



Jet substructure measurements in CMS experiment

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for the CMS Collaboration

HEPHY Vienna

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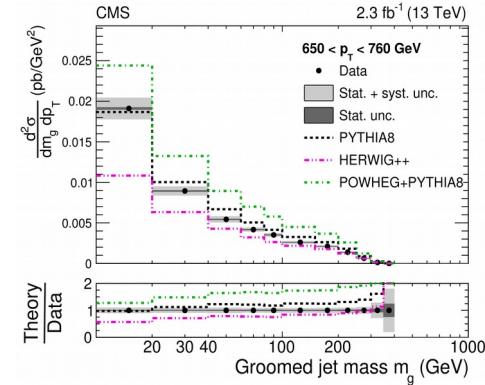


Why jet substructure measurements?

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Improved understanding of QCD

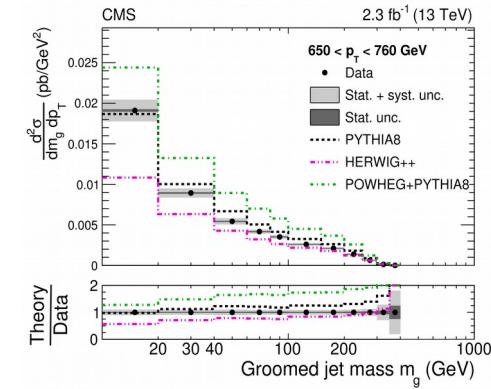
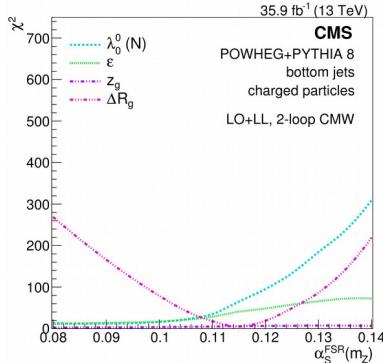
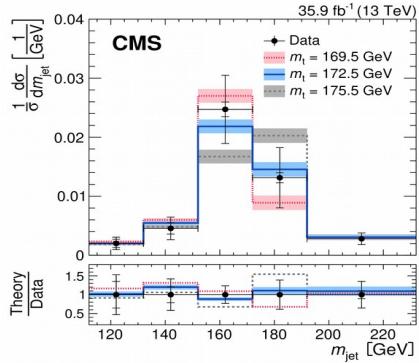
Resummation region enhanced by jet grooming



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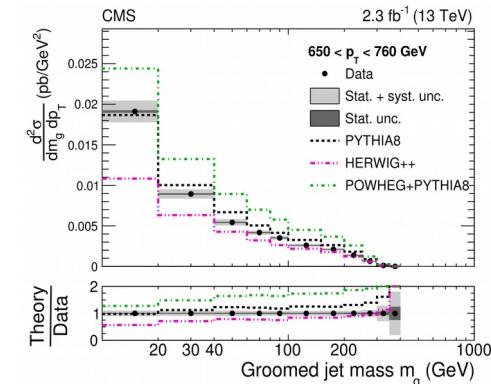
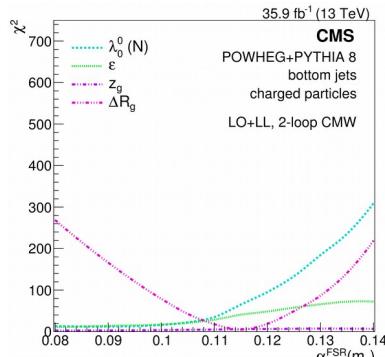
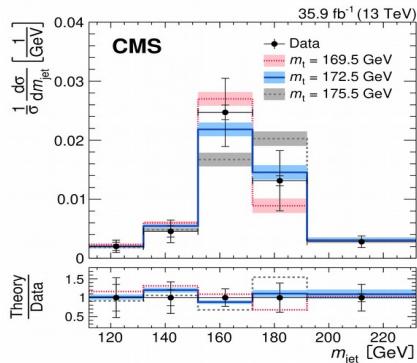
Precision tests of SM parameters
(and probing BSM effects)

α_s running, top quark mass

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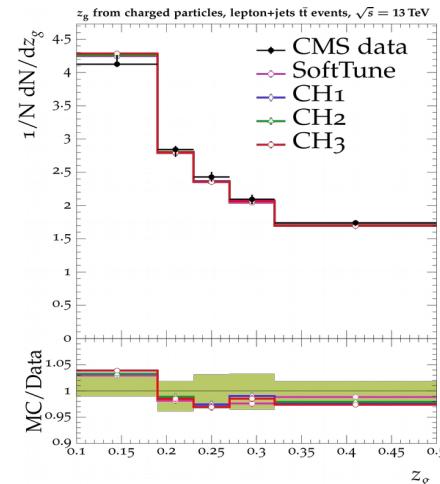
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Tuning general purpose MC generators

Understanding parton shower evolution

Improving underlying event description

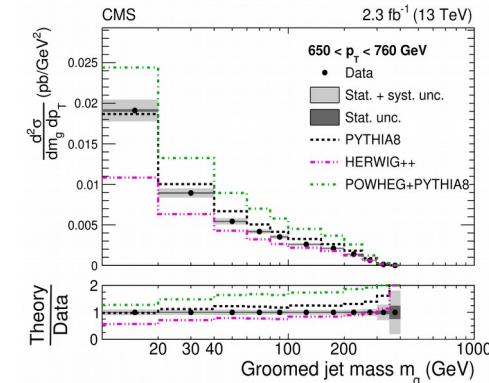
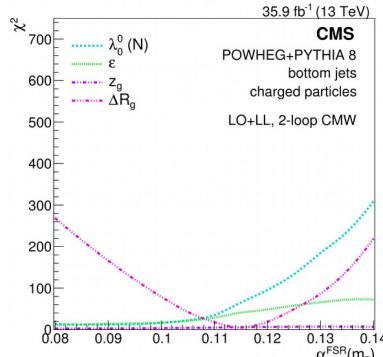
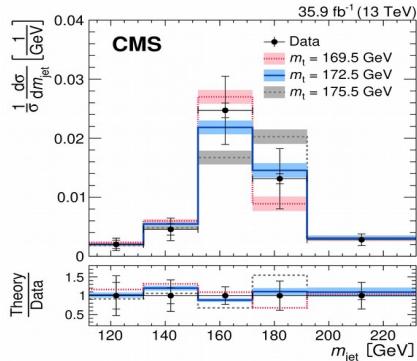
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Improves modeling of particle taggers → Helps measurements & searches

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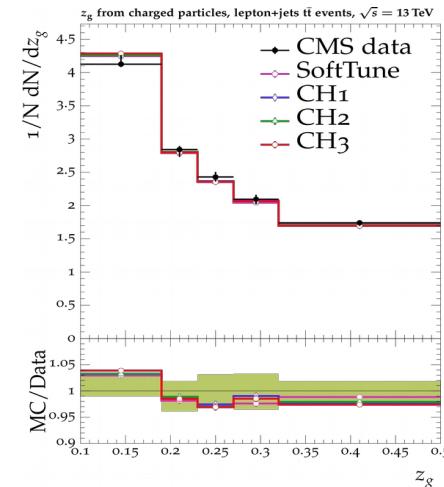
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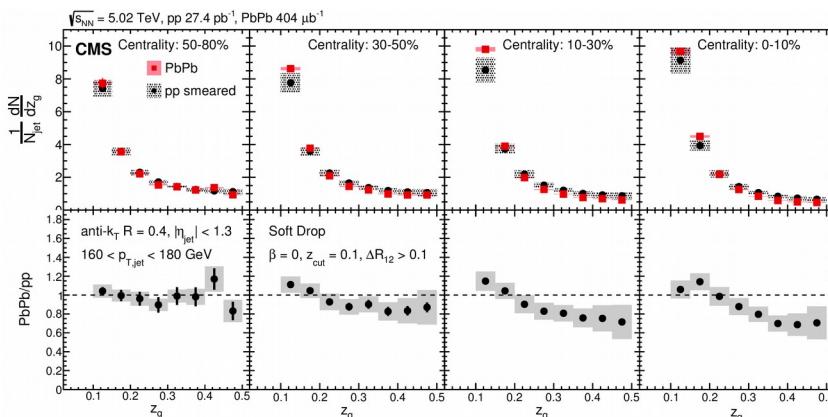
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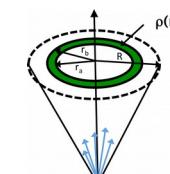
Sensing emergent phenomena

QGP
Dead cone effects

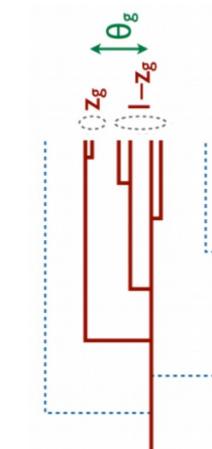
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Reference	\sqrt{s}	Collision	Events	Jet sample and kinematic region	Observables
1204.3170	7 TeV	pp	Inclusive jets	$q/g\text{-jets (AK7), } 20 < p_T < 1000 \text{ GeV}$ $q/g\text{-jets (AK5), } 50 < p_T < 1000 \text{ GeV}$	Jet shapes, charged hadron multiplicity, width
1205.5872	2.76 TeV	pp/PbPb	Dijet	$q/g\text{-jets (AK3), } 40 < p_T < 320 \text{ GeV}$	Jet fragmentation function
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1809.08602	2.76 TeV	pp/PbPb	Dijet	$q\text{-jets (AK3), } p_T > 30 \text{ GeV}$	Jet shapes
HIN-19-003	2.76 TeV	pp/PbPb	Dijet	$q/g\text{-jets (AK4), } p_T > 50 \text{ GeV}$	Jet shapes
QCD-10-041	7 TeV	pp	Dijet	$q/g\text{-jets (KT6), } 97 < p_T < 1032 \text{ GeV}$	Subjet multiplicities
1706.05868	8 TeV	pp	Inclusive jets	$q/g\text{-jets (AK5), } 400 < p_T < 1500 \text{ GeV}$	Jet charge
2004.00602	5.02 TeV	pp/PbPb	Inclusive jets	$q/g\text{-jets (AK4), } p_T > 120 \text{ GeV}$	Jet charge
1703.06330	8 TeV	pp	$t\bar{t}$	top-jets (CA12), $p_T > 400 \text{ GeV}$	Jet mass
1303.4811	8 TeV	pp	Dijet + W/Z jet	$q/g\text{-jets (AK7), } 220 < p_T < 1500 \text{ GeV}$ $q\text{-jets (AK7, CA8/12), } 125 < p_T < 450 \text{ GeV}$	Nominal + groomed (trimming, pruning, filtering) jet mass
1805.05145	5.02 TeV	pp/PbPb	Inclusive jets	$q/g\text{-jets (AK4), } 140 < p_T < 300 \text{ GeV}$	Soft-drop jet mass
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1808.07340	13 TeV	pp	$t\bar{t}$	$q\text{-jets (AK4), } p_T > 30 \text{ GeV}$ $g\text{-jets (AK4), } p_T > 30 \text{ GeV}$ $b\text{-jets (AK4), } p_T > 30 \text{ GeV}$	Jet substructure and soft-drop observables
SMP-20-010	13 TeV	pp	Dijet, Z+jets	$q/g\text{-jets (AK4), } 50 < p_T < 4000 \text{ GeV}$ $q\text{-jets (AK4), } 50 < p_T < 4000 \text{ GeV}$	Jet angularities

$$z = \frac{p_{\parallel}^{\text{track}}}{p_{\perp}^{\text{jet}}}, \quad \xi = \ln \frac{1}{z},$$

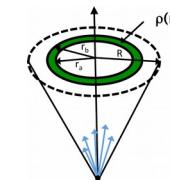


List of jet substructure measurements in CMS

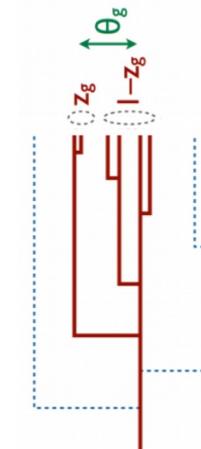


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Highlight of today's talk					
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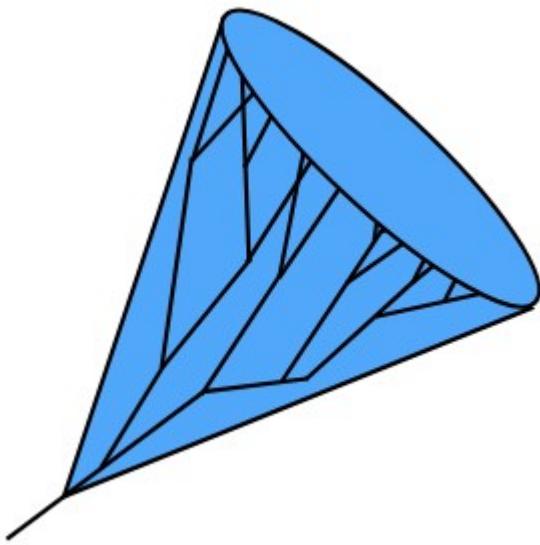


List of jet substructure measurements in CMS



Highlight of today's talk

Jet substructure measurements in CMS



Observables

Generalized angularities

$$\lambda_{\beta}^{\kappa} = \sum_{i \in jet} (z_i)^{\kappa} (\theta_i)^{\beta}$$

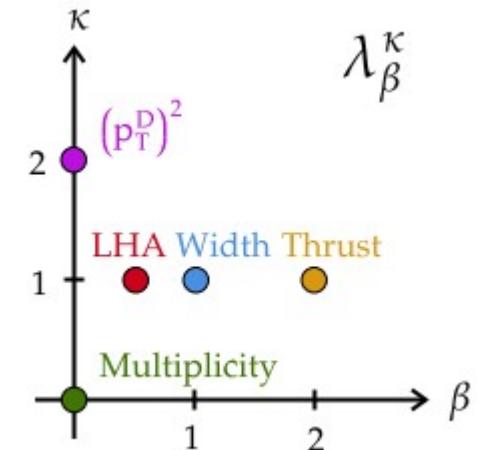
$$z_i = p_{T,i} / \sum p_{T,j}$$

$$\theta_i = \Delta R_{i,\hat{n}} / R_{jet}$$

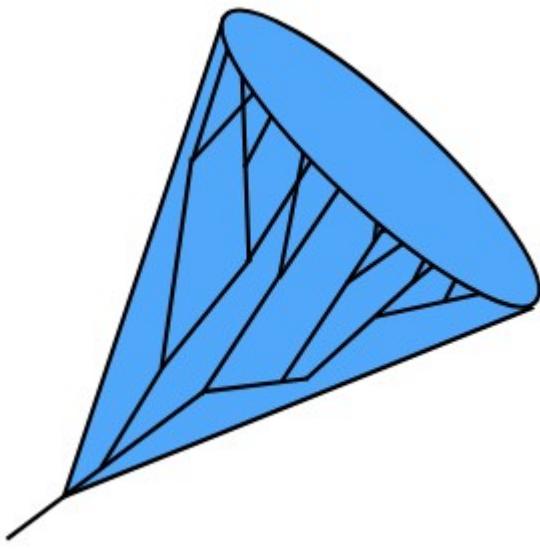
n: jet axis

$\beta \leq 1$: Winner-takes-all (WTA) axis

$\beta > 1$: Anti- k_T axis



Jet substructure measurements in CMS



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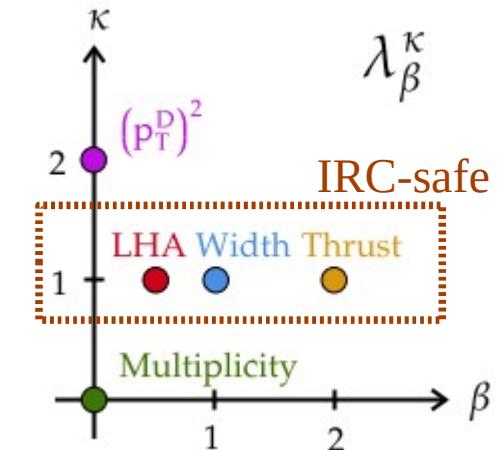
$$\theta_i$$

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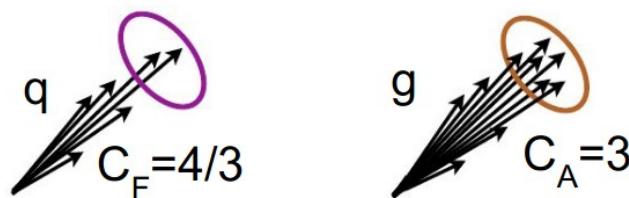
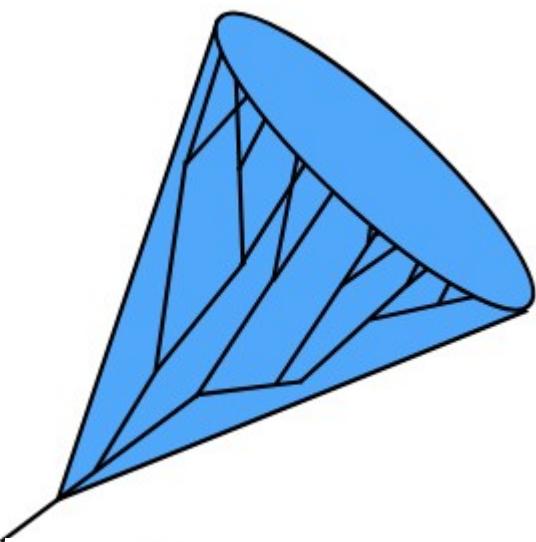
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Jet substructure measurements in CMS



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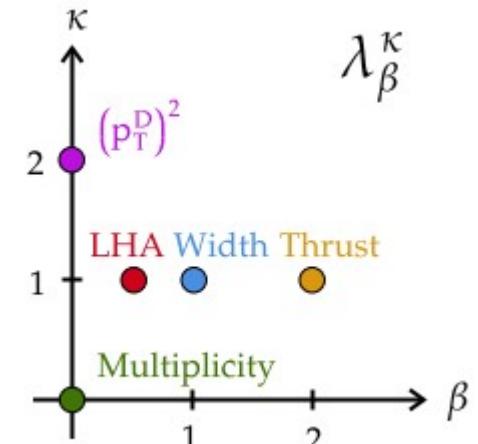
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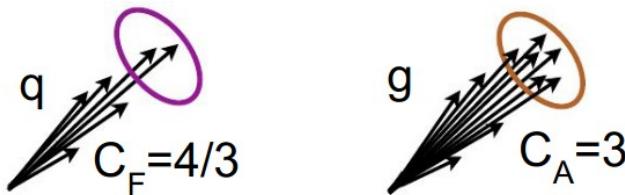
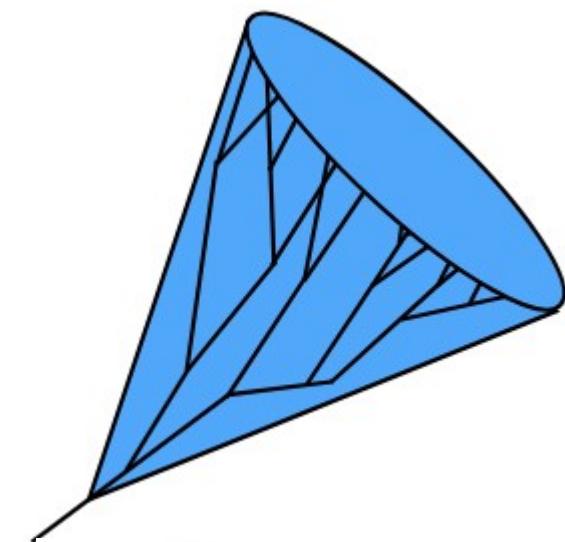


$\beta \leq 1$: Winner-takes-all (WTA) axis

$\beta > 1$: Anti- k_T axis

← Sensitive to differences between quark & gluon jets

Jet substructure measurements in CMS



Observables

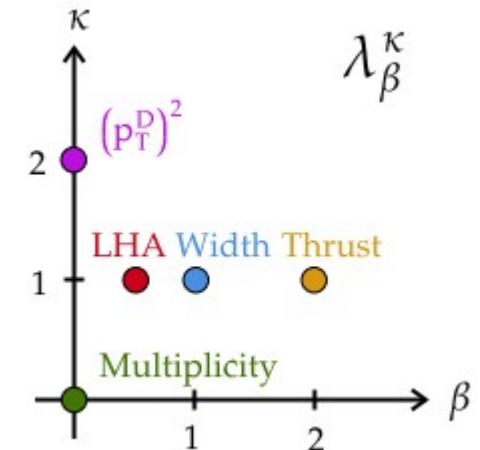
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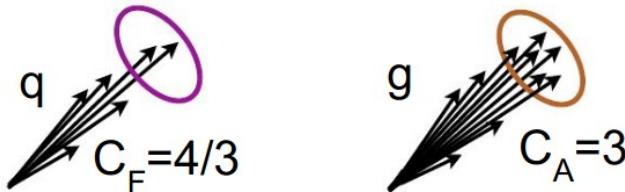
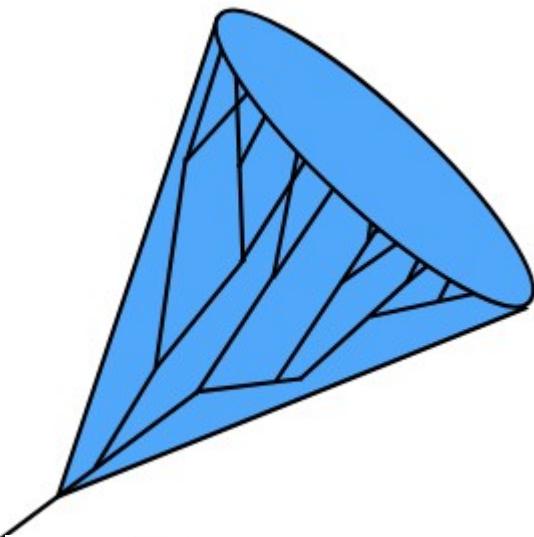


$\beta \leq 1$: Winner-takes-all (WTA) axis
 $\beta > 1$: Anti- k_T axis

Measurements: Five λ_{κ}^{β} variables in quark- and gluon-enriched jet samples
 (results reported in particle-level)

Study motivated by JHEP 1707 (2017) 091 (Gras et al.)

Jet substructure measurements in CMS

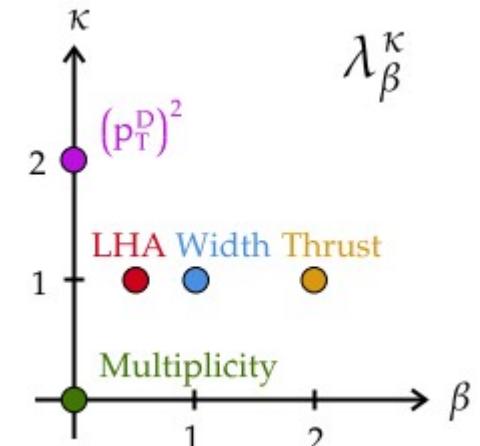


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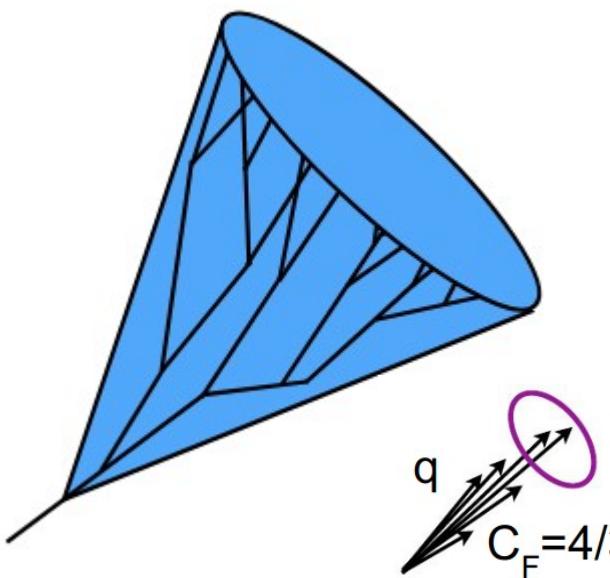


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Measurements: Five λ_{κ}^{β} variables in quark- and gluon-enriched jet samples
(results reported in particle-level)

Purpose: Detailed understanding of jet composition & its modeling
(not designing a quark-gluon tagger)

Jet substructure measurements in CMS



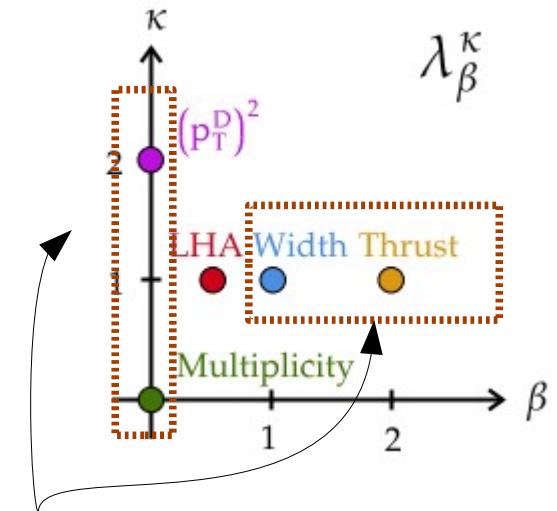
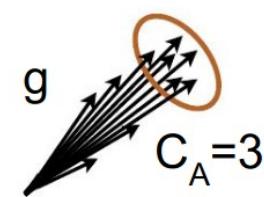
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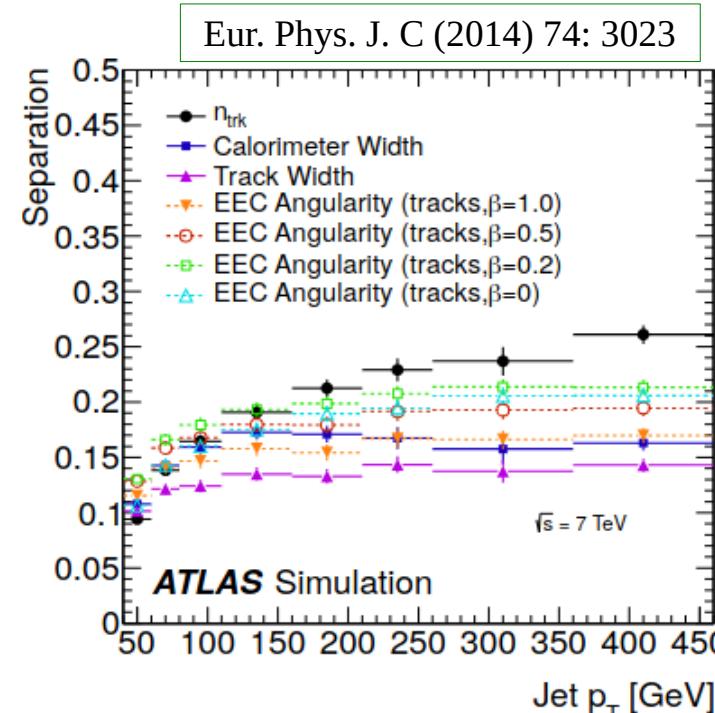
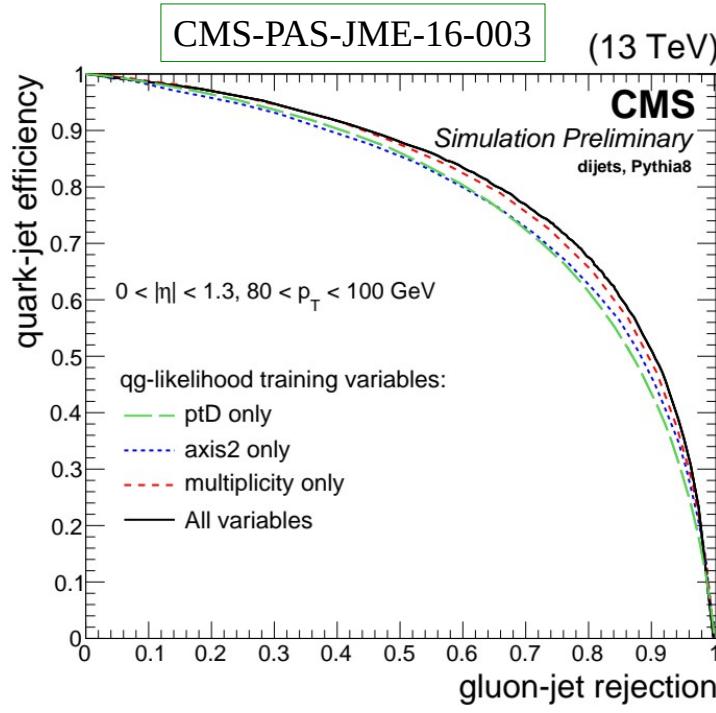
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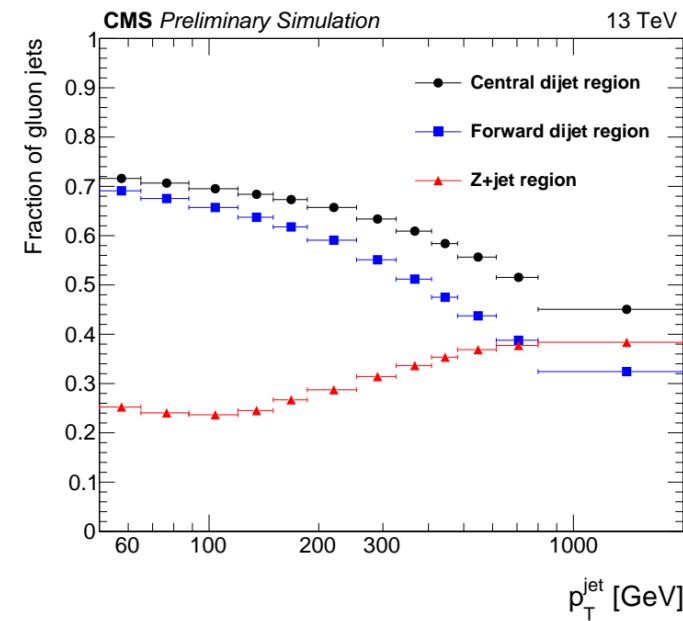
$$\theta_i = \Delta R_{i,\hat{n}} / R_{jet}$$



Used by experiments for quark-gluon tagging



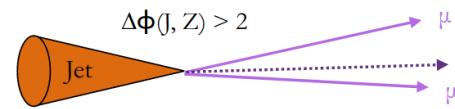
Quark- and gluon-enriched event samples



Quark-enriched jets from $Z(\mu\mu) + \text{jets}$ region:

1+ jets, 2+ muons

Leading jet must pass p_T , $|y|$ cuts,
not overlap with Z muons



$$|p_T(J) - p_T(Z)| / \sum p_T < 0.3$$

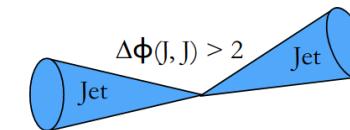
$$|m_{\mu\mu} - 90| < 20 \text{ GeV}$$

$$p_T^{\mu\mu} > 30 \text{ GeV}$$

Gluon-enriched jets from dijet region:

2+ jets

Leading & subleading jets must pass p_T , $|y|$ cuts

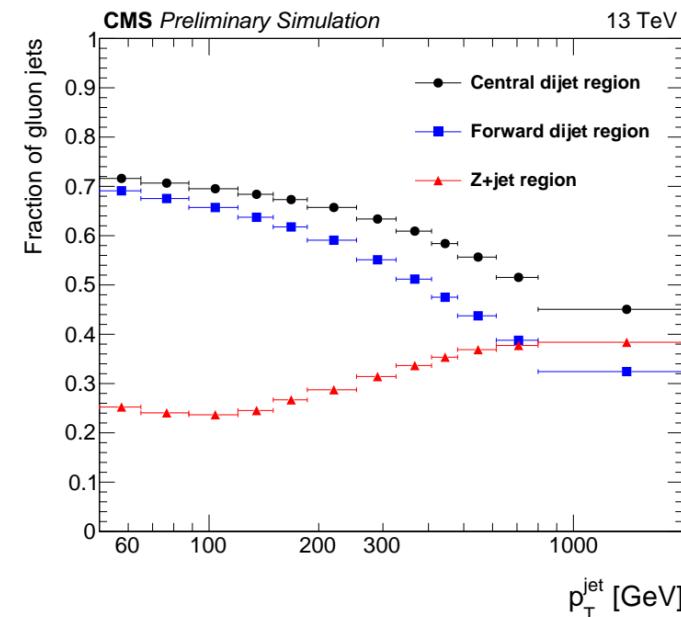


$$\Delta p_T / \sum p_T < 0.3$$

(avoids cutting on 3rd jet explicitly)

CMS-PAS-SMP-20-010

Quark- and gluon-enriched event samples



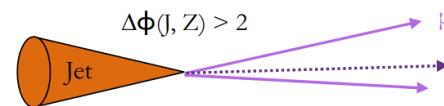
CMS-PAS-SMP-20-010

Small impact of detector response on ratio

Quark-enriched jets from $Z(\mu\mu) + \text{jets}$ region:

1+ jets, 2+ muons

Leading jet must pass $p_T, |y|$ cuts,
not overlap with Z muons

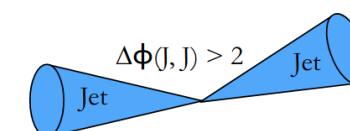


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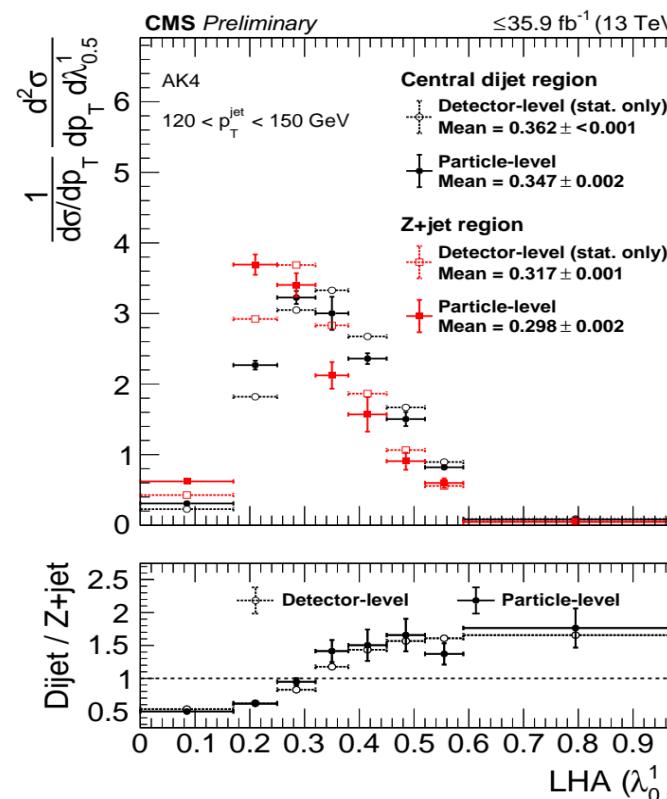
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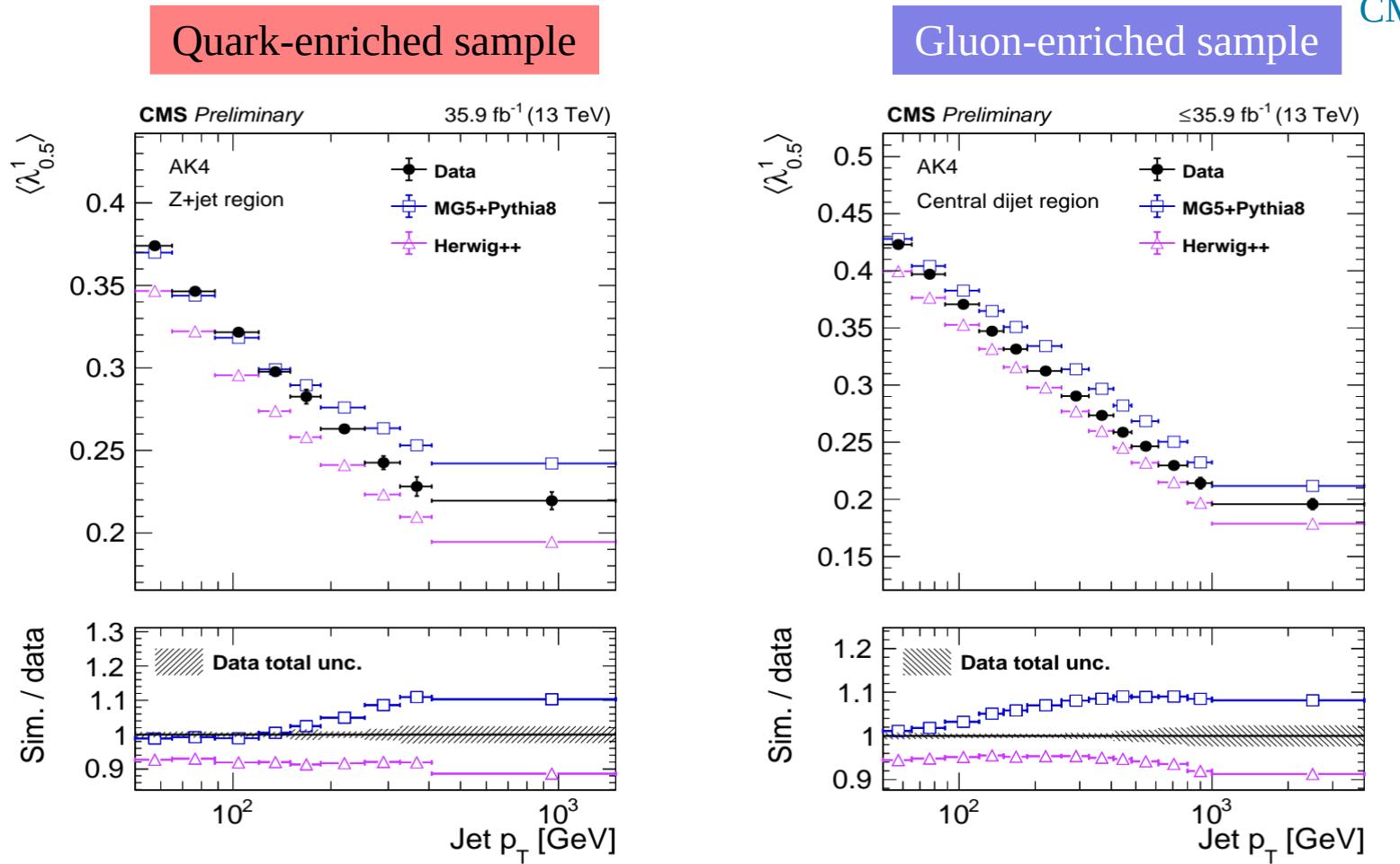
$\Delta p_T / \sum p_T < 0.3$
(avoids cutting on 3rd jet explicitly)



Statistical + systematic uncertainty
 $\sim 5\%$

Radiation more spread out in gluon jet
 \rightarrow Larger value of LHA

Differential distributions at particle-level



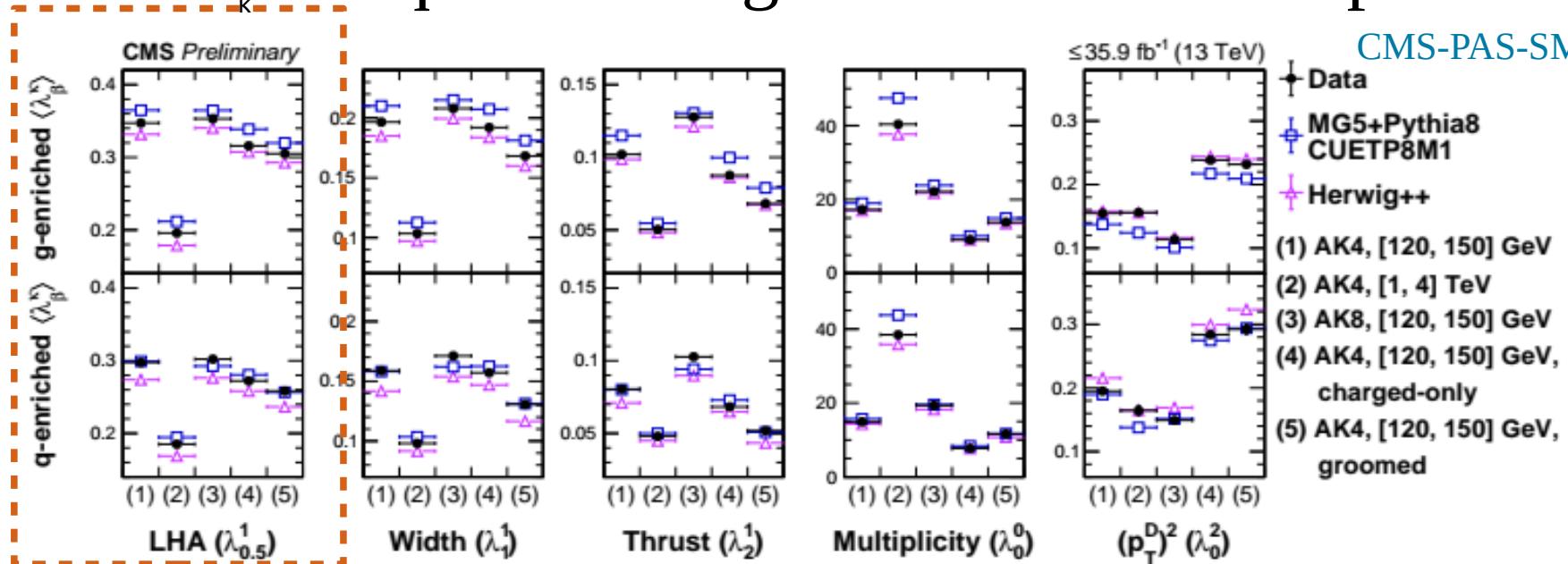
Good modeling of data by PYTHIA parton shower in quark-enriched samples

PYTHIA & HERWIG++ on opposite sides of data in gluon-enriched samples

HERWIG++ describes the p_T -dependence well but underestimates normalization

$\langle \lambda^\beta \rangle$ in quark- and gluon-enriched samples

CMS-PAS-SMP-20-010



Measurements in

Event sample

Inputs from jet

Jet size

Grooming

Energy

Dijet (central)

All particles in jet

AK4

No grooming

In ranges of
(ungroommed) jet p_T
(50 GeV → 1 TeV)

Dijet (forward)

Charged particles only

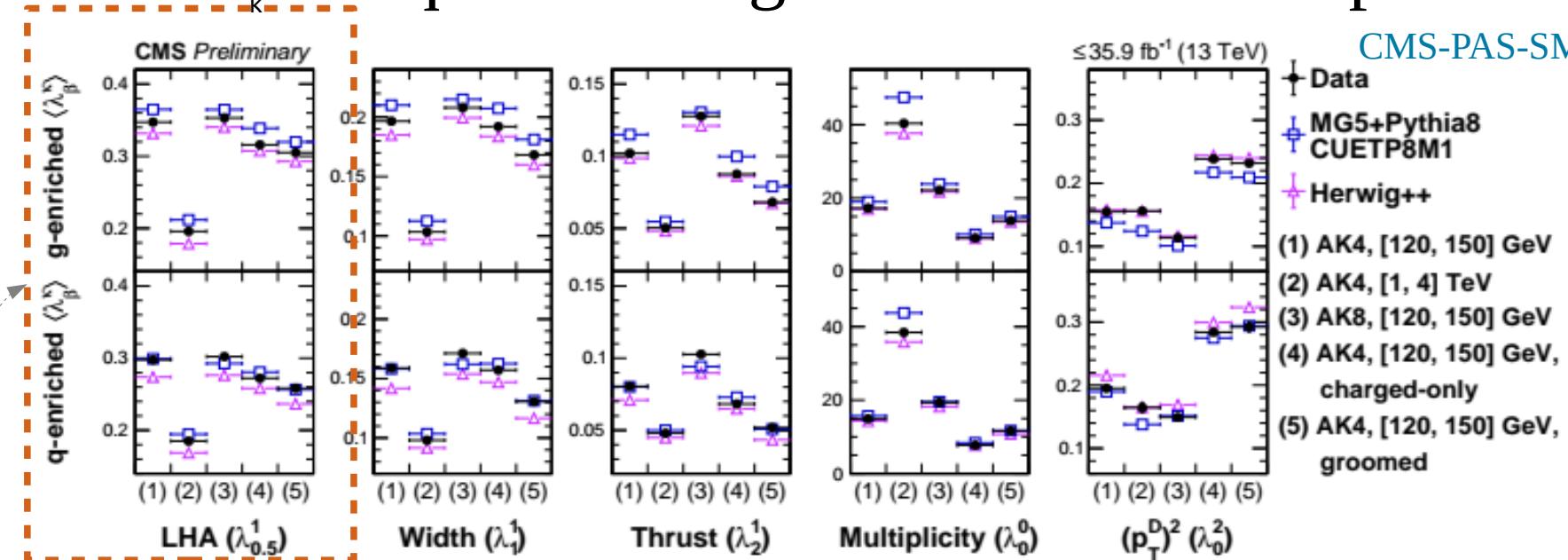
AK8

Soft drop
($z_{\text{cut}} = 0.1, \beta = 0$)

Z+ jet

$\langle \lambda^\beta \rangle$ in quark- and gluon-enriched samples

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Event sample

Jet composition

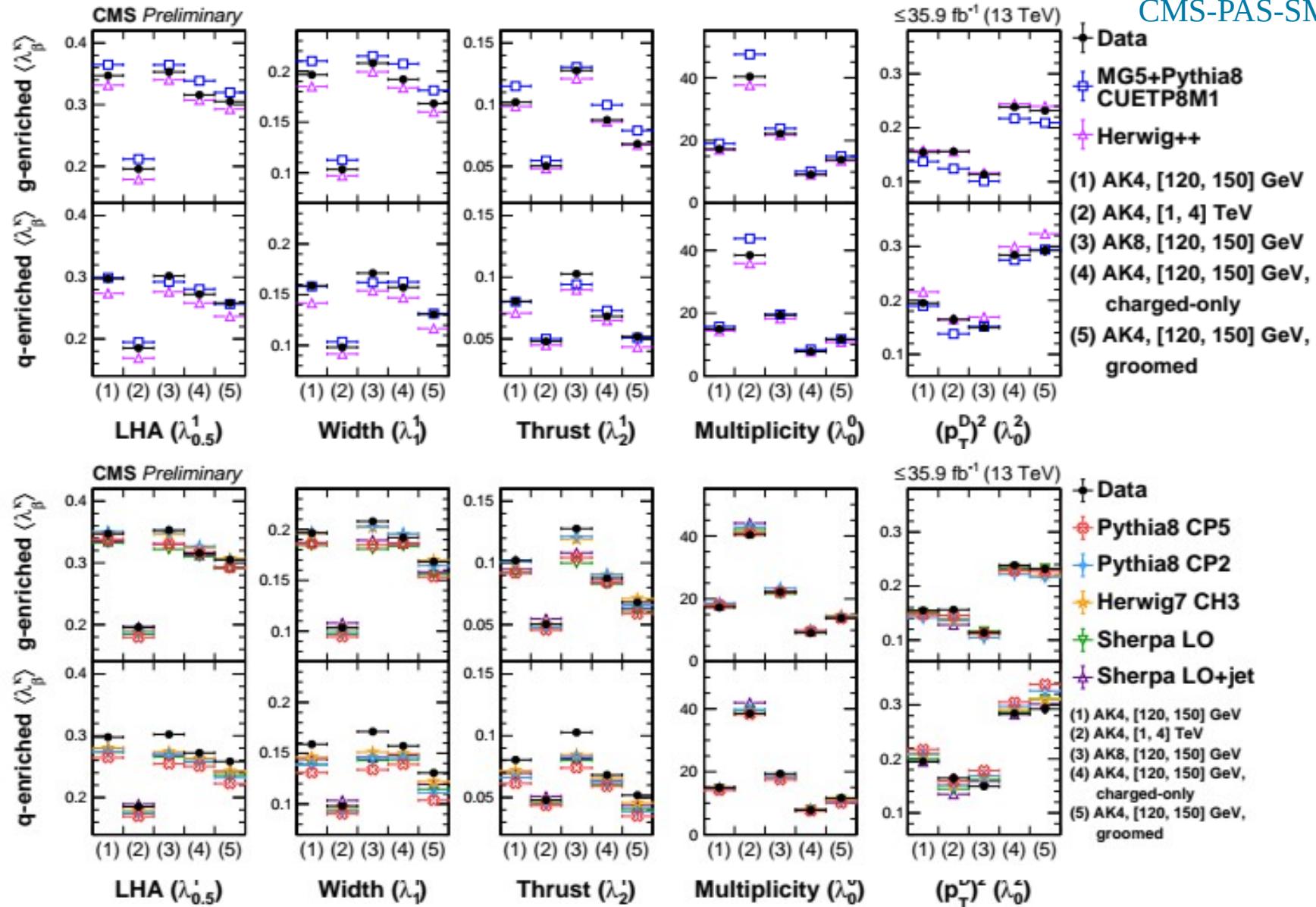
Dijet (central) \longrightarrow g-enriched

Dijet (forward) \longrightarrow q-enriched at [1, 4] TeV

Z+ jet \longrightarrow q-enriched at [120, 150] GeV

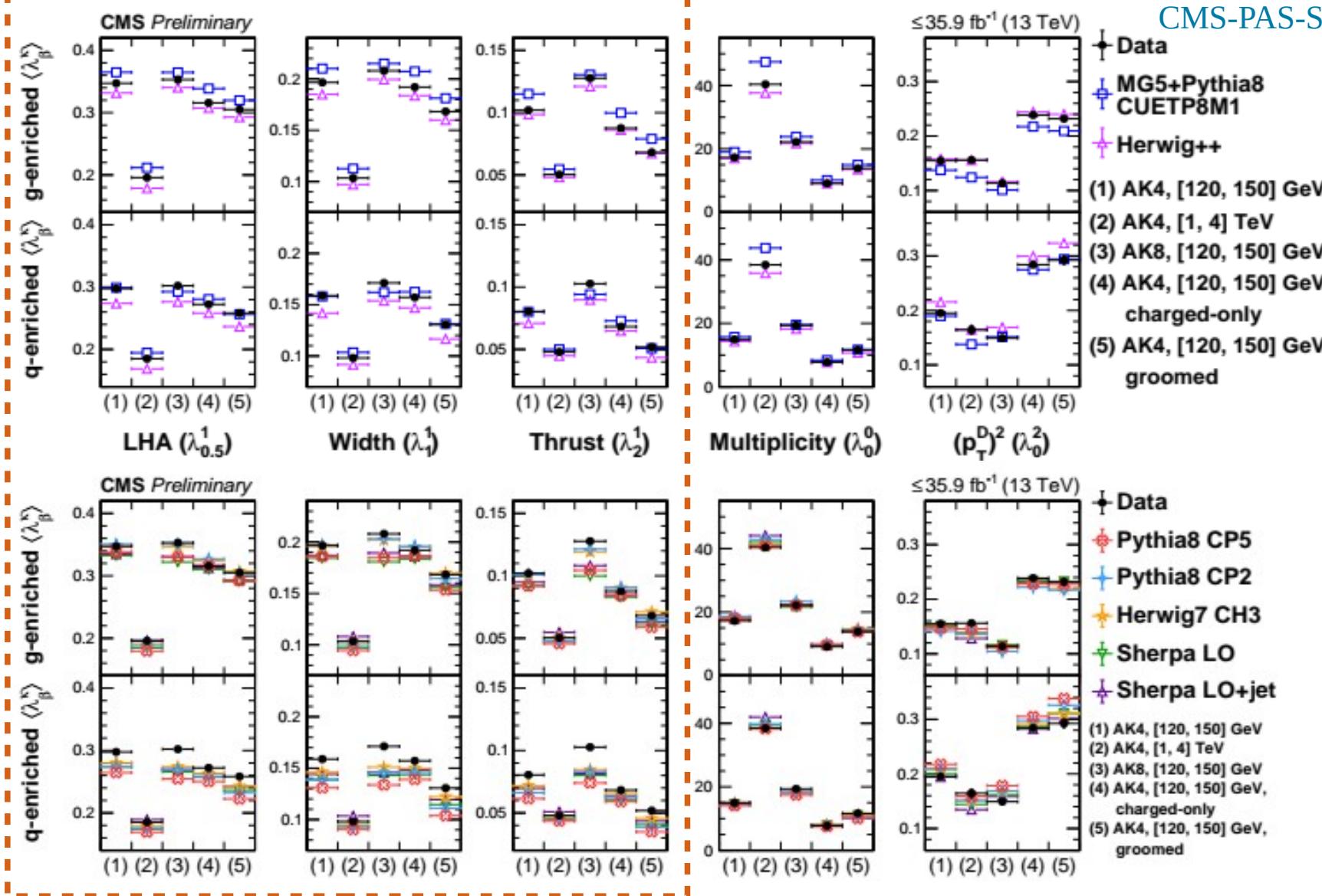
$\langle \lambda_\beta^\beta \rangle$ in quark- and gluon-enriched samples

CMS-PAS-SMP-20-010



$\langle \lambda^\beta \rangle$ in quark- and gluon-enriched samples

CMS-PAS-SMP-20-010

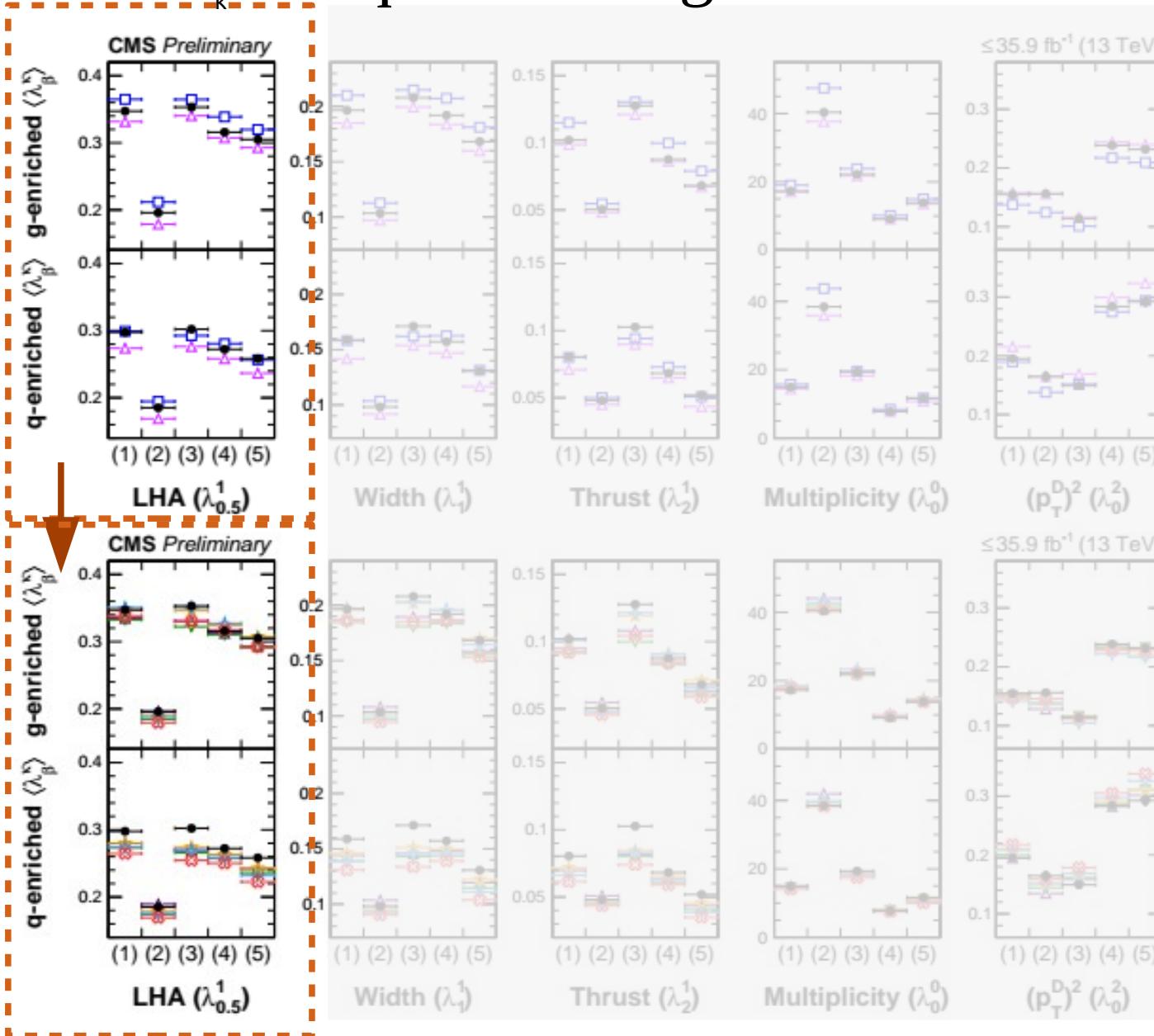


- IRC-safe variables not necessarily better modeled

=> Mismodeling by generators not only in non-perturbative region

$\langle \lambda^\beta \rangle$ in quark- and gluon-enriched samples

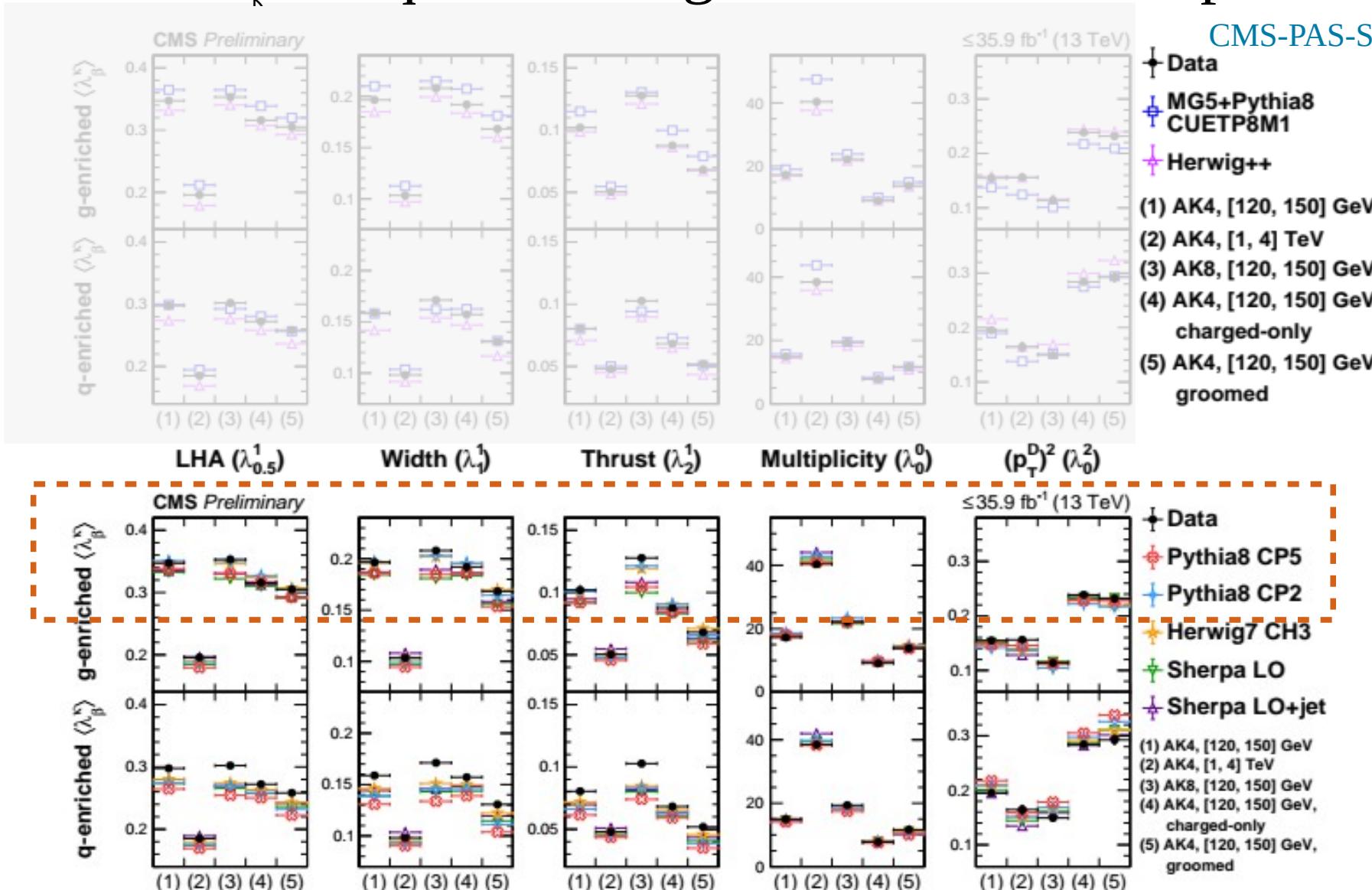
CMS-PAS-SMP-20-010



- Better modeling of gluon-enriched samples in modern generators + UE tunes

$\langle \lambda_\beta^\beta \rangle$ in quark- and gluon-enriched samples

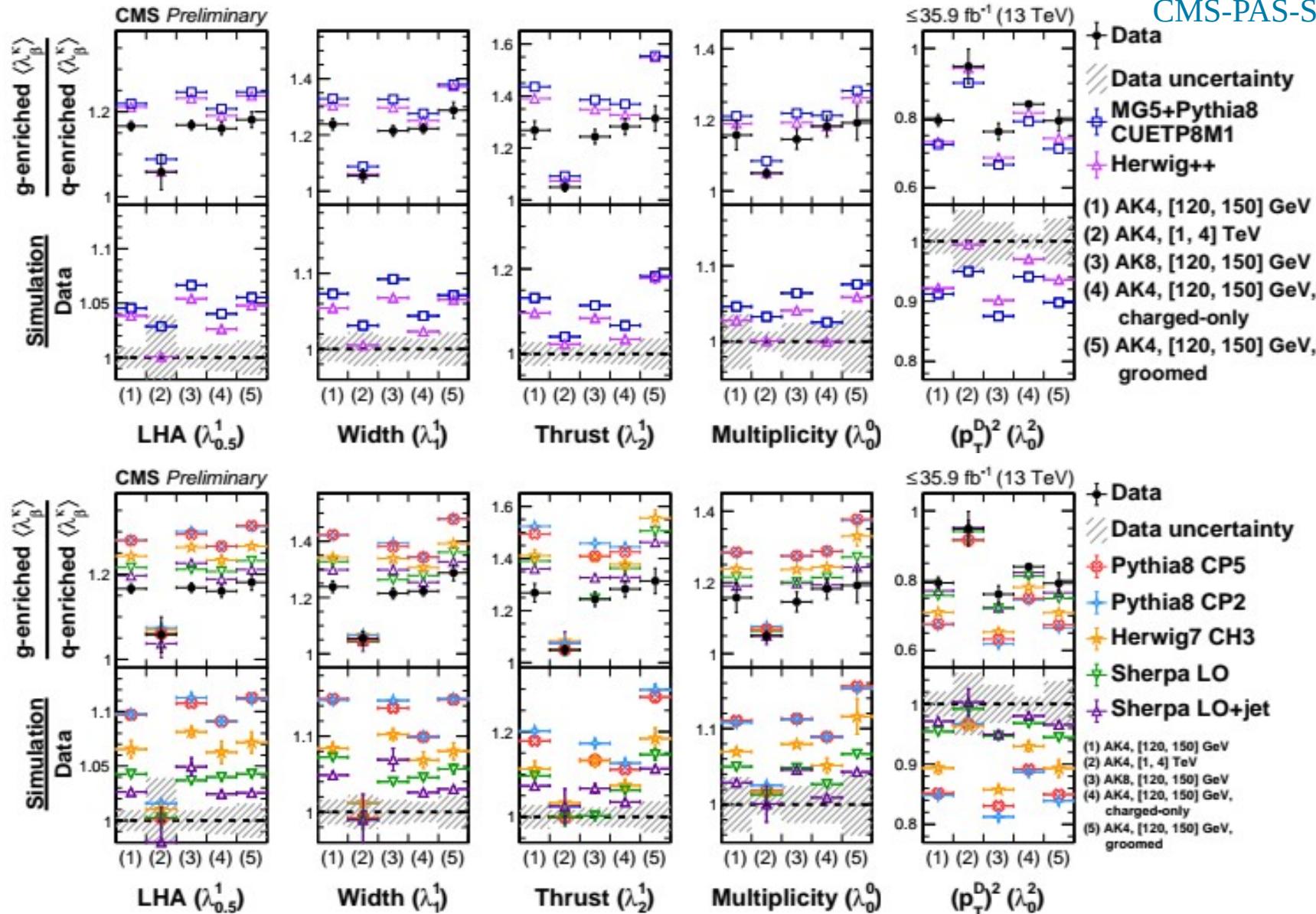
CMS-PAS-SMP-20-010



- CP2 tune describes gluon-enriched samples better than CP5 tune
 (larger α_s & smaller color reconnection range in CP2)

Quark-gluon discrimination power in λ_K^β

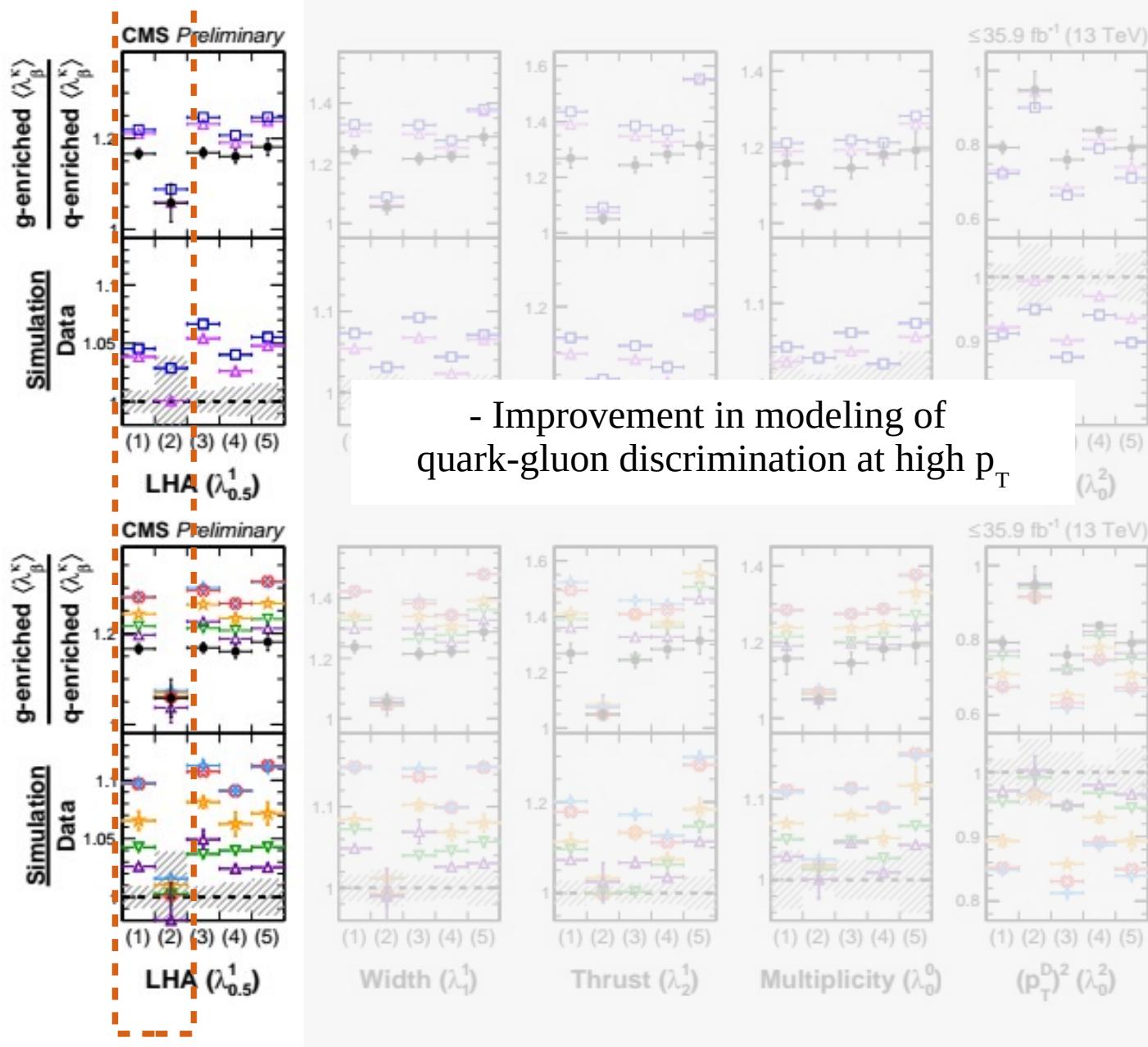
CMS-PAS-SMP-20-010



- Overestimation of quark-gluon discrimination by all the generators (except for λ_0^2)
- Sherpa LO+jet simulation is the closest to data

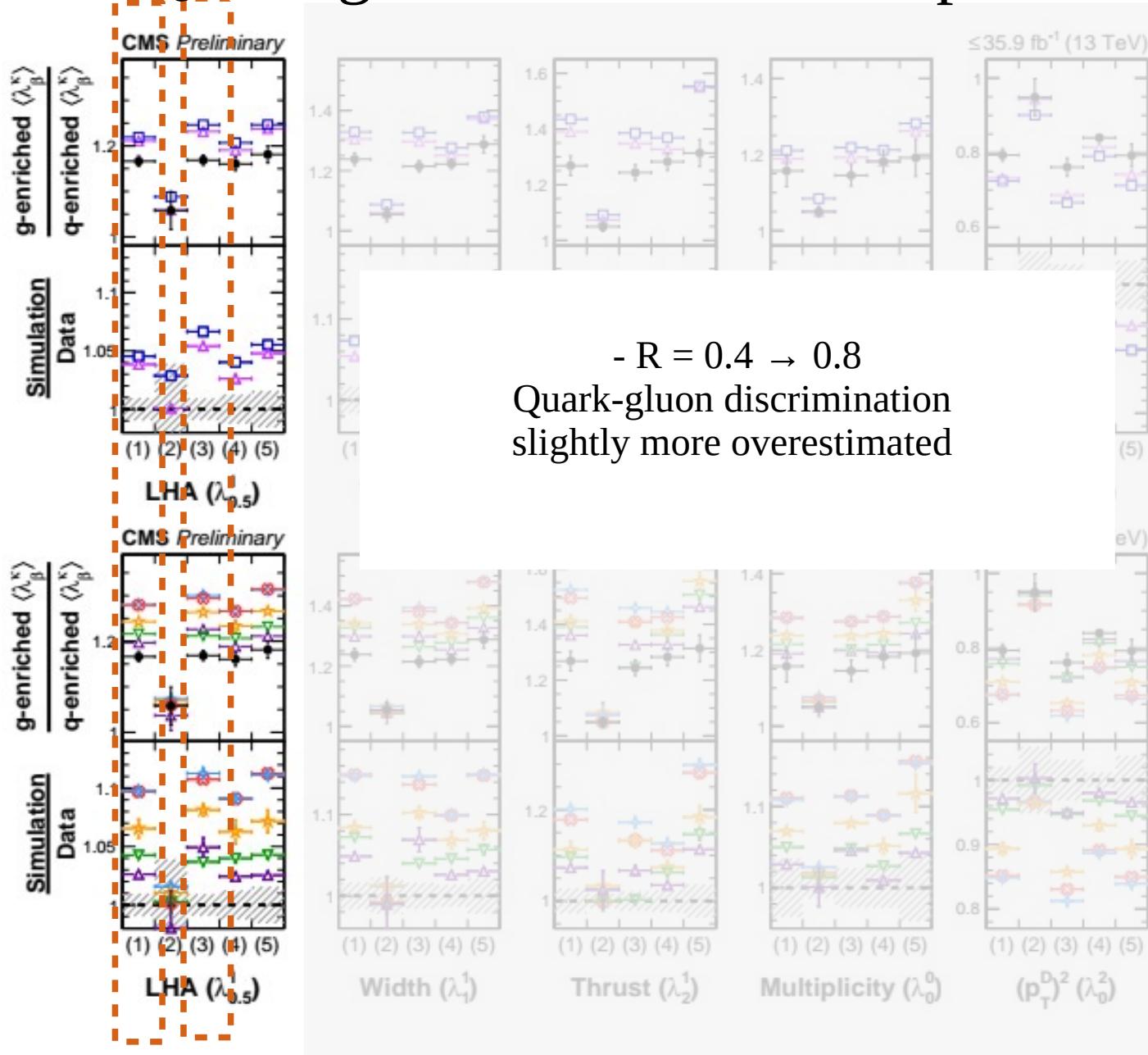
Quark-gluon discrimination power in λ_K^β

CMS-PAS-SMP-20-010



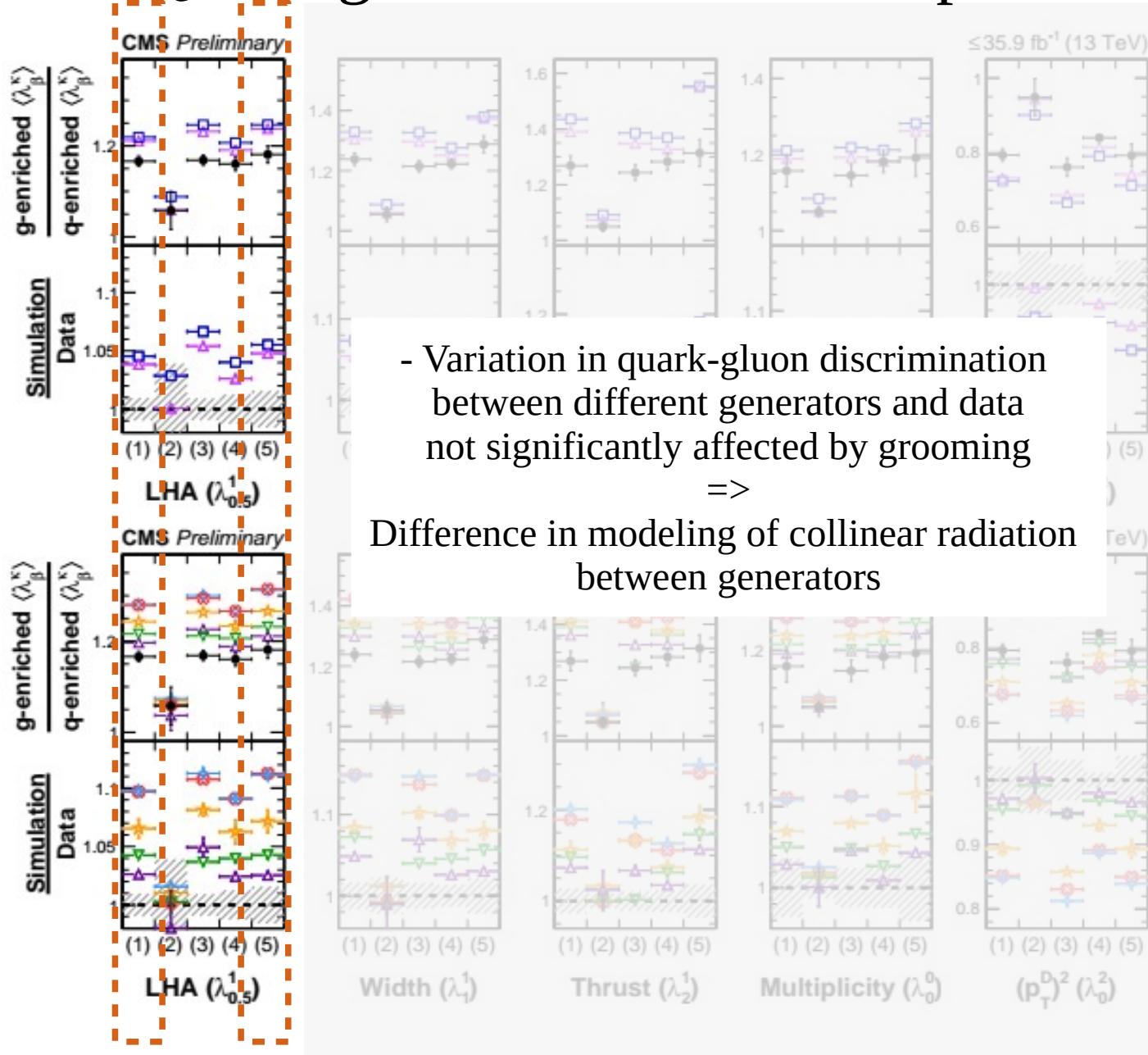
Quark-gluon discrimination power in λ_K^β

CMS-PAS-SMP-20-010



Quark-gluon discrimination power in λ_K^β

CMS-PAS-SMP-20-010



- Variation in quark-gluon discrimination between different generators and data not significantly affected by grooming
=>

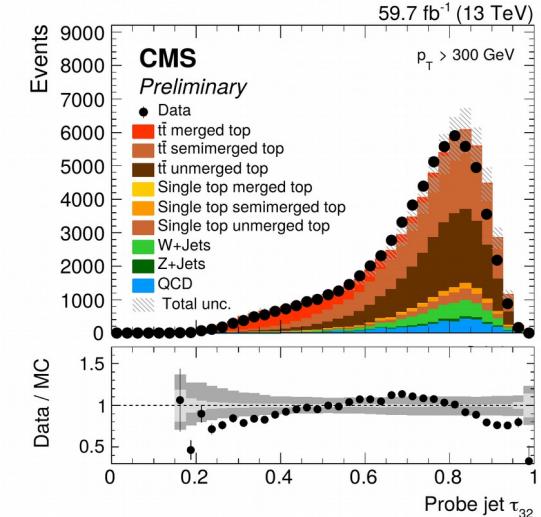
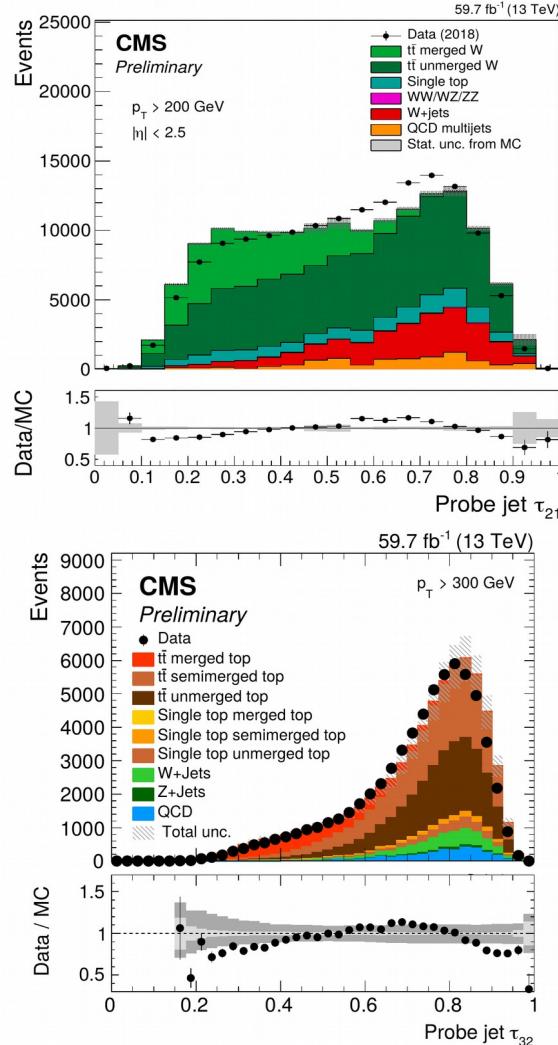
Difference in modeling of collinear radiation between generators

W & top jet identification with n-subjettiness ratio

$\tau_{n(n-1)} = \tau_n / \tau_{n-1}$ measures consistency of jet with n-prong structure

$\tau_{21} \rightarrow W$ tagging
 $\tau_{32} \rightarrow$ top tagging

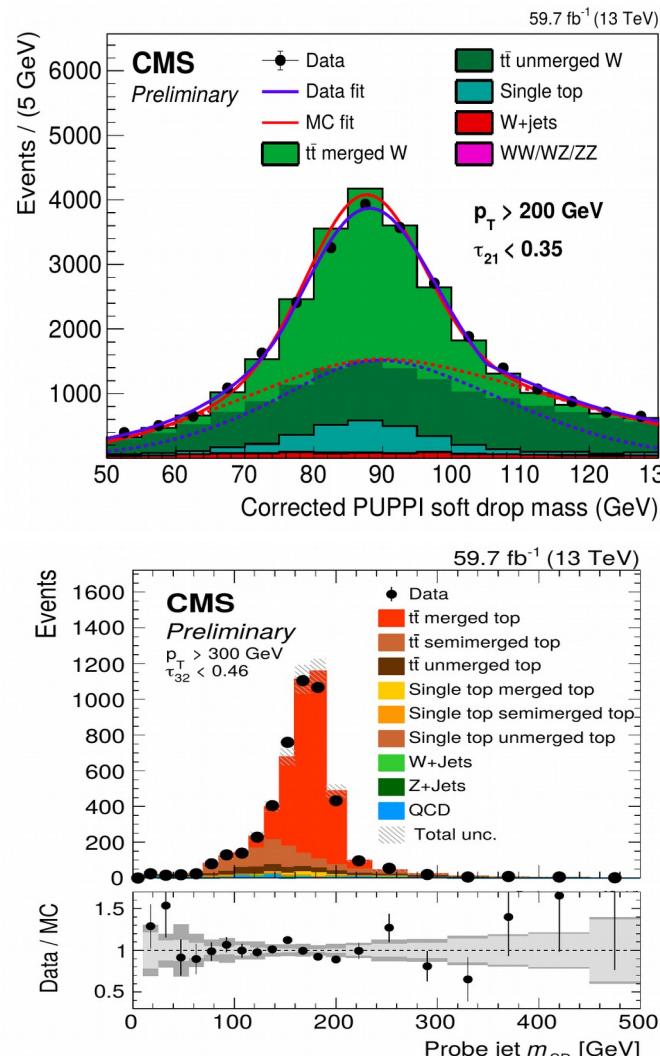
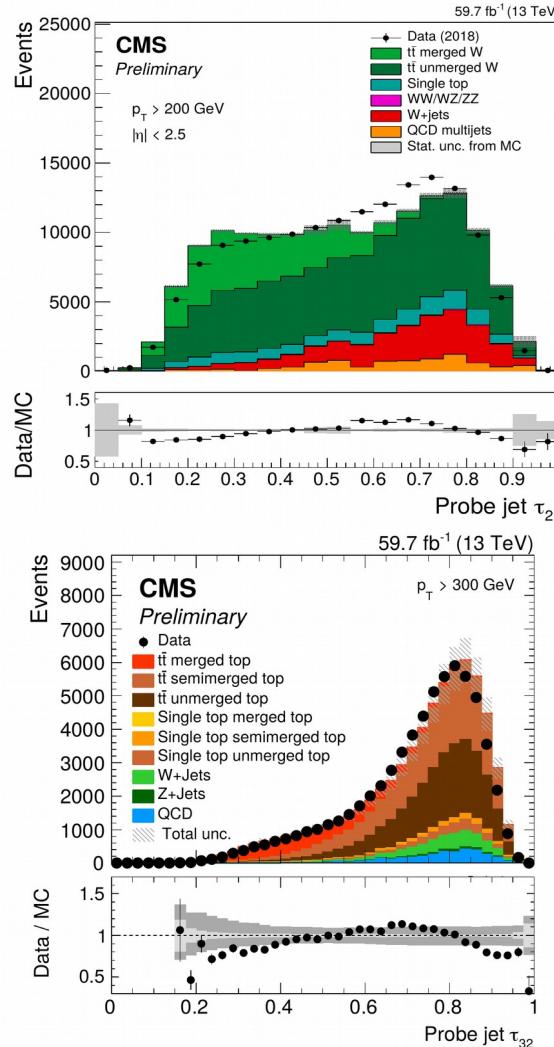
CMS-DP-20-025



- Measurements in muon + jets events (dominated by semileptonic $t\bar{t}$)
- Room for improvement of description by simulation

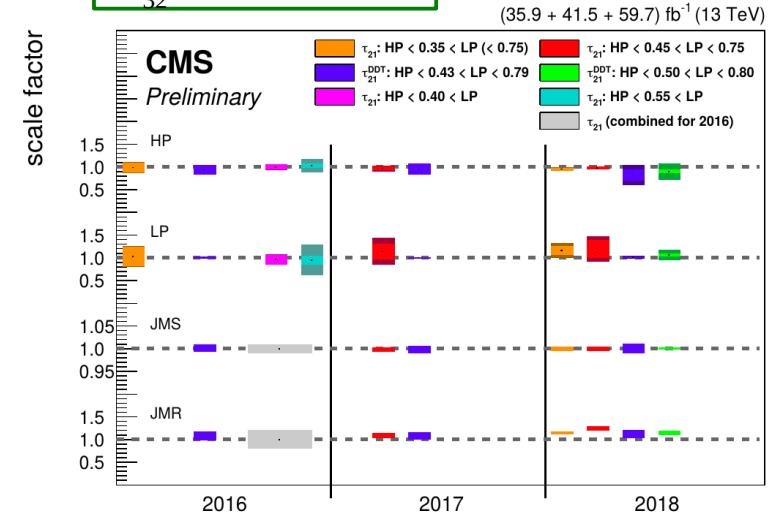
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CMS-DP-20-025

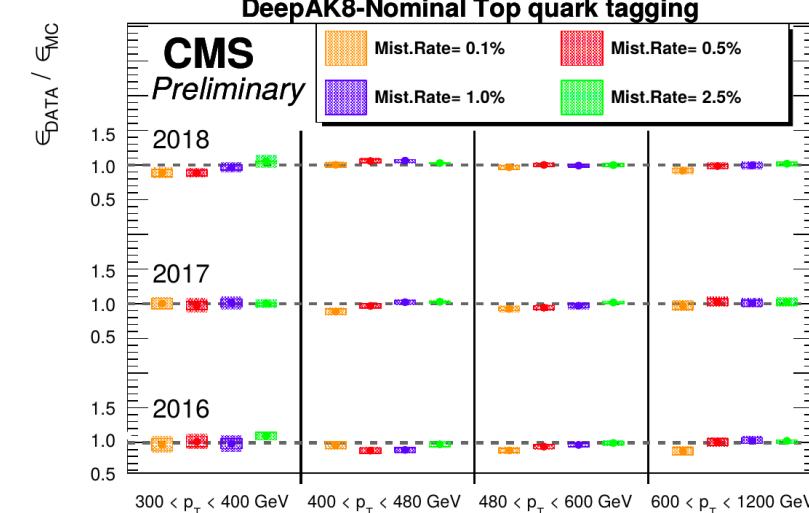
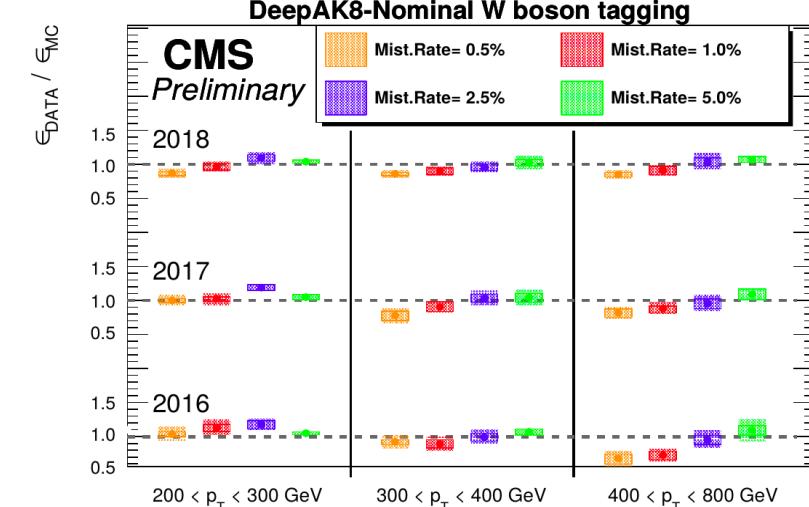
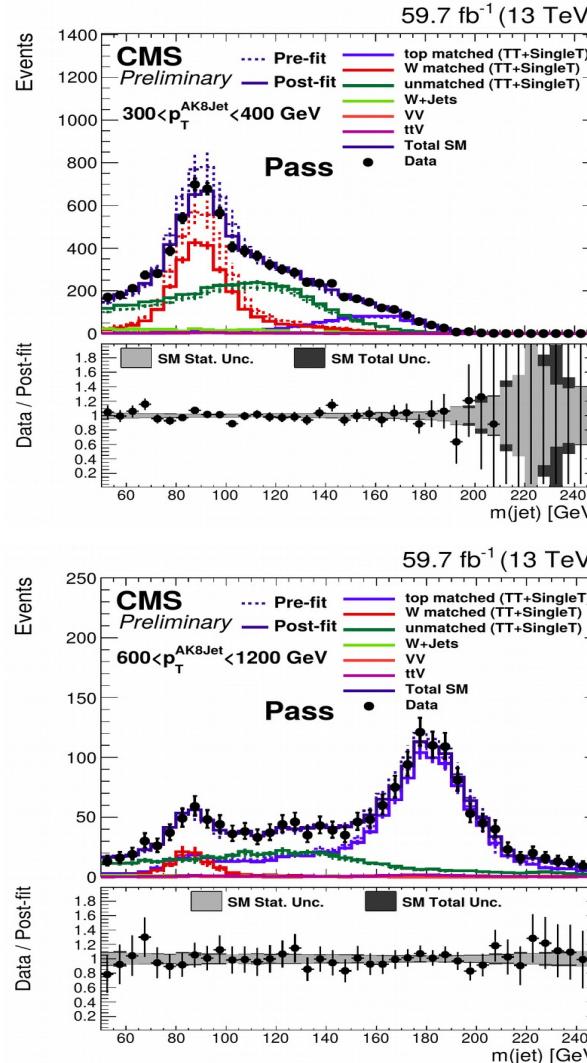
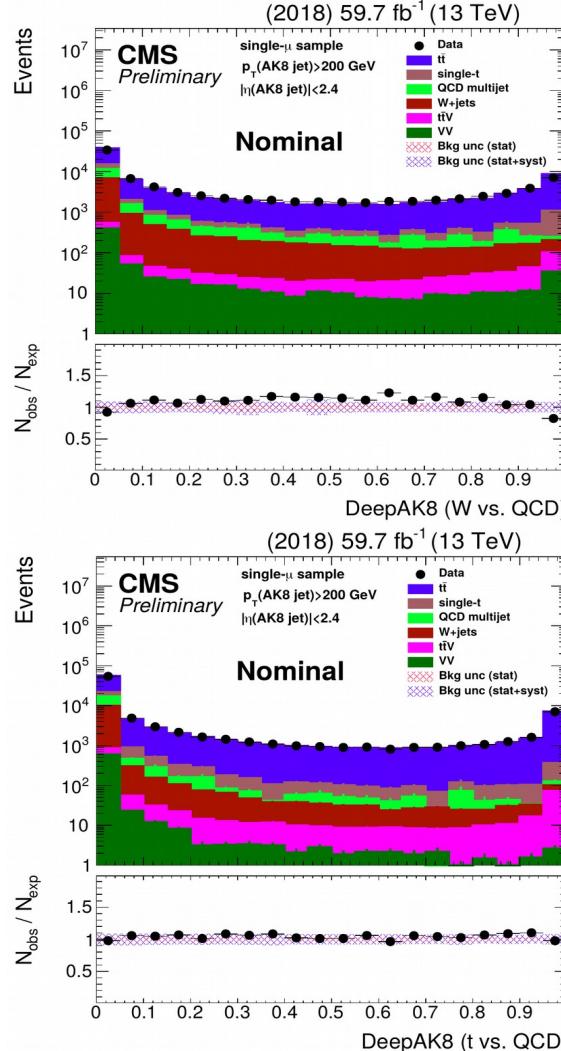


- Measurements in muon + jets events (dominated by semileptonic $t\bar{t}$)
- Room for improvement of description by simulation
- Tagging efficiencies (measured using tag-and-probe method) are similar in data & simulation

W & top jet identification with DeepAK8 tagger

DNN-based tagger using (almost) all the particles & secondary vertices in AK8 jet

CMS-DP-20-025



- Measurements in muon + jets events (dominated by semileptonic tt)
- Moderately good description by simulation
- Tagging efficiencies (measured using tag-and-probe method) are similar in data & simulation

See applications in [Anna Benecke's talk](#)

Details of DeepAK8 tagger in
JINST 15 (2020) P06005

Summary and Outlook

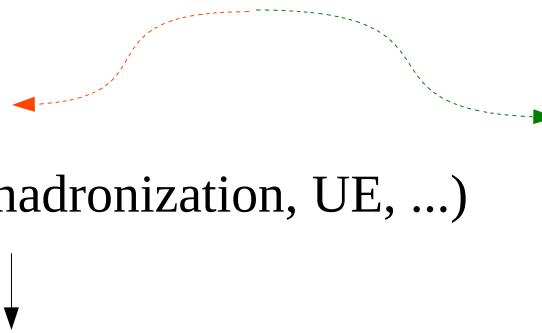
- A detailed study of jet substructure observables is performed

Useful for

Better modeling of

Parton shower

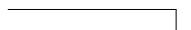
Non-perturbative effects (hadronization, UE, ...)



pQCD calculations

Fixed order + resummation

Handle to reduce modeling uncertainty of particle identifiers
exploiting jet substructure



→ Improve measurements & searches

- Comparison with analytic calculation in progress

[JHEP 07 (2021) 076]

- Calibration measurement performed for
heavy particle taggers

- More measurements are coming soon!

Summary and Outlook

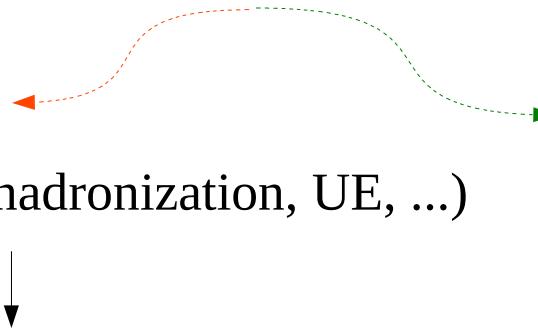
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pQCD calculations

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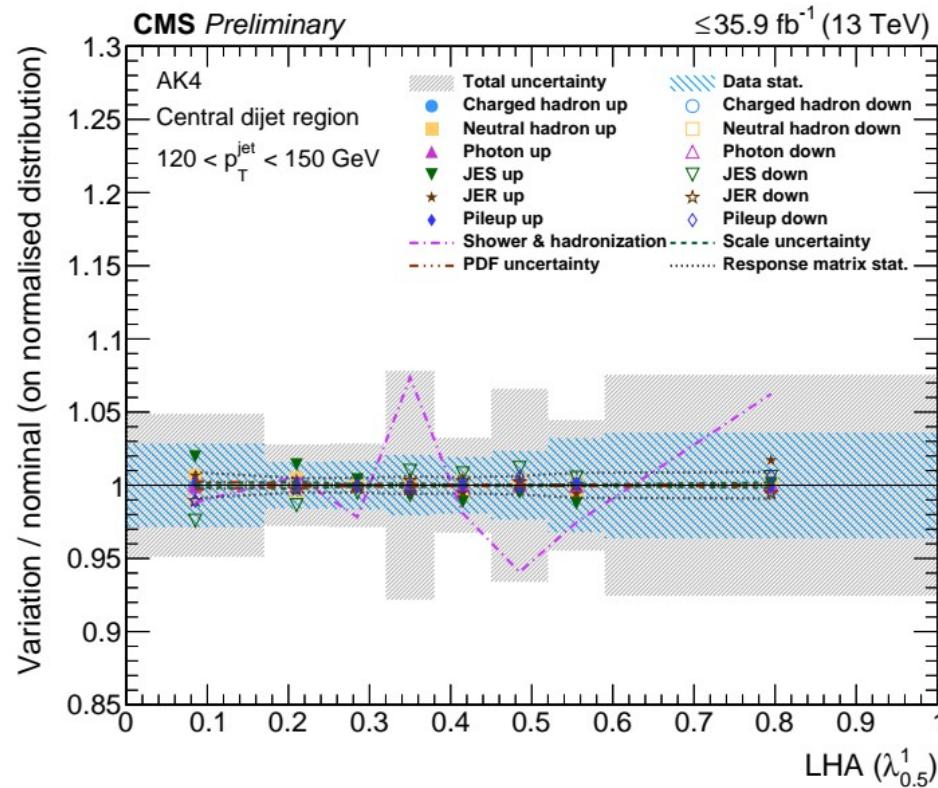
→ Improve measurements & searches

- Comparison with analytic calculation in progress
[JHEP 07 (2021) 076]
- Calibration measurement performed for
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- More measurements are coming soon!



Extra material

Uncertainties in LHA



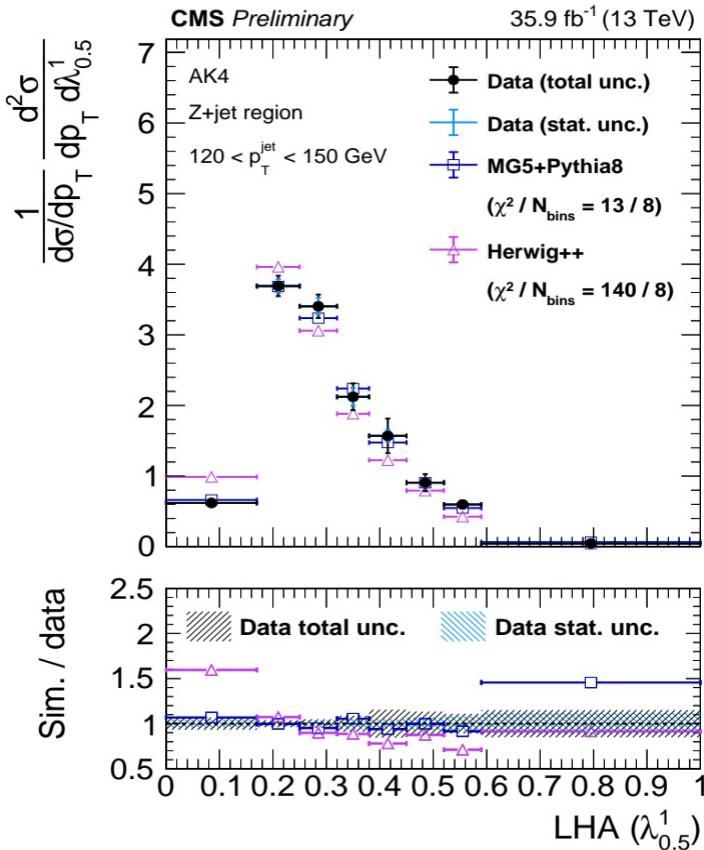
Showering+hadronization uncertainty is the dominant among all the systematic uncertainty sources



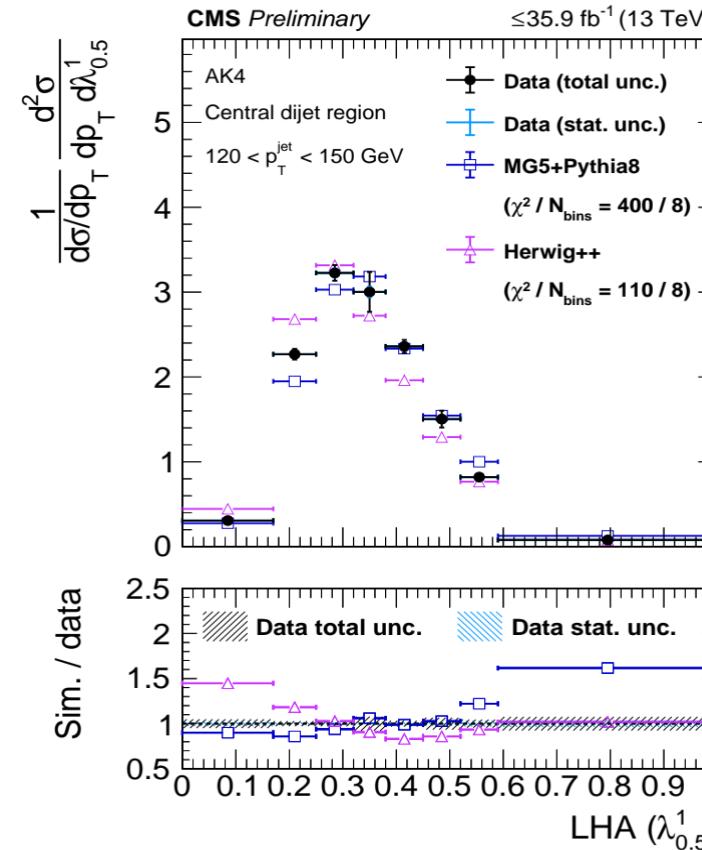
Differences of the unfolded distributions derived using response matrices constructed from MG5+Pythia8 and Herwig++

Differential distributions at particle-level

Quark-enriched sample



Gluon-enriched sample



CMS-PAS-SMP-20-010

Good modeling of data by PYTHIA parton shower in quark-enriched samples

PYTHIA & HERWIG++ on opposite sides of data in gluon-enriched samples

Top tagging efficiency

CMS-DP-20-025

Tagger	Working point	Signal efficiency [%]	Background efficiency [%]
AK8 PUPPI	$\tau_{32} < 0.40$	17	0.2
	$\tau_{32} < 0.46$	26	0.5
	$\tau_{32} < 0.54$	37	1.7
	$\tau_{32} < 0.65$	49	5.1
	$\tau_{32} < 0.80$	62	15.9
AK8 PUPPI + subjet btag	$\tau_{32} < 0.40$	16	0.1
	$\tau_{32} < 0.46$	23	0.3
	$\tau_{32} < 0.54$	33	0.6
	$\tau_{32} < 0.65$	43	1.8
	$\tau_{32} < 0.80$	53	5.3
HOTVR PUPPI	$\tau_{32} < 0.56$	37	2.6
DeepAK8	Mistag rate 0.1%	37	0.1
	Mistag rate 0.5%	52	0.5
	Mistag rate 1.0%	59	1.0
	Mistag rate 2.5%	67	2.5
DeepAK8 MD	Mistag rate 0.1%	28	0.1
	Mistag rate 0.5%	48	0.5
	Mistag rate 1.0%	57	1.0
	Mistag rate 2.5%	66	2.5

Table 1: The top tagging efficiencies including the respective mass windows are estimated from simulation in 2018 before the template fit for the AK8 PUPPI, HOTVR and DeepAK8 taggers. The efficiencies for signal are measured in $t\bar{t}$ events where the angular distance between the generated top and the probe jet is $\Delta R < 0.6$. Background efficiencies are measured using QCD multijet events. Only events are considered where the probe jet fulfills $480 < p_T < 600$ GeV. The exact values of efficiencies strongly depend on the selection applied. Therefore, the purpose of the presented numbers is to give a rough estimate and comparison between algorithms.

W tagging efficiency

CMS-DP-20-025

Tagger	Working point	Signal efficiency [%]	Background efficiency [%]
AK8 PUPPI	$\tau_{21} < 0.35$	53	2.0
	$\tau_{21} < 0.45$	69	4.7
	$\tau_{21}^{\text{DDT}} < 0.43$	12	0.1
	$\tau_{21}^{\text{DDT}} < 0.50$	32	0.6
DeepAK8	Mistag rate 0.5%	51	0.5
	Mistag rate 1.0%	62	1.0
	Mistag rate 2.5%	74	2.5
	Mistag rate 5.0%	79	5.0
DeepAK8 MD	Mistag rate 0.5%	38	0.5
	Mistag rate 1.0%	50	1.0
	Mistag rate 2.5%	66	2.5
	Mistag rate 5.0%	76	5.0

Table 2: The W tagging efficiencies including the respective mass windows are estimated from simulation in 2018 for the working points of the AK8 PUPPI and DeepAK8 taggers. The efficiencies for signal are measured in $Z' \rightarrow WW$ events where the angular distance between generated W and the probe jet is $\Delta R < 0.6$. Background efficiencies are measured using QCD multijet events. Only events are considered where the probe jet fulfills $300 < p_T < 500$ GeV. The exact values of efficiencies strongly depend on the selection applied. Therefore, the purpose of the presented numbers is to give a rough estimate and comparison between algorithms.