

$$\left| \rho(t') \right\rangle \equiv \mathcal{U}(t', t) \left| \rho(t) \right\rangle$$