

$$|\rho^{\text{V}}_{\infty}) \approx - \int_t^{\infty} d\tau \, \textcolor{red}{v}_I^{(\epsilon)}(\textcolor{red}{\tau}) |\rho(t))$$