

Short About PROFFIT

Prepared by Albert for the
MC meeting in Karlsruhe, 4/12-2009

- Based on the same principle as PROFESSOR.
- Originally developed for fitting uPDFs
- Written in Fortran – reads hbook-files –
Several HERA analyses good for fitting (u)PDF – exist already coded in HZTOOL
- Singular Value Decomposition used to determine the polynomial describing the MC grid.
If few parameters are fitted a 4th order polynomial can be used to described the MC grid.
However, while a 3rd order poly is a clear improvement over 2nd order, the 4th order do usually nor improve the $\chi^2(\text{MC} - \text{Poly})$.
- The fit of the MC parameters (in the polynomial) to the data is done by Minuit (MIGRAD)
- Currently equidistant MC grids has been used (PROFESSOR use randomized grids(?))

- The statistical errors of the MC is propagated to the coefficients of the polynomial. A co-variance matrix for the coefficients are calculated.
- The CTEQ error calculation is used to take the correlated errors in the data into consideration. Basically the Chi2 is differently calculated.
- In the fit of the MC parameters to the data the uncorrelated errors and the different correlated errors are treated separately according to:

$$\chi^2 = \sum \frac{(X_{Data} - X_{Polynomial})^2}{\alpha^2} - \sum_j \sum_{j'} B_j (A^{-1})_{jj'} B_{j'}$$

$$\alpha^2 = \text{Sum of uncorrelated errors (data and polynomial)}$$

$$\sum_j \sum_{j'} B_j (A^{-1})_{jj'} B_{j'} = \text{Term related to the correlated systematic errors (vector } B), \text{ and their correlations (matrix } A)$$

(From the CTEQ group, hep/ph/0101051,
code from Federico von Samson-Himmels tjerna)

$$xA_0(x, k_T, \bar{q}_0) = N \cdot x^{-B} \cdot (1 - x)^C \cdot \exp\left(-\frac{(k_T - \mu)^2}{2\sigma^2}\right)$$

Fitting F2 in the range $x < 0.005$, $Q^2 > 4.5$,
gives:

Minimum

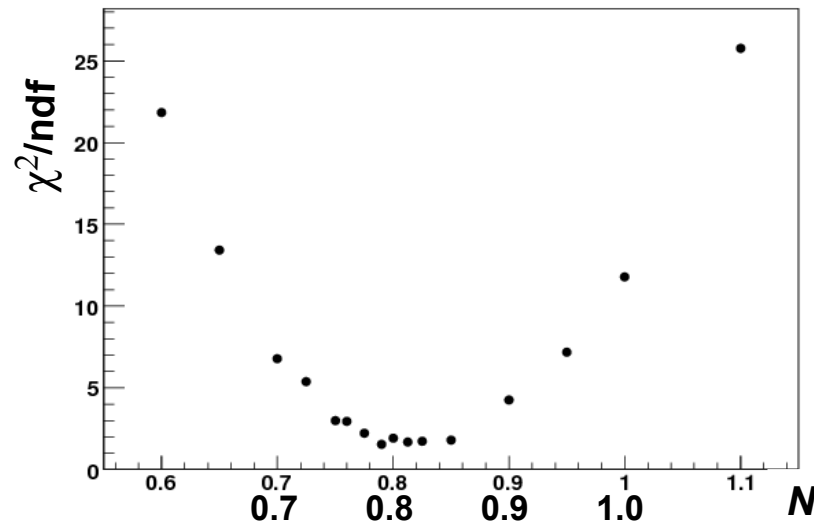
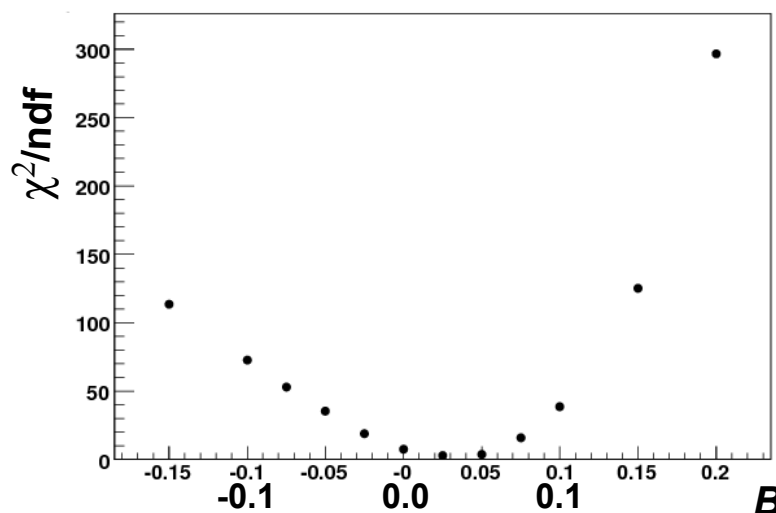
$N = 0.807 \pm 0.016$

$B = 0.029 \pm 0.004$

$\chi^2/\text{ndf} = 1.2$

This is a good fit which reconstructs the parameter values in an already existing uPDF tuned to F2 within the same kinematic range...
(Good validation of the method.)

χ^2 - profiles as for the fitted parameters:



Some fitting results

However if we **open up the phase space and fit all the F2 data points in the measurement**, we obtain the minimum:

$$xA_0(x, k_T, \bar{q}_0) = N \cdot x^{-B} \cdot (1-x)^C \cdot \exp\left(-\frac{(k_T - \mu)^2}{2\sigma^2}\right)$$

Minimum

$$N = 0.767 \pm 0.001$$

$$B = 0.028 \pm 0.000$$

$$\text{Chi2/ndf} = 5.4$$

Inspired by the CTEQ people we added an extra factor in the starting distribution

$$xA_0(x, k_T, \bar{q}_0) = N \cdot x^{-B} \cdot (1-x)^C \cdot (1 - Dx) \cdot G(k_T)$$

Fitting F2 over the full range in x gives a slightly different gluon then before.
uPDF allowed to be **more pronounced at low and high x**:

Minimum

$$N = 0.487 \pm 0.007$$

$$B = 0.097 \pm 0.003$$

$$D = -5.10 \pm 0.35$$

$$\text{Chi2/ndf} = 2.8$$

$$(\text{Before: Chi2/ndf} = 5.4)$$

