

# High-Energy QCD Matter Theory

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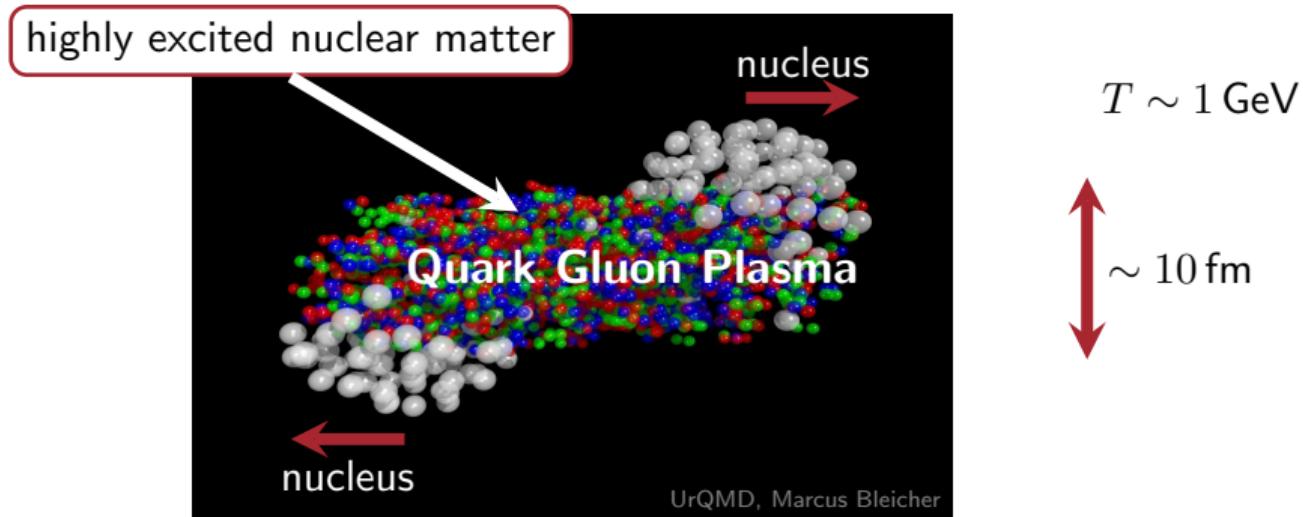
July 27, 2021



## High-energy nuclear collisions — a new direction to study QCD

High-energy physics concentrate higher energy in smaller and smaller volume.

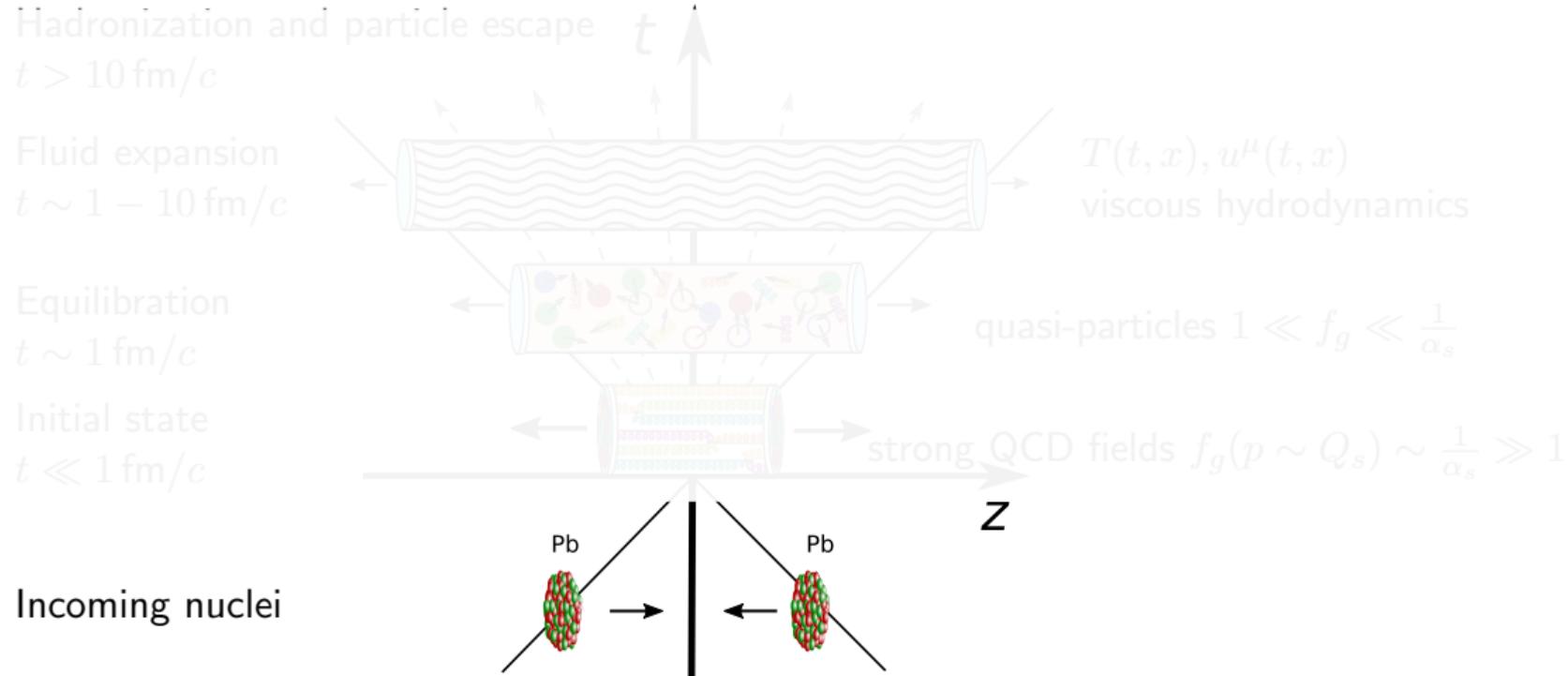
Turn to a different direction and study new phenomena *“by distributing high energy or high nucleon density over a relatively large volume.”* – T.D. Lee, 1974



*Unique chance to study the many-body dynamics of non-abelian gauge theory:*  
thermalisation, transport properties, phase diagram, hadron production, . . .

# QCD thermalisation in high-energy nuclear collisions

At the high-energy limit can use first-principles effective descriptions of QCD.

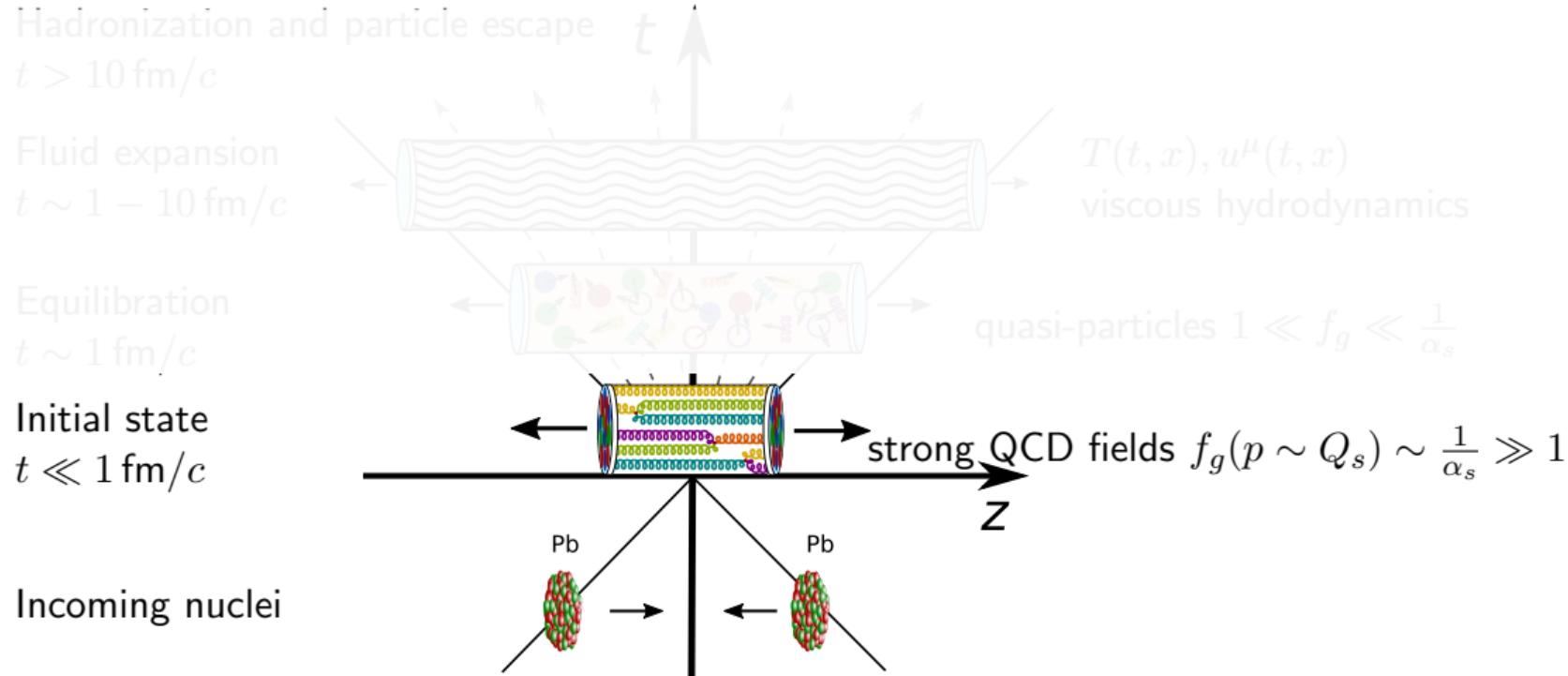


*Formation of thermalised QCD matter is a natural limit of high-energy collisions.*

# Thermalisation in QCD at weak couplings $\alpha_s \ll 1$

Berges, Heller, AM, Venugopalan (2020) [1]

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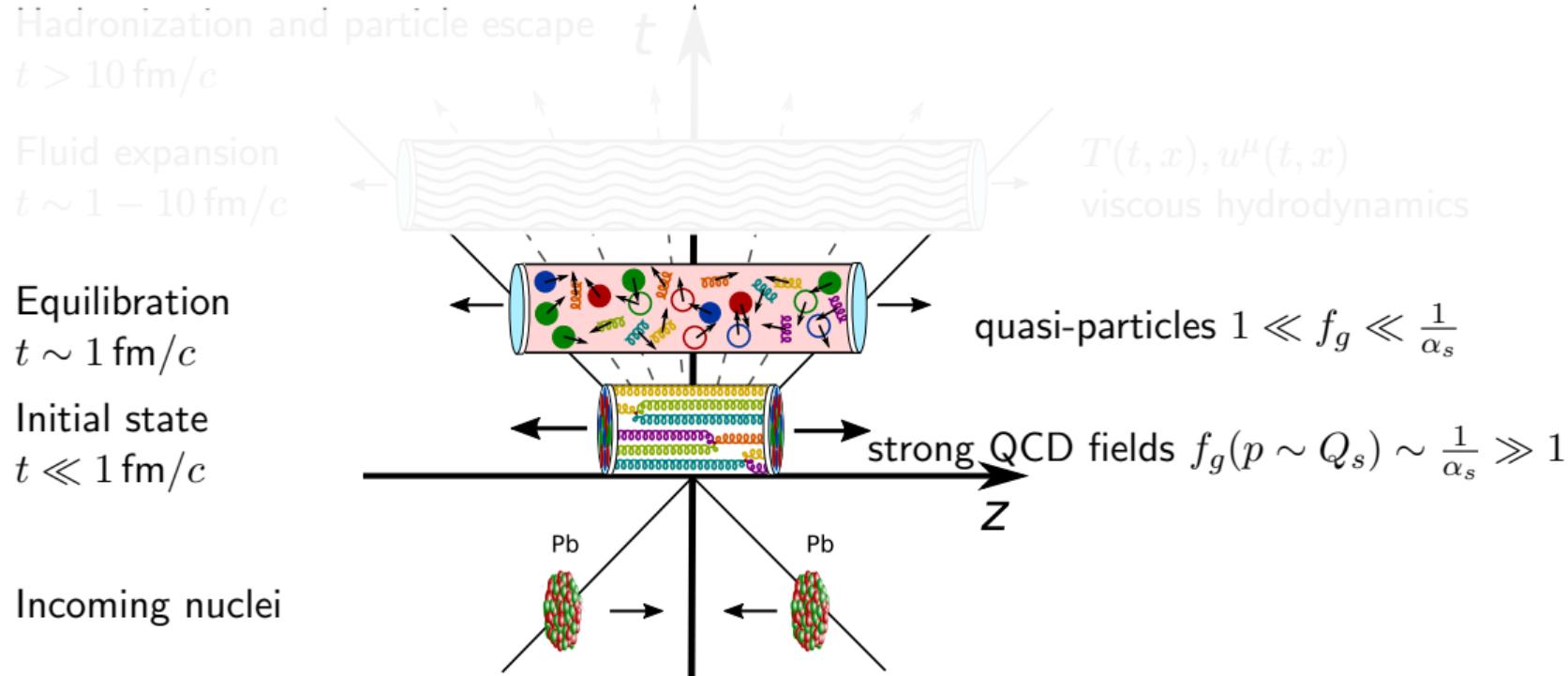


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Hadronization and particle escape

$t > 10 \text{ fm}/c$

Fluid expansion

$t \sim 1 - 10 \text{ fm}/c$

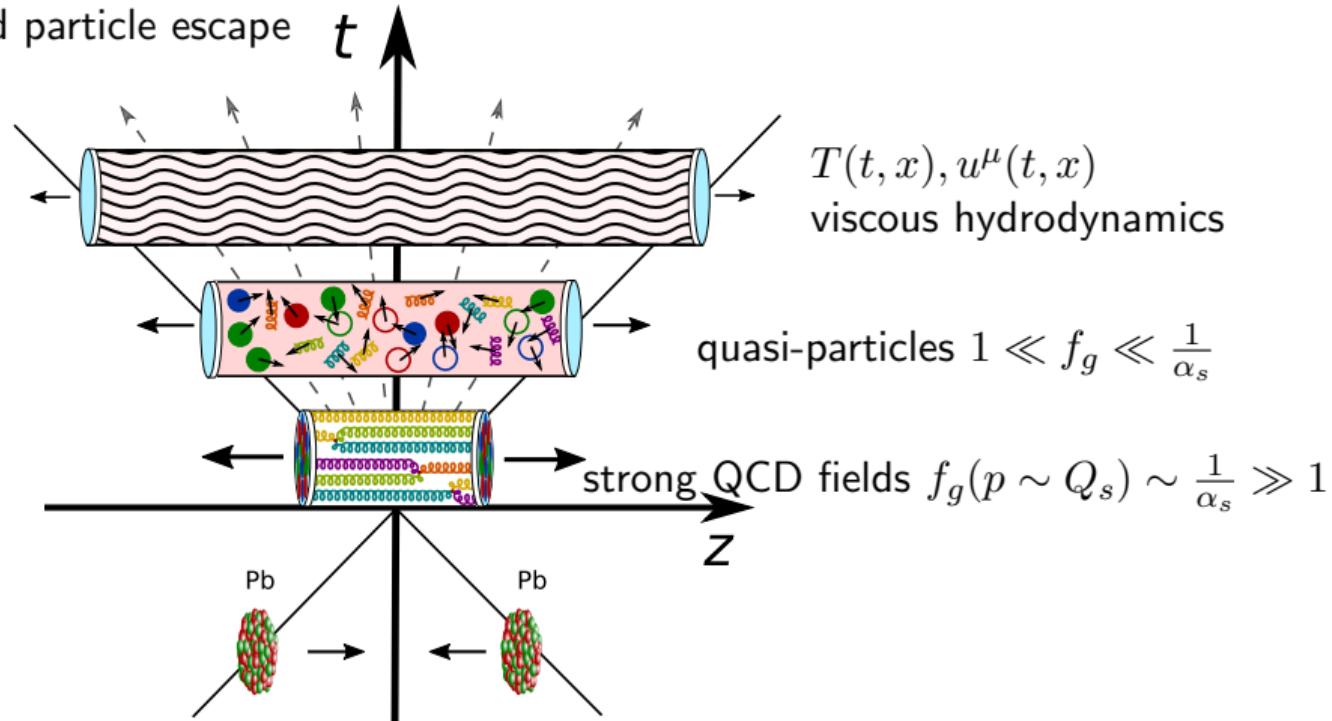
Equilibration

$t \sim 1 \text{ fm}/c$

Initial state

$t \ll 1 \text{ fm}/c$

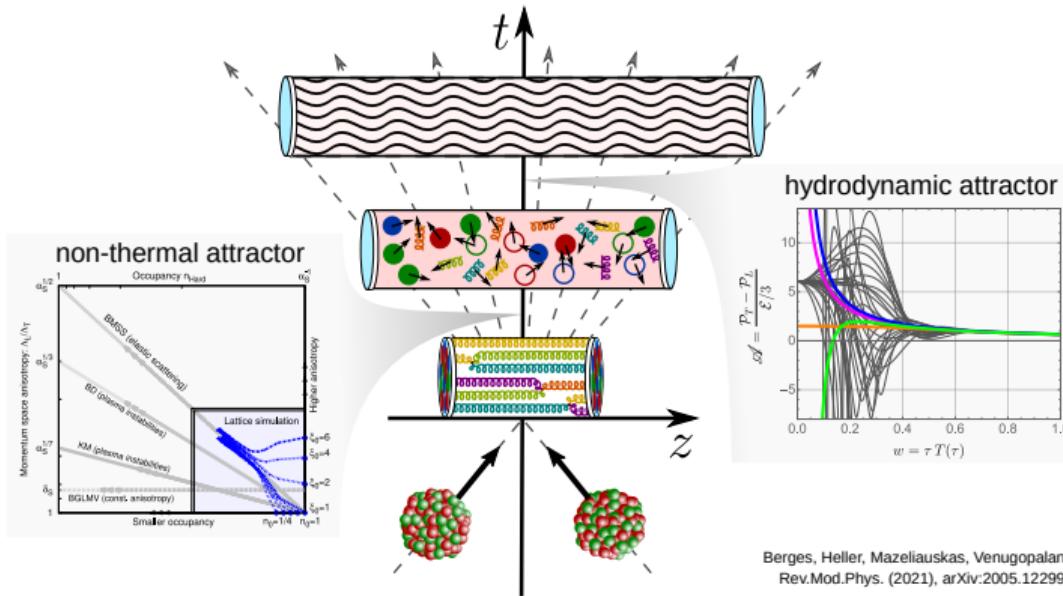
Incoming nuclei



*Formation of thermalised QCD matter is a natural limit of high-energy collisions.*

# Non-thermal and hydrodynamic attractors in QCD thermalisation

- Remarkable simplification of nonequilibrium QCD evolution.
- *Emergence of fluid dynamics behaviour at timescales of  $\tau \sim 1/T \sim 1 \text{ fm}/c$ .*
- Supported by QCD kinetic theory, QFTs with gravity duals.
- Rethinking applicability of hydrodynamics.

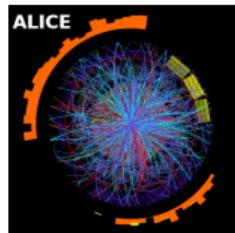


See also reviews by Florkowski, Heller and Spalinski (2017)[2], Romatschke and Romatschke (2017) [3]

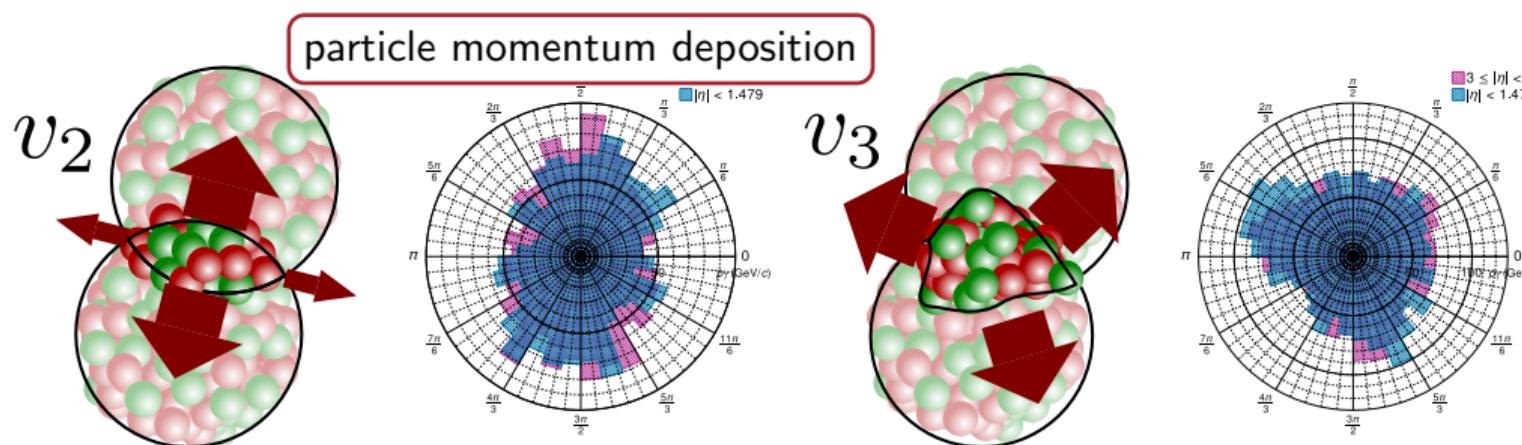
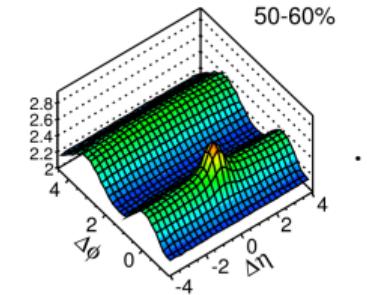
Collective behaviour of QCD matter

# Multiparticle collective flows

Produced particles show significant angular modulations  $v_n$



$$\frac{dN}{d\phi} = \frac{N}{2\pi} (1 + 2v_2 \cos(2\phi) + 2v_3 \cos(3\phi) \dots)$$

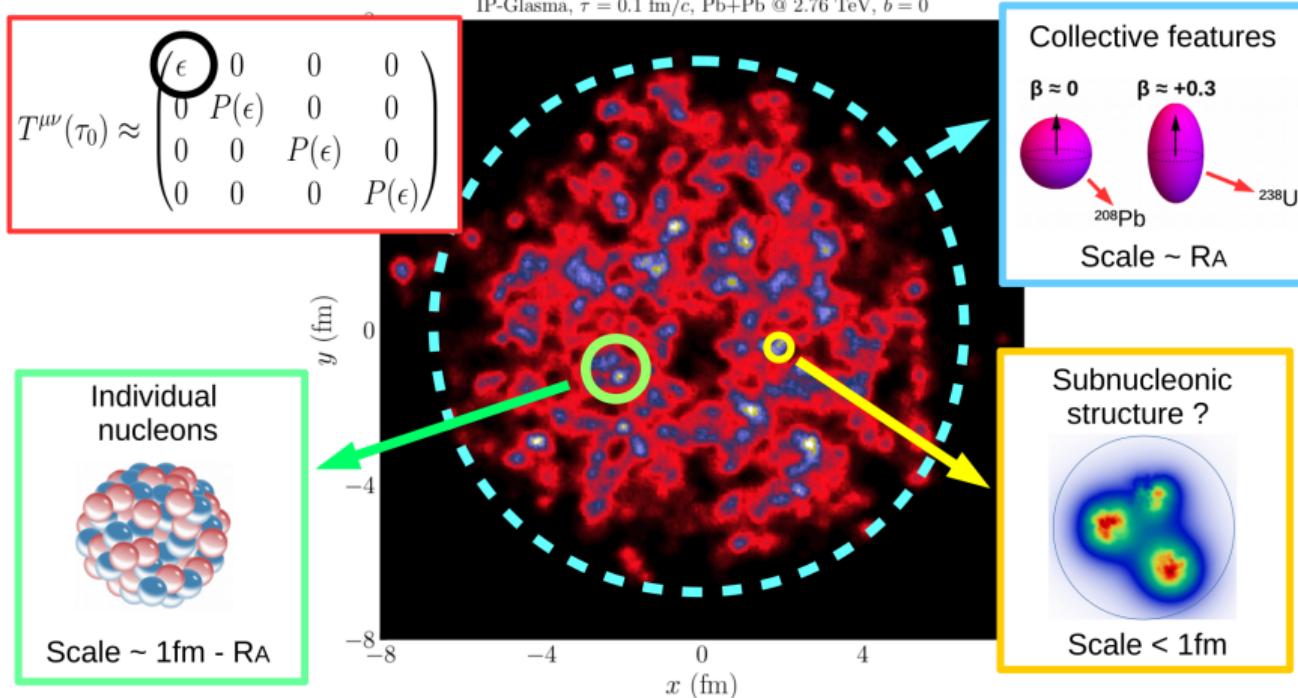


CMS Detector Performance Plots [4]

Collective particle flow is explained by pressure gradient driven QGP expansion.

# Initial conditions in nuclear collisions: sources of fluctuations

Structure of nuclei across length scales → primordial anisotropy → observed anisotropy



from Giacalone, SEWM 2021 [indico]

Experimental sensitivity allows to test both large and small scale nuclear structure.

# Hydrodynamic modelling of nuclear collisions in a nutshell



Numerically solve 2D or 3D relativistic fluid equations of motion

$$\partial_\mu T^{\mu\nu} = 0, \quad T^{\mu\nu} = eu^\mu u^\nu + (\underbrace{p + \zeta \partial_\mu u^\mu}_{\eta}) \Delta^{\mu\nu} + \underbrace{\pi^{\mu\nu}}_{-\eta \partial^{(\mu} u^{\nu)}} + \dots$$

$p(e)$  – equation of state, obtained from lattice QCD.

$\eta, \zeta$  – shear and bulk viscosity – fundamental transport properties of QGP.

- difficult to extract from lattice QCD, because of sign problem.
- perturbatively calculable only at very small couplings.

NLO computations by Ghiglieri, Moore and Teaney (2018) [5, 6]

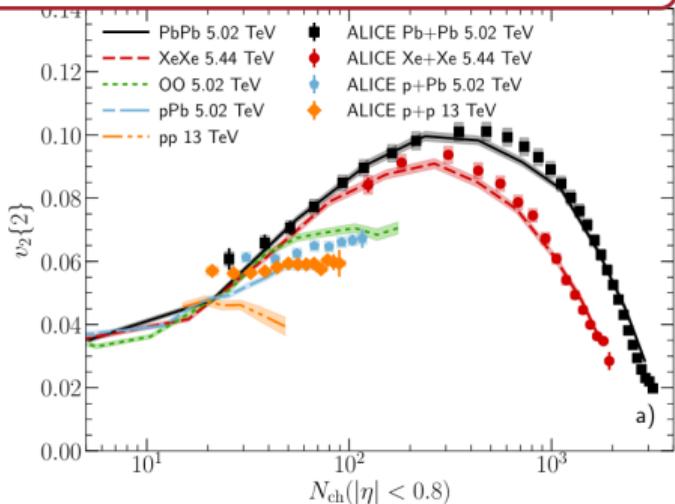
- excellent experimental data  $\Rightarrow$  can extract  $\eta/s, \zeta/s$  and higher transport coefficients from particle spectra and collective flow data.

*For QGP  $\eta/s \sim 0.1$  (in natural units) — smallest of all known fluids!*

# Multi-parameter model fits to multi-observable multi-system data

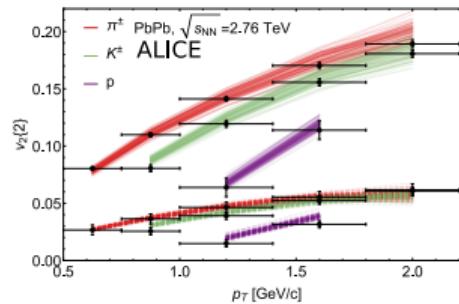
Many comprehensive analyses: Novak, Novak, Pratt, Vredevoogd, Coleman-Smith, Wolpert (2013) [7], Niemi, Eskola, Paatelainen (2015) [8]  
Bernhard, Moreland, Bass, Liu, Heinz (2016) [9], Devetak, Dubla, Floerchinger, Grossi, Massiocchi, AM, Selyuzhenkov (2019) [10], ...

## simultaneous multi-system predictions



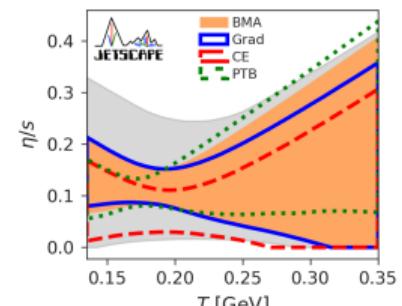
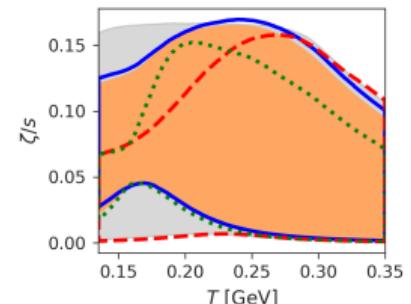
MUSIC: Schenke, Shen and Tribedy (2020) [12]

## Bayesian $\eta/s, \zeta/s$ analysis



TRAJECTUM: Nijs, van der Schee, Gürsoy, Snellings (2020) [11] JETSCAPE (2020) [13, 14]

## model averaging

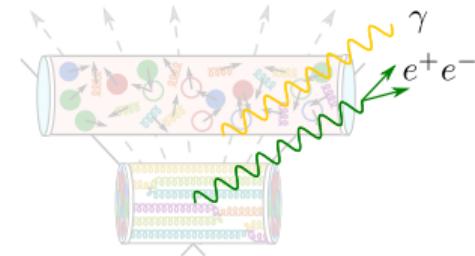


*Current focus—increasing precision, reducing systematics, accessing new properties.*

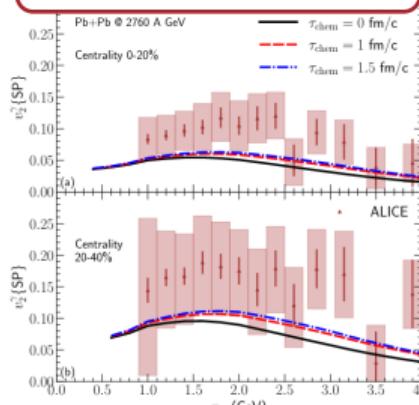
# Multi-messenger (QCD+QED) study of high-energy nuclear matter

Photon and dilepton production is sensitive to

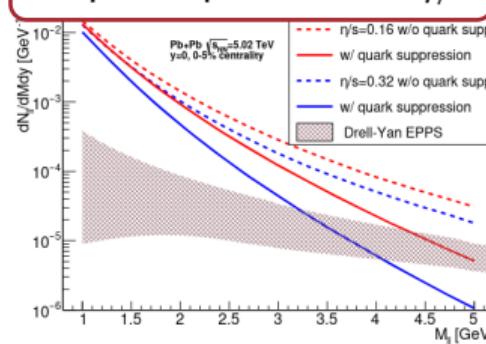
- Chemical equilibration
- QGP properties and temperature
- Early-time expansion



photon  $v_2$  and  $\tau_{\text{chem}}$



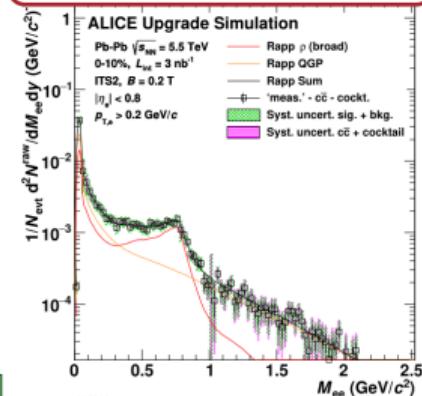
dilepton spectra and  $\eta/s$



Coquet, Du, Ollitrault, Schlichting, Winn (2021) [16]

Gale, Paquet, Schenke, Shen (2021) [15]

dileptons in runs 3+4



Yellow report (2018) [17]

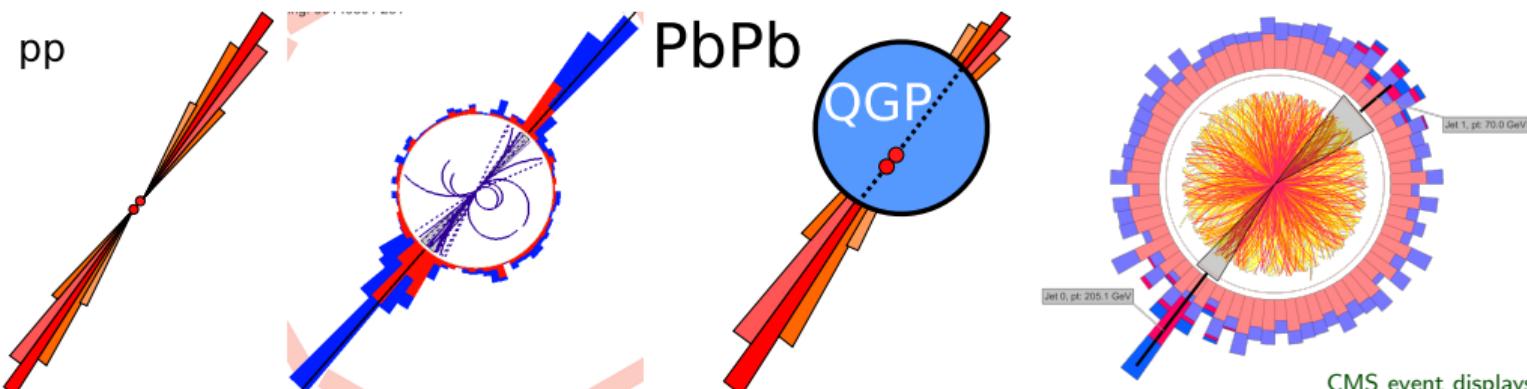
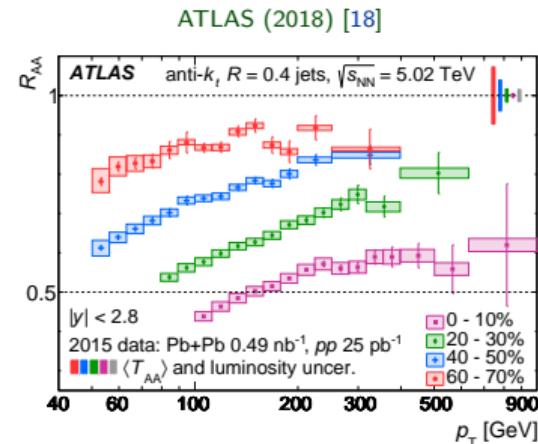
*Penetrating electromagnetic probes give unique window into QCD thermalisation.*

High momentum transfer processes in QCD matter

# High $p_T$ parton energy loss — jet quenching

High-energy jets are suppressed in nuclear collisions compared to proton-proton

$$R_{AA} = \frac{dN_{AA}^j/dp_T}{N_{\text{coll}} dN_{pp}^j/dp_T} < 1$$

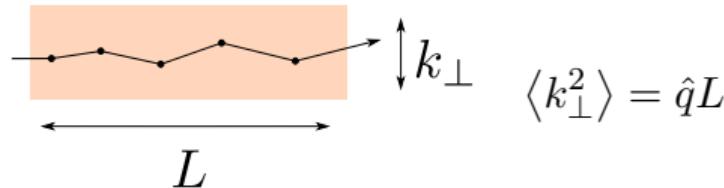


*Jet quenching is explained by energy loss in strongly interacting plasma.*

# Medium induced gluon radiation

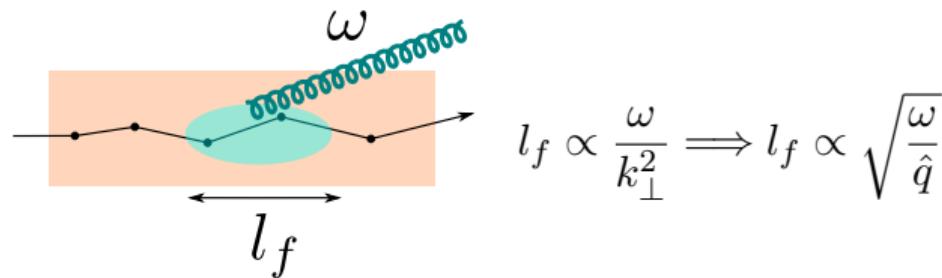
Baier, Dokshitzer, Mueller, Peigne, Schiff (1996) [19], Zakharov (1996) [20] and others

Partons suffers multiple soft scatterings in the medium  $\Rightarrow$  momentum diffusion



$\hat{q}$  – quenching parameter, property of the medium.

Finite emission formation time and interference  $\Rightarrow$  LPM suppression

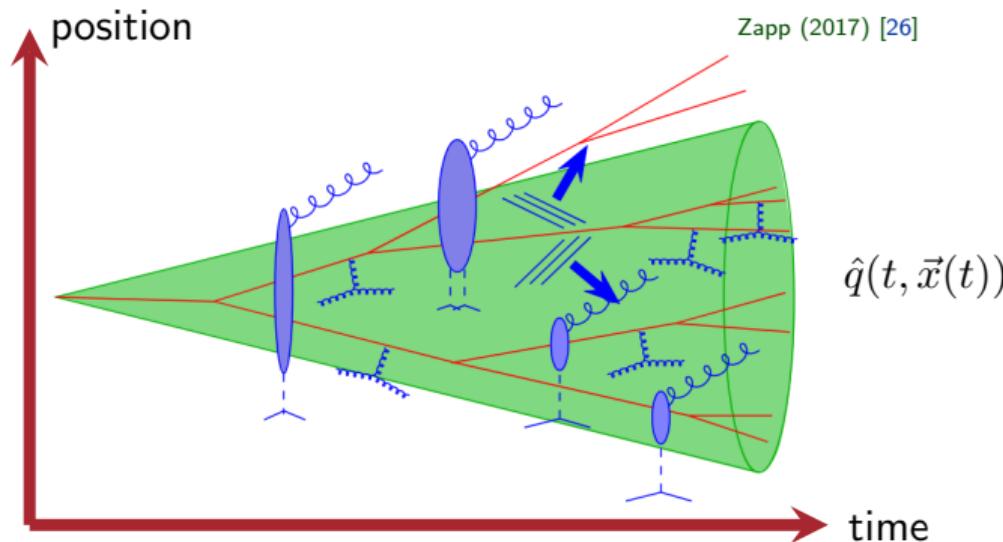


Gluon radiation induces energy loss of parent parton.

For progress on double emission see Arnold, Gorda, Iqbal (2020) [21], improved opacity expansion Barata, Mehtar-Tani (2020)[22], full resummation Andres, Apolinario, Dominguez (2020) [23], non-perturbative broadening Moore, Schlichting, Schlusser, Soudi (2021) [24], vacuum and in-medium factorization Cauchal, Iancu, Soyez (2020) [25], ...

## Jets in high-energy QCD matter

*Different from vacuum – need to know the space-time structure of parton shower.*



There are ongoing community efforts to improve all aspects of the modelling:

- Jet-medium interactions, e.g., onset of jet-quenching
- Background medium evolution, e.g., hydrodynamics tuned to soft observables.

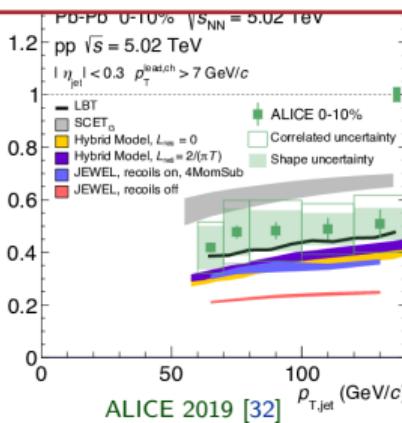
Casalderrey-Solana, Hulcher, Milhano, Pablos, Rajagopal (2018) [27], Andres, N  stor, Niemi, Paatelainen, Salgado (2019) [28]

Zigic, Ilic, Djordjevic, Djordjevic (2019) [29], Huss, Kurkela, AM, Paatelainen, van der Schee, Wiedemann (2020) [30], JETSCAPE (2021) [31]

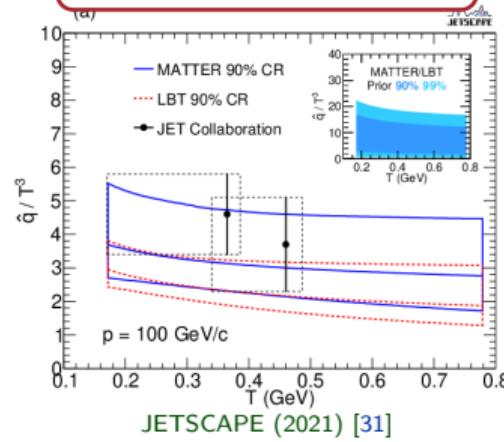
# Energy loss observables

- Inclusive jet, hadron suppression – nuclear modification factor  $R_{AA}$ .
- Coincidence measurements, e.g.,  $Z$  or  $\gamma$  tagged hadron or jet spectra  $I_{AA}$ .

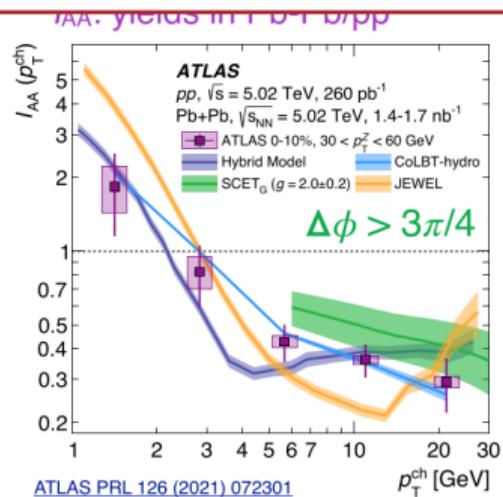
## Jet suppression in PbPb



## Bayesian $\hat{q}$ extraction



## Z-tagged hadron suppression



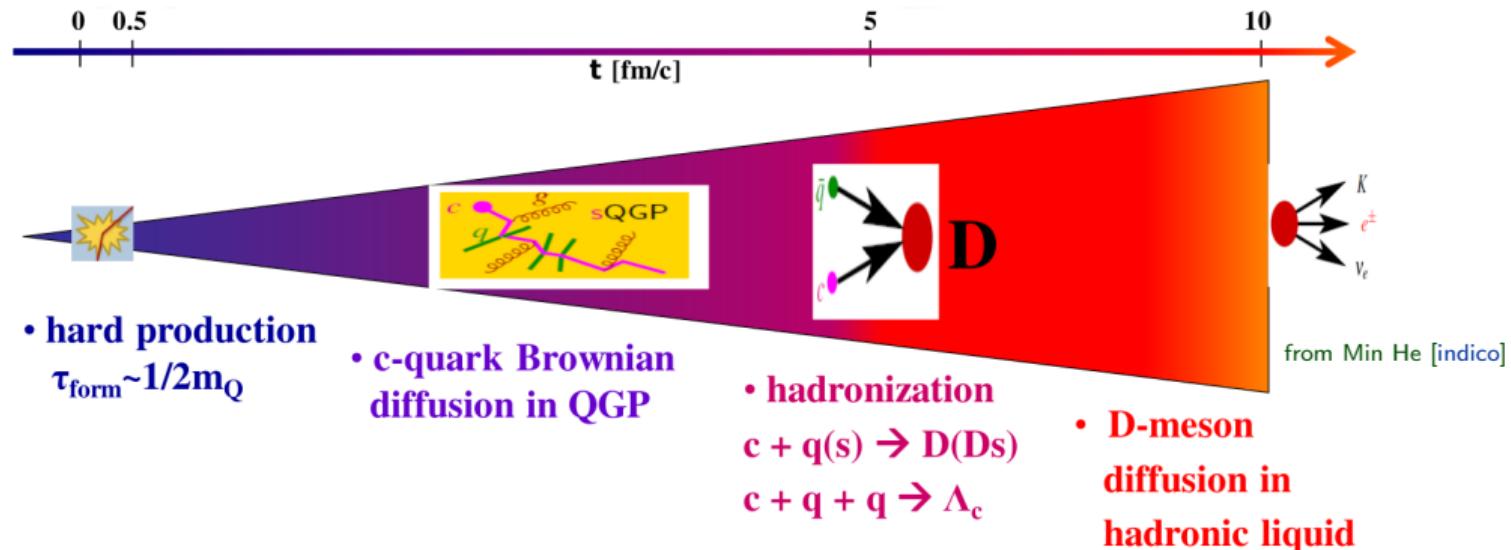
*Broad agreement among different models for basic observables  $\Rightarrow$  focus on controlling model systematics and more differential observables*

Heavy quarks in QCD matter

# Heavy quarks evolution in QGP

Charm and beauty quarks make excellent probes of QGP evolution

- Produced perturbatively ( $m_Q \gg T$ ) and at early times  $t_f \sim (2m_Q)^{-1}$
- Interacts strongly with QGP during evolution:  $D_s$  – diffusion coefficient.
- Quark flavour preserved – can be tagged.



*Focus on understanding heavy quark co-flow with the medium.*

# Hidden and open heavy quark dynamics

- Bound state  $q\bar{q}$  dissociation and recombination – open quantum system.

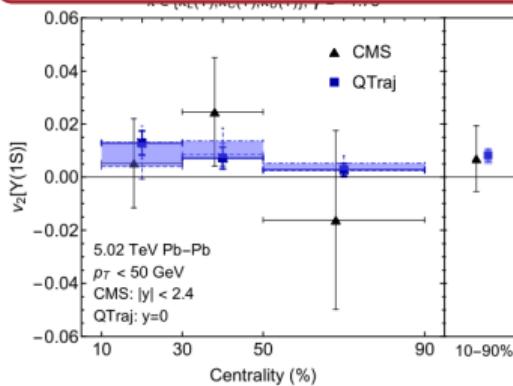
Lindblad equation for density matrix  $\rho$  Brambilla, Escobedo, Strickland, Vairo, Griend, Weber (2021) [33]

Coupled Boltzmann Transport Equations, Yao, Ke, Xu, Bass, Müller (2020) [34]

- Open heavy quark evolution – several approaches: Langevin diffusion, Boltzmann transport, energy loss, etc.

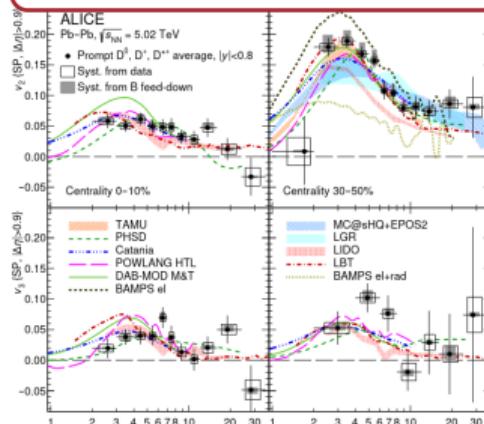
see Heavy-Flavor Transport in QCD Matter [indico]

## Elliptic flow of bottomonium



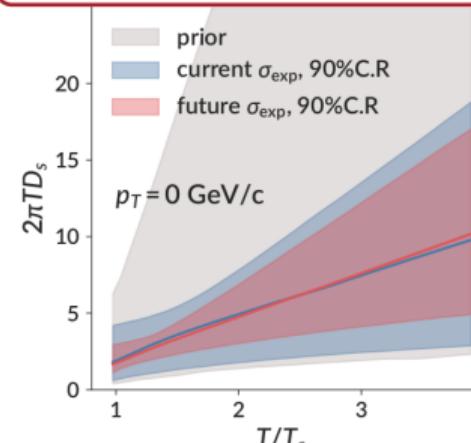
Brambilla, Escobedo, Strickland, Vairo, Griend, Weber (2021) [33]

## Elliptic flow of D mesons



ALICE (2020) [35]

## Diffusion coefficient run 3+4



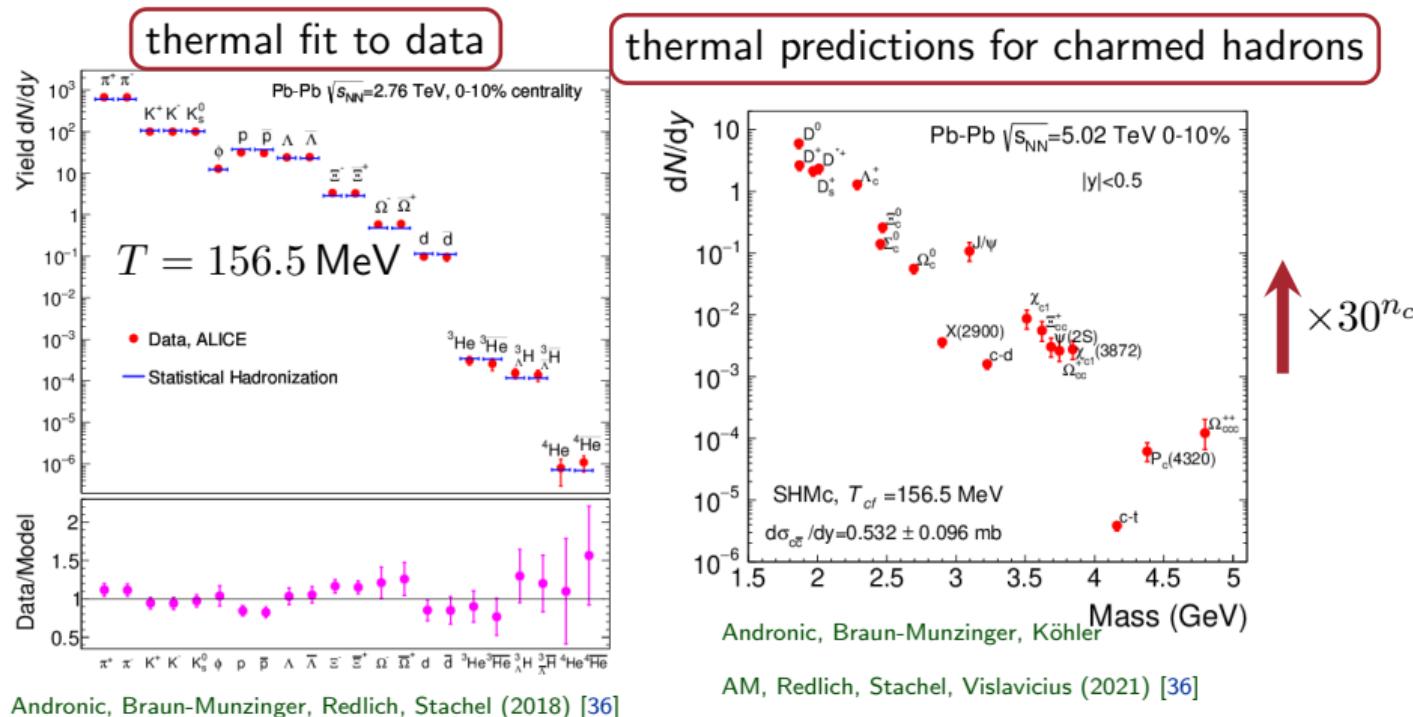
Yellow report (2018) [17]

Future runs will extend low  $p_T$  reach and pin down bottom quark flow  $\Rightarrow$  better constraints on heavy quark transport and thermalisation in QCD matter.

# Charm thermalisation in Statistical Hadronization Model (SHM)

Observed *thermal particle yields* with  $T \approx 156.5$  MeV from pions to  ${}^4\text{He}$ .

Multicharm hadron production is greatly enhanced, e.g.,  $\sim 2.7 \cdot 10^4$  times for  $\Omega_{ccc}$



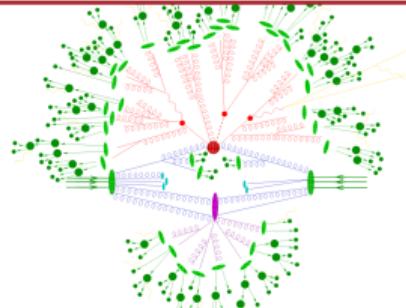
*ALICE 3 is ideally suited to measure multicharm baryon hierarchy.*

see EOI [37].

QCD matter in  $pp$  and  $p\text{Pb}$  and other small systems

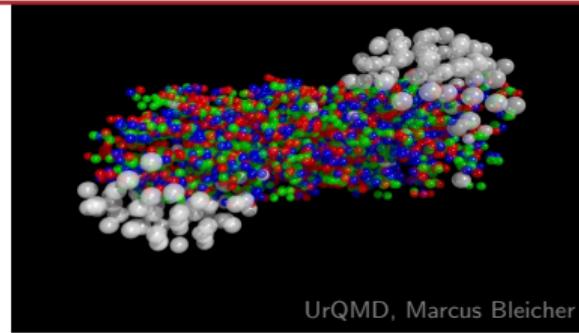
# Two successful paradigms of hadron collisions

free-streaming final state in  $pp$



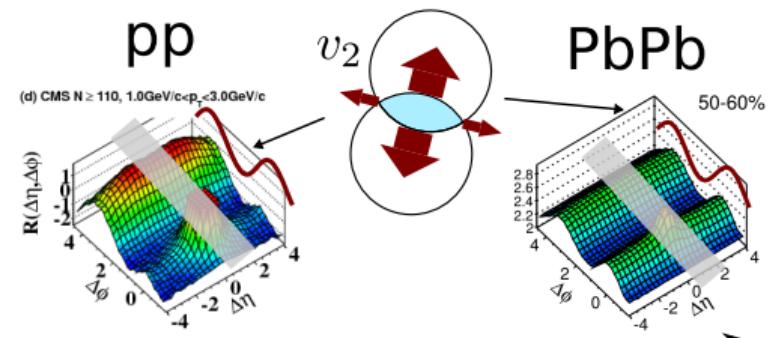
SHERPA, JHEP 02 (2009)

abundant parton re-scatterings in AA



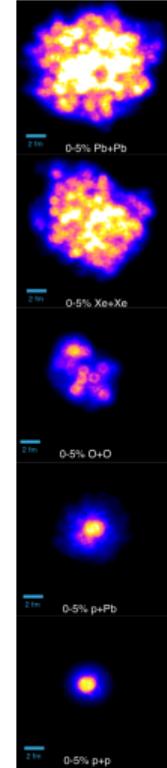
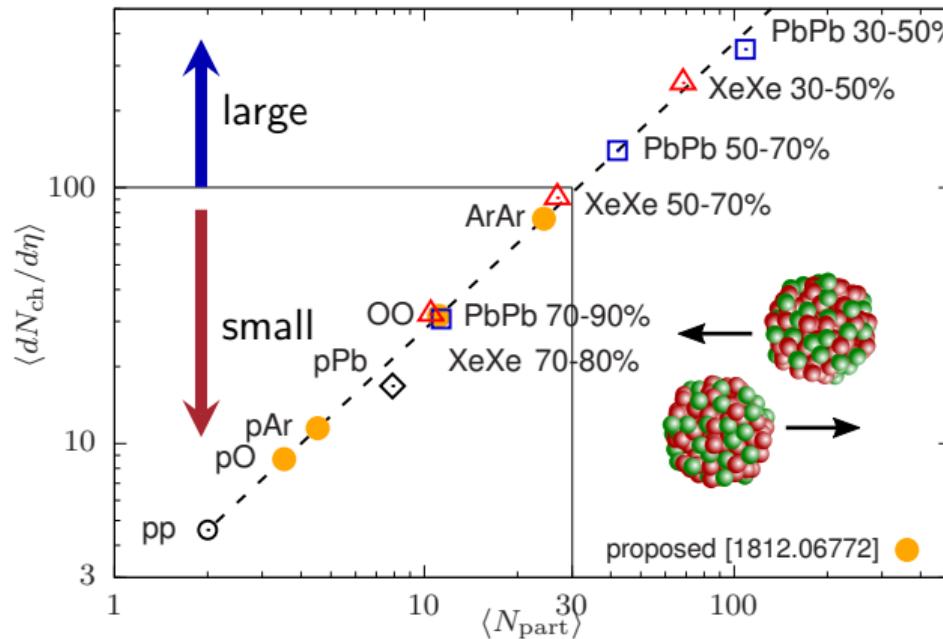
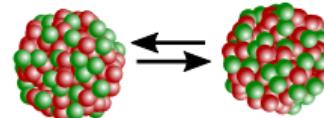
*Arguably the first discovery at LHC:  
long-range 2-particle correlations in  $pp$*   
CMS (2010) [38]

Now supported by *multi-particle correlations* and *strangeness enhancement* in  $pp$  and  $p\text{Pb}$ .



# Multiplicity as a measure of the system size

LHC: pp, pPb, XeXe, PbPb (OO, ArAr)

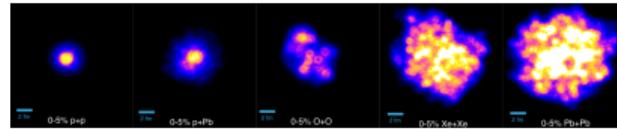
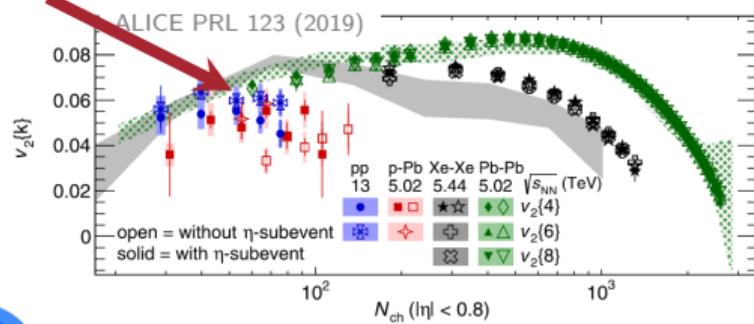


*Do all small systems exhibit the same collective phenomena?*

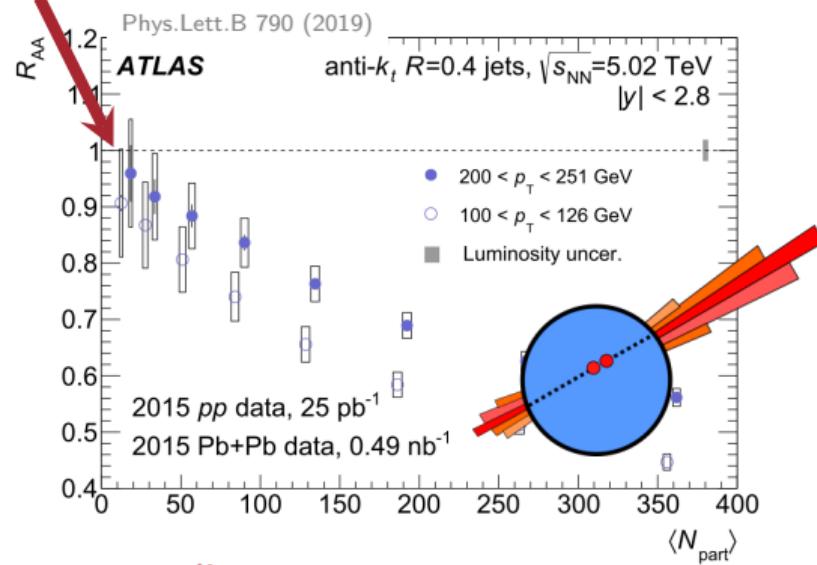
# Challenges to partonic rescattering paradigm in small systems

Different system size dependence of parton rescattering for soft and hard probes.

collective  $p_T \sim 1$  GeV particle flow



no suppression of  $p_T \sim 100$  GeV jets  
in peripheral PbPb or  $p$ Pb

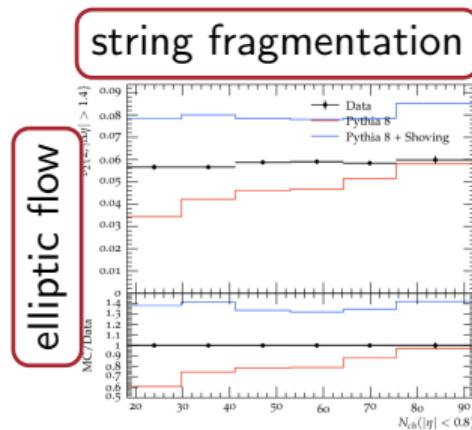


Absence of jet quenching contradicts the current paradigm:  
collective flow  $\Leftrightarrow$  high- $p_T$  energy loss.

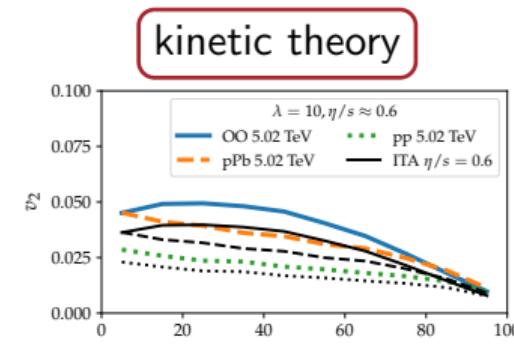
# What is the microscopic origin of collectivity in small systems?

Competing approaches in small systems:

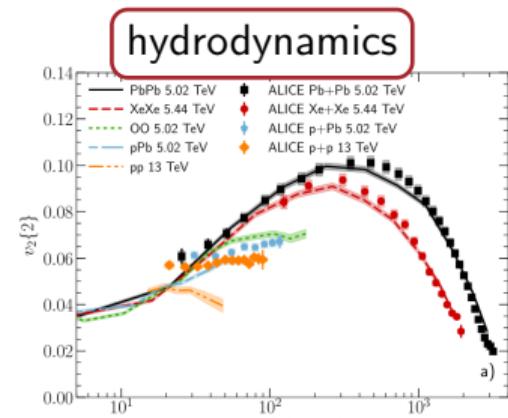
- From small to large: extending HEP event generators
- From large to small: pushing macroscopic descriptions to small size limits
- Intermediate descriptions: QCD kinetic theory in small systems.



Bierlich, Chakraborty, Gustafson, Lönnblad (2020) [39]



Kurkela, AM, Törnkvist (2021) [40]



Schenke, Shen, Prithwish (2020) [12]

*Collectivity in small systems  $\implies$  window to microscopic dynamics of QCD.*

# Light-ions at the LHC

Light-ions (e.g. O, Ar, Kr) [Yellow report \(2018\)](#) [17]:

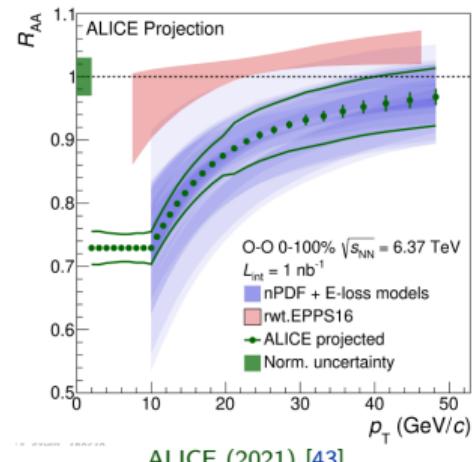
- High achievable luminosity.
- Short oxygen run planned in LHC Run 3.
- $p\text{O}$ : strong interest from cosmic ray physics.
- OO comparable to  $p\text{Pb}$ , but better geometry control.
- Many physics opportunities [see OppOatLHC \[indico\]](#)

Experimental projections and theory calculations show measurable energy loss signal in  $10 \text{ GeV} < p_T < 50 \text{ GeV}$ .

Huss, Kurkela, AM, Paatelainen, van der Schee, Wiedemann (2020) [41]

*Opportunity to discover jet quenching in small systems.*

Brewer, AM, van der Schee (2021) [42]



ALICE (2021) [43]

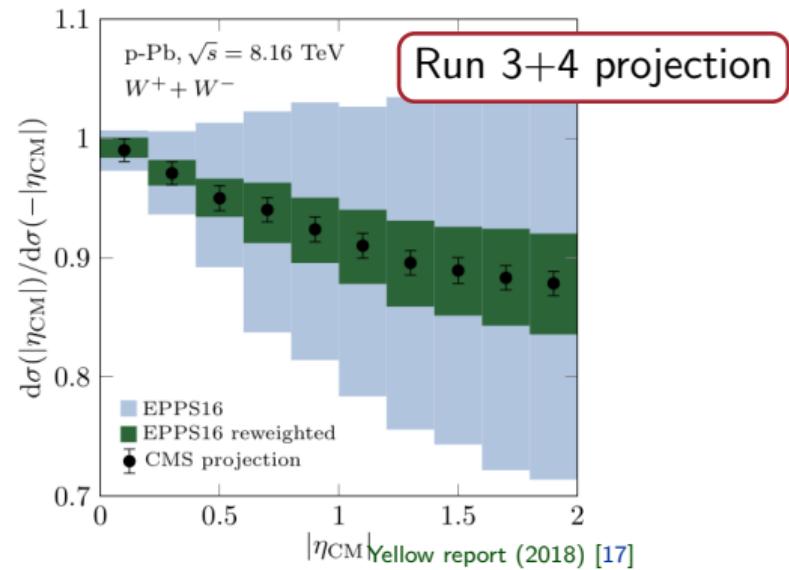
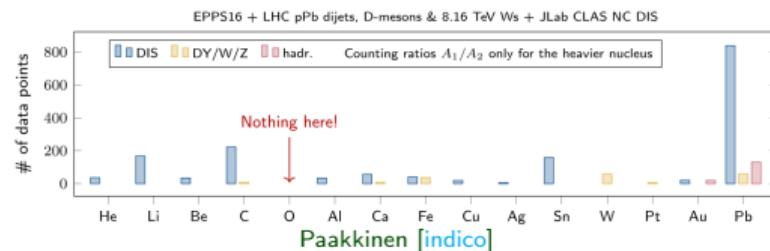
# Nuclear parton distribution functions from $pA$

nPDFs are crucial ingredients in perturbative of QCD matter probes:

- jets, high- $p_T$  hadrons
- heavy quark production

*Precision determination of hard probes modification requires precise null baselines.*

## Global nPDF fits to nuclear data



*High statistics  $pPb \Rightarrow$  smaller nPDF uncertainties,  $pO \Rightarrow$  mass number dependence.*

## Summary

*Experiments with nuclear collisions have revealed many new phenomena of high-energy QCD matter.*

- Detailed theoretical picture of QCD thermalisation.
- Successful extraction of QGP properties from precise data.
- Strong high- $p_T$  and heavy quark interaction with QCD matter.

Outlook:

- LHC run 3 and 4 will deliver high-statics  $pp$ ,  $pPb$  and  $PbPb$  data  
*access to rare observables, e.g., Z-tagging, bottom quark flow*
- Advanced models and statistical analysis of extensive datasets  
*the field is ready for precision era*
- Small system scan: high-multiplicity  $pp$ , peripheral  $PbPb$ ,  $pPb$  and light-ions.  
*time for a unified picture of collectivity in all hadronic collisions*

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