

# Improving iterative phase retrieval using neural networks

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# Phase retrieval - background

$u$ ...object of interest

$v$ ...exit wave

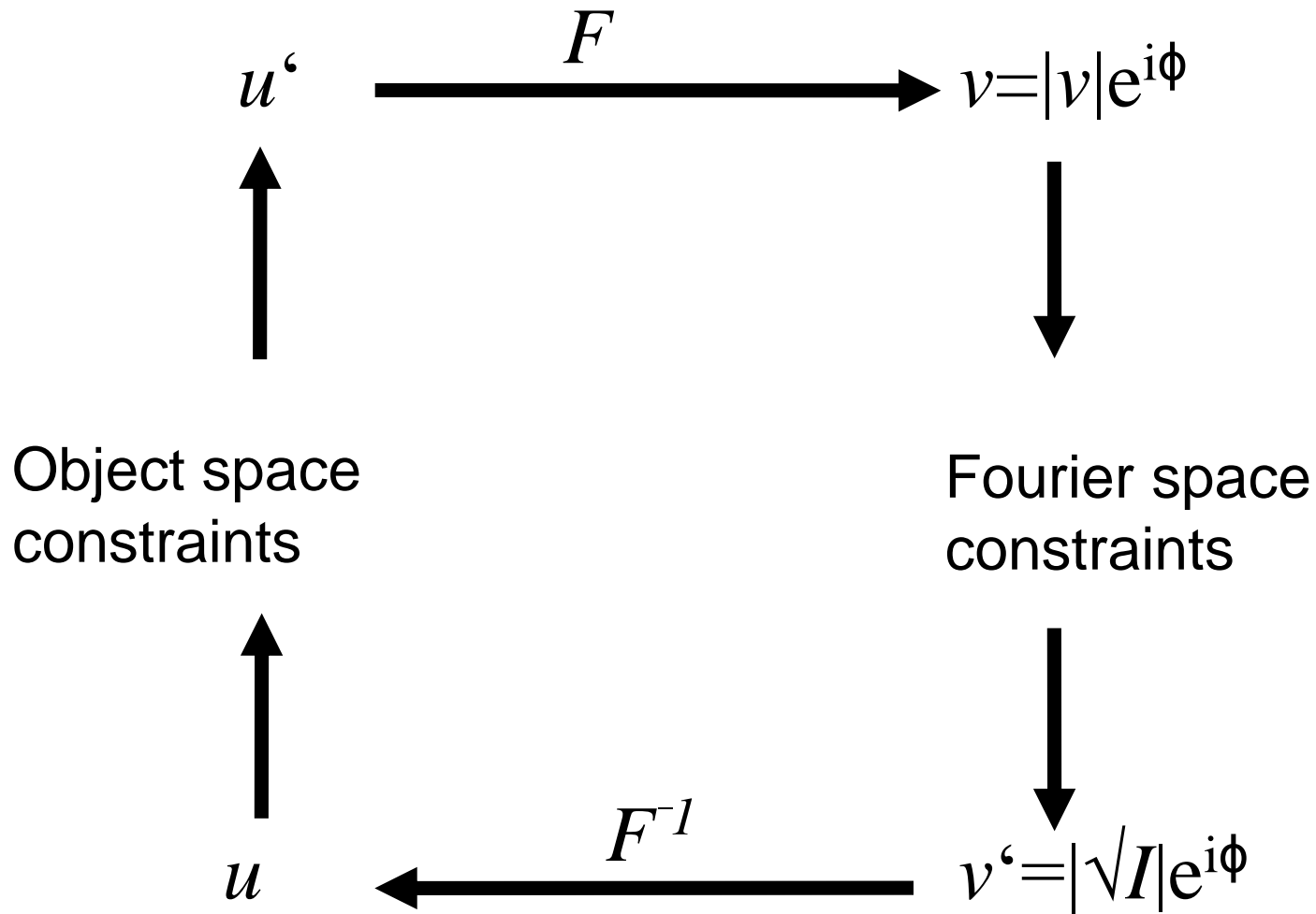
$I$ ...detected intensity on detector

$\Phi$ ...phase which is not detected

$$I \sim |v|^2 = |\mathcal{F}(u)|^2$$

$$v(q) = |v(q)|e^{i\phi q}$$

# Phase retrieval – iterative reconstruction



# Phase retrieval – iterative reconstruction

## Methods:

- Error reduction [Gerchberg, Saxton, 1972]
- Hybrid-input-output [Fienup, 1982]
- Extensions, e.g. Relaxed Averaged Alternating Reflections [Luke 2005]:

$$u_{i+1}^{RAAR} = u_i^M D + (\beta u_i + (1 - 2\beta)u_i^M)\overline{D}$$

where  $u_i^M$  is calculated from  $u_{i-1}$  being projected to  $M$ :

$$M = \{u \text{ with } |\mathcal{F}(u)|^2 = I\}$$

## Drawbacks:

- Not robust, e.g. for noisy data
- Empirical optimization
- Not working for 1D data without further constraints

# Phase retrieval – how to measure reconstruction quality?

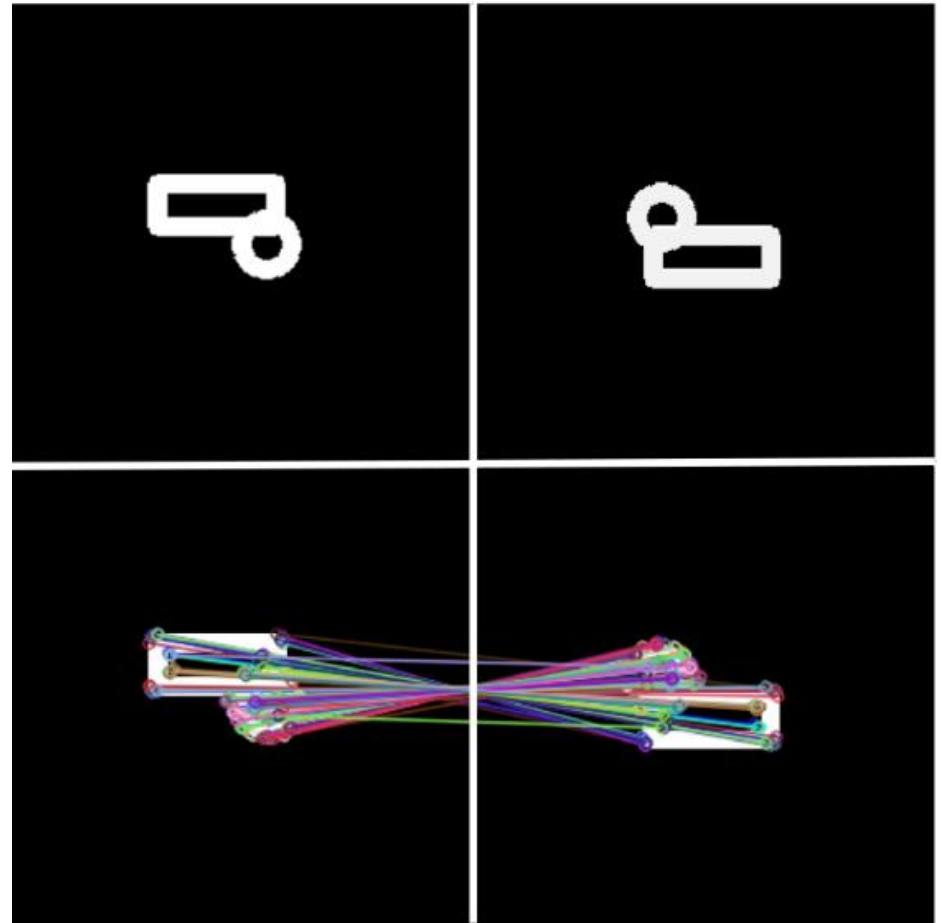
Characteristic solutions  
(Bates '82) are also valid, i.e.  
translations and phase shifts

⇒ Need for translation-  
invariant quality measure

⇒ ORB ratio based on  
„feature“ comparison

⇒ From Computer Vision

⇒ Applied in Clemens  
Reinhardt's master thesis



# Phase retrieval – how to measure good reconstruction?

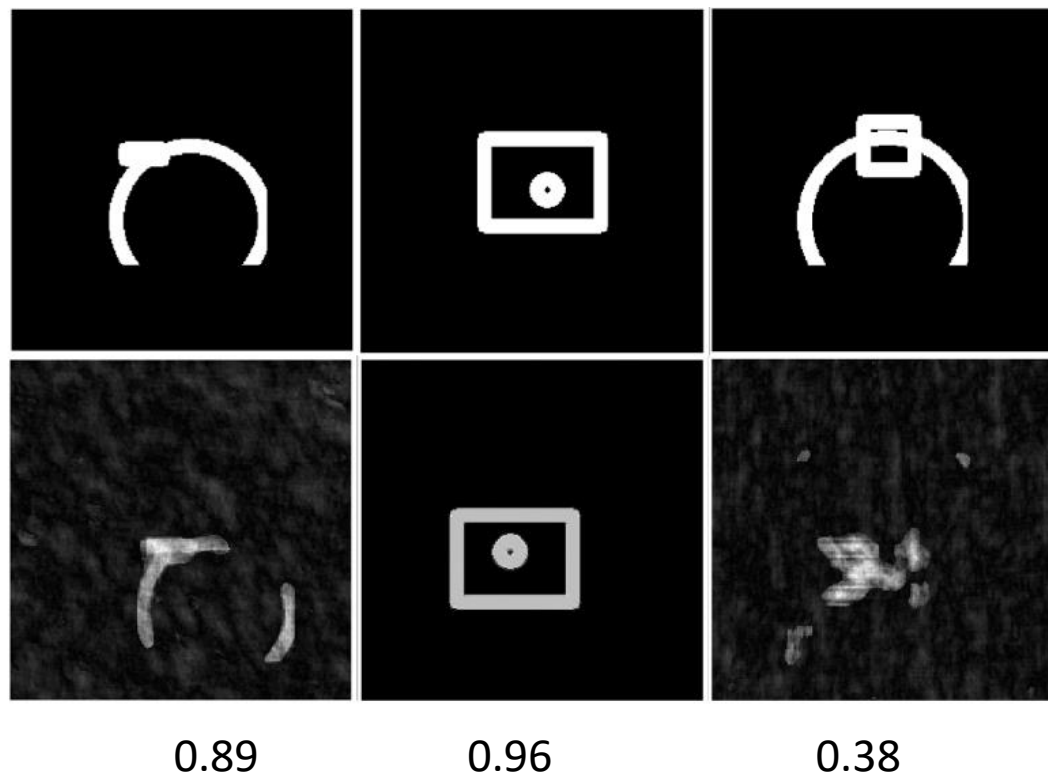
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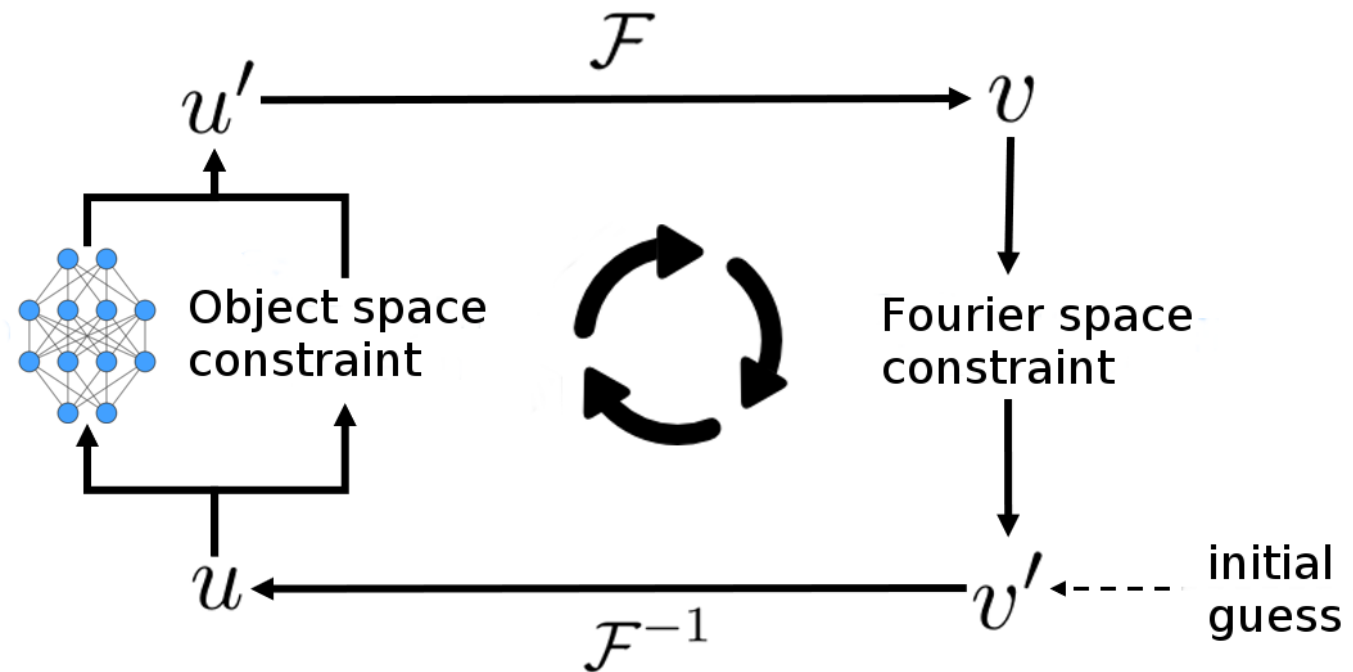
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# Phase retrieval – the ML approach

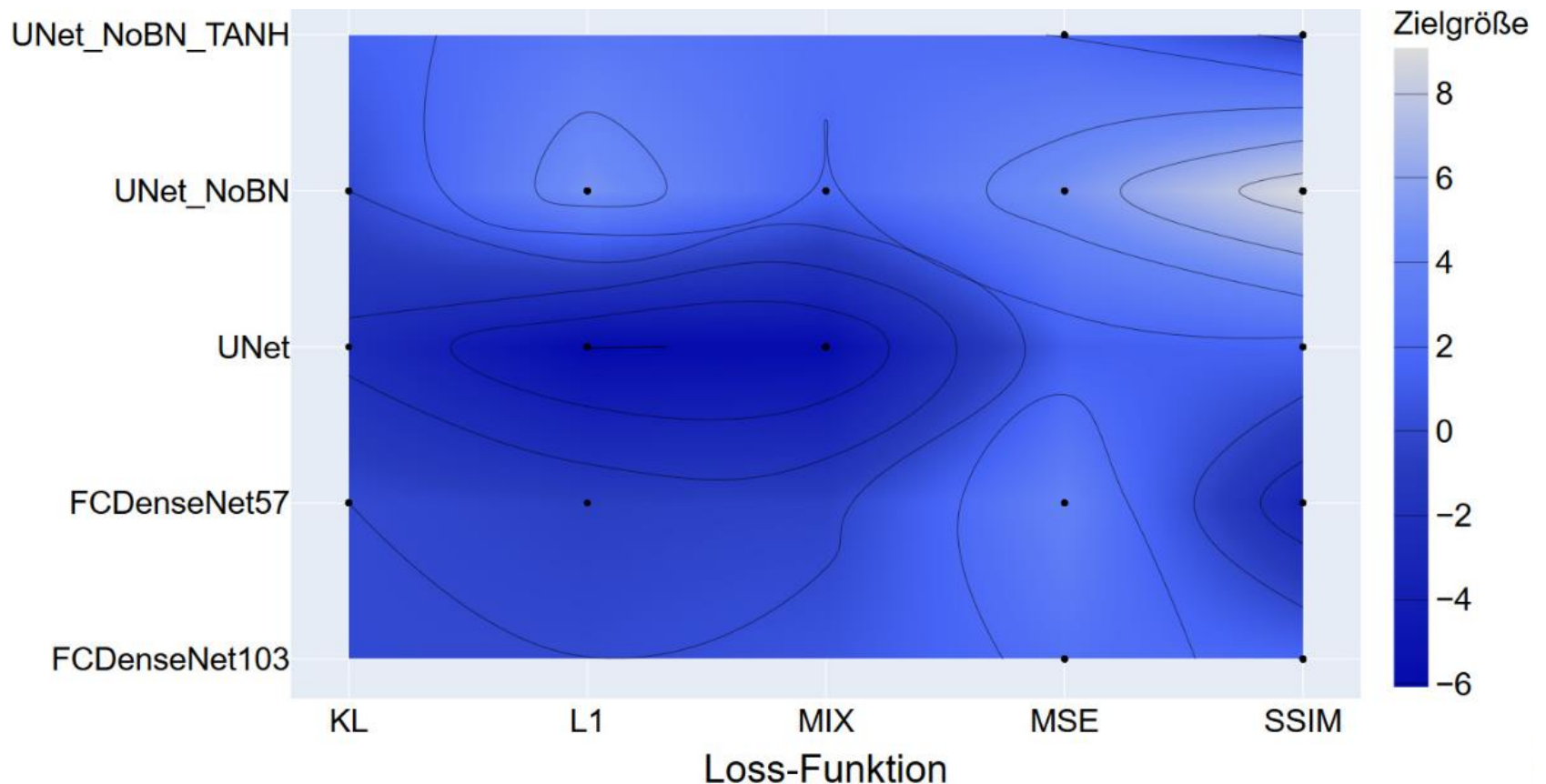


$$u_{i+1} = \alpha u_{i+1}^{RAAR} + (1 - \alpha) u_{i+1}^{NN}$$

# The ML approach

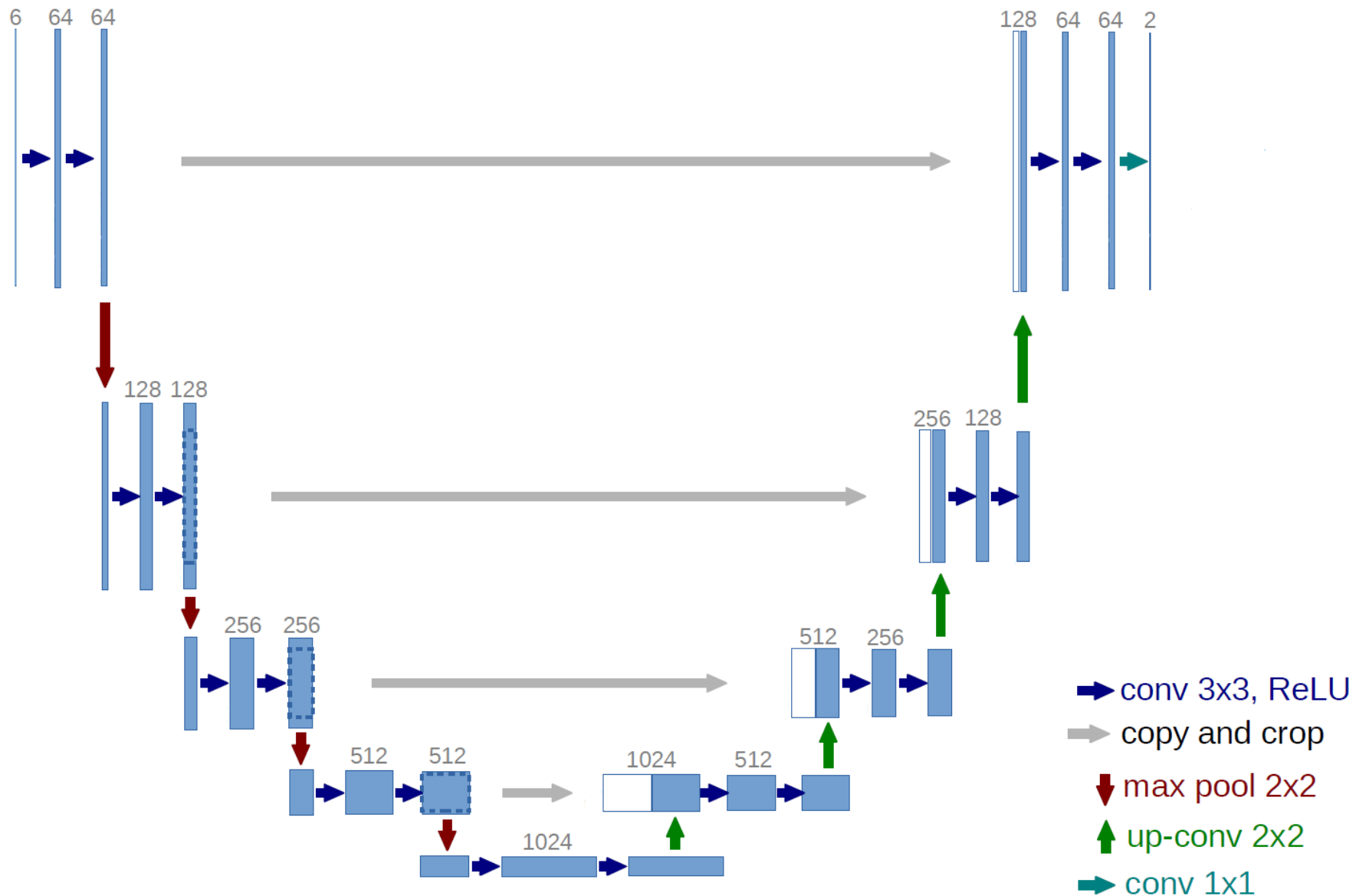
How to find a suitable neural network?

⇒ Optimization strategy for architecture and parameters using the framework OPTUNA

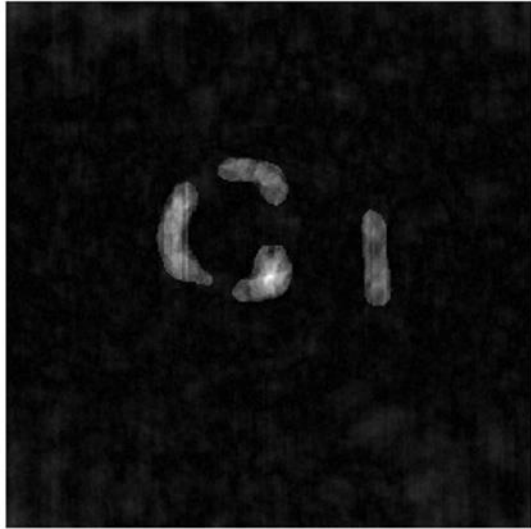




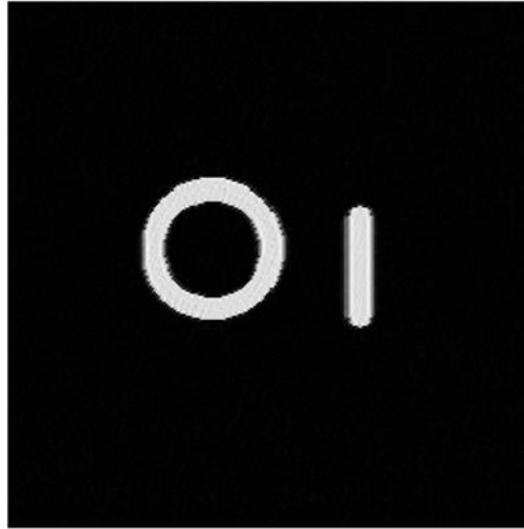
# The ML approach – the winning network



## The ML approach - results



RAAR

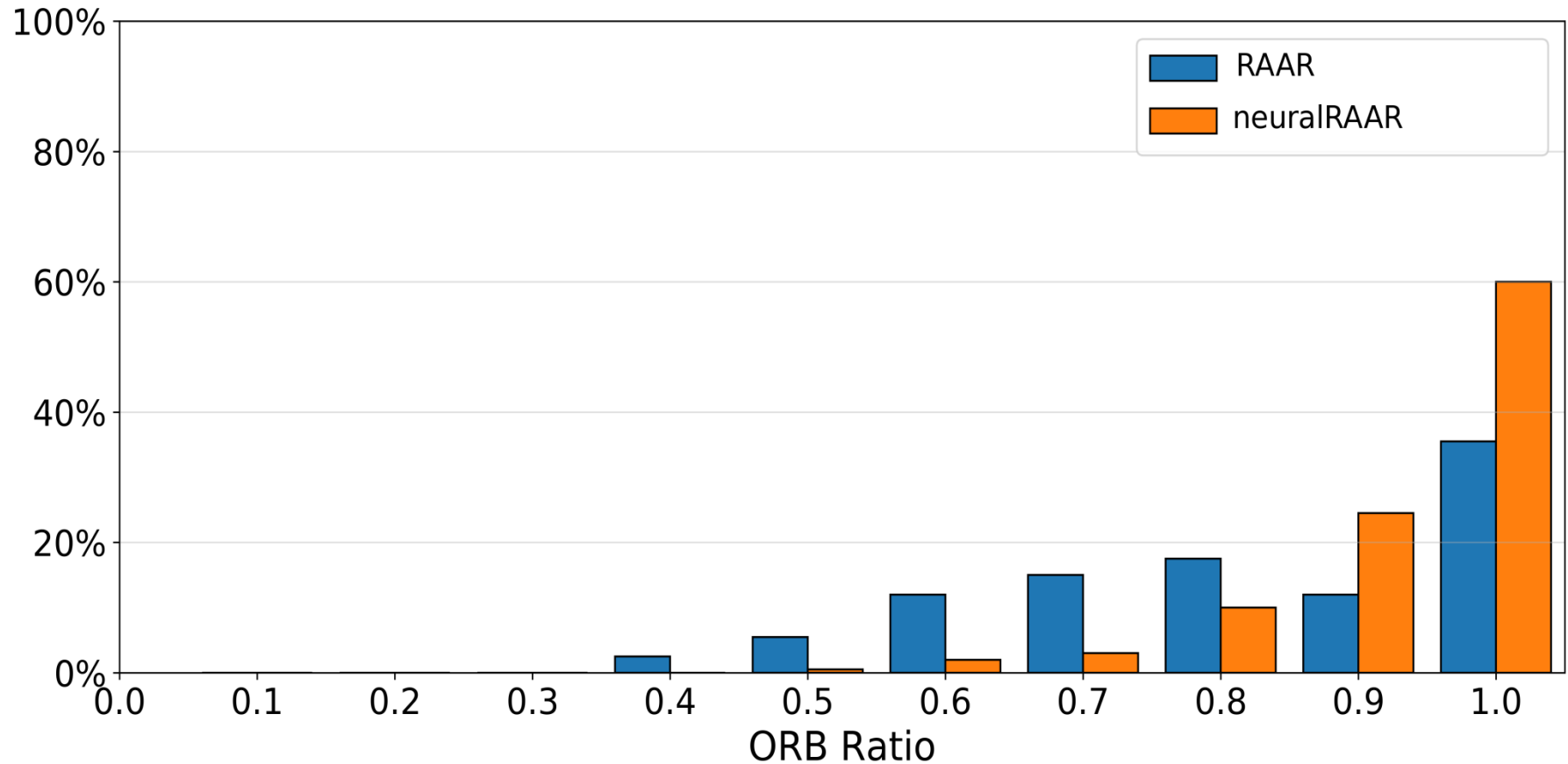


neuralRAAR

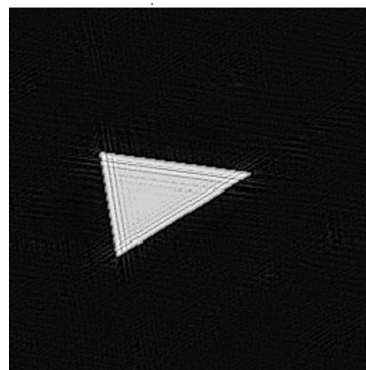


ground truth

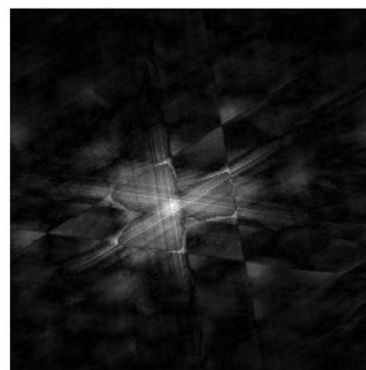
## The ML approach - results



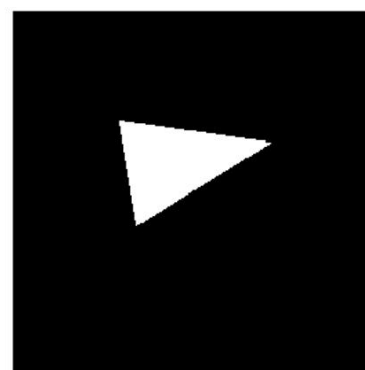
## The ML approach - generalization



neuralRAAR



RAAR



ground truth

