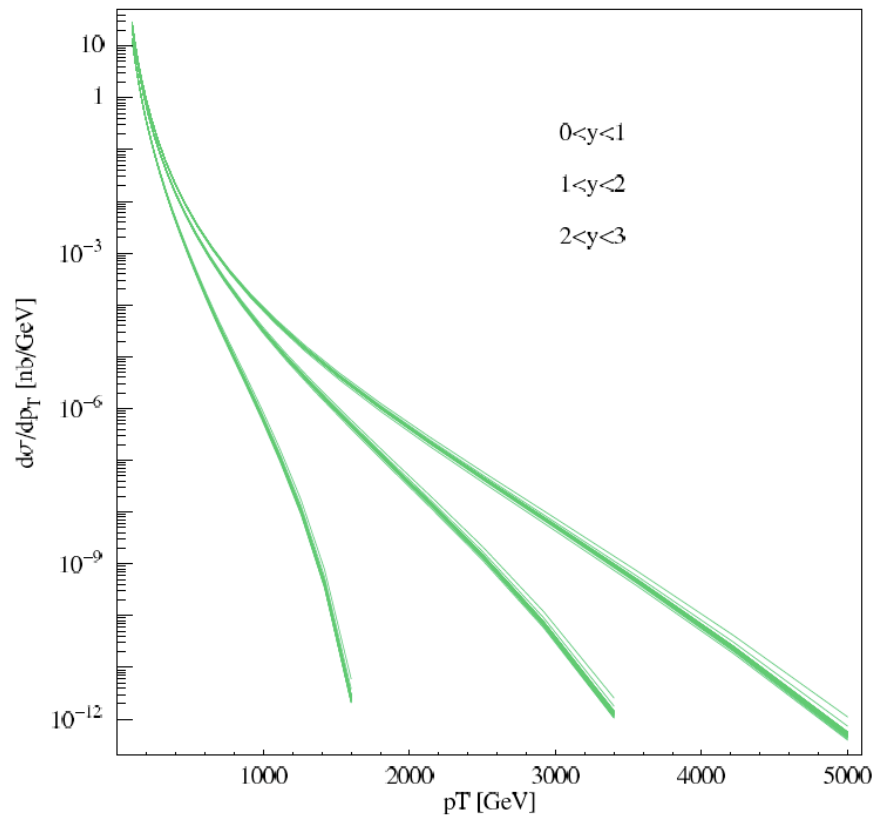
JET PHYSICS: RESULTS OVERVIEW



- Jet physics is a well-established and well-understood field.
- Excellent basis for QCD studies at the LHC.
 - Some difficult phase space regions.
- Note that jets are of more importance than “only” for QCD studies.

JET PHYSICS: LHC

- Will have jets up to several TeV!
 - Factor 10 higher energies than at the Tevatron!
 - Massive reach for QCD studies and ...



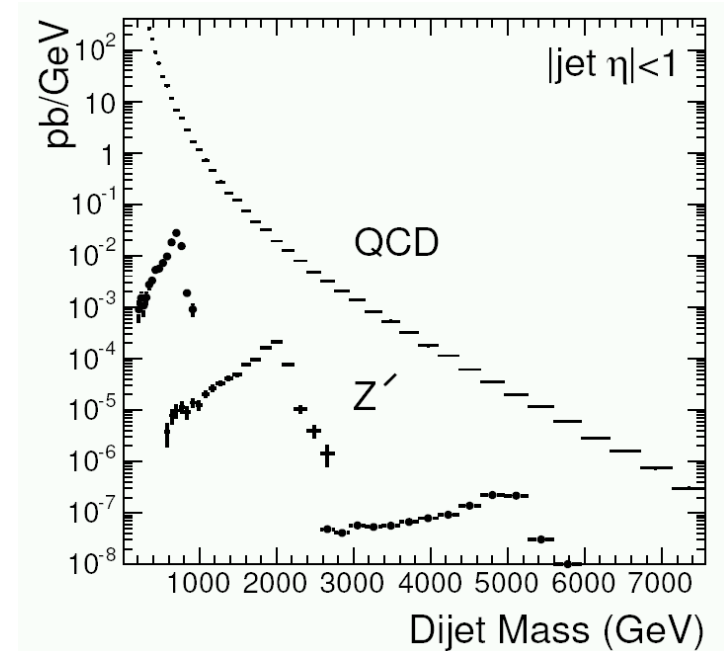
JET PHYSICS

> ... at different experiments:



- Jets play crucial role in many new physics scenarios

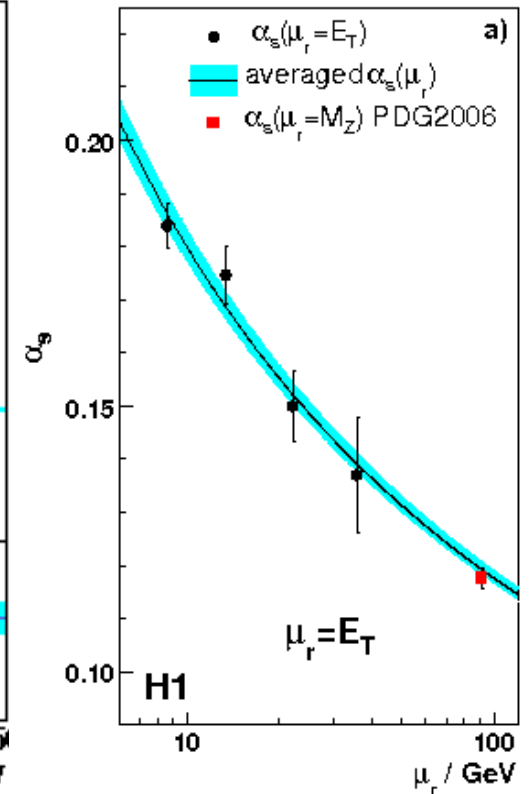
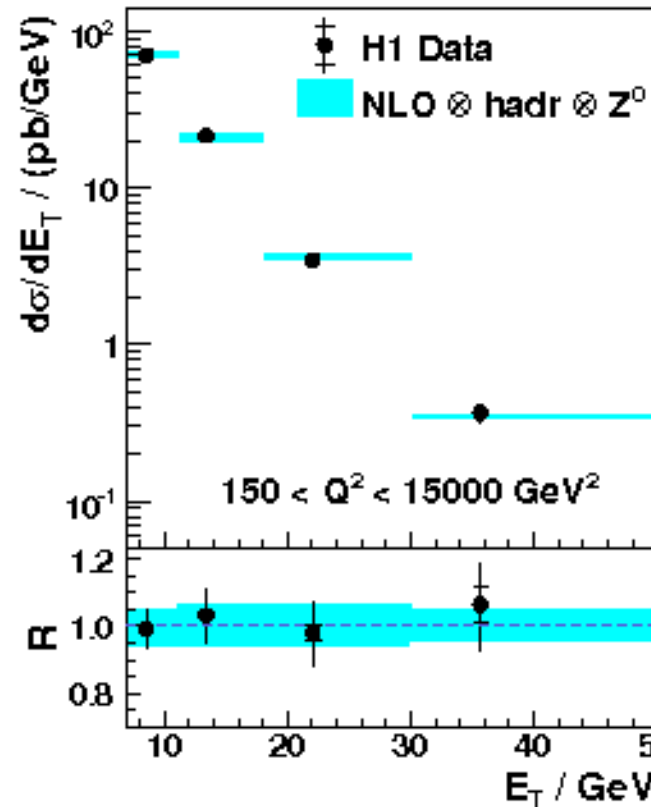
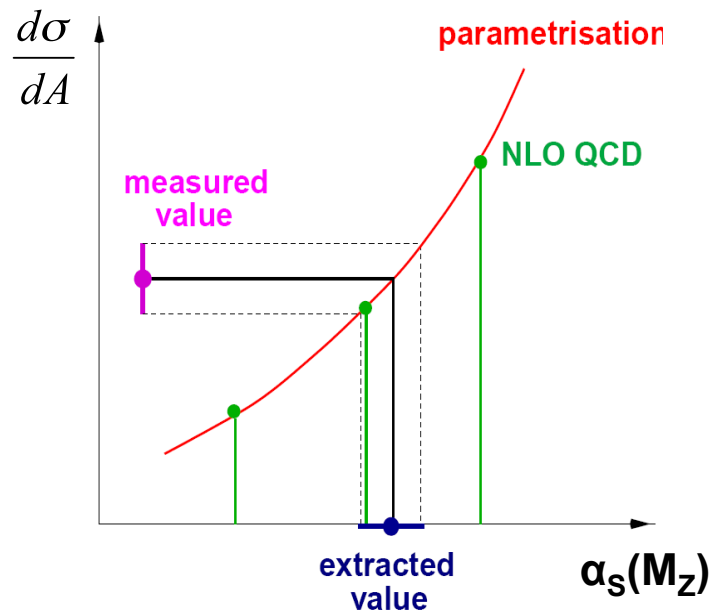
-
- The diagram illustrates a proton-proton collision. Two incoming protons, labeled 'p', interact at a vertex (represented by a yellow star). This interaction produces a gluon (g) and a quark (q). The gluon (g) then interacts with a gluino (g̃) and a squark (q̃). The quark (q) interacts with a gluino (g̃) and a squark (q̃). The gluino (g̃) and squark (q̃) then interact with a gluino (g̃) and a squark (q̃). Finally, the gluino (g̃) and squark (q̃) decay into a gluon (g) and a quark (q). The diagram uses various colors and line styles to represent different particles and interactions.



JETS AND THE STRONG COUPLING

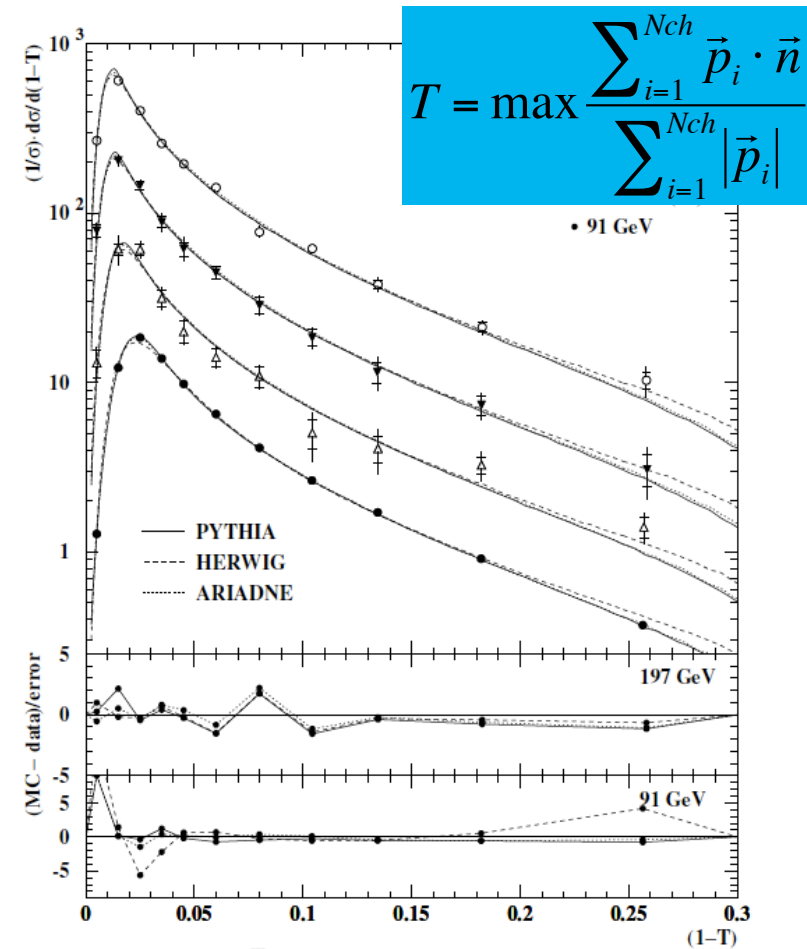
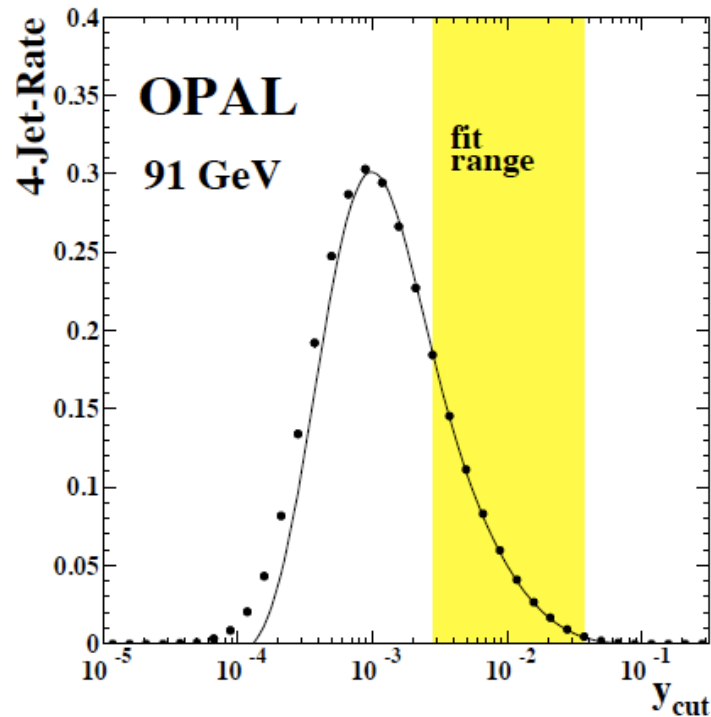
> One example: HERA jet data

$$\left. \frac{d\sigma(\alpha_s(M_Z))}{dA} \right|_{NLO} = C_1 \alpha_s(M_Z) + C_2 \alpha_s^2(M_Z)$$



THE STRONG COUPLING: e+e- EXAMPLES

> Thrust, and the four-jet rate



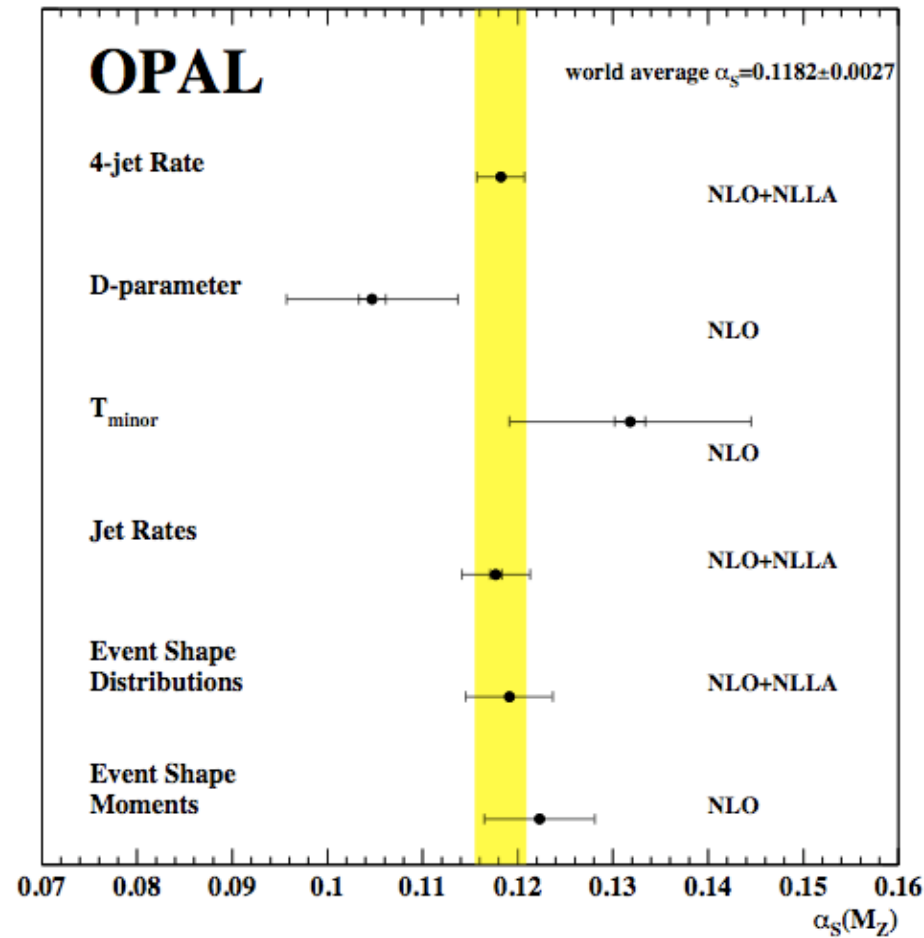
$$T = \max \frac{\sum_{i=1}^{Nch} \vec{p}_i \cdot \vec{n}}{\sum_{i=1}^{Nch} |\vec{p}_i|}$$

$$\ln R_{\mathcal{O}(\alpha_s^2)}(y) = \mathcal{A}(y)\bar{\alpha}_s + \left[\mathcal{B}(y) - \frac{1}{2}\mathcal{A}(y)^2 \right] \bar{\alpha}_s^2 + \mathcal{O}(\alpha_s^3)$$

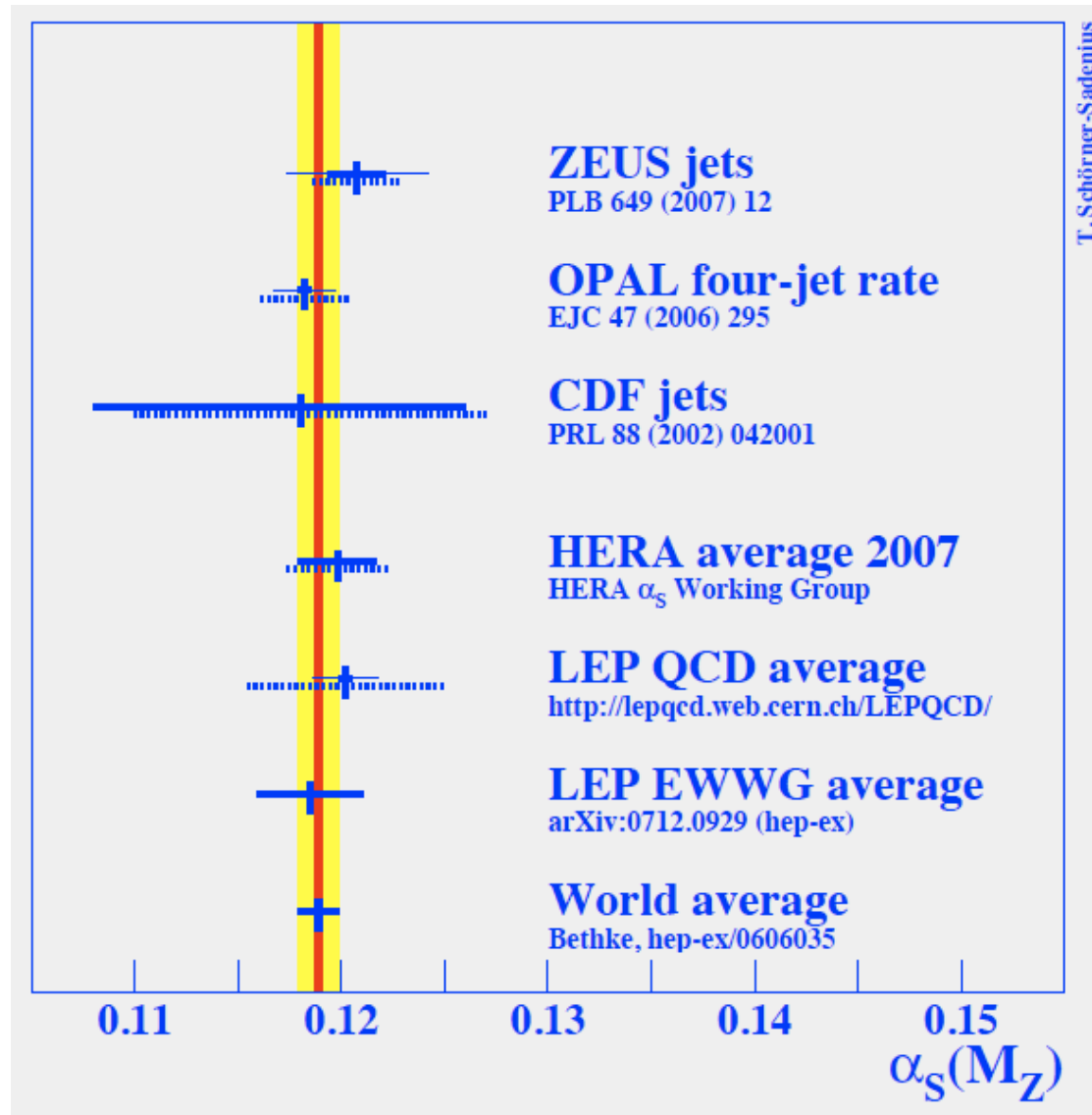
$$\ln R_{\text{NLLA}}(y) = Lg_1(\alpha_s L) + g_2(\alpha_s L) + C_1\bar{\alpha}_s + \left[C_2 - \frac{1}{2}C_1^2 \right] \bar{\alpha}_s^2 + \mathcal{O}(\alpha_s^3)$$

THE STRONG COUPLING: e+e- EXAMPLES

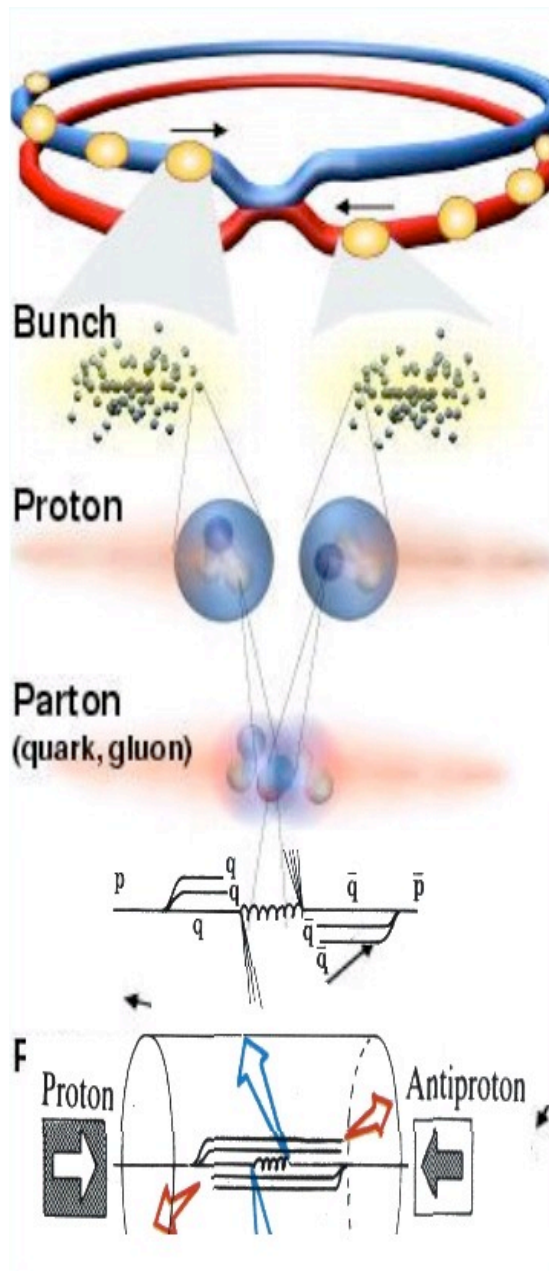
➤ Extracted values of the strong coupling:



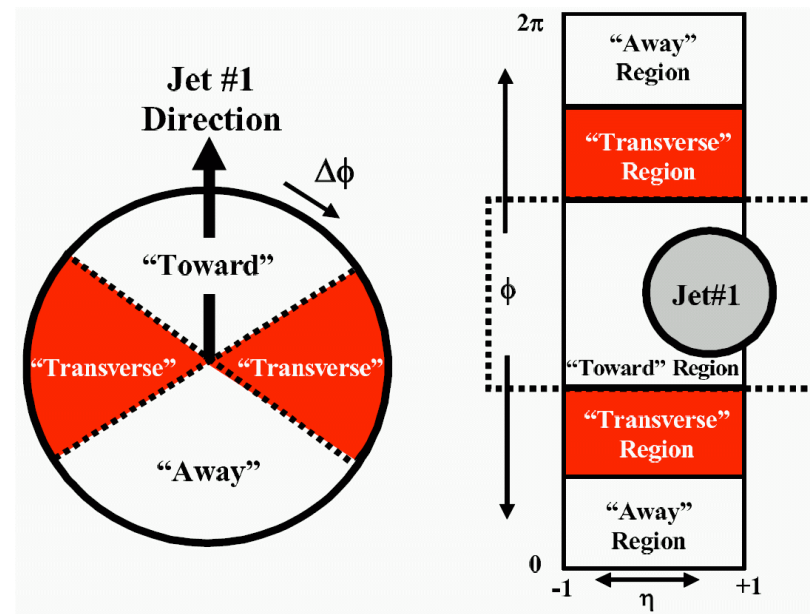
THE STRONG COUPLING: SUMMARY



FEW SLIDES: THE UNDERLYING EVENT



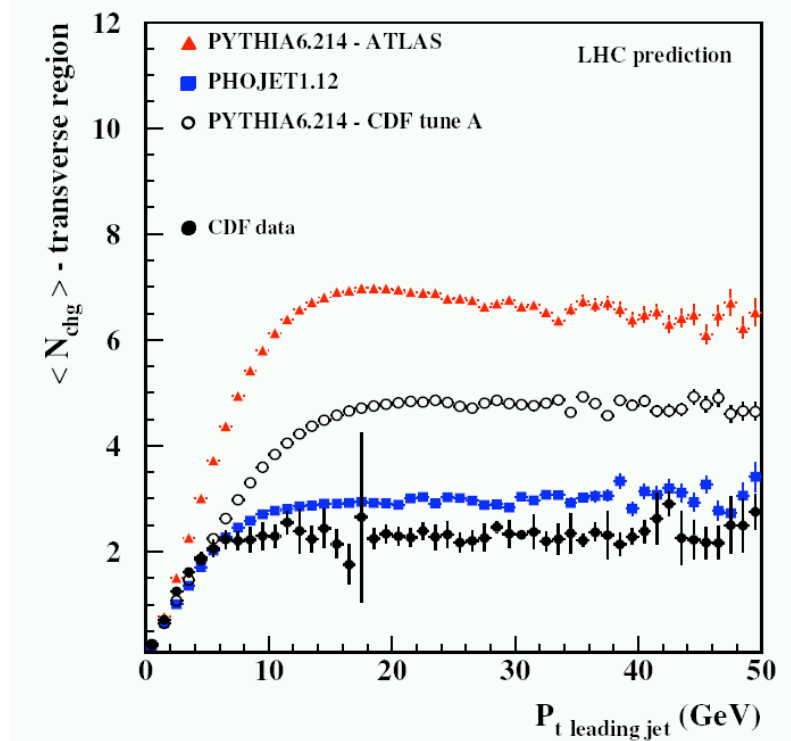
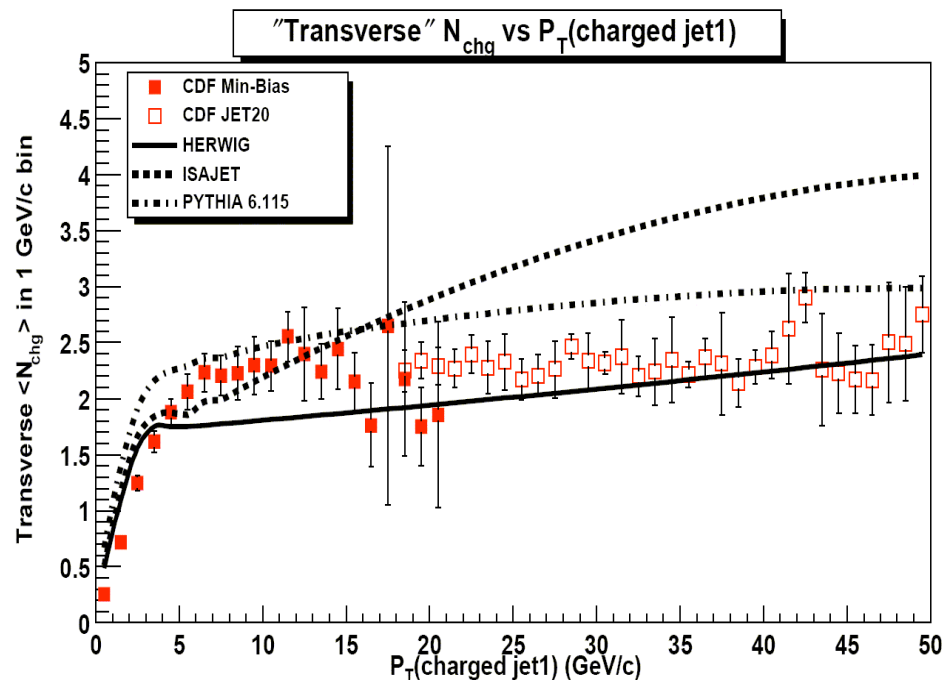
- Possibility of multi-parton interactions (and also pile-up)
 - Potentially large impact on analyses!
 - Study using for example energy flow in different regions.



FEW SLIDES: THE UNDERLYING EVENT

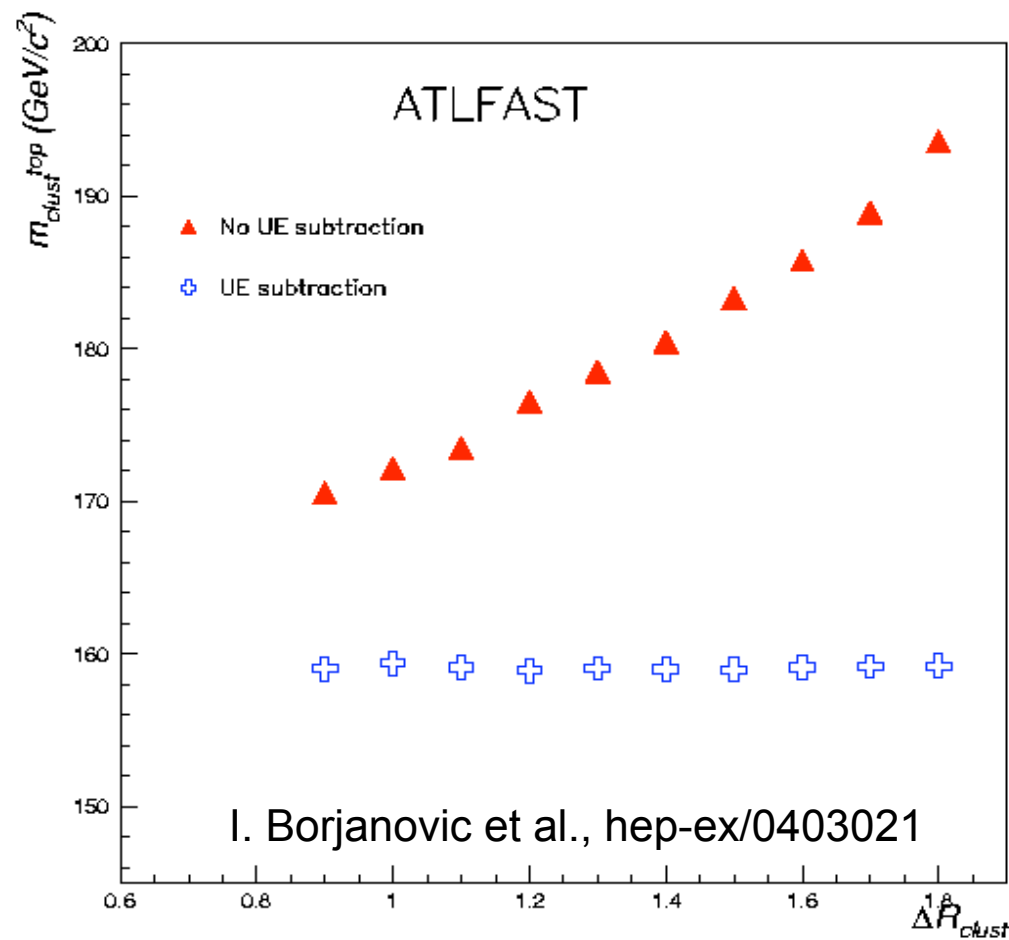
➤ Studies at the Tevatron (and also at HERA)!

- Models can describe data ...
- ... but fail in interpolation to LHC energies!



FEW SLIDES: THE UNDERLYING EVENT

- Impact on top mass reconstruction!



SUMMARY

- > QCD was a major topic at all previous and running high-energy colliders – and continues to be important at the LHC
 - Signal
 - Background
- > QCD has many different aspects:
 - Particle production
 - Jet physics
 - Determination of QCD parameters like strong coupling α_s .
- > Jet physics is a very interesting topic
 - QCD at highest scales
 - Discovery potential for new physics
 - Question of algorithms, calibration, uncertainties,
- > Many other aspects of QCD (at the LHC) not covered here ...
- > Now enjoy the QCD/jets tutorial!