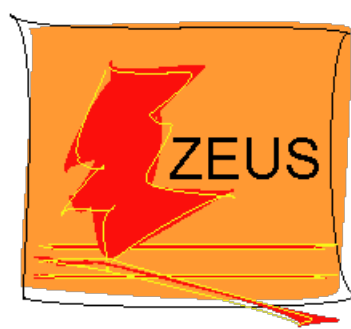




ZEUS-prel-19-001

H1prelim-19-041

# NNLO QCD fits to HERA jets and extraction of $\alpha_s$

## Status report → towards final results

A. Cooper-Sarkar, K. Wichmann

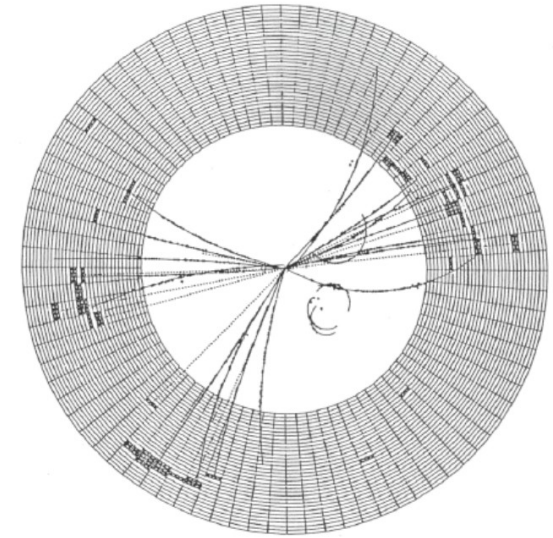
# 41 years of jet production @ DESY



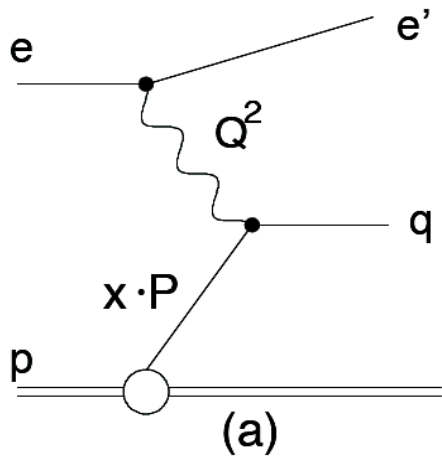
At HERA direct information on gluon distribution and  $\alpha_s$  comes from jet production

→ Possible simultaneous determination of parton densities and  $\alpha_s$

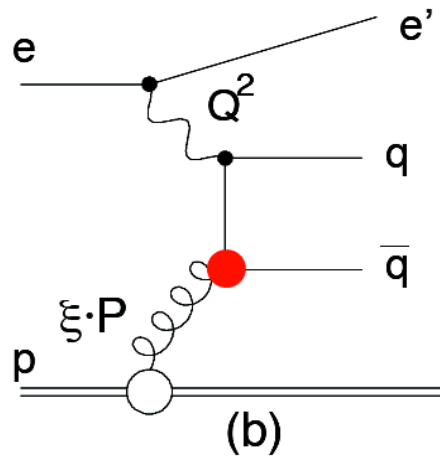
## Jets at PETRA, 1979



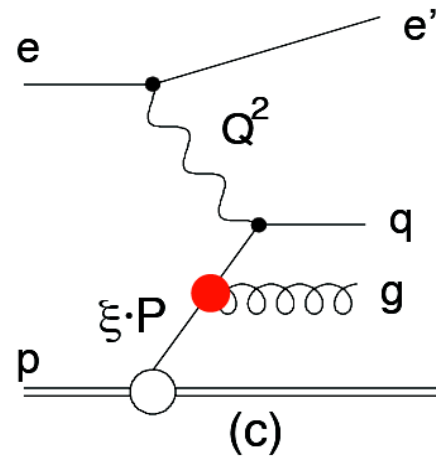
## Jets at HERA



elweak coupling

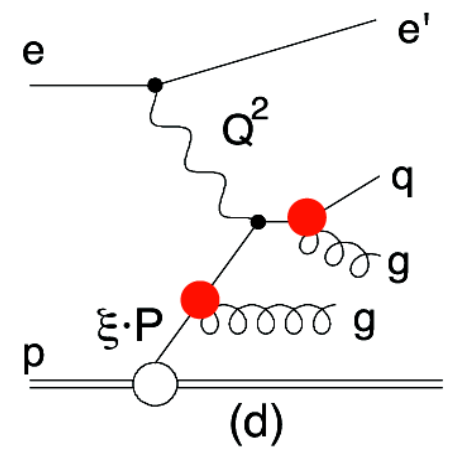


$\propto \alpha_s$



$\propto \alpha_s$

dijets



$\propto \alpha_s^2$

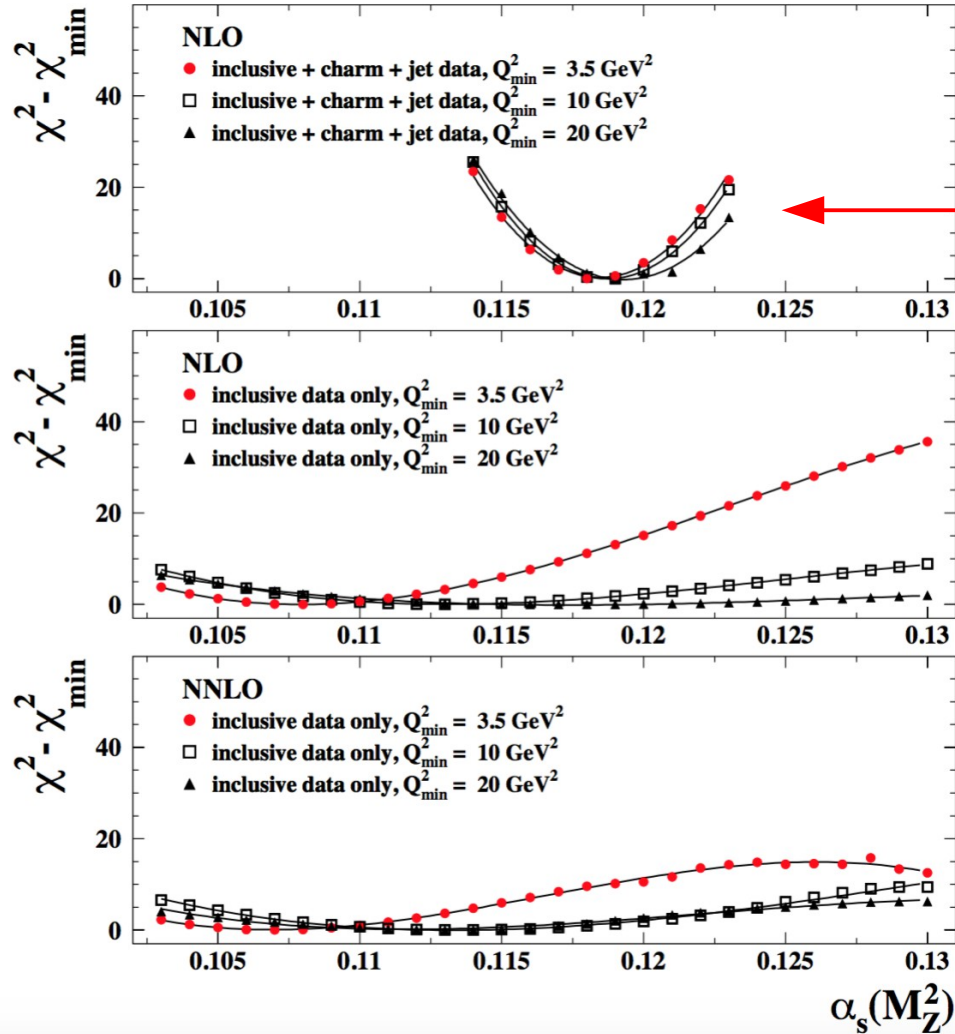
trijets



\*\*\* SUMS (GeV) \*\*\* P10T 35.768 PTRANS 29.954 PLONG -15.788 CHARGE -2  
TOTAL CLUSTER ENERGY 15.169 PHOTON ENERGY 4.693 NR OF PHOTONS 11

# Why study jets @ HERA?

## H1 and ZEUS



- HERA inclusive data carry little information on  $\alpha_s$
- Jet data sensitive to  $\alpha_s$
- So far NLO available

New NNLO calculations for  
HERA ep jet production  
available now

- Implemented in FastNLO and APPEGRID → fast cross section calculation possible

→ Possible simultaneous determination of parton densities and  $\alpha_s$  at NNLO

# Global analysis of parton distributions

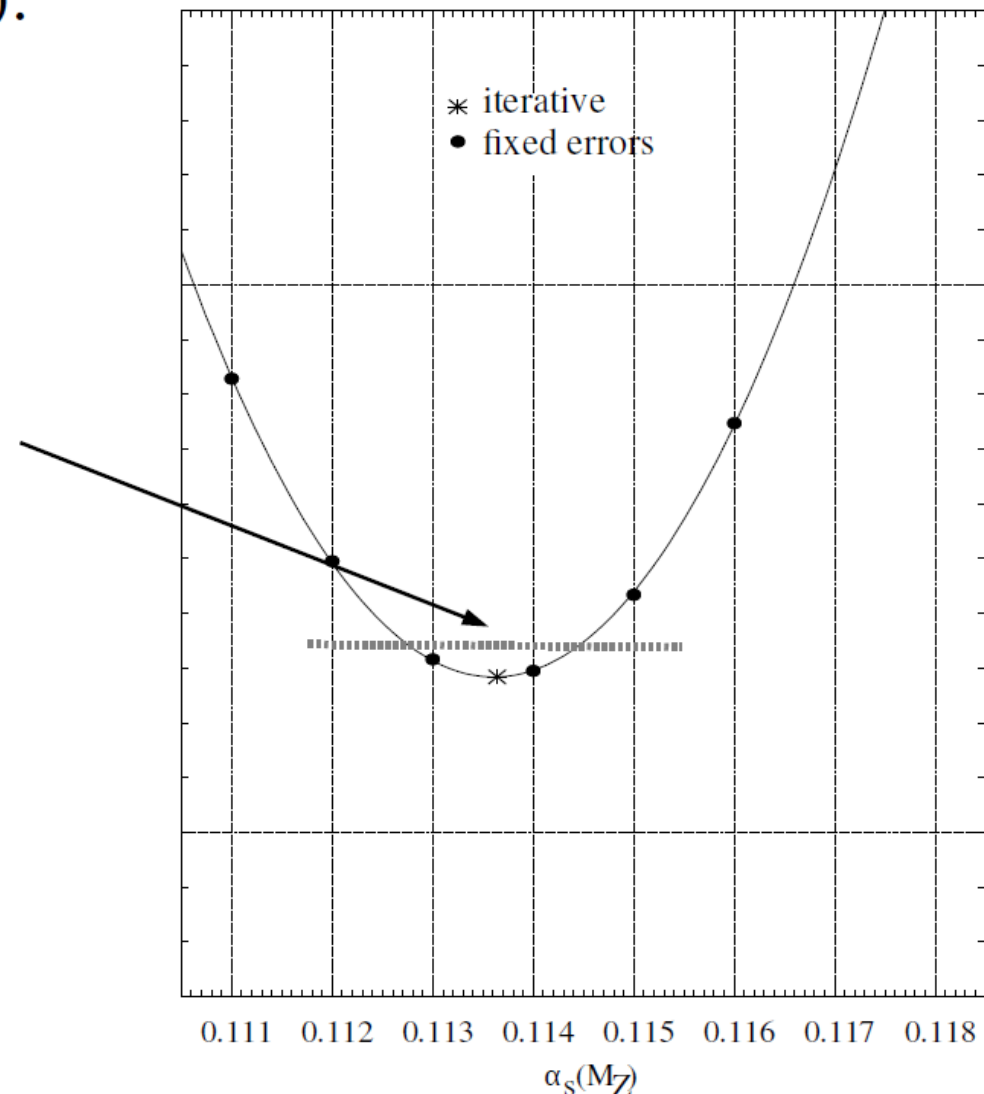
Goal: determination of the *input distributions* (for light quarks and gluons):

Method: Parametrizations  $xf(x, Q_0^2) = Nx^a(1-x)^b$  function( $x$ )  
and usual *statistical estimation* (fits):

$$\chi^2(p) = \sum_{i=1}^N \left( \frac{\text{data}(i) - \text{theory}(i, p)}{\text{error}(i)} \right)^2$$

Position of minimum gives the value  
and curvature gives the error (region  
within a certain “tolerance”  $\Delta\chi^2 = 1$ )  
(Monte Carlo methods can also be used)

Usually the chi-square definition is  
more sophisticated, experimental  
correlations are also treated, etc.





# HERAPDF2.0 parameterisation

$$xf(x) = Ax^B(1-x)^C(1+Dx+Ex^2)$$

$$xg(x) = A_g x^{B_g} (1-x)^{C_g} - A'_g x^{B'_g} (1-x)^{C'_g},$$

$$xu_v(x) = A_{uv} x^{B_{uv}} (1-x)^{C_{uv}} (1 + E_{uv} x^2),$$

$$xd_v(x) = A_{dv} x^{B_{dv}} (1-x)^{C_{dv}},$$

$$x\bar{U}(x) = A_{\bar{U}} x^{B_{\bar{U}}} (1-x)^{C_{\bar{U}}} (1 + D_{\bar{U}} x),$$

$$x\bar{D}(x) = A_{\bar{D}} x^{B_{\bar{D}}} (1-x)^{C_{\bar{D}}}.$$

- Additional constraints

- $A_{uv}, A_{dv}, A_g$ : constrained by the quark-number sum rules and momentum sum rule

- $B_{\bar{U}} = B_{\bar{D}}$

- $x\bar{s} = f_s x\bar{D}$  at starting scale,  $f_s = 0.4$



# PDF uncertainties

## HERAPDF experimental, model and parameterisation uncertainties

### Experimental uncertainties:

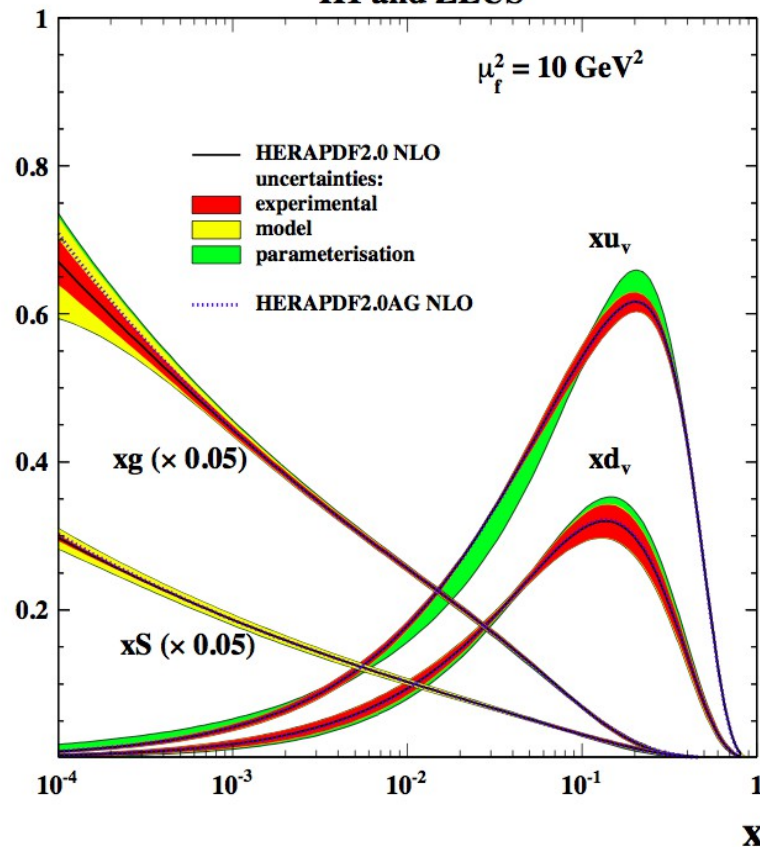
- Hessian method
- Conventional  $\Delta\chi^2 = 1 \Rightarrow 68\% \text{ CL}$

| Variation                                | Standard Value | Lower Limit | Upper Limit |
|------------------------------------------|----------------|-------------|-------------|
| $Q_{\min}^2 [\text{GeV}^2]$              | 3.5            | 2.5         | 5.0         |
| $Q_{\min}^2 [\text{GeV}^2] \text{ HiQ2}$ | 10.0           | 7.5         | 12.5        |
| $M_c(\text{NLO}) [\text{GeV}]$           | 1.47           | 1.41        | 1.53        |
| $M_c(\text{NNLO}) [\text{GeV}]$          | 1.43           | 1.37        | 1.49        |
| $M_b [\text{GeV}]$                       | 4.5            | 4.25        | 4.75        |
| $f_s$                                    | 0.4            | 0.3         | 0.5         |
| $\mu_{f_0} [\text{GeV}]$                 | 1.9            | 1.6         | 2.2         |

Adding D and E parameters to each PDF

H1 and ZEUS

$\mu_f^2 = 10 \text{ GeV}^2$



- Model uncertainties
  - variations added in quadrature

- Parameterisation uncertainties
  - largest deviation

- When jets included - also hadronisation uncertainty
  - offsetting corrections given for each jet data set

## The plan for work to complete the analysis is outlined in the talk from November 29<sup>th</sup>: IN SUMMARY

- Finish the NNLO analysis much in the way that the DIS19 preliminary was done but with new mc,mb settings accounting for the new c,b combined data
- Using the same data sets, same cuts, same scale choice, same parametrisation --- (all checks done --ie settings and parametrisation choice iterated) – **done**

### FOR:

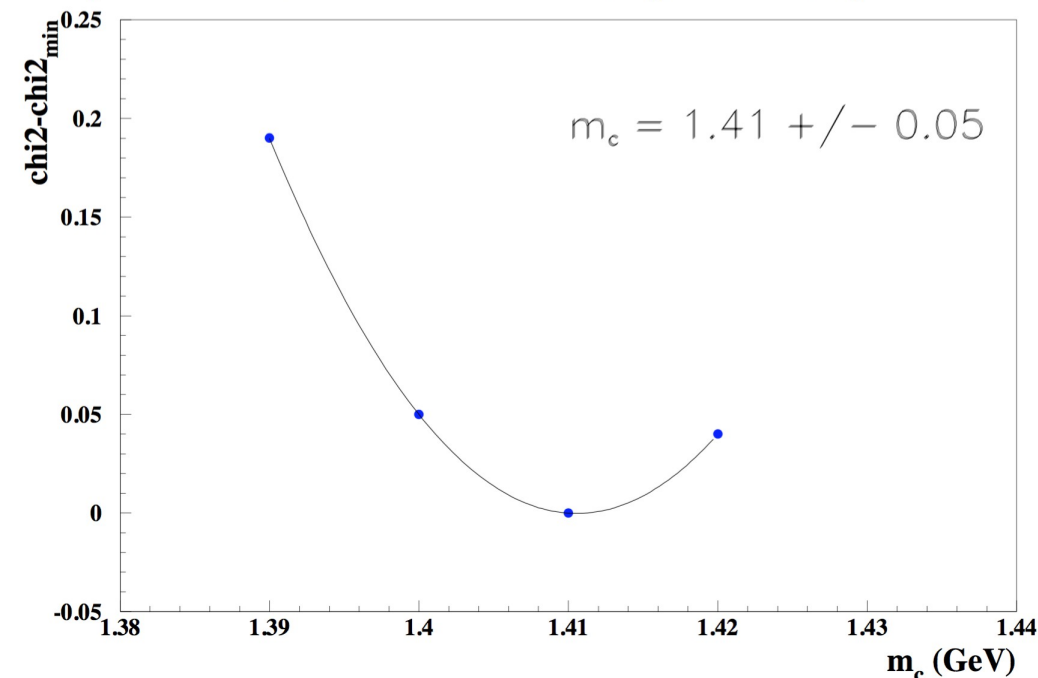
- $\alpha_s(M_Z) = 0.115$
- $\alpha_s(M_Z) = 0.118$
- Free alphas
- All model/ parametrisation uncertainties treated as agreed: vary  $Q^2_0$  down ONLY and symmetrise; vary  $M_c$  up ONLY and symmetrise **done**
- Hadronisation by offset consistently ie set hadronisation uncertainty of H1 2016 low  $Q^2$  jets=zero for central job (it was the 13<sup>th</sup> systematic uncertainty) **in progress**
- Scale uncertainty ½ correlated , ½ uncorrelated as for HERAPDF2.0NLOJets **in progress**
- Do not revisit NLO other than to say that the current scale choice would have resulted in  $\alpha_s(M_Z) = 0.121$  rather than 0.118
- Maybe also say not revisiting it because the most significant new data set—H1 low  $Q^2$  jets 2016 is not well fitted at NLO



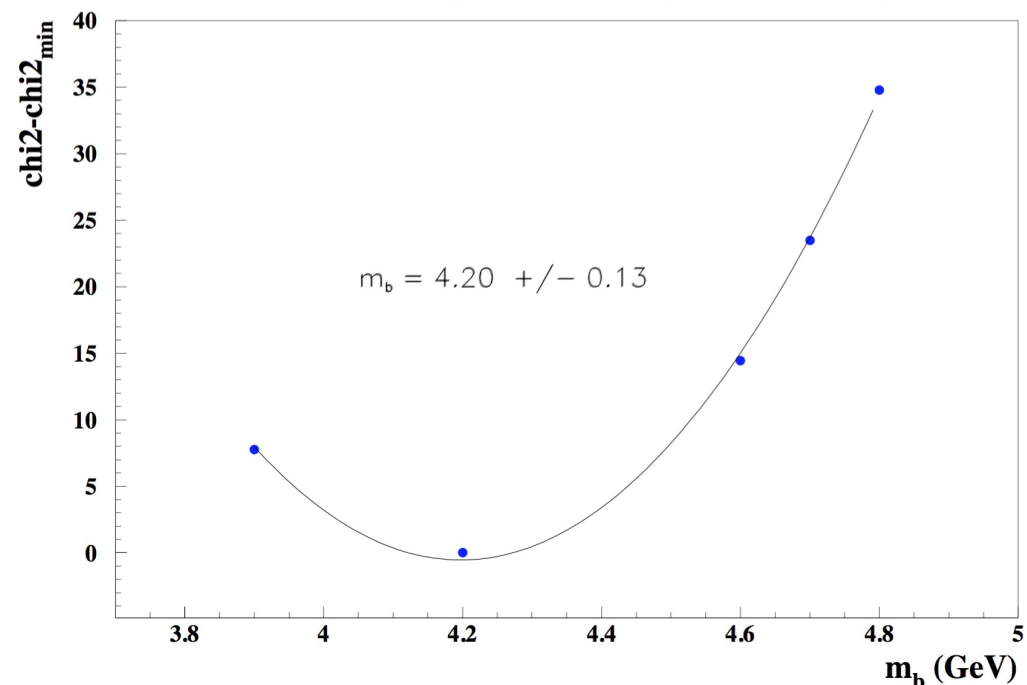
# Updates for final results

- New charm and beauty masses
  - from final H1/ZEUS beauty results [Eur. Phys. J C 78 \(2018\) 473](#)
  - Charm mass  $m_c = 1.41 \pm 0.05$
  - Beauty mass  $m_b = 4.20 \pm 0.13$

$m_c$  scan, NNLO, incl+charm  $> 3.5 \text{ GeV}^2$ ,  $m_b = 4.2 \text{ GeV}$ ,  $Q_0^2 = 1.9 \text{ GeV}^2$



incl+charm  $> 3.5 \text{ GeV}^2$ ,  $m_c = 1.41 \text{ GeV}$ ,  $Q_0^2 = 1.9 \text{ GeV}^2$ ,  $\alpha_s = 0.115$



# Updates for final results

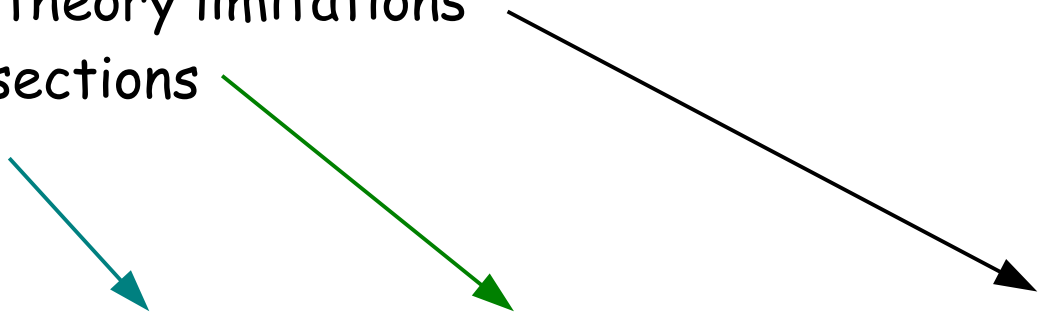


- Other settings stay the same
  - parameter scan done using new settings → as before: 14 params
  - $\alpha_s$  repeated with new parameters → very small differences compared to preliminary results (both studies already presented in H1/ZEUS meetings)
- New points in jet data (5 points) → see next slide
  - Studies shown by Mandy on jan. 22nd



# HERA jet data used in PDF fit

- Inclusive jets and **dijets**
- Some data points excluded due theory limitations
- Absolute and **normalised** cross sections
- **Low- $Q^2$**  and high- $Q^2$  production
- HERAI and HERAII



| Data Set                                                           | taken<br>from to          | $Q^2$ [GeV <sup>2</sup> ] range<br>from to | $\mathcal{L}$<br>pb <sup>-1</sup> | $e^+/e^-$     | norma-<br>lised | all<br>points | used<br>points |
|--------------------------------------------------------------------|---------------------------|--------------------------------------------|-----------------------------------|---------------|-----------------|---------------|----------------|
| H1 HERAI <b>normalised</b> jets                                    | 1999 – 2000               | 150 15000                                  | 65.4                              | $e^+ p$       | yes             | 24            | 24             |
| H1 HERAI jets at <b>low <math>Q^2</math></b>                       | 1999 – 2000               | 5 100                                      | 43.5                              | $e^+ p$       | no              | 28            | 16             |
| H1 <b>normalised</b> inclusive jets at high $Q^2$                  | 2003 – 2007               | 150 15000                                  | 351                               | $e^+ p/e^- p$ | yes             | 30            | 24             |
| H1 <b>normalised</b> <b>dijets</b> at high $Q^2$                   | 2003 – 2007               | 150 15000                                  | 351                               | $e^+ p/e^- p$ | yes             | 24            | 24             |
| H1 <b>normalised</b> inclusive jets at <b>low <math>Q^2</math></b> | 2005 – 2007               | 5.5 80                                     | 290                               | $e^+ p/e^- p$ | yes             | 48            | 32             |
| H1 <b>normalised</b> <b>dijets</b> at <b>low <math>Q^2</math></b>  | 2005 – 2007               | 5.5 80                                     | 290                               | $e^+ p/e^- p$ | yes             | 48            | 32             |
| ZEUS inclusive jets                                                | 1996 – 1997               | 125 10000                                  | 38.6                              | $e^+ p$       | no              | 30            | 30             |
| ZEUS <b>dijets</b> 1998 – 2000 & 2004 – 2007                       | 1998 – 2000 & 2004 – 2007 | 125 20000                                  | 374                               | $e^+ p/e^- p$ | no              | 22            | 16             |

- 6 data points added
  - H1 normalised inclusive jets at high  $Q^2$
  - for each  $Q^2$  bin low- $p_+$  point added



What we have as preliminary and how  
it compares to new results  
→ not everything finished yet

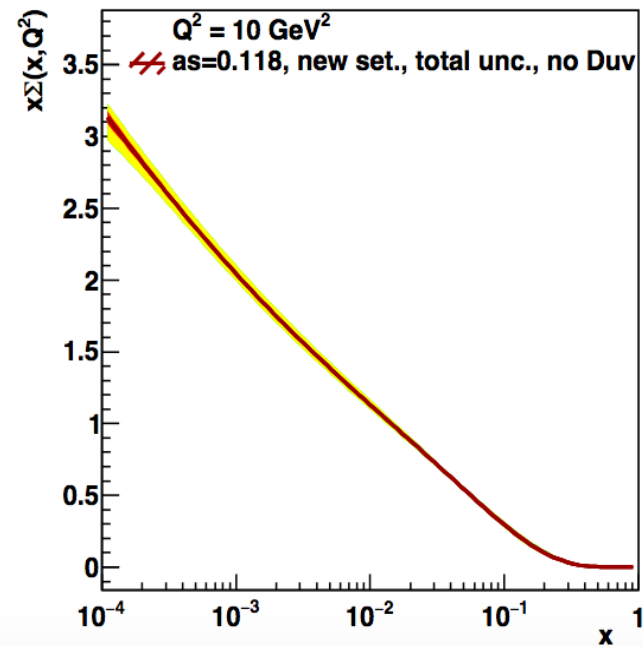
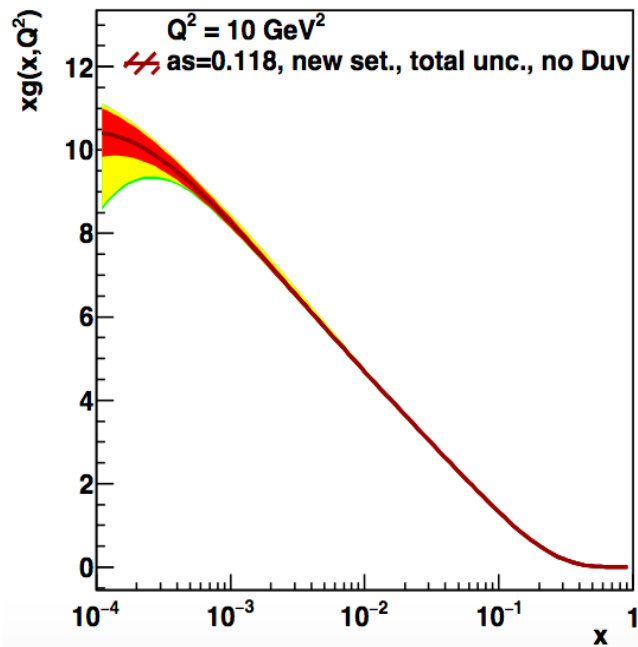
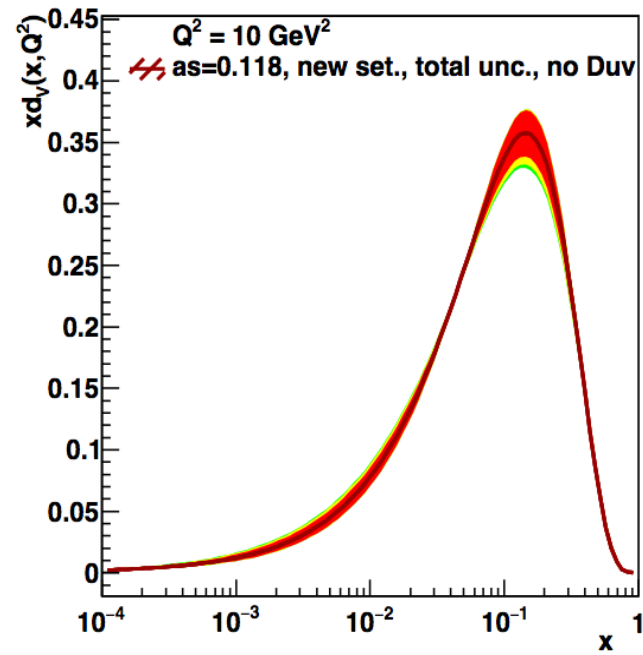
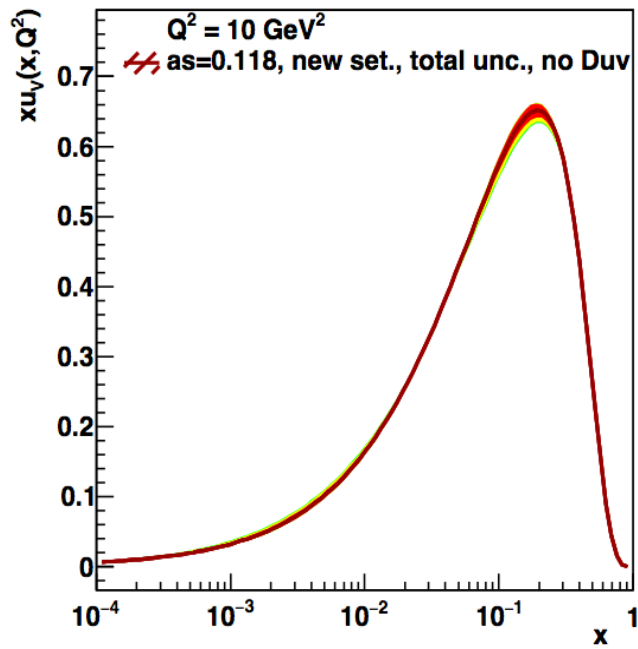
PDF fits for  
 $\alpha_s = 0.118$



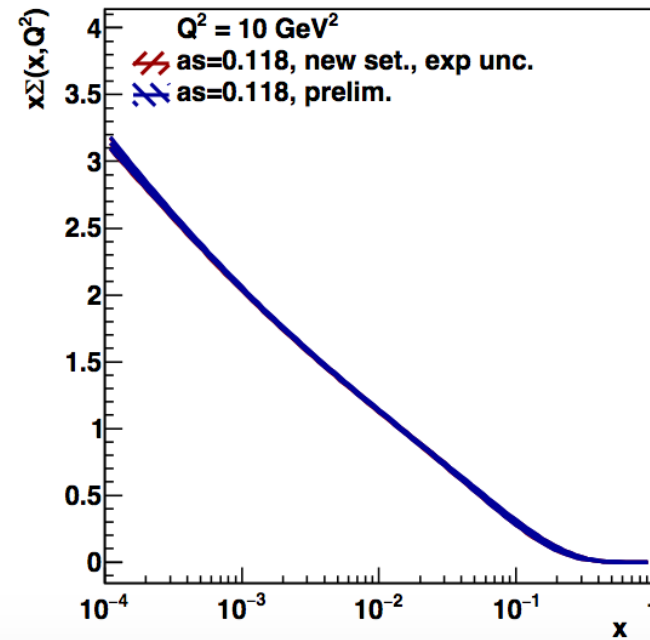
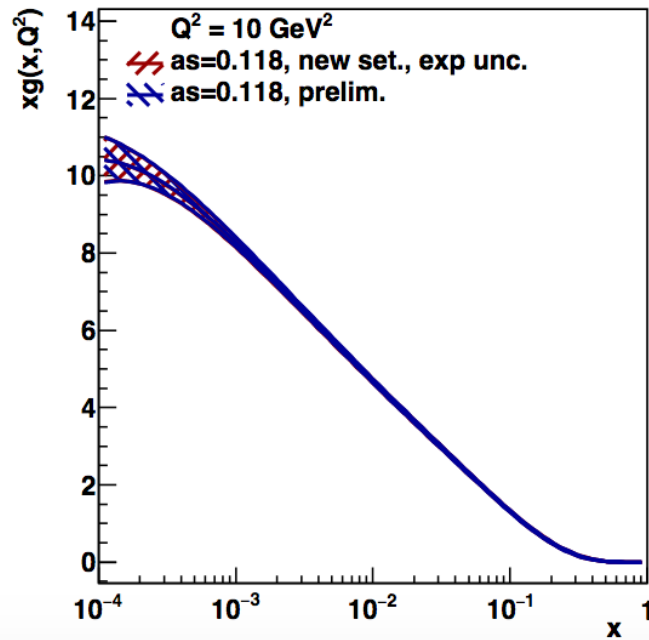
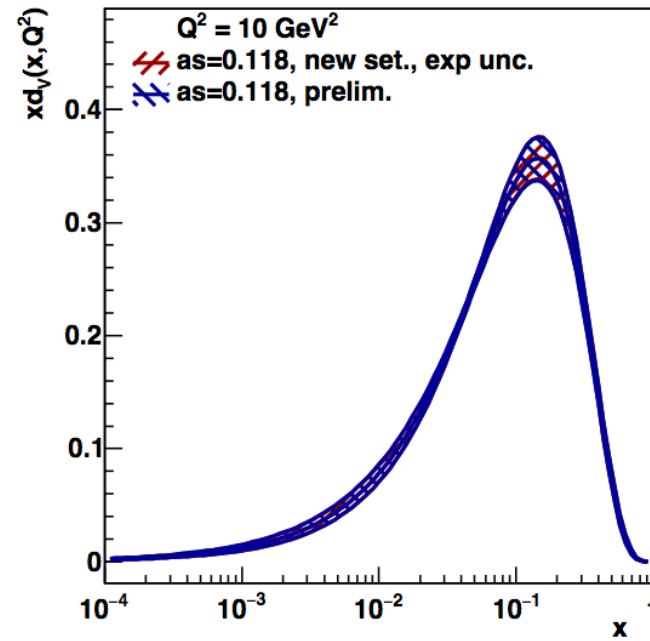
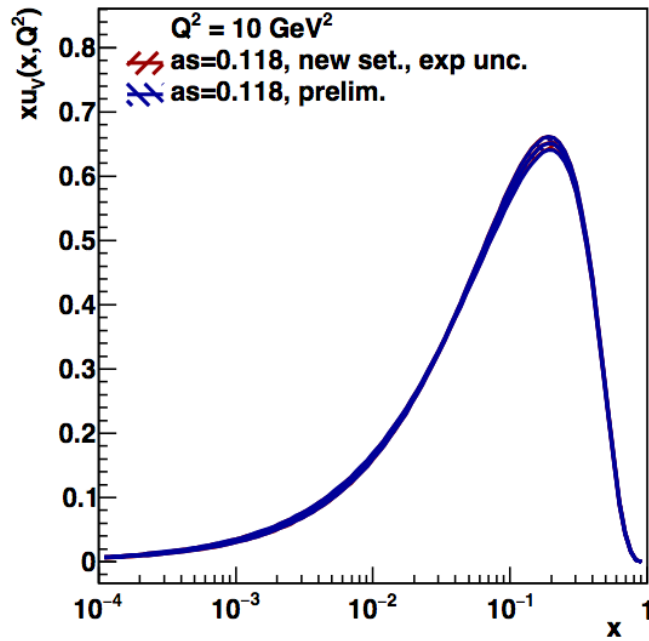
# Caution: not done yet

- For parameterisation uncertainty
  - Adding Duv paramter  $\rightarrow$  15 parameters
    - $\rightarrow$  very difficult fits, problems with convergence, work in progress
    - $\rightarrow$  affects mostly valence quarks distributions

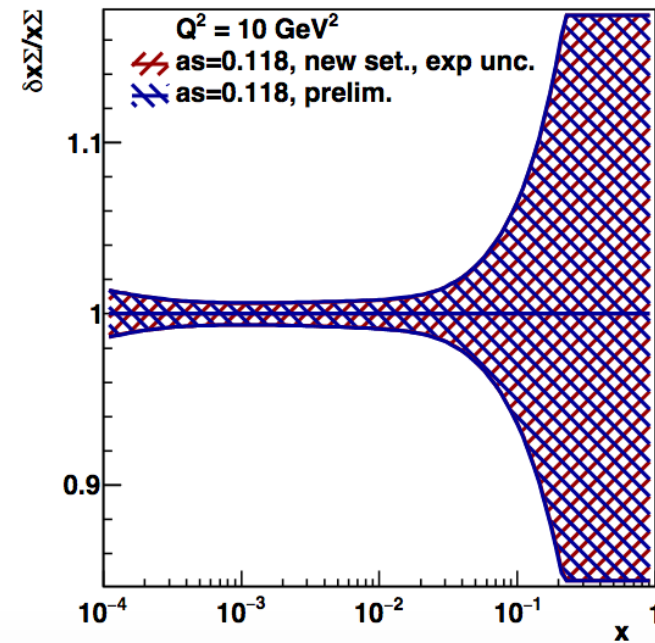
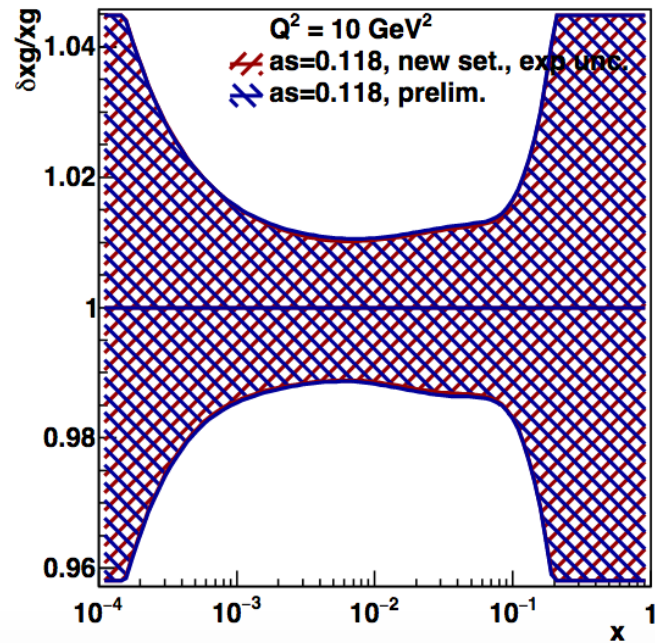
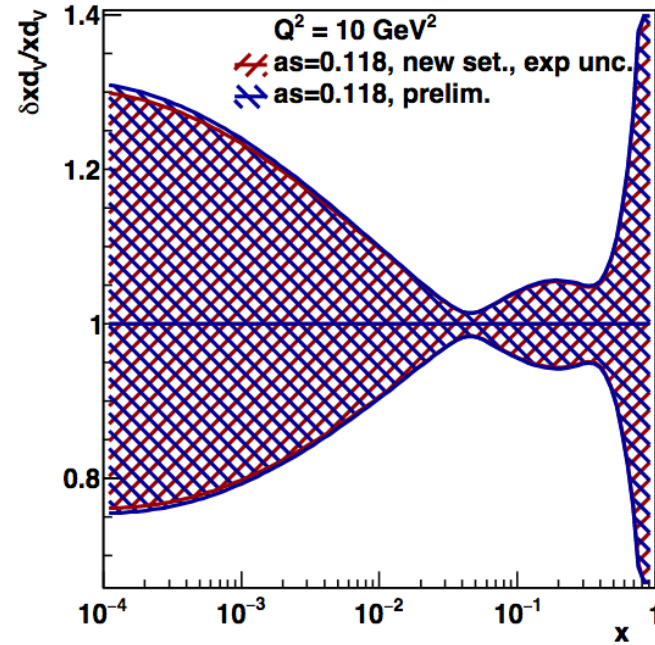
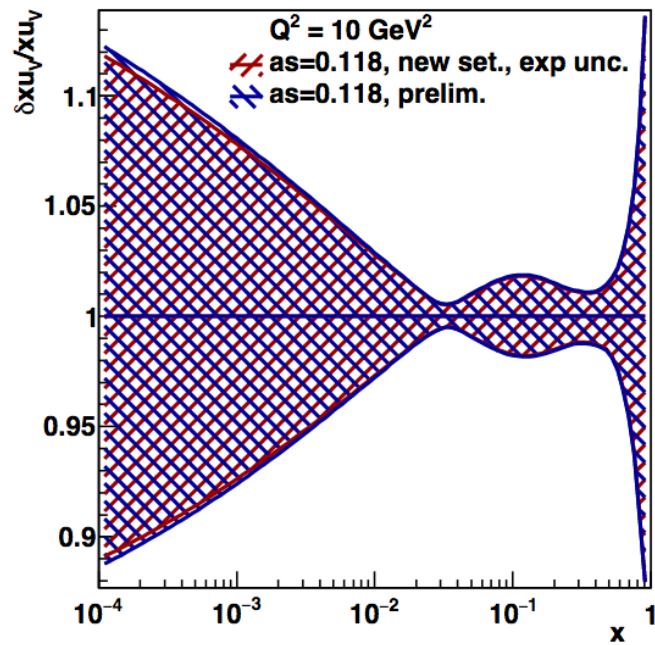
$$\alpha_s = 0.118$$



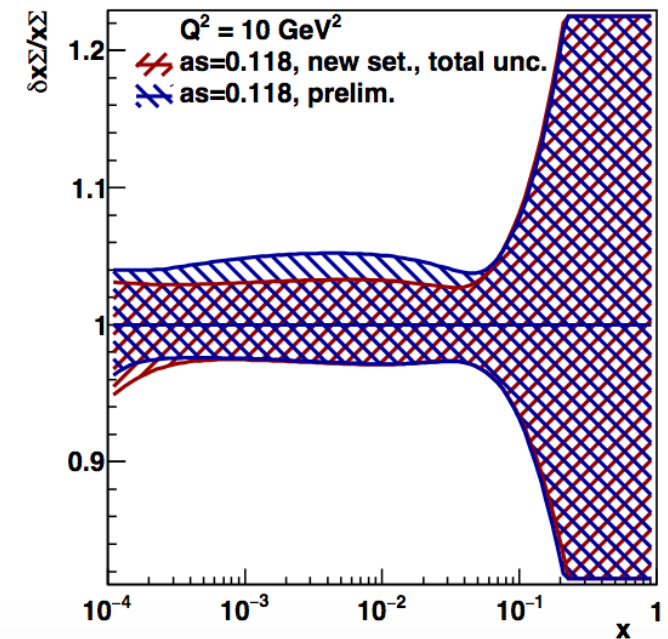
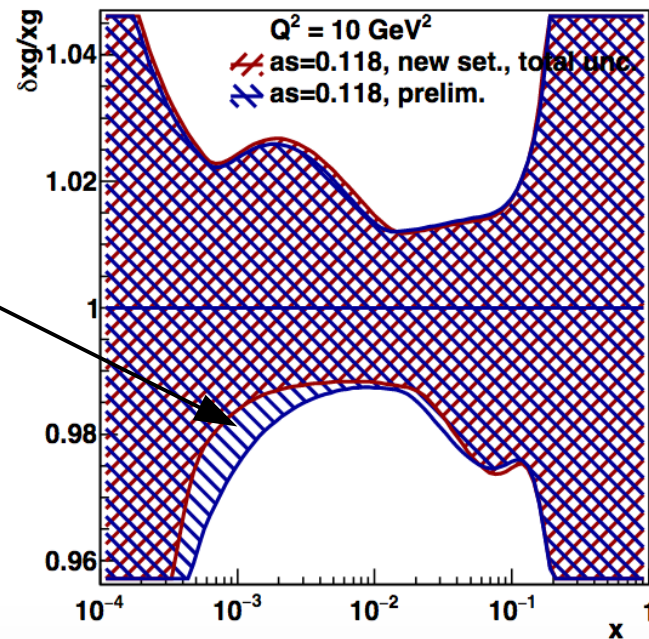
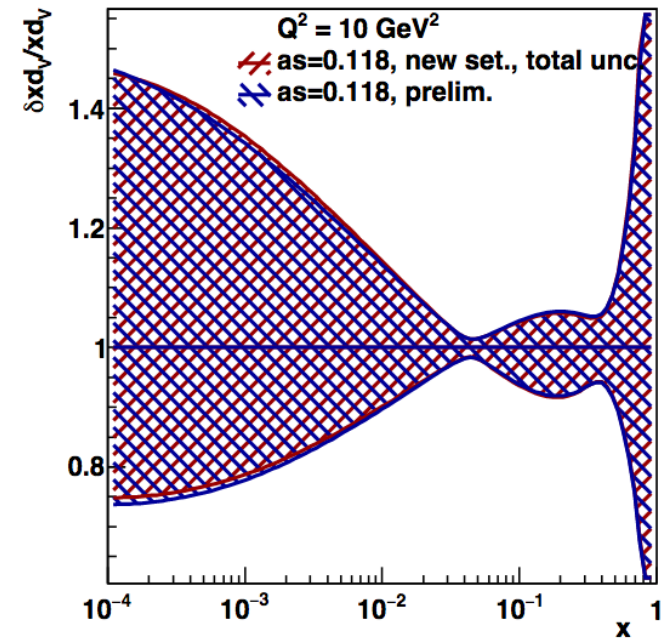
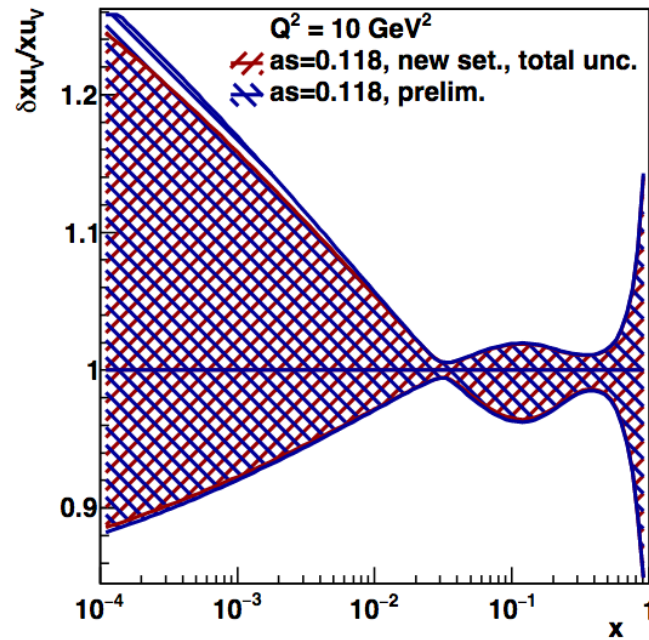
# Comparison with preliminary fit



# Experimental uncertainties



# Total uncertainties



Double counting in preliminary results from varying  $m_c$  and  $Q_0^2$  variations simultaneously



What we have as preliminary and how  
it compares to new results  
→ not everything finished yet

we revisit  $\alpha_s$  now

# Preliminary $\alpha_s$

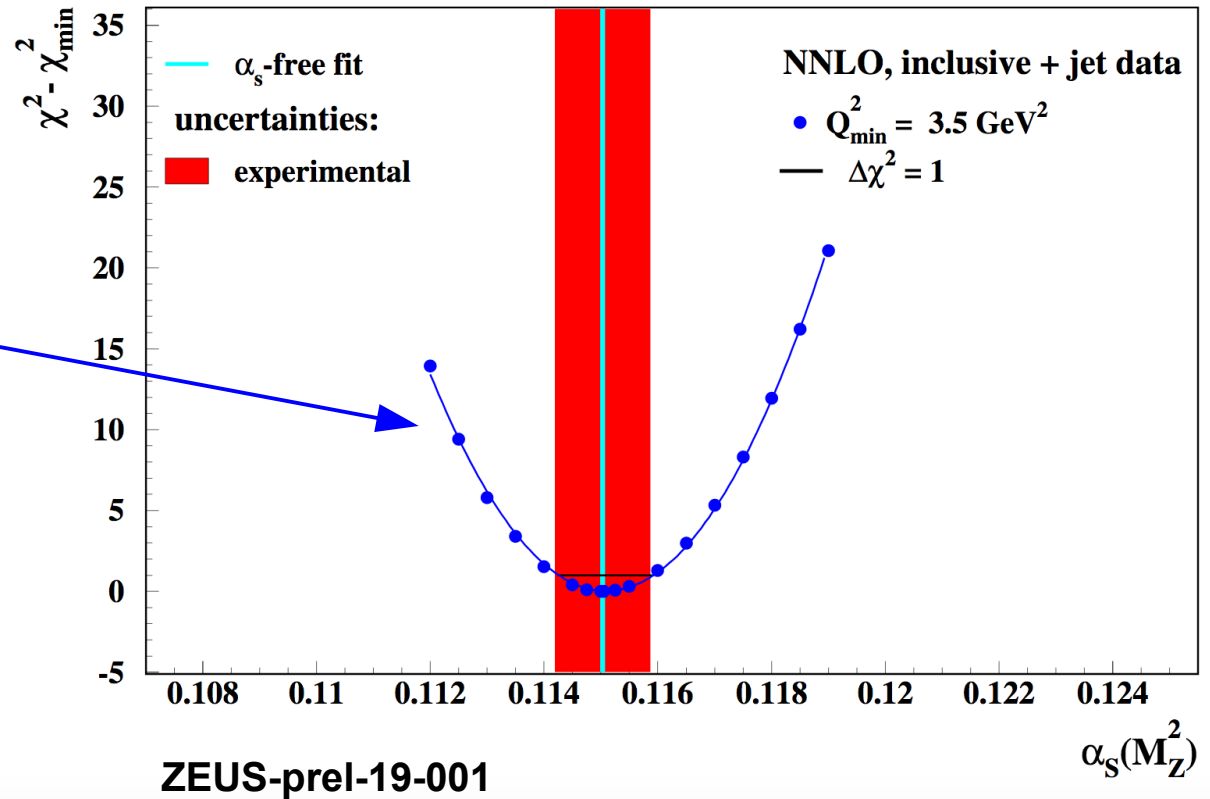


## H1 and ZEUS preliminary

- Two ways of estimating  $\alpha_s$   
@NNLO using HERA jet data

→  $\alpha_s$ -scan  
→ simultaneous fit of PDFs  
and  $\alpha_s$

- Both methods give the same  
result



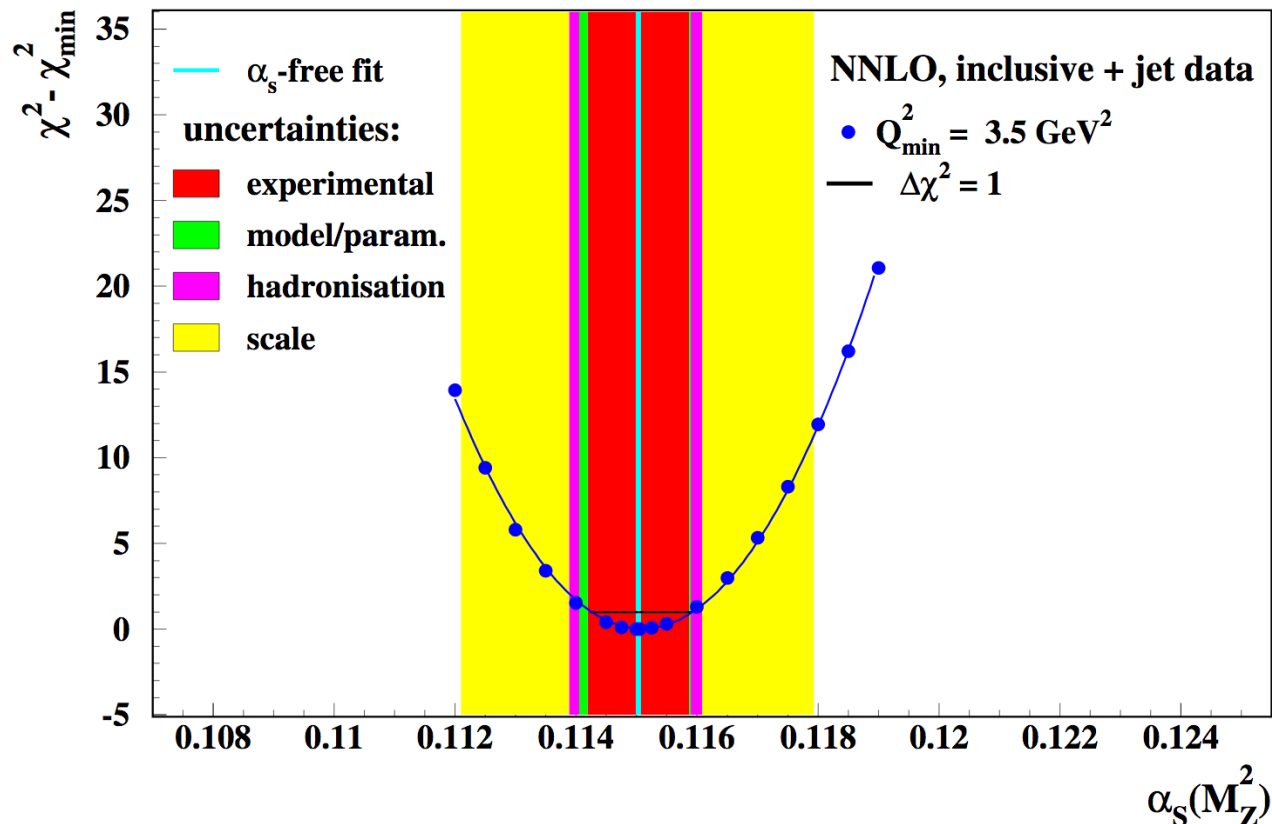
$$\alpha_s(M_Z^2) = 0.1150 \pm 0.0008(\text{exp})$$



# Preliminary $\alpha_s$ with full uncertainties

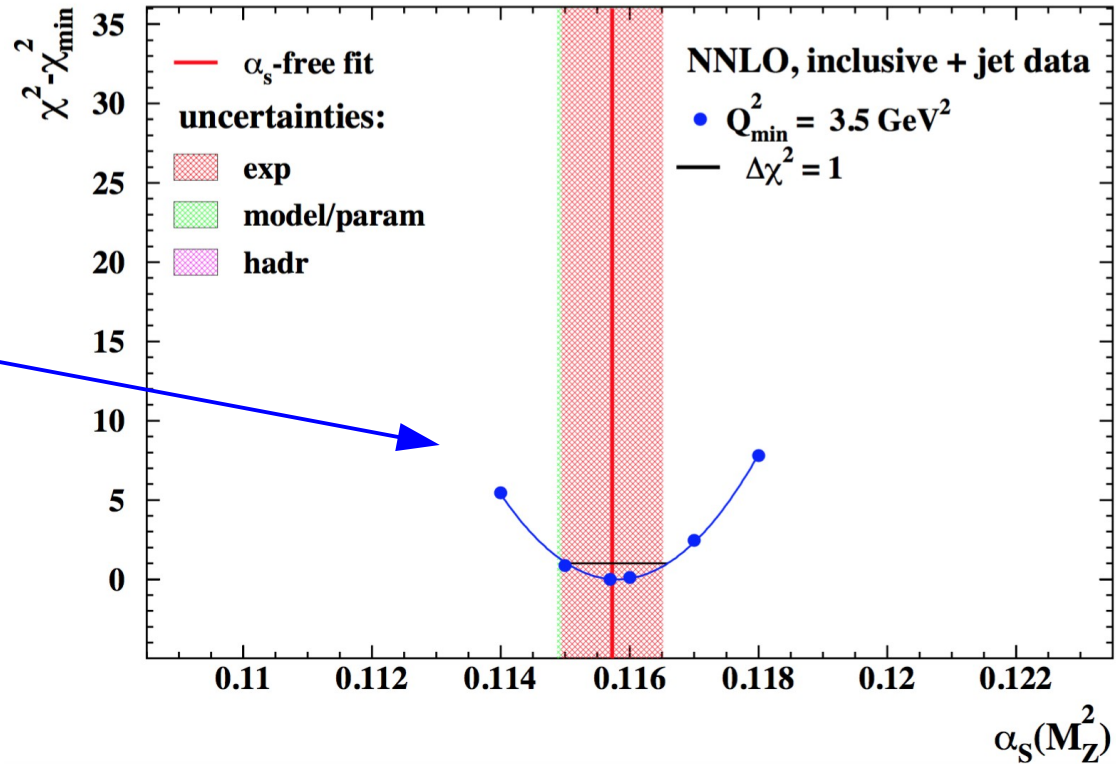
- Experimental, model, parametrisation and hadronisation uncertainties
- In fits with free  $\alpha_s(M_Z)$  **scale uncertainty** important
  - factorisation and renormalisation scales varied both separately and simultaneously by a factor of two and taking maximal positive and negative deviations (assumed to be 50% correlated and 50% uncorrelated)

## H1 and ZEUS preliminary



# New $\alpha_s$

## H1 and ZEUS - towards final results



- Two ways of estimating  $\alpha_s$  @NNLO using HERA jet data

→  $\alpha_s$ -scan  
→ simultaneous fit of PDFs and  $\alpha_s$

- Both methods give the same result

- Fit:

$$\alpha_s(M_Z^2) = 0.1157 \pm 0.0008(\text{exp})$$

- $\alpha_s$ -scan:  $\alpha_s = 0.1158 \pm 0.0008$



# New $\alpha_s$

$$\alpha_s(M_Z^2) = 0.1157 \pm 0.0008(\text{exp})$$

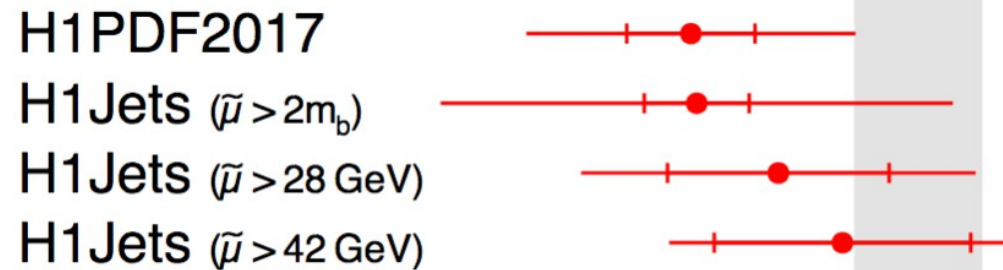
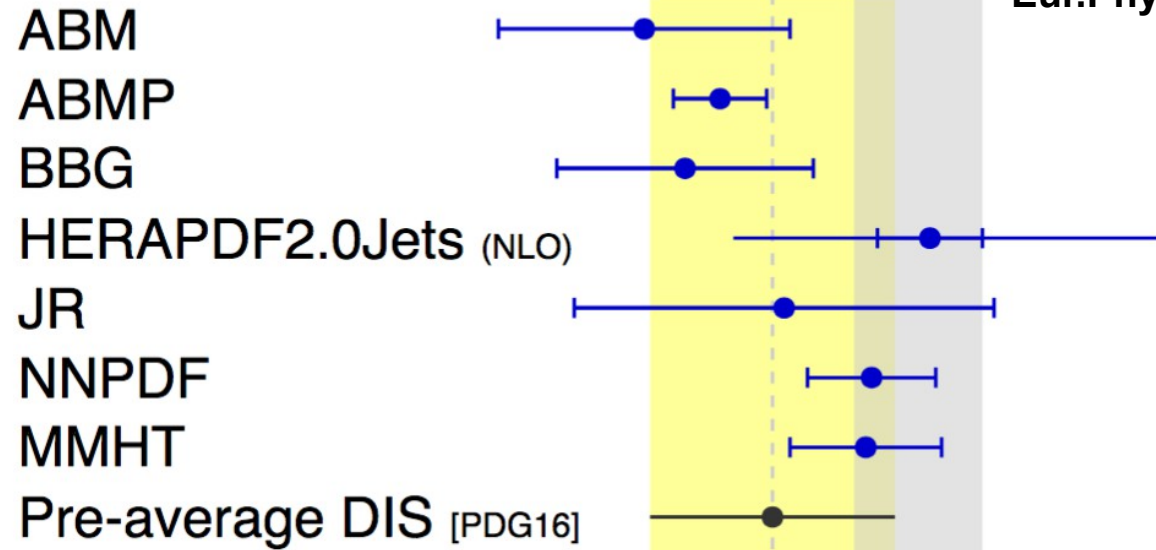
- Compared to  
0.1150 +/- 0.0008 → preliminary  
0.1151 +/- 0.0008 → new settings, no low- $p_T$  jet points
- Model/parameterisation uncertainty  
+0.0001 -0.0003
- Compared to  
+0.0002 -0.0005 → preliminary
- Difference for positive uncertainty comes from double counting mentioned before
- Difference for negative uncertainty comes from large difference for added EUbar parameter (more stable fit now?)
- In any case → scale uncertainty dominates

# Comparison to other NNLO results

$\alpha_s$  determinations in NNLO

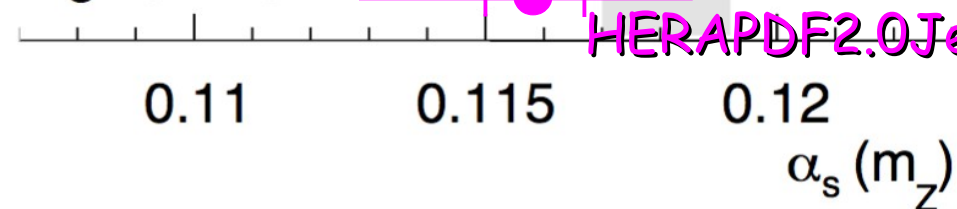
H1 and NNLOJET

Eur.Phys.J.C77 (2017), 791



HERAPDF2.0Jets NNLO (prel.)

World average [PDG16]



HERAPDF2.0Jets NNLO (prel.)

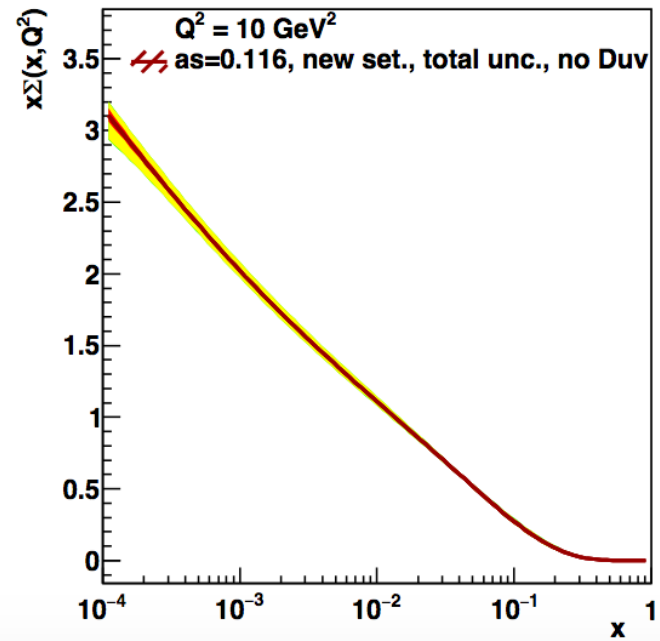
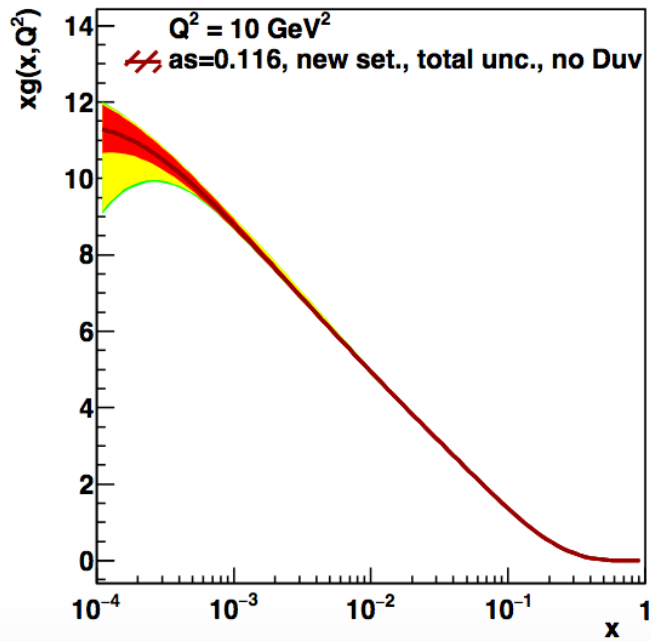
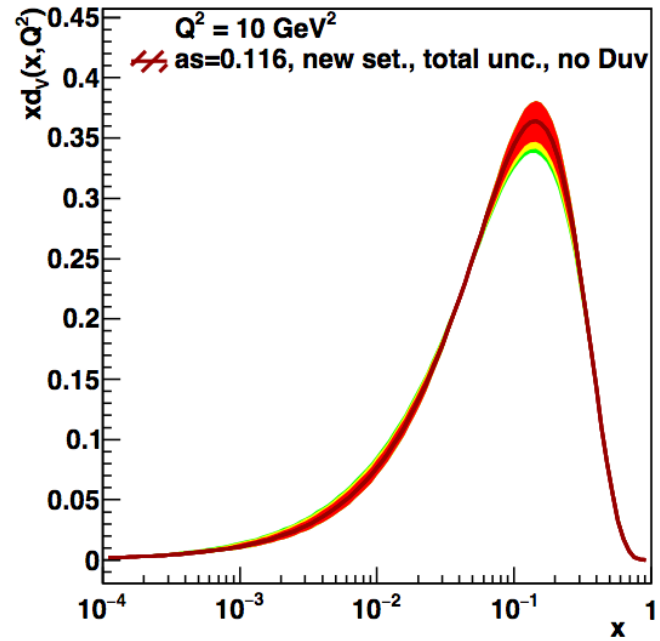
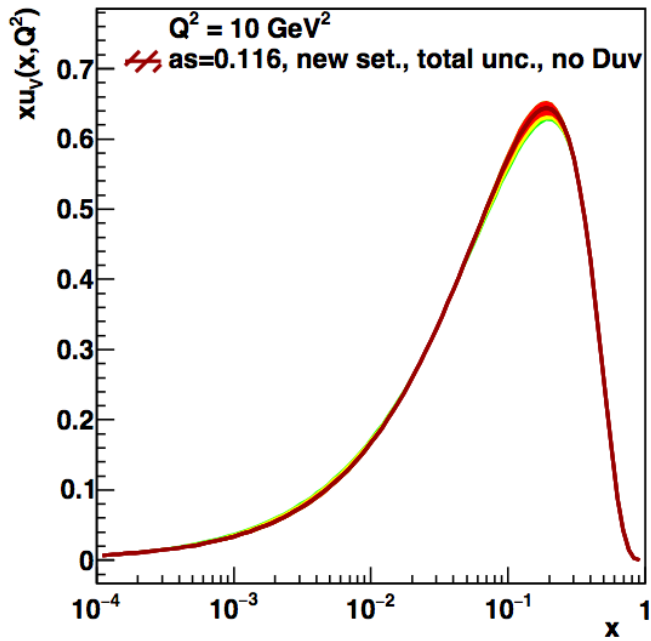


What we have as preliminary and how  
it compares to new results  
→ not everything finished yet

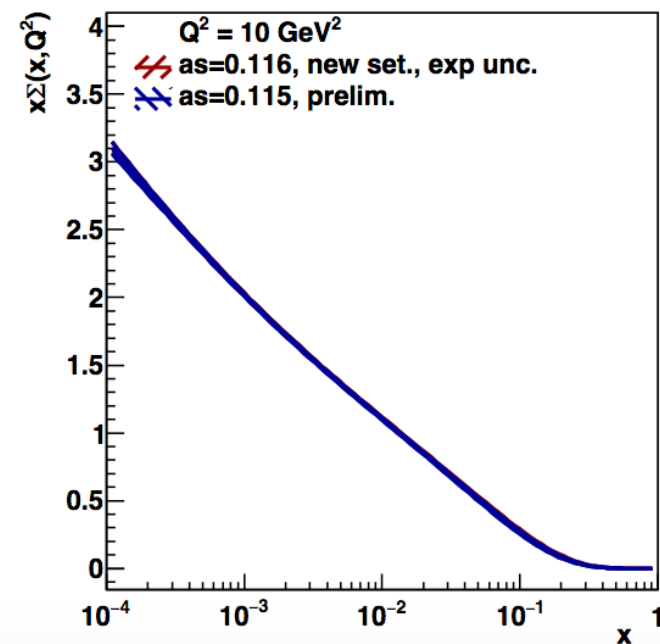
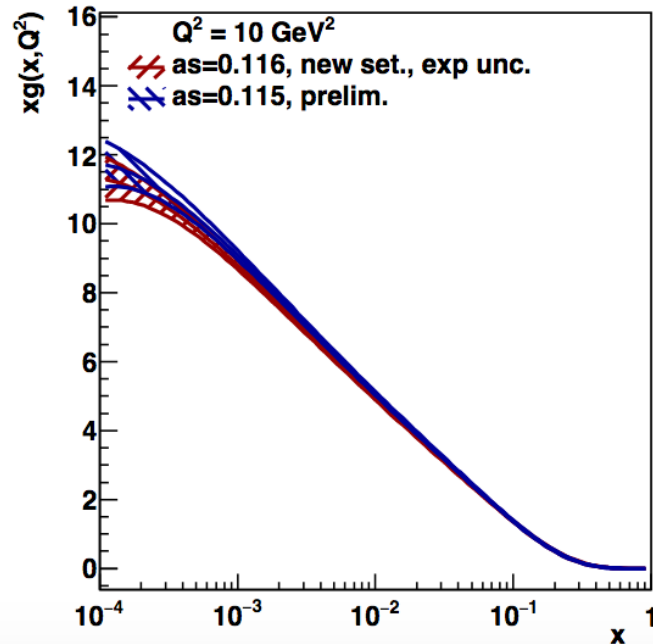
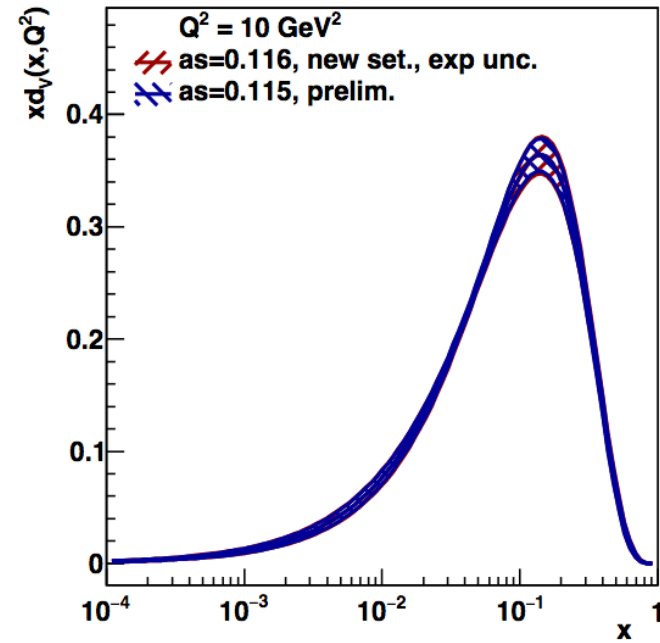
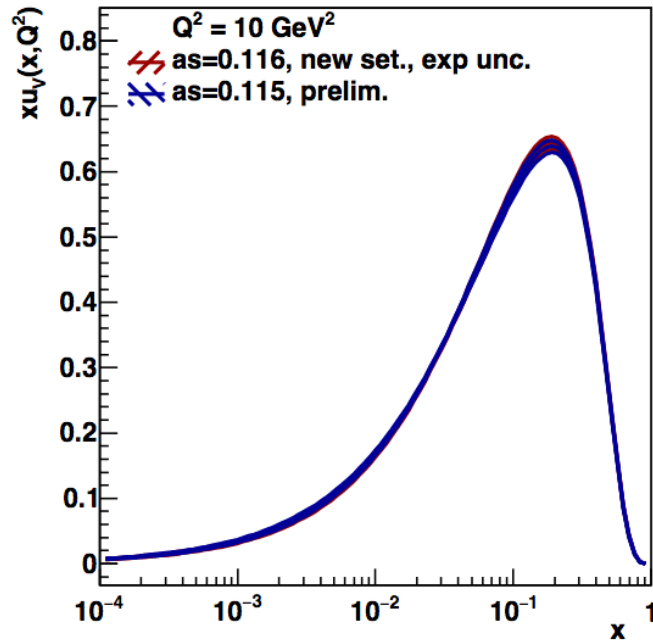
PDF fits for  
nominal  $\alpha_s = 0.116$   
(used to be 0.115 for preliminary)

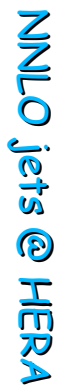


$$\alpha_s = 0.116$$

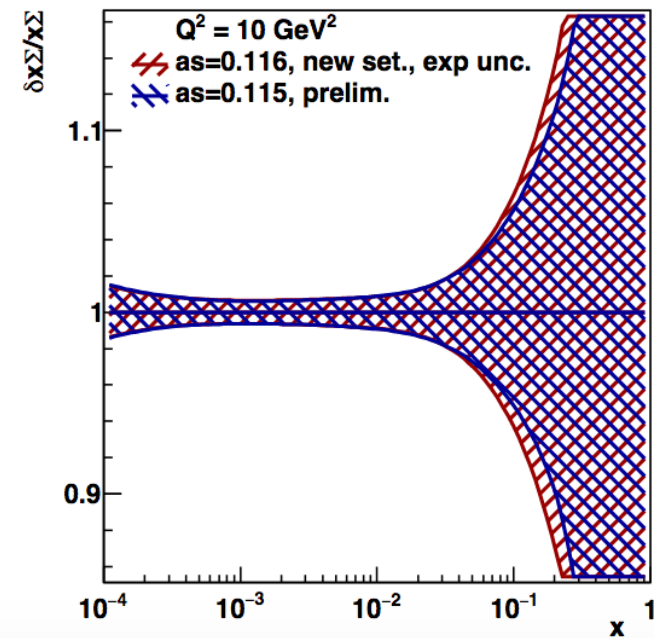
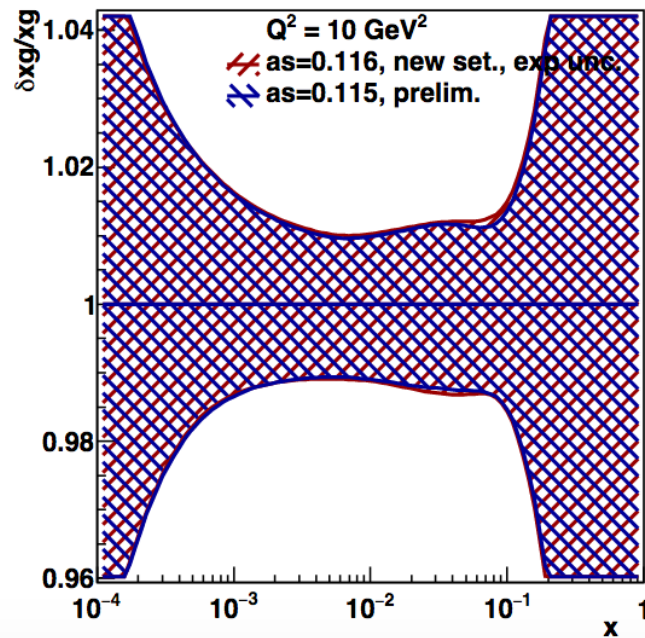
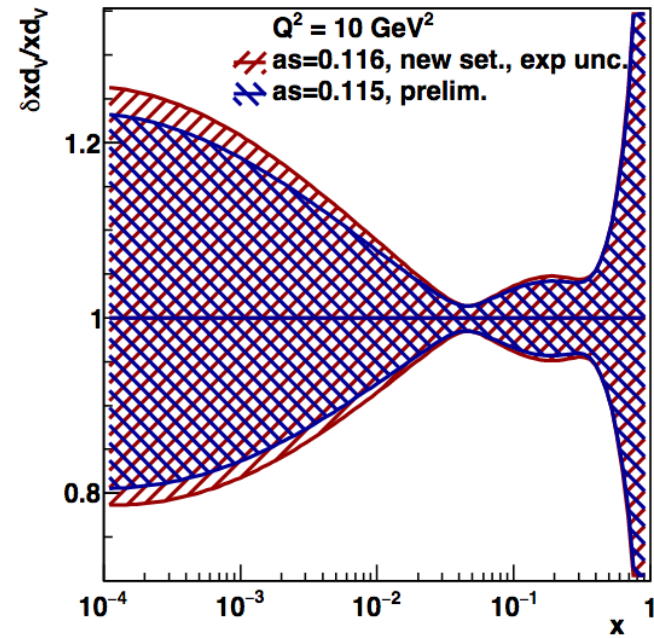
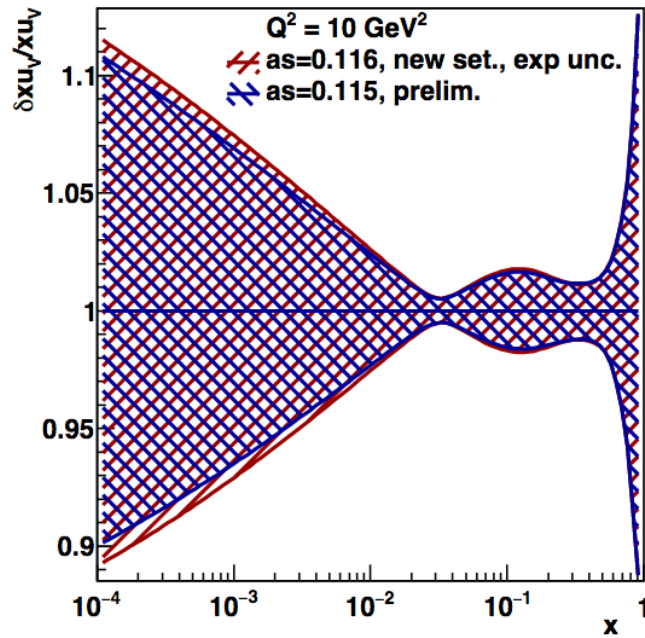


# Experimental uncertainties

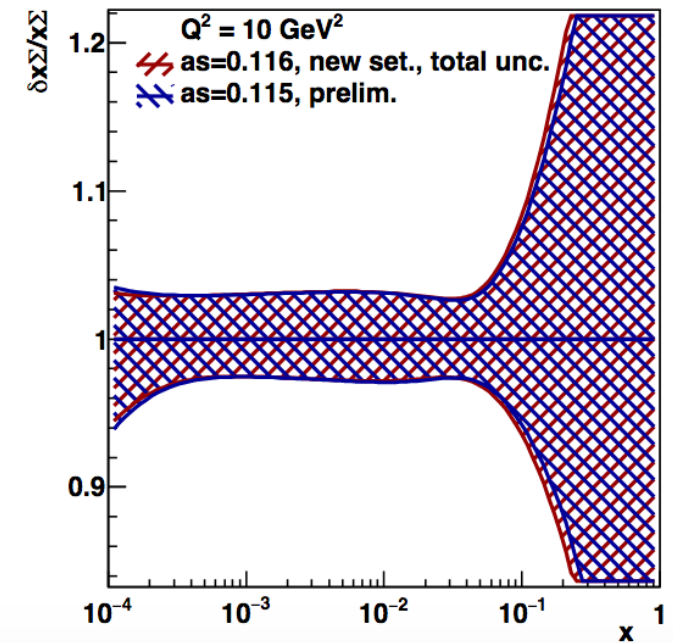
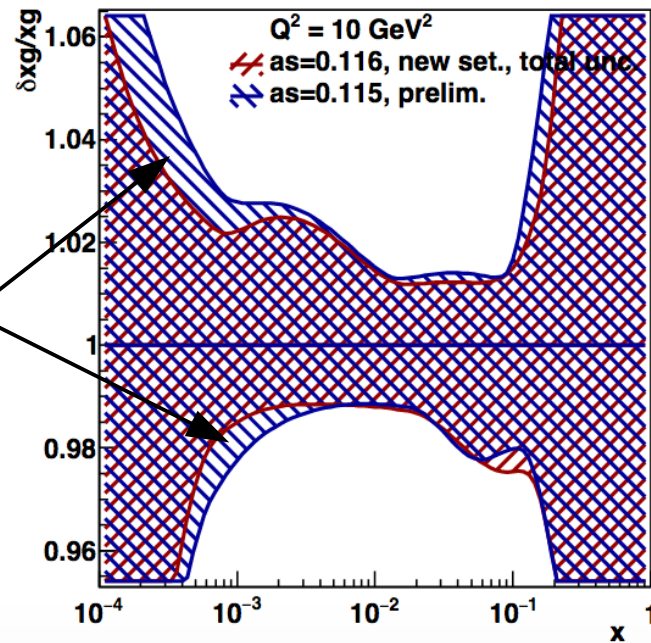
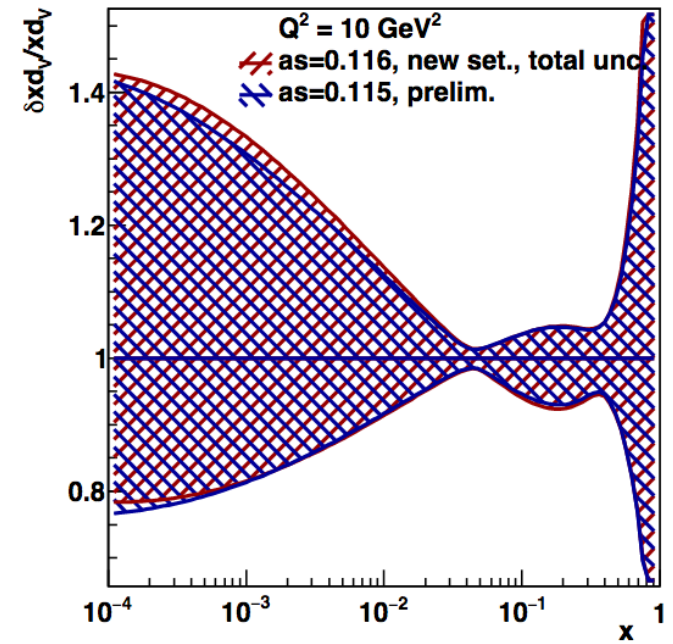
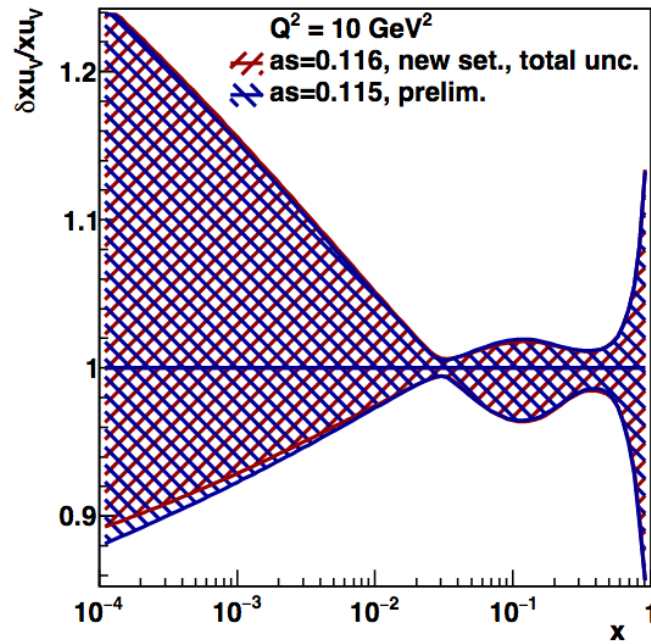




## Experimental uncertainties



# Total uncertainties



Double counting in preliminary results from varying  $m_c$  and  $Q_0^2$  variations simultaneously

- Missing incl variation



Scans with harder  $Q^2$  cuts

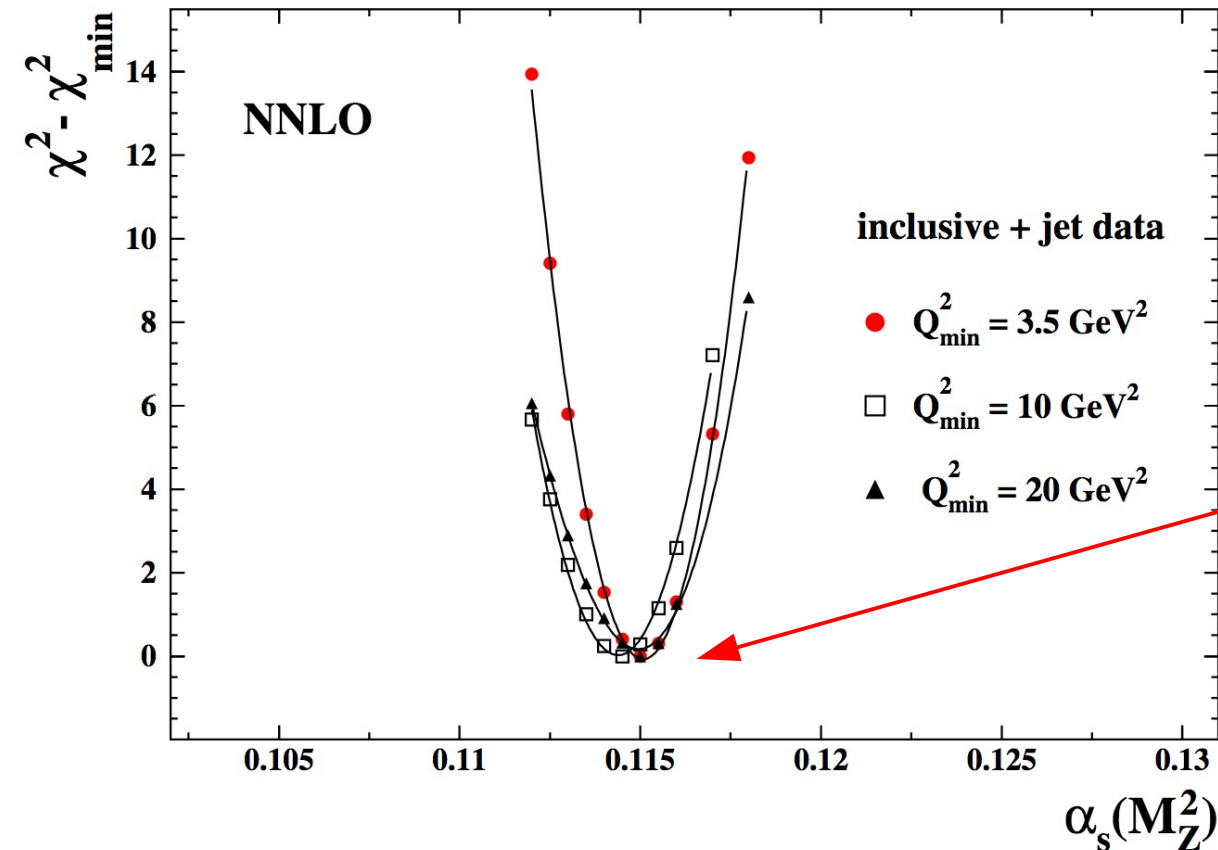


# Preliminary: scans with harder $Q^2$ cuts

- HERA data at low  $x$  and  $Q^2$  may be subject to need for  $\ln(1/x)$  resummation or higher twist effects

→  $\chi^2$  scans performed with harder  $Q^2$  cuts

H1 and ZEUS preliminary



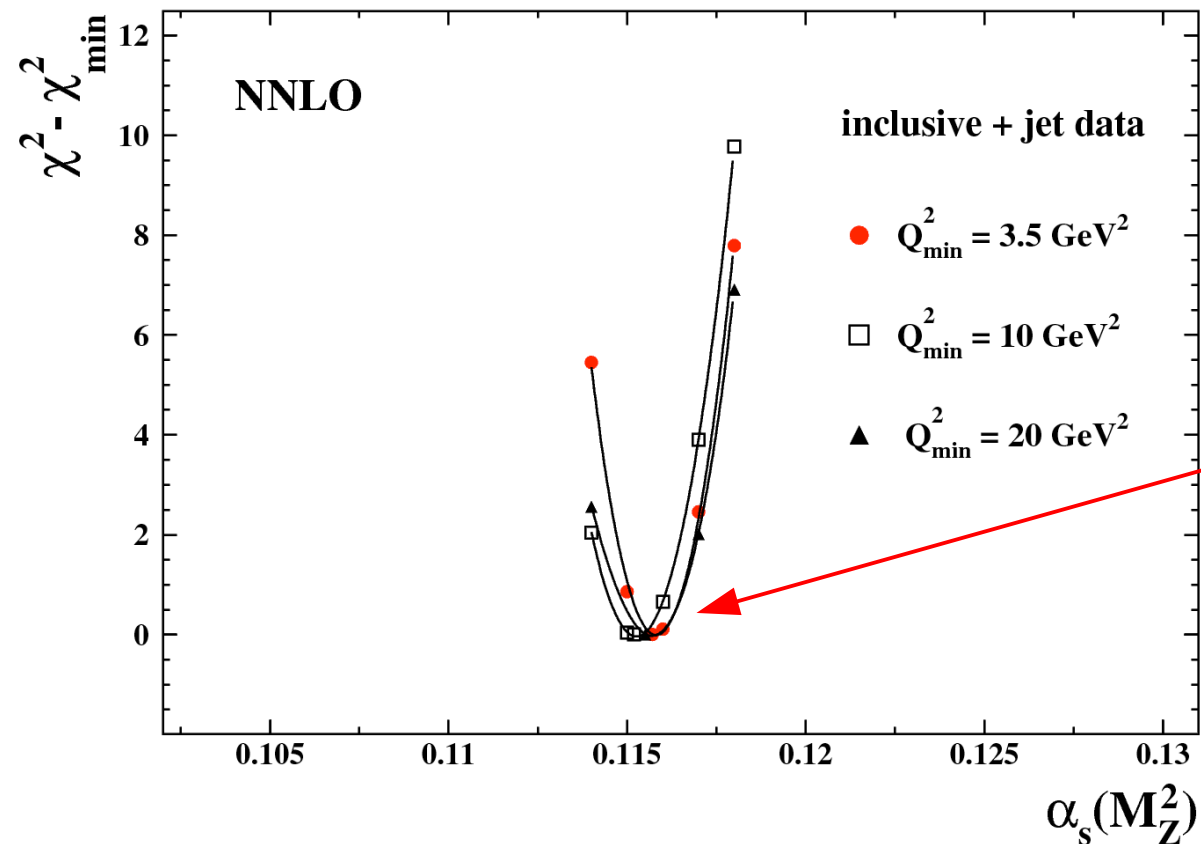
$Q^2$  cuts do not result in any significant change to the value of  $\alpha_s(M_Z)$



# Preliminary: scans with harder $Q^2$ cuts

- Results with new settings and low- $p_T$  data, same  $Q^2$  cuts
  - $Q^2 > 10 \text{ GeV}^2$ : scan:  $\alpha_s = 0.1153 \pm 0.0009$ ;  $\alpha_s$ -free fit:  $\alpha_s = 0.1152 \pm 0.0008$
  - $Q^2 > 20 \text{ GeV}^2$ : scan:  $\alpha_s = 0.1155 \pm 0.0010$ ;  $\alpha_s$ -free fit:  $\alpha_s = 0.1155 \pm 0.0008$

H1 and ZEUS towards final results

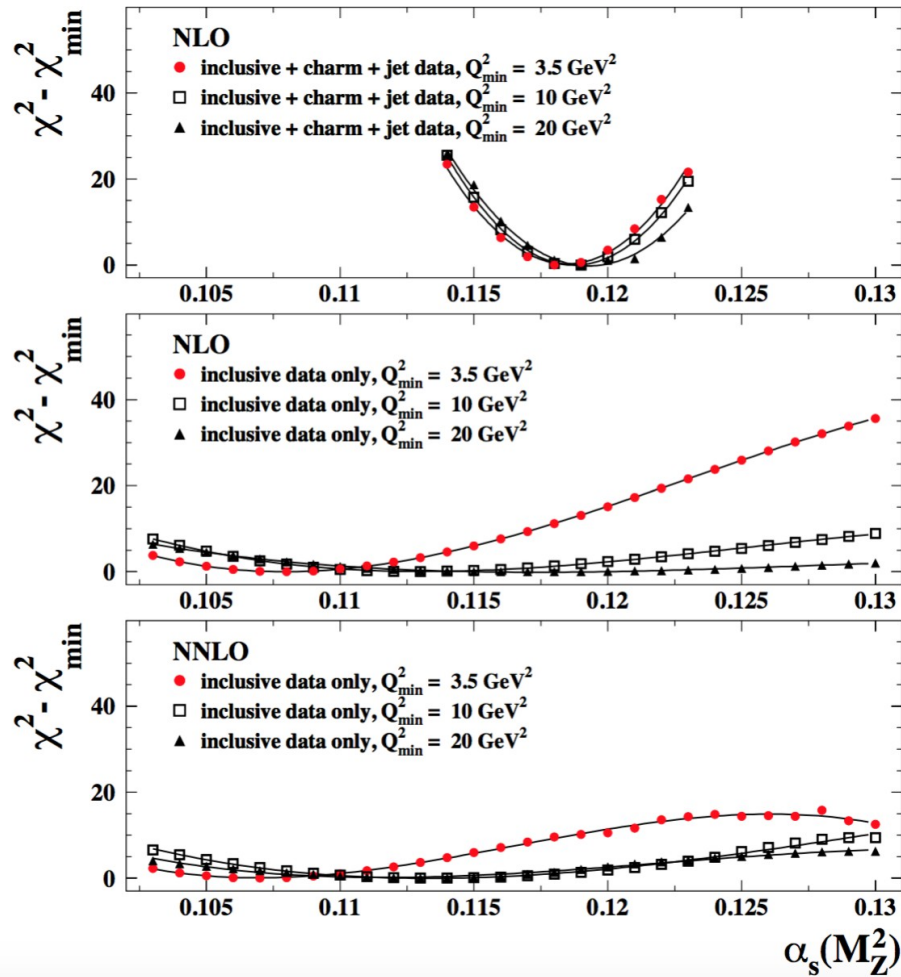


$Q^2$  cuts do not result in any significant change to the value of  $\alpha_s(M_Z)$

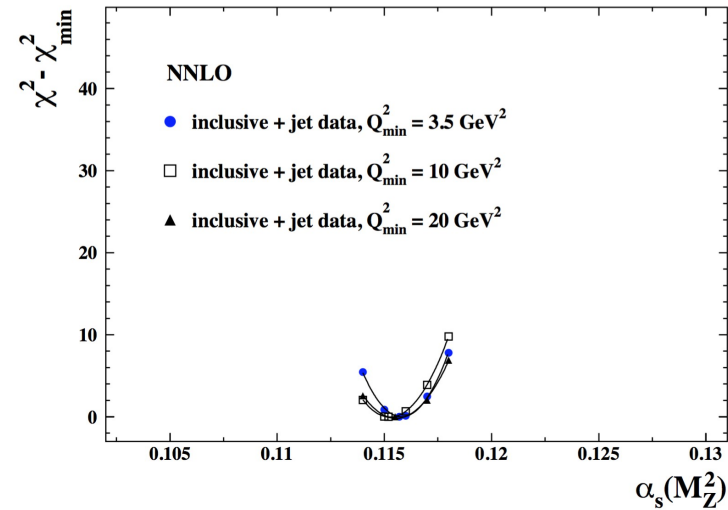
# Finally a full picture of jets@HERA



H1 and ZEUS



H1 and ZEUS towards final results



- Just as at NLO the jet data constrain  $\alpha_s(M_Z)$
- Similar level of accuracy at NNLO and NLO
- $\alpha_s(M_Z)$  clearly lower at NNLO



# Summary & conclusions

→ no real change since preliminary

- HERAPDF2.0 family completed
  - new settings and low- $p_T$  points added, analysis repeated
  - some things still need to be done:
    - Hadronisation and scale uncertainties (we do not expect them to change)
    - Some model/param uncertainties to be added (Duv, one inclusive cut)

- Jet data allow us to constrain  $\alpha_s(M_Z)$

PRELIMINARY

$$\alpha_s(M_Z^2) = 0.1150 \pm 0.0008(\text{exp})_{-0.0005}^{+0.0002}(\text{model/parameterisation}) \\ \pm 0.0006(\text{hadronisation}) \pm 0.0027(\text{scale}) .$$

NEW

- Compared to new  $\alpha_s(M_Z^2) = 0.1150 \pm 0.0008(\text{exp})_{-0.0003}^{+0.0001}(\text{model/parameterisation})$

$$\alpha_s(M_Z^2) = 0.1183 \pm 0.0009(\text{exp}) \pm 0.0005(\text{model/parameterisation}) \\ \pm 0.0012(\text{hadronisation})_{-0.0030}^{+0.0037}(\text{scale}) .$$

- Compared to NLO result

Systematic shift downwards at NNLO and reduction of scale uncertainty

# Outlook

- Next steps are rather clear
  - finish missing parts of analysis
  - show these results tomorrow at H1/ZEUS meeting; ask for their "approval" (so lack of trouble ...)
  - paper draft v0 in place
  - would like to start official publishing procedure in april





## Comparison to other HERAPDF2.0 fits

- NNLO fits with and without jets of similar quality
  - $\chi^2/\text{d.o.f} = 1.203$  for free  $\alpha_s(M_Z)$  fit with 1328 degrees of freedom
  - $\chi^2/\text{d.o.f} = 1.205$  for HERAPDF2.0NNLO with only 1131 degrees of freedom
- NLO and NNLO results for  $\alpha_s(M_Z)$  consistent within experimental uncertainties
  - **Scale uncertainties reduced**
    - as expected for NNLO calculations

### HERAPDF2.0Jets NNLO (prel.), free $\alpha_s(M_Z)$

$$\alpha_s(M_Z^2) = 0.1150 \pm 0.0008(\text{exp})_{-0.0005}^{+0.0002}(\text{model/parameterisation}) \pm 0.0006(\text{hadronisation}) \pm 0.0027(\text{scale}) .$$

### HERAPDF2.0Jets NLO

$$\alpha_s(M_Z^2) = 0.1183 \pm 0.0009(\text{exp}) \pm 0.0005(\text{model/parameterisation}) \pm 0.0012(\text{hadronisation}) \begin{matrix} +0.0037 \\ -0.0030 \end{matrix}(\text{scale}) .$$