Comparison of pp and $p\bar{p}$ differential elastic cross sections and observation of the exchange of a colorless C-odd gluonic compound



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- Introduction to the Odderon
- D0 and TOTEM data
- Extrapolation of TOTEM data to Tevatron energies
- Comparison between D0 data and TOTEM extrapolated data



What is the odderon? The QCD picture



- Multi-gluon exchanges in hadron-hadron interactions in elastic *pp* interactions (Bartels-Kwiecinski-Praszalowicz)
- From B. Nicolescu: The Odderon is defined as a singularity in the complex plane, located at J = 1 when t = 0 and which contributes to the odd crossing amplitude



- Leads to contributions on 3,... gluon exchanges in terms of QCD for the perturbative odderon
- Colorless C-odd 3-gluon state (odderon) predicts differences in elastic dσ/dt for pp and pp̄ interactions since it corresponds to different amplitudes/ interferences

Measurement of elastic scattering at Tevatron and LHC



- Study of elastic pp → pp reaction: exchange of momentum between the two protons which remain intact
- Measure intact protons scattered close to the beam using Roman Pots installed both by D0 and TOTEM collaborations
- From counting the number of events as a function of |t| (4-momentum transferred square at the proton vertex measured by tracking the protons), we get $d\sigma/dt$

D0 elastic $p\bar{p} \ d\sigma/dt$ cross section measurements



- D0 collected elastic pp̄ data with intact p and p̄ detected in the Forward Proton Detector with 31 nb⁻¹ Phys. Rev. D 86 (2012) 012009
- Measurement of elastic $p\bar{p} \ d\sigma/dt$ at 1.96 TeV for 0.26 <|t| < 1.2 GeV²

TOTEM cross section measurements



TOTEM elastic $pp \ d\sigma/dt$ cross section measurements

- Elastic *pp* $d\sigma/dt$ measurements: tag both intact protons in TOTEM Roman Pots 2.76, 7, 8 and 13 TeV
- Very precise measurements at 2.76, 7, 8 and 13 TeV: Eur. Phys. J. C 80 (2020) no.2, 91; EPL 95 (2011) no. 41004; Nucl. Phys. B 899 (2015) 527; Eur. Phys. J. C79 (2019) no.10, 861



Comparison of pp and pp differential elastic cross sections and observation of the exchange of a colorly

Strategy to compare pp and $p\bar{p}$ data sets



- In order to identify differences between pp and pp̄ elastic dσ/dt data, we need to compare TOTEM measurements at 2.76, 7, 8, 13 TeV and D0 measurements at 1.96 TeV
- All TOTEM dσ/dt measurements show the same features, namely the presence of a dip and a bump in data, whereas D0 data do not show this feature

Reference points of elastic $d\sigma/dt$



• Define 8 characteristic points of elastic pp $d\sigma/dt$ cross sections (dip, bump...) that are feature of elastic pp interactions

- Determine how the values of |t| and $d\sigma/dt$ of characteristic points vary as a function of \sqrt{s} in order to predict their values at 1.96 TeV
- We use data points closest to those characteristic points (avoiding model-dependent fits)
- Data bins are merged in case there are two adjacent dip or bump points of about equal value
- This gives a distribution of t and $d\sigma/dt$ values as a function of \sqrt{s} for all characteristic points



- Bump over dip ratio measured for *pp* interactions at ISR and LHC energies
- Bump over dip ratio in *pp* elastic collisions: decreasing as a function of \sqrt{s} up to ~ 100 GeV and flat above
- D0 $p\bar{p}$ shows a ratio of 1.00 ± 0.21 given the fact that no bump/dip is observed in $p\bar{p}$ data within uncertainties: more than 3σ difference between pp and $p\bar{p}$ elastic data (assuming flat behavior above $\sqrt{s} = 100 \, GeV$)

Variation of t and $d\sigma/dt$ values for reference points



 $|t| = a \log(\sqrt{s} [\text{TeV}]) + b$ $(d\sigma/dt) = c\sqrt{s} [\text{TeV}] + d$

Fits of TOTEM extrapolated characteristic points at 1.96 TeV

- The last step is to predict the *pp* elastic cross sections at the same *t* values as measured by D0 in order to make a direct comparison
- Fit the reference points extrapolated to 1.96 TeV from TOTEM measurements using a double exponential fit ($\chi^2 = 0.63$ per dof): $h(t) = a_1 e^{-b_1|t|^2 c_1|t|} + d_1 e^{-f_1|t|^3 g_1|t|^2 h_1|t|}$
 - This function is chosen for fitting purposes only
 - Low-*t* diffractive cone (1st function) and asymmetric structure of bump/dip (2nd function)
 - The two exponential terms cross around the dip, one rapidly falling and becoming negligible in the high *t*-range where the other term rises above the dip
- Systematic uncertainties evaluated from an ensemble of MC experiments in which the cross section values of the eight characteristic points are varied within their Gaussian uncertainties. Fits without a dip and bump position matching the extrapolated values within their uncertainties are rejected, and slope and intercept constraints are used to discard unphysical fits
- Such formula leads also to a good description of TOTEM data in the dip/bump region at 2.76, 7, 8 and 13 TeV

Relative normalization between D0 measurement and extrapolated TOTEM data: total *pp* cross section at 1.96 TeV



- Differences in normalization taken into account by adjusting TOTEM and D0 data sets to have the same cross sections at the optical point $d\sigma/dt(t=0)$ (NB: OP cross sections expected to be equal if there are only C-even exchanges)
- Predict the *pp* total cross section from extrapolated fit to TOTEM data ($\chi^2 = 0.27$)

$$\sigma_{tot} = a_2 \log^2 \sqrt{s} [\text{TeV}] + b_2$$

Other parametrizations lead to same results

• Leads to estimate of pp σ_{tot} =82.7 \pm 3.1 mb at 1.96 TeV

Relative normalization between D0 measurement and extrapolated TOTEM data: Rescaling TOTEM data

- Adjust 1.96 TeV $d\sigma/dt(t=0)$ from extrapolated TOTEM data to D0 measurement
- From TOTEM $pp \sigma_{tot}$, obtain $d\sigma/dt(t=0)$:

$$\sigma_{tot}^2 = \frac{16\pi(\hbar c)^2}{1+\rho^2} \left(\frac{d\sigma}{dt}\right)_{t=0}$$

- Assuming $\rho = 0.145$, the ratio of the imaginary and the real part of the elastic amplitude, as taken from COMPETE extrapolation
- This leads to a TOTEM $d\sigma/dt(t=0)$ at the OP of 357.1 \pm 26.4 mb/GeV²
- D0 measured the optical point of $d\sigma/dt$ at small t: 341 ± 48 mb/GeV²
- \bullet TOTEM data rescaled by 0.954 \pm 0.071
- NB: We do not claim that we performed a measurement of $d\sigma/dt$ at the OP at t = 0 (it would require additional measurements closer to t = 0), but we use the two extrapolations simply in order to obtain a common and somewhat arbitrary normalization point

Predictions at $\sqrt{s}=1.96$ TeV

- Reference points at 1.96 TeV (extrapolating TOTEM data) and 1σ uncertainty band
- Comparison with D0 data



Comparison between D0 measurement and extrapolated TOTEM data

• χ^2 test to examine the probability for the D0 and TOTEM $d\sigma/dt$ to agree

$$\chi^{2} = \sum_{i,j} [(T_{i} - D_{i})C_{ij}^{-1}(T_{j} - D_{j})] + \frac{(A - A_{0})^{2}}{\sigma_{A}^{2}} + \frac{(B - B_{0})^{2}}{\sigma_{B}^{2}}$$

where T_j and D_j are the $j^{th} d\sigma/dt$ values for TOTEM and D0, C_{ij} the covariance matrix, A(B) the nuisance parameters for scale (slope) with $A_0(B_0)$ their nominal values

- Slopes constrained to their measured values (*pp* to $p\bar{p}$ integrated elastic cross section ratio (dominated by the exp part) becomes 1 in the limit $\sqrt{s} \to \infty$ which means similar slopes at small |t| as observed in data)
- Test using the difference of the integrated cross section in the examined |t|-range with its fully correlated uncertainty, and the experimental and extrapolated points with their covariance matrices
- Given the constraints on the OP normalization and logarithmic slopes of the elastic cross sections, the χ^2 test with six degrees of freedom yields the *p*-value of 0.00061, corresponding to a significance of 3.4σ

Combination with additional TOTEM measurement: ρ measurement



• Measure elastic scattering at very low t: Coulomb-Nuclear interference region

$$rac{d\sigma}{dt} \sim |A^{C} + A^{N}(1 - lpha \mathcal{G}(t))|^{2}$$

- The differential cross section is sensitive to the phase of the nuclear amplitude
- In the CNI region, both the modulus and the phase of the nuclear amplitude can be used to determine $\rho = \frac{Re(A^N(0))}{Im(A^N(0))}$ where the modulus is constrained by the measurement in the hadronic region and the phase by the t dependence

A previous measurement by TOTEM: ρ and σ_{tot} measurements as an indication for odderon



- ρ is the ratio of the real to imaginary part of the elastic amplitude at t = 0
- Using low |t| data in the Coulomb-nuclear interference region, measurement of ρ at 13 TeV: $\rho = 0.09 \pm 0.01$ (EPJC 79 (2019) 785)
- Combination of the measured ρ and σ_{tot} values not compatible with any set of models without odderon exchange (COMPETE predictions above as an example)
- This result can be explained by the exchange of the Odderon in addition to the Pomeron Comparison of *pp* and *pp* differential elastic cross sections and observation of the exchange of a colorly 16 / 18

- Combination with the independent evidence of the odderon found by the TOTEM Collaboration using ρ and total cross section measurements at low t in a completely different kinematical domain
- For the models included in COMPETE, the TOTEM ρ measurement at 13 TeV provided a 3.4 to 4.6 σ significance, to be combined with the D0/TOTEM result
- The combined significance ranges from 5.3 to 5.7 σ depending on the model
- Models without colorless *C*-odd gluonic compound are excluded including the Durham model and different sets of COMPETE models (blue, magenta and green bands on the previous slide)

Conclusion

- Detailed comparison between $p\bar{p}$ (1.96 TeV from D0) and pp (2.76, 7, 8, 13 TeV from TOTEM) elastic $d\sigma/dt$ data FERMILAB-PUB-20-568-E; CERN-EP-2020-236
- *R* ratio of bump/dip shows a difference of more than 3σ between D0 (*R*=1.0±0.21), and TOTEM (assuming flat behavior above $\sqrt{s} = 100$ GeV)
- Fits of 8 "characteristic" points of elastic $pp \ d\sigma/dt$ data such as dip, bump, etc as a function of \sqrt{s} in order to predict pp data at 1.96 TeV
- pp and $p\bar{p}$ cross sections differ with a significance of 3.4 σ in a model-independent way and thus provides evidence that the Colorless *C*-odd gluonic compound i.e. the odderon is needed to explain elastic scattering at high energies
- When combined with the ρ and total cross section result at 13 TeV, the significance is in the range 5.3 to 5.7 σ and thus constitutes the first experimental observation of the odderon: Major discovery at CERN/Tevatron

