













Intro to Quantum Computing

Workshop on Quantum Computing and Quantum Sensors **DESY, August 11, 2020**

Martin J Savage



INSTITUTE for NUCLEAR THEORY

Quantum Information Science and Computing

- QIS: the nature, acquisition, storage, manipulation, computing, transmission, and interpretation of information.
- Entanglement and superposition distinguish quantum information from classical information.
- Improving control of superposition and entanglement over macroscopic space-time volumes has produced first devices for quantum computation and quantum sensing. Defining the Quantum-2 era.



The Potential of Quantum Computing



 \sim 100 qubit devices can address problems in chemistry that are beyond classical computing

50 qubits : ~ 20 petabytes ~ Leadership-Class HPC facility

300 qubits : more states [1090] than atoms in universe [1086]

Where a quantum advantage may be achieved







Quantum Field Theories and Fundamental Symmetries

- indefinite particle number
- gauge symmetries and constraints neutrino-nucleus interactions
- entangled ground states

Real-Time Dynamics

- parton showers
- fragmentation
- - neutrinos in matter
 - early universe
 - phase transitions matter?
 - non-equilibrium

Dense Matter

- neutron stars
- gravity waves
- > medium nuclei
- chemical potentials

Where a quantum advantage may be achieved - 2







Classical Computing

- Euclidean space
- high-lying states difficult
- signal-to-noise
- severe limitations for real-time or inelastic collisions or fragmentation

Quantum Computing

- real-time Minkowski space evolution
- exponentially-large Hilbert spaces
- S-matrix
- mitigated sign problem(s) (naively)
- integrals over phases

"First Qubits" for Scientific Applications



Hemmerling, Cornel, <u>https://www.photonics.com/Article.aspx?AID=64150</u>

NISQ-era quantum devices for applications

Analog, Digital and Hybrid Simulation



H : native to system e.g. atoms in optical lattices SRF cavities BECs

systematics?

e.g. trapped-ions, superconducting qubits H : universal gate sets

NISQ, a while before error-corrected

QPU "like" a GPU for the intrinsically quantum parts of the computation

Scaling?

Analog Simulation (classic) examples

Allan Adams1, Lincoln D Carr2,3,6, Thomas Schäfer4, Peter Steinberg5 and John E Thomas4

Published 19 November 2012 • IOP Publishing and Deutsche Physikalische Gesellschaft New Journal of Physics, Volume 14, November 2012







cold atom simulation

Elliptic flow

Analog Simulation examples SRF cavities

LLNL and FermiLab







Toward nuclear reactions and field theory

Analog Simulation : Quantum Field Theory - ideas

Simulating Lattice Gauge Theories within Quantum Technologies

M.C. Bañuls^{1,2}, R. Blatt^{3,4}, J. Catani^{5,6,7}, A. Celi^{3,8}, J.I. Cirac^{1,2}, M. Dalmonte^{9,10}, L. Fallani^{5,6,7}, K. Jansen¹¹, M. Lewenstein^{8,12,13}, S. Montangero^{7,14}, C.A. Muschik³, B. Reznik¹⁵, E. Rico^{16,17}, L. Tagliacozzo¹⁸, K. Van Acoleyen¹⁹, F. Verstraete^{19,20}, U.-J. Wiese²¹, M. Wingate²², J. Zakrzewski^{23,24}, and P. Zoller³

arXiv:1911.00003v1 [quant-ph] 31 Oct 2019

Towards analog quantum simulations of lattice gauge theories with trapped ions

Zohreh Davoudi,^{1,2,*} Mohammad Hafezi,^{3,4} Christopher Monroe,^{3,5} Guido Pagano,^{3,5} Alireza Seif,³ and Andrew Shaw¹

arXiv:1908.03210v1 [quant-ph] 8 Aug 2019



Quantum Simulation of the Abelian-Higgs Lattice Gauge Theory with Ultracold Atoms

Daniel González-Cuadra^{1,2}, Erez Zohar² and J. Ignacio Cirac²

¹ ICFO – The Institute of Photonic Sciences, Av. C.F. Gauss 3, E-08860, Castelldefels (Barcelona), Spain
² Max-Planck-Institut für Quantenoptik, Ham-Kopfermann-Straße 1, D-85748 Gaeching,

Max-Planck-Institut für Quantenoptik, Ham-Kopfermann-Straße 1, D-85748 Garching, ermany



Figure 23: Different atomic species reside on different vertical layers. Green straight lines show how the auxiliary atoms have to move in order to realise interactions with the link atoms and the fermions, or to enter odd plaquettes. Red arrows show selective tunnelling of fermions across even horizontal links. From [152]. Quantum Link Models (see Schladaming lectures by Uwe-Jens Wiese, 2015)

A Framework for Simulating Gauge Theories with Dipolar Spin Systems

Di Luo,^{1, 2, *} Jiayu Shen,^{1, *} Michael Highman,¹ Bryan K. Clark,^{1, 2} Brian DeMarco,¹ Aida X. El-Khadra,¹ and Bryce Gadway¹ ¹Department of Physics and IQUIST, University of Illinois at Urbana-Champaign, IL 61801, USA ²Institute for Condensed Matter Theory, University of Illinois at Urbana-Champaign, IL 61801, USA



Figure 1. Emulating quantum link models (QLMs) with arrays of dipolar molecules. (a) Mapping between the rotational levels of molecules in an array and the sites and links of the QLM for spin S = 1/2. The designation of particular molecules as sites or links $(S_x, L_x, S_{x+1}, L_{x+1})$ for a given unit cell) is enforced through local laser control of level-dependent light shifts. (b) Low-lying molecular rotational levels $|N, m_N\rangle$ and their redefinition in terms of states $|a\rangle$, $|b\rangle$, $|c\rangle$, and $|d\rangle$. (c) The hopping of "fermions" between sites and the associated spin operations on the links are realized by a second-order dipolar exchange of rotational excitations.

Digital Simulation



quantum circuits using a set of gates

e.g., entangling gate $CNOT(1;2) = \Lambda_0 \otimes I + \Lambda_1 \otimes \sigma_x$



https://www.extremetech.com/extreme/204553-ibm-gets-closer-to-real-quantum-computing

https://medium.com/@jonathan_hui/qc-how-to-build-a-quantum-computer-with-superconducting-circuit-4c30b1b296cd

Digital Simulation



Minimal or no error correction

- Few hundred qubits with modest gate depth
- Imperfect quantum gates/operations like ``running experiments''
- Different ``flavors"
- NISQ-era is the next decade of quantum simulation
 - much to be gained during this period
 - learn by doing just like all experiments

First Steps being taken to understand our problems

 Searching to find Quantum Advantage(s) in scientific applications

Generically, 3 "workflow phases"

- 1. state preparation generally, entangled
- 2. time-evolution Trotterized evolution operator
- 3. measurement

Scalar Field Theory The Gold Standard - Jordan, Lee, Preskill



- Discretize 3-d Space
- Define Hamiltonian on grid
- Trotterized time evolution
- Technology transfer from Lattice QCD
- Digitize field(s)

$$\begin{split} \hat{H} &= \hat{H}_{\Pi} + \hat{H}_{\phi} \\ \hat{\mathcal{H}}_{\Pi} &= \frac{1}{2}\Pi^2 \ , \ \hat{\mathcal{H}}_{\phi} \ = \ \frac{1}{2}(\nabla\phi)^2 \ + \ \frac{1}{2}m^2\phi^2 + \frac{\lambda}{4!}\phi^4 \\ \hat{H}_{\phi} &= b\sum_x \left(\ \frac{1}{2}\phi_j\phi_{j+1} + \frac{1}{2}\phi_j\phi_{j-1} - \phi_j^2 \ + \ \frac{1}{2}m^2\phi_j^2 + \frac{\lambda}{4!}\phi_j^4 \right) \end{split}$$

Scattering Wavepackets in Scalar Field Theory

Quantum Computation of Scattering in Scalar Quantum Field Theories

Stephen P. Jordan,^{†§} Keith S. M. Lee,^{‡§} and John Preskill [§] *



1. Create wavepackets of free theory

- 2. Adiabatically evolve the system to interacting system
- 3. Evolve the prepared state forward
- 4. Adiabatically evolve systems to free theory OR introduce localized detectors into the simulation

Digital Simulation Dynamics in the Schwinger Model Baby steps using small, 1dim systems



Shaw, Alexander F.¹, Lougovski, Pavel¹, Stryker, Jesse R.², and Wiebe, Nathan^{3,4}

arXiv:2002.11146v1 [quant-ph]

Digital Simulation Examples



Towards fragmentation and hadronic structure



A quantum algorithm for high energy physics simulations

Christian W. Bauer, Wibe A. de Jong, Benjamin Nachman, Davide Provasoli, arXiv:1904.03196 [hep-ph]

$$\mathcal{L} = \bar{f}_1 (i\partial \!\!\!/ + m_1) f_1 + \bar{f}_2 (i\partial \!\!\!/ + m_2) f_2 + (\partial_\mu \phi)^2 + g_1 \bar{f}_1 f_1 \phi + g_2 \bar{f}_2 f_2 \phi + g_{12} \left[\bar{f}_1 f_2 + \bar{f}_2 f_1 \right] \phi .$$

Deeply inelastic scattering structure functions on a hybrid quantum computer

Niklas Mueller,^{*} Andrey Tarasov,[†] and Raju Venugopalan[‡] Physics Department, Brookhaven National Laboratory, Bldg. 510A, Upton, NY 11973, USA (Dated: August 21, 2019)

Parton Physics on a Quantum Computer

Henry Lamm,^{1,*} Scott Lawrence,^{1,†} and Yukari Yamauchi^{1,‡} (NuQS Collaboration)

¹Department of Physics, University of Maryland, College Park, Maryland 20742, USA (Dated: February 18, 2020)

Digital Simulation The role of spin models HEP Sandbox

e.g. From spin chains to real-time thermal field theory using tensor networks



https://phys.org/news/2013-03-scientists-coherent-propagation-impurity-chain.html

$$H_{obc} = -J \sum_{i=1}^{N_s - 1} \hat{\sigma}_i^x \hat{\sigma}_{i+1}^x - h_T \sum_{i=1}^{N_s} \hat{\sigma}_i^z.$$



Unmuth-Yockey et al.

Mari Carmen Bañuls,^{1,2,*} Michal P. Heller,^{3,†} Karl Jansen,^{4,‡} Johannes Knaute,^{3,5,§} and Viktor Svensson^{6,3,¶}

Matrix Elements Toward Inelastic Neutrino Nucleus Interactions

Linear Response on a Quantum Computer

Alessandro Roggero^{*} and Joseph Carlson[†] Theoretical Division, Los Alamos National Laboratory, Los Alamos, New Mexico 87545, U (Dated: April 13, 2018) Short-depth circuits for efficient expectation value estimation

A. Roggero^{*} Institute for Nuclear Theory, University of Washington, Seattle, WA 98195, USA

A. Baroni[†] Department of Physics and Astronomy University of South Carolina, 712 Main Street, Columbia, South Carolina 29208, USA (Dated: May 22, 2019)



- a unitary \hat{U}_G which prepares the ground-state of the Hamiltonian of interest
- a unitary \hat{U}_O which implements time evolution under \hat{O} for a short time $\gamma < poly(\delta_S)$
- a unitary \hat{U}_t which implements time evolution under the system Hamiltonian for time t



How to Digitize Scalar Fields

What is the optimal way to map field theories onto NISQ-era quantum computers?



e.g., 3 Qubits = 8 States

Jordan, Lee and Preskill - several works Rolanda Somma [LANL] Macridin, Spentzouris, ... [FNAL] Siopsis, Pooser, ...[ORNL/UTK] Klco,MJS [UW]

e.g., Gray-encoding Olivia diMatteo *et al*

Localized State Preparation and the RG



Digital Simulation Lattice Theories: Logical Qubits and Error Correction





Quantum Spin Liquids: a Review

Lucile Savary¹, Leon Balents²

Starting down the Path Digitizing SU(2) Gauge Theory

FermiLab

Digitizing Gauge Fields: Lattice Monte Carlo Results for Future Quantum Computers

Daniel C. Hackett,^{1,*} Kiel Howe,^{2,†} Ciaran Hughes,^{2,‡} William Jay,^{1,2,§} Ethan T. Neil,^{1,3,¶} and James N. Simone^{2,**}

¹Department of Physics, University of Colorado, Boulder, Colorado 80309, USA ²Fermi National Accelerator Laboratory, Batavia, Illinois, 60510, USA ³RIKEN BNL Research Center, Brookhaven National Laboratory, Upton, New York 11973, USA



22



SU(2) Gauge Theory on IBMs Devices Two plaquettes with j_{max}=1/2 ... a toy

Simulating Lattice Gauge Theories within Quantum Technologies

M.C. Bañuls^{1,2}, R. Blatt^{3,4}, J. Catani^{5,6,7}, A. Celi^{3,8}, J.I. Cirac^{1,2}, M. Dalmonte^{9,10}, L. Fallani^{5,6,7}, K. Jansen¹¹, M. Lewenstein^{8,12,13}, S. Montangero^{7,14} ^a, C.A. Muschik³, B. Reznik¹⁵, E. Rico^{16,17} ^b, L. Tagliacozzo¹⁸, K. Van Acoleyen¹⁹, F. Verstraete^{19,20}, U.-J. Wiese²¹, M. Wingate²², J. Zakrzewski^{23,24}, and P. Zoller³

SU(2) non-Abelian gauge field theory in one dimension on digital quantum computers

Natalie Klco, Jesse R. Stryker and Martin J. Savage¹

¹Institute for Nuclear Theory, University of Washington, Seattle, WA 98195-1550, USA (Dated: August 19, 2019 - 13:7)





Digital Simulation New ``Tricks"

Hamiltonian Simulation Algorithms for Near-Term Quantum Hardware

Laura Clinton*1,2, Johannes Bausch^{†1,3}, and Toby Cubitt^{‡1}

¹PhaseCraft Ltd.

²Department of Computer Science, University College London ³Department of Applied Mathematics and Theoretical Physics, University of Cambridge

March 2020



(d) On-site terms in H₅.





(c) Hopping terms in H₄.



$$H_{\rm FH} \coloneqq \sum_{i=1}^{N} h_{\rm on-site}^{(i)} + \sum_{i < j,\sigma} h_{\rm hopping}^{(i,j,\sigma)} \coloneqq u \sum_{i=1}^{N} a_{i\uparrow}^{\dagger} a_{i\uparrow} a_{i\downarrow}^{\dagger} a_{i\downarrow} + v \sum_{i < j,\sigma} \left(a_{i\sigma}^{\dagger} a_{j\sigma} + a_{j\sigma}^{\dagger} a_{i\sigma} + a_{j\sigma}^{\dagger} a$$

$$\begin{split} h_{\text{on-site}}^{(i)} &\to \frac{u}{4} \left(\mathbb{1} - Z_{i\uparrow} \right) \left(\mathbb{1} - Z_{i\downarrow} \right) \\ h_{\text{hopping,hor}}^{(i,j,\sigma)} &\to \frac{v}{2} \left(X_{i,\sigma} X_{j,\sigma} Y_{f'_{ij},\sigma} + Y_{i,\sigma} Y_{j,\sigma} Y_{f'_{ij},\sigma} \right) \\ h_{\text{hopping,vert}}^{(i,j,\sigma)} &\to \frac{v}{2} (-1)^{g(i,j)} \left(X_{i,\sigma} X_{j,\sigma} X_{f'_{ij},\sigma} + Y_{i,\sigma} Y_{j,\sigma} X_{f'_{ij},\sigma} \right), \end{split}$$

$$e^{i\delta Z_1 Z_2 Z_3} \approx e^{-i\sqrt{\delta/2}Z_1 X_2} e^{i\sqrt{\delta/2}Y_2 Z_3} e^{i\sqrt{\delta/2}Z_1 X_2} e^{-i\sqrt{\delta/2}Y_2 Z_3},$$

$$e^{i\delta Z_1 Z_2 Z_3 Z_4} \approx e^{-i0.22\delta^{2/3}Y_2 Z_3 Z_4} e^{-i1.13\delta^{1/3}Z_1 X_2} e^{i0.44\delta^{2/3}Y_2 Z_3 Z_4} e^{i1.13\delta^{1/3}Z_1 X_2} e^{-i0.22\delta^{2/3}Y_2 Z_3 Z_4}.$$

Together with new Trotter product formulae error bounds, and a novel low-weight fermionic encoding, this improves upon state-of-the-art results by over three orders of magnitude in circuit-depth-equivalent.

(e) Hopping terms in H₁.

See also, Childs *et al* https://arxiv.org/pdf/1912.08854.pdf

Digital Simulation New ``Tricks" Measurement-Error Correction

Measurement Error Mitigation in Quantum Computers Through Classical Bit-Flip Correction

Lena Funcke¹, Tobias Hartung², Karl Jansen³, Stefan Kühn⁴, Paolo Stornati^{3,5}, and Xiaoyang Wang⁶

promising development may scale better invertible by construction see also IBM, Rigetti







$$V_{device} = M.V_{mc}$$

IBM protocol Minimization to find M Apply to all measurements Costly to go to scale time-dependence -> high rep. rate

Lattice Simulations Distillable Entanglement

Natalie Klco+MJS

"Harmonic Chains" > 2004 Reznik, Marcovitch, Retzker, Plenio, Tonni, Calabrese, Cardy,....











- Quantum Simulations are expected to be able to address HEP problems inaccessible to HPC in the future
- ``spinning-up'' develop algorithms, expertise and workforce to move toward solving beyond-classical problems.
- Qualitative new understandings likely to feed back into classical?
- Sensors and simulators are intertwined
- Diverse collaboration are essential,
 - HEP, NP, BES, QIS, expt, theory

FIN

Analog Simulation : dense matter example

Selection of different experimental systems/atoms, controls, (number of) species and accessible observables

New Frontier

non-equilibrium dynamics of strongly-interacting systems e.g. evolution of domain walls

One example: Dilute neutron matter



Short-range correlations The ``Contact'' Unitary Fermi Gas



Fig. 5. (color online) Density and pressure distribution determined by the EOS. (a) Inside a neutron star. (b) Ultracold atoms trapped in an optical dipole trap.

Biswaroop Mukherjee, Parth B. Patel, Zhenjie Yan, Richard J. Fletcher, Julian Struck, Martin W. Zwierlein Spectral response and contact of the unitary Fermi gas, arXiv:1902.08548

https://arxiv.org/pdf/1901.00985.pdf

of Technology, Graduate School of Science

The University of Tokyo ps, Dunkyo-itu, Tokyo 115-8636, Japan hori@psc.Lu-takyo.ac.jp

Symmetric Exponentials on Poughkeepsie 3-spatial sites

Natalie Klco and MJS

IBM Poughkeepsie



Working with FermiLab to prepare entangled ground state

2+1, 3+1 Gauge Theories

Gauss's Law, Duality, and the Hamiltonian Formulation of U(1) Lattice Gauge Theory David B. Kaplan, Jesse R. Stryker, arXiv:1806.08797 [hep-lat]

SU(2) lattice gauge theory: Local dynamics on nonintersecting electric flux loops

Ramesh Anishetty, Indrakshi Raychowdhury, Phys.Rev. D90 (2014) no.11, 114503 arXiv:1408.6331 [hep-lat]

Digital quantum simulation of lattice gauge theories in three spatial dimensions

Julian Bender, Erez Zohar, Alessandro Farace, J. Ignacio Cirac, New J.Phys. 20 (2018) no.9, 093001, arXiv: 1804.02082 [quant-ph]

Quantum Simulation of Gauge Theories

NuQS Collaboration (Henry Lamm et al.). e-Print: arXiv:1903.08807 [hep-lat]



