



**UNIVERSITÉ  
DE LYON**

# New constraints on flavour violating supersymmetry

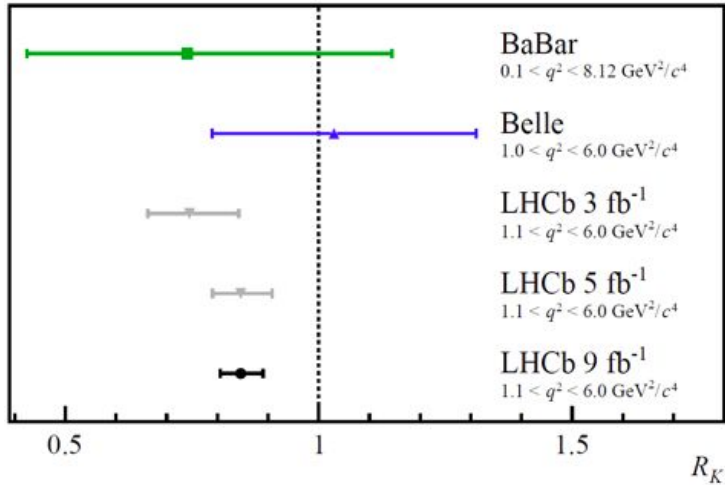
**Mohamed Amine Boussejra (IP2I Lyon, France)**  
Nazila Mahmoudi (Advisor)

EPS-HEP  
Searches for New Physics T10  
26 - 30 July 2021

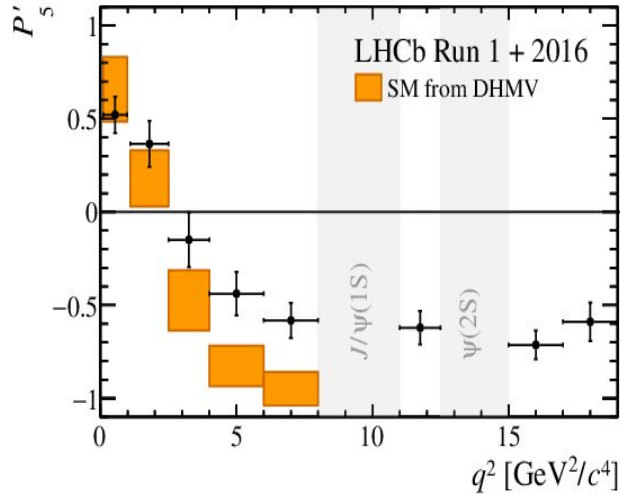
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# Context

# Flavour anomalies and LHCb



$R_K$  latest update (March 2021).  
 $3.1\sigma$  tension with the SM  
[\[2103.11769\]](#)



Tension in  $P'_5$  :  $2.5\sigma$  for  $q^2$  bins :  
 $[4,6[$  for  $2.9\sigma$  for  $[6,8[$ , [\[2003.04831\]](#)

**They are not alone !**

A coherent set of observables present similar tensions:  $R_K$ ,  $BR(B^0 \rightarrow K^* \mu^+ \mu^-)$ , etc.

All observables in the  $b \rightarrow s$  II sector admit a coherent NP fit ([\[2104.10058\]](#), [\[2012.12207\]](#), etc).

$$\mathcal{H}_{\text{eff}} = -\frac{4G_F}{\sqrt{2}} K_{ts}^* K_{tb} \left[ \sum_{i=1}^8 C_i(\mu) O_i + \frac{\alpha}{4\pi} \sum_{i=9}^{10} \tilde{C}_i(\mu) O_i \right] \quad O_9 = (\bar{s}_L \gamma_\mu b_L) \bar{l} \gamma^\mu l$$



# Flavour anomalies in the SUSY context

- Strong and persisting flavour anomalies.
- The flavour structure of the SM is still unexplained.
- Exploration of non-universal flavour models is pertinent.
- No SUSY signal so far at 13 TeV.
- Explored models are simple and heavily constrained, constraints often model dependent
- SUSY contributes to  $C_9$  at +1-loop level -> difficult to significantly reduce its value.

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# Theoretical set-up

- More general than constrained models (e.g. CMSSM).
- Still reasonably small to allow for doable computations.
- Main assumptions :
  - No new source of CP-violation
  - No FCNC
  - Universality of generations 1&2
  - Minimal Flavour Violation (MFV)
- 19 free parameters :

$$\tan \beta, \mu, M_A$$

higgs sector

$$M_1 M_2 M_3$$

gaugino sector

$$m_{\tilde{q}}, m_{\tilde{u}_R}, m_{\tilde{d}_R}, m_{\tilde{l}}, m_{\tilde{e}_R}$$

1/2 generation masses

$$m_{\tilde{Q}}, m_{\tilde{t}_R}, m_{\tilde{b}_R}, m_{\tilde{L}}, m_{\tilde{\tau}_R}$$

3rd generation masses

$$A_t, A_b, A_\tau$$

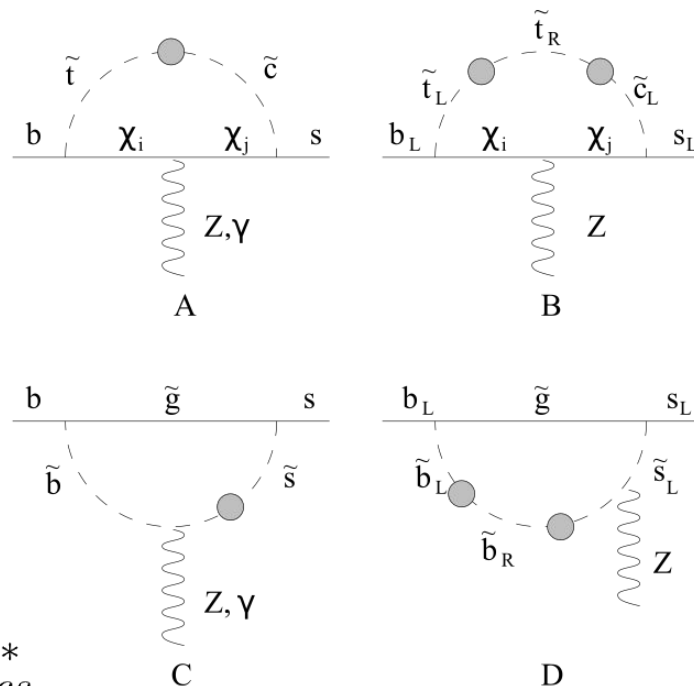
Trilinear couplings

# Non Minimal Flavour Violation and the MIA

- Mass Insertion Approximation in the  $b \rightarrow sll$  context [[9906286](#)]
- Flavour Expansion Theorem [[1504.00960](#)]
- Obtain Feynman rules in flavour basis, expand mass matrices around off-diagonal elements.


$$(m^{\tilde{f}})_{AB}^2 = \begin{pmatrix} ((m^{\tilde{f}})_{AB}^2)_{11} & (\Delta_{AB})_{12} & (\Delta_{AB})_{13} \\ (\Delta_{AB})_{21} & ((m^{\tilde{f}})_{AB}^2)_{22} & (\Delta_{AB})_{23} \\ (\Delta_{AB})_{31} & (\Delta_{AB})_{32} & ((m^{\tilde{f}})_{AB}^2)_{33} \end{pmatrix}$$

$$(\delta_{ij}^f)_{AB} = \frac{(m_{ij}^{\tilde{f}})_{AB}^2}{M_{sq}^2} \quad (C_9)_{\tilde{H}\tilde{W}}^Z \propto (\delta_{23}^u)_{LR} \frac{\lambda_t}{g_2} \frac{K_{cs}^*}{K_{ts}^*}$$



MIA diagrams contributing to  $b \rightarrow sll$ . [[9906286](#)].

# Exploring the parameter space


- 
- NMFV assuming only squark flavour mixing yields up to  $O(70)$  free parameters !
    - Grid Sampling efficiency :  $\sim 0.005\%$
    - ML methods ineffective for unknown distributions
    - Hamiltonian MC could prove efficient but not guaranteed

Needs simplifications for now.

- The **Mass Insertion Approximation** allows to add some flavour mixings and expand around the squark mass matrices.
- Additional parameters up to 10. (no slepton or gen 1-2 mix)  
with the pMSSM parameters ,  $\dim(\text{space}) \sim 30$ .
  - Theoretical constraints on/and parameter distribution known.
  - ML methods efficient for fast inference of parameters and observables.



# Set up

- 
- Parameters are varied over very wide ranges, and sampled from uniform distribution
  - RGE and spectrum performed using public code SOFTSUSY
  - Wilson coefficients and observables are calculated using Superiso (dev version)
  - Only theoretically valid pMSSM points in specific ranges of Wilson coefficients are kept.

# Parameter ranges

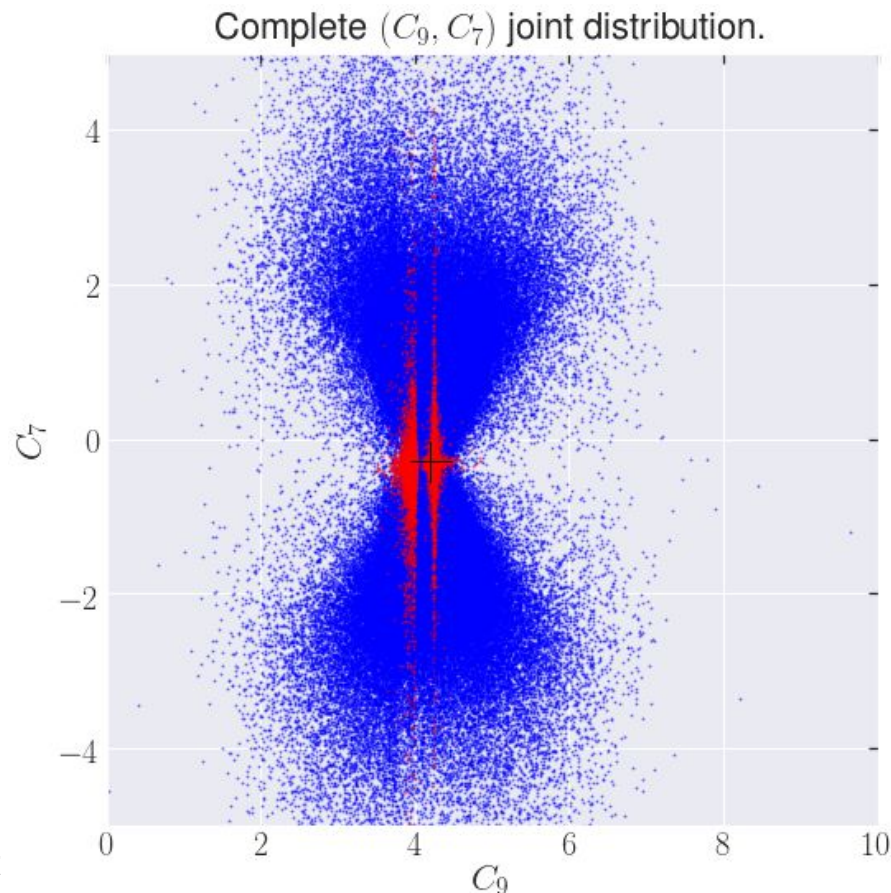
pMSSM parameter	Range		
		$M_{\tilde{e}_L} = M_{\tilde{\mu}_L}$	[50, 5000]
$M_1$	[50, 5000]	$M_{\tilde{e}_R} = M_{\tilde{\mu}_R}$	[50, 5000]
$M_2$	[50, 5000]	$M_{\tilde{\tau}_L}$	[50, 5000]
$M_3$	[50, 5000]	$M_{\tilde{\tau}_R}$	[50, 5000]
$M_A$	[50, 5000]	$M_{\tilde{q}_{1L}} = M_{\tilde{q}_{2L}}$	[50, 5000]
$\tan \beta$	[2, 60]	$M_{\tilde{q}_{3L}}$	[50, 3000]
$\mu$	[-10000, 10000]	$M_{\tilde{u}_R} = M_{\tilde{c}_R}$	[50, 5000]
$A_t$	[-10000, 10000]	$M_{\tilde{d}_R} = M_{\tilde{s}_R}$	[50, 5000]
$A_b$	[-10000, 10000]	$M_{\tilde{t}_R}$	[50, 5000]
$A_\tau$	[-10000, 10000]	$M_{\tilde{b}_R}$	[50, 5000]
			$(\delta_{23}^{\tilde{u}})_{LR}$ [-1, 1]
			$(\delta_{23}^{\tilde{u}})_{LL}$ [-1, 1]
			$(\delta_{33}^{\tilde{u}})_{LR}$ [-1, 1]
			$(\delta_{23}^{\tilde{d}})_{LL}$ [-1, 1]
			$(\delta_{23}^{\tilde{d}})_{RR}$ [-1, 1]
			$(\delta_{23}^{\tilde{d}})_{RL}$ [-1, 1]
			$(\delta_{23}^{\tilde{d}})_{LR}$ [-1, 1]
			$(\delta_{33}^{\tilde{d}})_{RL}$ [-1, 1]
			$(\delta_{33}^{\tilde{d}})_{LR}$ [-1, 1]

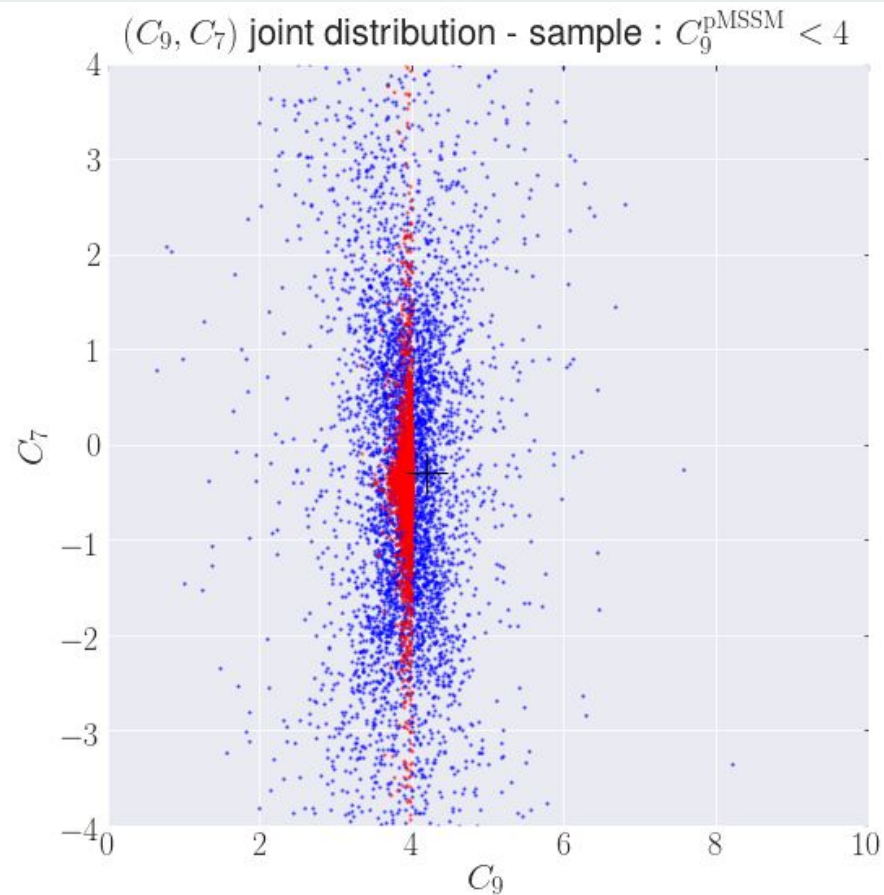
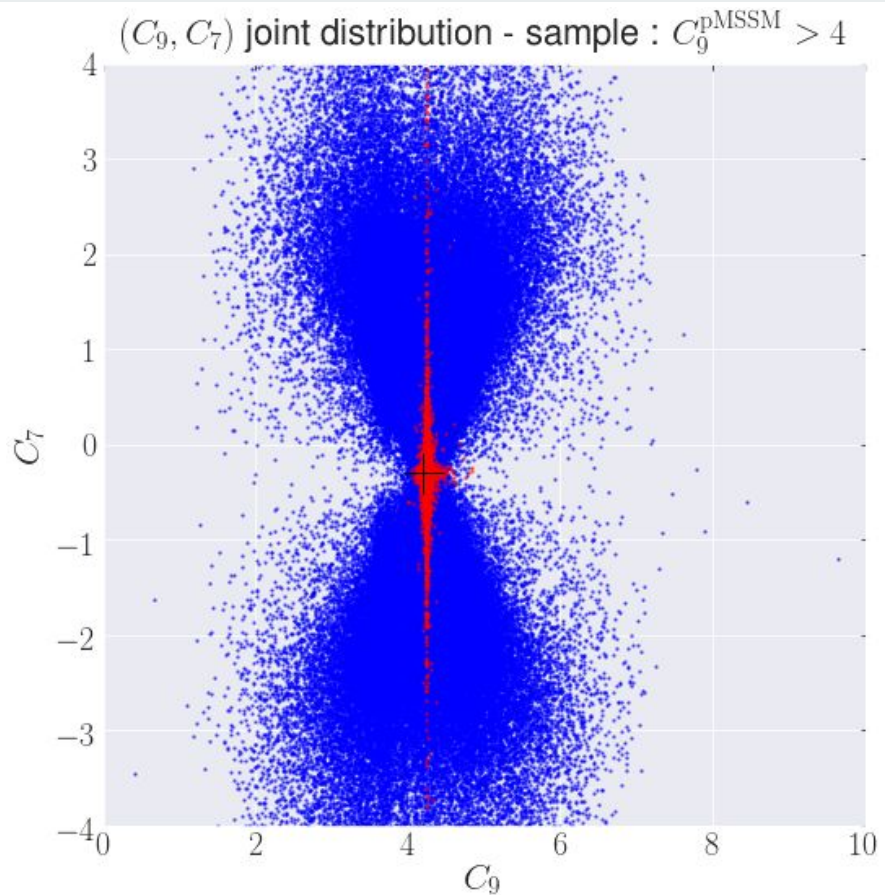
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# Results

# Spreading the distribution

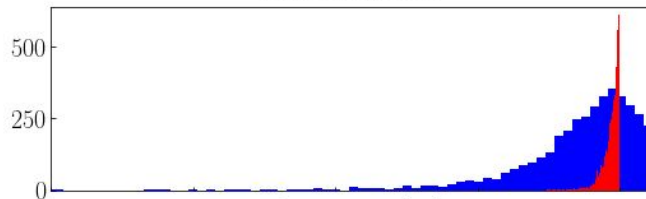
- $1.7 \times 10^5 / 1.6 \times 10^7$  valid points.
- Scan constraints :
  - Tachyon
  - Charged LSP
  - Excluded LEP masses
  - **Right set** :  $C_9$  in  $[4, 4.5]$
  - **Left set** :  $C_9 < 4$
- Corresponding **NMFV** points obtained by recalculating the Wilson coeffs. on the same **pMSSM** points.
- Impressive spreading of the pMSSM distribution.
- Most of these points ( $\sim 10^5$ ) are excluded, but behaviour is remarkable.



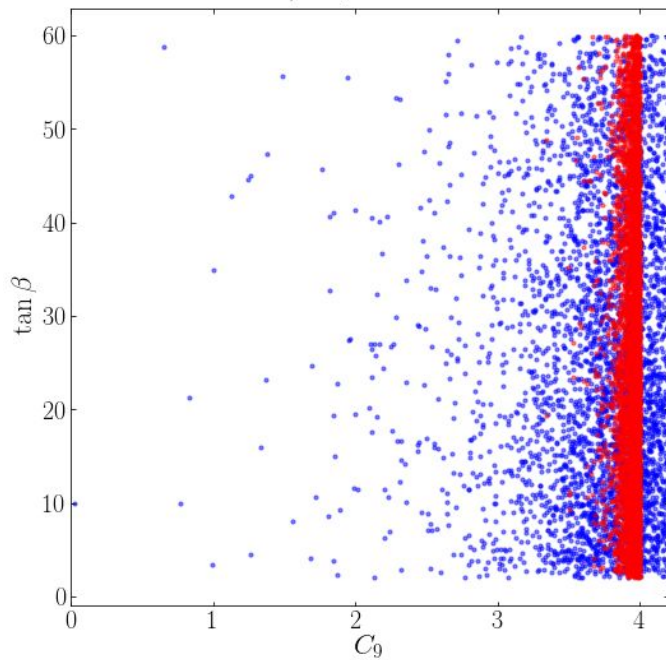


# Correlated distributions, $C_9^{\text{PMSSM}} < 4$

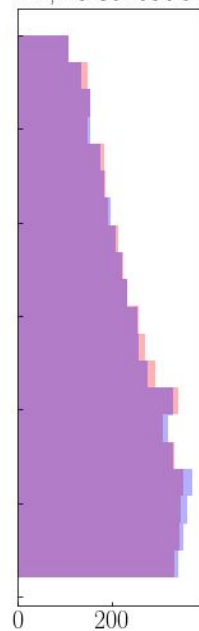
$C_9$  distribution



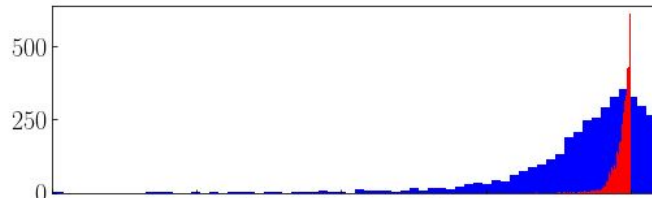
$\tan \beta$ - $C_9$  correlation



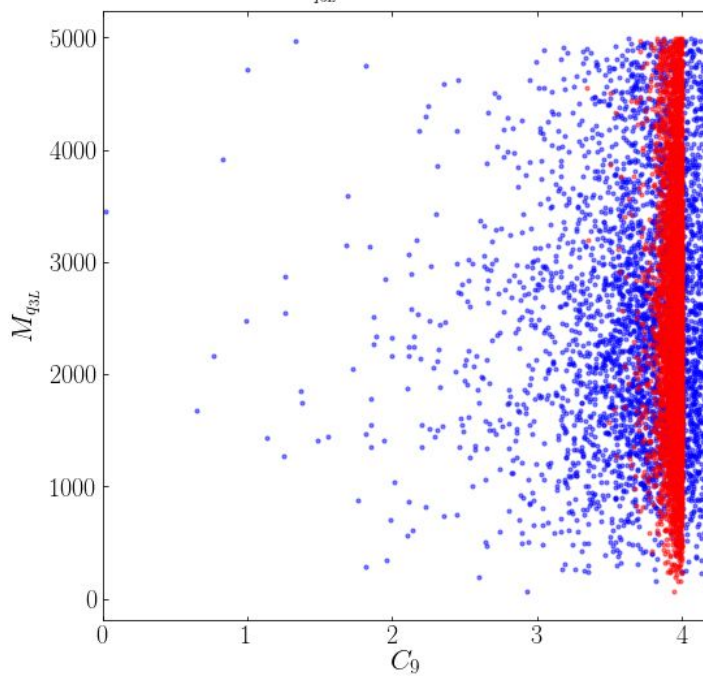
$\tan \beta$  distribution



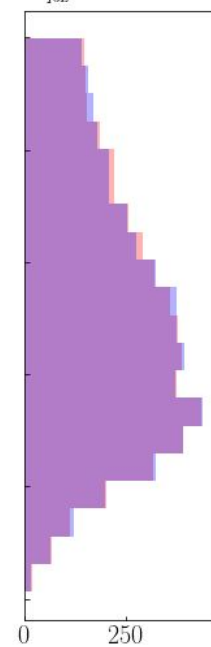
$C_9$  distribution



$M_{q3L}$ - $C_9$  correlation



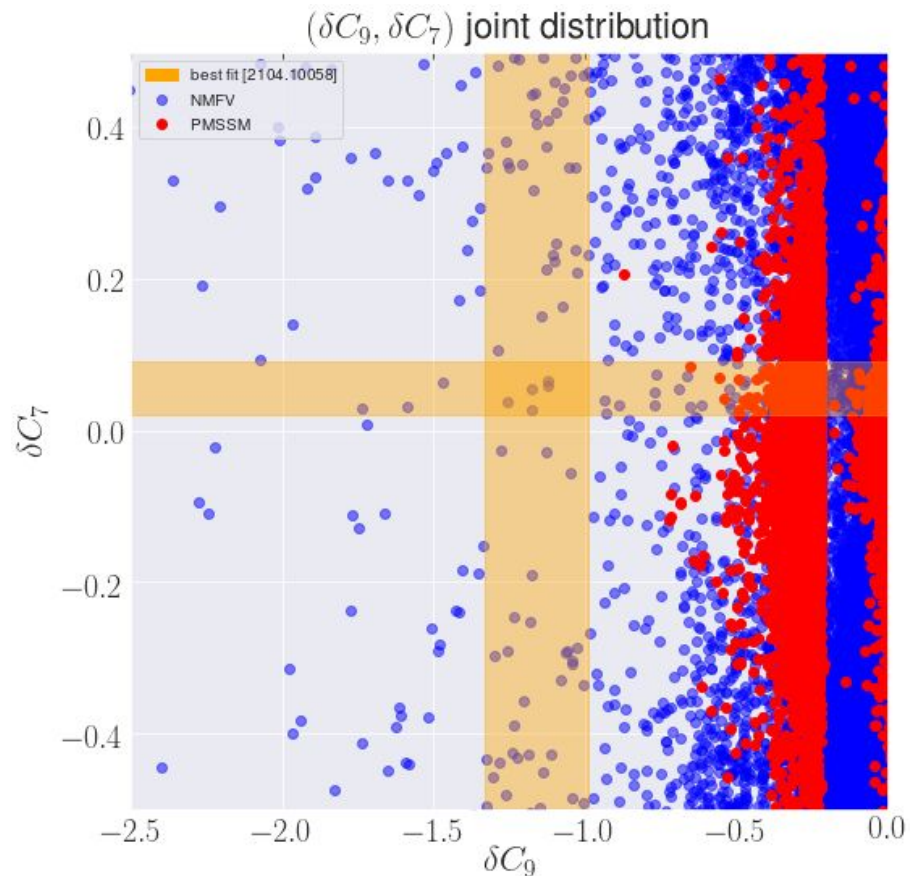
$M_{q3L}$  distribution





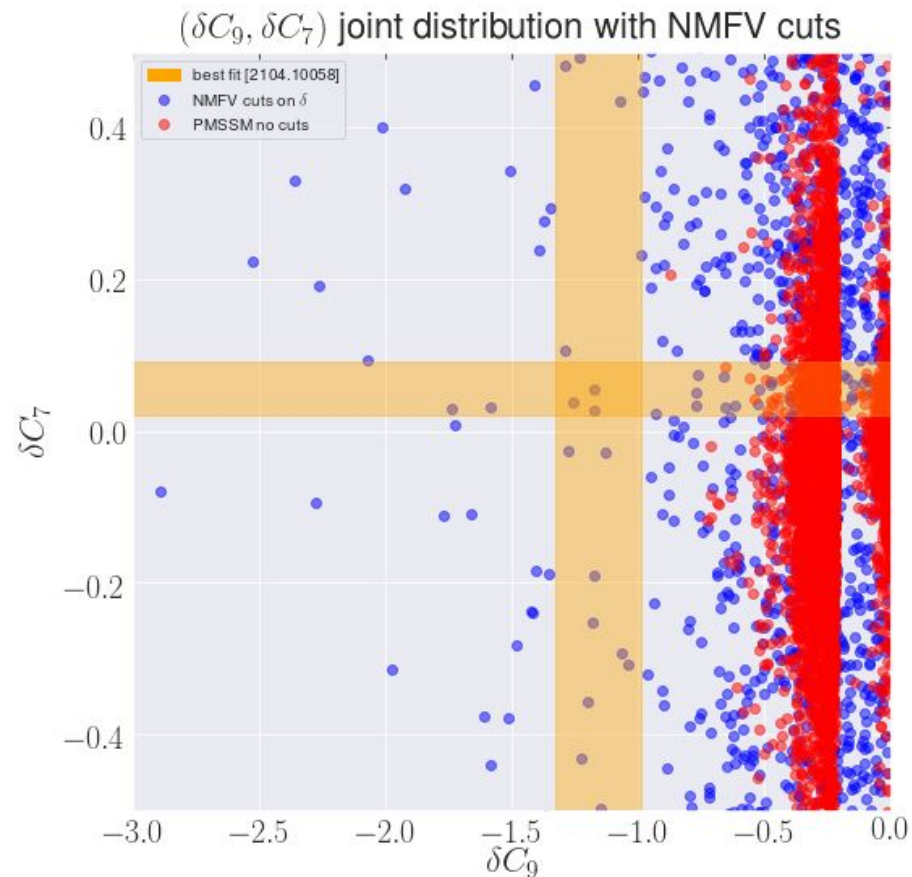
# Best fit for two Wilson coefficients

- Best fit in the  $(\delta C_9, \delta C_7)$  plane, using the 20 operator global fit from [[2104.10058](#)].
- Some points are compatible with this fit.
- Constraints :
  - RGE passing points (non tachyonic)
  - No charged LSP
  - LEP mass limits



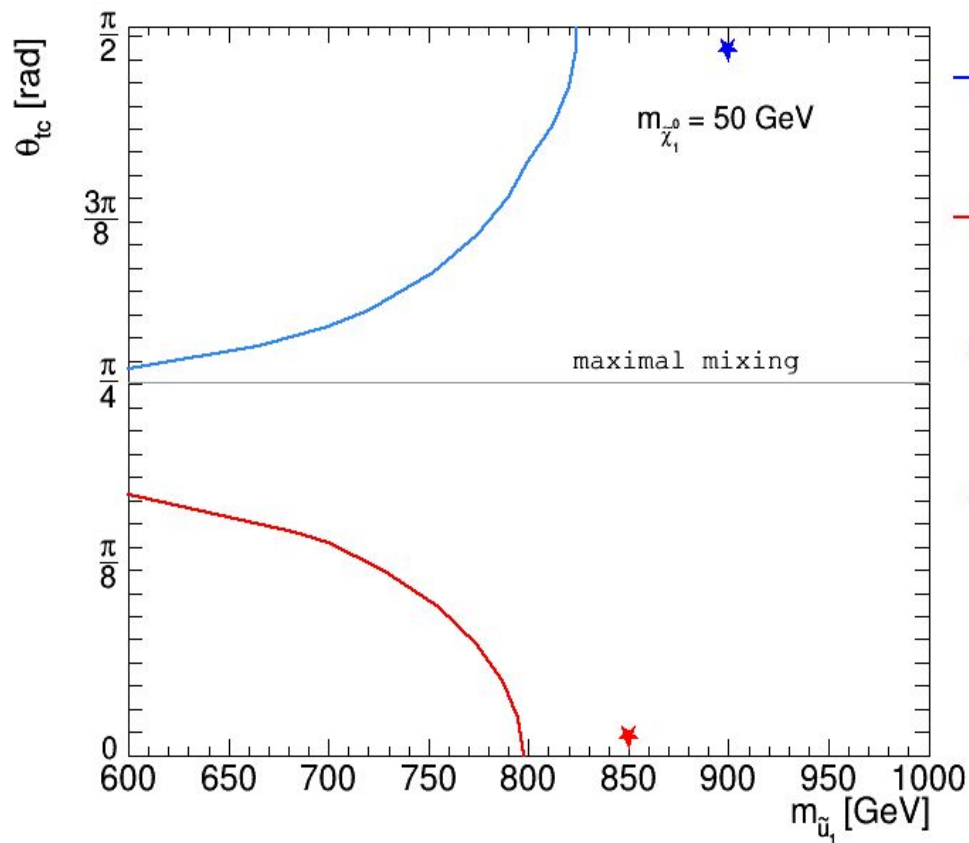
# Best-fit and other constraints

- Best fit in the  $(\delta C_9, \delta C_7)$  plane, using the 20 operator global fit from [[2104.10058](#)].
- Constraints :
  - RGE passing points (non tachyonic)
  - No charged LSP
  - LEP mass limits
  - NMFV constraints [[1509.05414](#)]





# Squark mixing and LHC limits



—  $t\bar{t}+E_T^{\text{miss}}$  [1711.11520]

$36 \text{ fb}^{-1}$  recast

—  $c\bar{c}+E_T^{\text{miss}}$  [1805.01649]

$36 \text{ fb}^{-1}$  recast

★  $t\bar{t}+E_T^{\text{miss}}$  [1711.11520]

$36 \text{ fb}^{-1}$  exclusion

★  $c\bar{c}+E_T^{\text{miss}}$  [1805.01649]

$36 \text{ fb}^{-1}$  exclusion

Simplified model of squark flavour violation :

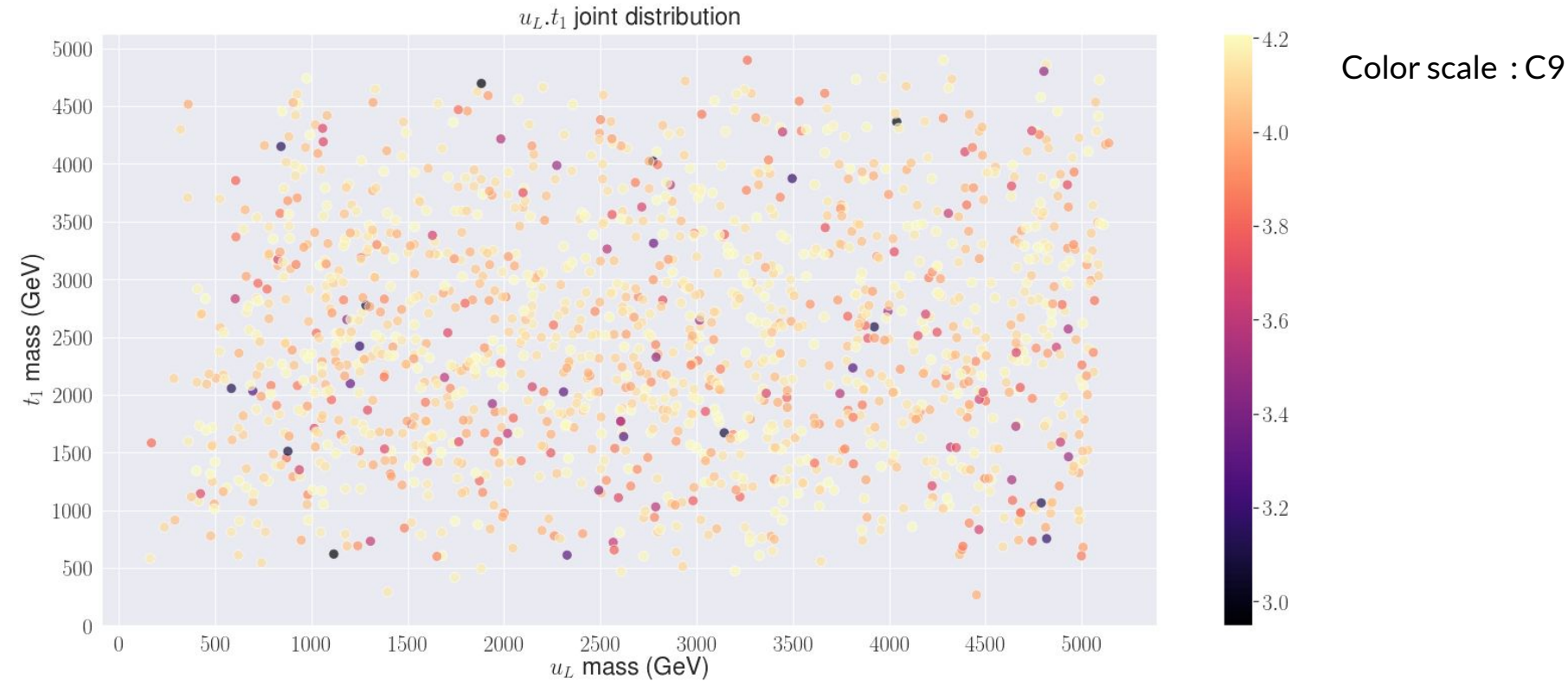
$$\begin{pmatrix} \tilde{u}_1 \\ \tilde{u}_2 \end{pmatrix} = \begin{pmatrix} \cos \theta_{tc} & \sin \theta_{tc} \\ -\sin \theta_{tc} & \cos \theta_{tc} \end{pmatrix} \begin{pmatrix} \tilde{c}_R \\ \tilde{t}_R \end{pmatrix}$$

$$m_{\chi_1^0} = 50 \text{ GeV}$$

The recast severely reduces the ATLAS limits on stop and scharm masses [50-250 GeV].

Recast of ATLAS searches by Chakraborty et al. [[1808.07488](#)]

# Squark mass distribution





# Conclusion

- The NMFV approach using the MIA/FET gives promising results in the Wilson coefficient sector.
- Some presented model points correspond to Wilson coefficient fits, but need further investigation to check direct search limits.
- Finding model points in these highly dimensional parameter spaces is challenging. First results encouraging.