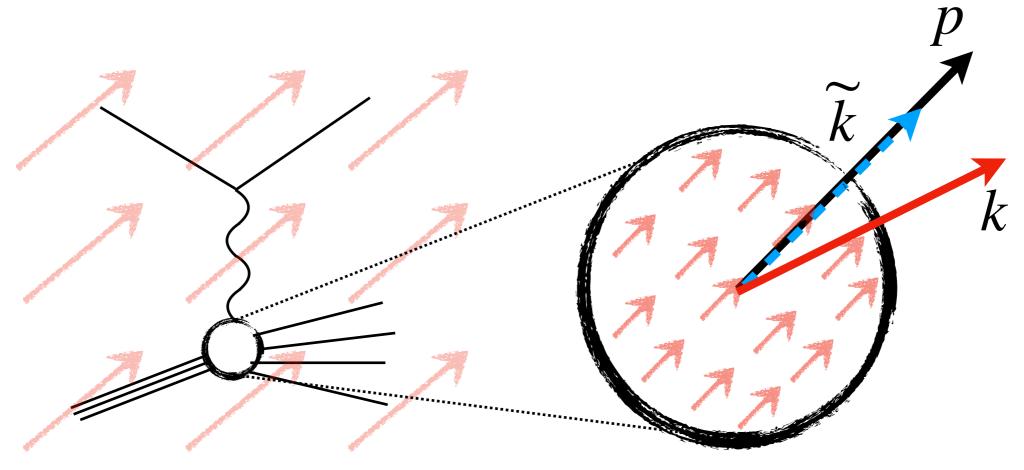
Lorentz violation analysis with ZEUS data





Nathan Sherrill Indiana University ZEUS meeting, January 2020



In collaboration with Enrico Lunghi

Talk overview

What is Lorentz violation?

How to search for Lorentz violation?

Effects on high-energy hadrons

Application: deep inelastic scattering

Estimates for colliders

An analysis with real data

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Based on: arXiv:1911.04002; PRD 98, 115018 (2018); PLB 769, 272 (2017)

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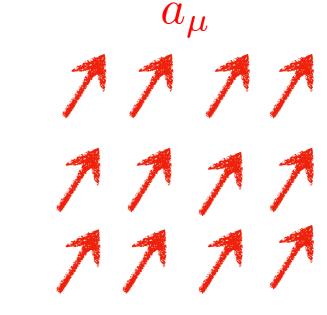
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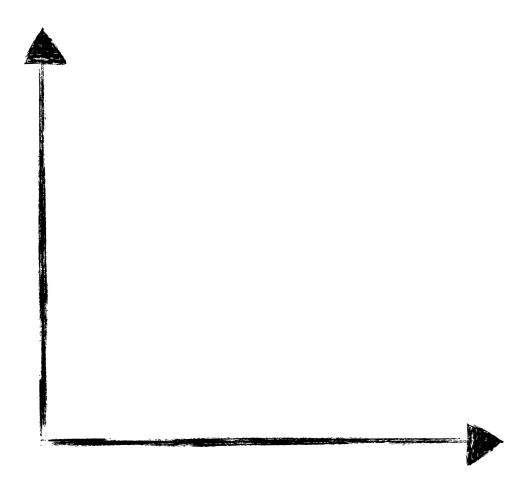
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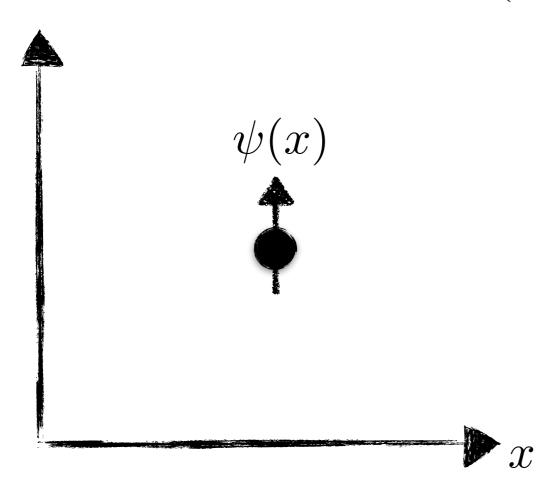
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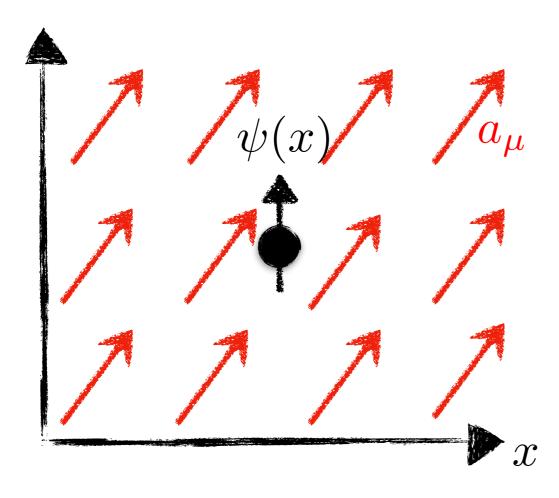
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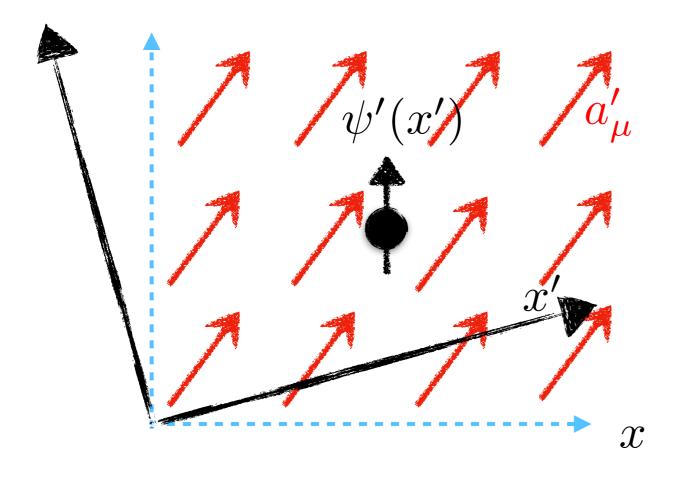
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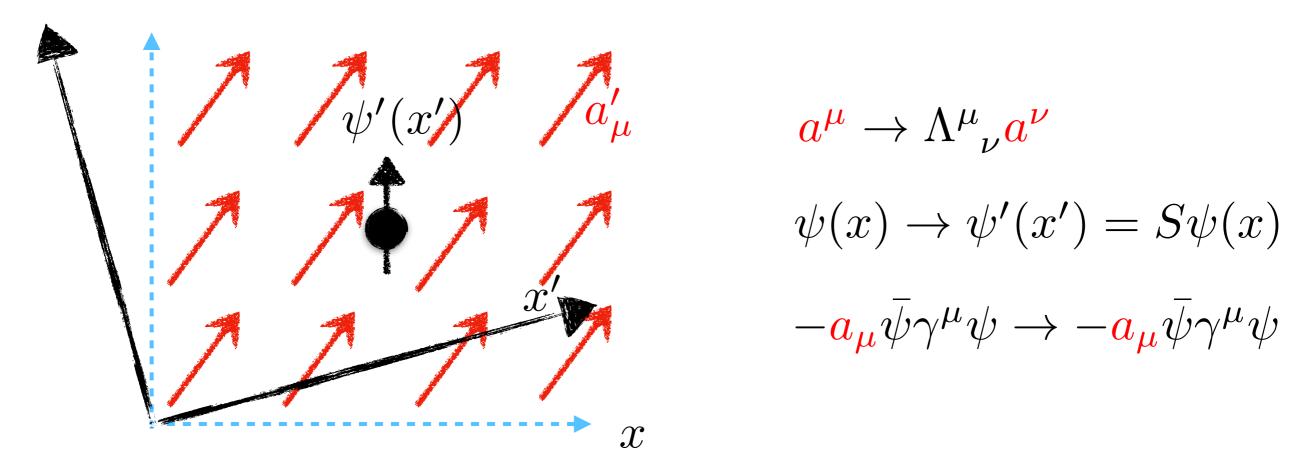
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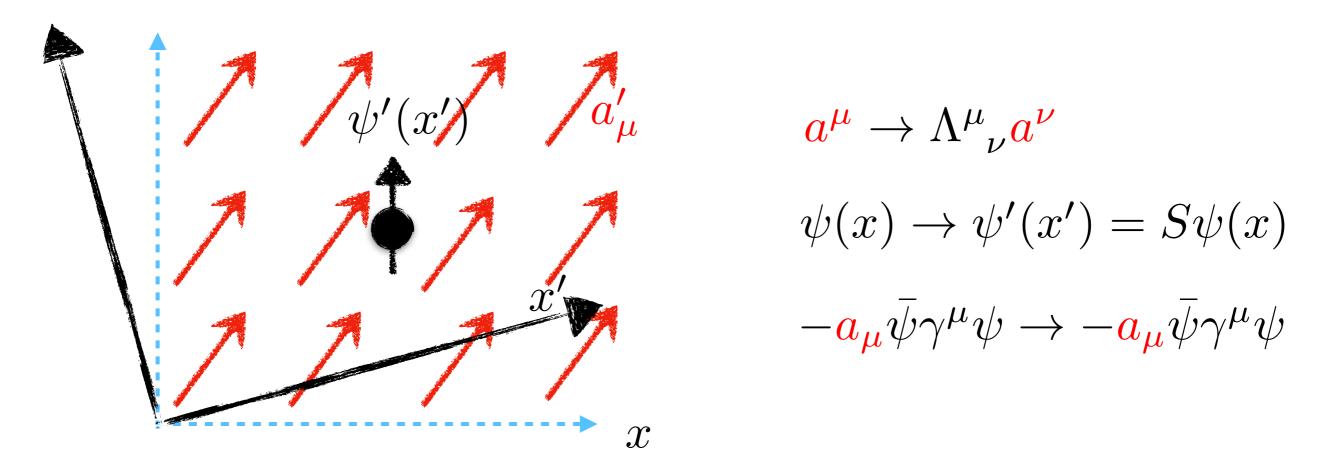


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An observer Lorentz transformation (OLT) is a coordinate transformation

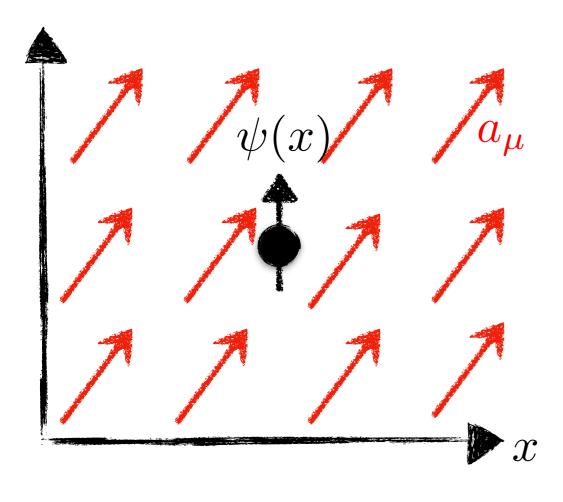


Under an OLT the background a_{μ} transforms like an ordinary four vector

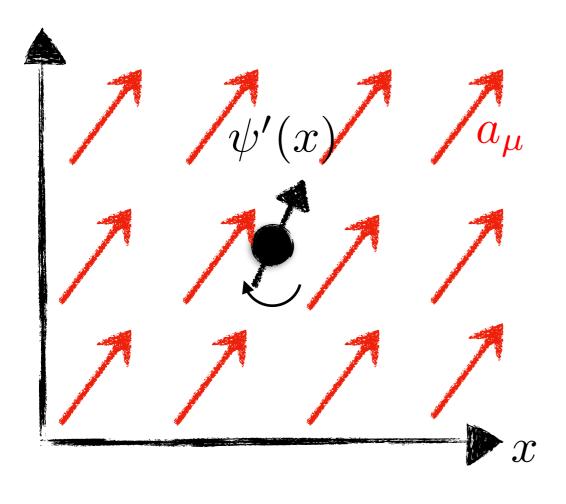
Hence, there is no change in the physics; the background cannot be seen by performing observer transformations (changing coordinates)

A particle Lorentz transformation (PLT) is a transformation of the physical system

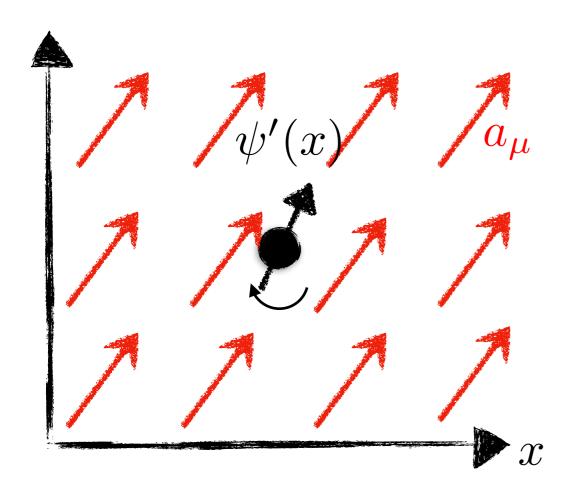
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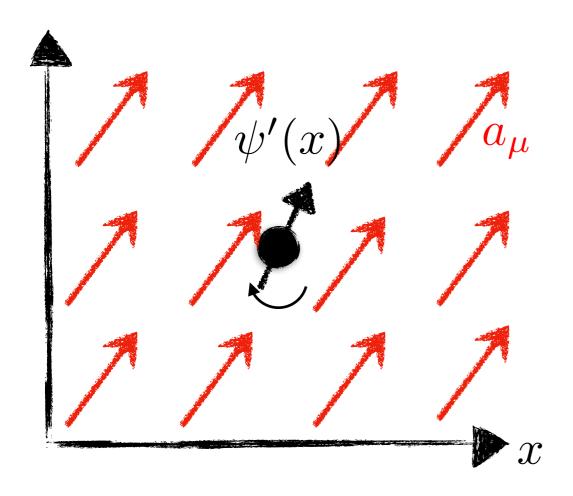
$$\psi(x) \to \psi'(x) = S\psi(\Lambda^{-1}x)$$

Net physical effect

$$-a_{\mu}\bar{\psi}\gamma^{\mu}\psi \to -\left(\Lambda^{-1}\right)_{\mu\nu}a^{\nu}\bar{\psi}\gamma^{\mu}\psi$$

$$\neq -a_{\mu}\bar{\psi}\gamma^{\mu}\psi$$

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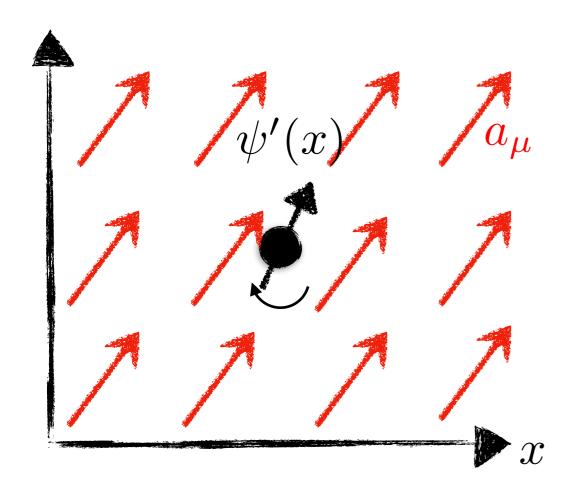
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Unlike OLTs, PLTs can produce physical effects as a result of the background

The rotated system obeys a different physical law than the same system with rotated coordinates

⇒ Lorentz violation!

We use a model-independent, effective field theory framework: the Standard-Model Extension (SME)*

*D. Colladay, V. A. Kostelecký, PRD 55, 6760 (1997); PRD 58, 1166002 (1998)

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- "Coefficients for Lorentz violation"
- Observer Lorentz tensors
- Coupling constants
- Necessarily small (perturbative)
- Experimentally accessible!

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Data Tables for Lorentz and CPT Violation

V. Alan Kostelecký^a and Neil Russell^b

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January 2020 update of Reviews of Modern Physics 83, 11 (2011) [arXiv:0801.0287]

This work tabulates measured and derived values of coefficients for Lorentz and CPT violation in the Standard-Model Extension. Summary tables are extracted listing maximal attained sensitivities in the matter, photon, neutrino, and gravity sectors. Tables presenting definitions and properties are also compiled.

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Table D19. Nonminimal photon sector, $d=7$					
Combination	Result	System	Ref.		
$ \sum_{jm} Y_{jm}(110.47^{\circ}, 71.34^{\circ})k_{(V)jm}^{(7)} $	$< 2 \times 10^{-6} \text{ GeV}^{-3}$	Spectropolarimetry	[170]		
$ \sum_{jm} Y_{jm}(110.47^{\circ}, 71.34^{\circ}) k_{(V)jm}^{(7)} \sum_{jm} Y_{jm}(330.68^{\circ}, 42.28^{\circ}) k_{(V)jm}^{(7)} $	$< 4 \times 10^{-6} \text{ GeV}^{-3}$	"	[170]		
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100s of bounds for nearly every major subfield of physics

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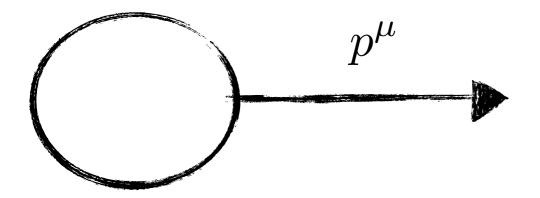
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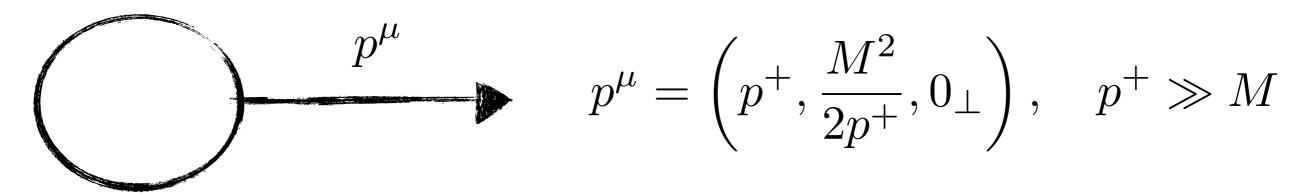
Much of the QCD sector is yet to be explored!

Consider a high-energy hadron

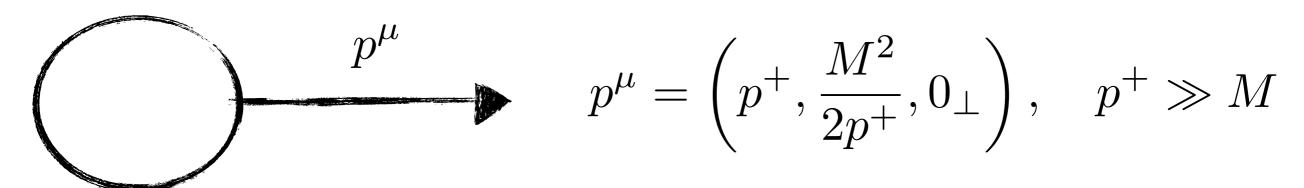
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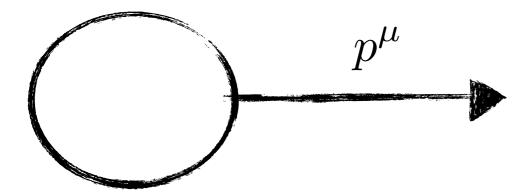
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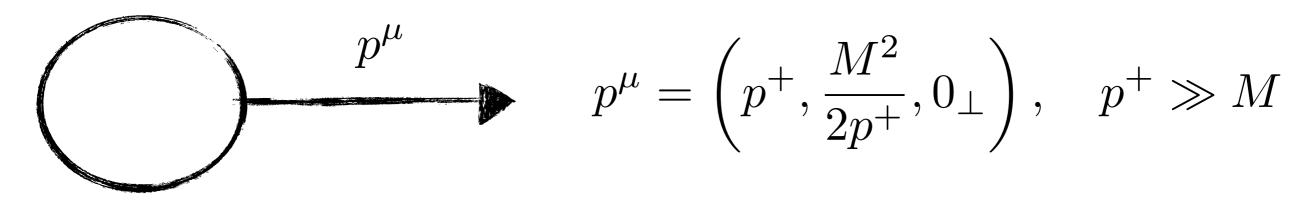
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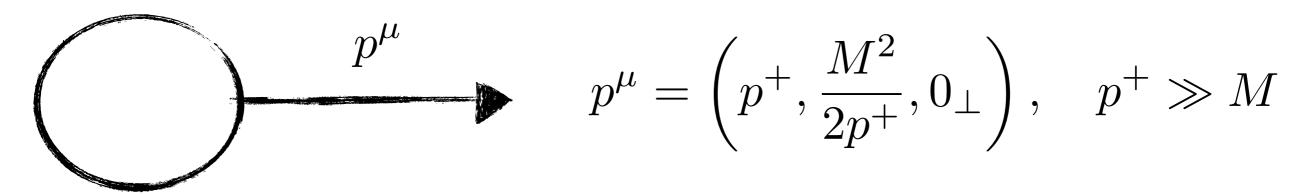
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Fraction of plus momenta is boost invariant, leading to familiar parameterization for high-energy, massless, on-shell partons within hadrons

$$\xi \equiv k^+/p^+$$
$$k^\mu = \xi p^\mu$$

Covariant expression; can be used in any frame

Massless quarks modified by Lorentz-violating effects

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+ \left(c^{(4)}\right)_{AB}^{\mu\nu}\bar{\psi}_{A}\gamma_{\mu}iD_{\nu}\psi_{B} + \left(d^{(4)}\right)_{AB}^{\mu\nu}\bar{\psi}_{A}\gamma_{5}\gamma_{\mu}iD_{\nu}\psi_{B} \cdots
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We consider the following (spin-independent, flavor-diagonal) effects

$$\mathcal{L} = \sum_{f=u,d} \frac{1}{2} \bar{\psi}_f \gamma^{\mu} i D_{\mu} \psi_f + \frac{1}{2} (c_f^{(4)})^{\mu\nu} \bar{\psi}_f \gamma_{\mu} i D_{\nu} \psi_f$$
$$- (a_f^{(5)})^{\mu\alpha\beta} \bar{\psi}_f \gamma_{\mu} i D_{(\alpha} i D_{\beta)} \psi_f + \text{h.c.}$$

Modified Dirac equation

$$[(\eta^{\mu\nu} + c_f^{\mu\nu})\gamma_{\mu}i\partial_{\mu} - a_f^{(5)\mu\alpha\beta}\gamma_{\mu}i\partial_{\alpha}i\partial_{\beta}]\psi_f = 0$$

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$$\widetilde{k}^2 = k^2 + \mathcal{O}(\text{coefficients}) = 0$$

$$E^2 = |\vec{k}|^2 + \mathcal{O}(\text{coefficients})$$

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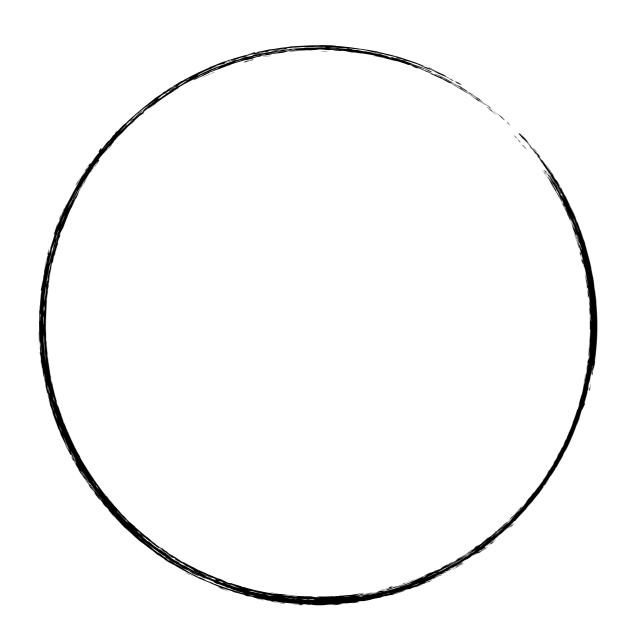
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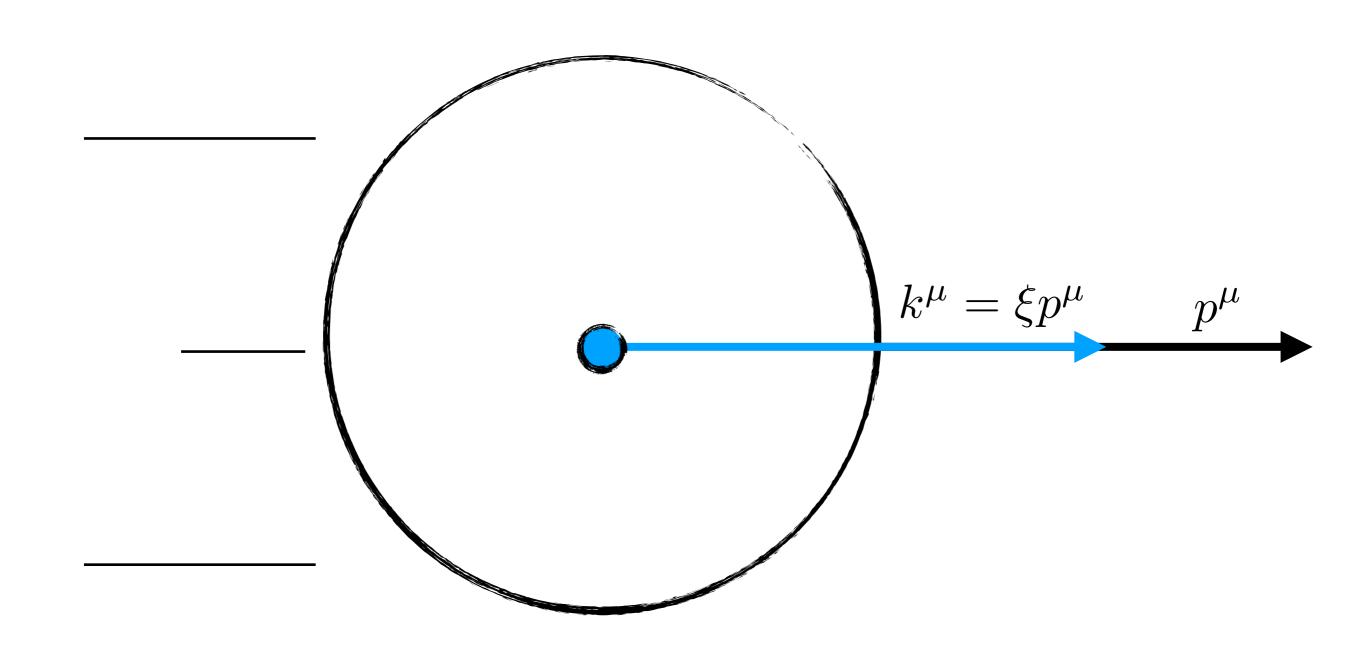
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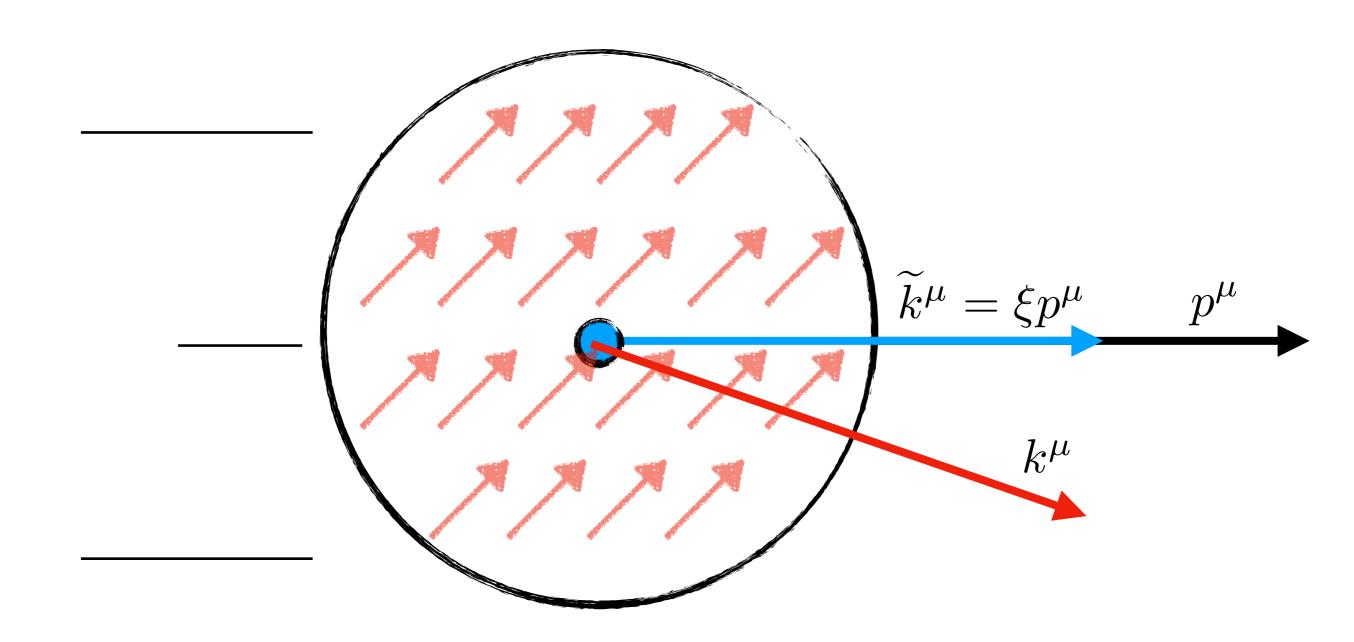
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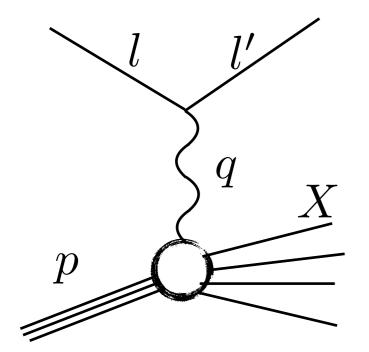
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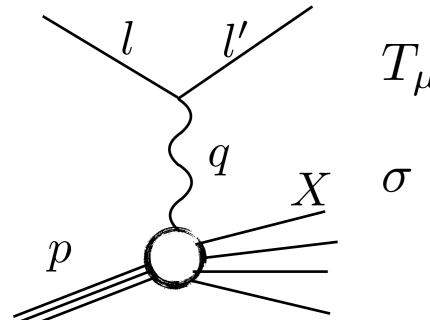
Instead, for a covariant definition to be retained $\,\widetilde{k}^{\mu} = \xi p^{\mu}\,$





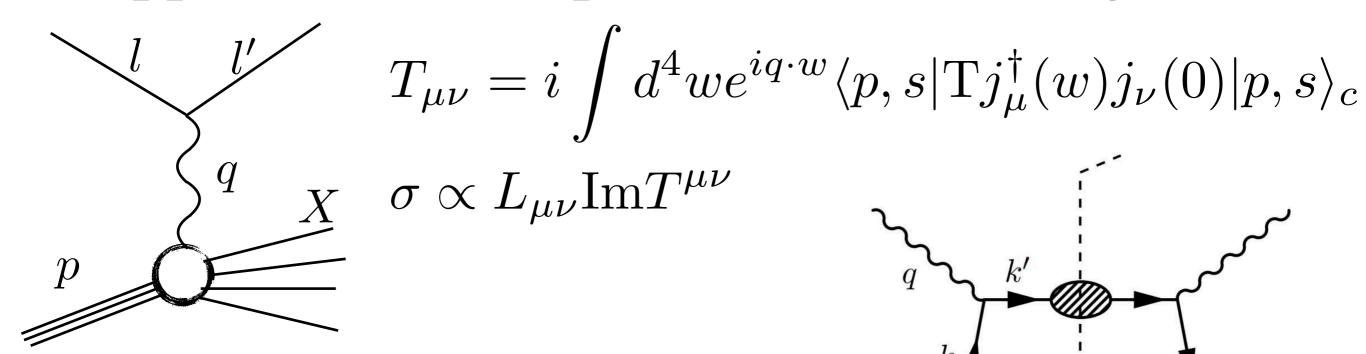




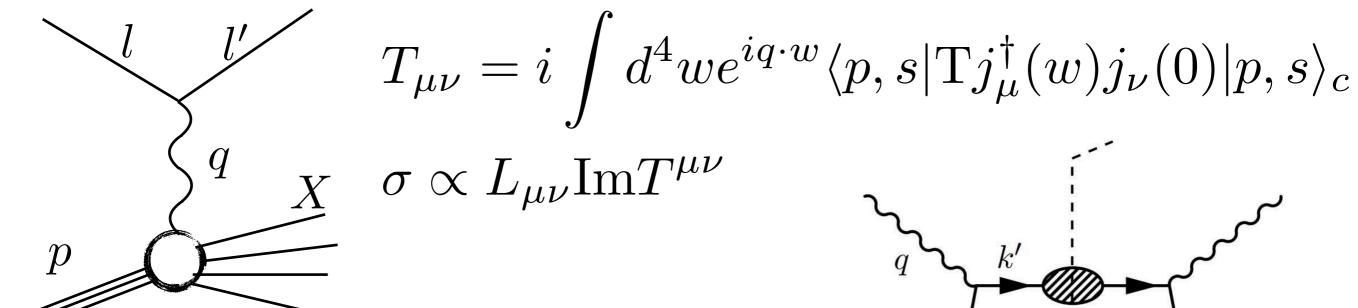


$$T_{\mu\nu} = i \int d^4w e^{iq \cdot w} \langle p, s | T j^{\dagger}_{\mu}(w) j_{\nu}(0) | p, s \rangle_c$$
$$\sigma \propto L_{\mu\nu} \text{Im} T^{\mu\nu}$$

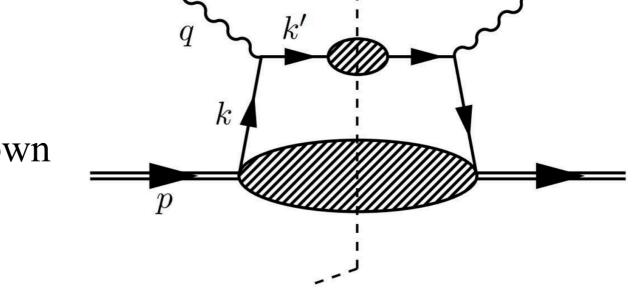
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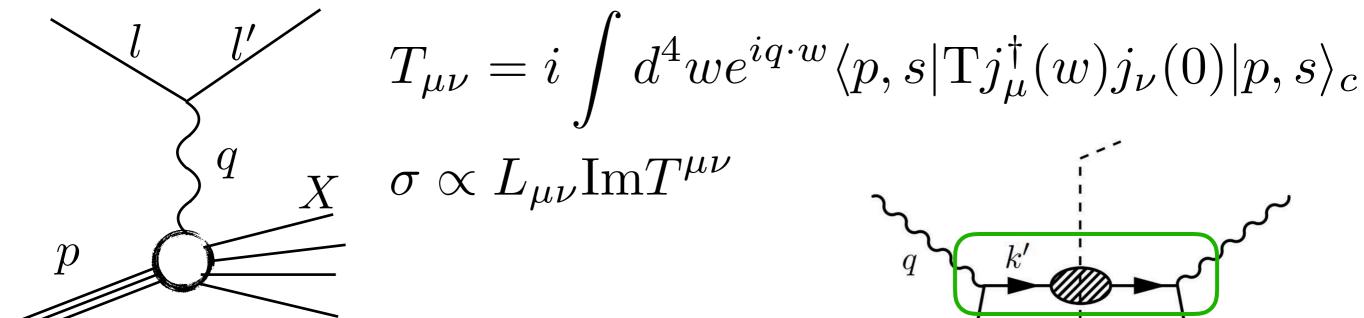
Factorization in DIS limit most simply shown in frame where $\vec{p} + \vec{q} = \vec{0}$



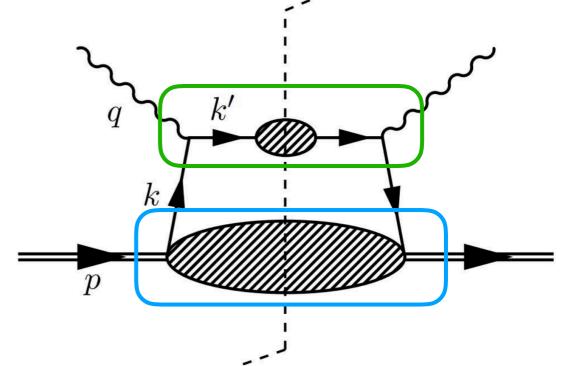
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$$\sigma \sim \int d\xi \sigma_{\rm parton}(\xi) f(\xi) + \text{small corrections}$$



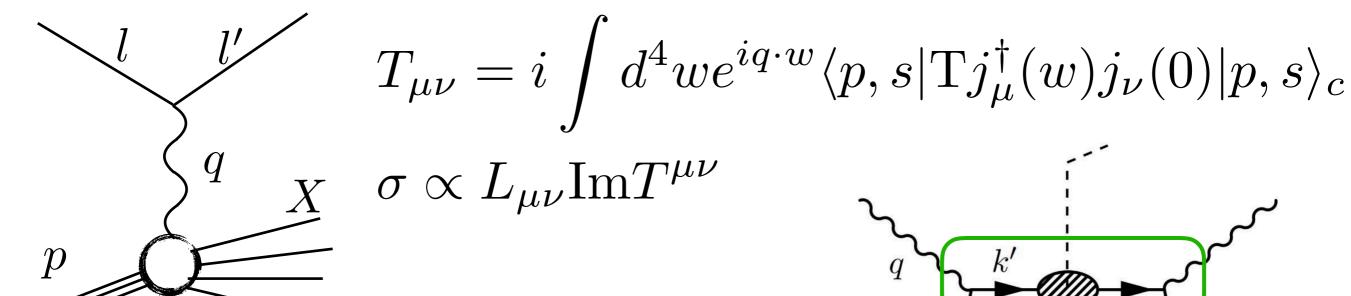
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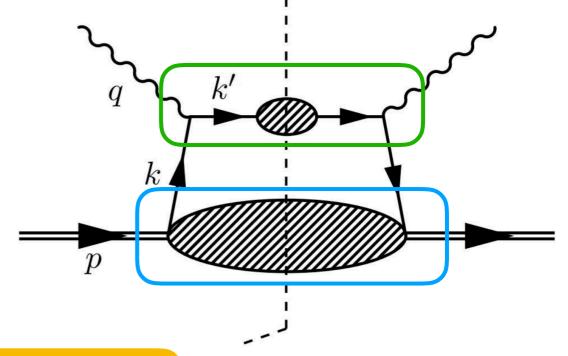
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- kinematical corrections
- radiative effects



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What happens when Lorentz violation is present?

In the presence of Lorentz violation, factorization occurs in a modified Breit frame

$$\vec{p} + \tilde{\vec{q}} = \vec{0}$$
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$$\operatorname{Im} \frac{1}{\widetilde{k}^2 + i\epsilon} = -\pi \left[\delta(\widetilde{k}^2) \theta(k^0) + \delta(\widetilde{-k}^2) \theta(-k^0) \right]$$

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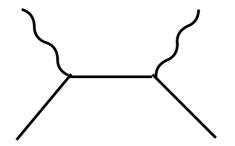
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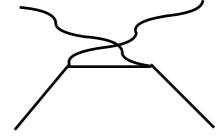
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Quark initiated

Antiquark initiated

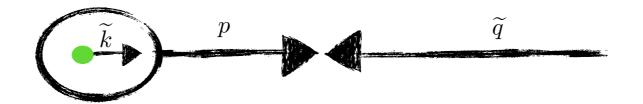
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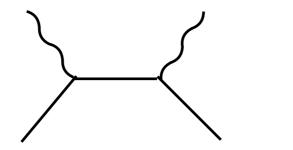
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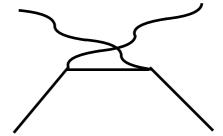
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Will focus on quark contribution

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$$\frac{\langle \text{hadron} | \Gamma^{+} | \text{hadron} \rangle}{\langle \text{hadron} | \Gamma^{+} | \text{hadron} \rangle} \sim f_{f}(\xi, \dots) = \int \frac{d\lambda}{2\pi} e^{-i\xi p \cdot n\lambda} \langle p | \bar{\psi}(\lambda \tilde{n}_{f}) \frac{\gamma_{\mu} n^{\mu}}{2} \psi(0) | p \rangle$$

$$n^{\mu} + c_{f}^{\mu \alpha} n_{\alpha}$$

"Shifted" conventional scenario

Using data from HERA, the LHC, and the future electron-ion collider (EIC) we obtain *estimates* on the sensitivity to the coefficients of interest

Technique relies on coefficient combinations that exhibit sidereal time dependence

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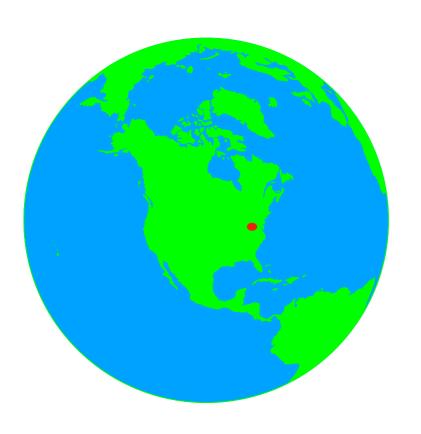
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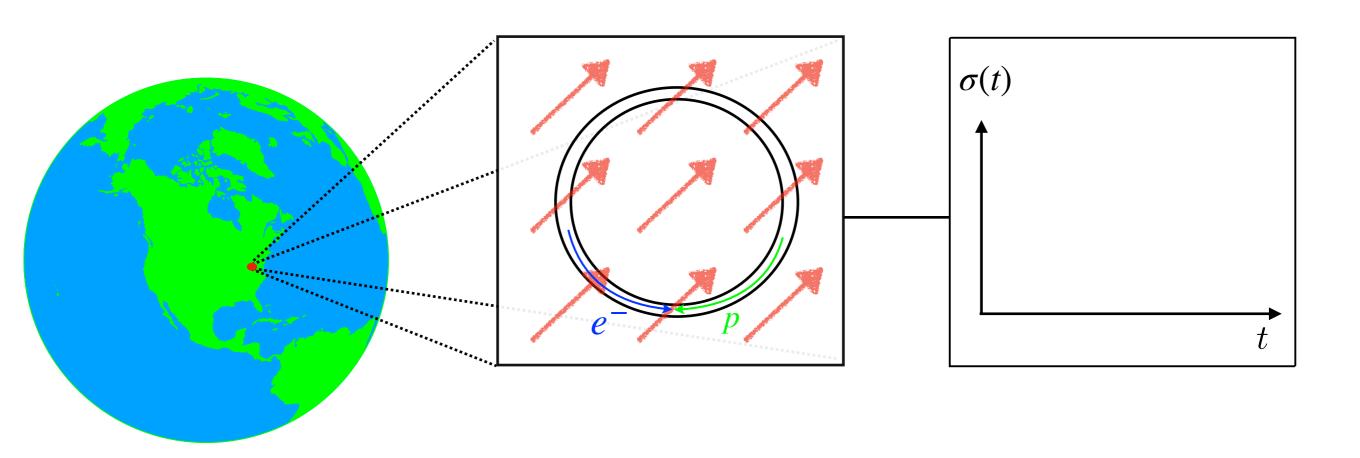
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23 hrs 56 mins

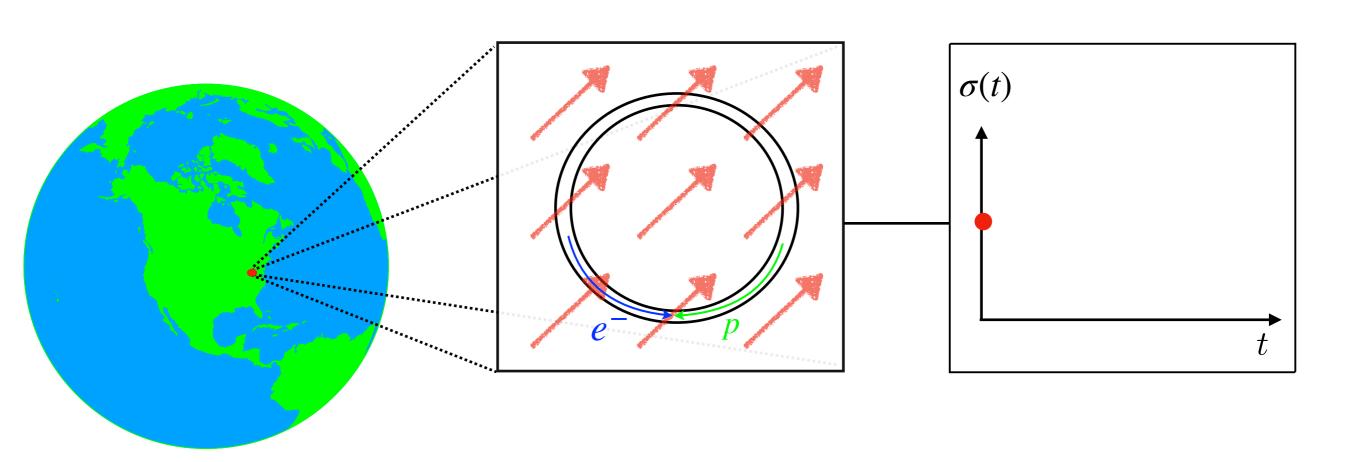
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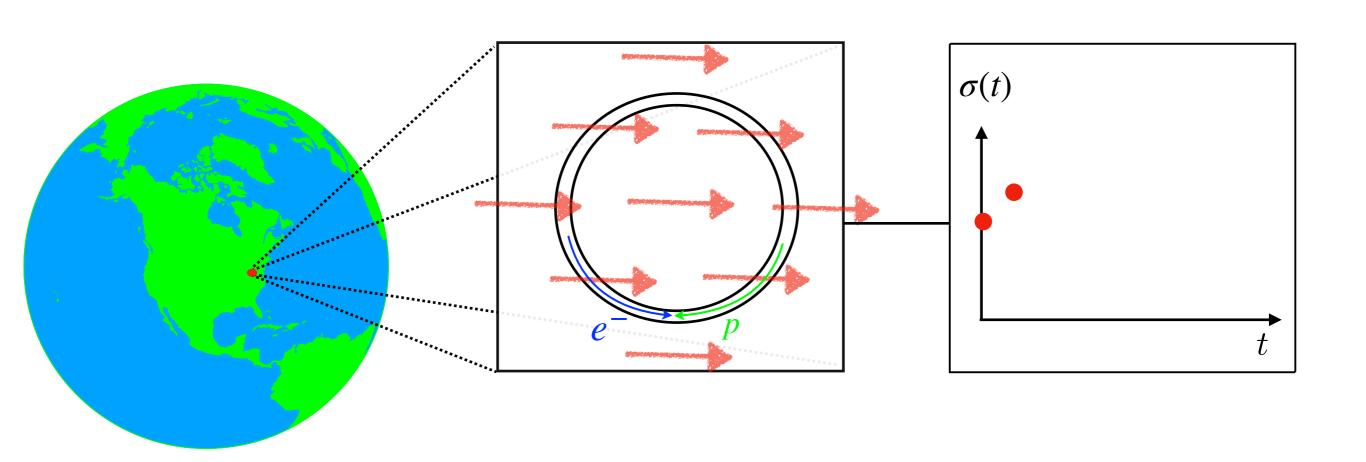
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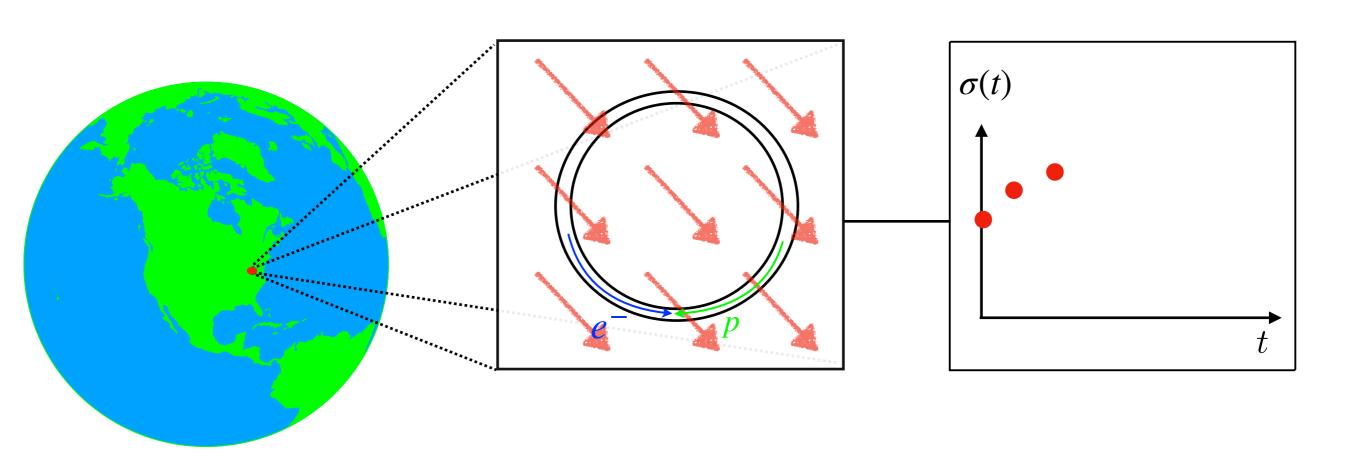
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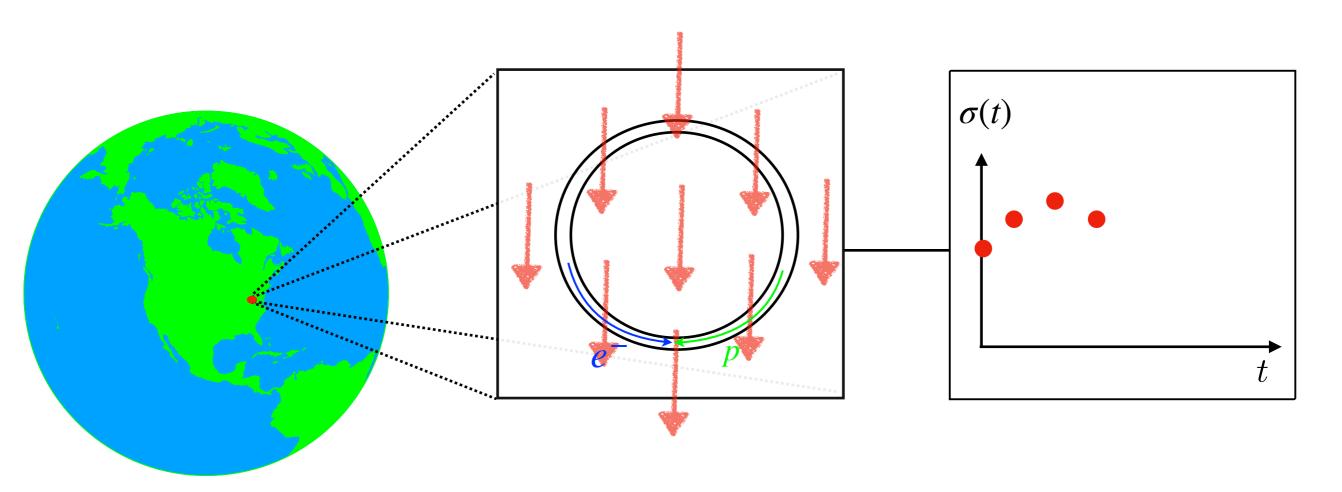
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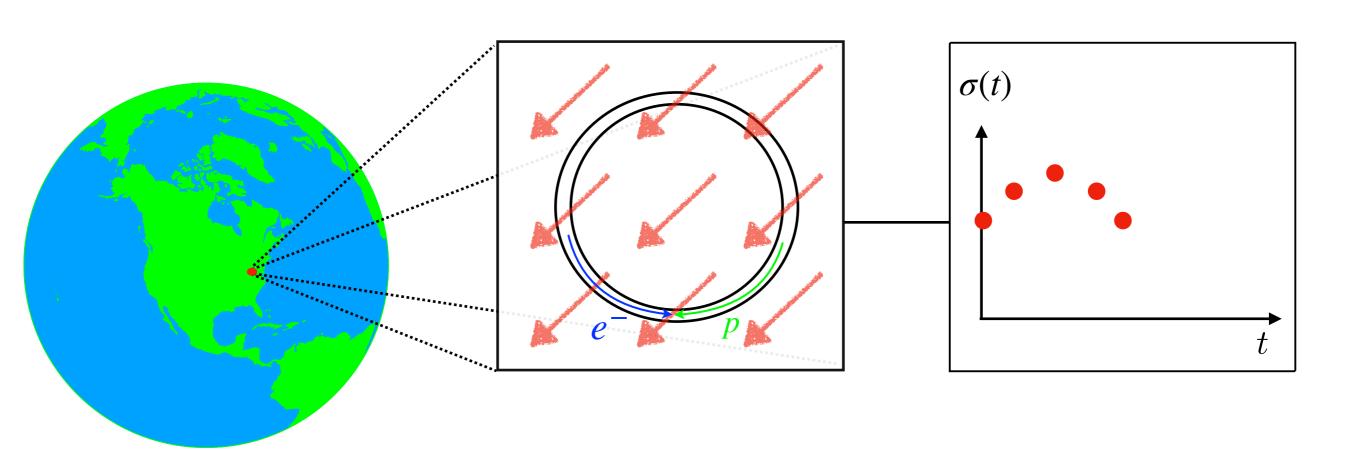
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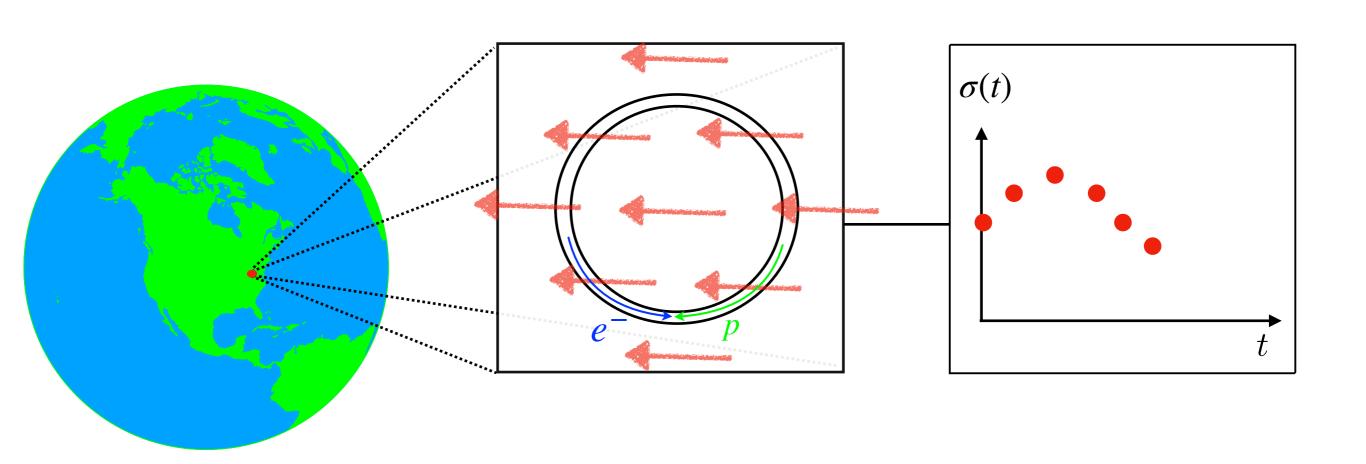
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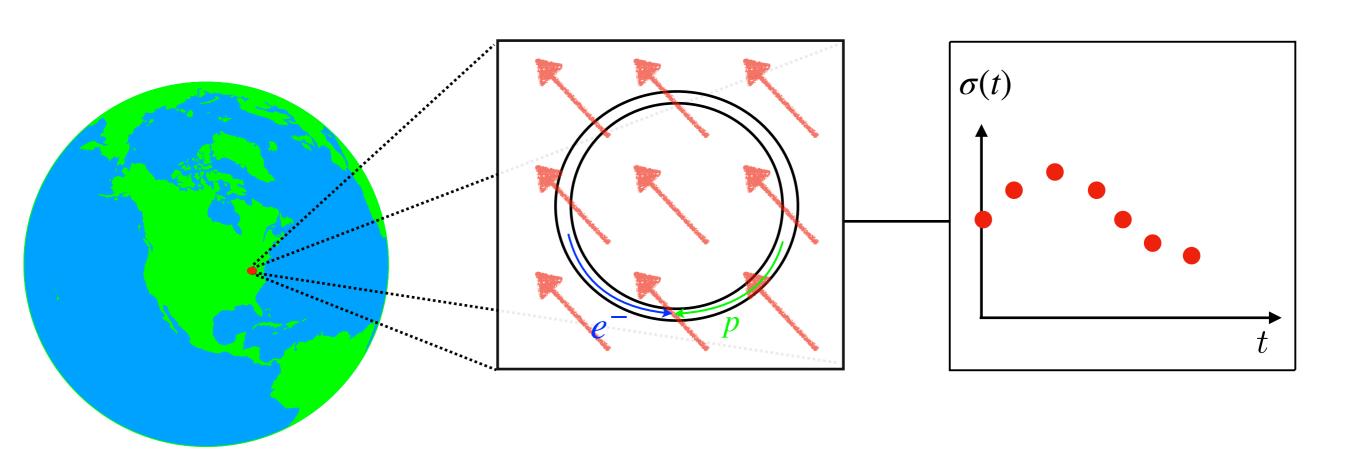
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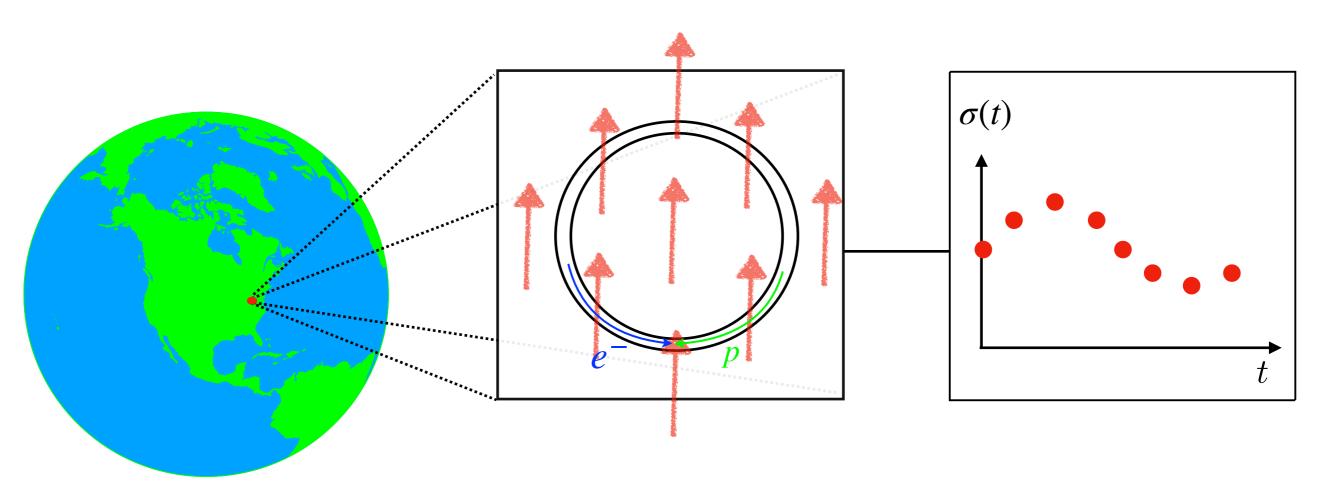
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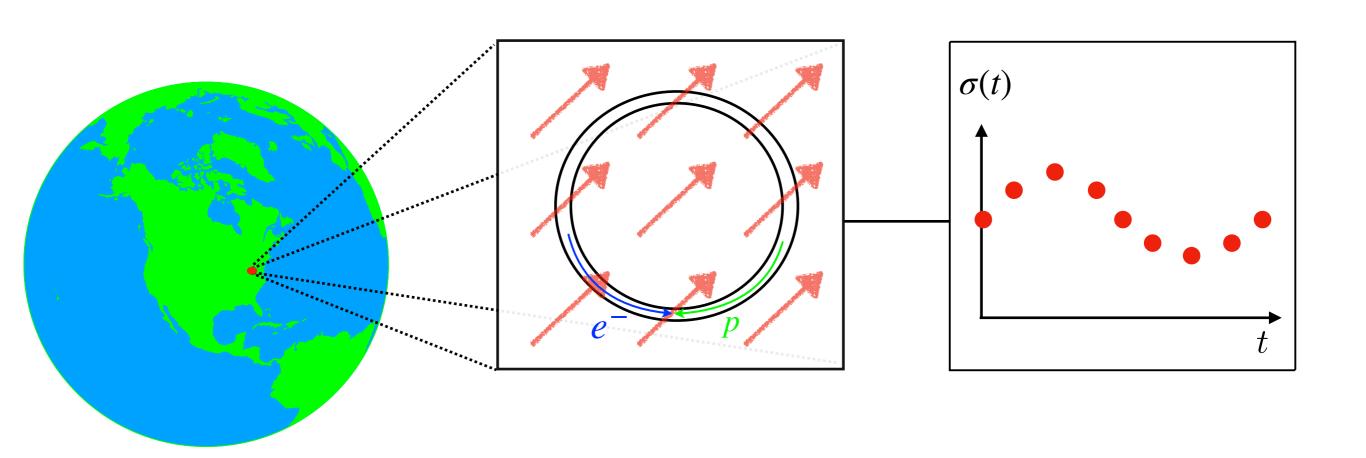
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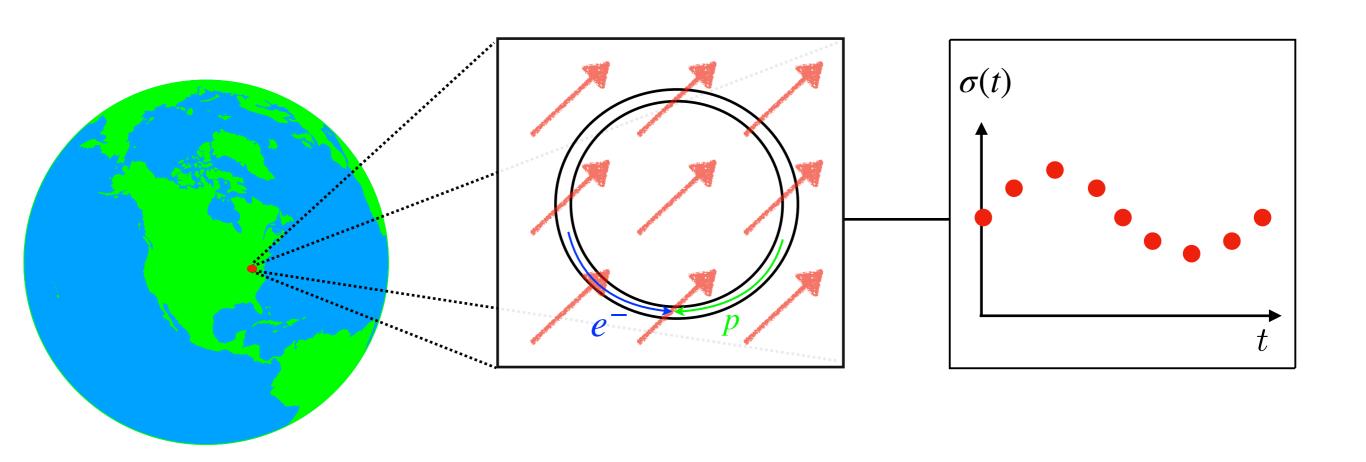
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Coefficients also depend on laboratory colatitude and beam directions!

Extract bounds on coefficients: Using H1 and ZEUS combined 644 neutral-current DIS measurements (Eur. Phys. J. C75 (2015)). For each (x,Q) value:

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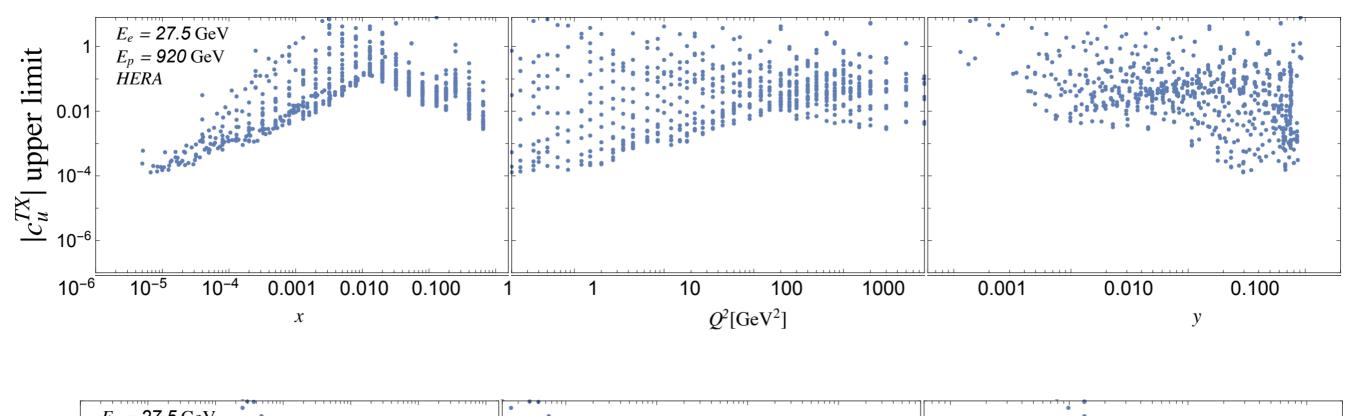
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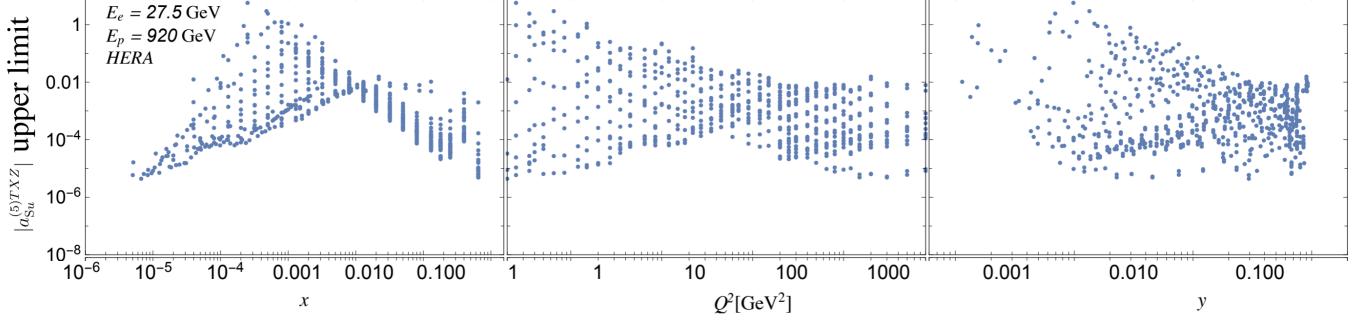
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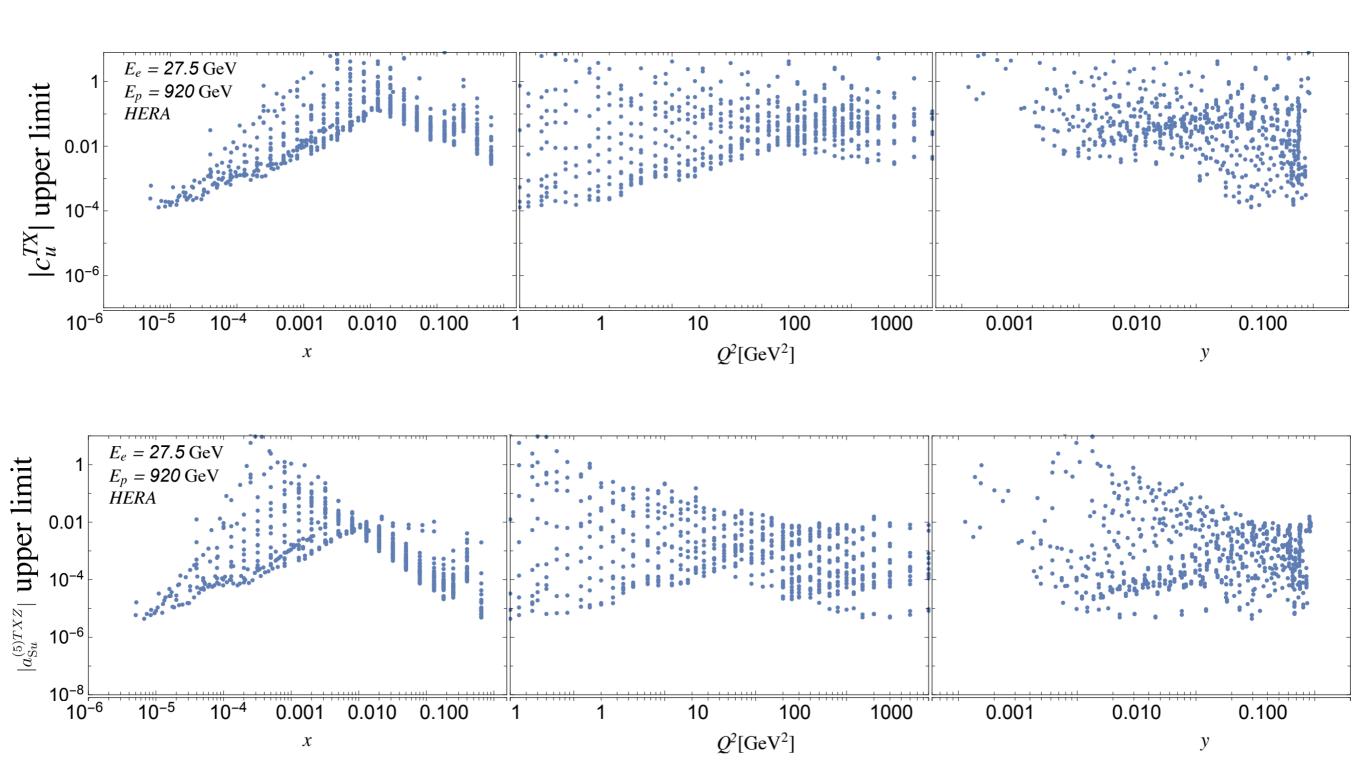
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• Minimize and extract 95% CL constraint







Generally speaking, region of most sensitivity at low x, low-moderate Q, and higher collision energies

An actual experimental search

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What is needed (?):

- Cross sections as functions of (x, Q) in (4-8) bins of sidereal time
- Understanding of systematics: which uncertainties matter over the course of a few hours in a day? E.g., beam luminosity ~ constant?
- Since SME cross section is different in each bin, can construct observables that partially shield against systematics

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