



Generative Models in High Energy Physics

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Conclusions

Generative Models are powerful techniques

Object of an intense R&D , require careful **validation**

Many applications in High Energy Physics

Simulation is one of the main applications

High level of **accuracy** & **speed**

Multiple features/capabilities

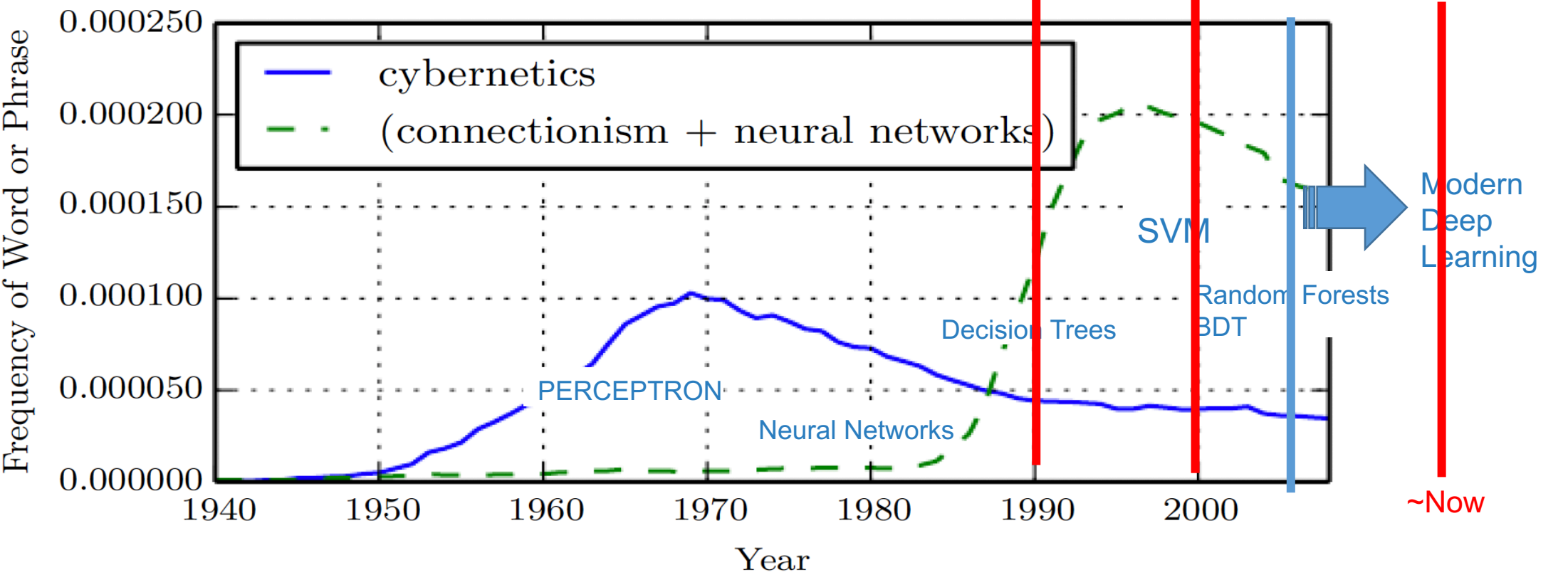
Deep Learning is a driving force toward changing our computing model

DL workloads are HPC friendly

Benefit from dedicated hardware and accelerators

Some background

Image from "Deep Learning", I. GoodFellow, MIT press book



Theories on biological learning
First linear models
Layer-wise pre-training through greedy algorithms

Back-propagation

Deep Learning in HEP

DL **recognize patterns** in large complicated data sets

Better performances if applied directly to **raw data**

Re-cast physics problems as “DL problems”

Detector output as **images** and apply **computer vision** techniques

Physics events as **sentences** and apply NLP techniques

Intense R&D activity

Performance requirements

Model **interpretability**

Results **Validation** against classical methods

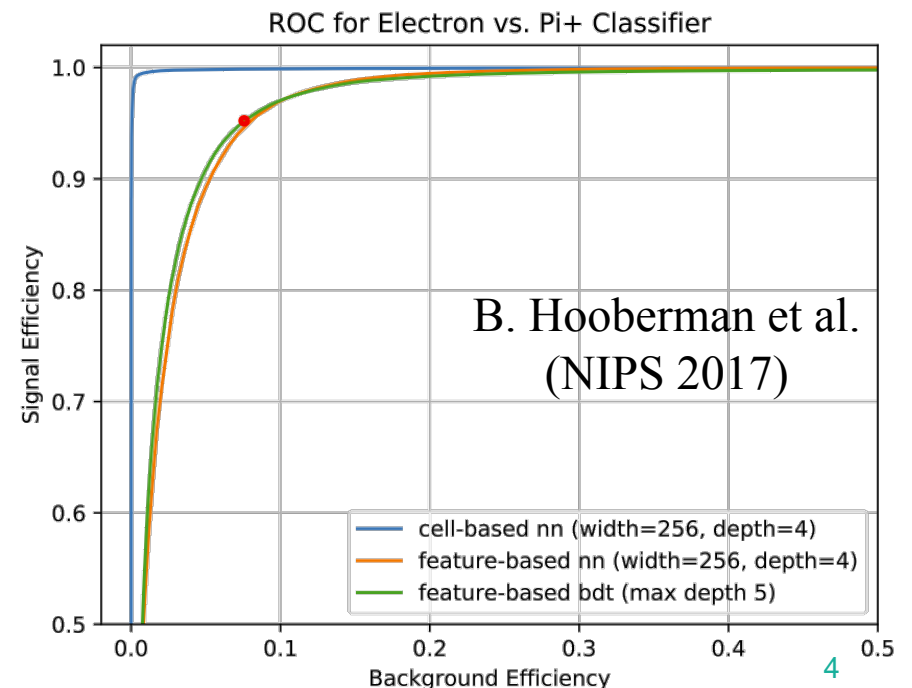
Detailed **Systematics studies**

“New” **computing models**

Accelerators and dedicated hardware

HPC integration

Cloud environment & **Big Data** platforms

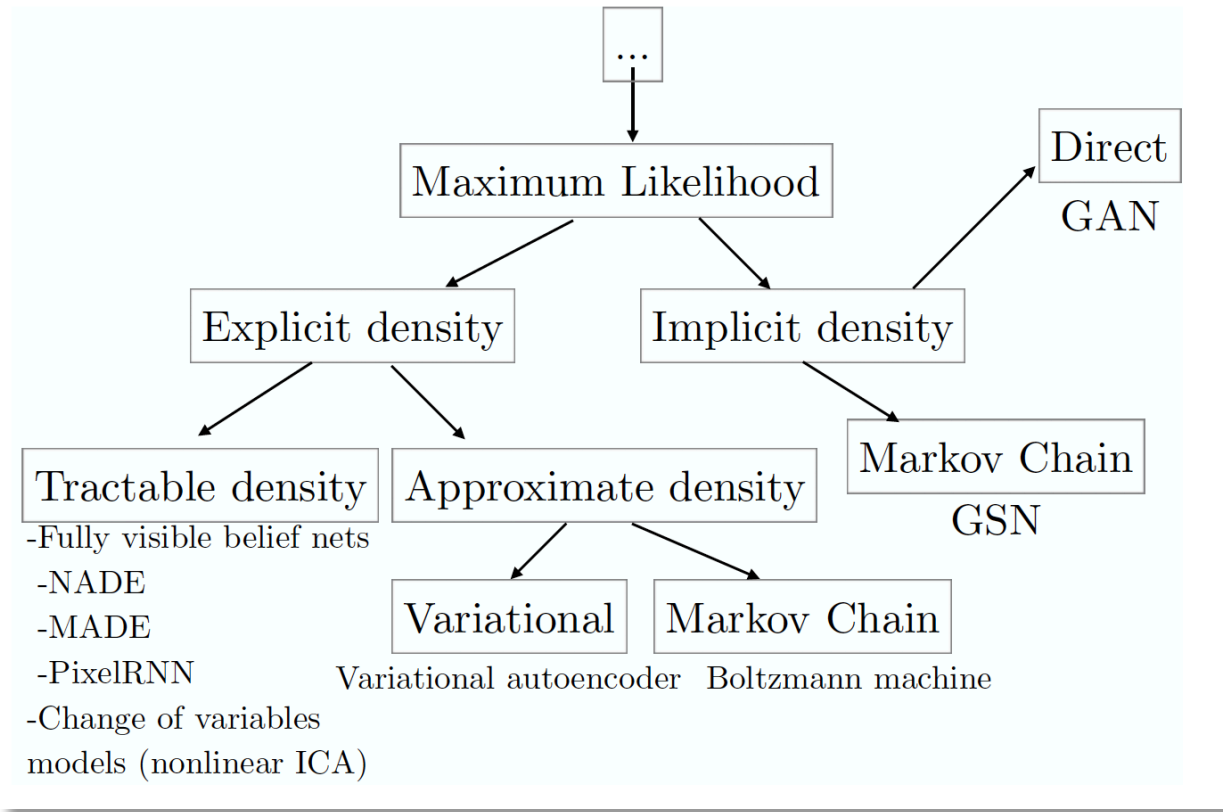


Generative Models

Basic concepts

Some references:

- NIPS 2016 Tutorial on Generative Adversarial Networks, I. Goodfellow
- [2018 Generative Models tutorial, D. Rezende](#)
- [2019 Stanford course on Deep Generative Models](#)



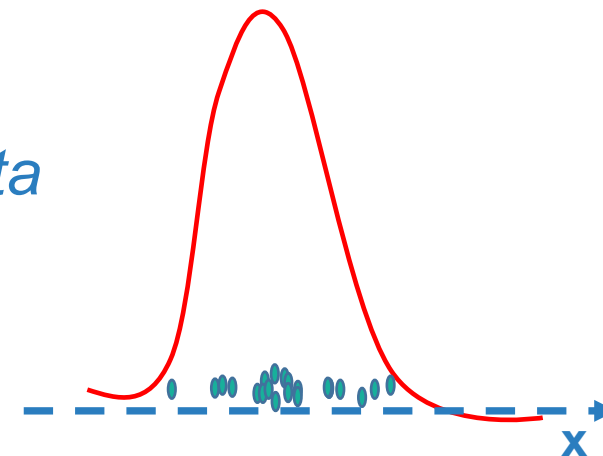
“GM Taxonomy” Image from NIPS 2016 Tutorial, I. Goodfellow

GM as Density Estimators

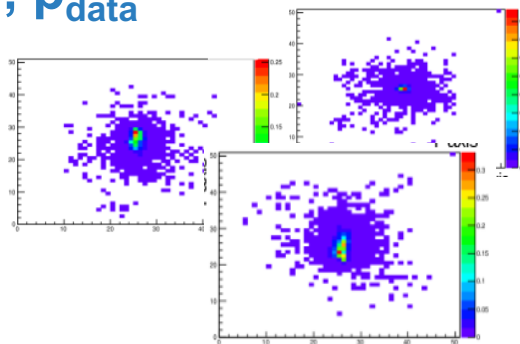
Generative models learn probability distributions from data

Given a collection of **samples** $\mathbf{x}_i$ and the underlying $\mathbf{p}_{\text{data}}$ **distribution**

Choose parameters $\{\theta\}$ so that $\mathbf{p}_{\{\theta\}}(\mathbf{x}) \approx \mathbf{p}_{\text{data}}$



$\{\mathbf{x}_i\}$, $\mathbf{p}_{\text{data}}$

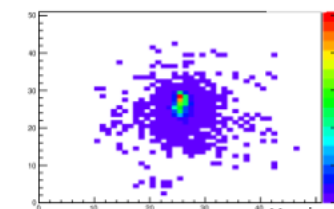


$\mathbf{P}_{\{\theta\}}(\mathbf{x})$

Neural
Network



New samples



Prior knowledge?

Generative models use **some** prior knowledge



Extract meaningful **representations** directly from data but need:

Loss functions

Learning principle

Optimisation algorithms

Domain knowledge

Probability divergence $D(p,q)$

Name	Formula
f -divergences	$D(p; q) = \mathbb{E}_q[f(\frac{q}{p})]$
Relative entropy (KL)	$D(p; q) = \mathbb{E}_q[\ln \frac{p}{q}]$
Jensen-Shannon (JS)	$D(p; q) = \frac{1}{2}\text{KL}(p; m) + \frac{1}{2}\text{KL}(q; m)$
Stein divergence	$D(p; q) = \sup_f \mathbb{E}_q[\nabla \ln p f + \nabla f]^2$
Energy distance	$D(p; q) = \mathbb{E}[2\ x - y\ - \ x - x'\ - \ y - y'\]$
Wasserstein distance	$D_\alpha(p; q) = [\inf_\rho \mathbb{E}_\rho[\ x - x'\ ^\alpha]]^{\frac{1}{\alpha}}$
Max-min dis. (MMD)	$D(p; q) = \sup_f (\mathbb{E}[f]_p - \mathbb{E}[f]_q)$

Multiple Applications

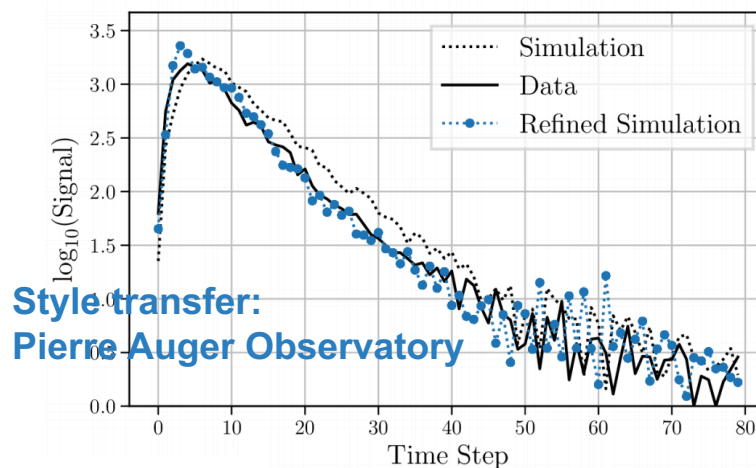
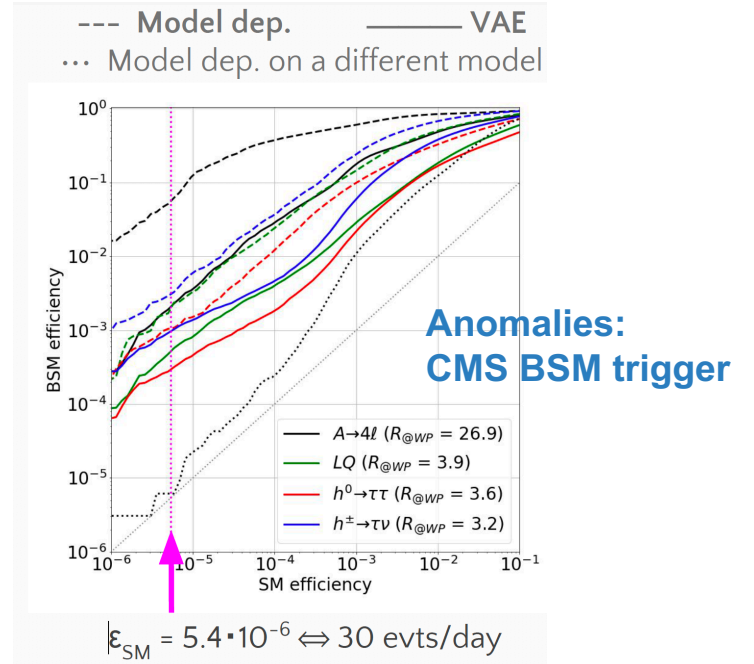
Event sampling (**Simulation**)

Find Underlying Factors (**Discovery**)

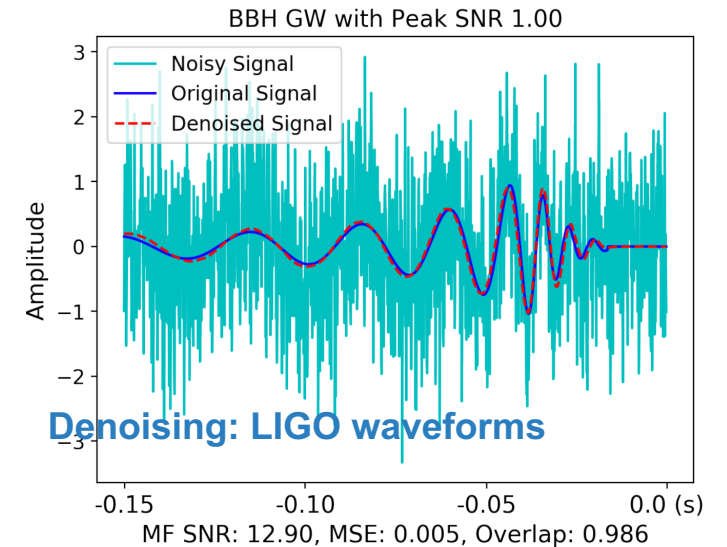
Detect Rare events (**Anomaly Detection**)

Predict future events (**Planning**)

Find Analogies (**Transfer Learning & Style Transfer**)



arXiv:1802.03325



Shen H, 2017 (Preprint 1711.09919)

(Deep) Generative Models

Internal representations learned by shallow systems are simple (Bengio & LeCun 2007, Bengio 2009)

Incapable of learning complex hidden structures

Large amounts of labeled data

→ Deep Generative Models

→ Higher levels of abstraction

→ Improved generalisation and transfer

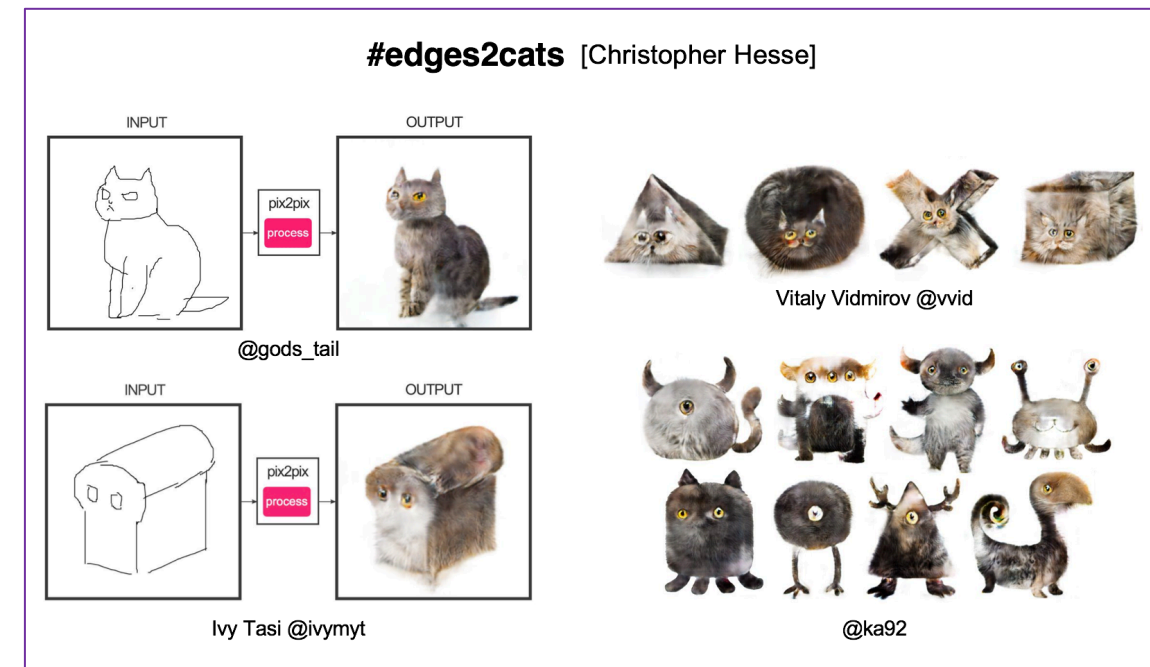
→ Categorized according to

→ Feature representation

→ Fully observed, or latent variables based

→ Learning principles

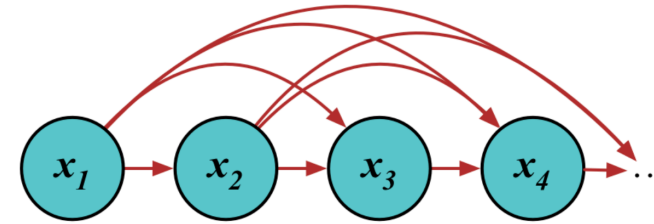
→ MLE, variational, or likelihood-free



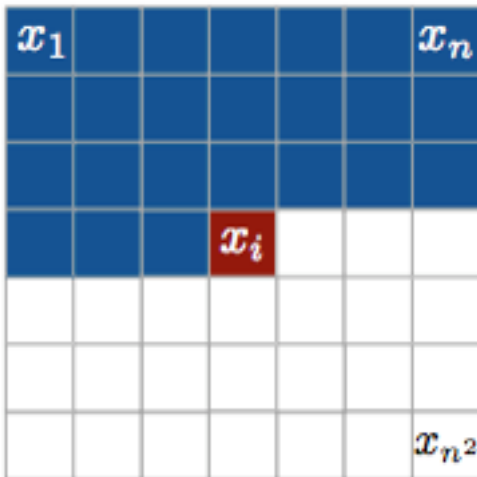
Fully Observed Models

Directly observe data without introducing new local (latent) variables

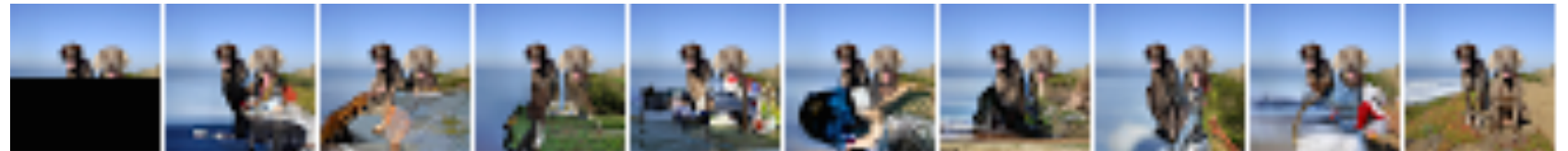
$$p(x_1, \dots, x_N) = \prod_{i=1}^N p(x_i | x_1, \dots, (i-1))$$



Ex. Pixel Recurrent Neural Networks:



$$p(x_t | x_{1:t-1}) = p(x_t^{red} | x_{1:t-1}) p(x_t^{green} | x_{1:t-1}, x_t^{red}) p(x_t^{blue} | x_{1:t-1}, x_t^{red}, x_t^{green})$$



Latent Variables models

Unsupervised representation learning

Introduce an **unobserved random variable** for every observed data point to **explain features**.

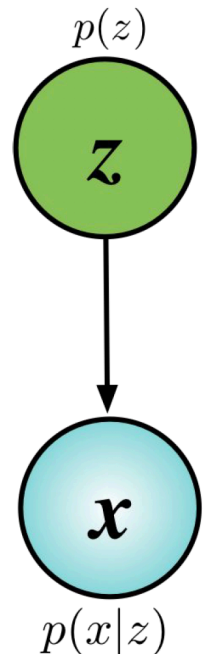
Prescribed models: Use observer likelihoods and assume observation noise.

Implicit models: Likelihood-free models.



$$x \in \mathbb{R}^{d_x} \quad z \in \mathbb{R}^{d_z} \quad \theta \in \mathbb{R}^{d_\theta}$$
$$\mathcal{D} = \{x_i\} \quad i \in \{1, \dots, N\}$$

$$\log p_\theta(x) = \log \int p_\theta(x|z)p(z)dz = \log \mathbb{E}_{p(z)}[p_\theta(x|z)]$$
$$\log p_\theta(\mathcal{D}) = \sum_{i=1}^N \log \mathbb{E}_{p(z)}[p_\theta(x_i|z)]$$



Variational AutoEncoders

Describe training dataset in latent space

Explicit constraints on the encoded representations

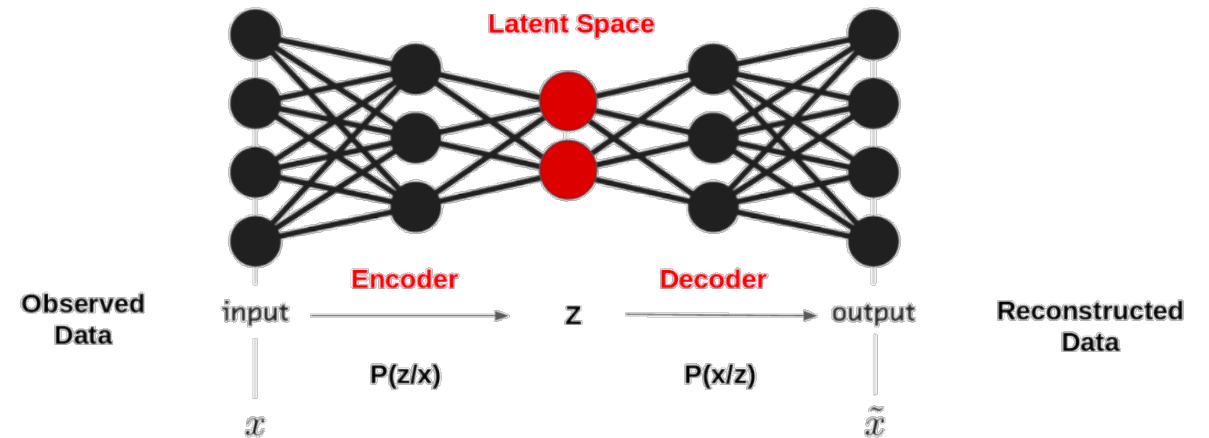
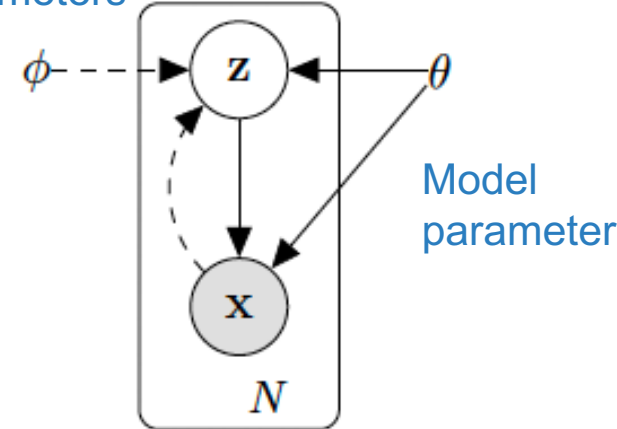
Learn the **latent variable distribution**

Two components in the loss function

reconstruction loss

KL divergence between the learned latent distribution and the prior regularization

Variational parameters



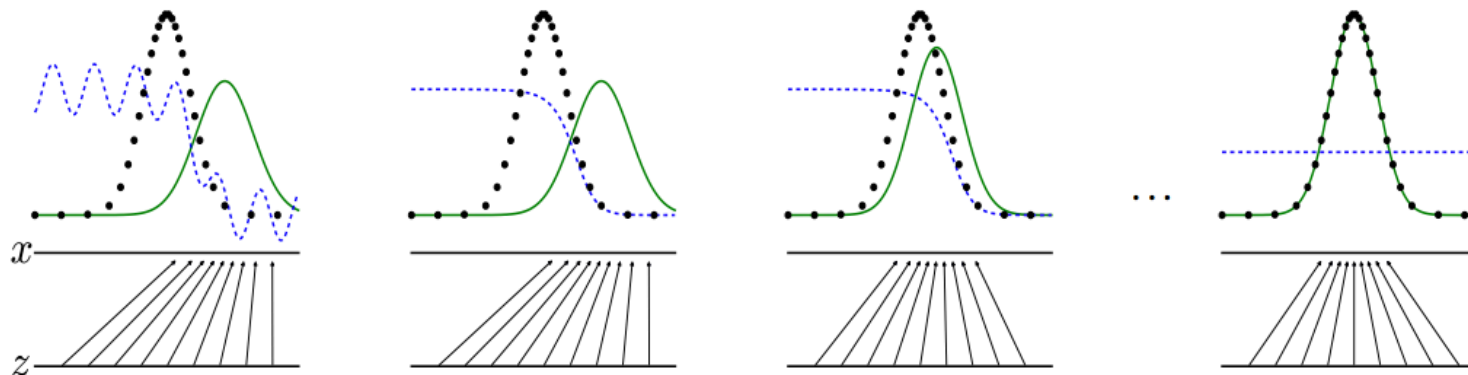
Likelihood-free learning

Density estimation by comparison

Compare the **estimated distribution** $q(x)$ to the **true distribution** $p^*(x)$ using samples.

Build an **auxiliary model** to indicate how data simulated from the generative model differs from observed data.

Adjust model parameters to better match the data distribution



Adversarial training

Assume a deterministic generator: $\mathbf{x} = G_{\theta}(\mathbf{z})$

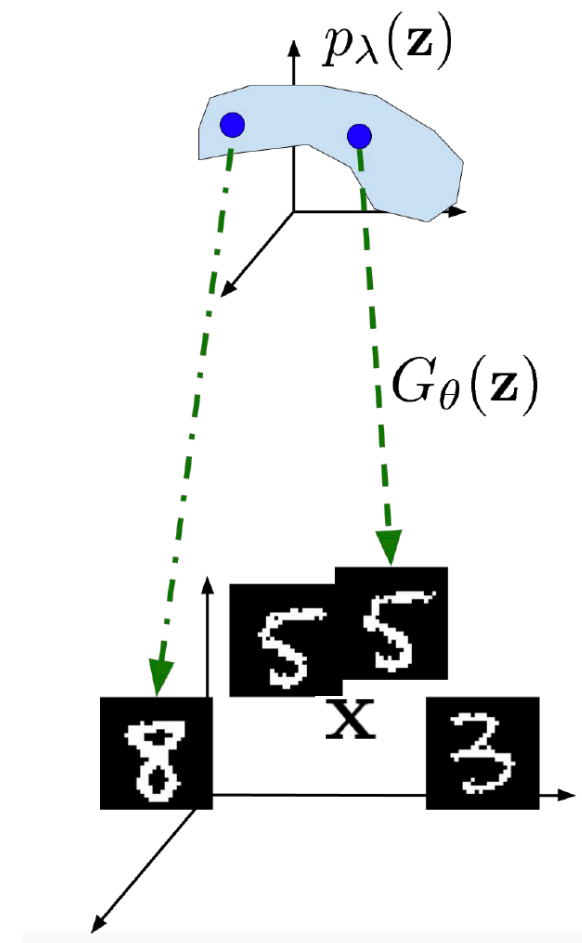
A prior over latent space: $\mathbf{z} \sim p_{\lambda}(\mathbf{z})$

Define a discriminator: $D_{\psi}(\mathbf{x}) \in [0, 1]$

A learnable loss function from the min-max game

$$\min_{\theta} \max_{\psi} \mathbb{E}_{\mathbf{x} \sim p_{data}} [\ln D_{\psi}(\mathbf{x})] - \mathbb{E}_{\mathbf{z} \sim p_{\lambda}(\mathbf{z})} [\ln (1 - D_{\psi}(G(\mathbf{z})))]$$

$$\min \max \quad \mathbf{E}_{x \sim \mathcal{D}_{real}} [D_{\psi}(x)] - \mathbf{E}_h [D_{\psi}(G_{\theta}(h))]$$



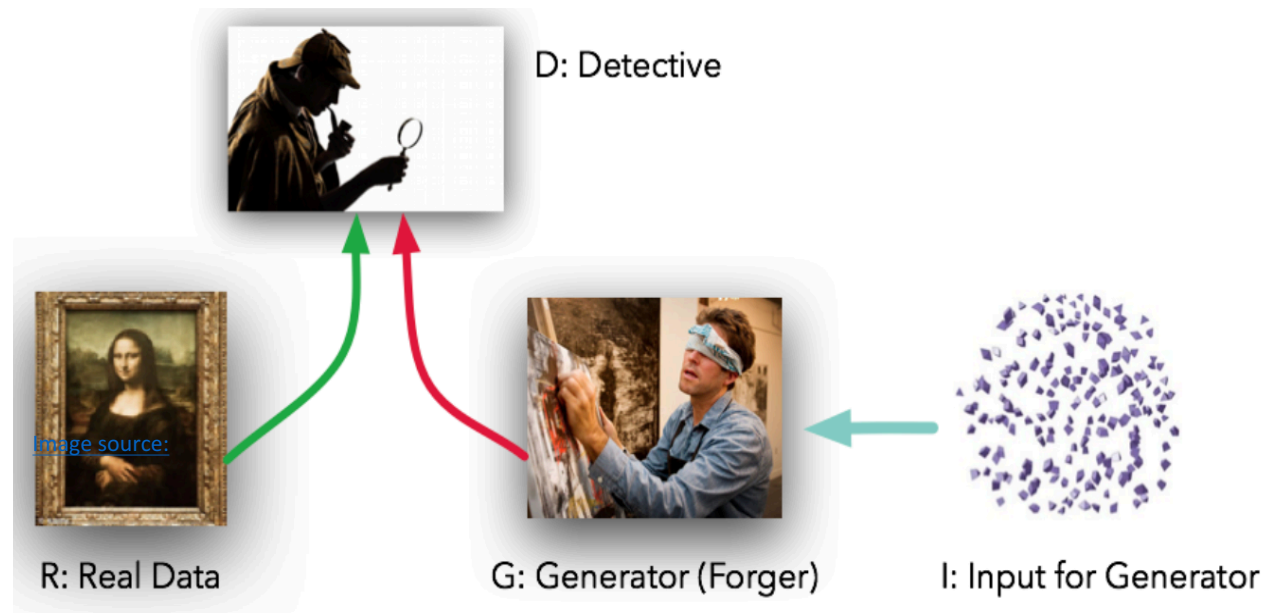
Wasserstein loss

Generative adversarial networks

Simultaneously train two networks that compete and cooperate with each other

Generator G generates data from random noise

Discriminator D learns how to distinguish real data from generated data



<https://arxiv.org/pdf/1701.00160v1.pdf>

Multiple GAN flavors

Different base layers technologies:

Original GAN was based on MLP in 2014

Deep Convolutional GAN in 2015

Graph GAN

Recurrent -GAN

Different “information paths”

Conditional GAN

Extended to learn a parameterized generator $p_{\text{model}}(x|\theta)$

Useful to obtain a single generator object for all θ configurations

Interpolate between distribution

Auxiliary Classifier GAN

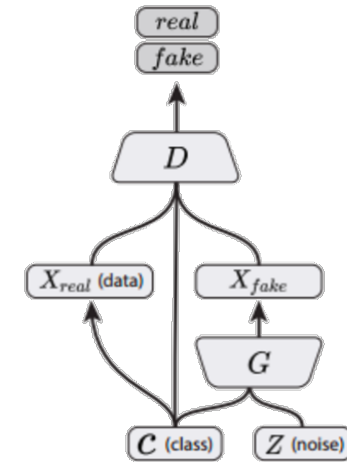
D can assign a class to the image

Progressive growing GAN

VAE-GAN

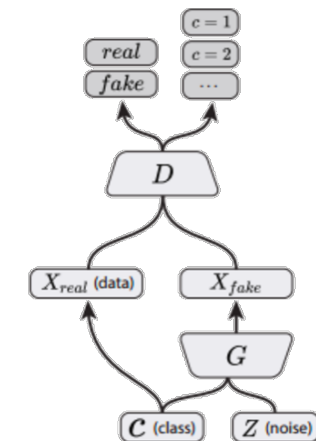
Stack GAN

BiGAN



Conditional GAN
(Mirza & Osindero, 2014)

[arXiv: 1411.1784](https://arxiv.org/abs/1411.1784)



AC-GAN
(Present Work)

[arXiv:1610.0958](https://arxiv.org/abs/1610.0958)

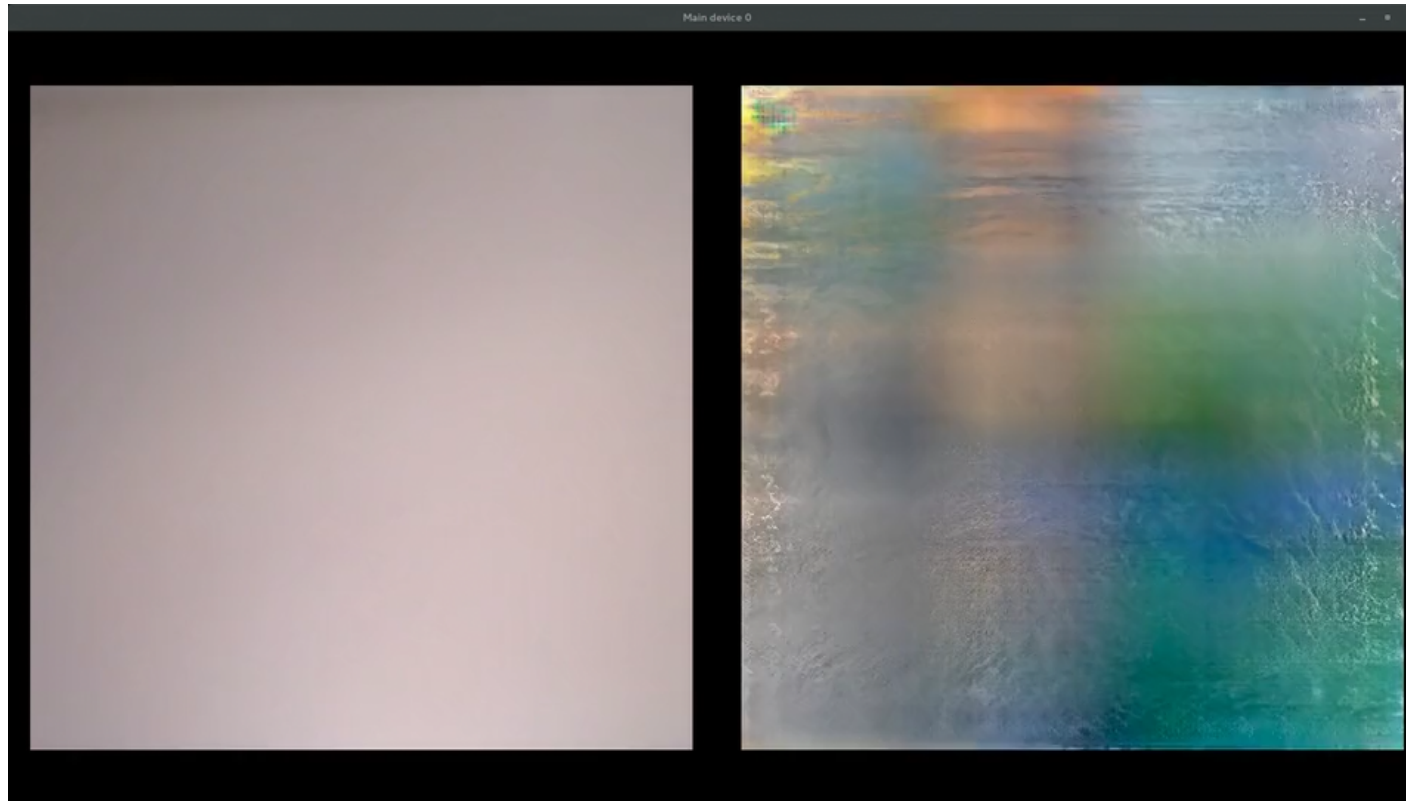


<https://thispersondoesnotexist.com/>



GAN for Art?

Image-to-Image Translation with Conditional Adversarial Networks



Evaluating performance is tricky

Different applications

Density estimation

Sampling/generation

Latent representation learning

Custom task (i.e. image translation, compressions..)

Tractable likelihood models

Split dataset into train, validation, test sets

Evaluate gradients on **train** set

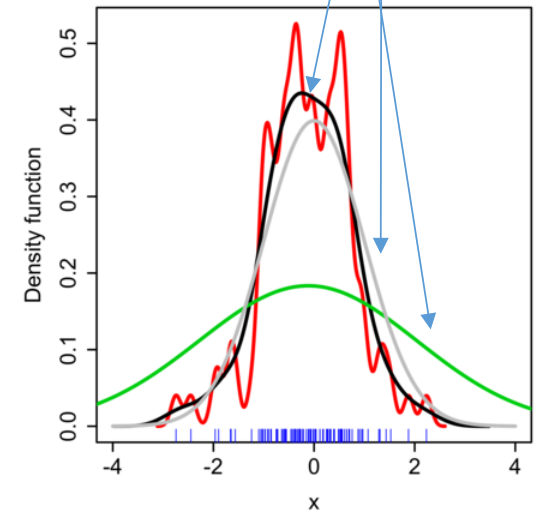
Tune hyperparameters on **validation** set

Evaluate generalization by reporting likelihoods on **test** set

Non-tractable likelihood or likelihood-free models

Use **lower bounds** or **approximations** (l,e ELBO, KDE)

$$\hat{p}(\mathbf{x}) = \frac{1}{n} \sum_{\mathbf{x}^{(i)} \in \mathcal{S}} K\left(\frac{\mathbf{x} - \mathbf{x}^{(i)}}{\sigma}\right)$$



GAN for simulation

Measure **convergence**

Evaluate difference between model PDF and real PDF

At convergence evaluate **sample quality**

Mixing and coverage (diversity)

Saliency

Mode collapse or mode dropping

Overfitting

Need quantities that are **invariant** to small translation, rotation, intensity changes

Simple pixel space Euclidean distances don't work

Define a way to **map input into a feature space**

Inception score

Maximum Mean Discrepancy

Fréchet Inception Distance

Structural Similarity Index

+ Physics Quantities Validation

Generated support space

Size of the dataset

GANs produce distributions with **limited support**

Support size grows ~linearly with discriminator size

Training dataset size does not help much for a given discriminator

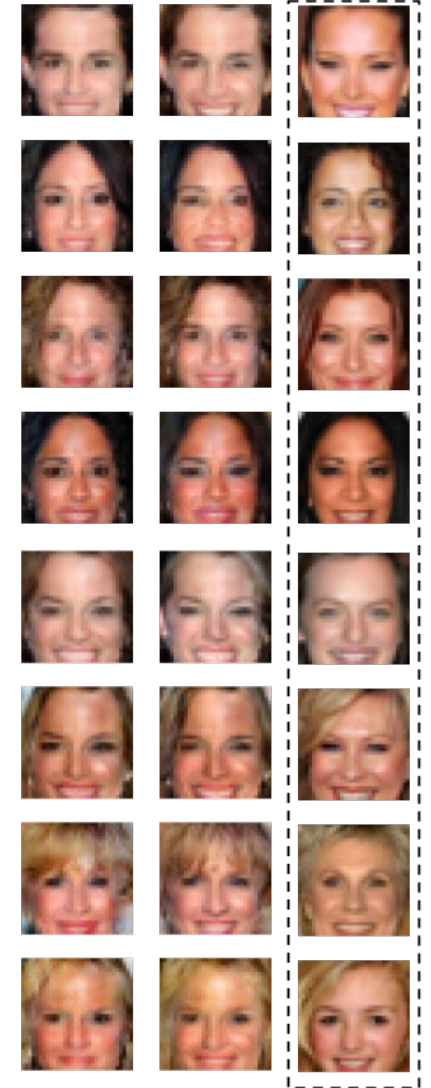
Example: BiGAN

support size is around 1M (training set ~200k)

Birthday paradox test*

If a sample of size s has near-duplicate images with prob $> 1/2$, then distribution has only s^2 distinct images.

Search for nearest neighbor

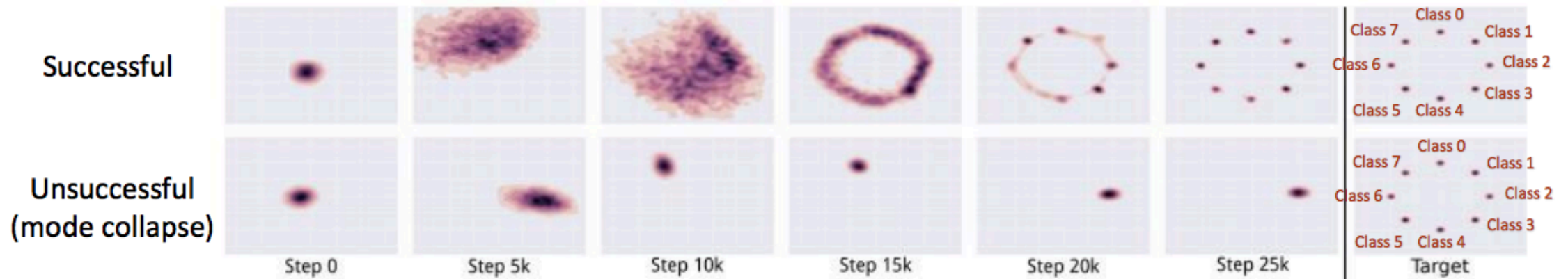


DCGAN

*Zhang A., ICML'17 21

One extreme case: Mode collapse

Goal is to generate fake examples imitating real sample
Simple solution is to just generate easy modes (classes).



Duality Gap

A natural metric in minimax games

For a given set of Discriminator and Generator: $(u^*, v^*) \in K_1 \times K_2$

$$\text{DualGap} := \max_{v \in K_2} M(u^*, v) - \min_{u \in K_1} M(u, v^*)$$

Fix **generator**, find most
adversarial **discriminator**

Fix **discriminator**, find most
adversarial **generator**

- Obtaining an unbiased estimate

1. Train a GAN and obtain (G^*, D^*)

(use a training set)

2. Find the worst D and G i.e.

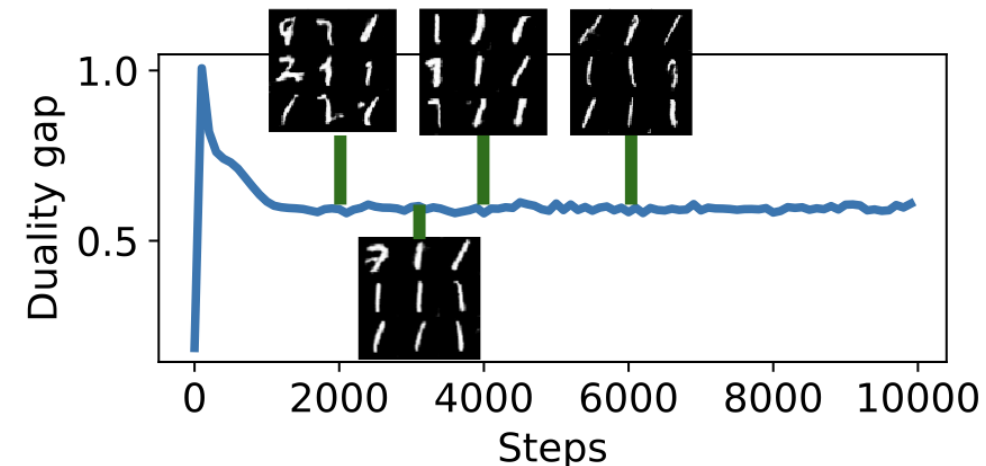
$$G_{\text{worst}} \leftarrow \arg \min_G M(G, D^*) \quad D_{\text{worst}} \leftarrow \arg \max_D M(G^*, D)$$

(use an adversary finding set)

3. Compute: $\text{DG} := M(G^*, D_{\text{worst}}) - M(G_{\text{worst}}, D^*)$

(use a test set)

Mode Collapse detection



Conclusions

Generative Models are powerful techniques

Object of an intense R&D , require careful **validation**

Many applications in High Energy Physics

Simulation is one of the main applications

High level of **accuracy & speed**

Multiple features/capabilities

Deep Learning is a driving force toward changing our computing model

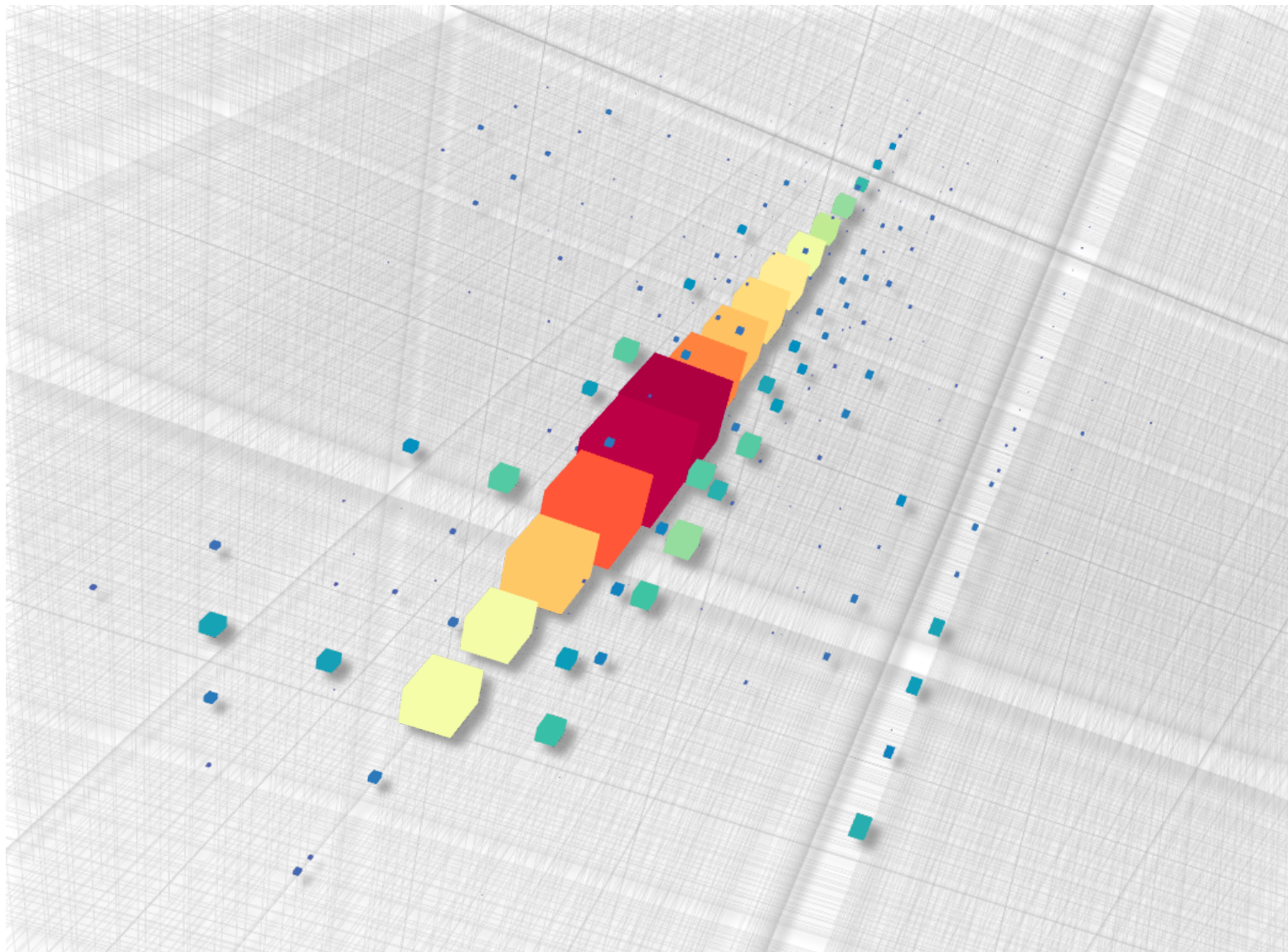
DL workloads are HPC friendly

Benefit from dedicated hardware and accelerators

3DGAN



Mission-Critical Computing
NSF CENTER FOR SPACE, HIGH-PERFORMANCE,
AND RESILIENT COMPUTING (SHREC)



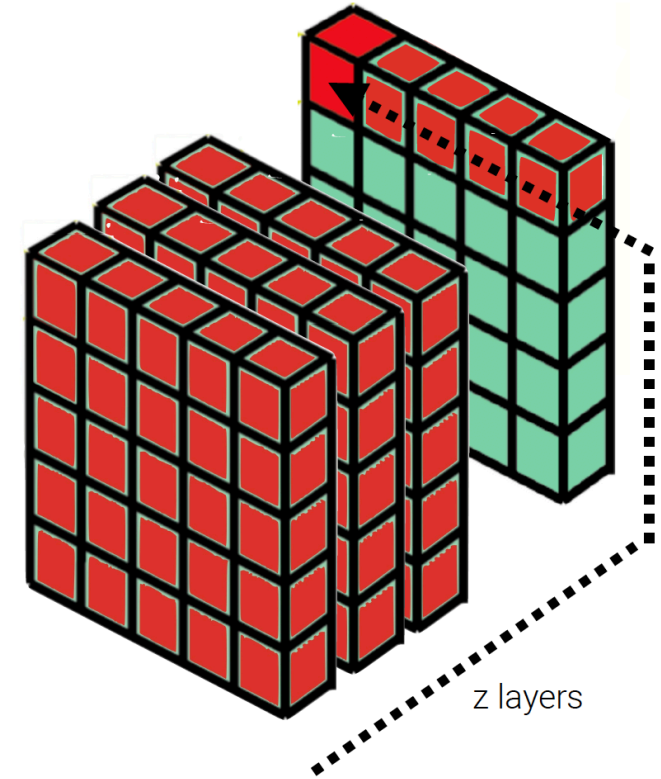
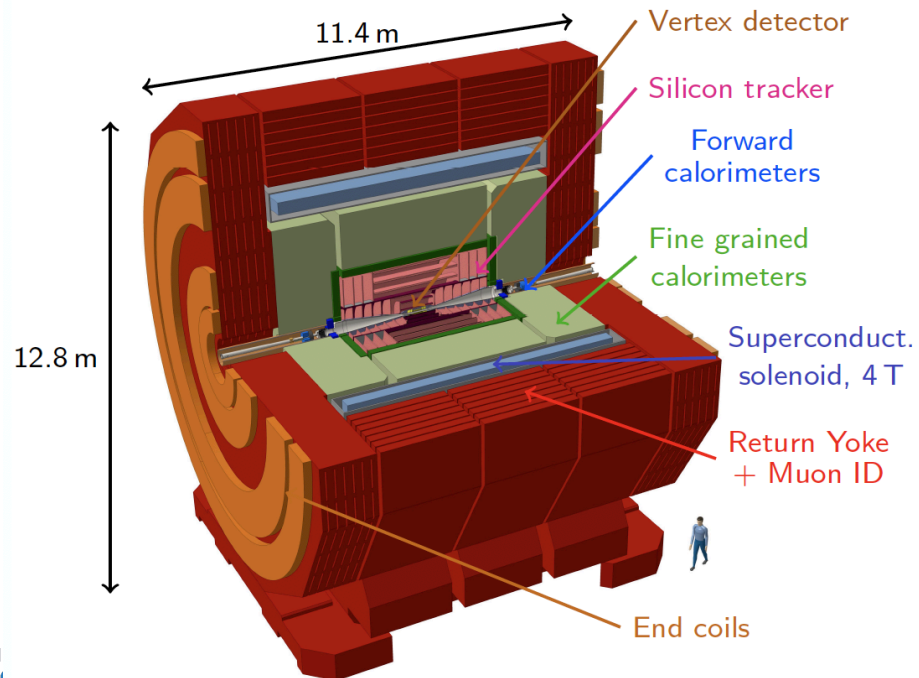
<https://openlab.cern/project/fast-simulation>

Compact Linear Collider

High-luminosity linear e^+e^- collider

Three energy stages up to 3 TeV

Associated detector studies



Electromagnetic calorimeter detector design

1.5 m inner radius

5 mm×5 mm segmentation

25 tungsten absorber layers + silicon sensors

High Granularity Calorimeter

Open data set developed for ML applications ⁽¹⁾

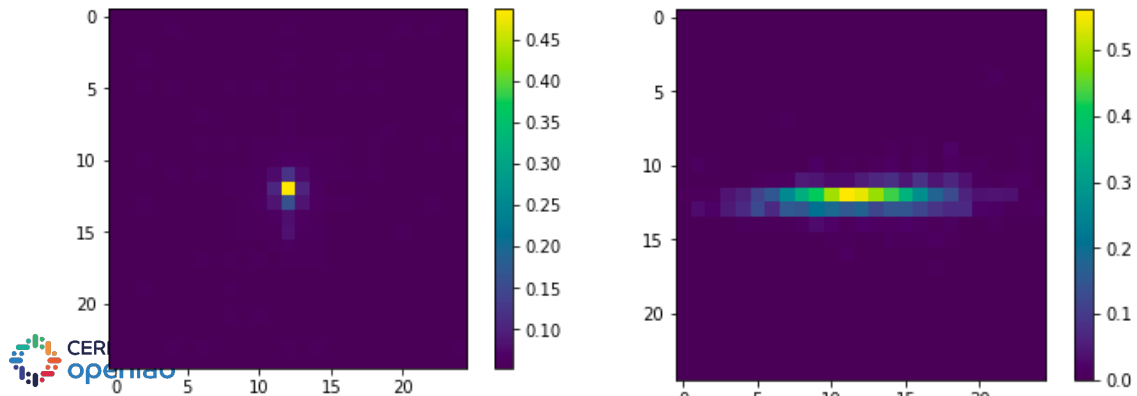
Pixelized detector volume to fully contain shower

1M single particle samples (e, γ , π) with flat energy spectrum (10-500) GeV

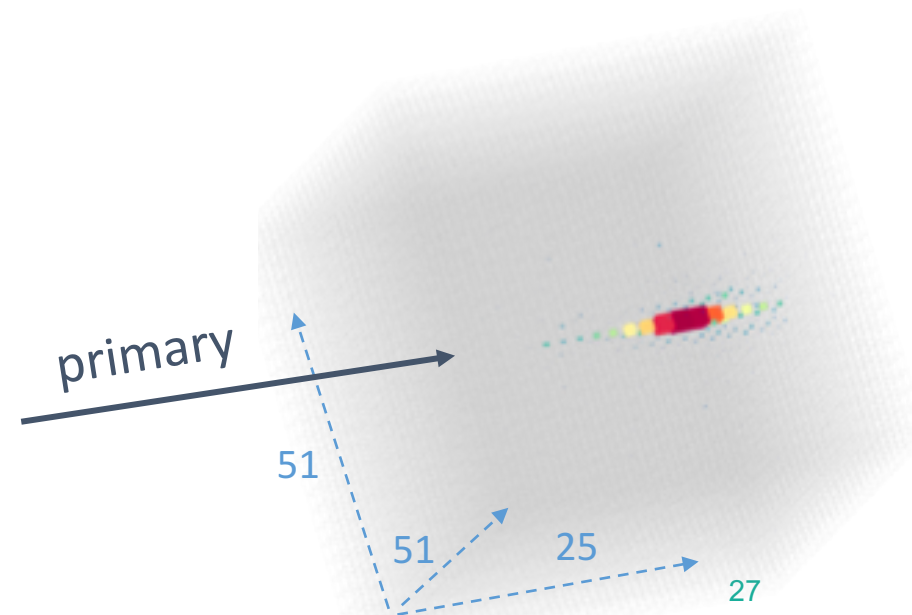
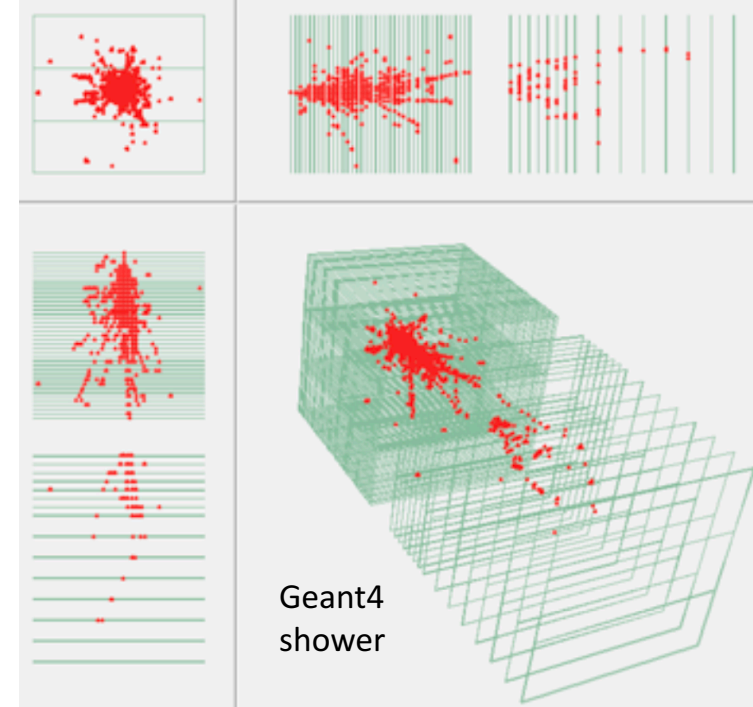
$\alpha = \pm 30^\circ$ random incident angle

Detector response as 3D images (51x51x25 pixels)

Large dynamic range, Sparsity



⁽¹⁾ M. Pierini et al. NIPS 2017

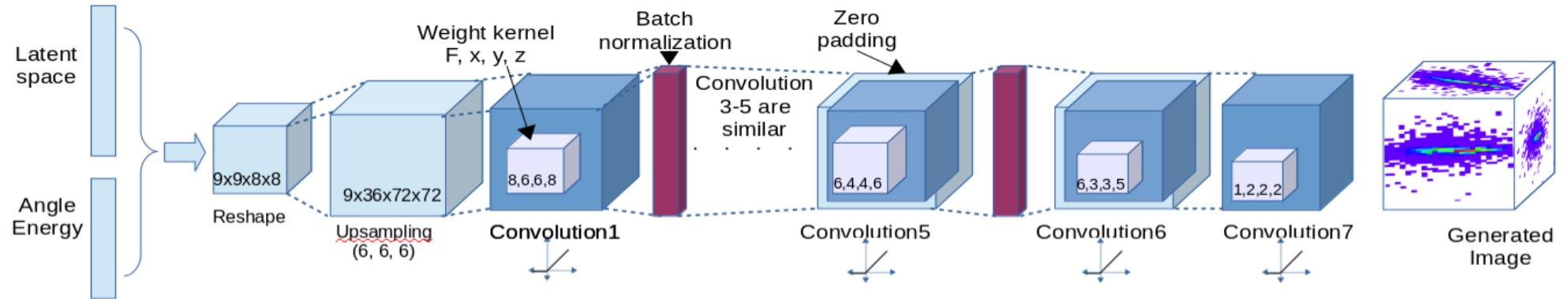


3D Generative Adversarial Networks

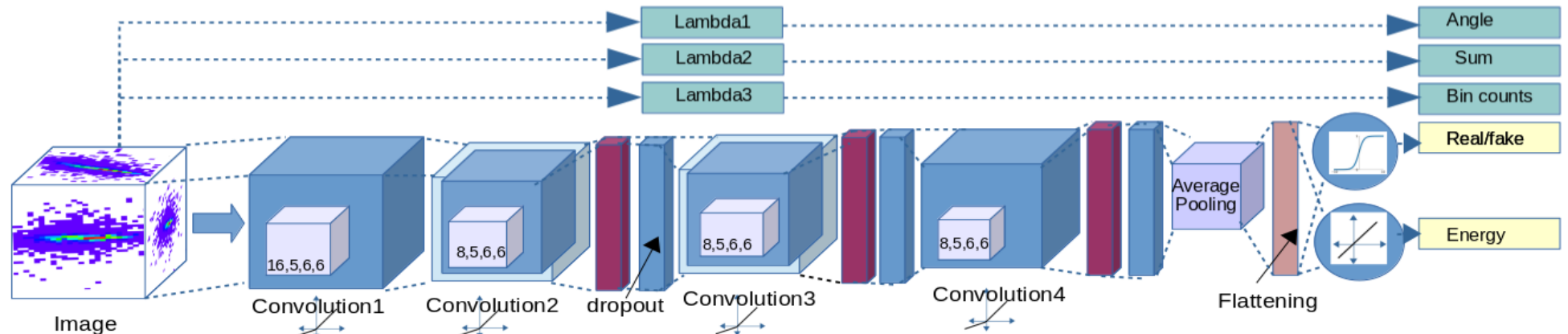
Condition training on input variables, **Custom losses**

Auxiliary regression tasks assigned to the discriminator

Generator:



Discriminator:



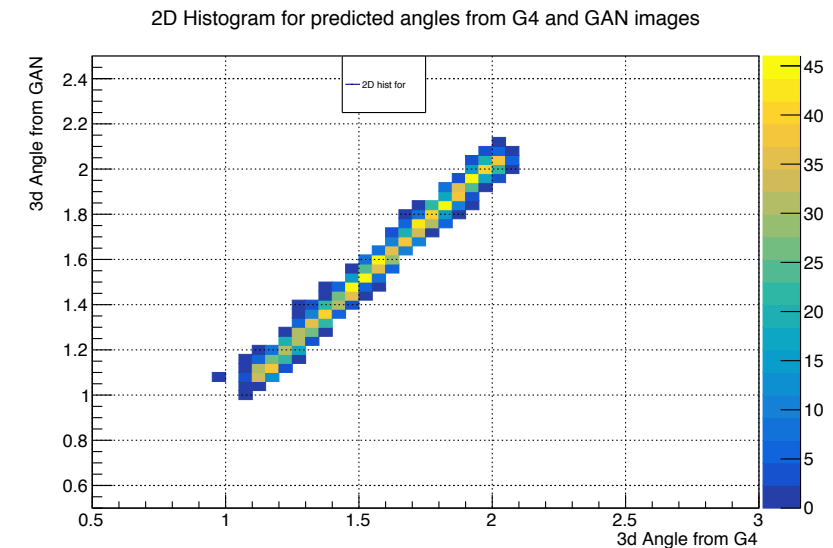
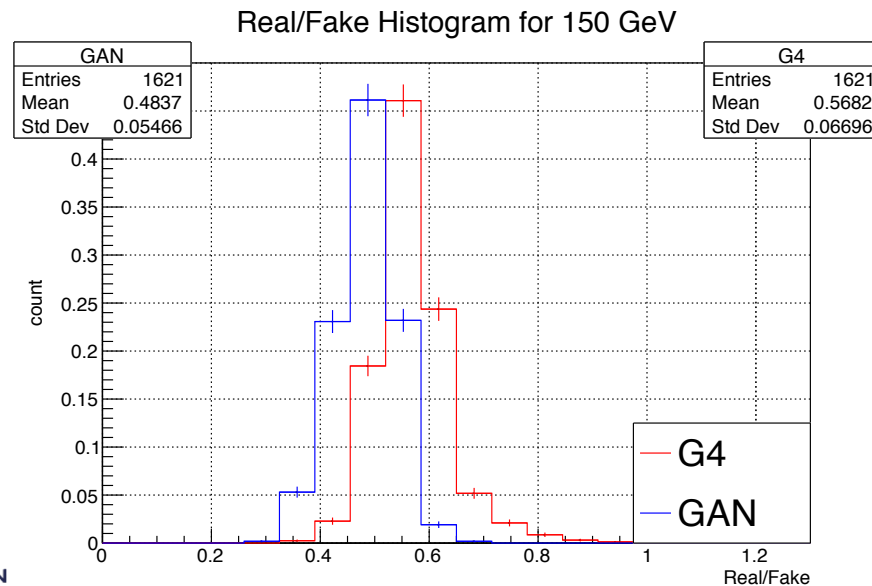
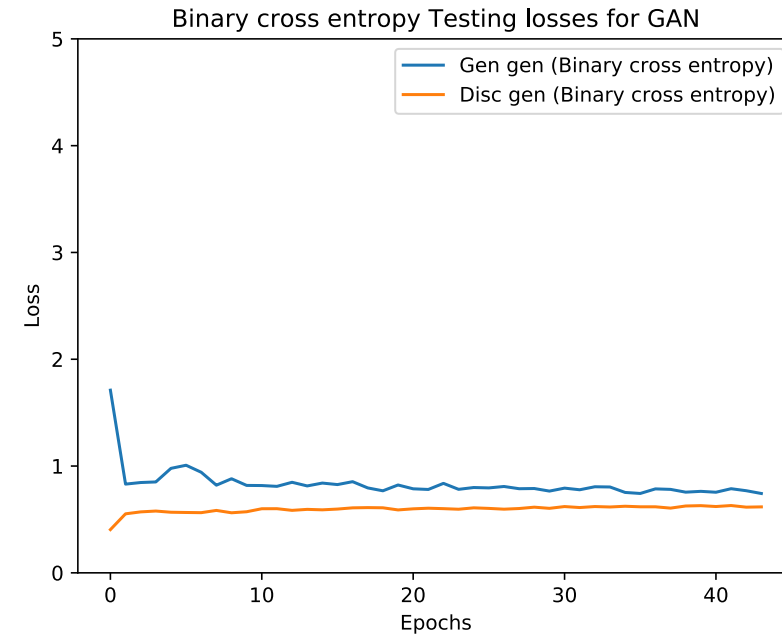
Convergence

and discriminator performance

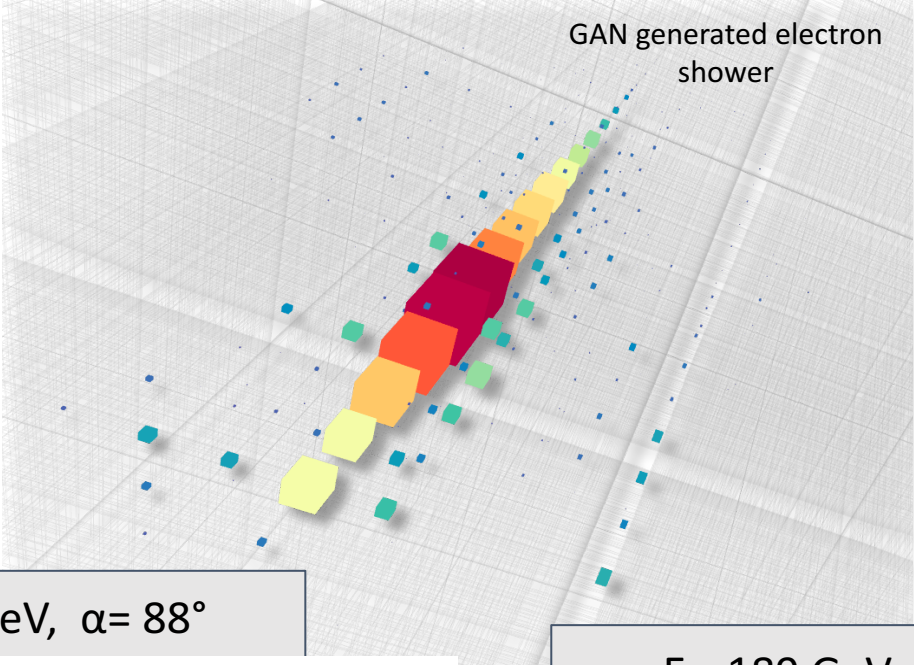
Stable test loss

Discriminator Real/Fake
probability peaks at ~50%

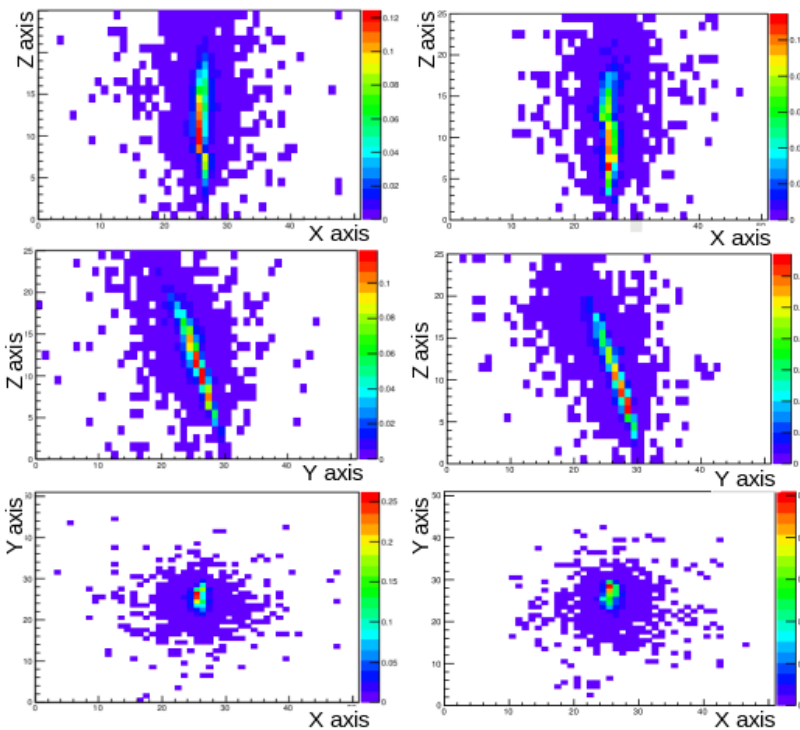
Correct incident angle



Generated events



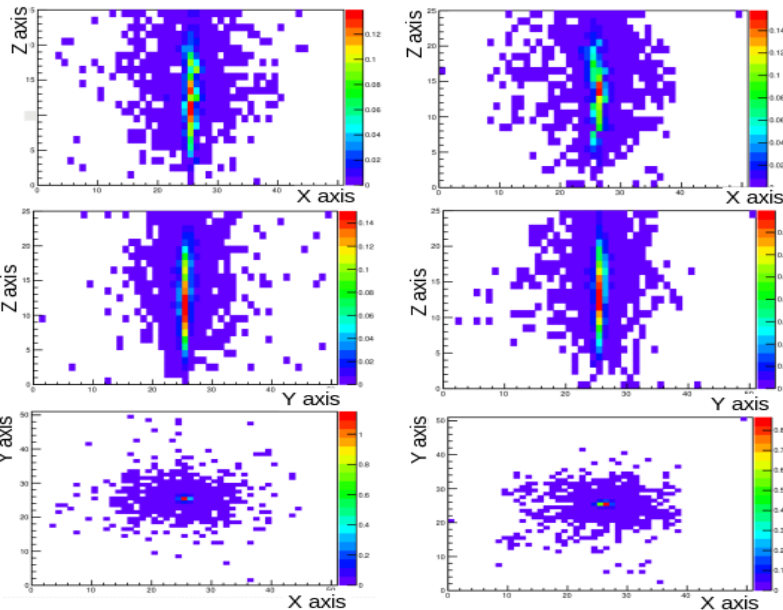
$E_p=111\text{ GeV}, \alpha=115^\circ$



Geant4

GAN

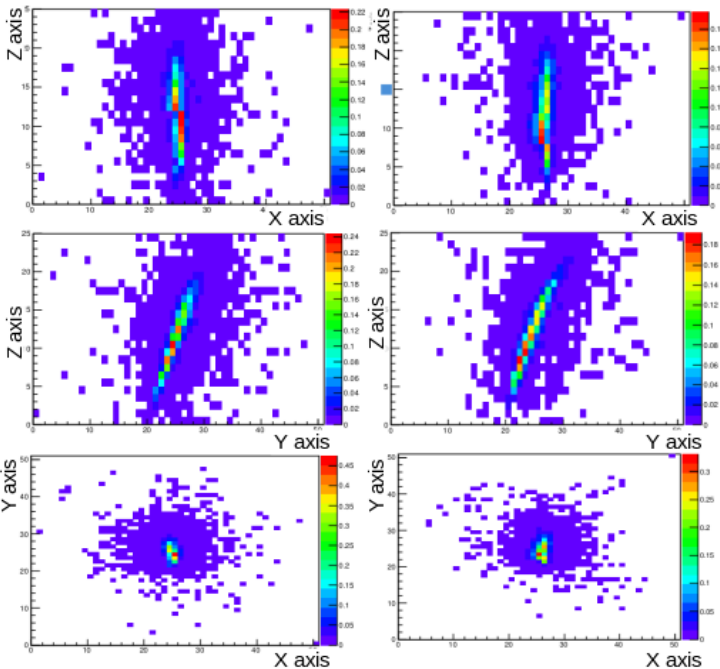
$E_p=147\text{ GeV}, \alpha=88^\circ$



Geant4

GAN

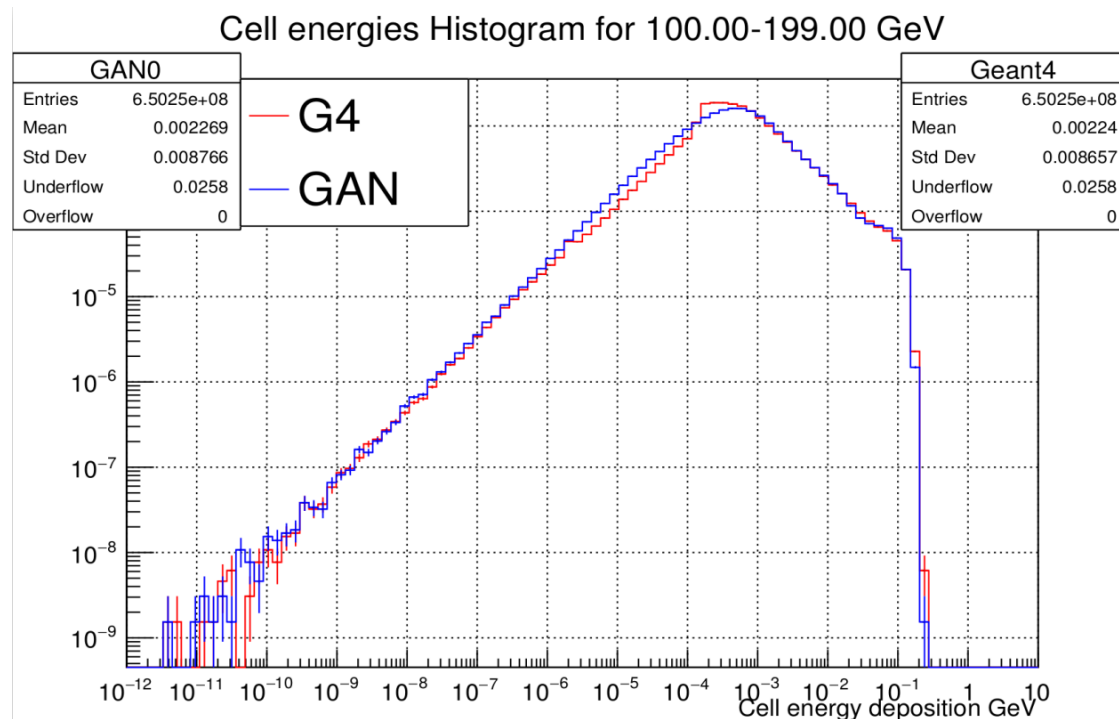
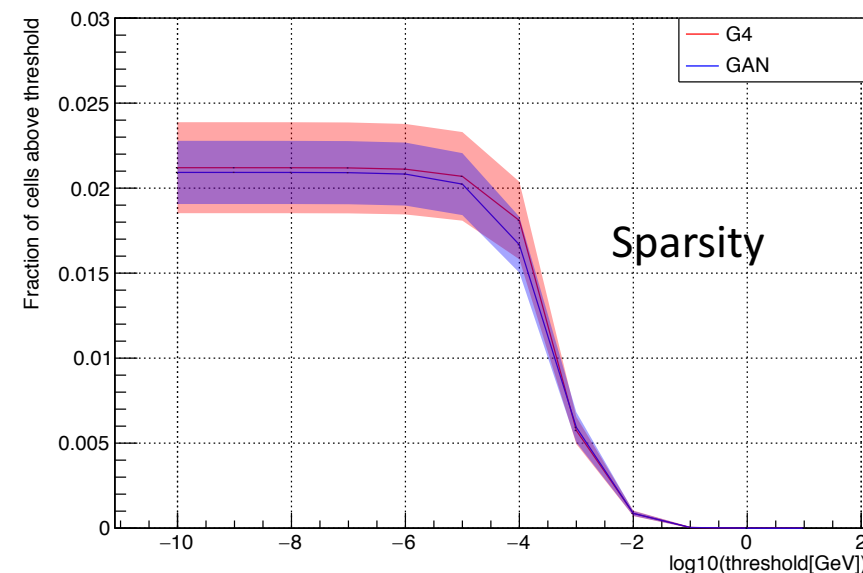
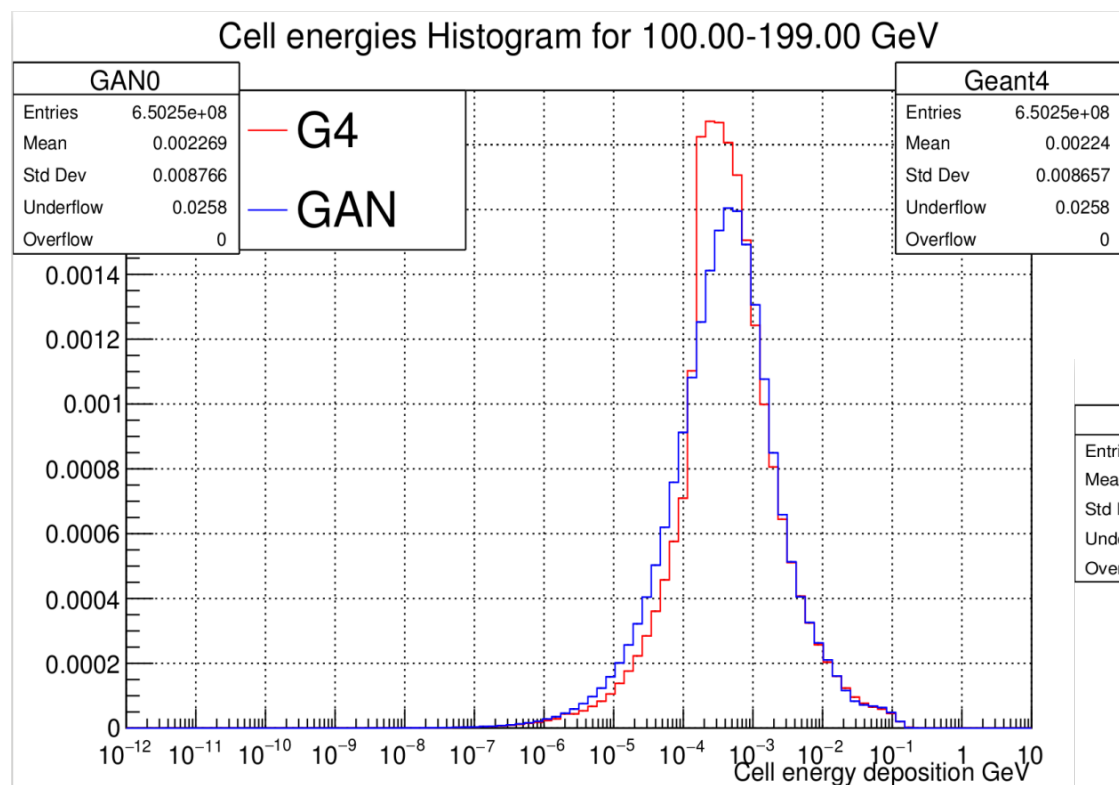
$E_p=189\text{ GeV}, \alpha=63^\circ$



Geant4

GAN

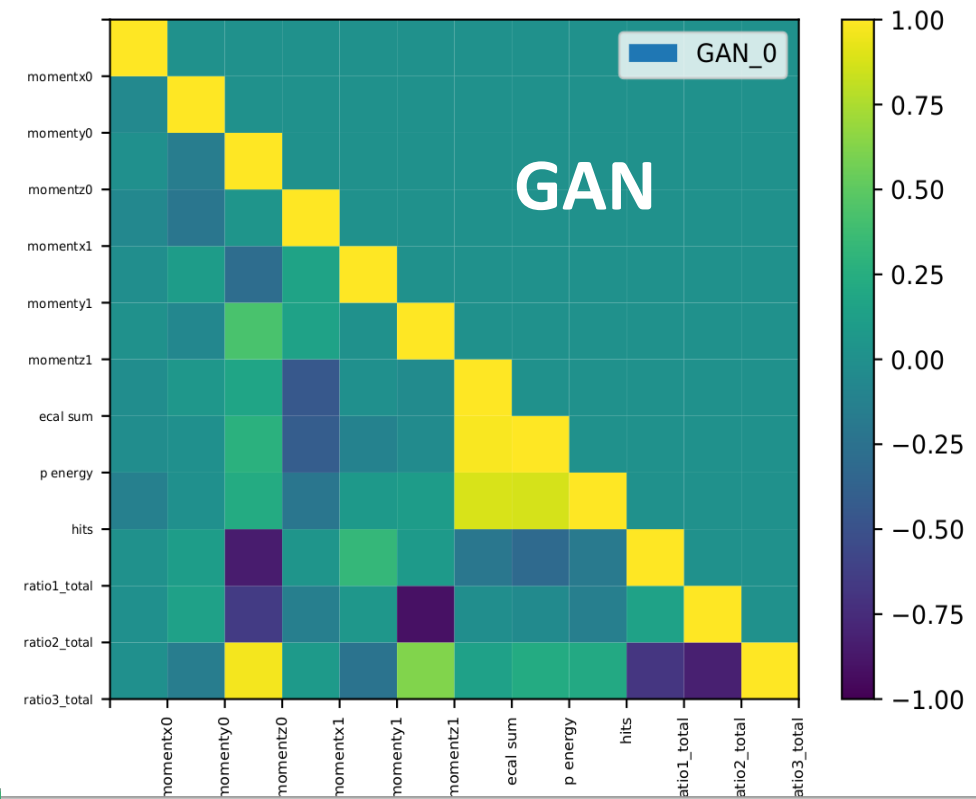
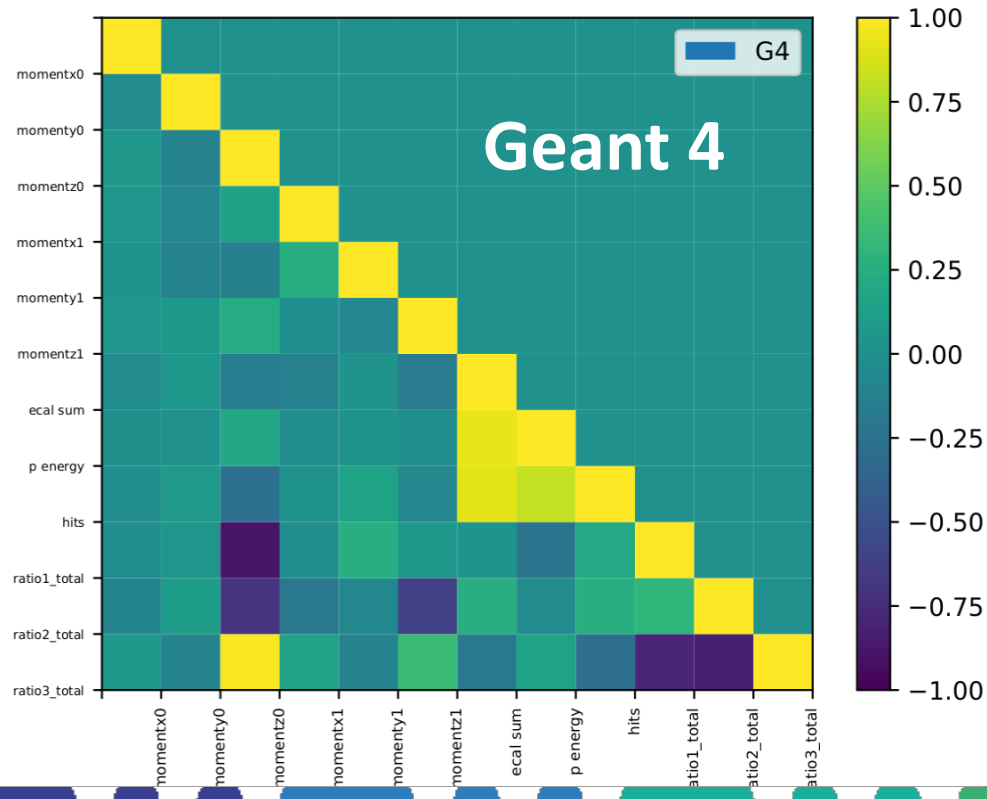
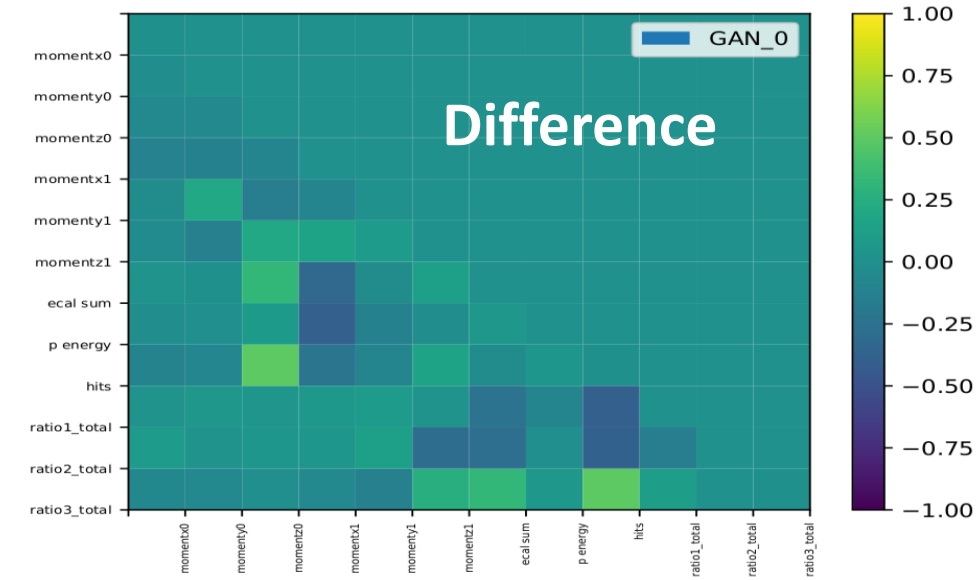
Single cell energy



Agreement to Geant4 down to 500 keV

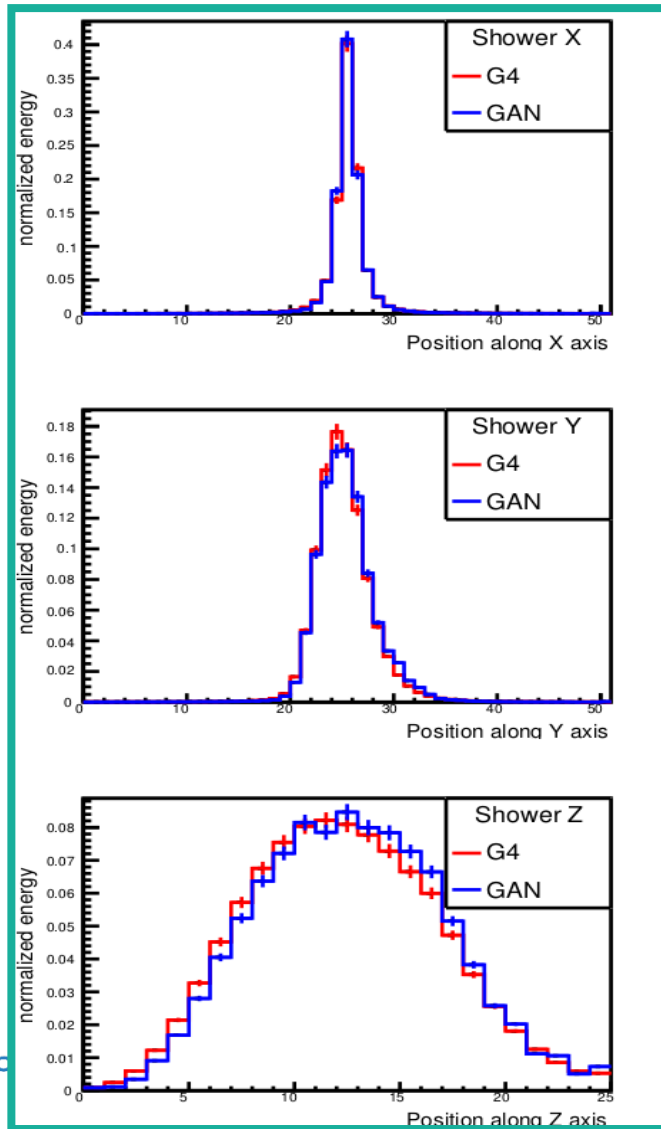
Low energy features missing

Internal Correlations

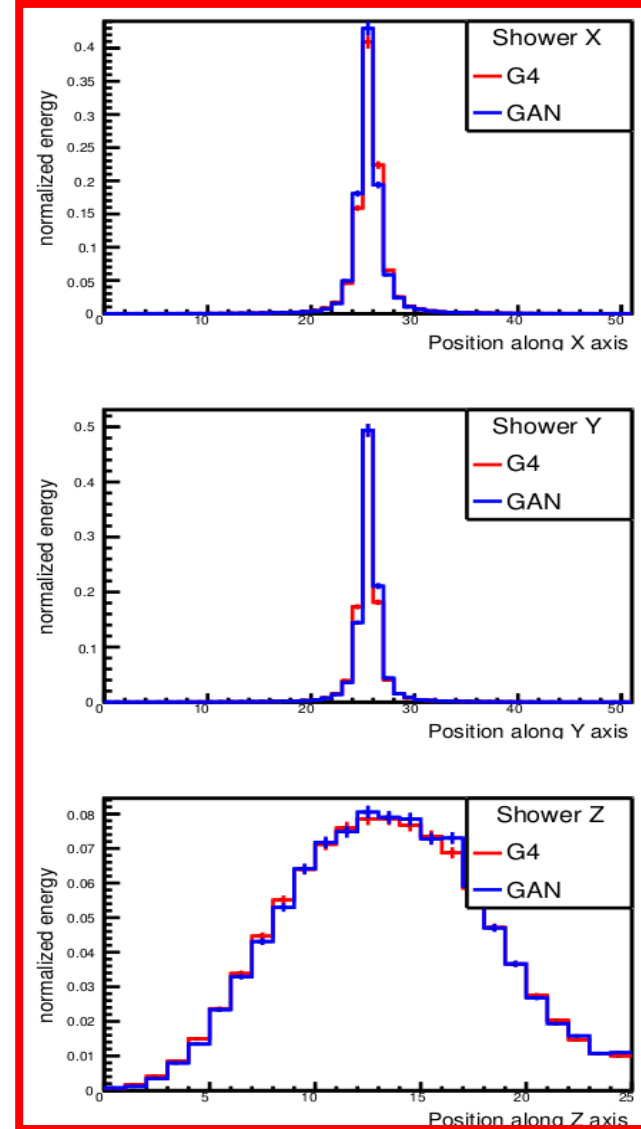


Energy shower shapes

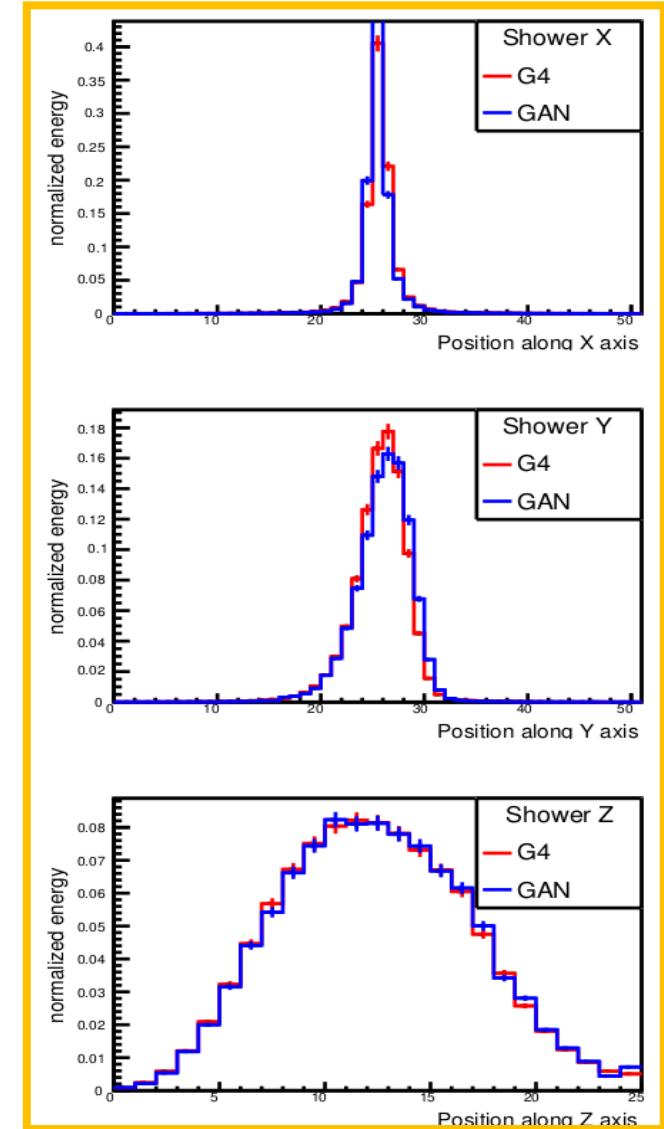
$\alpha = 60^\circ$



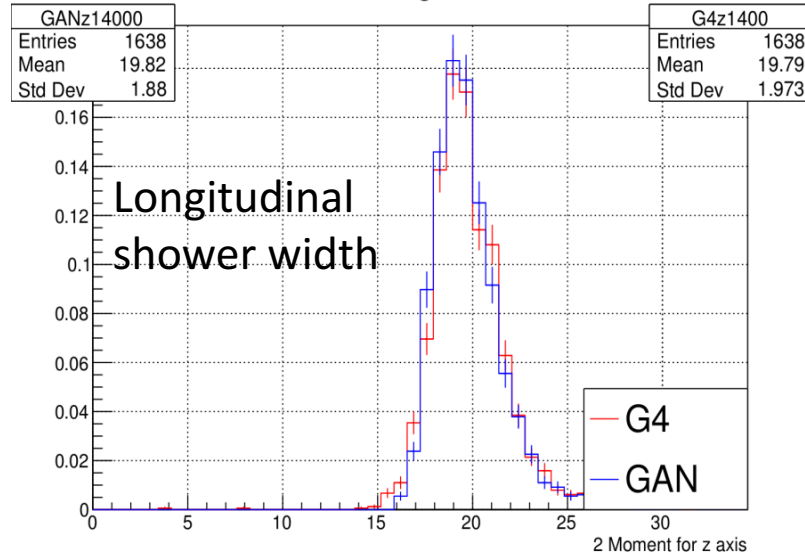
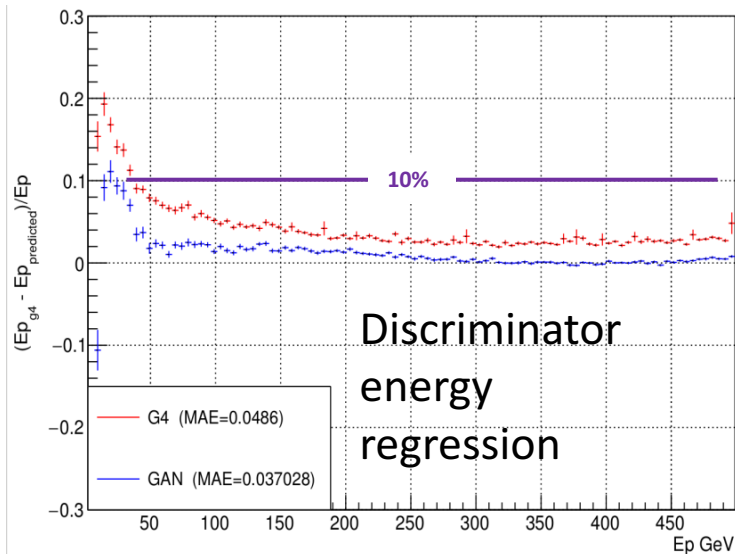
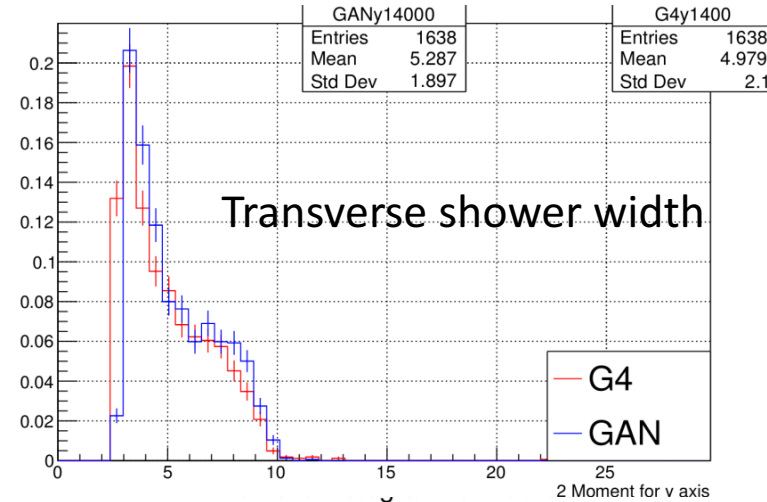
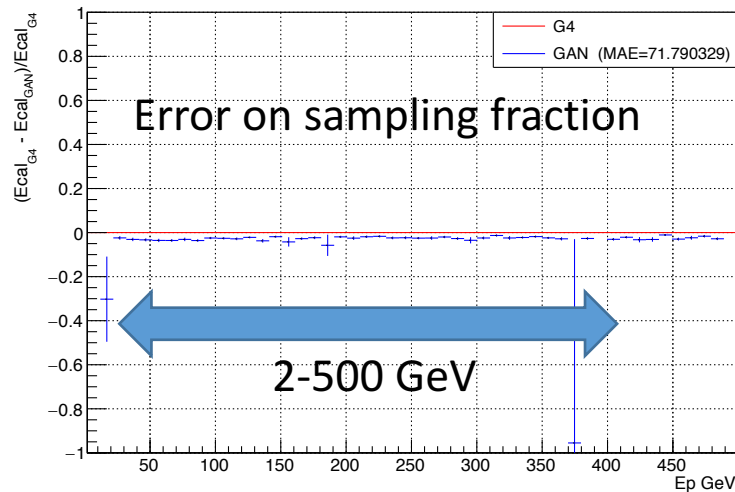
$\alpha = 90^\circ$



$\alpha = 120^\circ$

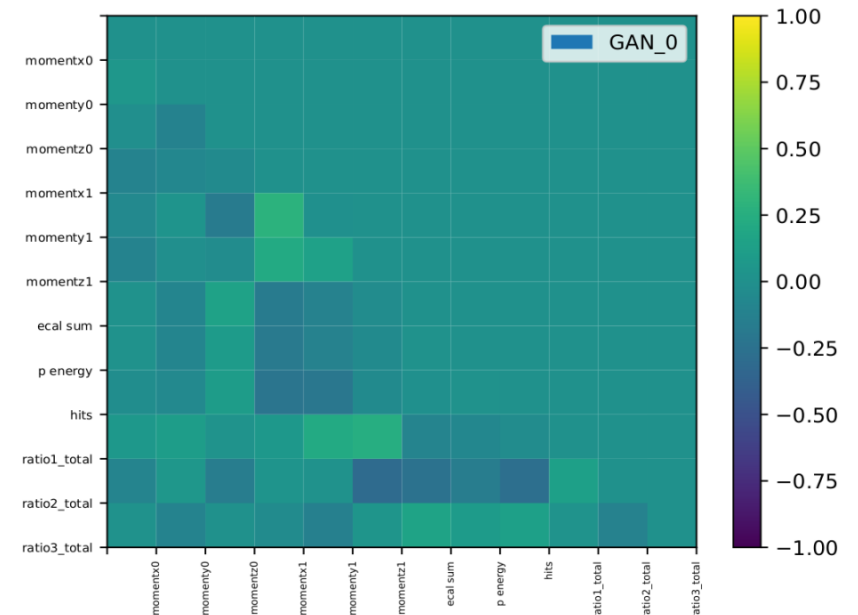


Transfer learning: extending the energy range



- Transfer learning from 100-200 GeV pre-trained network
- Double training dataset statistics, 3 epochs training

Improved correlation description!



Further Validation (I)

Structural Similarity Index (SSIM) is used to assess image similarity

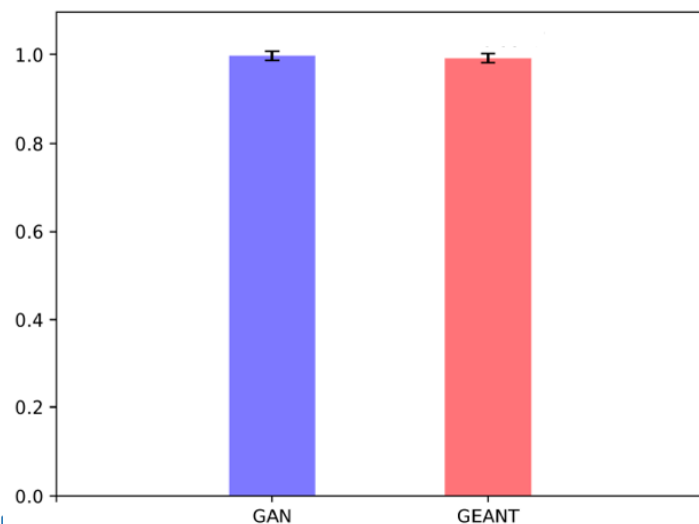
Measure **diversity** in GAN generated images

Run Triforce on GAN/GEANT4 events

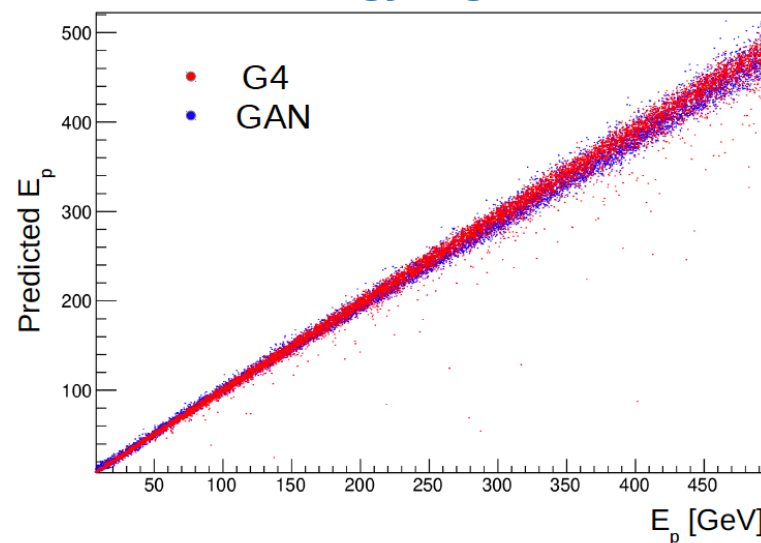
Trained on Geant4 data

SSIM (scale)	SSIM G4 vs G4	SSIM GAN vs GAN
1	0.94	0.95
1e-2	0.21	0.25
1e-4	0.045	0.061
1e-6	0.045	0.051

electron identification



energy regression



Triforce, Matt Zhang,
https://github.com/BucketOfFish/Triforce_CaloML

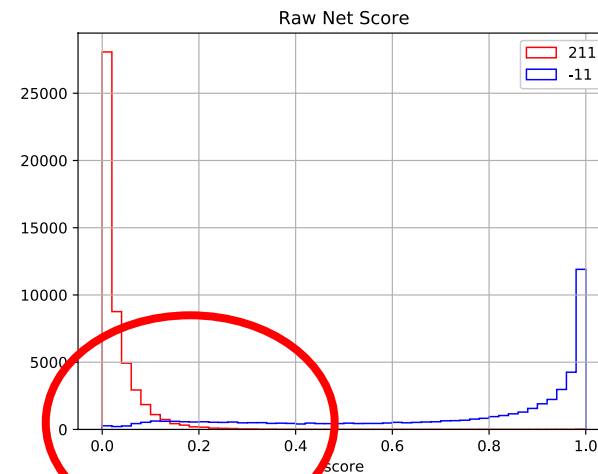
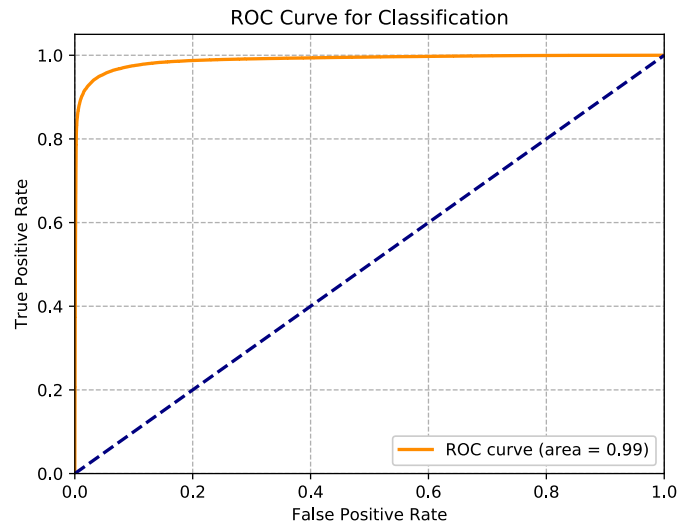
Further validation (II)

Train TriForce classifier on GAN data

Similar to **Classification Accuracy Score** idea⁽¹⁾

Train Triforce with a mix of GAN (electrons) and Geant4 (pions) data

Validate performance on Geant4:
Obtain very good results (99% AUC)



Some electrons are
not classified correctly

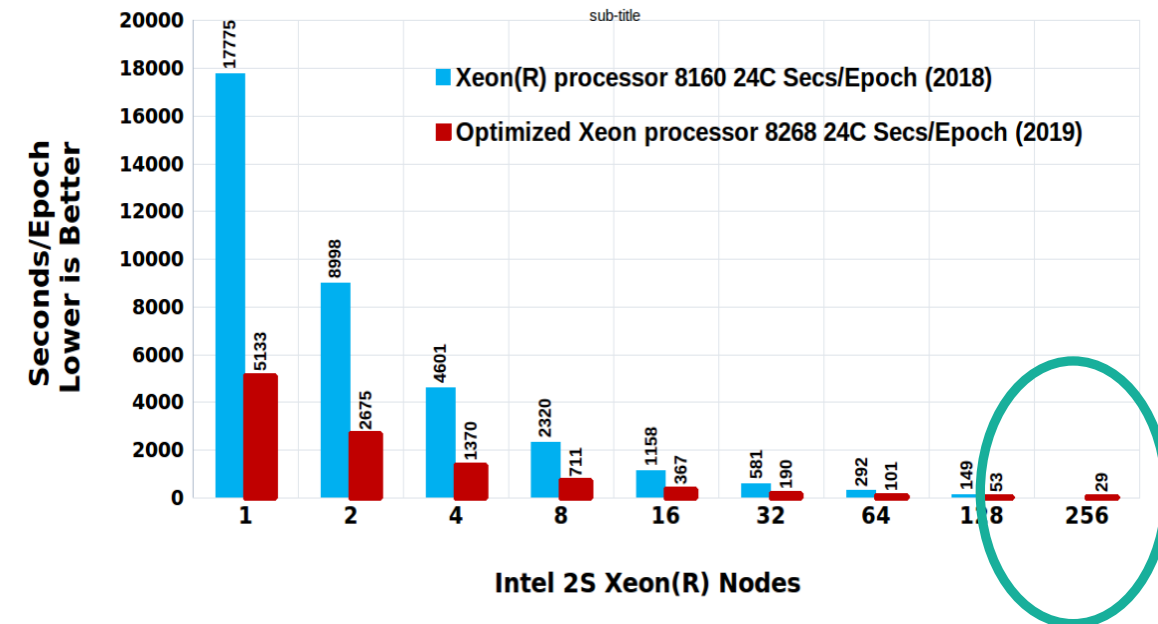
Computing performance

20000x faster than Geant4

Time to create an electron shower		
Method	Machine	Time/Shower (msec)
Full Simulation (geant4)	Intel Xeon Platinum 8180	17000
3d GAN (batch size 128)	Intel Xeon Platinum 8160 (TF 1.12)	0.8

Convergence in 15min

CERN High Energy Physics: 3D GANS Training Performance
Intel 2S Xeon(R) Cluster, OPA Fabric
Xeon(R) 8268 (2019) vs Xeon(R) 8160 (2018)

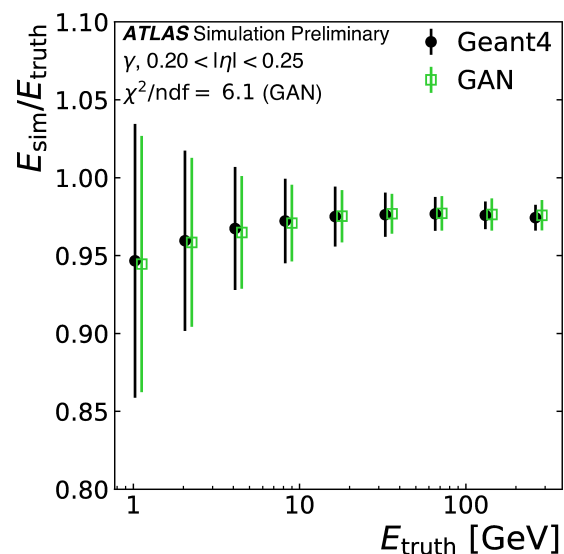
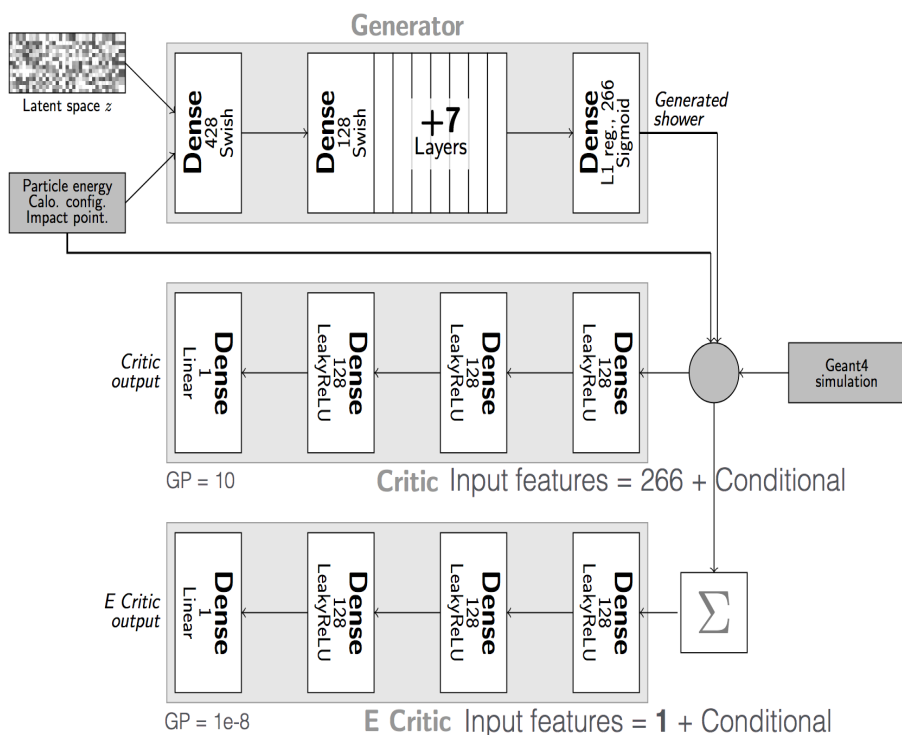
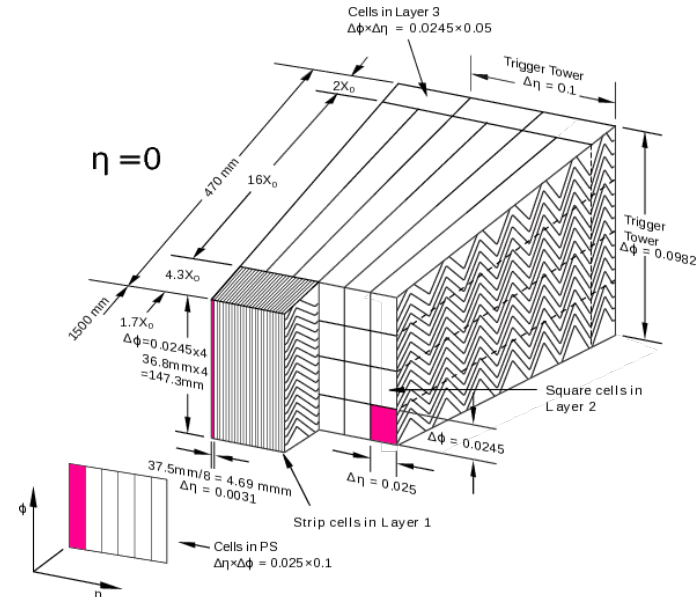


Other simulation examples at the LHC

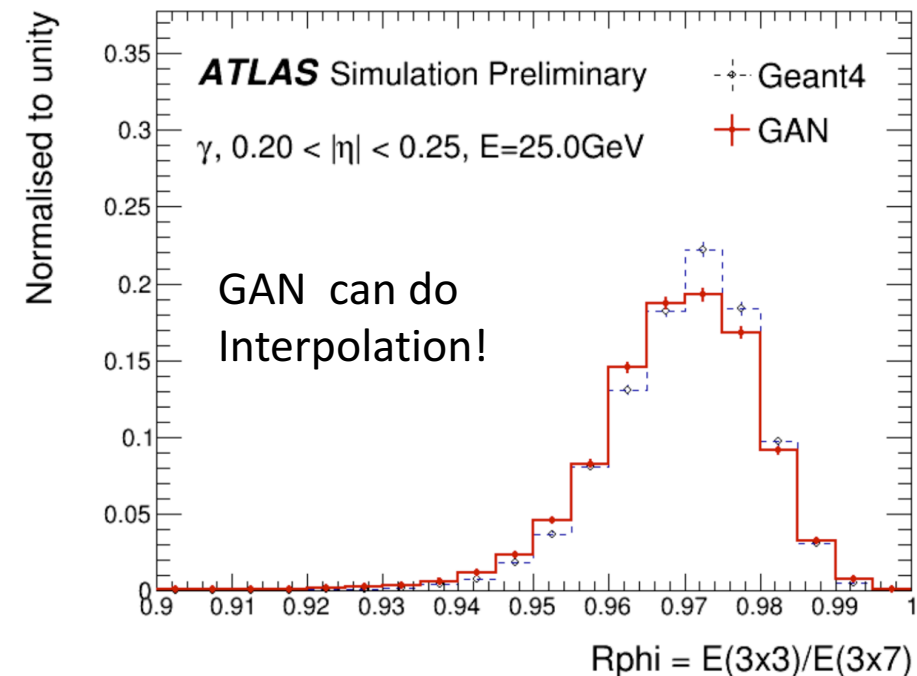
ATLAS LAr calorimeter

Complex geometrical structure

Wasserstein GAN: One generator against two critics



Ghosh, CHEP 2019
ATL-SOFT-PUB-2018-001



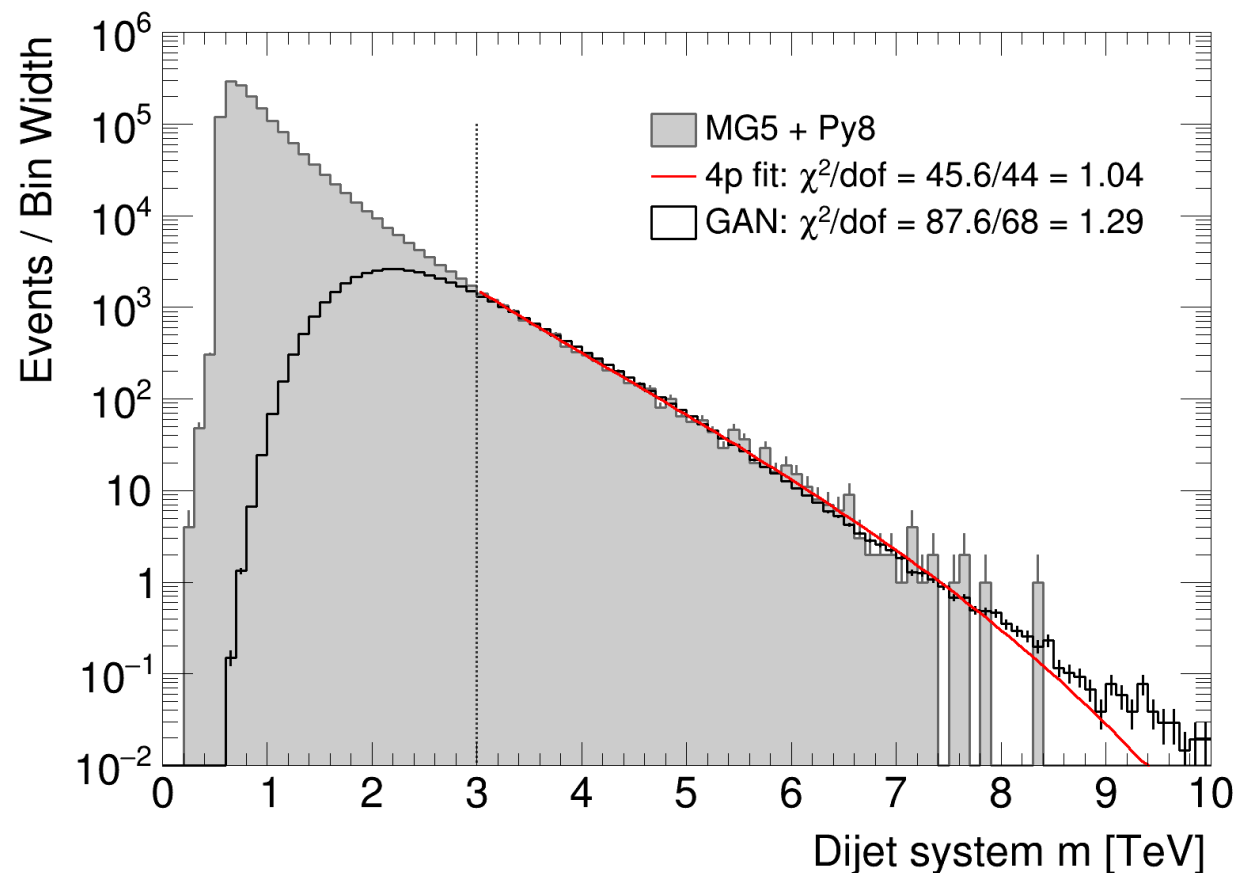
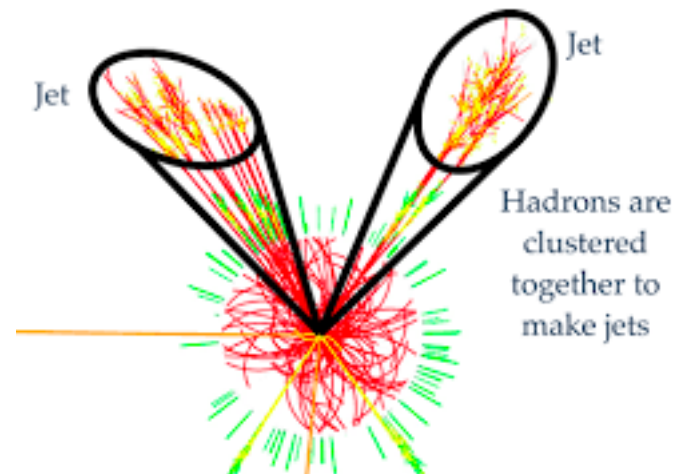
DijetGAN

QCD dijet events at the LHC

Investigate regions of the phase spaces with **low cross-section** → interesting kinematic region for BSM searches

GAN can produce **"reasonable"** output beyond the training data phase space!

S. Palazzo, IML WG 2019



CMS HGCAL prototype

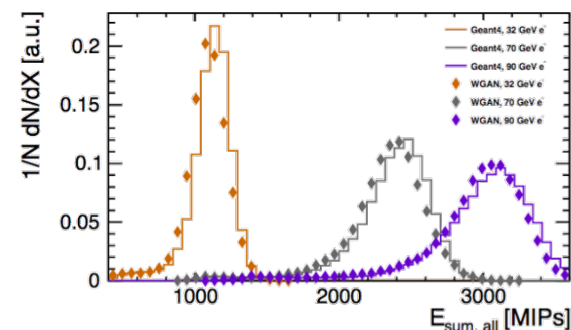
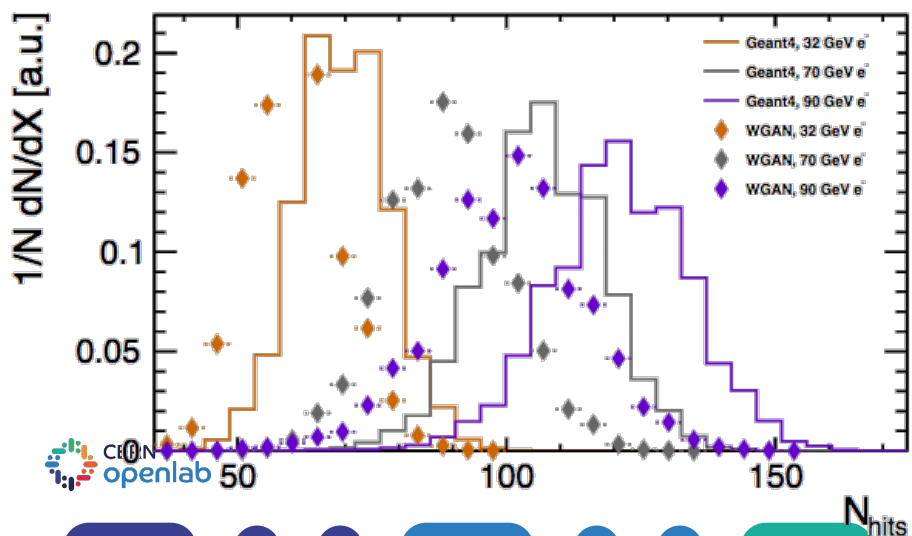
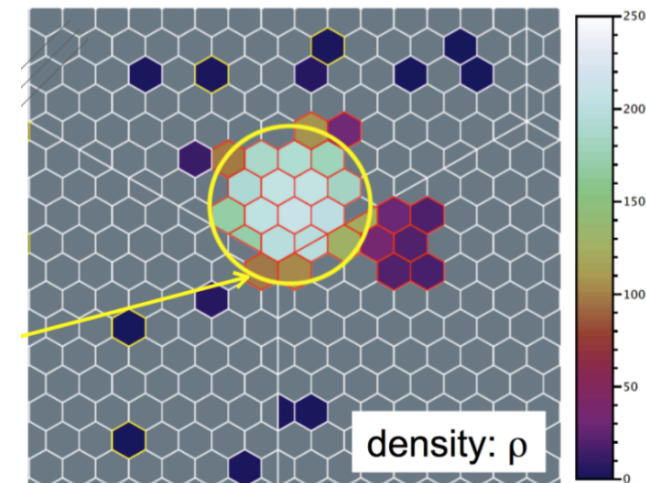
High Granularity and Hexagonal cells for CMS upgrade

Wasserstein conditional GAN (convolutions)

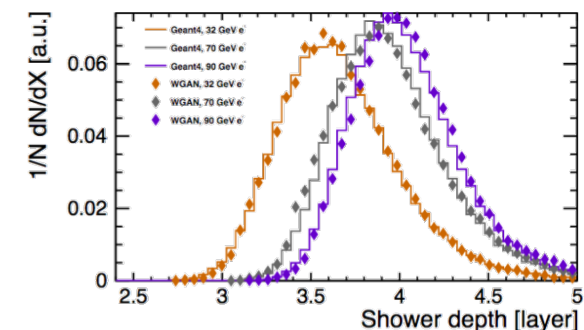
Train a generator against a **critic** and **2 constrainer networks** reconstructing energy and impact point coordinates

Good agreement to Geant4

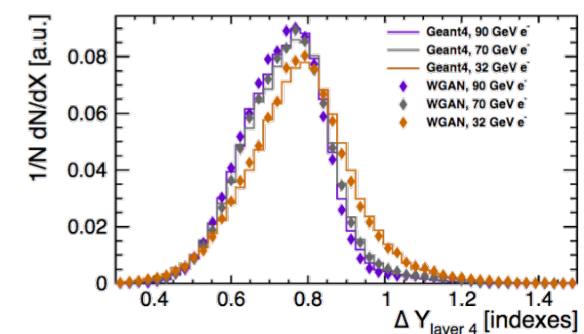
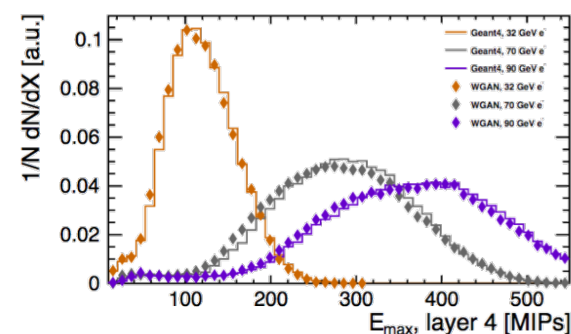
Some problems at low energy



(a)



(b)



Other applications in HEP (simulation)

Generative models for ALICE TPC simulation (ACAT2019)

GAN in LHCb: calorimeter and RICH simulation (CHEP2019)

Graph-GAN for CMS HGCal (ACAT2019)

Variational AutoEncoders to simulate ATLAS LAr calorimeter (CHEP19)

Wasserstein GANs to generate high-level physics variables based on Monte Carlo ttH (superfast-simulation) (IML WG 04/18)

Particle-GAN for Full Event Simulation at the LHC (ACAT2019)

Refining Detector Simulation using Adversarial Networks (CHEP2019)

Model-Assisted GANs for the optimisation of simulation parameters
(AISIS2019)

Conclusions

Generative Models are powerful techniques

Object of an intense R&D , require careful **validation**

Many applications in High Energy Physics

Simulation is one of the main applications

High level of **accuracy** & **speed**

Multiple features/capabilities

Deep Learning is a driving force toward changing our computing model

DL workloads are HPC friendly

Benefit from dedicated hardware and accelerators

Addressing Computing challenges

Millions of operations

Mostly matrix-multiplications

HEP models are designed and
optimised for specific tasks

Generally **custom** models

~**Fewer weights** and operations than
out-of-the-box tools

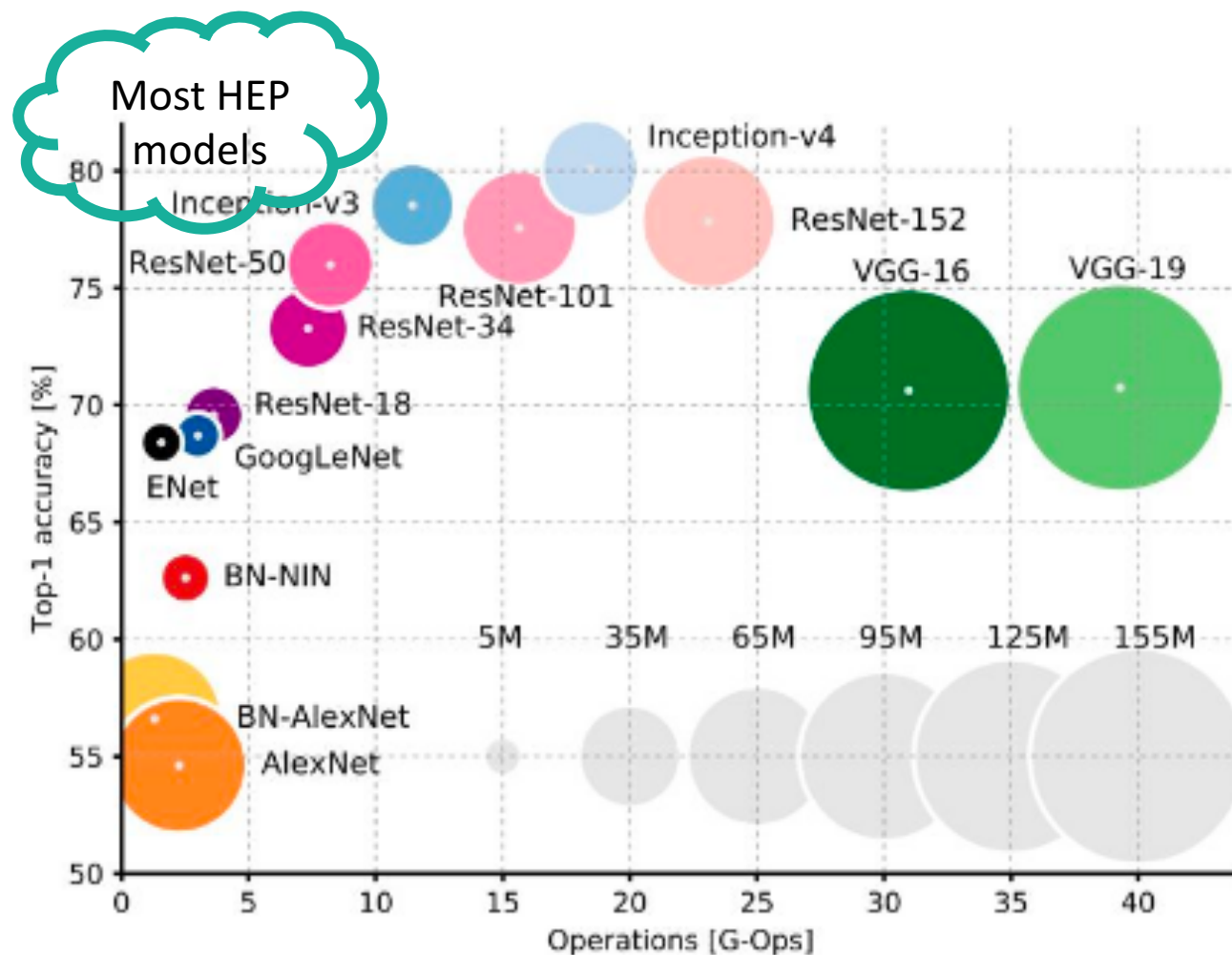
Higher accuracy

Depending on the task, we might
need:

Fast inference

Online training capability

Fast training for large optimisations



Accelerators

Deep Learning workloads are naturally **accelerator friendly**

Large number of frameworks and ecosystems to simplify deployments

Can work with half precision arithmetic (16FP, ...)

GPUs are de-facto **standard** to run DL

R&D on reducing bottlenecks (memory size, I/O. ...)

FPGAs can provide **low latency** inference

Network compression/quantization/parallelisation

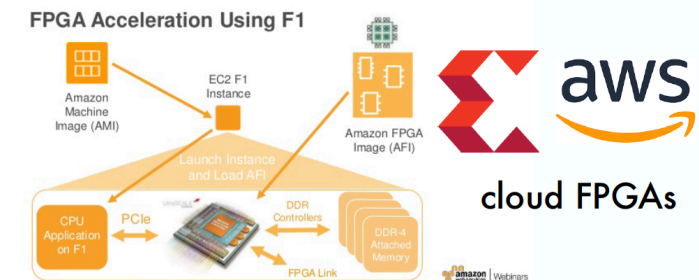
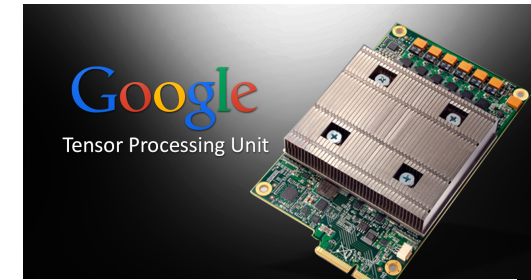
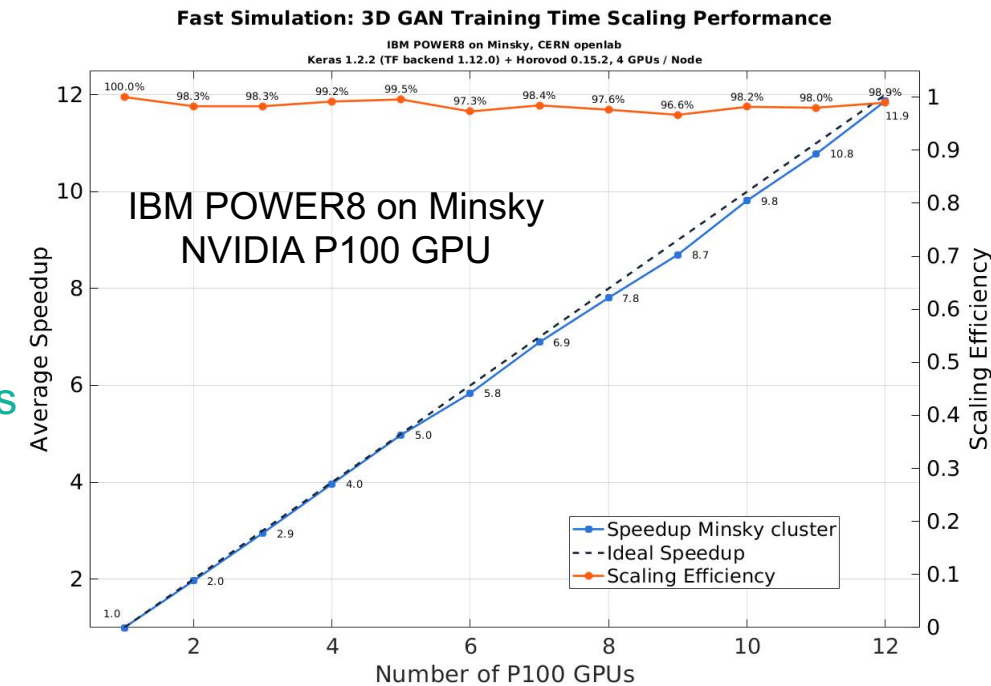
Different programming approaches Hardware Description Language vs High Level Synthesis

Frameworks exist that “compile” ML code for different hardware

Customisation

Available in cloud environments for **on-demand access**

Initial tests to time inference on cloud vs local



Heterogeneous computing

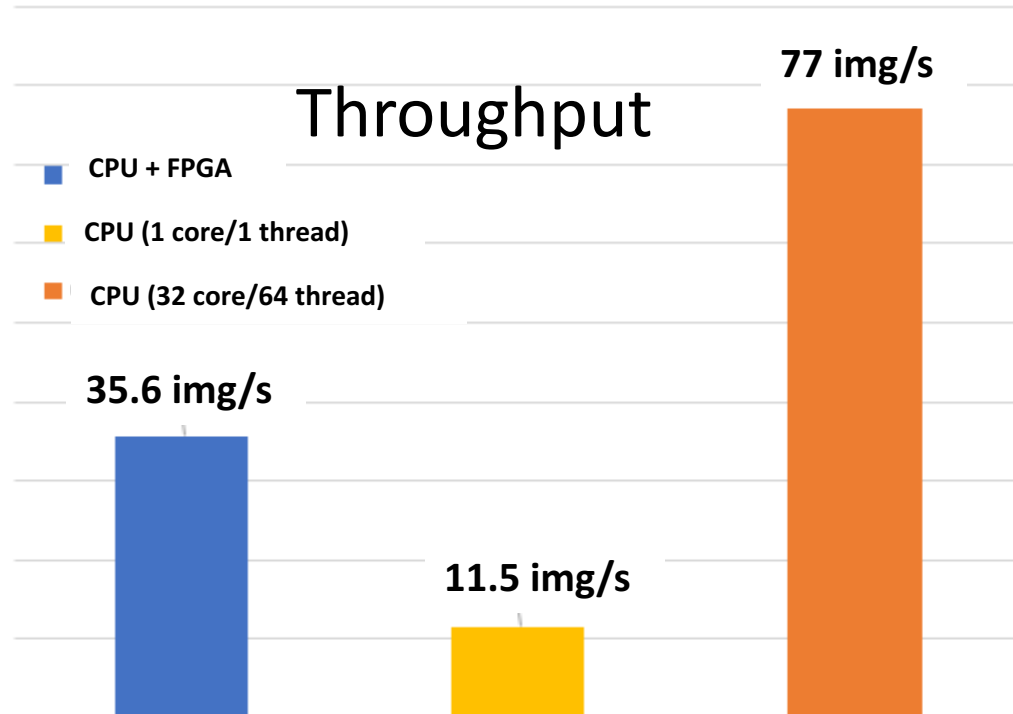
FPGA-acceleration of 3DGAN inference

Intel PAC Arria 10 card; OpenVINO; DLA design suite

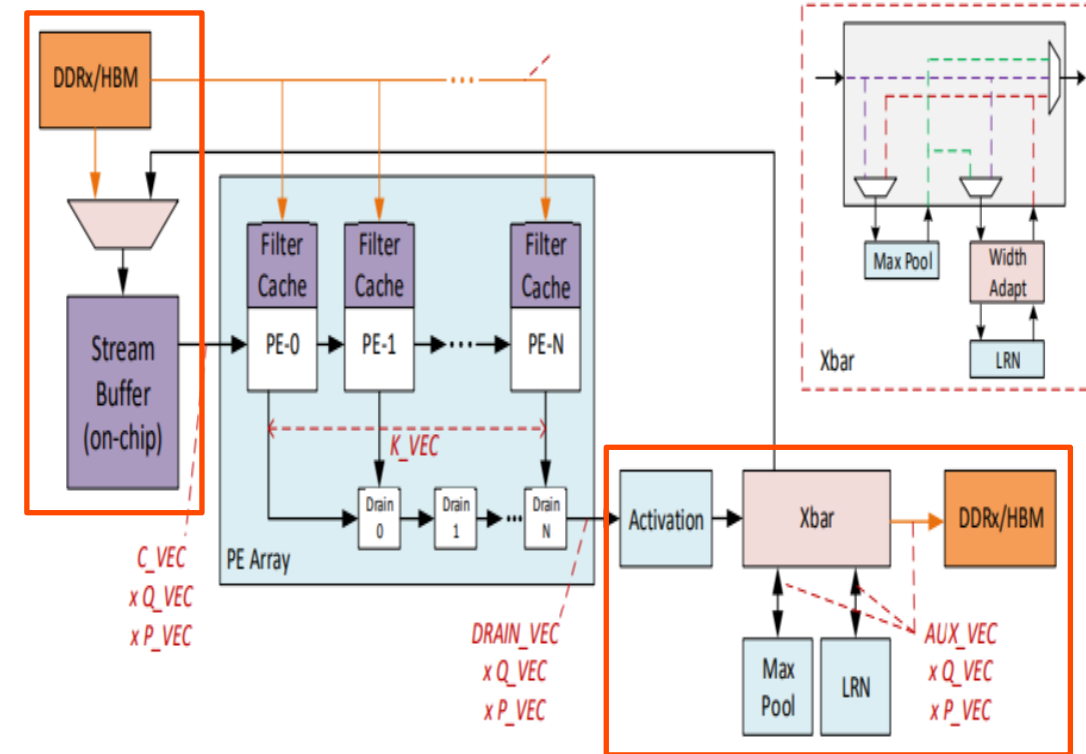
Implement missing components:

3D convolutions (done)

3D upsampling (inprogress)



DLA customization



presented at CHEP2019⁴⁶

Distributing the training process

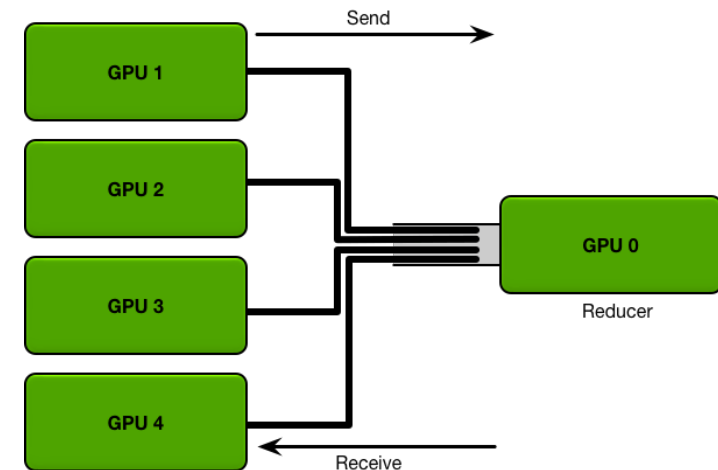
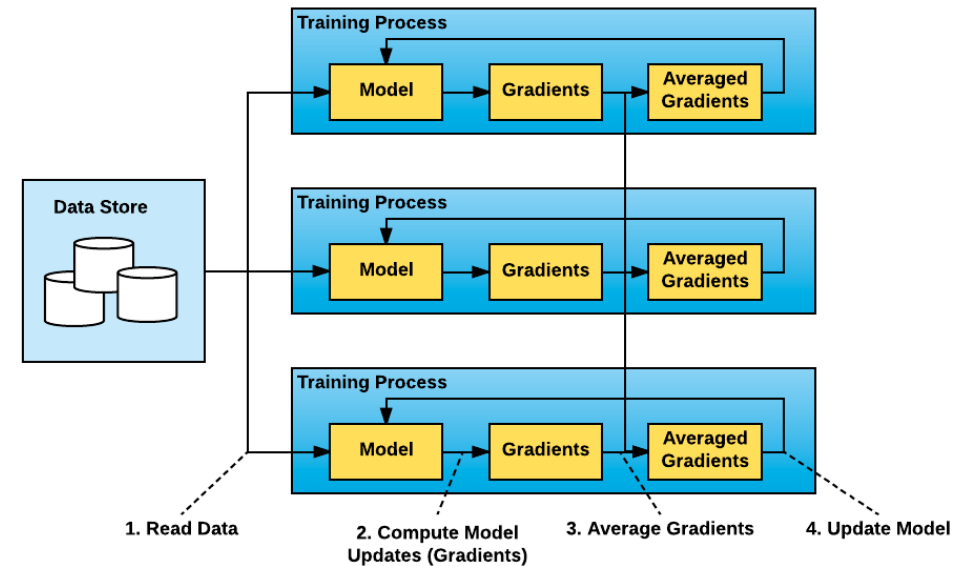
- **Data distribution**
 - Compute gradients on several batches **independently**
 - Update the model **synchronously or asynchronously**
 - Applicable to **large dataset**

Data is sent and received from a single node

Can have high communication costs

Smart update strategies

Computation or bandwidth bottleneck



HPC resources

HPC "creates" new DL models

Most powerful systems are **hybrid**

Ease access to the resources

Integration in HEP infrastructure

Software stack deployment ?

Containers

Most DL framework provide containerised versions

Workflow management ?

Native **DL platforms** are natural choice (i.e. Kubeflow)

Adapt HTC job schedulers ?

Data access/management ?

S3 works very well

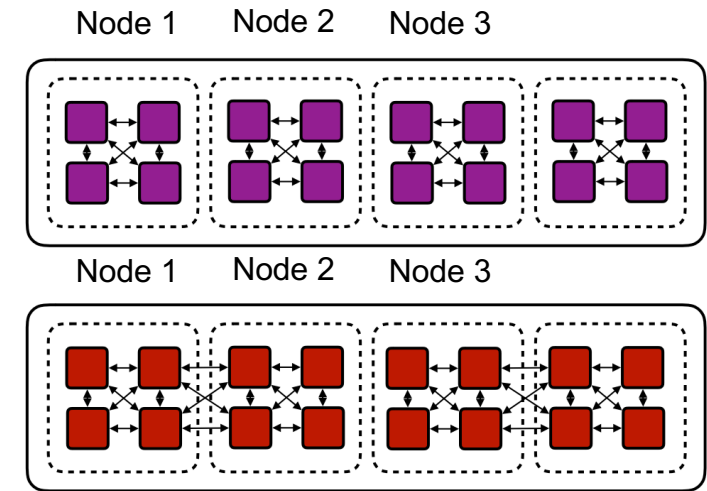
Supported widely in **commercial clouds**

Not all HPC centers allow access to it

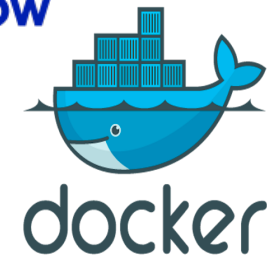
HTC



**Efficient
Intra-node
communication
is key**



kubernetes



docker

Distributed training on Cascade Lake

Training 3DGAN can take days

Implements data parallel approach using Horovod.

128 Nodes:

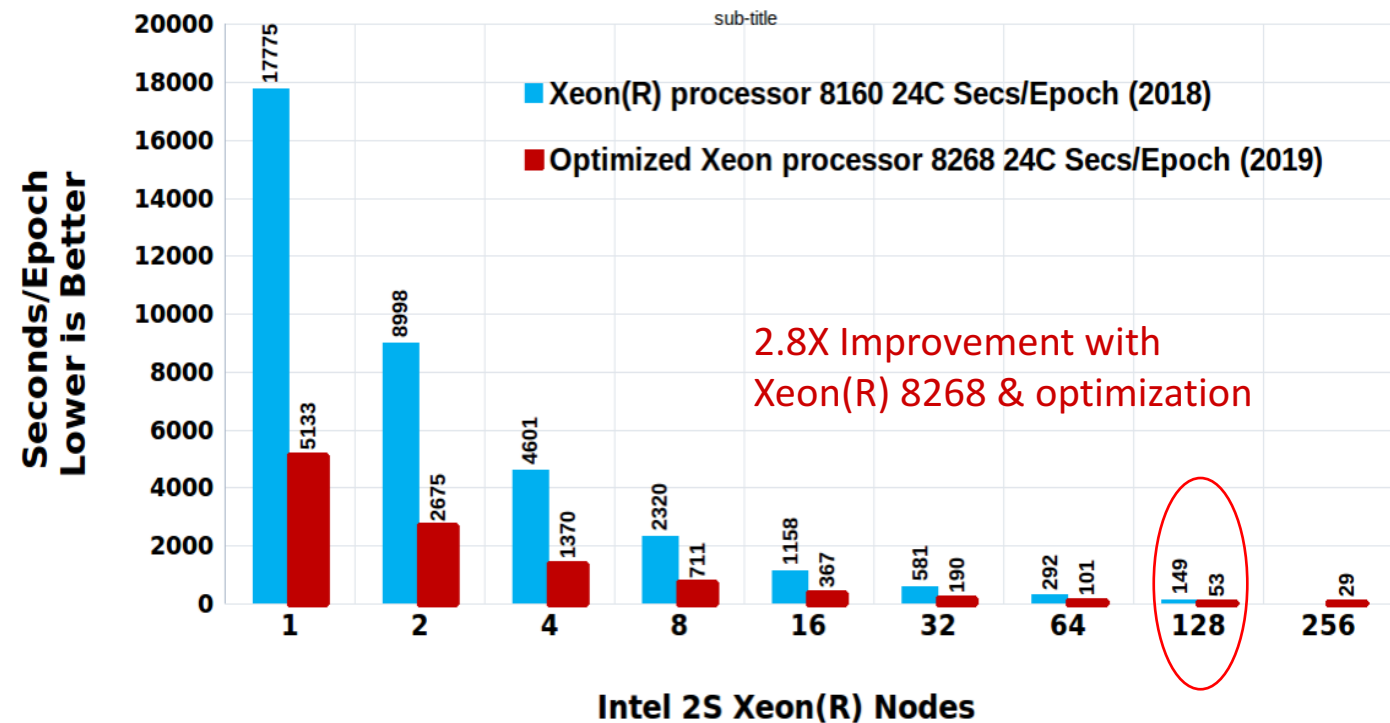
Xeon 8160 (Sky Lake): ~2 Mins/Epoch

Xeon 8268 (Cascade Lake): < 1 Min/Epoch

256 Nodes:

Time to Convergence: ~15 Mins

CERN High Energy Physics: 3D GANS Training Performance
Intel 2S Xeon(R) Cluster, OPA Fabric
Xeon(R) 8268 (2019) vs Xeon(R) 8160 (2018)



Intel Endeavour cluster: *Xeon® 8268 Cascade Lake, 2 Sockets /node, 24 cores per socket, Intel® Omni-Path Architecture*
Software: *Tensorflow 1.14 (Intel optimized), MKL-DNN 0.18, Horovod 0.16.4, Keras 2.2.4*

Containerized deployment on HPC

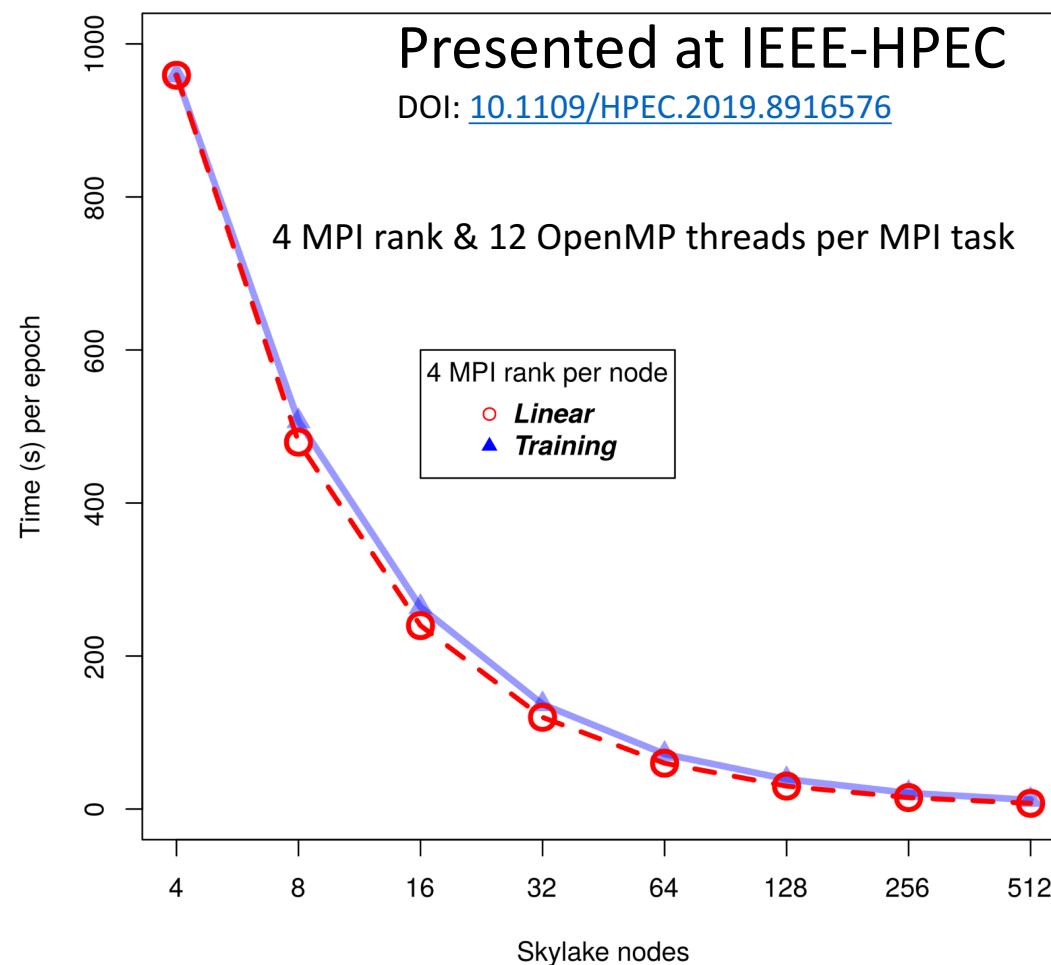
Transition AI algorithms from laptops to supercomputers

Deploy 3DGAN training on SuperMuc-NG using CharlieCloud

Intel Xeon Platinum 8174 (Skylake)

48 cores

Intel® Omni-Path Architecture



Cloud resources

A solution to consider for offline applications

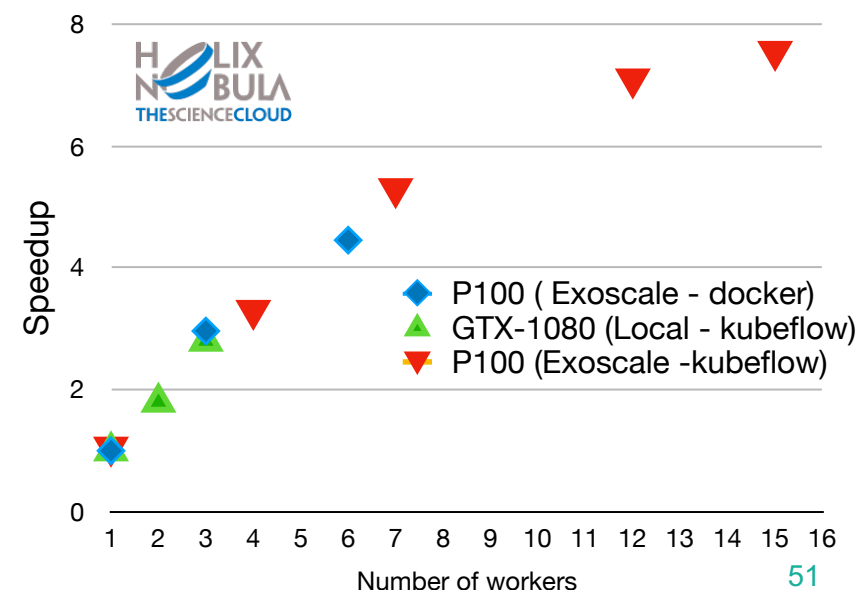
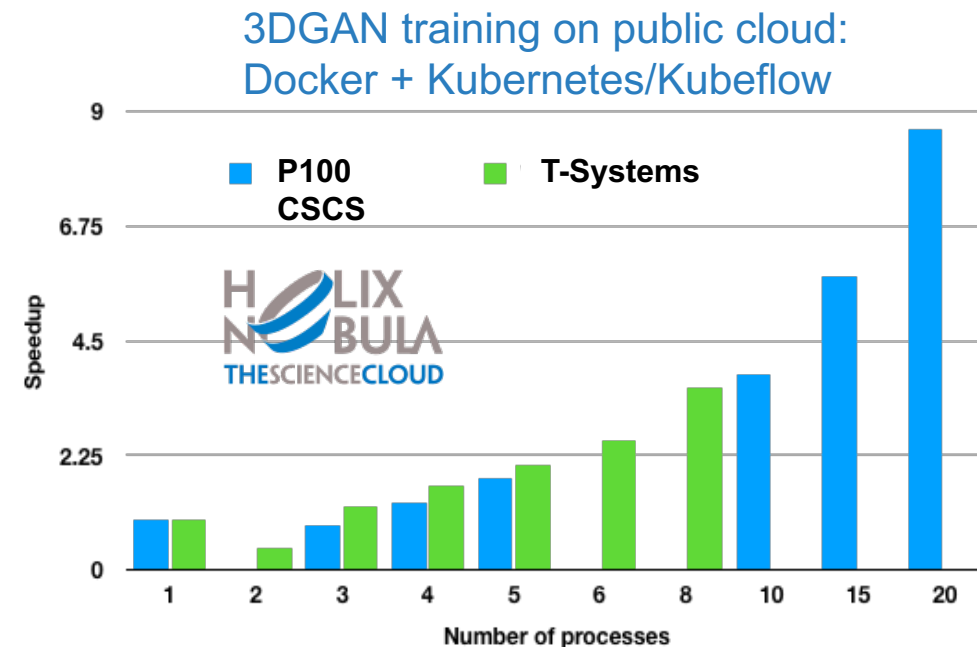
Not always feasible/effective to **buy**
specialized hardware

Most MLaaS solutions are not
customizable enough for scientific use
cases

Great opportunities for R&D with industry

New initiatives to increase access to
commercial clouds

deploy **hybrid models** (OCRE in the
context of the EOSC)



Bonus Material

Refining Simulation using GANs : Ultra High Energy Cosmic Rays
Pushing the boundaries: Quantum GAN

Refining Simulation using GANs

Pierre Auger Observatory

Detection of UHECR $E > 10^{17.5}$ eV

Hybrid Technique

27 Nitrogen Fluorescence (ultra-violet) telescopes

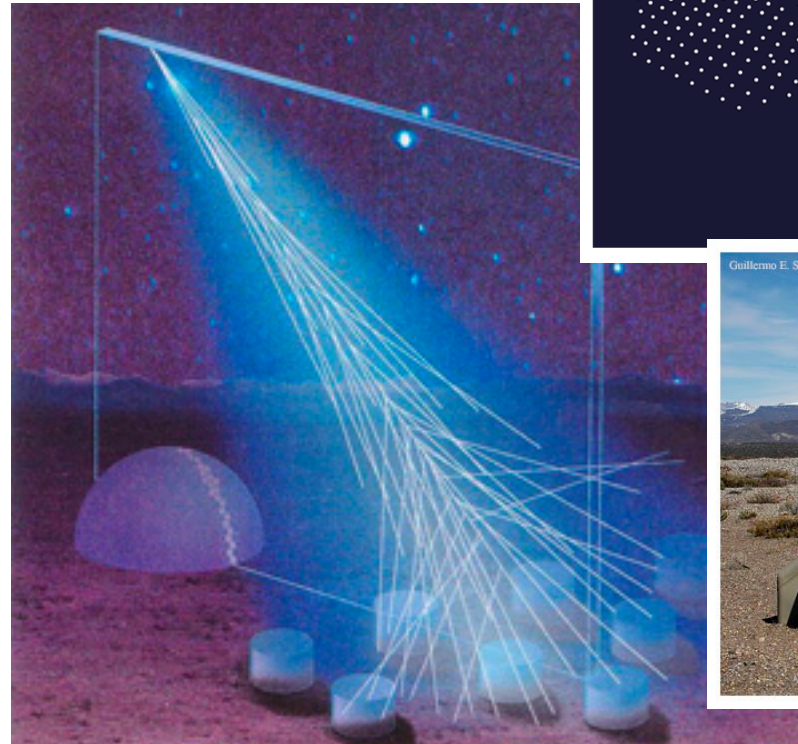
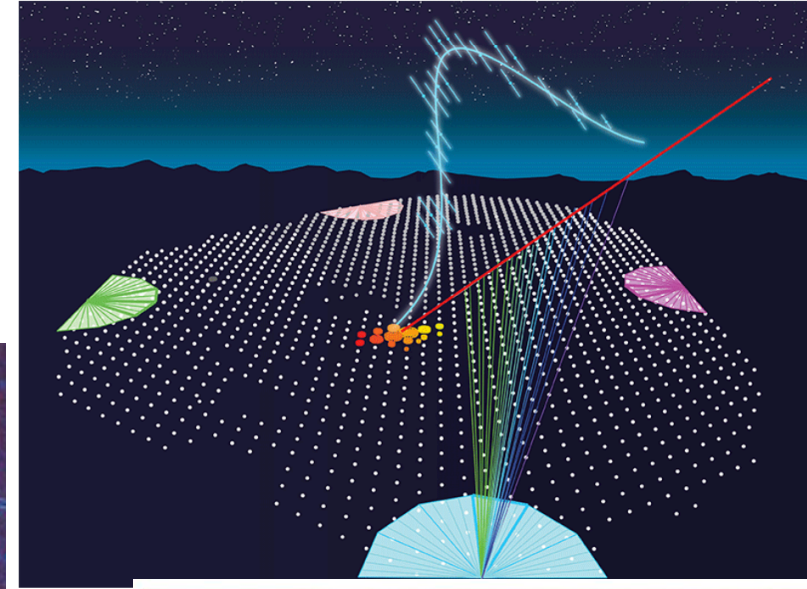
1660 Surface detectors (water tanks)

3000 km² array size

Simulation/Data mismatch

Refine simulation using WGAN

Train DNN on refined simulation



Refining Simulation using GANs

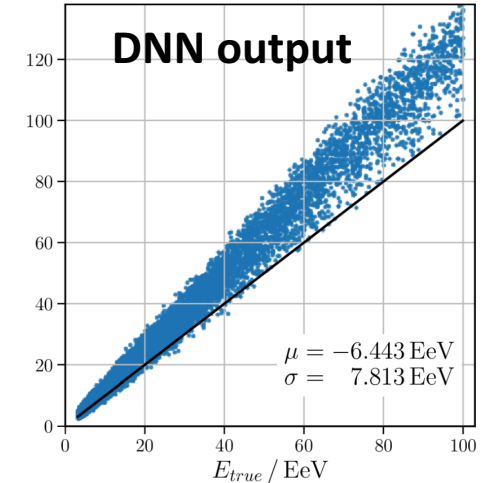
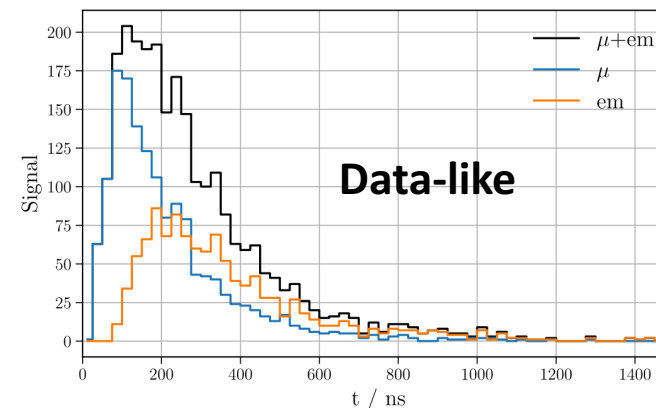
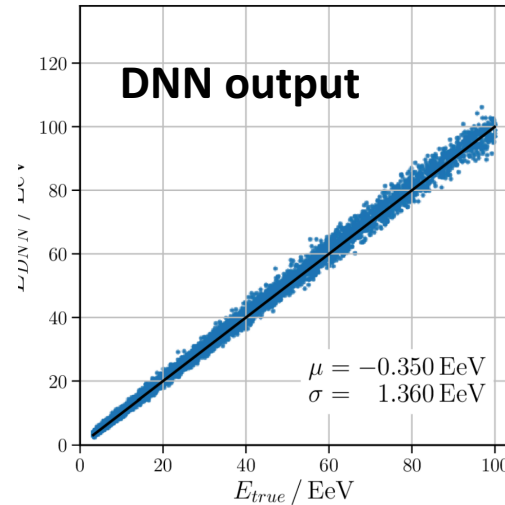
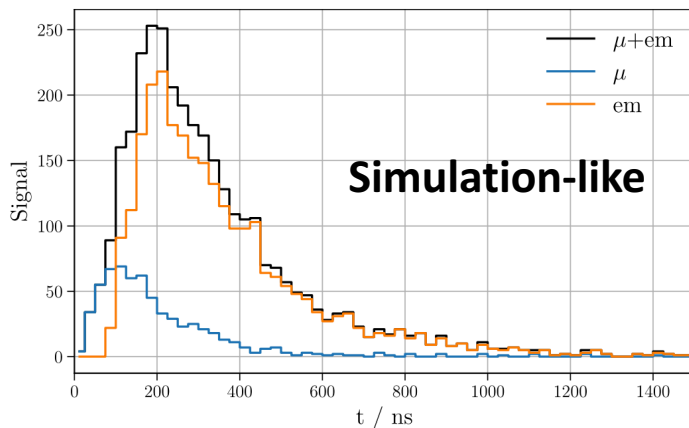
DNNs very sensitive to simulation / data mismatches

Simulation underestimates the muon component

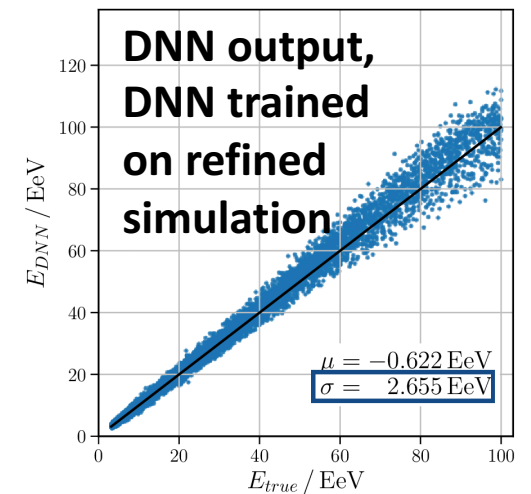
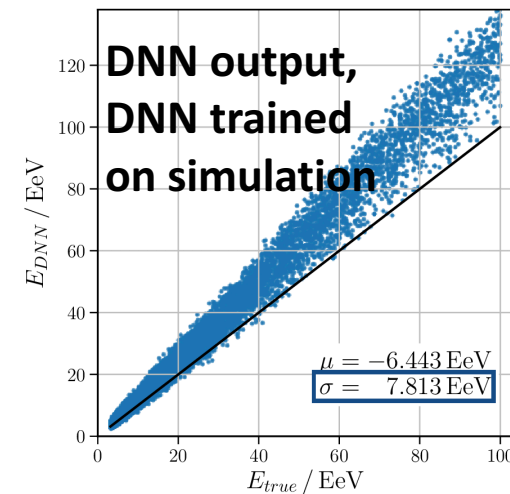
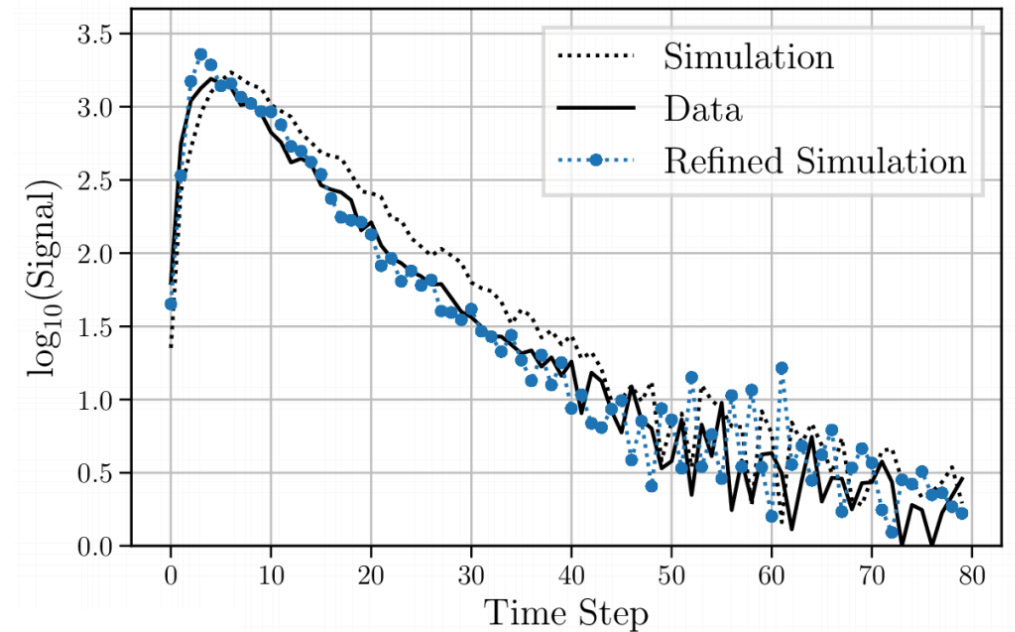
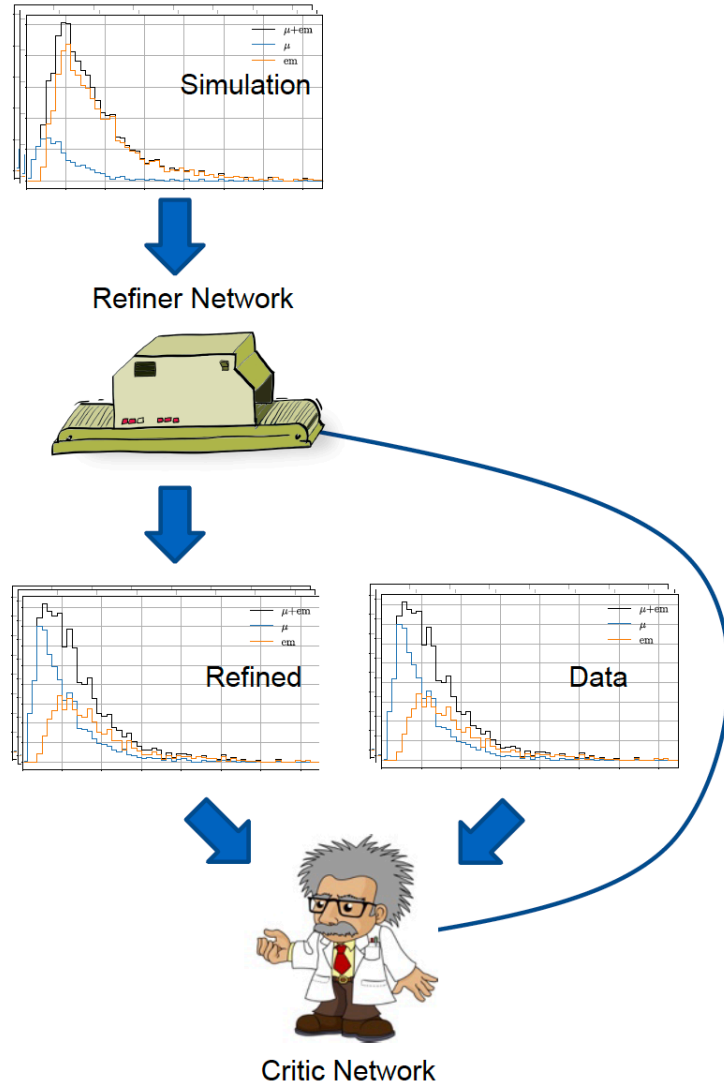
Generate 2 datasets “data-like” and “simulation-like”

Run DNN regression on them

→ DNN does not fit the “data-like” events because it is trained on simulation



Refining Simulation using GANs



Why Quantum Machine Learning?

Quantum approach to ML could solve more complicated problems... faster

ML based tool can recognize complicated (hidden) patterns in data

Quantum processors can produce statistical patterns that are computationally difficult to produce with classical approaches

→ Could quantum processors recognize more complicated patterns in data?

Defining what quantum speed-up means is a complicated task

Need to compare to the “best available” classical algorithm

Quantum ML

... and ML for Quantum Computing

QML introduces quantum algorithms as part of a larger implementation

Fully quantum or hybrid classical/quantum approaches

Input data could be quantistic → ML for QC

How do we construct Quantum Neural Networks (QNN) ?

Direct association between neurons and qubits

Encode information into amplitudes of a quantum state

How do we represent learning rules?

Need association rule between NN activation patterns and pure quantum states

How do we address data loading?

Quantum state preparation

Direct access through qRAM ?

Possible to train on large datasets by only loading a small number of samples!

Principle of Quantum Computing

Circuit model

$$|0\rangle = \begin{pmatrix} 1 \\ 0 \end{pmatrix}, |1\rangle = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

Based on quantum mechanics → Encoding in Quantum Bits (= Qubit)

Superposition of states ; 2^n possible states $|0\rangle, |1\rangle, \dots, |2^n-1\rangle$ for n qubit quantum system

$$|\psi\rangle = \sum_{k=0}^{2^n-1} \alpha_k |k\rangle, \sum_{k=0}^{2^n-1} |\alpha_k|^2 = 1$$

Able to manipulate computations in **parallel**

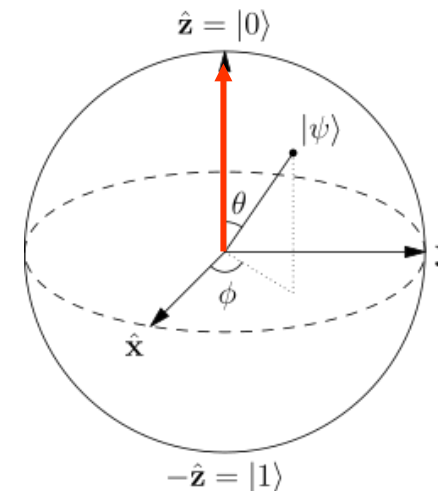
Computation described in unitary quantum logic gates → **Reversible**

Exponentially reduced in space and time

Example :
Pauli-Y-Rotation

$$R_y(\theta) = \begin{pmatrix} \cos \frac{\theta}{2} & -\sin \frac{\theta}{2} \\ \sin \frac{\theta}{2} & \cos \frac{\theta}{2} \end{pmatrix}$$

$$R_y(\theta)|0\rangle = \cos(\theta/2)|0\rangle + \sin(\theta/2)|1\rangle$$



Quantum GAN

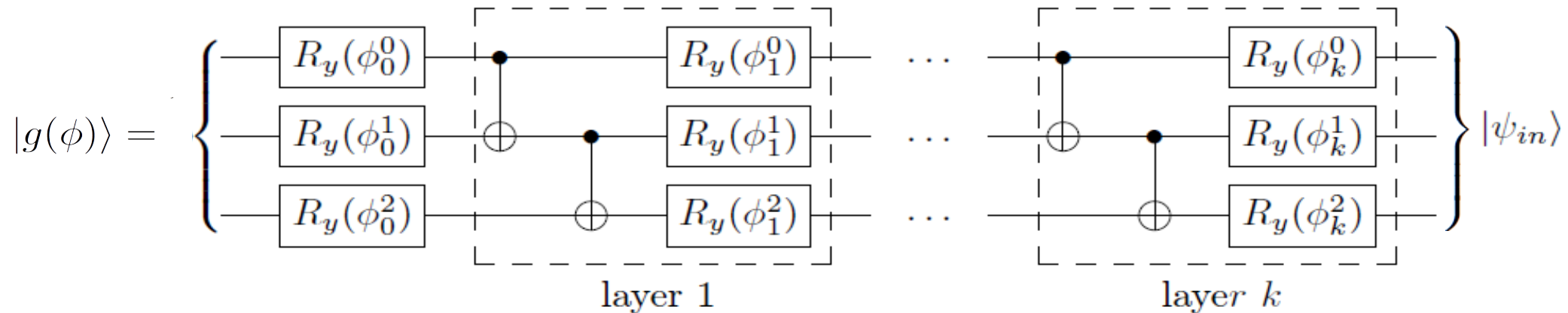
$$G(\phi) |\psi_{in}\rangle = |g(\phi)\rangle = \sum_{i=0}^{N-1} \sqrt{p_g^i(\phi)} |i\rangle$$

Based on **IBM QGAN** implementation

Hybrid model : Quantum Generator + Classical Discriminator

Efficient in **loading and learning a probability** over discrete values

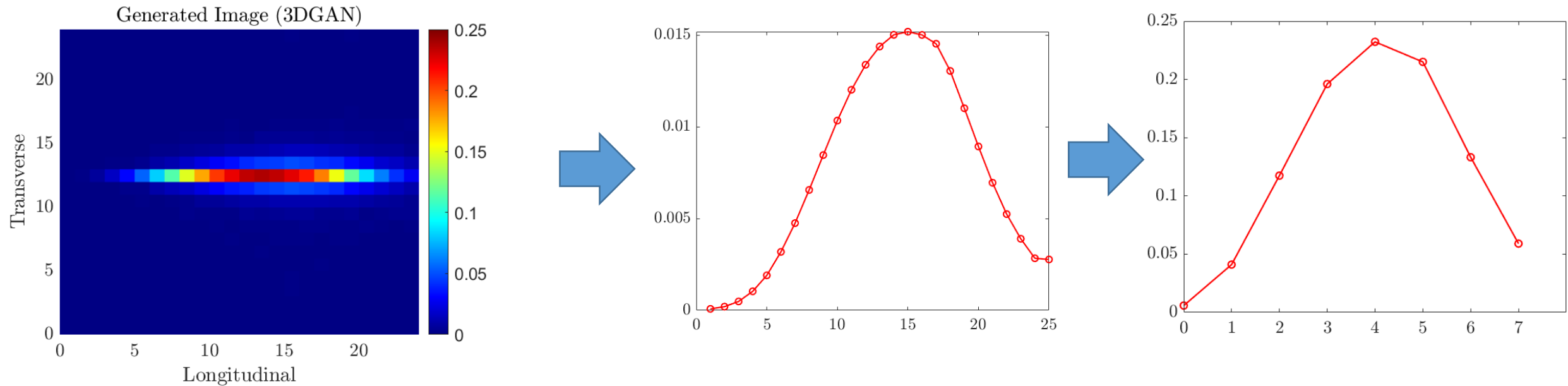
Increase resolution by adding qubit



A simplified 3DGAN

25x25x25 too big for initial test: reduce to 1D distribution

Focus on longitudinal energy profile



Binned into $2^n = N$ pixels $\rightarrow$ Map to 8 values expressed by 3-qubit generator

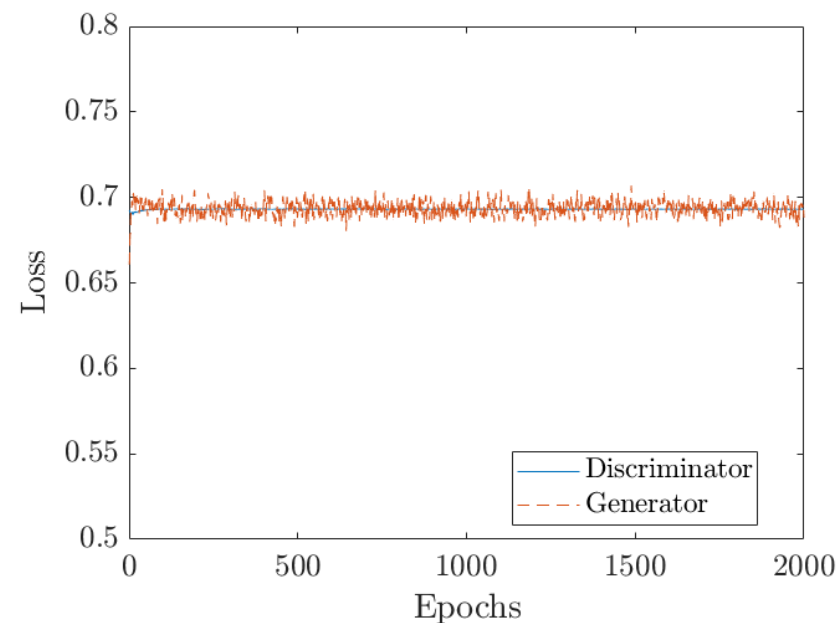
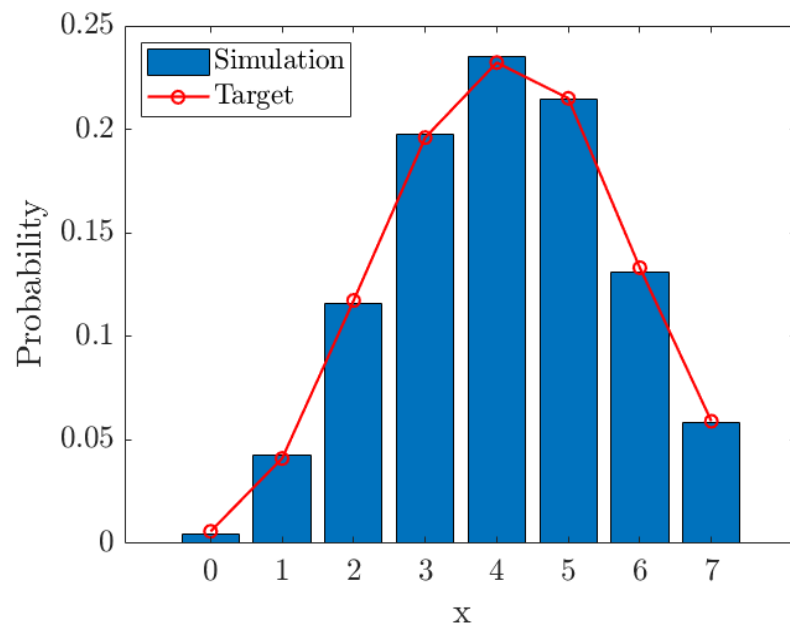
Probability of getting state $|k\rangle$ = (Relative) Energy at pixel k

Reproducing longitudinal energy shape

Generator: 3 qubits, 3 layers

Classical Discriminator: 512 nodes + Leaky ReLU $\rightarrow$ 216 nodes + Leaky ReLU $\rightarrow$ single-node + sigmoid

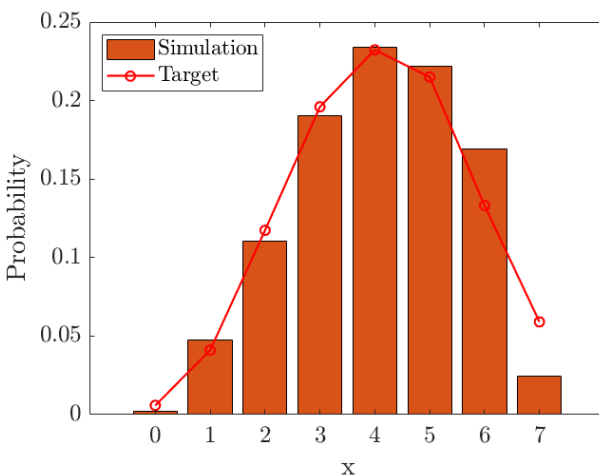
AMSGRAD optimizer for both generator and discriminator



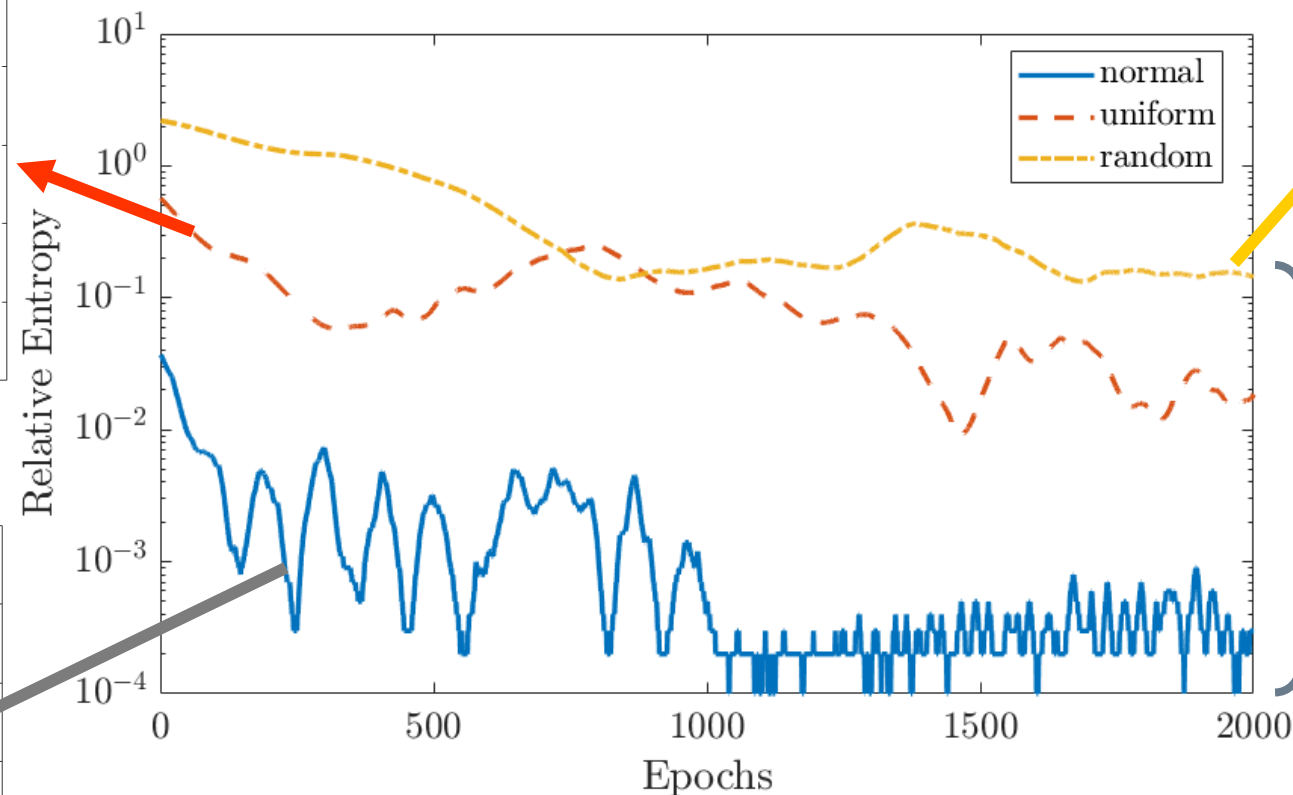
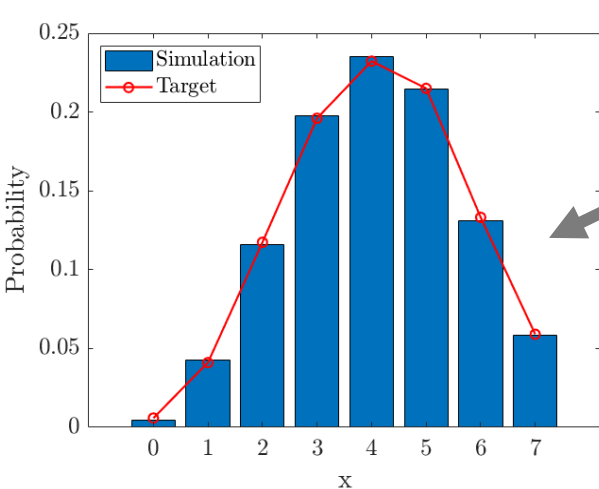
Preparation of the initial state

Progress in relative entropy for 3 qubits & depth 3

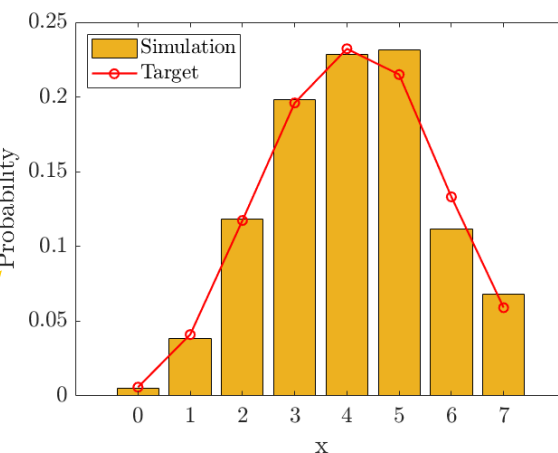
Uniform



Normal



Random



Quality of result depends on initial states

Understanding performance

Kolmogorov-Smirnov Statistics : Measures equality between $P(x)$ & $Q(x)$

→ With 95% confidence level & 1,000 samplings, null hypothesis is accepted if $D_{KS} \leq 0.0547$

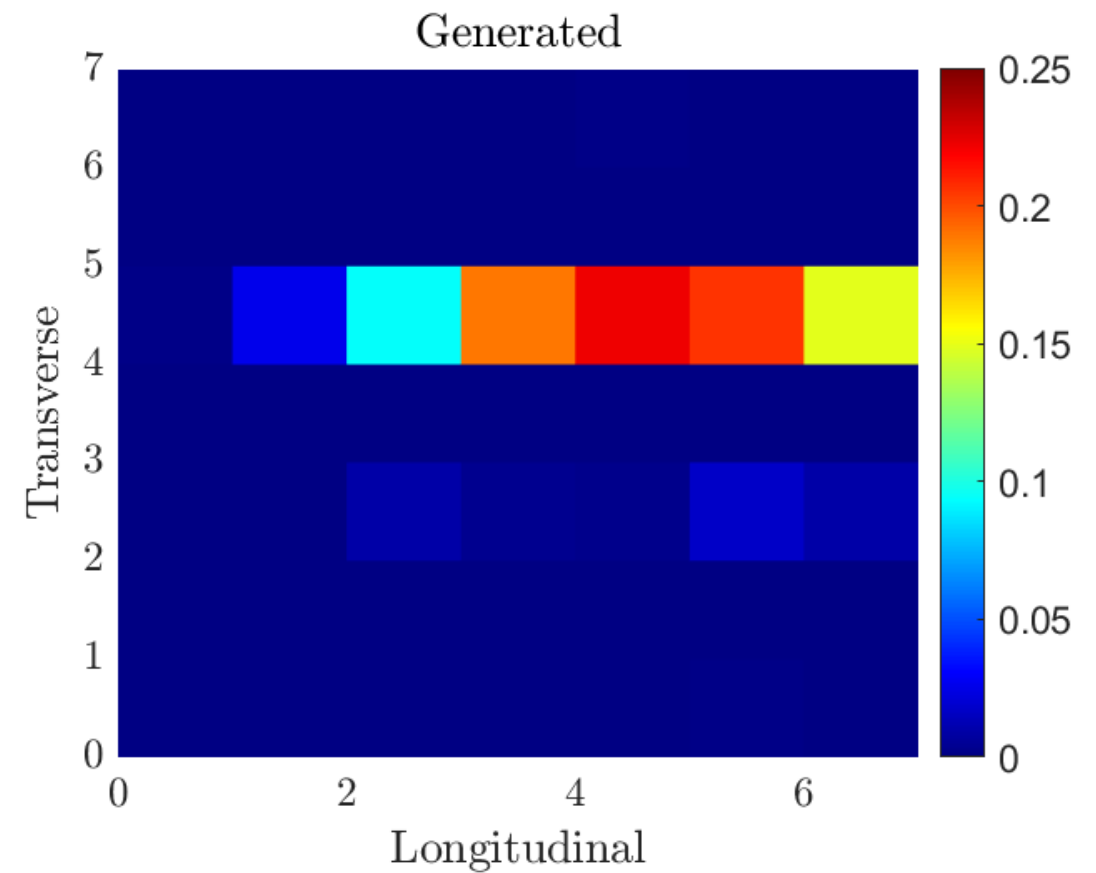
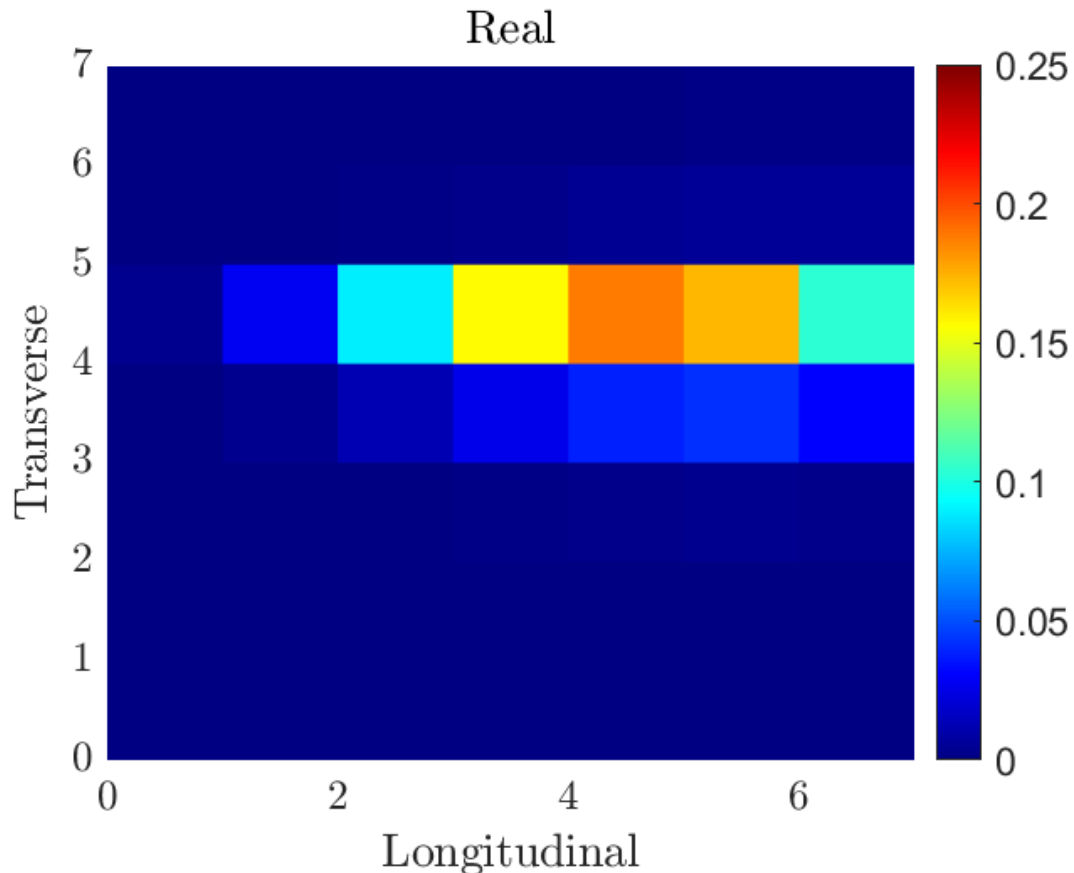
Initialization	depth	D_{KL}	$D_{KS} (\times 10^{-2})$	Accept/Reject
normal	1	0.031 ± 0.042	0.033 ± 0.024	Accept
	2	$(1.9 \pm 1.7) \cdot 10^{-3}$	0.024 ± 0.002	Accept
	3	$(5.0 \pm 3.0) \cdot 10^{-4}$	0.038 ± 0.008	Accept
uniform	1	0.044 ± 0.003	0.048 ± 0.007	Accept
	2	0.12 ± 0.04	0.072 ± 0.018	Reject
	3	0.070 ± 0.039	0.054 ± 0.017	Accept
random	1	0.051 ± 0.096	0.042 ± 0.015	Accept
	2	0.096 ± 0.162	0.042 ± 0.026	Accept
	3	0.072 ± 0.078	0.059 ± 0.017	Reject

First attempts at 2D (6 qubits)

Using more powerful discriminator (4 hidden layers)

Uniform initialization + depth 1

After 3,000 epochs, able to reproduce similar shape



Conclusions... again

Generative Models are powerful techniques

Fast simulation applications are reaching a high level of accuracy

Performance validation remains a key issue

Need to start designing **common procedures**

Results validations

Integration

Computing resources availability is a driving factor of the problem size we can solve

Benefit from dedicated hardware and accelerators (GPUs, FPGAs, TPUs)

DL development is accelerated by a diversified community

Continuous R&D and **collaboration** with external partner is essential

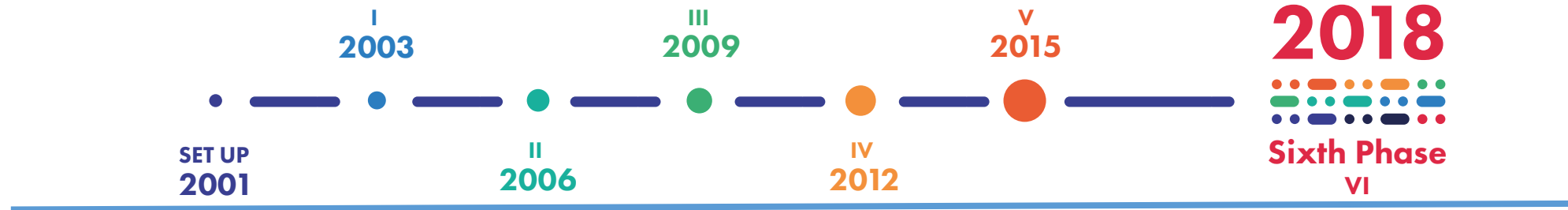
Thanks!

Questions?



CERN OPENLAB

Driving Innovation since 2001



Evaluate and test state-of-the-art technologies in a challenging environment. **Improve** them in collaboration with industry

JOINT R&D

MANAGEMENT

INNOVATION & KNOWLEDGE SHARING

Collaborate with other communities. Create knowledge and innovation.

Communicate results, demonstrate **impact**, and **outreach**.

COMMUNICATION

EDUCATION

Train the next generation of engineers/researchers, **promote** education and cultural exchanges.

JOINT R&D PROJECTS

