

# *NEUTRAL HIGGS PRODUCTION*

Michael Spira (PSI)

I Introduction

II Higgs Boson Production @ LHC: Gluon Fusion

III Summary

# I INTRODUCTION

## (i) Standard Model

- LEP2:  $M_H > 114.4$  GeV

- triviality and vacuum stability:

$$\Rightarrow M_H \lesssim 700 \text{ GeV } [\Lambda \sim 1 \text{ TeV}]$$

$$130 \text{ GeV} \lesssim M_H \lesssim 190 \text{ GeV } [\Lambda \sim M_{GUT}]$$

Cabibbo  
Sher  
Lindner  
Lüscher, Weisz  
Hasenfratz, ...  
...

- elw. fits:  $M_H \lesssim 193$  GeV (95% CL)

LEP/SLC

- LHC:  $gg \rightarrow H$  dominant

F

$$M_H \lesssim 140 \text{ GeV}: H \rightarrow \gamma\gamma, (b\bar{b})$$

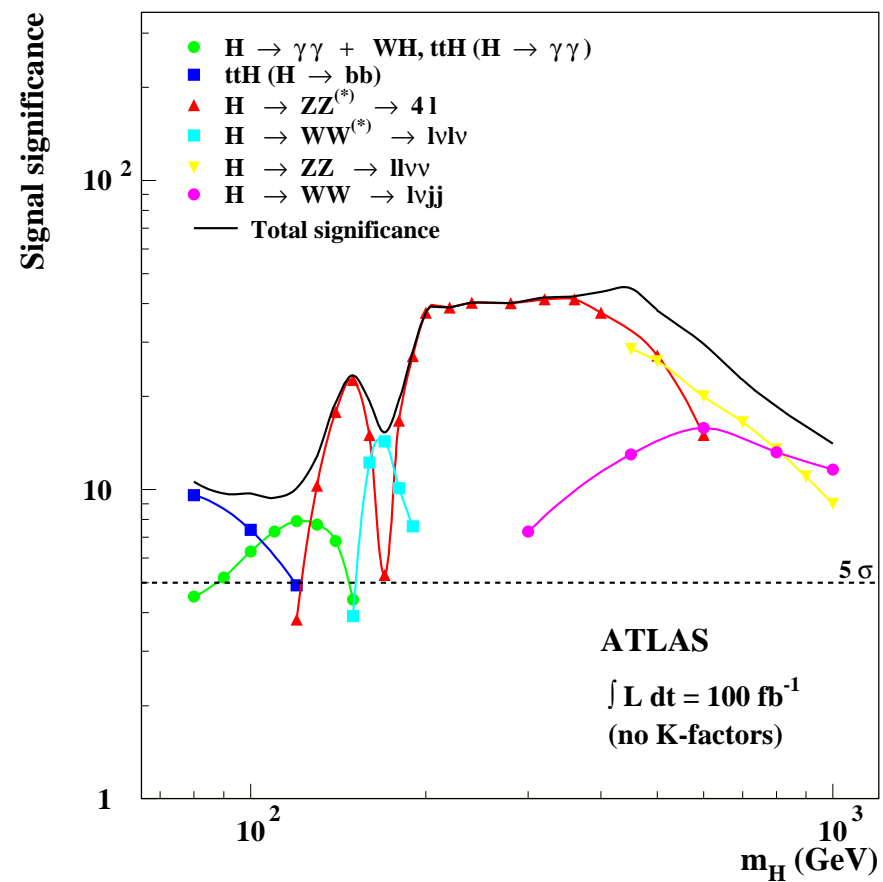
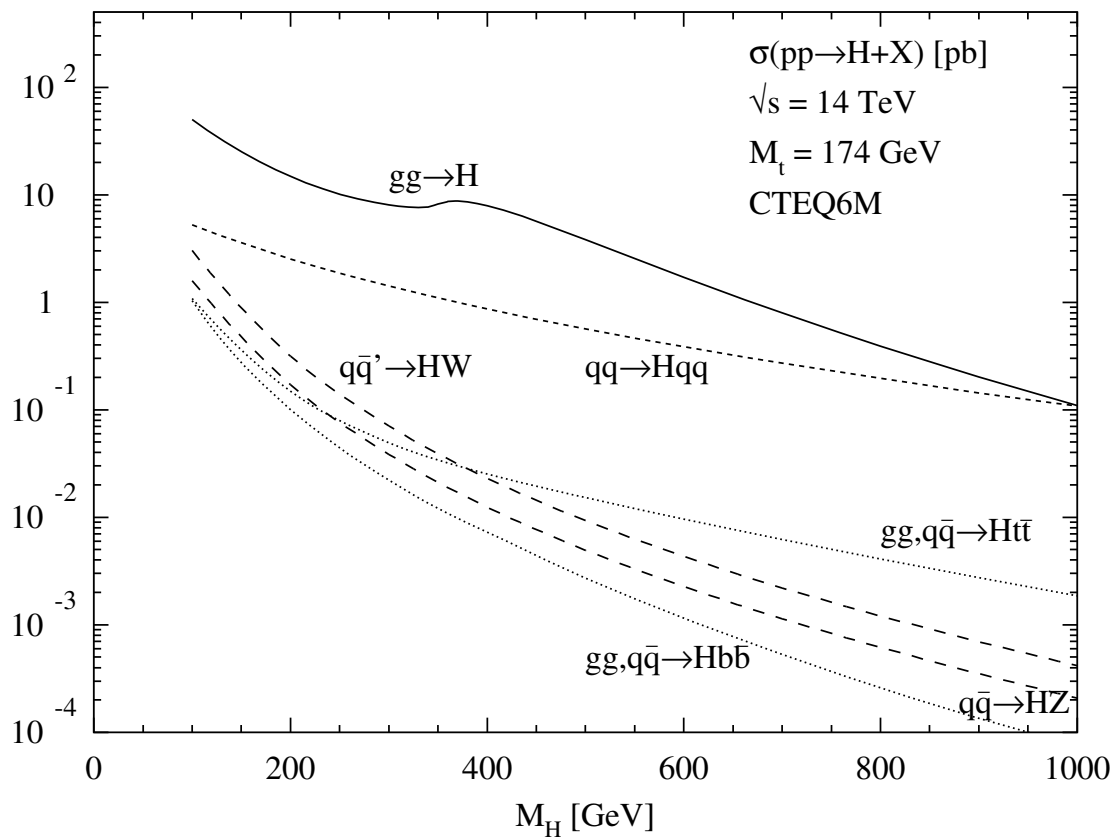
F

$$140 \text{ GeV} \lesssim M_H \lesssim 1 \text{ TeV}: H \rightarrow ZZ^{(*)} \rightarrow 4\ell^\pm$$

$$H \rightarrow WW, ZZ \rightarrow \ell's, jets$$

$$120 \text{ GeV} \lesssim M_H \lesssim 200 \text{ GeV}: H \rightarrow WW^{(*)} \rightarrow \ell^+\ell^-\nu\bar{\nu} \text{ [ang. corr.]}$$

Dittmar, Dreiner



ATLAS

## (ii) MSSM

- 2 Higgs doublets  $\xrightarrow{\text{ESB}}$  5 Higgs bosons:  $h, H, A, H^\pm$

- LO: 2 input parameters:  $M_A, \text{tg}\beta = \frac{v_2}{v_1}$

- radiative corrections  $\propto m_t^4 \log \frac{m_{\tilde{\tau}_1} m_{\tilde{\tau}_2}}{m_t^2} \rightarrow \boxed{M_h \lesssim 135 \text{ GeV}}$

Haber  
Carena, ...  
Heinemeyer, ...  
Zhang  
Slavich, ...  
...

- Yukawa couplings:  $\text{tg}\beta \uparrow \Rightarrow g_u^\phi \downarrow \quad g_d^\phi \uparrow \quad g_V^\phi \downarrow$

- LHC:  $gg \rightarrow \phi$  dominant for  $\text{tg}\beta \lesssim 10$   
 $gg \rightarrow \phi b\bar{b}$  dominant for  $\text{tg}\beta \gtrsim 10$

F

$$h \rightarrow \gamma\gamma, b\bar{b}$$

$$H, A \rightarrow \tau^+\tau^-, \mu^+\mu^-$$

$$H^\pm \rightarrow \tau\nu_\tau$$

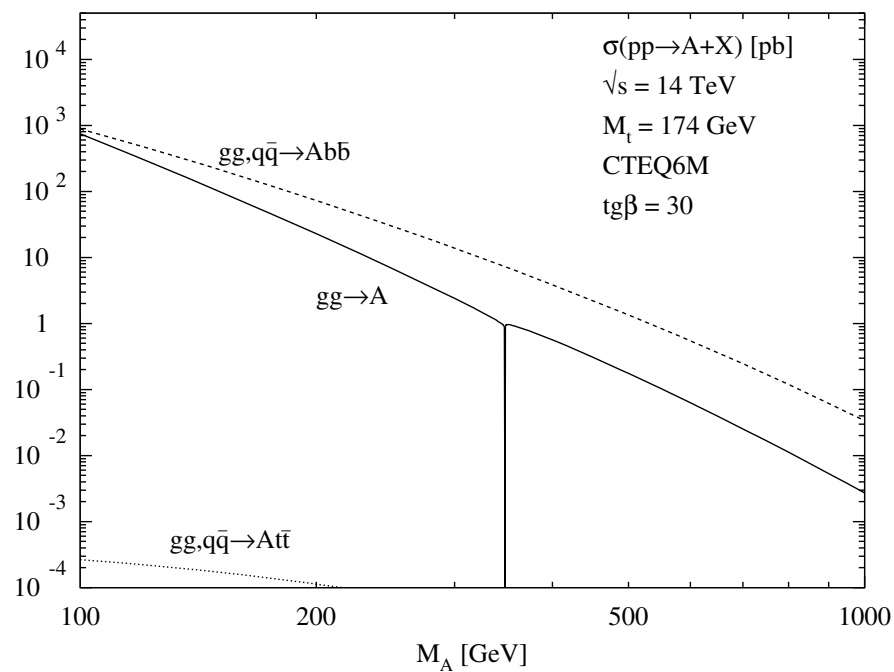
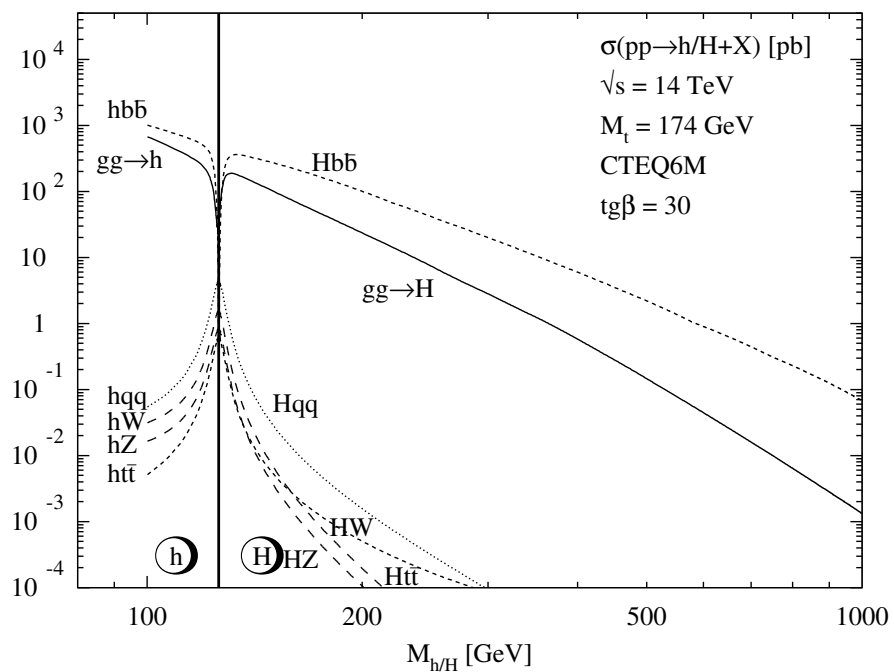
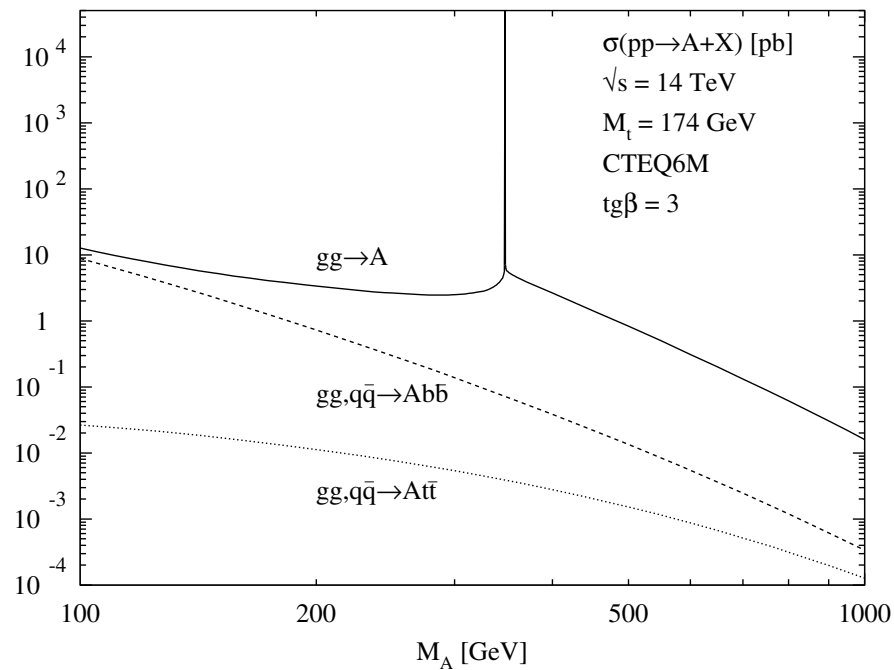
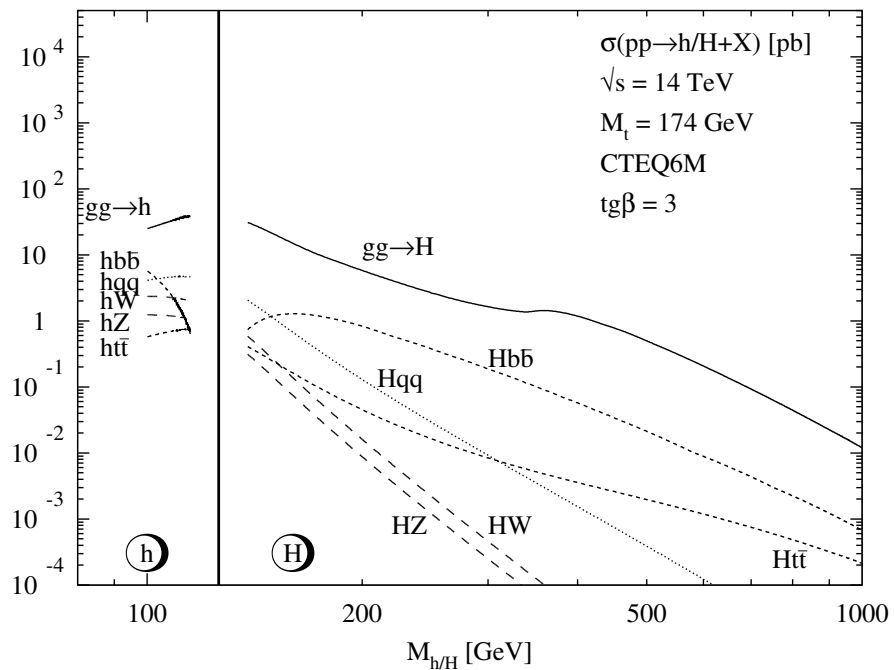
$$\underline{\text{and}} \quad VV \rightarrow h, H \rightarrow \tau^+\tau^-$$

F

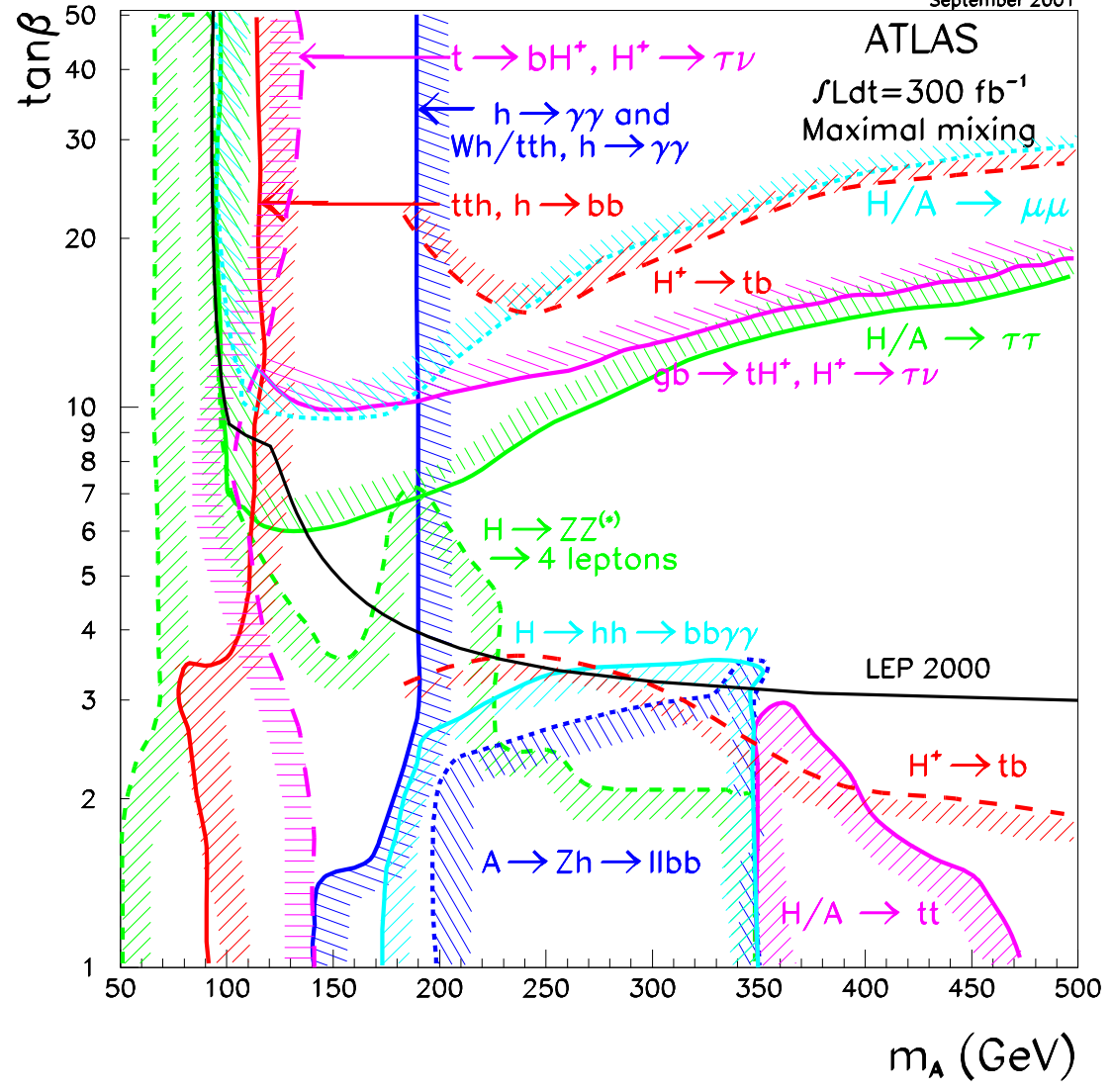
Kauer, ...

- $h \rightarrow b\bar{b}$  in SUSY production

Paige, ...

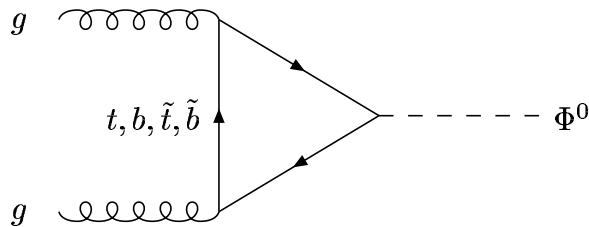


September 2001



## II HIGGS BOSON PRODUCTION @ LHC

(i) Gluon fusion:  $pp \rightarrow gg \rightarrow h/H/A$



- third generation dominant [ $\tilde{t}, \tilde{b}$ :  $m_{\tilde{q}} \lesssim 400$  GeV]

- two-loop QCD corrections:  $\sim 10 \dots 100\%$   
[moderate for large  $\tan\beta \leftarrow b$ -loop]

- NNLO calculated for  $m_t \gg M_\phi \Rightarrow +20\text{--}30\%$

- NNNLO estimated  $m_t \gg M_\phi \Rightarrow$  scale stabilization  
scale dependence:  $\Delta \lesssim 10 - 15\%$

- NNLL resummation:  $+10\%$

- NNLO mass effects calculated  
for  $M_H \lesssim 300$  GeV  $\Rightarrow \mathcal{O}(0.5\%)$

- NLO electroweak corrections:  $-4\% - 6\%$

Georgi,...

Gamberini,...

SDGZ

Dawson, Kauffman

Harlander, Kilgore  
Anastasiou, Melnikov  
Ravindran,...

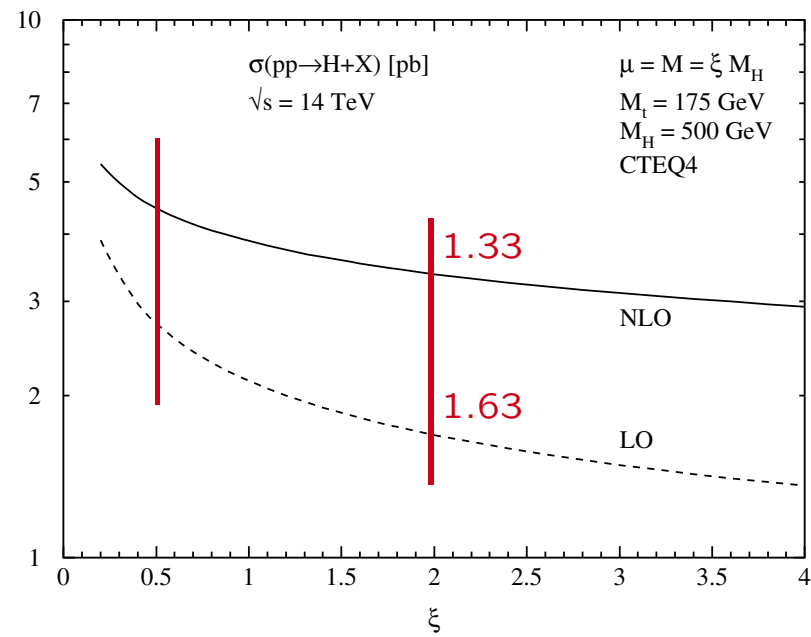
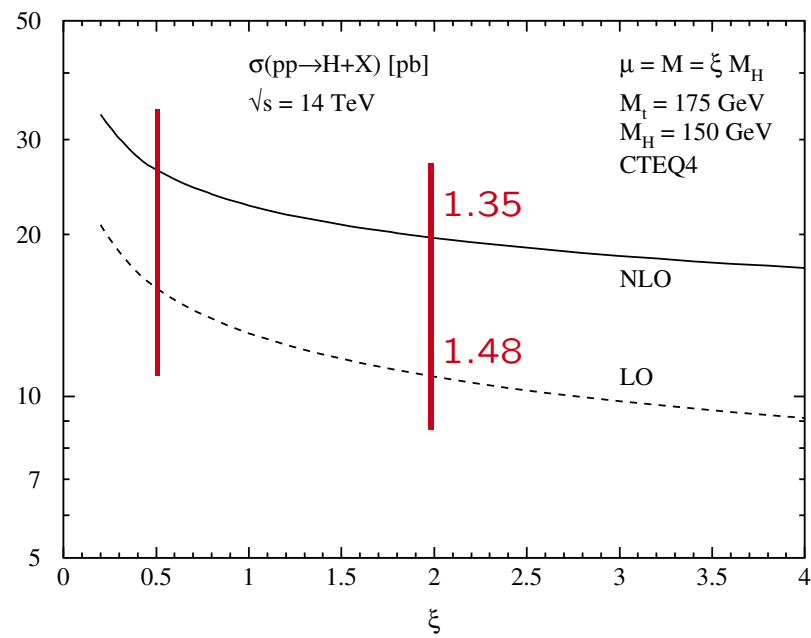
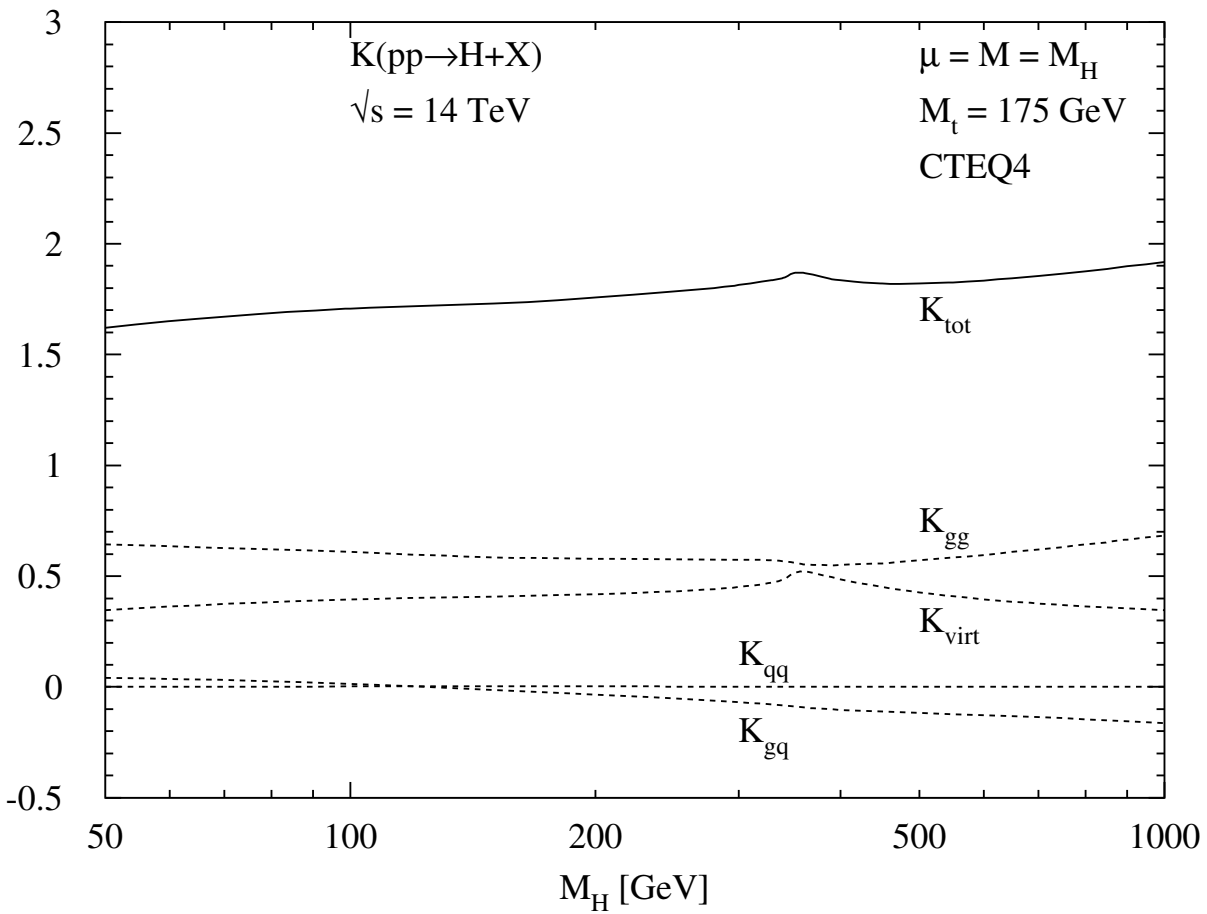
Moch, Vogt  
Ravindran

Catani, De Florian, Grazzini, Nason

Harlander, Ozeren  
Pak, Rogal, Steinhauser  
Marzani, Ball, Del Duca, Forte, Vicini

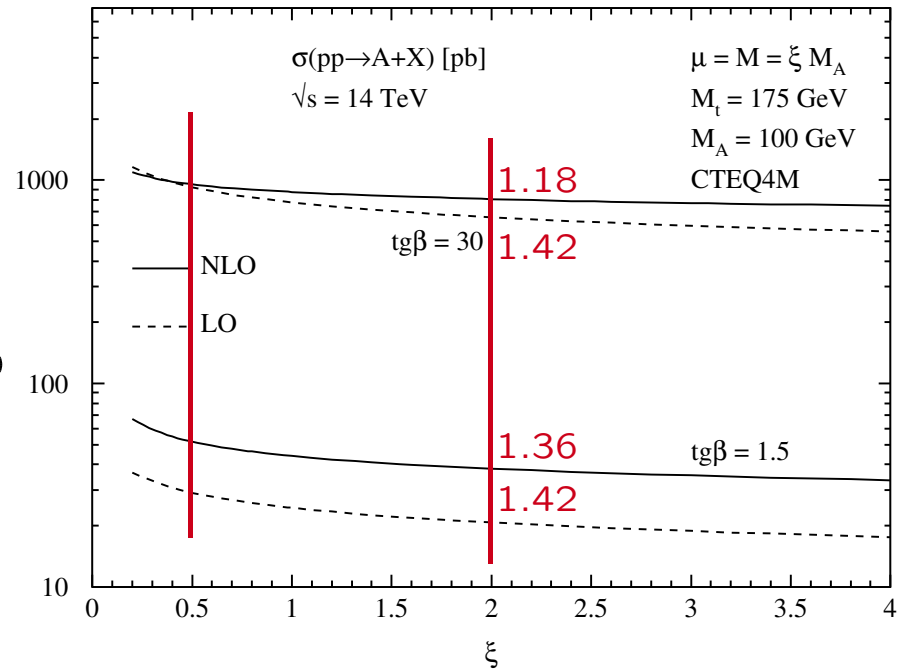
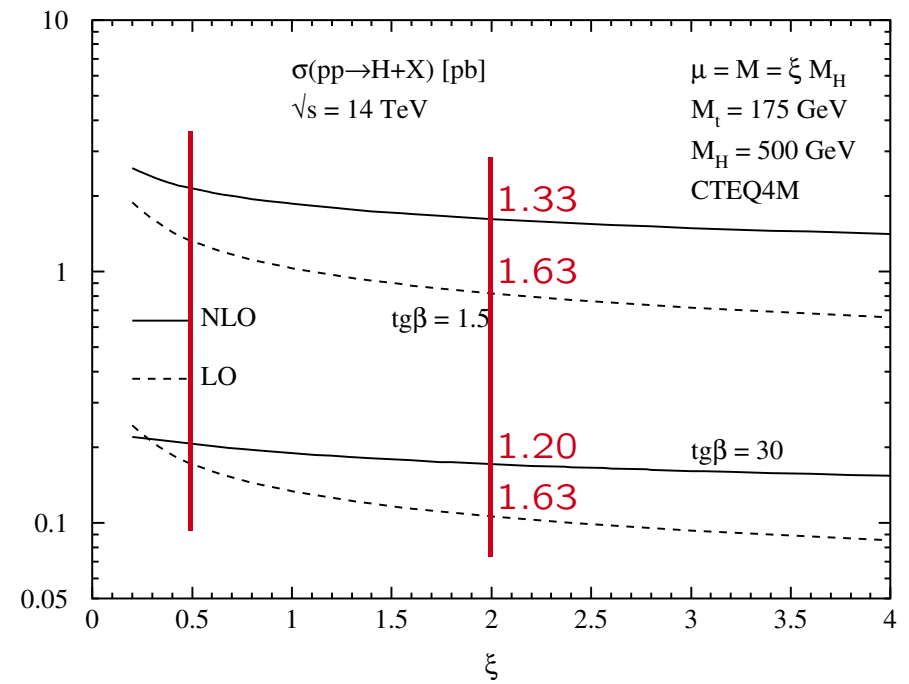
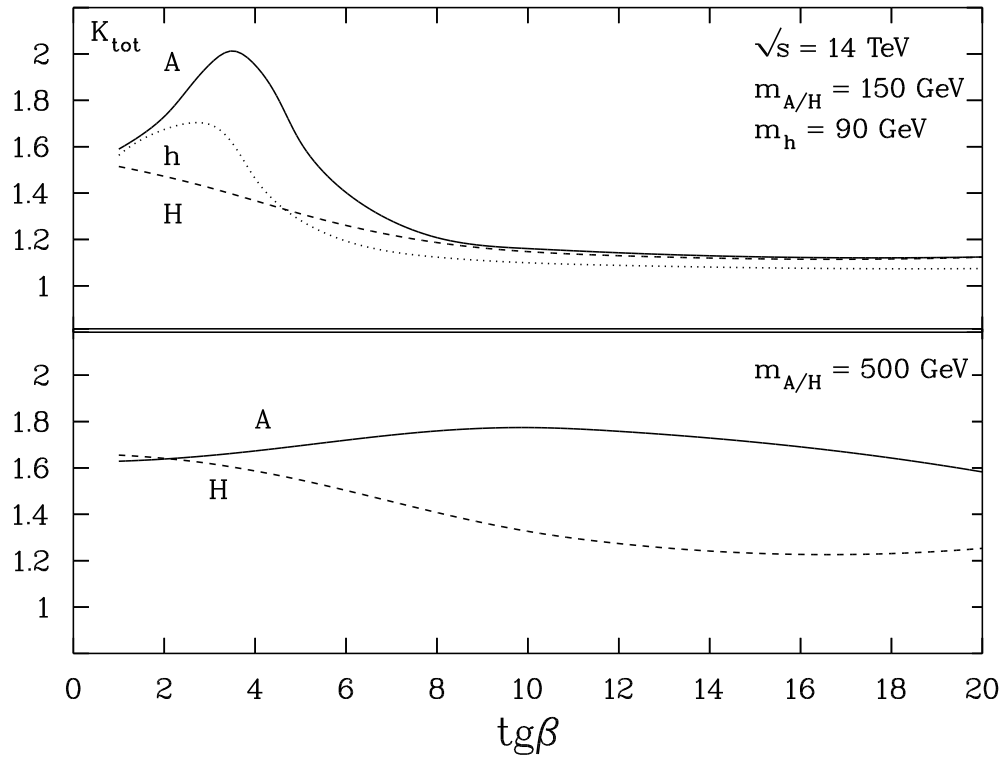
Aglietti,...

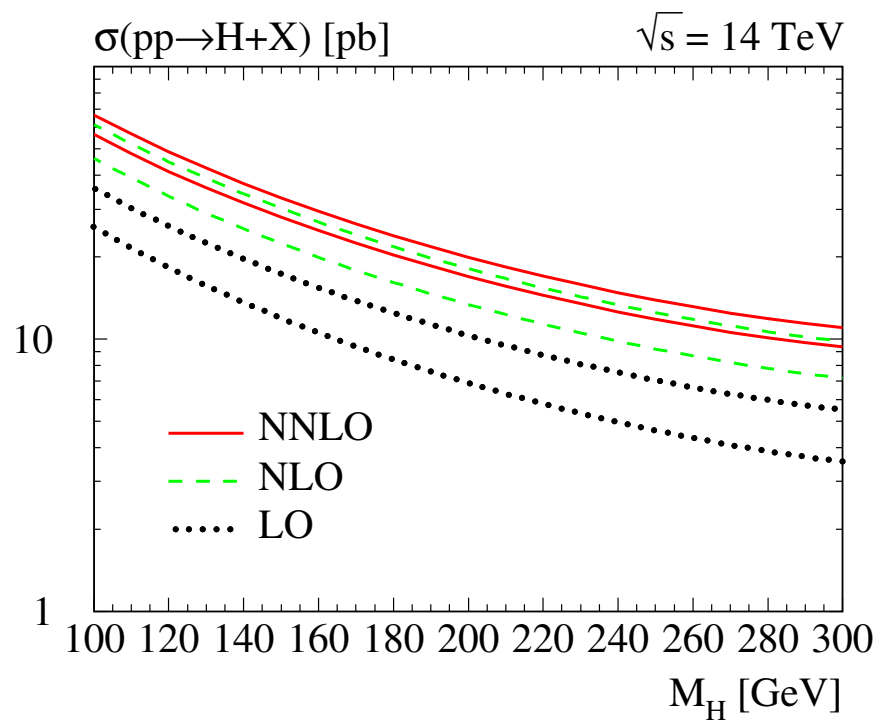
Degrassi, Maltoni  
Actis,...



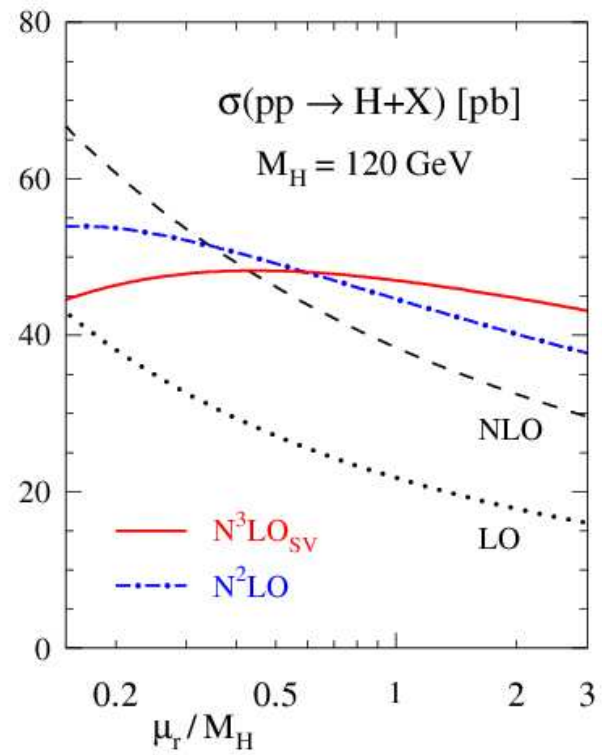
S., Djouadi, Graudenz, Zerwas



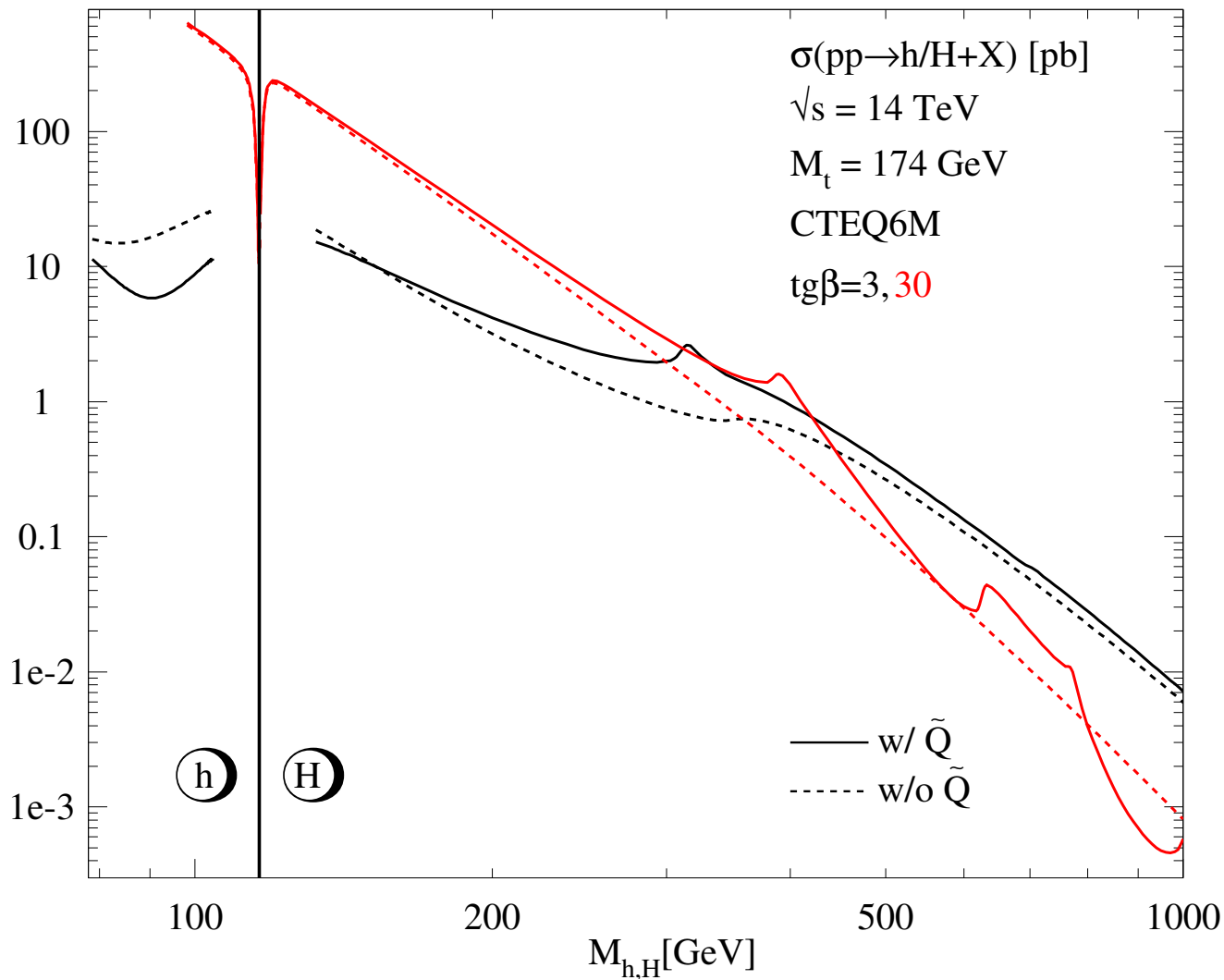




Harlander, Kilgore



Moch, Vogt



Mühlleitner, S.

gluophobic scenario

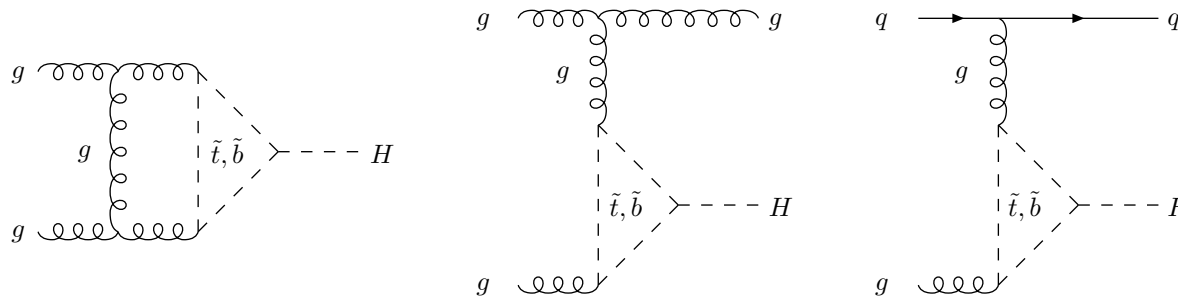
$\text{tg}\beta = 3$ :  $m_{\tilde{t}_1} = 156$  GeV,  $m_{\tilde{t}_2} = 516$  GeV,  $m_{\tilde{b}_1} = 346$  GeV,  $m_{\tilde{b}_2} = 358$  GeV

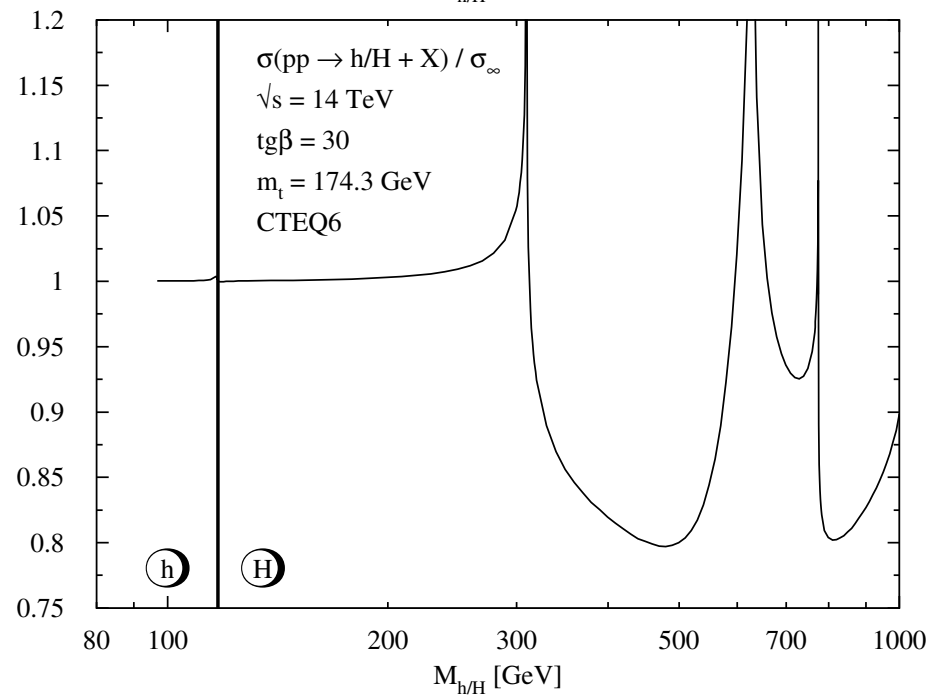
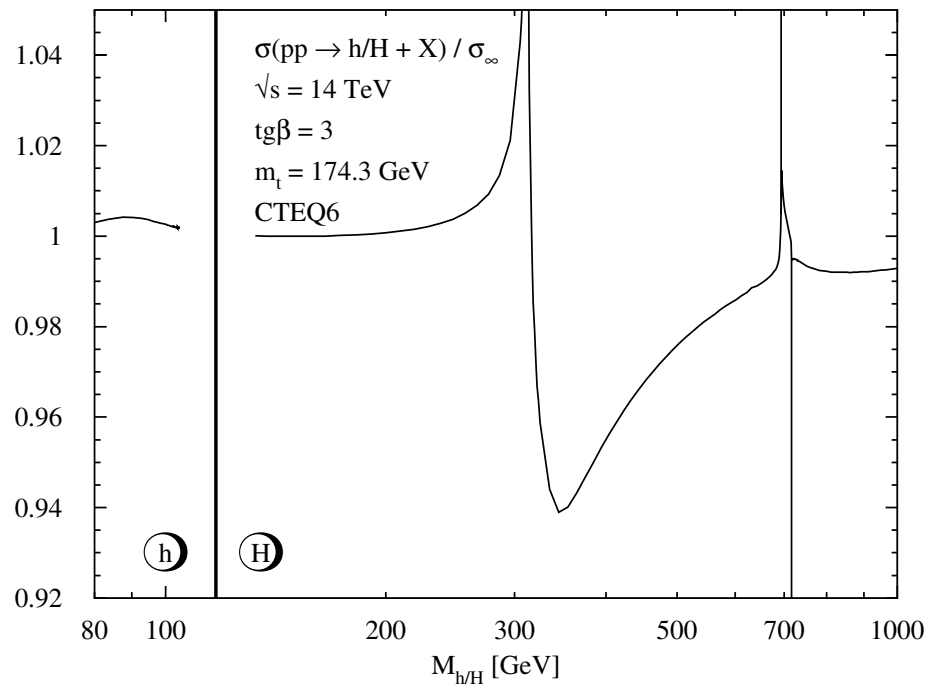
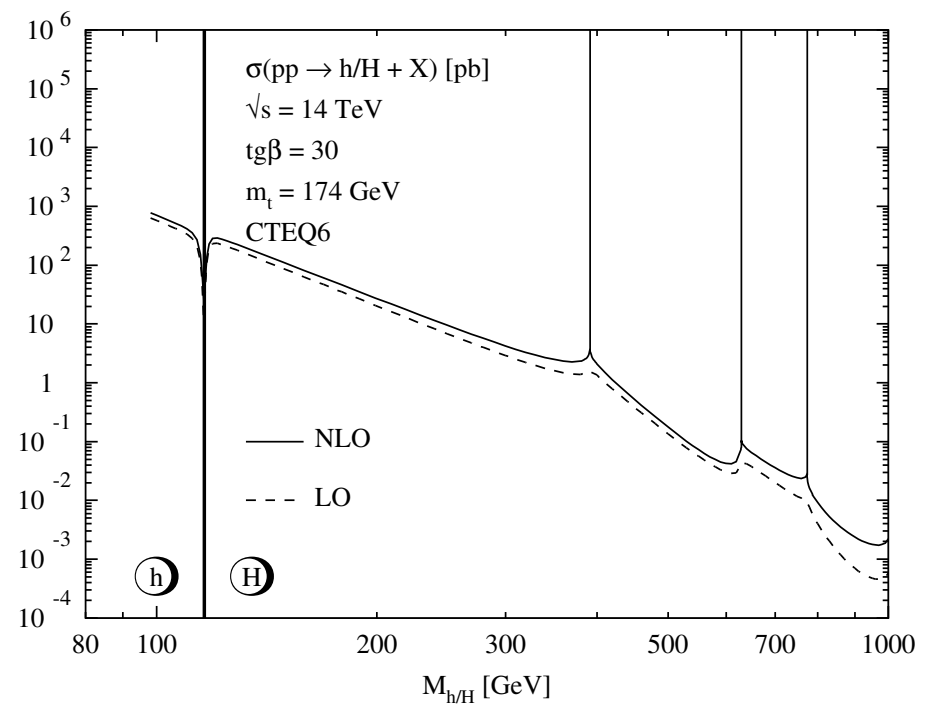
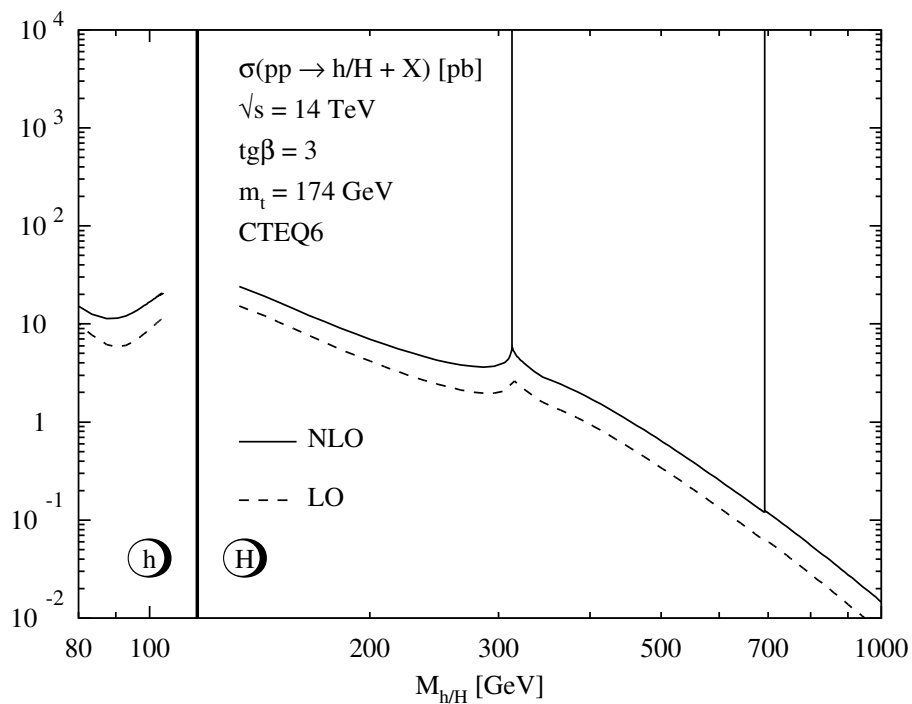
$\text{tg}\beta = 30$ :  $m_{\tilde{t}_1} = 195$  GeV,  $m_{\tilde{t}_2} = 502$  GeV,  $m_{\tilde{b}_1} = 315$  GeV,  $m_{\tilde{b}_2} = 387$  GeV

- QCD corrections to squark loops:

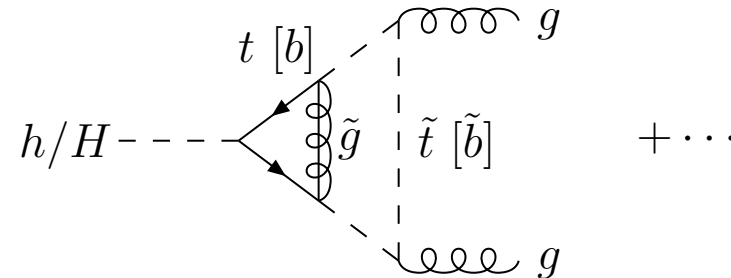
decouple gluino contributions as first step ← adjust renormalization  
 [gluino contribution:  $\mathcal{O}(10\%)$ ]

Harlander, Steinhauser, Hofmann  
 Degrassi, Slavich





genuine SUSY-QCD corrections:

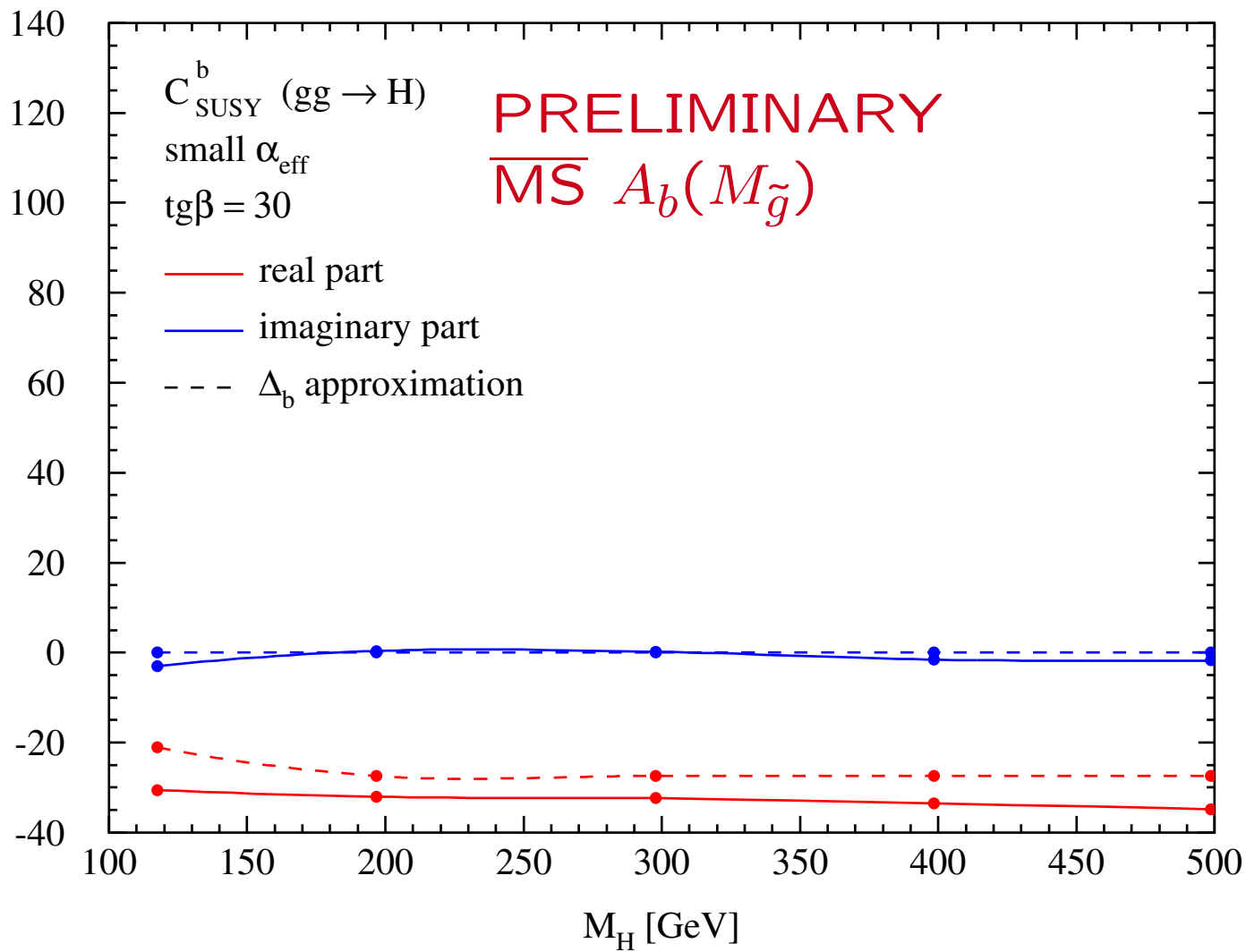


Anastasiou, Beerli, Daleo  
Mühlleitner, Rzehak, S.

$$\sigma_{LO}(pp \rightarrow \phi^0) = \sigma_0^\phi \tau_\phi \frac{d\mathcal{L}^{gg}}{d\tau_\phi}$$

$$\sigma_0^{h/H} = \frac{G_F \alpha_s^2}{288 \sqrt{2} \pi} \left| \sum_Q g_Q^{h/H} A_Q^{h/H}(\tau_Q) + \sum_{\tilde{Q}} g_{\tilde{Q}}^{h/H} A_{\tilde{Q}}^{h/H}(\tau_{\tilde{Q}}) \right|^2 \quad \sigma_0^A = \frac{G_F \alpha_s^2}{128 \sqrt{2} \pi} \left| \sum_Q g_Q^A A_Q^A(\tau_Q) \right|^2$$

- numerical analysis:  $A_Q^{h/H}(\tau_Q) \rightarrow A_Q^{h/H}(\tau_Q) \left[ 1 + C_{SUSY}^Q \frac{\alpha_s}{\pi} \right]$   
 → M. Mühlleitner



Mühlleitner, Rzehak, S.

## SUSY-QCD Corrections to $b\bar{b}\phi^0$

$[\Delta \lesssim 1\%]$

$$\mathcal{L}_{eff} = -\lambda_b \bar{b}_R \left[ \phi_1^0 + \frac{\Delta_b}{\text{tg}\beta} \phi_2^{0*} \right] b_L + h.c. \quad \text{valid to all orders in } \Delta_b$$

$$\begin{aligned} = & -m_b \bar{b} \left[ 1 + i\gamma_5 \frac{G^0}{v} \right] b - \frac{m_b/v}{1 + \Delta_b} \bar{b} \left[ g_b^h \left( 1 - \frac{\Delta_b}{\text{tg}\alpha \text{tg}\beta} \right) h \right. \\ & \left. + g_b^H \left( 1 + \Delta_b \frac{\text{tg}\alpha}{\text{tg}\beta} \right) H - g_b^A \left( 1 - \frac{\Delta_b}{\text{tg}^2\beta} \right) i\gamma_5 A \right] b \end{aligned}$$

$$\Delta_b = \Delta_b^{QCD(1)} + \Delta_b^{elw(1)}$$

$$\Delta_b^{QCD(1)} = \frac{2}{3} \frac{\alpha_s(\mu_R)}{\pi} M_{\tilde{g}} \mu \text{tg}\beta I(m_{\tilde{b}_1}^2, m_{\tilde{b}_2}^2, M_{\tilde{g}}^2)$$

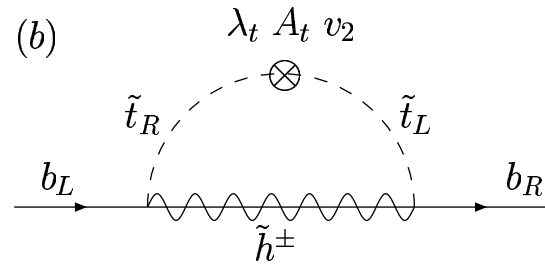
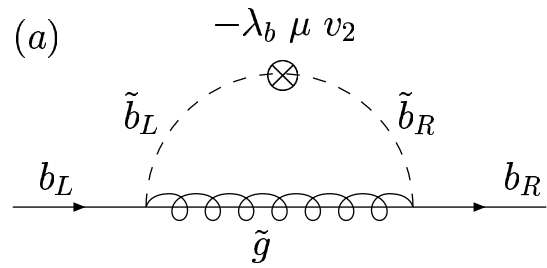
$$\Delta_b^{elw(1)} = \frac{\lambda_t^2(\mu_R)}{(4\pi)^2} \mu A_t \text{tg}\beta I(m_{\tilde{t}_1}^2, m_{\tilde{t}_2}^2, \mu^2)$$

$$I(a, b, c) = -\frac{ab \log \frac{a}{b} + bc \log \frac{b}{c} + ca \log \frac{c}{a}}{(a-b)(b-c)(c-a)}$$

$\Rightarrow$  resummed Yukawa couplings

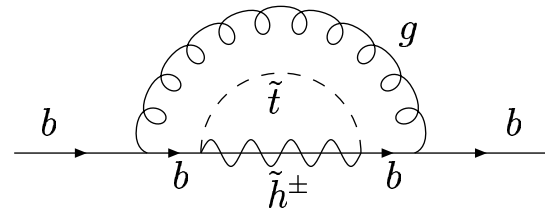
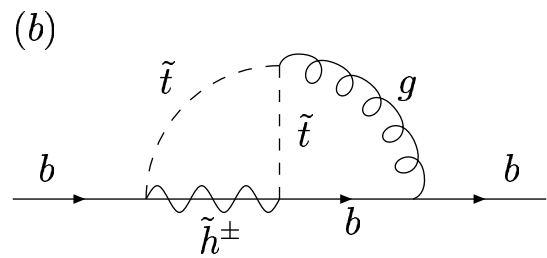
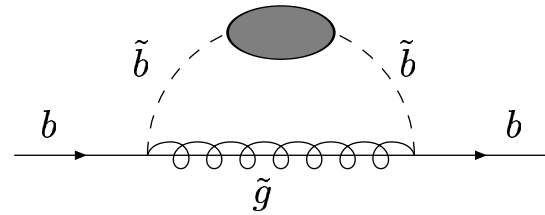
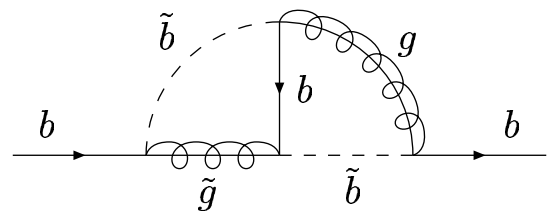
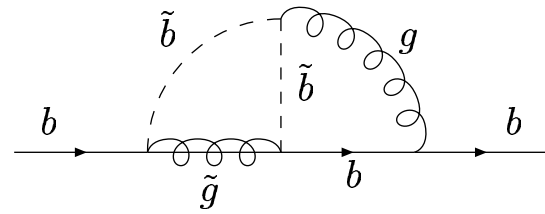
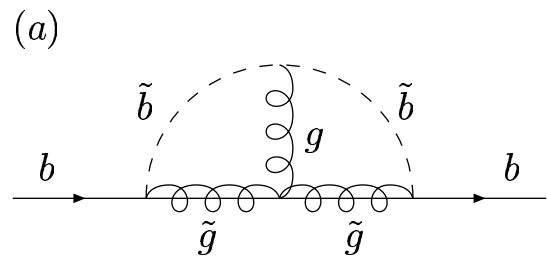
Carena, Garcia, Nierste, Wagner  
Guasch, Häfliger, S.





• LET:  $v_2 \rightarrow \sqrt{2}\phi_2^{0*}$

Ellis,...  
Shifman,...



- 2-loop self-energies @ vanishing momentum
- dimensional regularization in  $n = 4 - 2\epsilon$  dimensions
- integration by parts: reduction to 1-point functions

$$A_0(m) = \int \frac{d^n k}{(2\pi)^n} \frac{1}{k^2 - m^2}$$

and one 2-loop master integral

$$T_{134}(m_1, m_3, m_4) = \int \frac{d^n k}{(2\pi)^n} \frac{d^n q}{(2\pi)^n} \frac{1}{(k^2 - m_1^2)[(k - q)^2 - m_3^2](q^2 - m_4^2)}$$

- $\alpha_s, \lambda_t$ :  $\overline{\text{MS}}$  scheme [5 flavours]  
masses,  $A_t$ : on-shell
- dim. reg. violates SUSY: anomalous counter terms

$$\hat{g}_s = g_s \left[ 1 + \left( \frac{C_A}{6} - \frac{C_F}{8} \right) \frac{\alpha_s}{\pi} \right]$$

$$\lambda_{Hbb} = \lambda_{H\tilde{b}\tilde{b}} \left[ 1 + \frac{C_F}{4} \frac{\alpha_s}{\pi} \right] = \lambda_{\tilde{H}\tilde{b}\tilde{b}} \left[ 1 + \frac{3}{8} C_F \frac{\alpha_s}{\pi} \right]$$

Martin, Vaughn

## Limits

- $m_t^2 \ll m_{\tilde{g}}^2 = m_{\tilde{b}_i}^2 = \mu^2 = m_{\tilde{t}_i}^2 \equiv M^2$ :

$$\Delta_b^{QCD(1)} = \frac{C_F \alpha_s(\mu_R)}{4\pi} \text{tg}\beta$$

$$\Delta_b^{QCD(2)} = \frac{\alpha_s}{\pi} \left\{ \frac{C_A}{3} + C_F + \frac{N_F + 1}{4} + \underbrace{\frac{1}{6} \log \frac{M^2}{m_t^2}}_{\rightarrow \alpha_s^{(6)}} + \beta_0^L \log \frac{\mu_R^2}{M^2} \right\} \Delta_b^{QCD(1)}$$

$$\Delta_b^{elw(1)} = \frac{1}{2} \frac{\lambda_t^2(\mu_R) A_t \text{tg}\beta}{(4\pi)^2 M}$$

$$\Delta_b^{elw(2)} = C_F \frac{\alpha_s}{\pi} \left\{ \frac{7}{4} + \underbrace{\frac{3}{2} \log \frac{\mu_R^2}{m_t M}}_{\lambda_{t/b} \rightarrow \lambda_{\tilde{h}^\pm, MO}} \right\} \Delta_b^{elw(1)}$$

Noth, S.

$$\lambda_{t/b}(\mu_R) = \lambda_{\tilde{h}^\pm, MO}(\mu_R) \left\{ 1 - C_F \frac{\alpha_s}{\pi} \left[ \frac{3}{8} \log \frac{\mu_R^2}{m_{\tilde{g}}^2} + \frac{9}{16} \right] \right\} \quad [\mu_R \ll m_{\tilde{g}}]$$

- $m_t^2, m_{\tilde{b}_i}^2, \mu^2, m_{\tilde{t}_i}^2 \ll m_{\tilde{g}}^2$ :

$$\Delta_b^{QCD(1)} = \frac{C_F \alpha_s(\mu_R) \mu \text{tg}\beta}{2 \pi m_{\tilde{g}}} \left\{ -\log \frac{m_{\tilde{g}}^2}{m_{\tilde{b}_2}^2} + \frac{m_{\tilde{b}_1}^2}{m_{\tilde{b}_2}^2 - m_{\tilde{b}_1}^2} \log \frac{m_{\tilde{b}_2}^2}{m_{\tilde{b}_1}^2} \right\}$$

$$\Delta_b^{QCD(2)} = \frac{\alpha_s}{\pi} \left\{ \frac{4}{3} C_A + C_F \left[ \log \frac{m_{\tilde{g}}^2}{m_{\tilde{b}_2}^2} - \frac{m_{\tilde{b}_1}^2}{m_{\tilde{b}_2}^2 - m_{\tilde{b}_1}^2} \log \frac{m_{\tilde{b}_2}^2}{m_{\tilde{b}_1}^2} + \frac{5}{2} \right] - \frac{N_F + 1}{2} \right.$$

$$\left. + \frac{1}{6} \log \frac{m_{\tilde{g}}^2}{m_t^2} + \frac{1}{24} \sum_{\tilde{q}} \log \frac{m_{\tilde{g}}^2}{m_{\tilde{q}}^2} + \beta_0^L \log \frac{\mu_R^2}{m_{\tilde{g}}^2} \right\} \Delta_b^{QCD(1)}$$

$\xrightarrow{\alpha_s^{(SUSY)}}$

$$\Delta_b^{elw(2)} = C_F \frac{\alpha_s}{\pi} \left\{ \frac{23}{8} + \frac{3}{2} \log \frac{\mu_R^2}{m_t m_{\tilde{g}}} \right\} \Delta_b^{elw(1)}$$

$\lambda_{t/b} \rightarrow \lambda_{t/b, MO}^{\tilde{h}^\pm}$

Noth, S.

small  $\alpha_{eff}$  scenario [modified]

$$\text{tg}\beta = 30$$

$$M_{\tilde{Q}} = 800 \text{ GeV}$$

$$M_{\tilde{g}} = 1000 \text{ GeV} \quad \leftarrow$$

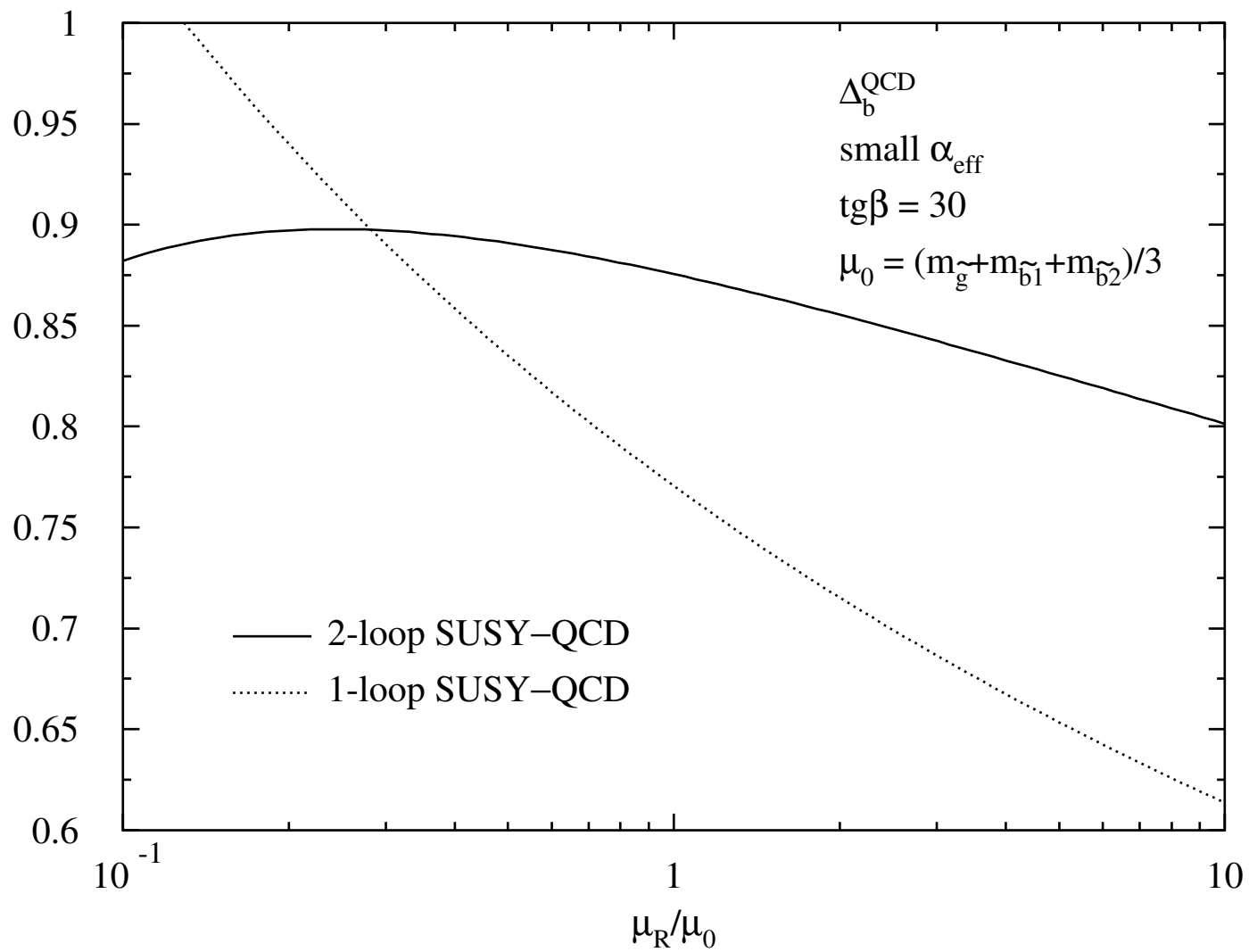
$$M_2 = 500 \text{ GeV}$$

$$A_b = A_t = -1.133 \text{ TeV}$$

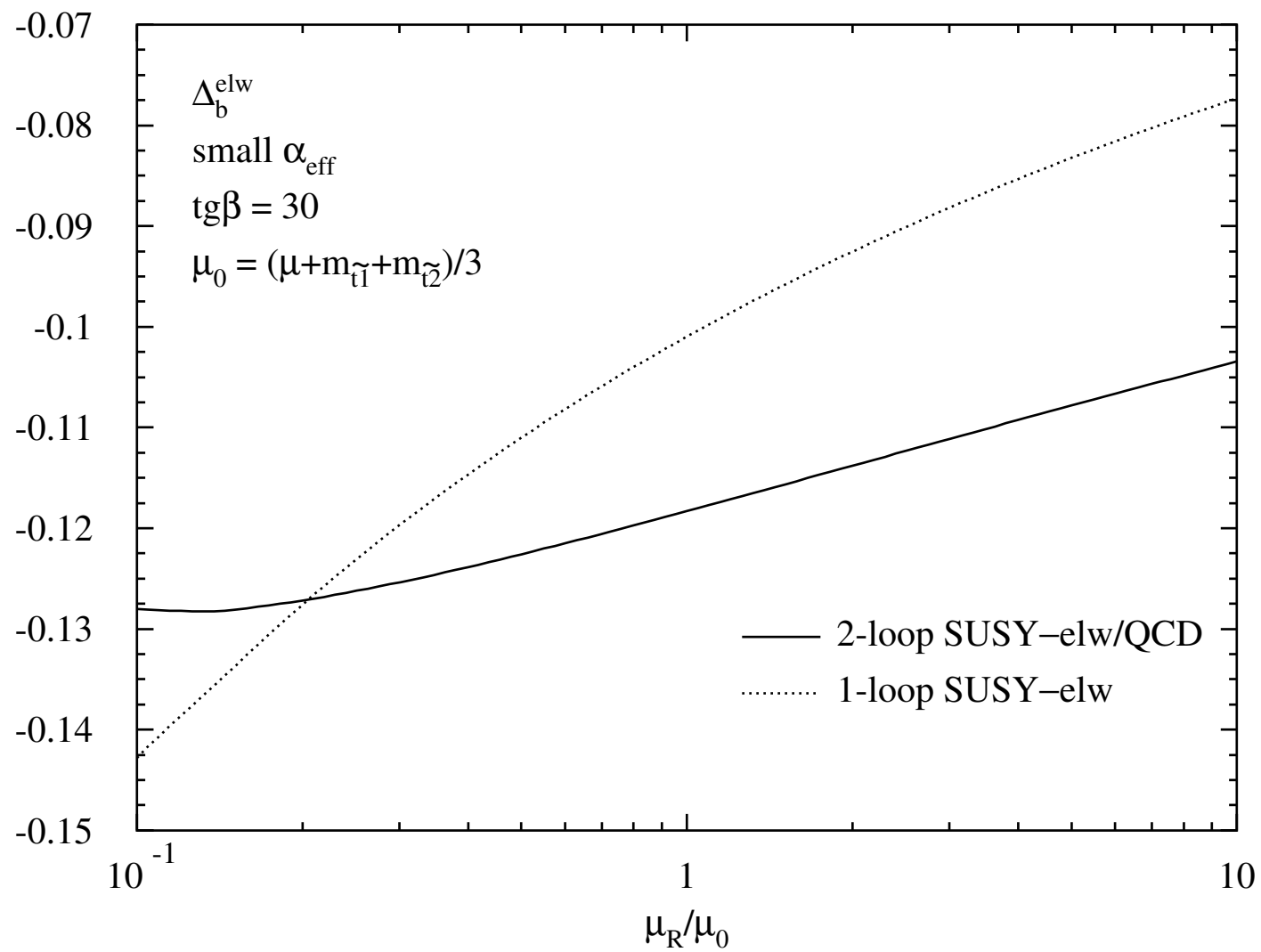
$$\mu = 2 \text{ TeV}$$

$$m_{\tilde{t}_1} = 679 \text{ GeV} \quad m_{\tilde{t}_2} = 935 \text{ GeV}$$

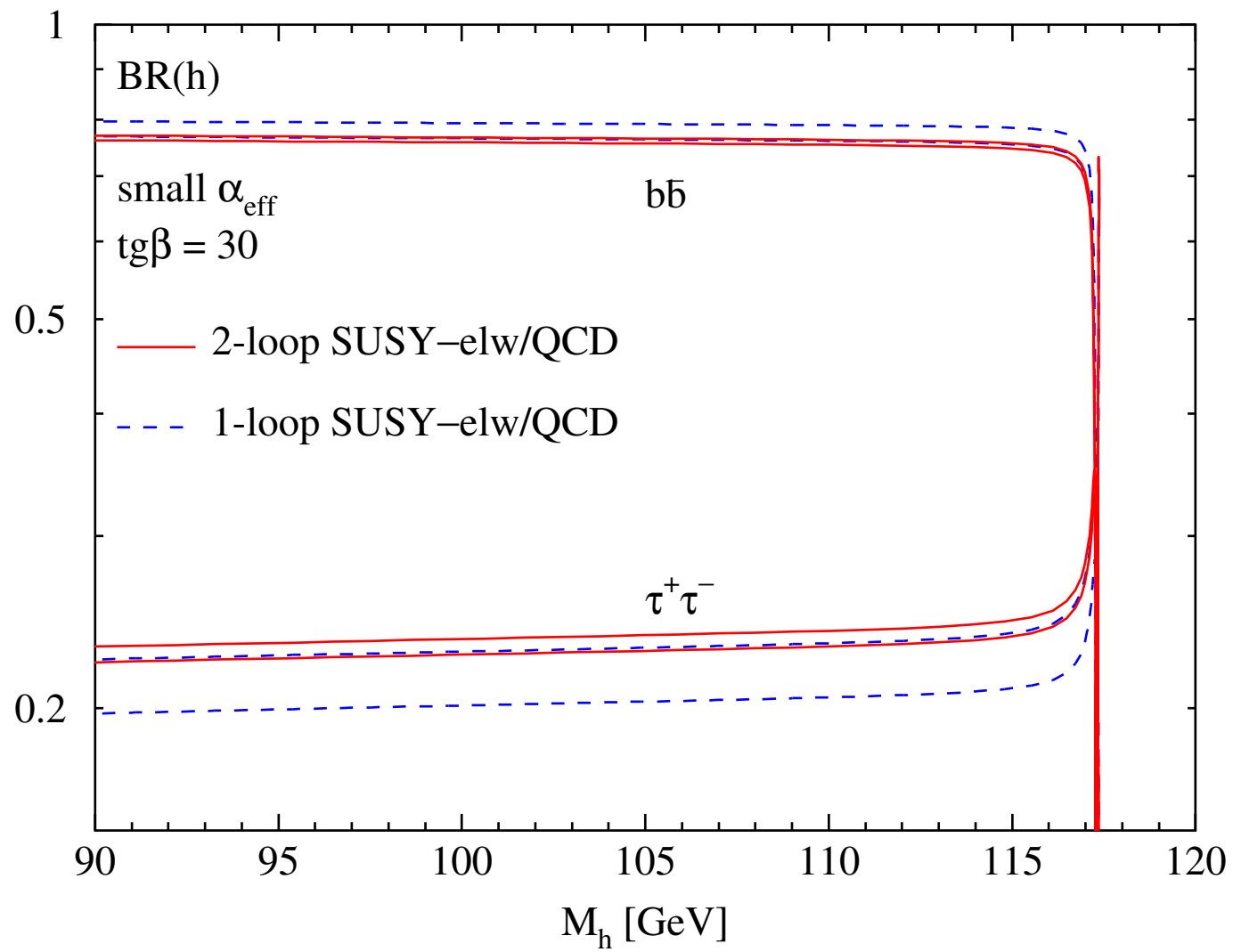
$$m_{\tilde{b}_1} = 601 \text{ GeV} \quad m_{\tilde{b}_2} = 961 \text{ GeV}$$



Noth, S.

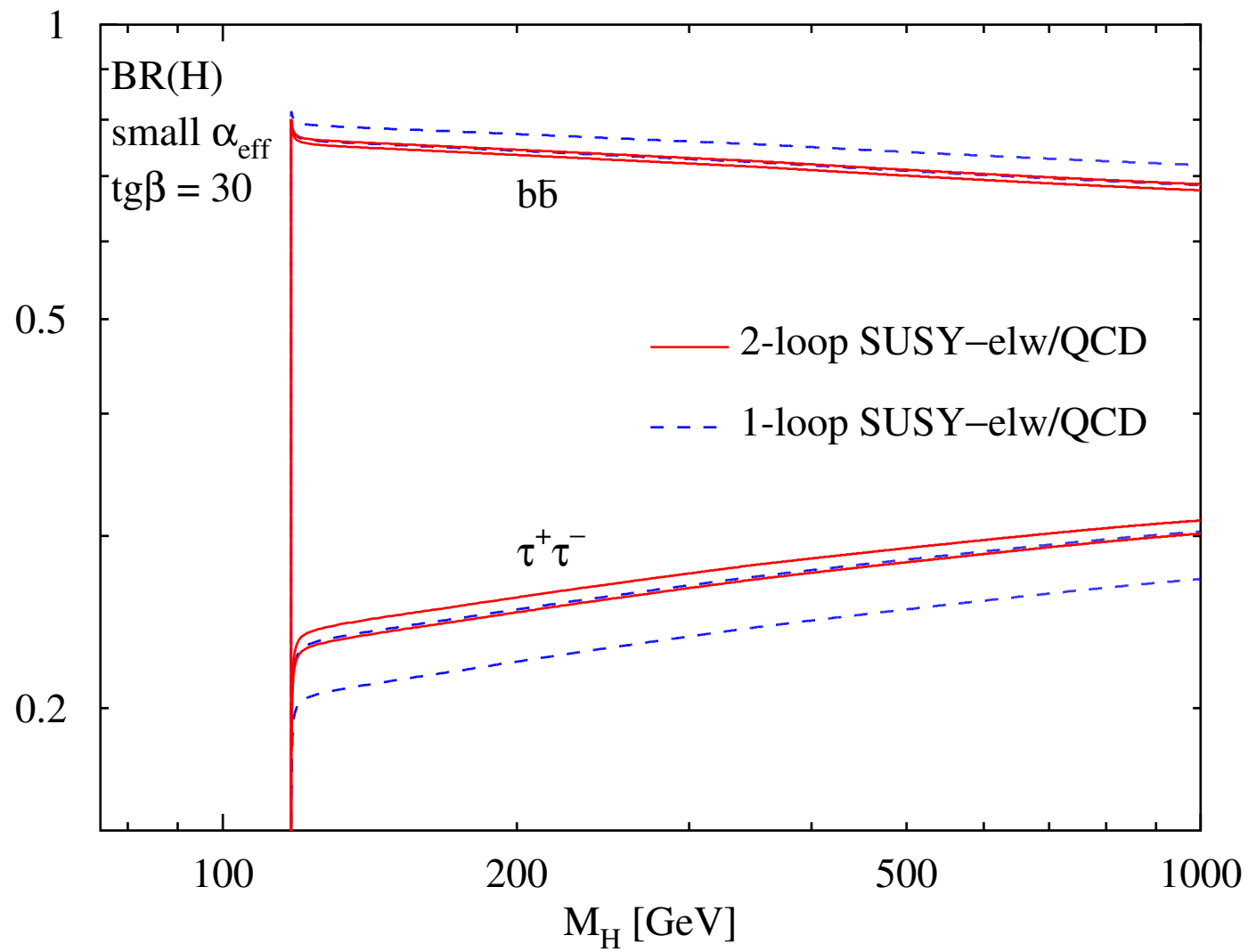


Noth, S.

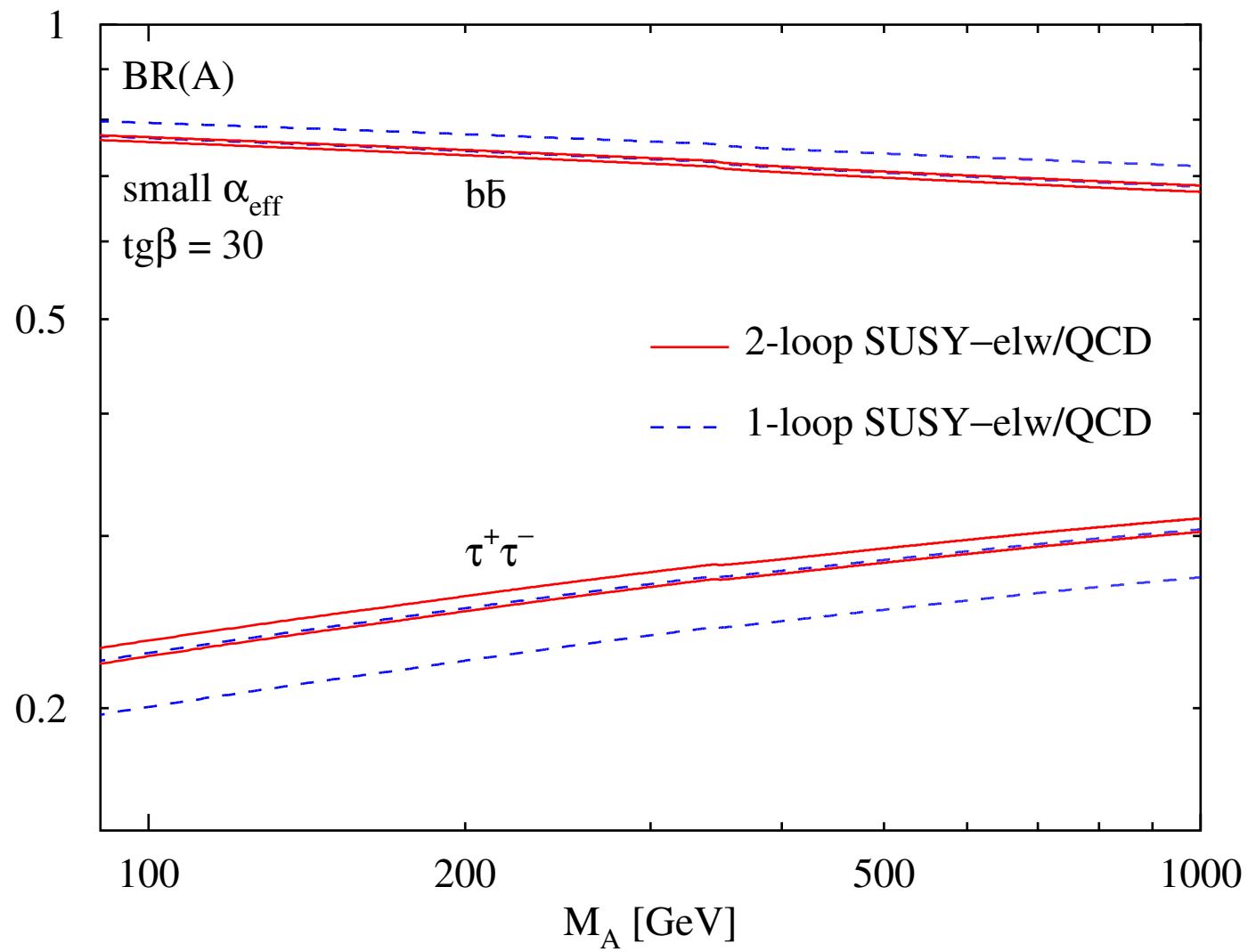


Noth, S.





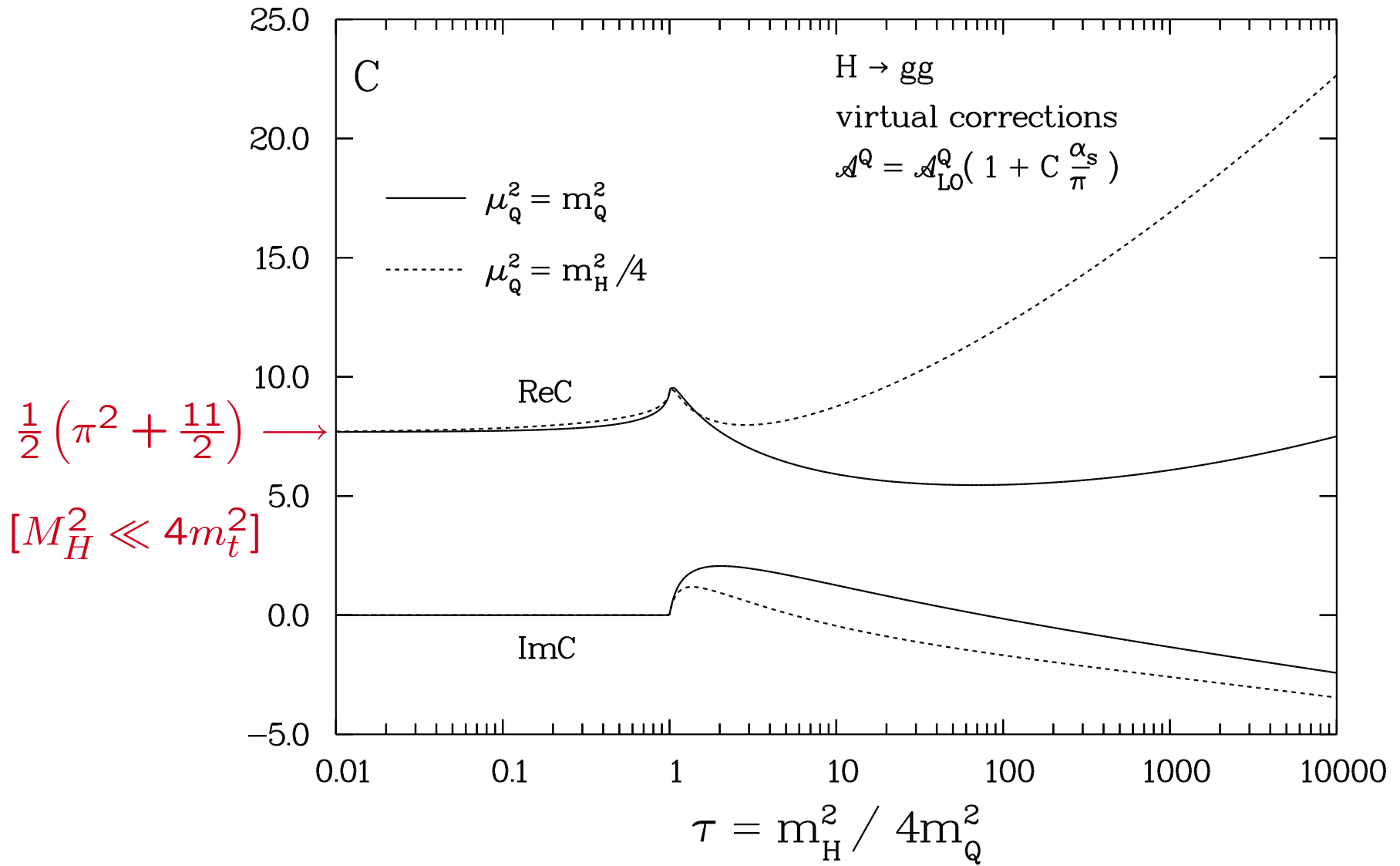
Noth, S.



Noth, S.

## HIGLU

- LHAPDF ✓
- $M_b \leftrightarrow \bar{m}_b(\mu)$   
[ $\mu \sim M_H$  disfavoured!] ✓
- distributions:  $p_T$  ( $LO$ ) ✓  
 $y$  ( $NLO$ ) takes time...  
 $p_T$  ( $NLO$ ) takes more time...
- electroweak corrections ✓
- NNLO, NNLL corrections takes (much?) more time...
- MSSM:  $\sigma_{NLO} = g_t^2 \sigma_{tt}^{SM} + g_t g_b \sigma_{tb}^{SM} + g_b^2 \sigma_{bb}^{SM}$   
 $\sigma_{(N)NLO} = \sigma_{NLO} + g_t^2 \sigma_{tt}^{LO} \Delta K_{NNLO}$
- $\tilde{Q}$  loops ✓
- SUSY-QCD corrections ???



# V SUMMARY

- Higgs boson searches @ LHC major endeavours
- LHC will find at least one Higgs boson [light  $h$ ]
- most (SUSY-)QCD and electroweak corrections known  
⇒ large corrections to gluon fusion  
remaining theoretical uncertainties:  $\sim 100\% \longrightarrow \lesssim 10 - 15\%$
- HIGLU [upgraded], HggTotal, HNNLO, ggh@NNLO  
Anastasiou, . . .  
De Florian, Grazzini  
Harlander, Kilgore
- close collaboration of experimentalists and theorists necessary

*BACKUP SLIDES*

## SPS 5

$$\operatorname{tg}\beta = 5$$

$$\mu = 639.8 \text{ GeV}$$

$$A_t = -1671.4 \text{ GeV}$$

$$A_b = -905.6 \text{ GeV}$$

$$m_{\tilde{g}} = 710.3 \text{ GeV}$$

$$m_{\tilde{q}_L} = 535.2 \text{ GeV}$$

$$m_{\tilde{b}_R} = 620.5 \text{ GeV}$$

$$m_{\tilde{t}_R} = 360.5 \text{ GeV}$$

$$\longrightarrow m_{\tilde{t}_1} = 230.4 \text{ GeV}, m_{\tilde{t}_2} = 637.8 \text{ GeV}$$

## SPS 1b

$$\text{tg}\beta = 30$$

$$\mu = 495.6 \text{ GeV}$$

$$A_t = -729.3 \text{ GeV}$$

$$A_b = -987.4 \text{ GeV}$$

$$m_{\tilde{g}} = 916.1 \text{ GeV}$$

$$m_{\tilde{q}_L} = 762.5 \text{ GeV}$$

$$m_{\tilde{b}_R} = 780.3 \text{ GeV}$$

$$m_{\tilde{t}_R} = 670.7 \text{ GeV}$$

$$\longrightarrow m_{\tilde{b}_1} = 745.8 \text{ GeV}, m_{\tilde{b}_2} = 798.9 \text{ GeV}$$



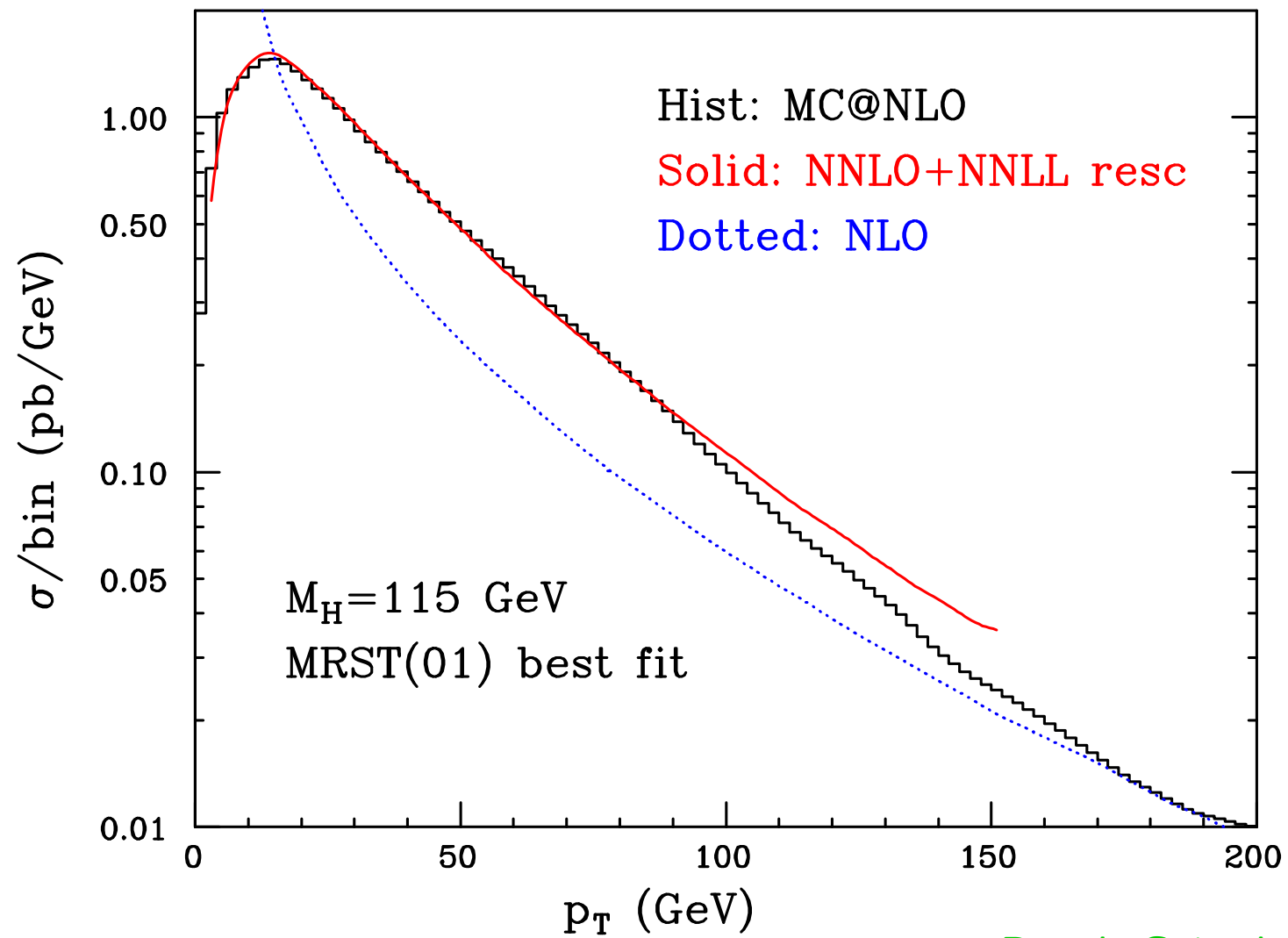
• SUSY decays:  $\phi^0 \rightarrow \chi_1^0 \chi_1^0$  [LSP]  $\Rightarrow$  invisible Higgs  $\rightarrow \cancel{E}_T$  if  $p_{T\phi} > 0$   
 $\Rightarrow gg \rightarrow \phi^0 g$  dominant

NLO corrections [ $m_t \gg M_\phi$ ]: 60–80%

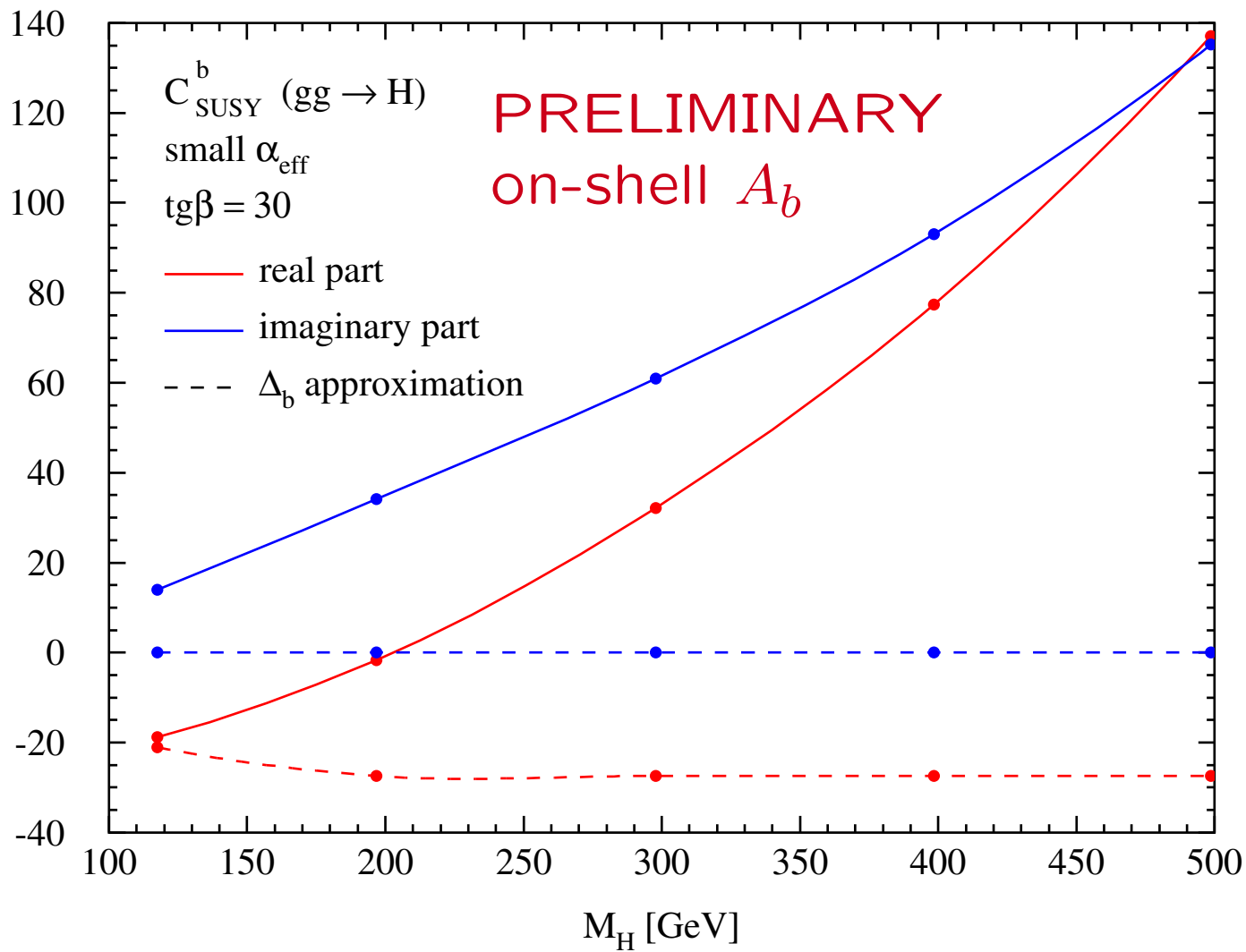
$\rightarrow$  resummation:  $\Delta \lesssim 15\%$

Schmidt  
de Florian, ...  
Ravindran, ...

Kauffman  
Balazs, Yuan  
Bozzi, ...

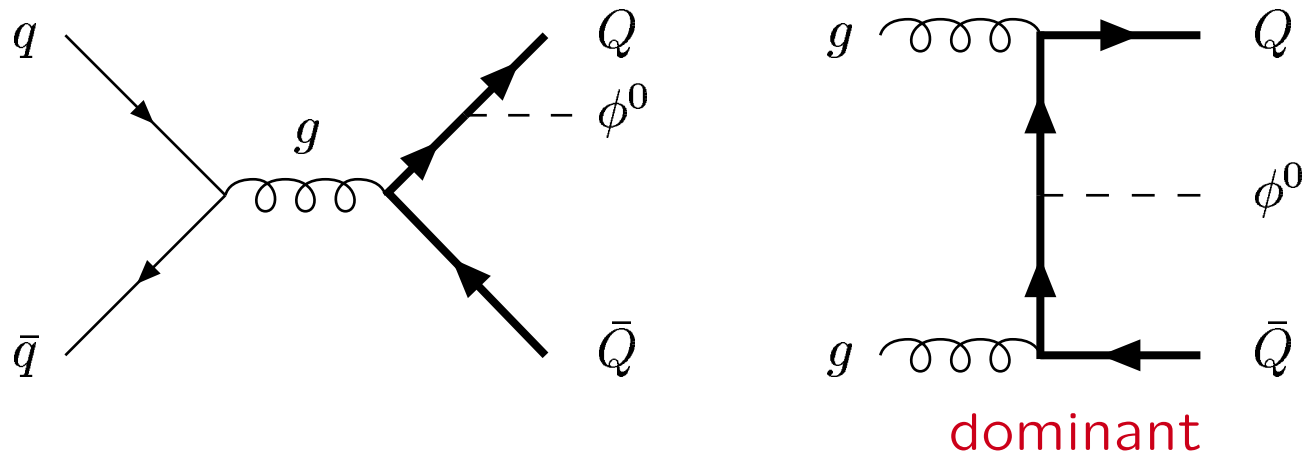


Bozzi, Catani, de Florian, Grazzini  
Frixione [MC@NLO]



Mühlleitner, Rzehak, S.

(iv) Bremsstrahlung:  $pp \rightarrow t\bar{t}/b\bar{b} + h/H/A$

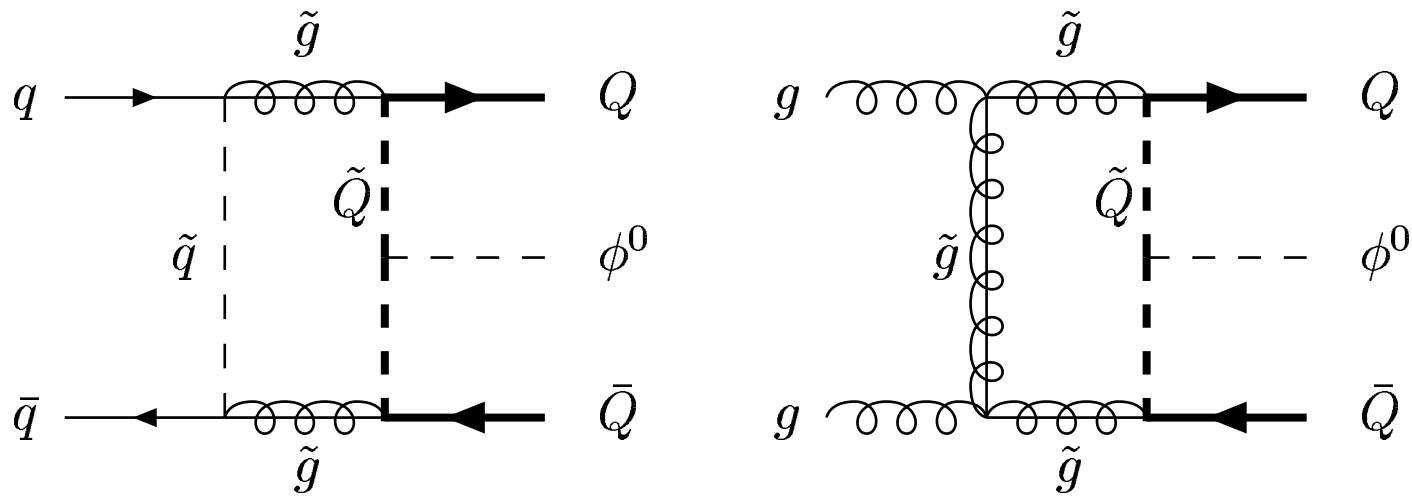


Kunszt  
Gunion  
Marciano, Paige

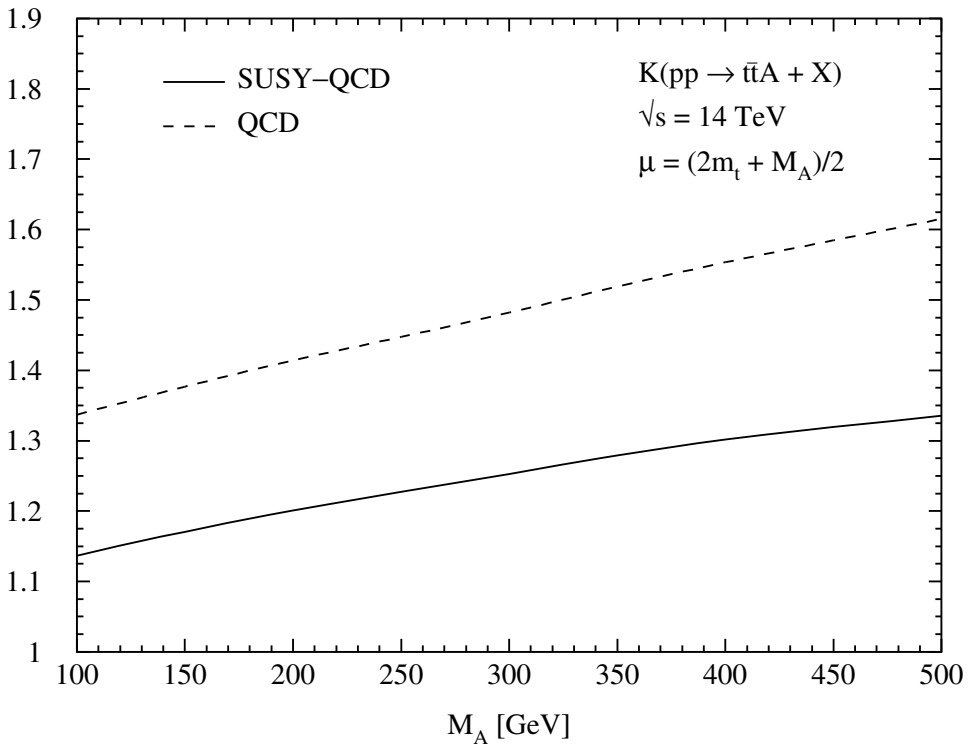
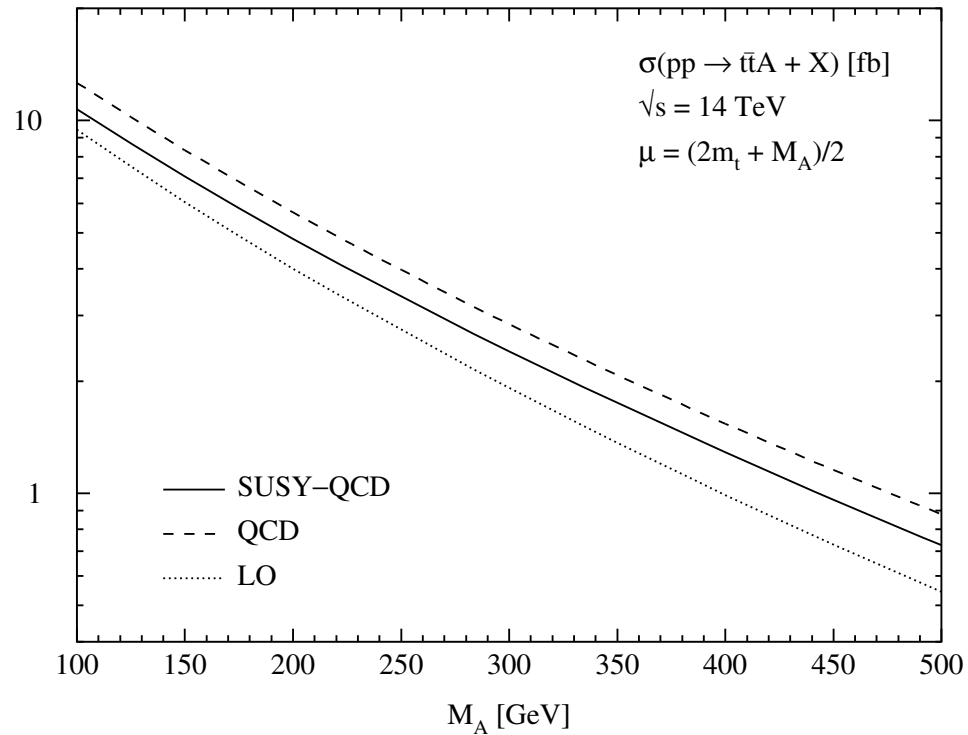
- possibility to measure top Yukawa cplg.
- $b\bar{b} + H/A$  dominant for large  $\tan\beta$  → M. Krämer
- measurement of  $\tan\beta$
- $t\bar{t}h$ : SUSY-QCD corrections computed

Peng, Wen-Gan, Hong-Shen,  
Ren-You, Liang  
Rauch, Hollik

## SUSY-QCD Corrections

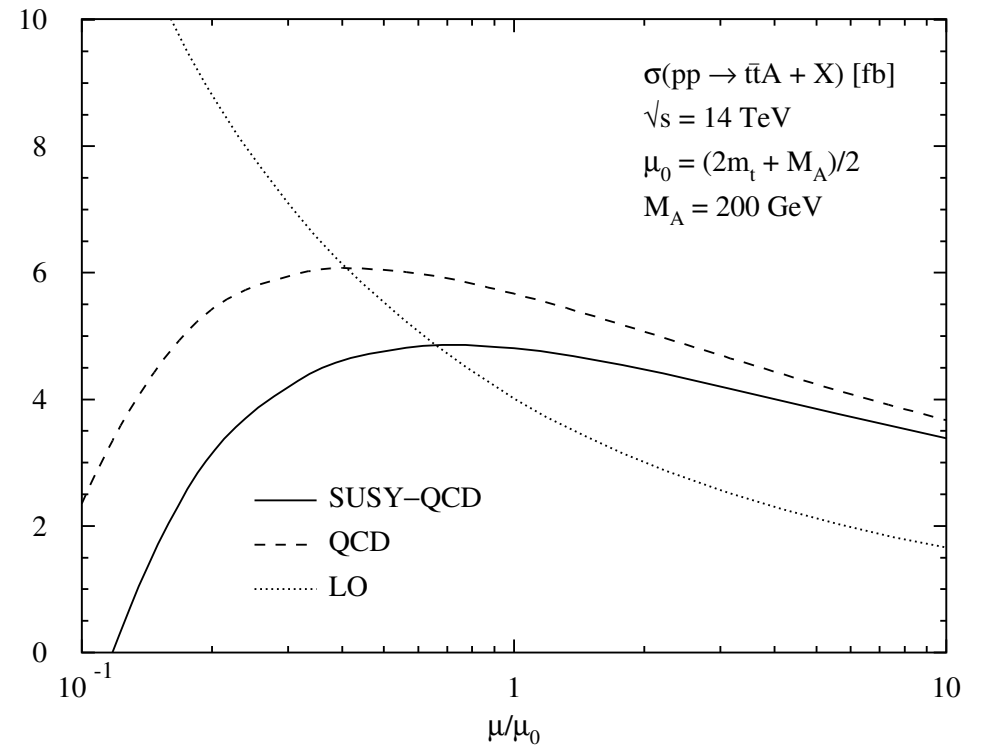


- no infrared singularities
- massive gluinos and squarks decoupled from  $\alpha_s \rightarrow 4/5$  active flavours



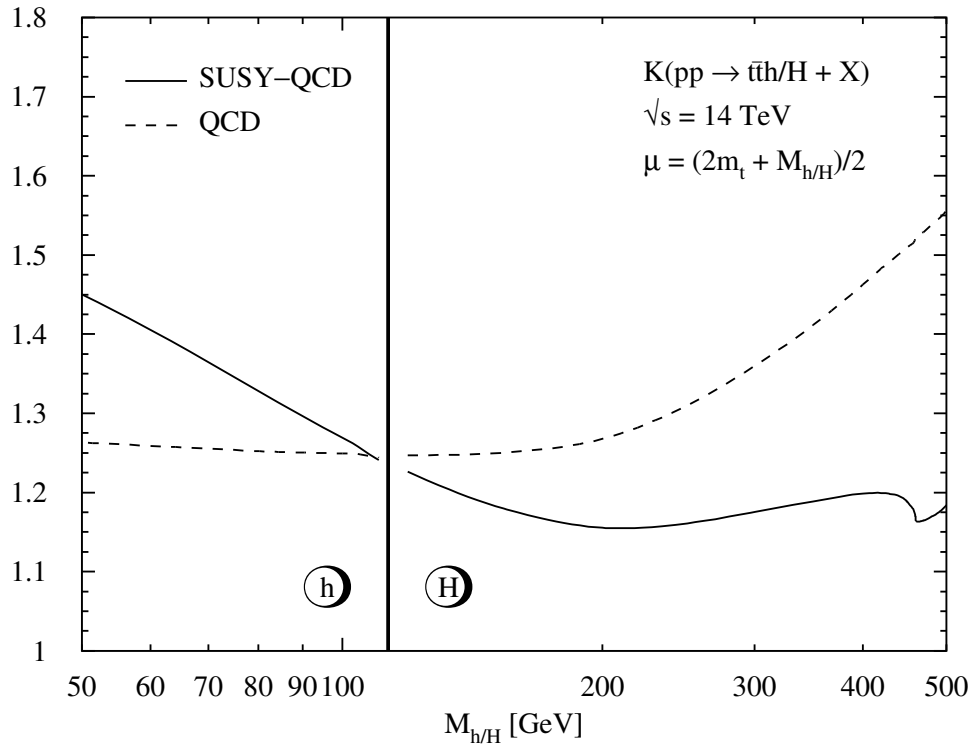
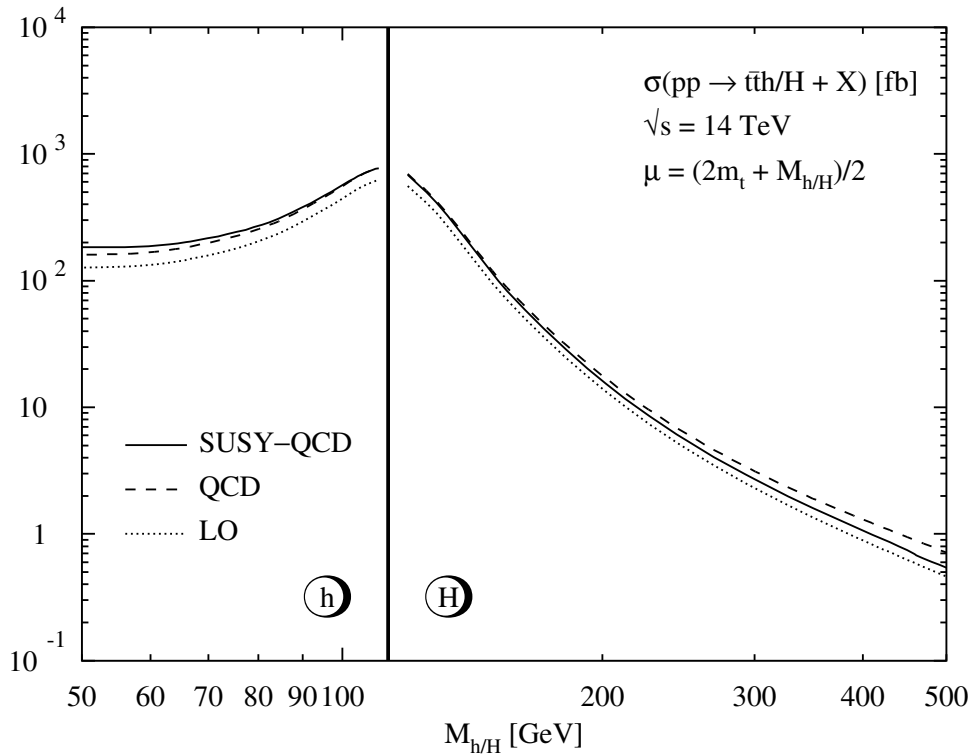
SPS5

PRELIMINARY



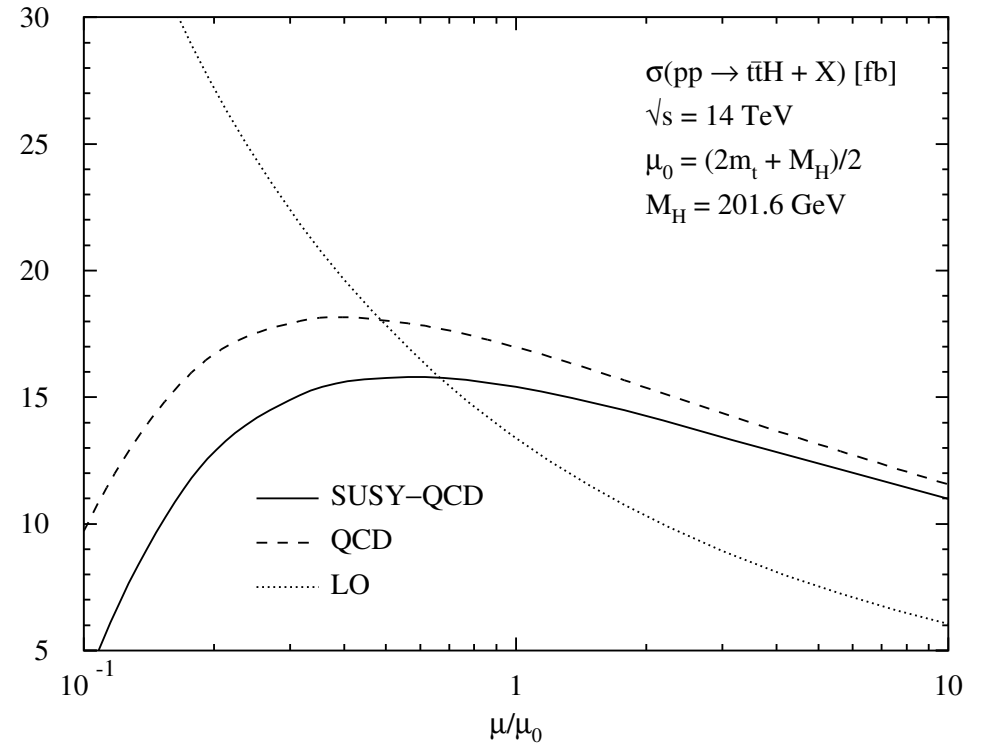
$\Rightarrow \Delta \lesssim 10\%$

Dittmaier, Häfliger,  
Krämer, S., Walser



SPS5

PRELIMINARY



$\Rightarrow \Delta \lesssim 10\%$

Dittmaier, Häfliger,  
Krämer, S., Walser