

# Methods and results on the search for gravitational wave echoes in the post-merger phase after binary black hole coalescences.

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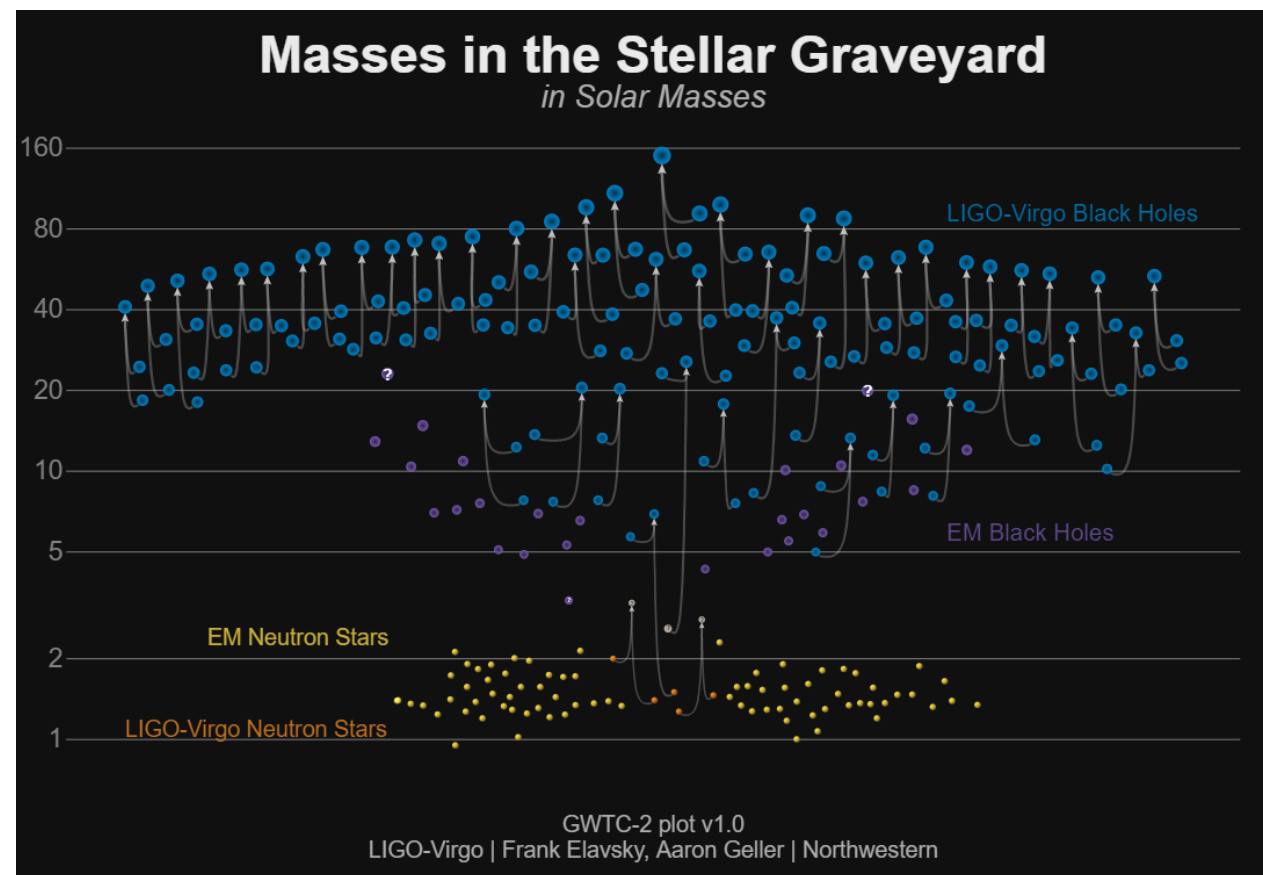
[8], Physik-Institut, University of Zurich, Winterthurerstrasse 190, 8057 Zurich,

# Outline of the presentation

1. Echoes search, WHY?
2. Echoes: state of the art.
3. Echoes: an unconstrained search.
4. Echoes: results of the search.
5. Conclusions.

## 1.1 - Echoes search, WHY?

- 2015, September 14 th: detection of the first gravitational wave (GW), [GW150914](#).
- LIGOs and Virgo interferometers had detected several GW signals in the past six years. [GWTC-1](#) (O1, O2 runs) and [GWTC-2](#) (O3a run).
- 45 (+3?) out of 50 detections are labelled as binary black hole (BBH) coalescences. **Are we sure of it?**



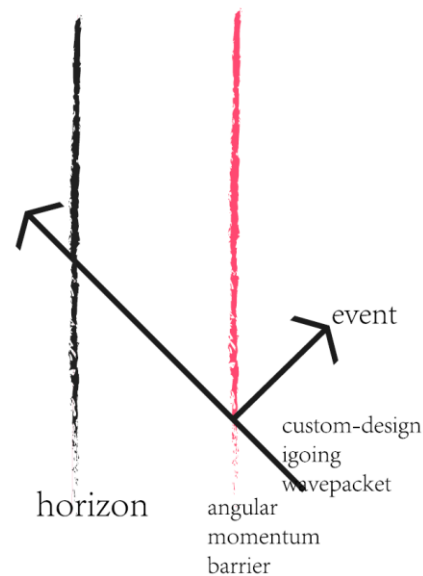
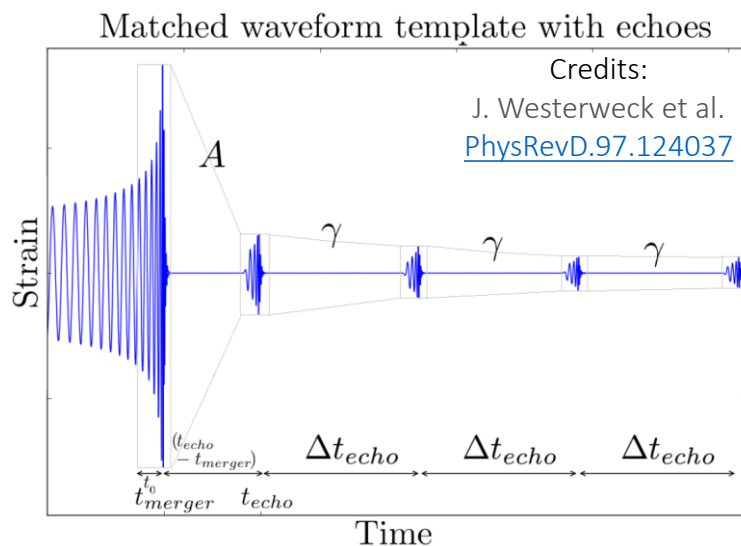
[Credit](#): Visualization: LIGO -Virgo / Frank Elavsky, Aaron Geller / Northwestern

## 1.2 - Echoes search, WHY?

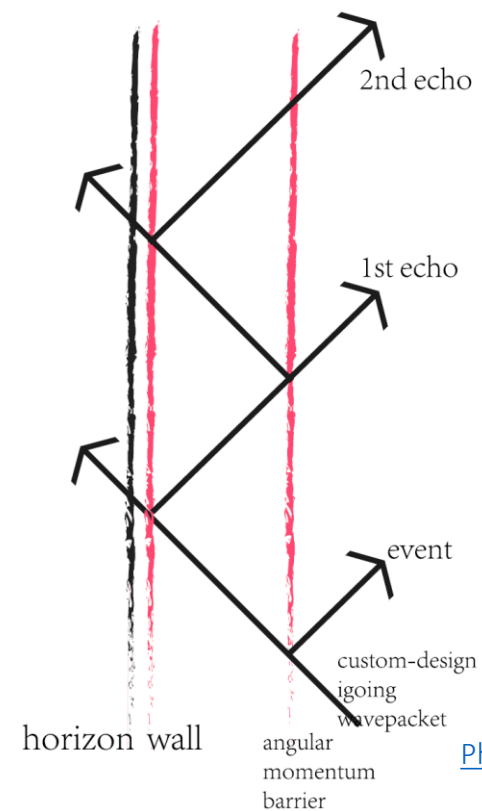
Several alternative models to BH, generally referred as **exotic compact objects (ECO)**, such as [Gravastars](#) or [Firewalls](#).

ECOs share a common feature.

Emission of GW pulses, called [echoes](#), in the post-merger ringdown phase of the coalescence.

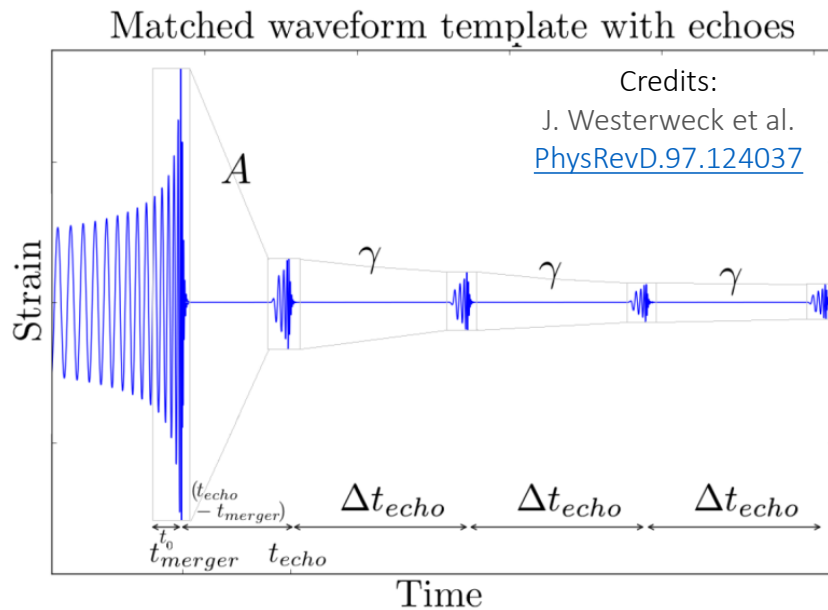


- Multiple reflection of ingoing GW signal.
- Horizon replaced by a surface of different nature.



Credits:  
Q. Wang et al.  
[PhysRevD.97.124044](#)

## 1.3 - Echoes search, WHY?



$$\Delta t_{\text{echo}} \sim n M \log \left( \frac{l}{M} \right), \quad l \ll M, \quad c = G = 1 \quad [1]$$

Parameter	Description
$\Delta t_{\text{echo}}$	time delay between subsequent echoes <ul style="list-style-type: none"> <li><math>n</math> -&gt; related to the nature of the ECO;</li> <li><math>M</math> -&gt; remnant mass of the final ECO;</li> <li><math>l</math> -&gt; radius length correction to the BH horizon;</li> </ul>
$t_{\text{echo}}$	time of the first echo signal
$\gamma$	amplitude damping factor of echoes
$A$	relative amplitude of the first echo wrt the CBC signal.

### WHY searching ECHOES?

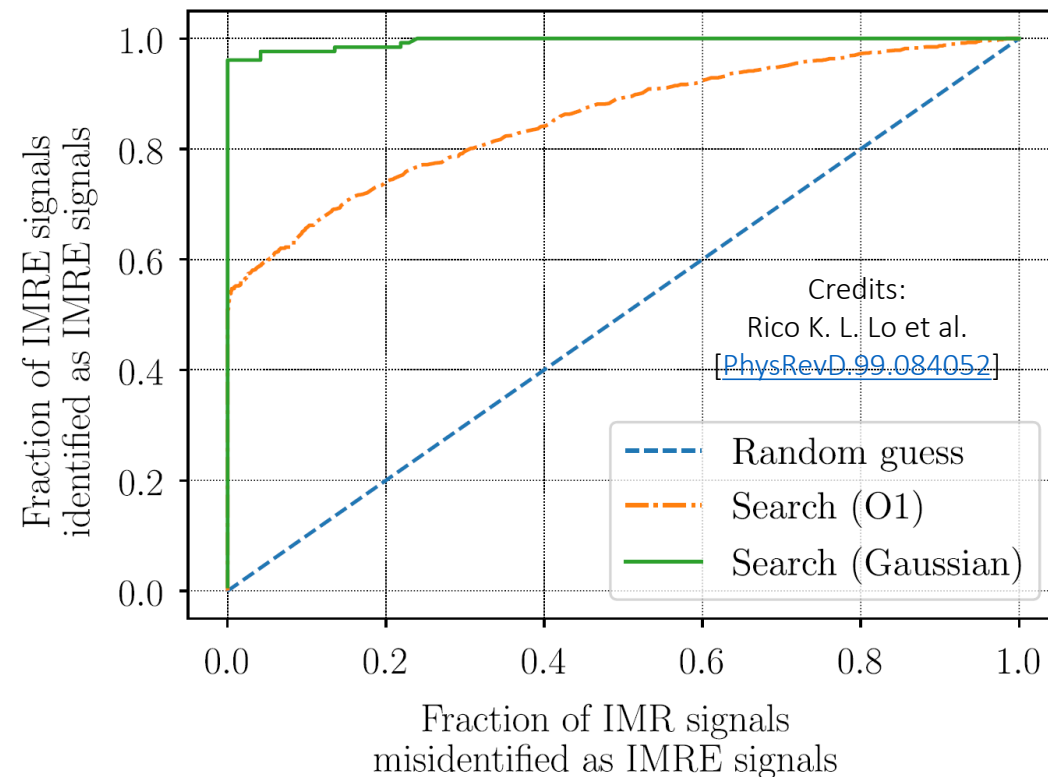
- Probe the general relativity (GR) theory.
- Investigate exotic state of matter.

[1] V. Cardoso et al. [PhysRevD.94.084031](https://arxiv.org/abs/1512.02075)

## 2 - Echoes: state of the art

Several echoes searches were performed in past years

- **template searches;**
  - Julian Westerweck et al. [[PhysRevD.97.124037](#)];
    - Injections' faithful reconstruction for strain  $\geq 10^{-22}$ ;
  - Rico K. L. Lo et al. [[PhysRevD.99.084052](#)];
- **unmodeled searches;**
  - Ka Wa Tsang et al. [[PhysRevD.98.024023](#)];
    - signal decomposed using sine-Gaussian wavelets:  
confident detection for  $\text{snr} \geq 12$ .



IMR : Inspiral-Merger-Ringdown

IMRE : Inspiral-Merger-Ringdown-Echoes


## 3.1 - Echoes: an unmodeled search

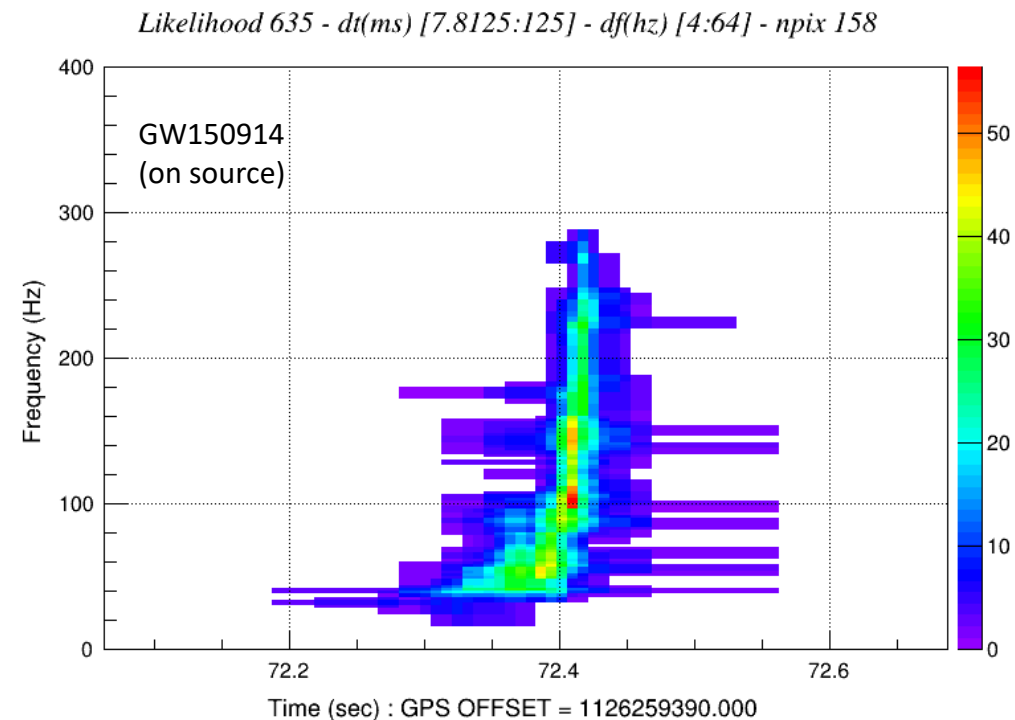
### Coherent Wave Burst (cWB) pipeline



- Unmodeled coherent search:
  - no assumptions on the signal morphology.
- Constrained maximum likelihood approach

#### cWB flowchart

- |                                                                                                                                                                   |                                                                                    |                  |
|-------------------------------------------------------------------------------------------------------------------------------------------------------------------|------------------------------------------------------------------------------------|------------------|
| <ul style="list-style-type: none"> <li>• Data conditioning</li> <li>• Whitening of the data (<math>\mathbf{x}[\mathbf{i}]</math>)</li> </ul>                      |  | Single detector  |
| <ul style="list-style-type: none"> <li>• Pixels selection</li> <li>• Likelihood maximization (<math>\mathbf{L}</math>)</li> <li>• Post production cuts</li> </ul> |                                                                                    | Combined network |



$$\mathbf{x}[\mathbf{i}] = \mathbf{h}[\mathbf{i}] + \mathbf{n}[\mathbf{i}];$$

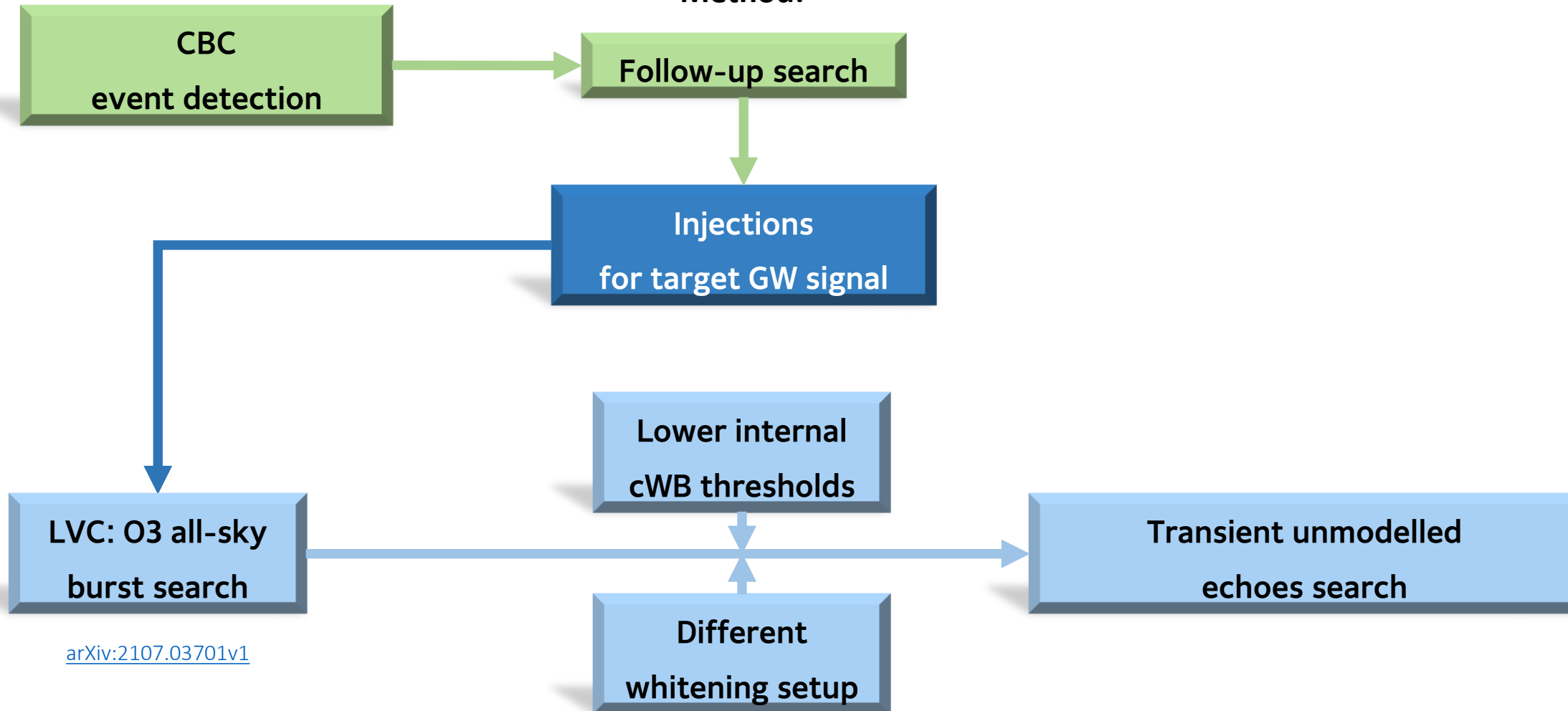
$$\mathbf{L} = \log \left( \frac{P(\mathbf{x}|\mathbf{H}_1)}{P(\mathbf{x}|\mathbf{H}_0)} \right);$$

$P(\mathbf{x}|\mathbf{H}_1)$ : probability of having a signal.

$P(\mathbf{x}|\mathbf{H}_0)$ : probability of the null hypothesis.

## 3.2 - Echoes: an unmodeled search

Method:



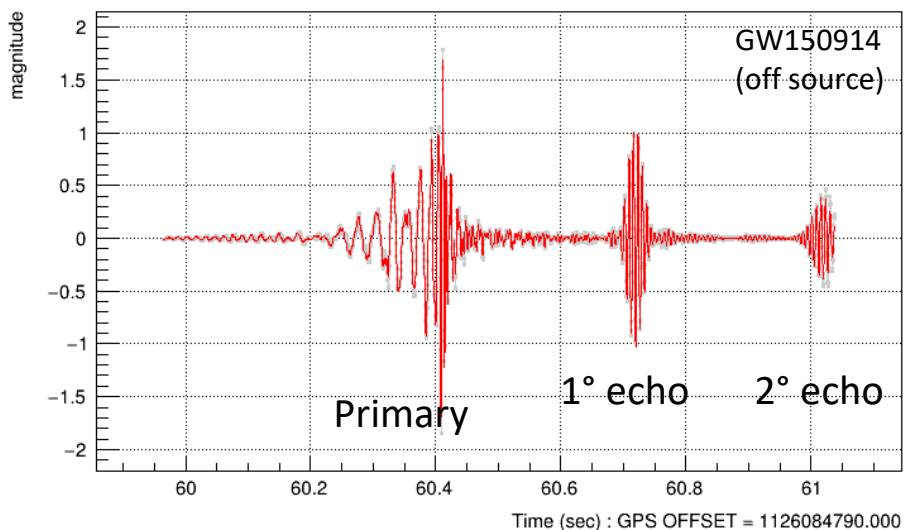


## 3.3 - Echoes: an unmodeled search

### Injections for target GW signal

Selected randomly from posterior waveforms (LAL inference).

Waveform model: IMRPhenomPv2



### Only Primary injections - [P]

- one injection every 600s;
- real noise (O1 and O2);

### Primary + «Echoes» injections - [P+E]

- same as [P] injections;
- echoes model = Elliptical sine-Gaussian (SGE);
- two echoes injected;
- $t_{echo} = 0.3s$  after binary coalescence time;
- $\Delta t_{echo} = 0.3s$ ;
- $\gamma = 0.5$ ;
- $A \in [0.05 - 1.0]$  relative to primary signal amplitude;
  - random uniform log amplitude distribution.

## 3.4 - Echoes: an unmodeled search

Statistic estimators for echoes detection:

Reconstructed energy:  $E^{\text{PMW}} = \sum_K \sum_i x_k[i]^2$

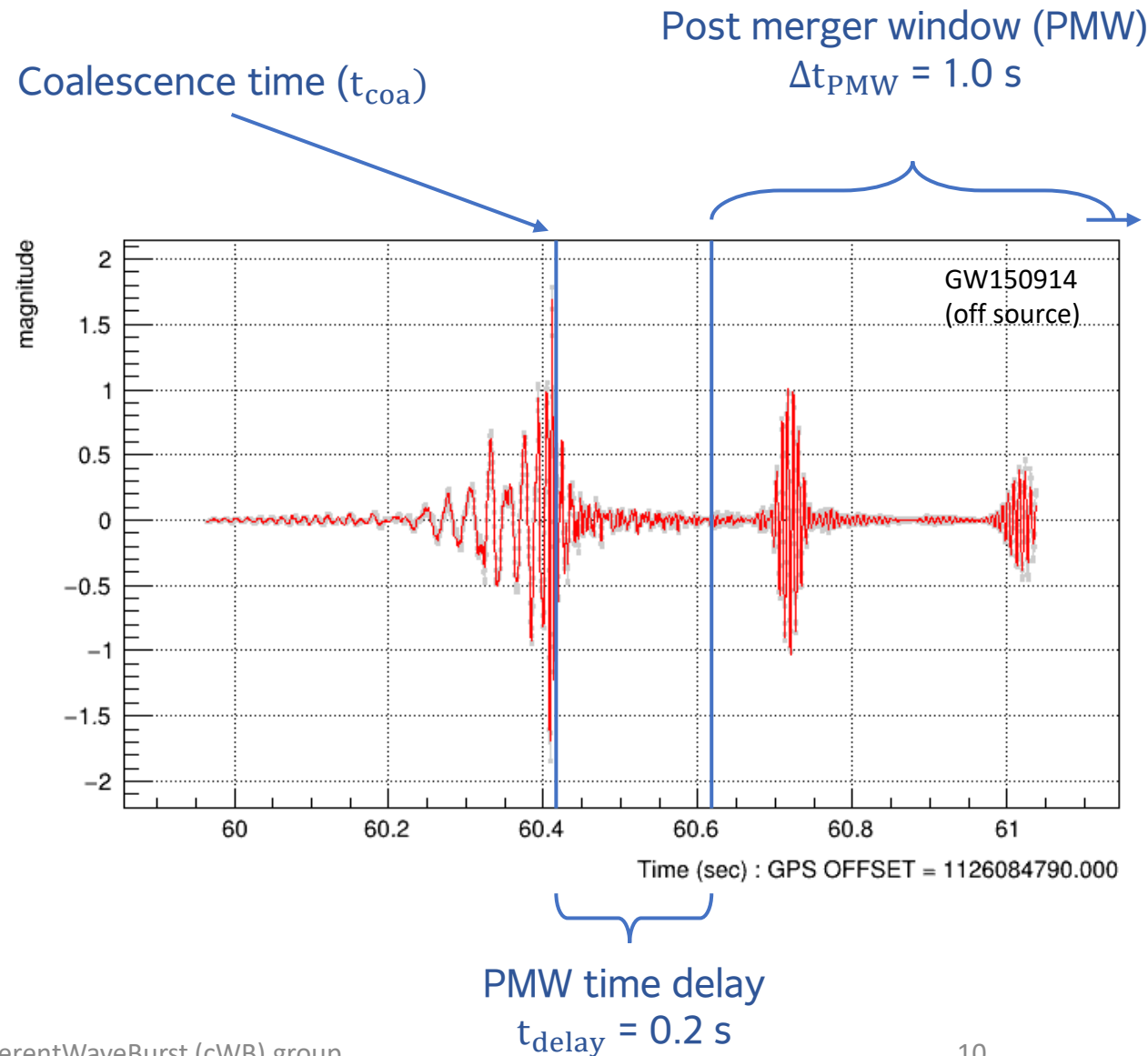
Coherence:  $cc^{\text{PMW}} = E_{\text{coh}}^{\text{PMW}} / (E_{\text{coh}}^{\text{PMW}} + E_{\text{null}}^{\text{PMW}})$

Echoes detection efficiency:

fraction of reconstructed events with  $\text{snr}^{\text{PMW}} > \text{th. snr}^{\text{PMW}}$   
in [P+E] injections.

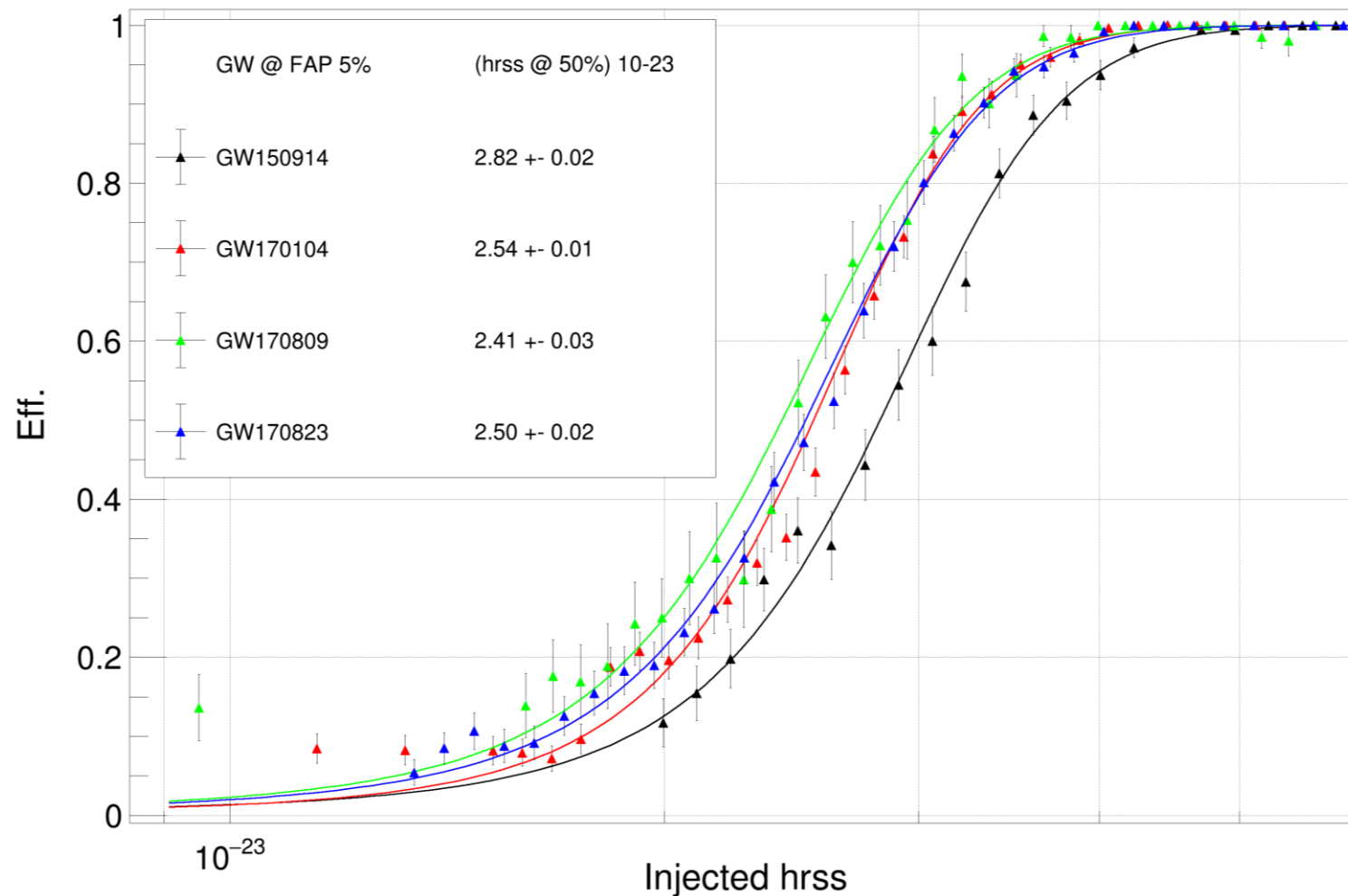
False alarm probability (FAP):

fraction of reconstructed events with  $\text{snr}^{\text{PMW}} > \text{th. snr}^{\text{PMW}}$   
in [P] injections.



## 4.1 - Echoes: result of the search

### Det. Efficiency inside PM window

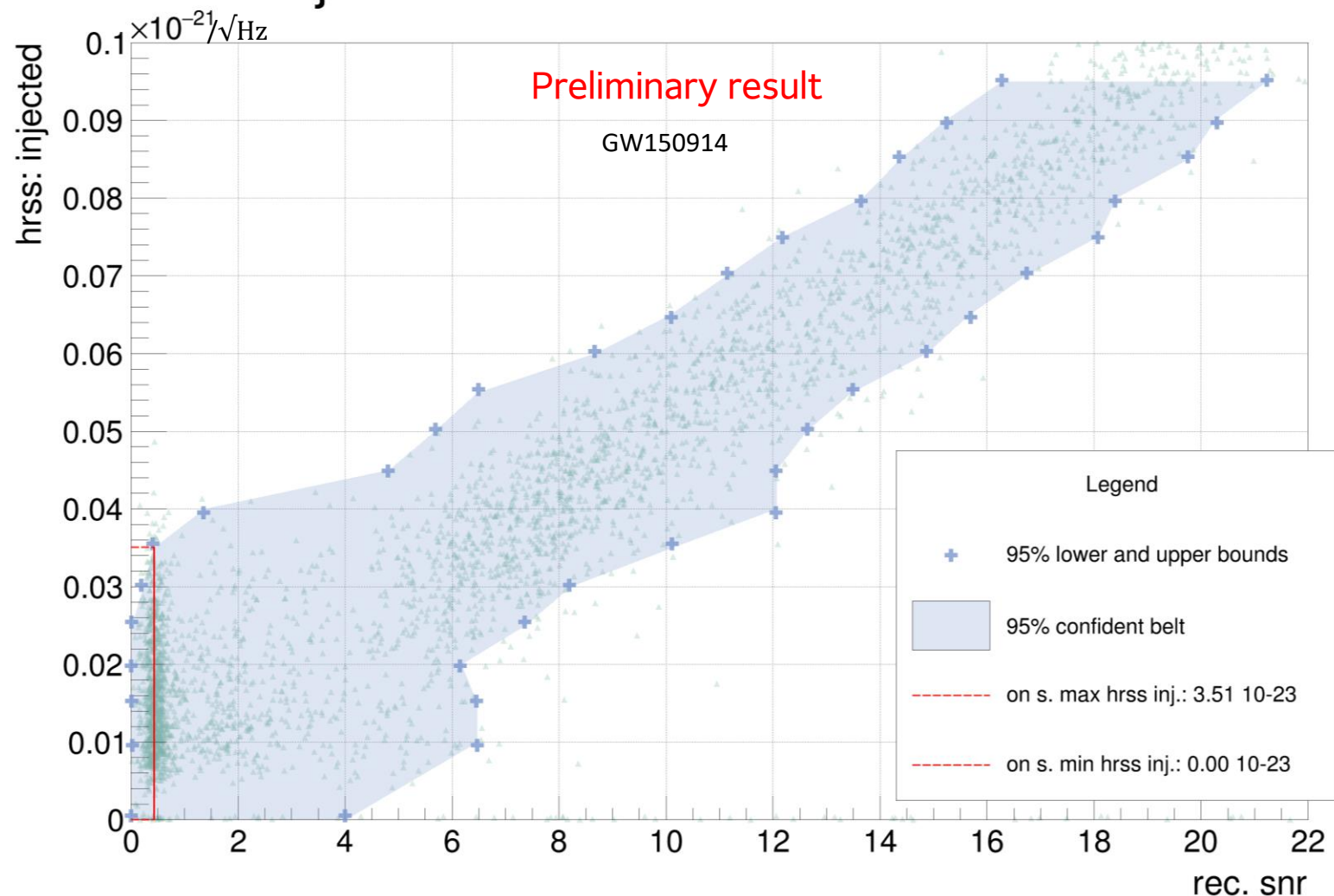


$$\frac{\# \text{ rec events with } \sqrt{E^{\text{PMW}}} > \text{snr}_{\text{thr}}}{\# \text{ total rec events}} \quad [\text{P+E}]$$

GW event	hrss <sub>w</sub> <sup>PM</sup> @50% det. Eff. for 5% FAP.
GW150914	$(2.82 \pm 0.02) \cdot 10^{-23}$
GW151012	$(2.60 \pm 0.03) \cdot 10^{-23}$
GW151226	$(2.72 \pm 0.03) \cdot 10^{-23}$
GW170104	$(2.54 \pm 0.01) \cdot 10^{-23}$
GW170608	$(2.63 \pm 0.01) \cdot 10^{-23}$
GW170729	$(2.53 \pm 0.01) \cdot 10^{-23}$
GW170809	$(2.41 \pm 0.03) \cdot 10^{-23}$
GW170814	$(2.53 \pm 0.02) \cdot 10^{-23}$
GW170823	$(2.50 \pm 0.02) \cdot 10^{-23}$

## 4.2 - Echoes: result of the search

### Injected hrss. VS Reconstructed snr.

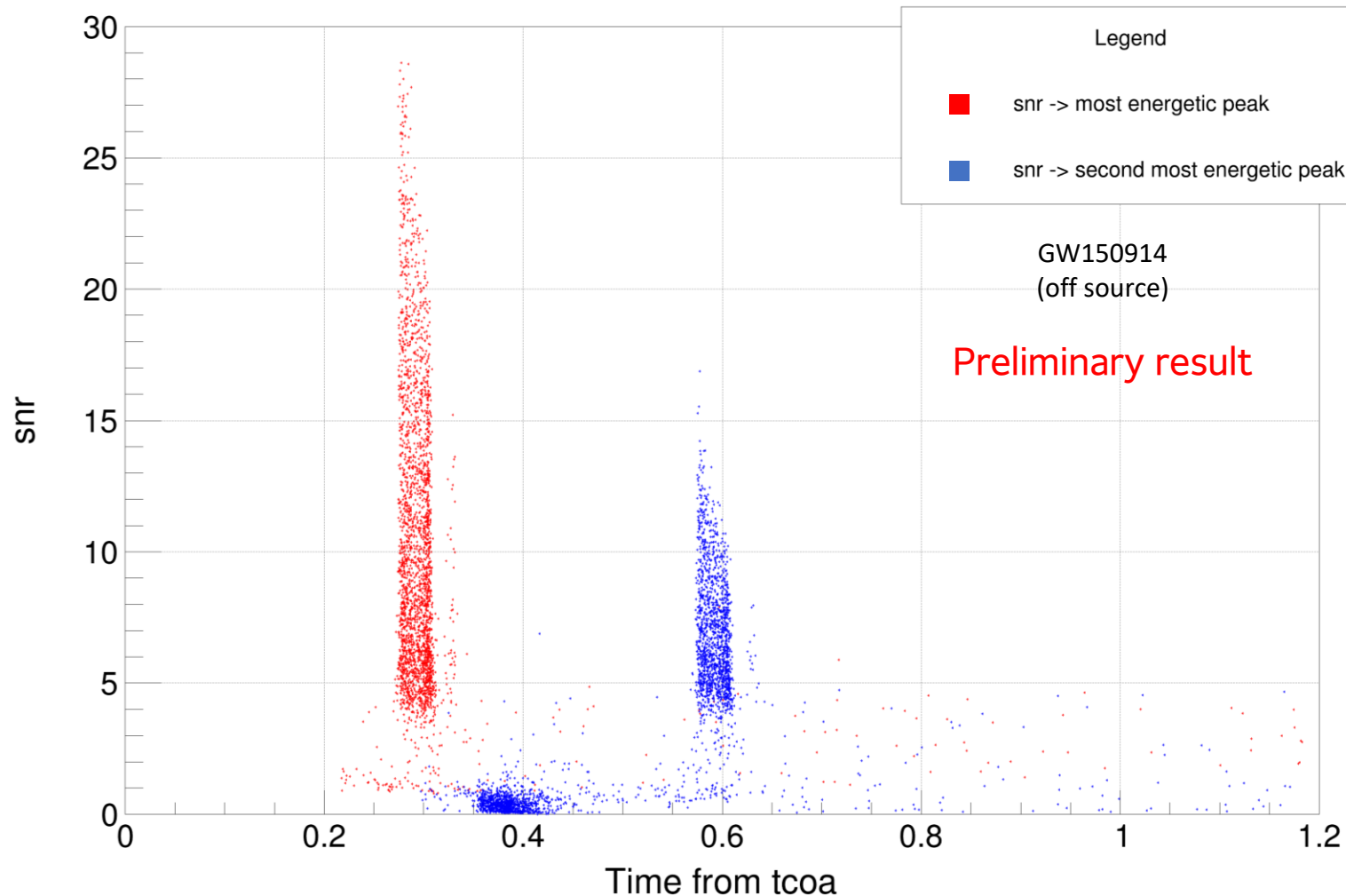


### 95% confident belt

- Preliminary result for GW150914.
- Reconstructed snr:  $\rightarrow$  define the interval of  $\text{hrss}_{\text{inj}}$  @ 95% confidence and set constraints over  $A$  or  $\gamma$  parameters.
- On source snr  $\rightarrow$  compatible with null hypothesis.

## 4.3 - Echoes: result of the search

Peak SNR distribution for FAP < 5%



Reconstructed SNR(t) inside a moving time interval, in PMW data segment.

The first two highest SNR(t) in PMW are plotted.

Echo's parameters that can be recovered and constrained:

- study:  $\Delta t_{\text{echo}}$ ;
- study:  $t_{\text{echo}}$  and  $A$ ;
- study:  $\gamma$ ;

## 5 - Conclusions

### TAKE HOME:

- Capability to recover fundamental echo morphological parameters ( $A, t_{\text{echo}}, \Delta t_{\text{echo}}, \gamma$ ).
- Capability to detect sub-thresholds burst signals with  $\text{FAP} < 5\%$ .

Threshold  $\text{snr}^{\text{PMW}}$  for a  $\text{FAP} = 5\% \in [\sim 1.3, \sim 2.7]$

- Detection efficiency even at very low  $\text{SNR}$  values.

### TO DO:

- Extending the analysis to O3 events.
- Perform calibrated echo injections for each BBH GW events of GWTC-1 and GWTC-2.

### FUTURE PLANS:

- Possibility to use the same searching procedure to study hyperbolic encounters and capture, memory effect, ecc.



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Francesco Salemi

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Gabriele Vedovato

Sergey Klimenko

Marco Drago

Edoardo Milotti

Odysse Hamil

Thank you  
for the attention!



Credits:  
C. Gray



Credits: J.  
Giaime



Credits: Virgo  
Collaboration



LIGO  
Scientific  
Collaboration  
collaboration

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## Backup Slides



## 6.1 – Appendix: cWB likelihood

CoherentWaveBurst (cWB) pipeline:

- **Unmodelled coherent search:**
  - no assumptions on the signal morphology.
- **Maximum likelihood approach**

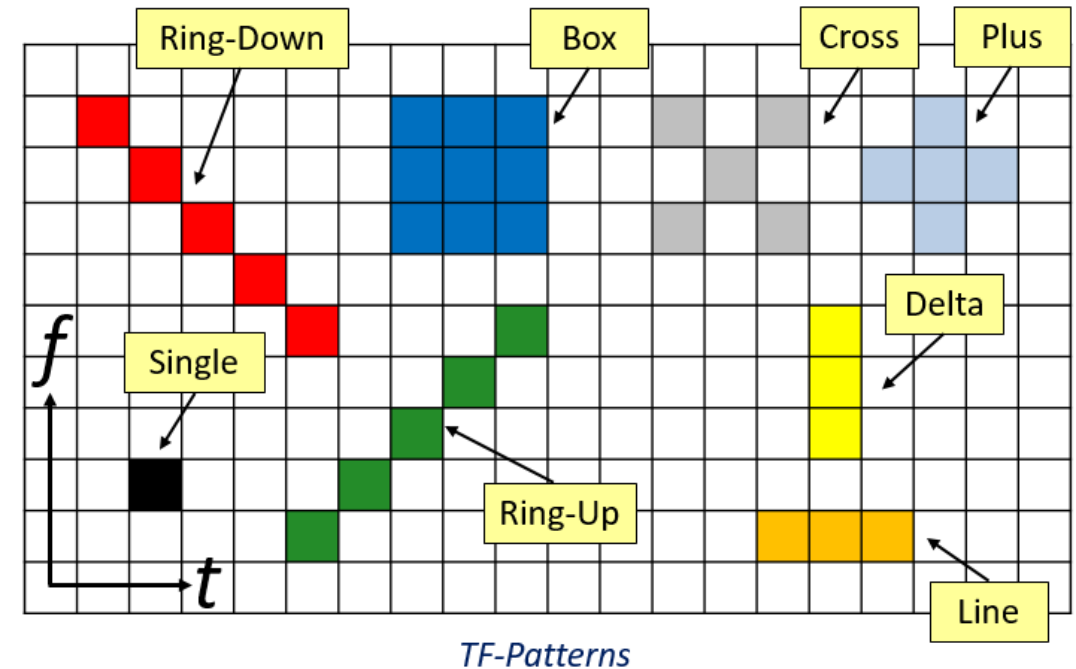
$$x[i] = h[i] + n[i];$$

$$P(x|H_1) = \prod_{i=1}^M \frac{1}{\sqrt{2\pi}\sigma} \exp\left(-\frac{(x[i] - \xi[i])^2}{2\sigma^2}\right)$$

$$P(x|H_0) = \prod_{i=1}^M \frac{1}{\sqrt{2\pi}\sigma} \exp\left(-\frac{x[i]^2}{2\sigma^2}\right)$$

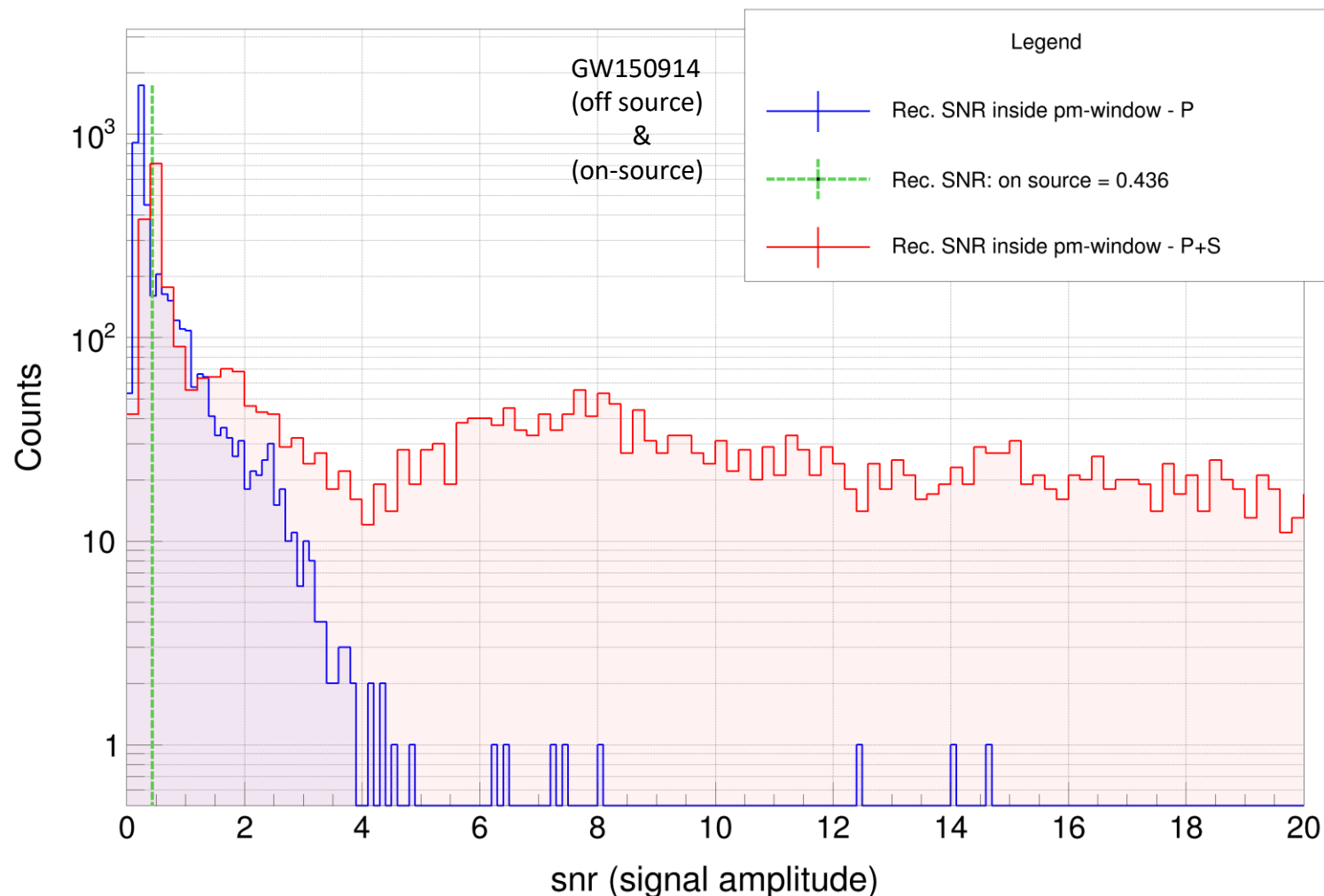


$$\mathbf{L} = \log\left(\frac{P(x|H_1)}{P(x|H_0)}\right) = \sum_{k=1}^N \sum_{i \in \Omega_{TF}} \left( \frac{x_k^2[i]}{\sigma_k^2[i]} - \frac{(x_k[i] - \xi_k[i])^2}{\sigma_k^2[i]} \right);$$



## 6.2 – Appendix: Reconstructed SNR

### Rec. - SNR inside pm-window

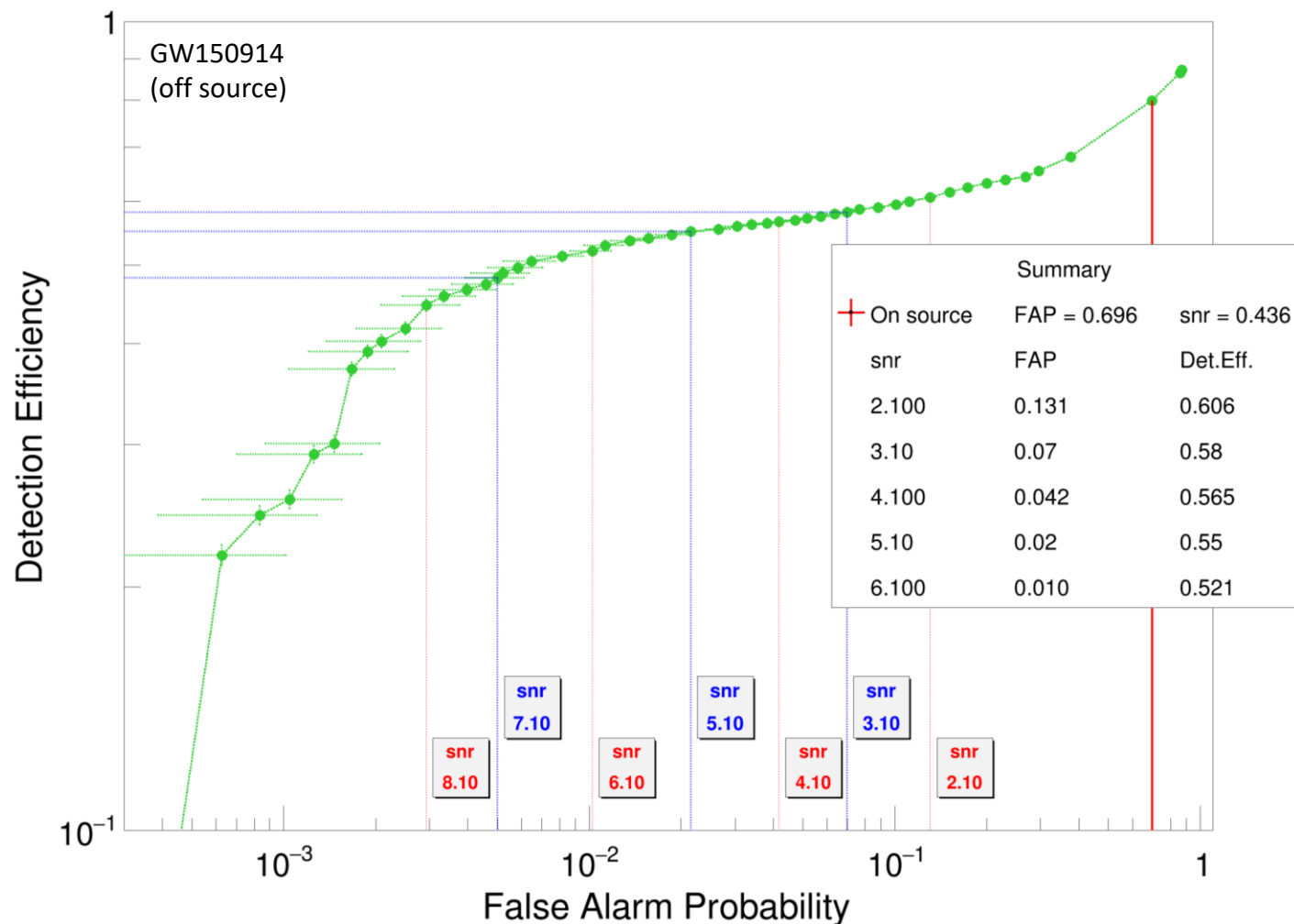


### Reconstructed snr inside the PM window

- **Blue distribution:** referred to results for “only primary” [P] injection.
- **Red distribution:** referred to results for “primary + echoes” [P+E] injection.
- **Green line:** snr value of the on-source event.

## 6.3 – Appendix: Receiver Operating Characteristic (ROC)

ROC - cc\_th = 0.5



ROC

(Receiver Operating Characteristic)

- **False Alarm Probability:** fraction of events with SNR in PM window above SNR threshold for “only primary” [P] injection.
- **Detection Efficiency:** fraction of events with SNR in PM window above SNR threshold for “primary + echoes” [P+E] injection.

## 6.4 – Appendix: O1 & O2 on source results

GW event	$\text{snr}^{\text{PMW}}$	$\text{snr}^{\text{PMW}}$ @ FAP5%	p-value $H_0$ (FAP)
GW150914	0.47	3.7	0.696
GW151012	7.87	1.3	0.001
GW151226	0.19	2.3	0.790
GW170104	0.07	2.5	0.888
GW170608	1.84	1.7	0.046
GW170729	2.99	1.7	0.035
GW170809	0.03	0.5	0.557
GW170814	0.27	2.7	0.450
GW170818			
GW170823	0.01	1.7	0.835



Here:

$$\text{snr}^{\text{PMW}} > \text{snr}^{\text{PMW}} @ \text{FAP5\%}$$

Cannot be compared: require a different pipeline setup.

- Agreement with: F. Salemi et al. [PhysRevD.100.042003](https://arxiv.org/abs/1907.04203)