

$$I = \lim_{\epsilon \rightarrow 0} \left[ \int_0^1 \frac{dx}{x} x^{-\epsilon} f(x) + \frac{1}{\epsilon} f(0) \right]$$