

# EPS-HEP Conference 2021

European Physical Society conference on high energy physics 2021

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## Measurements of mixed harmonic cumulants in Pb-Pb collisions at 5.02 TeV with ALICE

**You Zhou**

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(for the ALICE Collaboration)*



ALICE

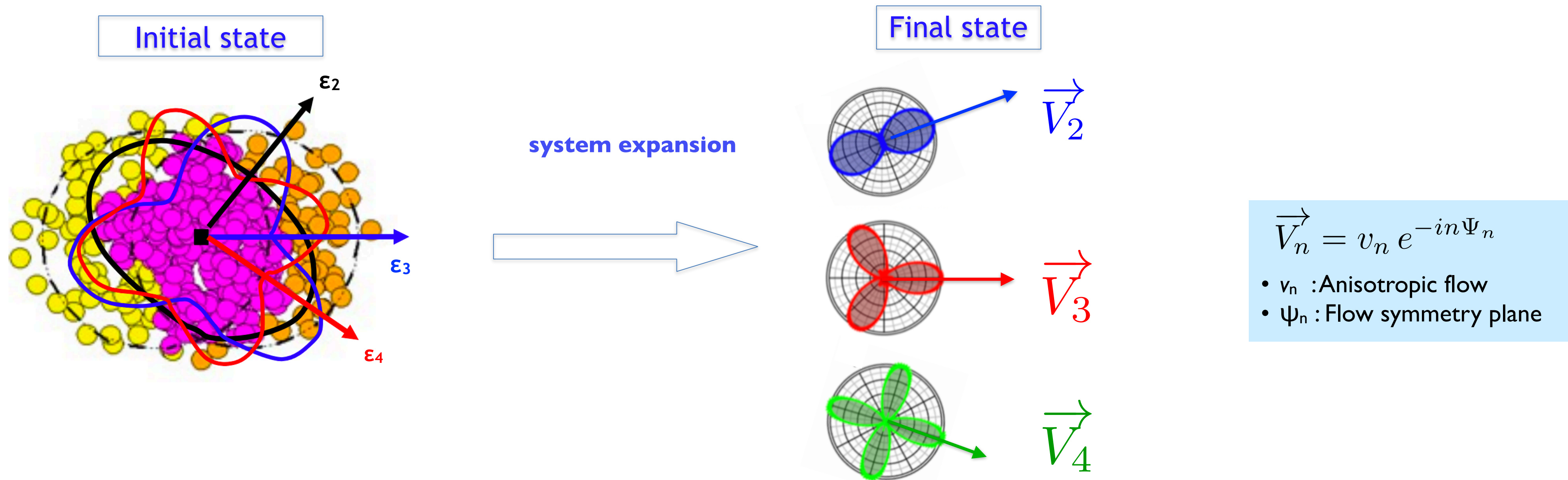


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# Studying QGP with anisotropic flow



## ❖ General questions:

- ▶ how does  $v_n$  fluctuate
- ▶ how does  $\Psi_n$  fluctuate
- ▶ correlations between  $\Psi_m$  and  $\Psi_n$
- ▶ **correlations between  $v_m$  and  $v_n$**
- ▶ new information on initial conditions and/or  $\eta/s(T)$ ?

ALICE, [JHEP 07 \(2018\) 103](#)  
 ALICE, [JHEP 09 \(2017\) 032](#)  
 ALICE, [JHEP05 \(2020\) 085](#)  
[JHEP06 \(2020\) 147](#)  
 ALICE, [PRL117, \(2016\) 182301](#)  
[PRC97, \(2018\) 024906](#)  
[PLB818 \(2021\) 136354](#)

# General correlations between flow coefficients

PHYSICAL REVIEW C **103**, 024913 (2021)

Generic algorithm for multiparticle cumulants of azimuthal correlations in high energy nucleus collisions

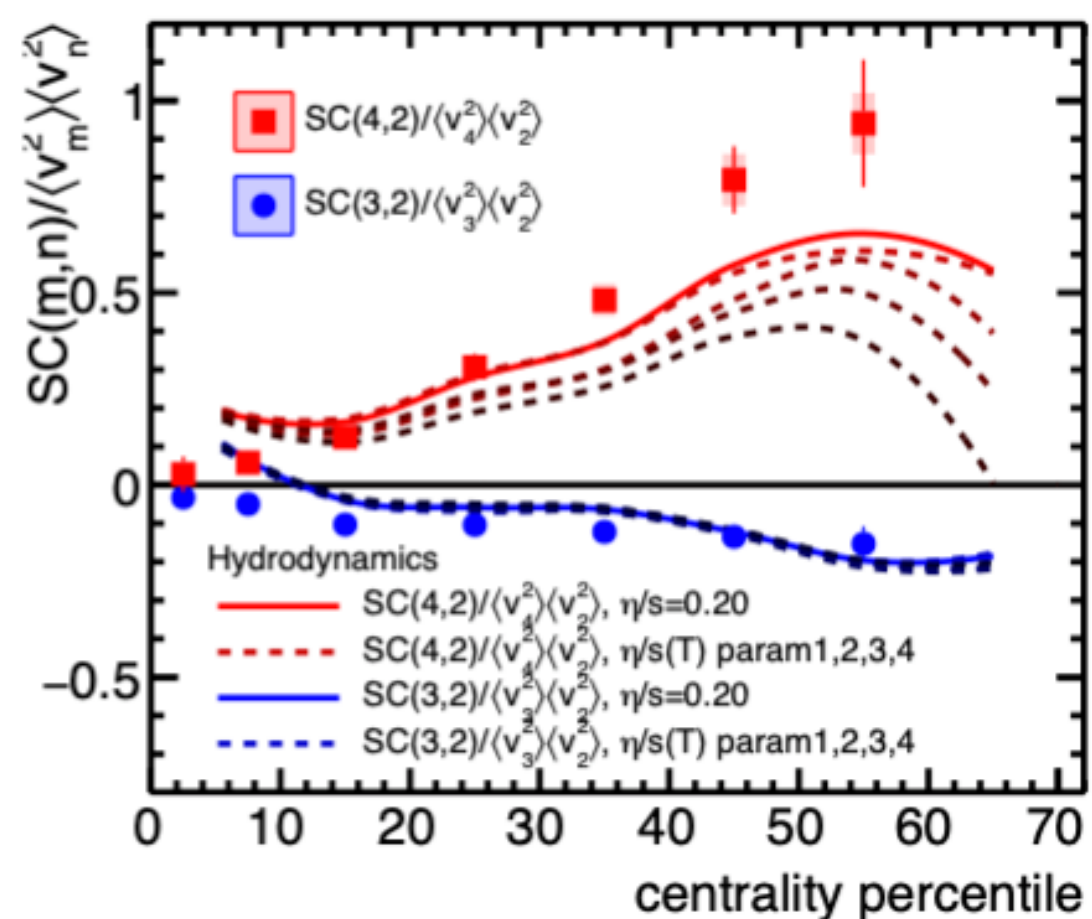
Zuzana Moravcova, Kristjan Gulbrandsen, and You Zhou  
Niels Bohr Institute, Blegdamsvej 17, 2100 Copenhagen, Denmark

- ❖ Multiparticle mixed harmonic cumulants
  - ▶ correlation between  $v_m^2$ ,  $v_n^2$  and  $v_p^2$
  - ▶ correlation between  $v_m^k$  and  $v_n^l$

## Mixed harmonic cumulants with 4-particles

$$\text{MHC}(v_m^2, v_n^2) = \text{SC}(m, n) = \langle v_m^2 v_n^2 \rangle - \langle v_m^2 \rangle \langle v_n^2 \rangle$$

$$\text{NSC}(m, n) = \frac{\text{SC}(m, n)}{\langle v_m^2 \rangle \langle v_n^2 \rangle}$$



Symmetric Cumulant, PRC89, 064904 (2014)

ALICE, PRL117, 182301 (2016)

- ▶ NSC(4,2) is sensitive to both initial conditions and  $\eta/s(T)$
- ▶ NSC(3,2) probes initial conditions

## Mixed harmonic cumulants with 6-particles

$$\begin{aligned} \text{MHC}(v_2^4, v_3^2) &= \langle \langle e^{i(2\varphi_1+2\varphi_2+3\varphi_3-2\varphi_4-2\varphi_5-3\varphi_6)} \rangle \rangle_c \\ &= \langle v_2^4 v_3^2 \rangle - 4 \langle v_2^2 v_3^2 \rangle \langle v_2^2 \rangle - \langle v_2^4 \rangle \langle v_3^2 \rangle \\ &\quad + 4 \langle v_2^2 \rangle^2 \langle v_3^2 \rangle. \end{aligned}$$

$$\begin{aligned} \text{MHC}(v_2^2, v_3^4) &= \langle \langle e^{i(2\varphi_1+3\varphi_2+3\varphi_3-2\varphi_4-3\varphi_5-3\varphi_6)} \rangle \rangle_c \\ &= \langle v_2^2 v_3^4 \rangle - 4 \langle v_2^2 v_3^2 \rangle \langle v_3^2 \rangle - \langle v_2^2 \rangle \langle v_3^4 \rangle \\ &\quad + 4 \langle v_2^2 \rangle \langle v_3^2 \rangle^2. \end{aligned}$$

$$\begin{aligned} \text{MHC}(v_2^2, v_3^2, v_4^2) &= \langle \langle e^{i(2\varphi_1+3\varphi_2+4\varphi_3-2\varphi_4-3\varphi_5-4\varphi_6)} \rangle \rangle_c \\ &= \langle v_2^2 v_3^2 v_4^2 \rangle - \langle v_2^2 v_3^2 \rangle \langle v_4^2 \rangle - \langle v_2^2 v_4^2 \rangle \langle v_3^2 \rangle \\ &\quad - \langle v_3^2 v_4^2 \rangle \langle v_2^2 \rangle + 2 \langle v_2^2 \rangle \langle v_3^2 \rangle \langle v_4^2 \rangle. \end{aligned}$$

## Mixed harmonic cumulants with 8-particles

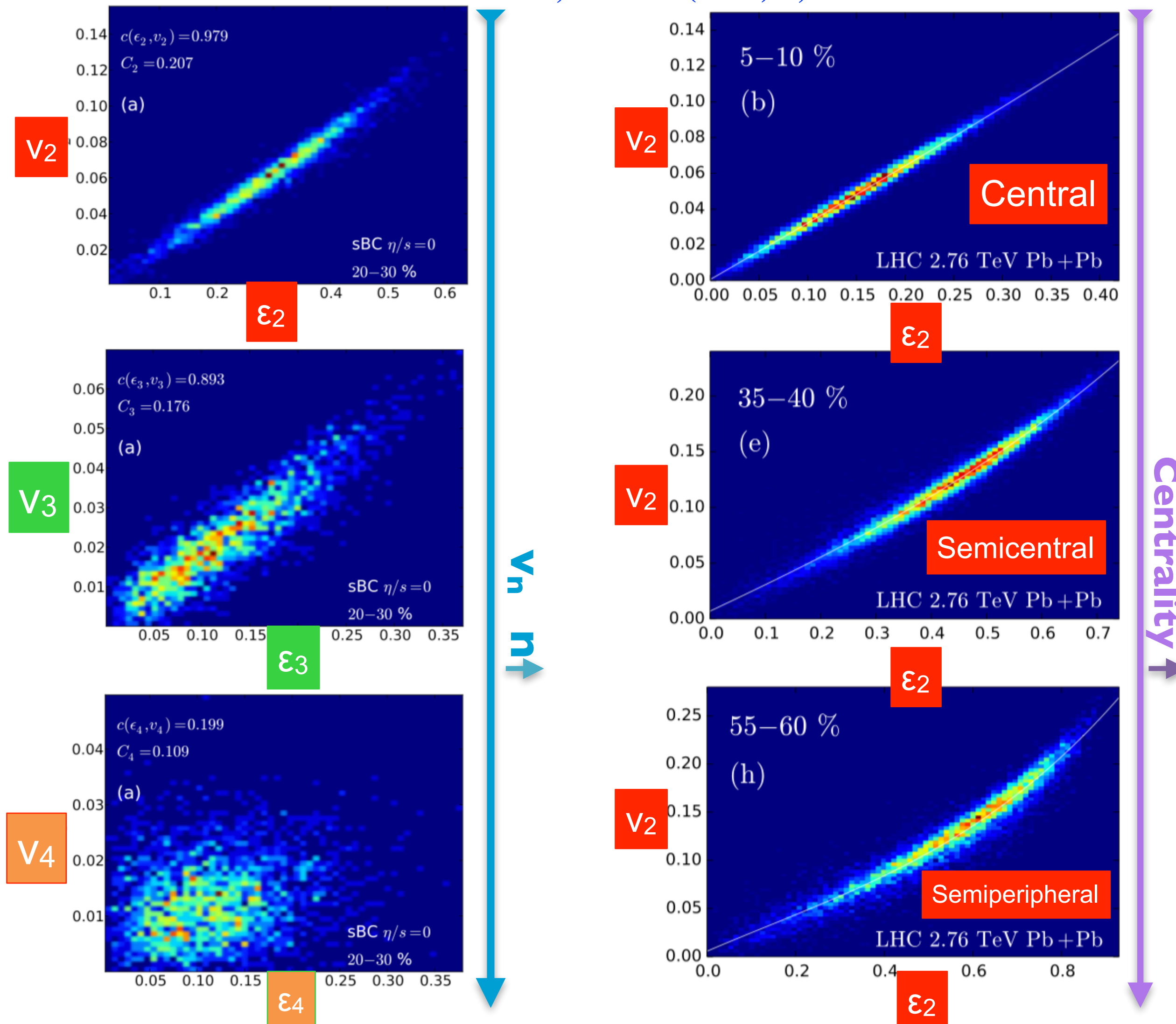
$$\begin{aligned} \text{MHC}(v_2^6, v_3^2) &= \langle \langle e^{i(2\varphi_1+2\varphi_2+2\varphi_3+3\varphi_4-2\varphi_5-2\varphi_6-2\varphi_7-3\varphi_8)} \rangle \rangle_c \\ &= \langle v_2^6 v_3^2 \rangle - 9 \langle v_2^4 v_3^2 \rangle \langle v_2^2 \rangle - \langle v_2^6 \rangle \langle v_3^2 \rangle \\ &\quad - 9 \langle v_2^4 \rangle \langle v_2^2 v_3^2 \rangle - 36 \langle v_2^2 \rangle^3 \langle v_3^2 \rangle \\ &\quad + 18 \langle v_2^2 \rangle \langle v_3^2 \rangle \langle v_2^4 \rangle + 36 \langle v_2^2 \rangle^2 \langle v_2^2 v_3^2 \rangle. \end{aligned}$$

$$\begin{aligned} \text{MHC}(v_2^4, v_3^4) &= \langle \langle e^{i(2\varphi_1+2\varphi_2+3\varphi_3+3\varphi_4-2\varphi_5-2\varphi_6-3\varphi_7-3\varphi_8)} \rangle \rangle_c \\ &= \langle v_2^4 v_3^4 \rangle - 4 \langle v_2^4 v_3^2 \rangle \langle v_3^2 \rangle \\ &\quad - 4 \langle v_2^2 v_3^4 \rangle \langle v_2^2 \rangle - \langle v_2^4 \rangle \langle v_3^4 \rangle \\ &\quad - 8 \langle v_2^2 v_3^2 \rangle^2 - 24 \langle v_2^2 \rangle^2 \langle v_3^2 \rangle^2 \\ &\quad + 4 \langle v_2^2 \rangle^2 \langle v_3^4 \rangle + 4 \langle v_2^4 \rangle \langle v_3^2 \rangle^2 \\ &\quad + 32 \langle v_2^2 \rangle \langle v_3^2 \rangle \langle v_2^2 v_3^2 \rangle. \end{aligned}$$

$$\begin{aligned} \text{MHC}(v_2^2, v_3^6) &= \langle \langle e^{i(2\varphi_1+3\varphi_2+3\varphi_3+3\varphi_4-2\varphi_5-3\varphi_6-3\varphi_7-3\varphi_8)} \rangle \rangle_c \\ &= \langle v_2^2 v_3^6 \rangle - 9 \langle v_2^2 v_3^4 \rangle \langle v_3^2 \rangle - \langle v_3^6 \rangle \langle v_2^2 \rangle \\ &\quad - 9 \langle v_3^4 \rangle \langle v_2^2 v_3^2 \rangle - 36 \langle v_2^2 \rangle \langle v_3^2 \rangle^3 \\ &\quad + 18 \langle v_2^2 \rangle \langle v_3^2 \rangle \langle v_3^4 \rangle + 36 \langle v_3^2 \rangle^2 \langle v_2^2 v_3^2 \rangle. \end{aligned}$$

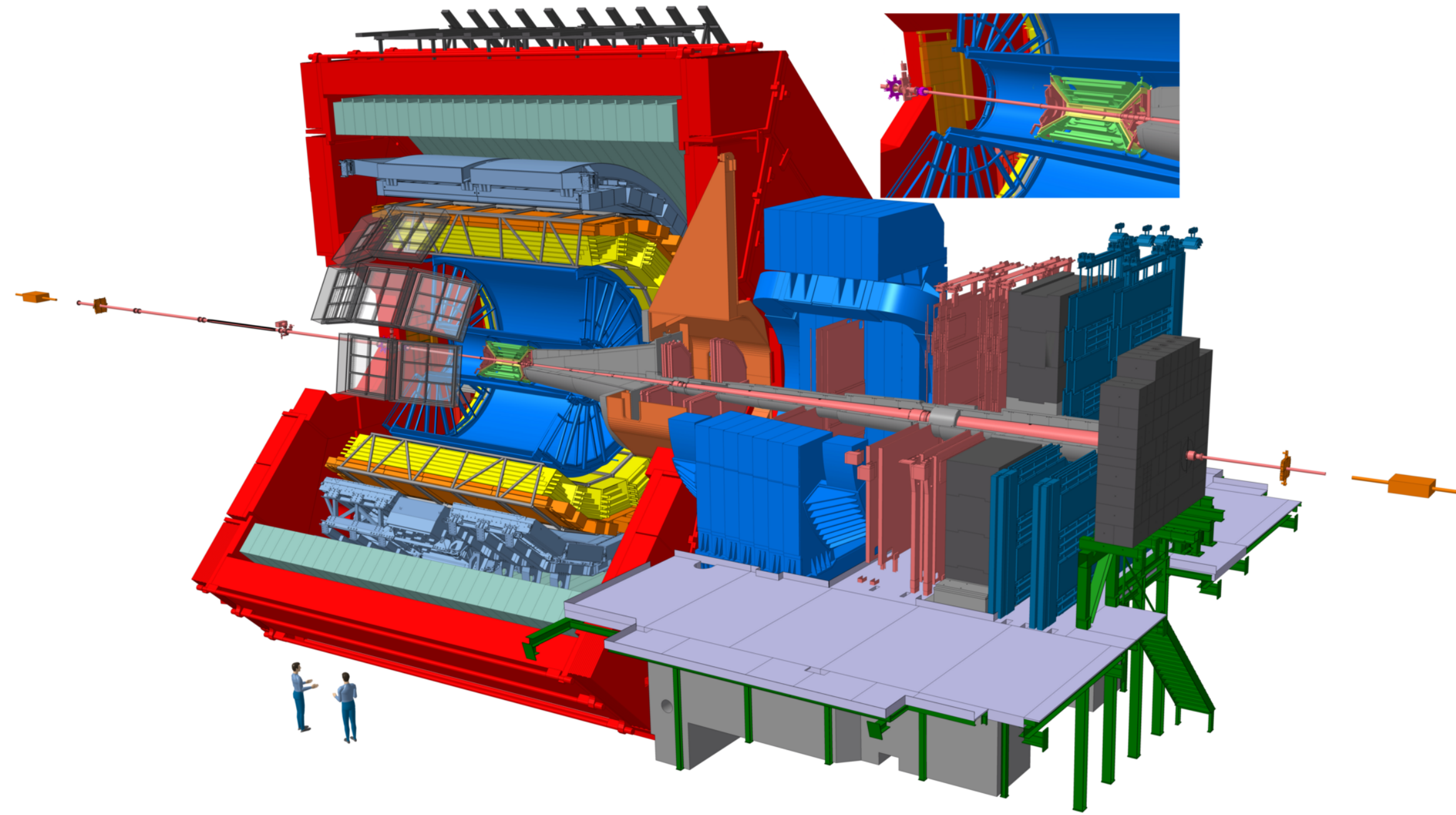
# Linear and nonlinear hydrodynamic response

H. Niemi etc, PRC 87 (2013) 5, 054901



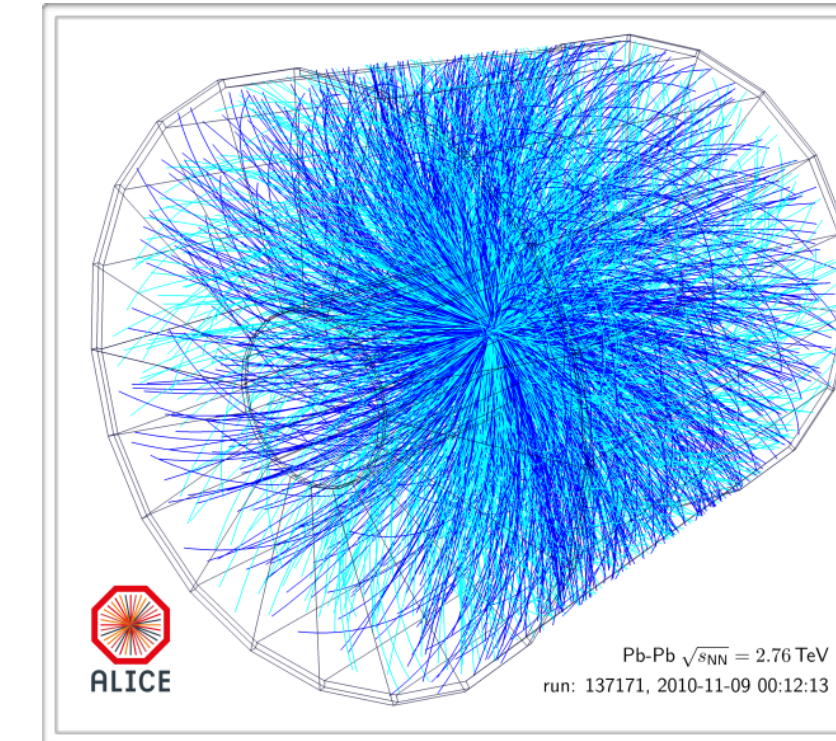
- ❖  $v_n$  has both linear and nonlinear hydrodynamic response to initial anisotropy
  - ▶ Stronger linear response in  $v_2$  than  $v_3$  and  $v_4$
  - ▶ Stronger linear correlations between  $v_n$  and  $\epsilon_n$  in central than peripheral collision
- ❖ Study linear and nonlinear hydrodynamic response with nMHC
  - ▶  $v_n = K_n \cdot \epsilon_n$  (linear response)
    - >  $nMHC(v_m^k, v_n^l) = nMHC(\epsilon_m^k, \epsilon_n^l)$
    - > use  $nMHC(v_m^k, v_n^l)$  to constrain the initial conditions
  - ▶  $v_n \neq K_n \cdot \epsilon_n$  (nonlinear response)
    - >  $nMHC(v_m^k, v_n^l) \neq nMHC(\epsilon_m^k, \epsilon_n^l)$
    - > use  $nMHC(v_m^k, v_n^l)$  to probe properties of QGP
- ❖ Expectations: better agreements in central collisions and for lower harmonics

# This analysis

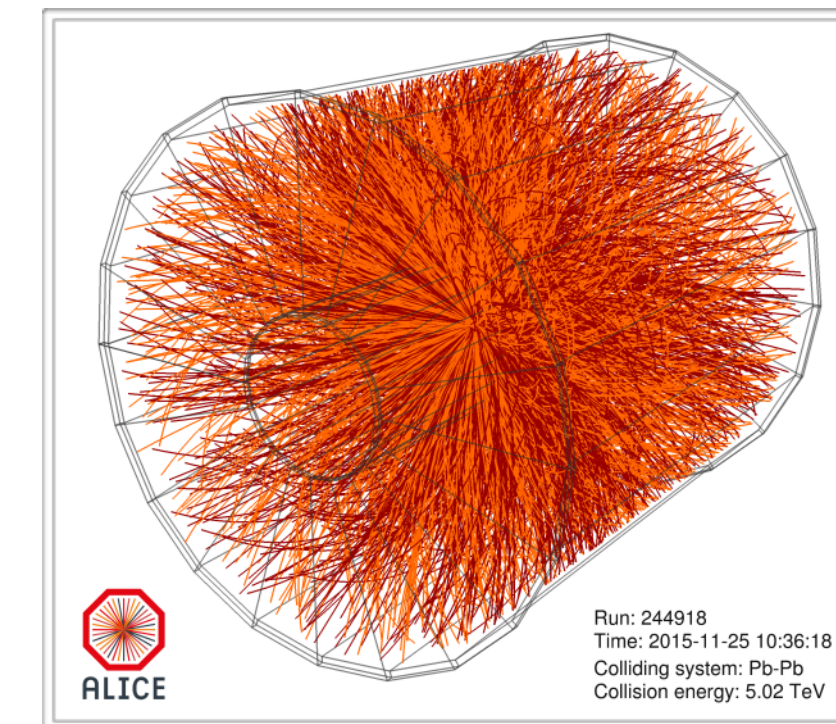


## ❖ Detectors used:

- ▶ Inner Tracking System  
(trigger, tracking and vertexing)
- ▶ Time Projection Chamber  
(tracking)
- ▶ V0 detectors  
(trigger, centrality determination)



Pb-Pb 2.76 TeV



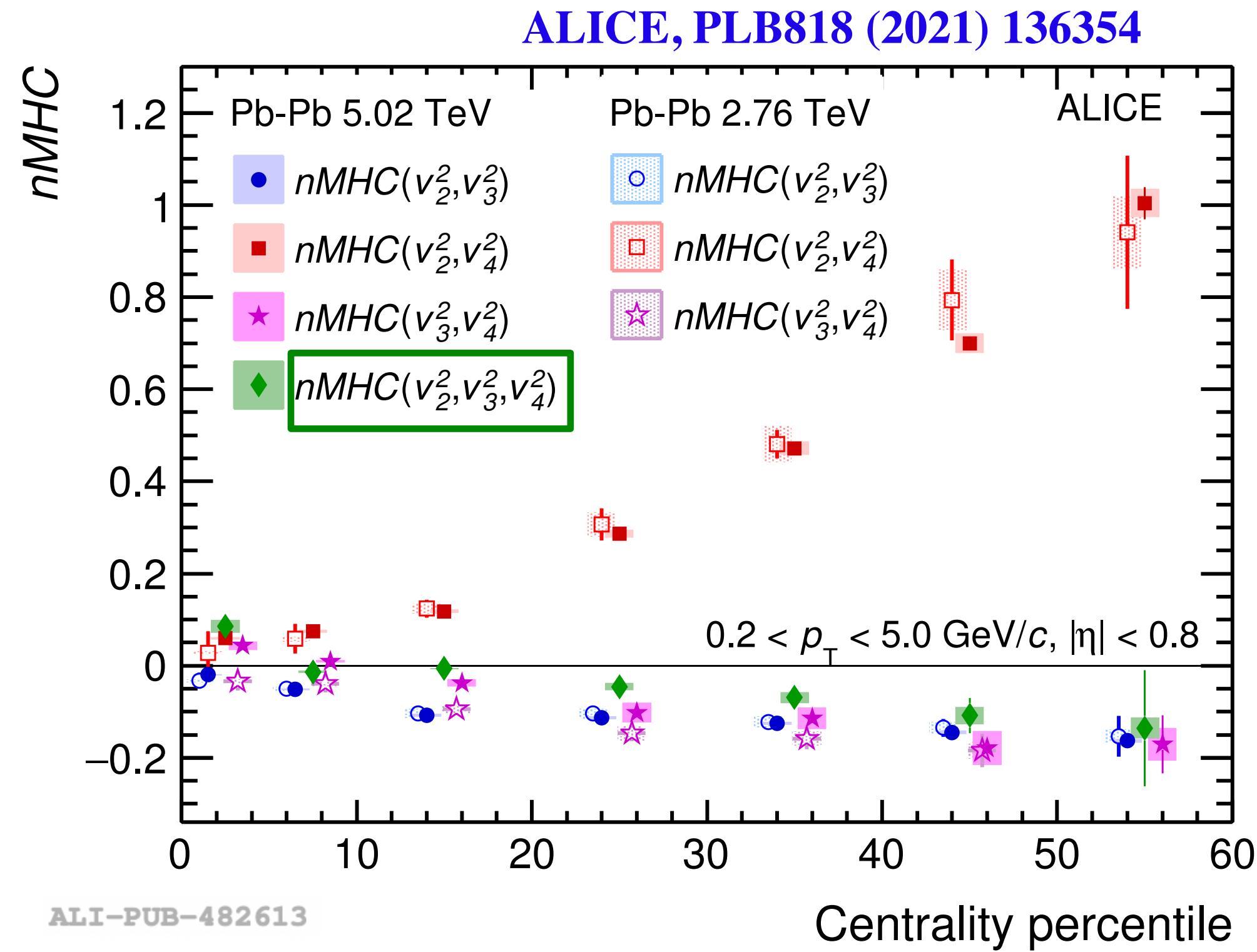
Pb-Pb 5.02 TeV

## ❖ Data samples:

- ▶ Pb-Pb at  $\sqrt{s_{NN}} = 2.76$  TeV
- ▶ Pb-Pb at  $\sqrt{s_{NN}} = 5.02$  TeV
- ▶ Tracks used:
  - $-0.8 < \eta < 0.8$
  - $0.2 < p_T < 5.0$  GeV/c

# Correlation between $v_m^2$ , $v_n^2$ and $v_p^2$

NEW

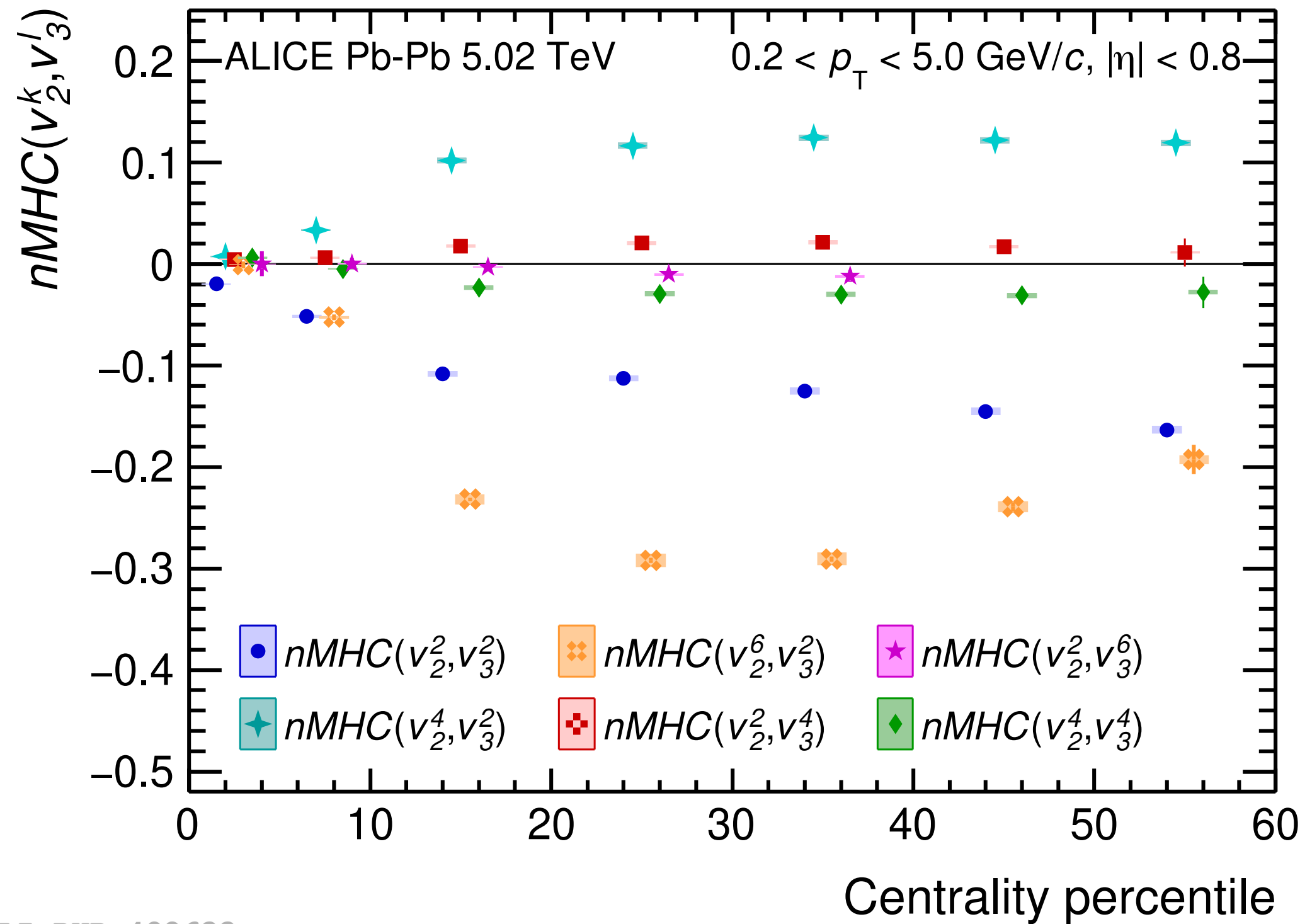


- ❖ Non-zero value of  $nMHC(v_2^2, v_3^2, v_4^2)$  in Pb-Pb collisions
  - ▶ Highly non-trivial correlations among three flow coefficients
  - ▶ The result is positive and closer to  $nMHC(v_2^2, v_4^2)$  and  $nMHC(v_3^2, v_4^2)$  in central collisions
  - ▶ It is negative and follows  $nMHC(v_2^2, v_3^2)$  and  $nMHC(v_3^2, v_4^2)$  in non-central collisions

# First measurement of $v_m^k$ and $v_n^l$ correlations

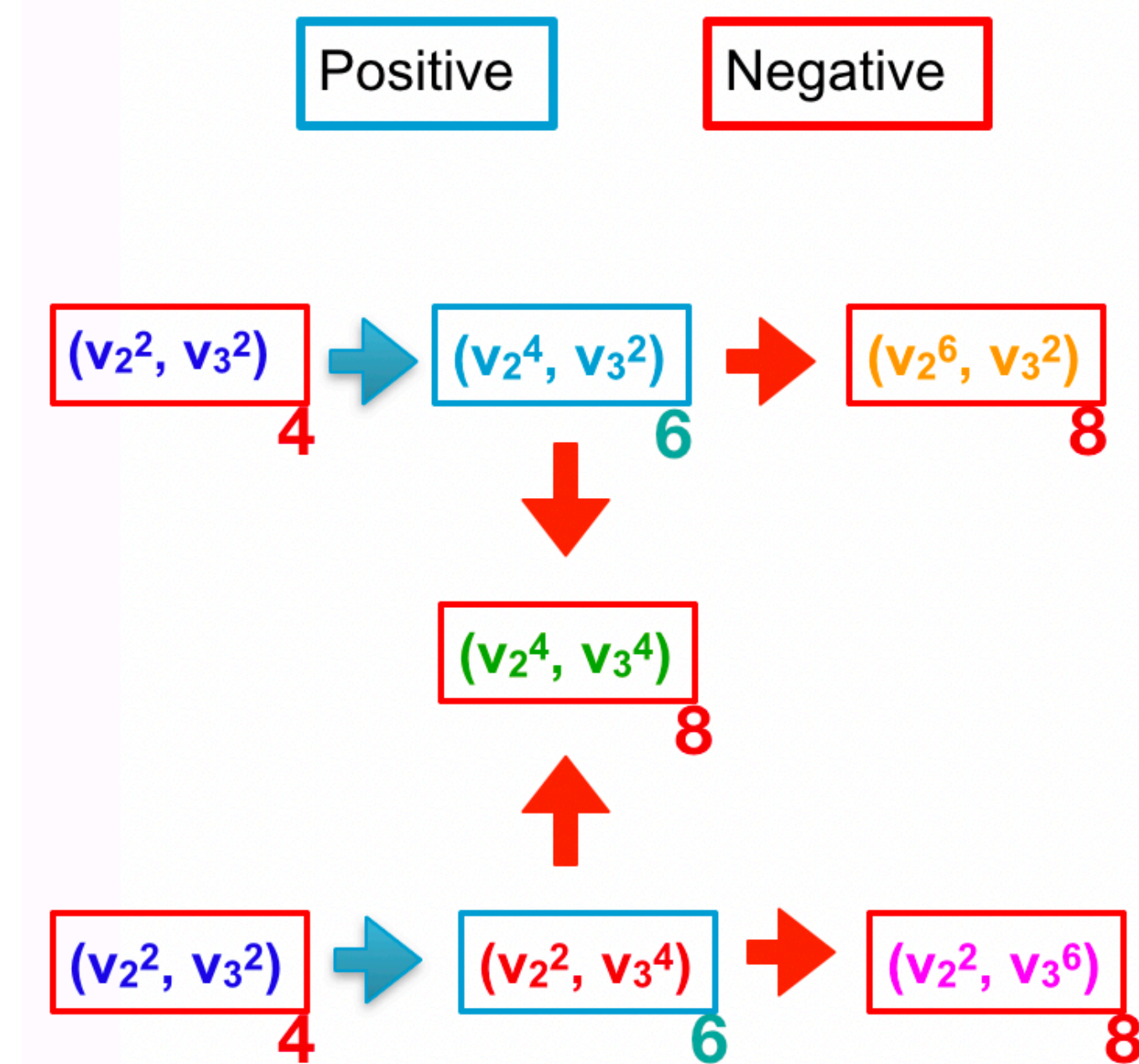
ALICE, PLB818 (2021) 136354

NEW



ALI-PUB-482633

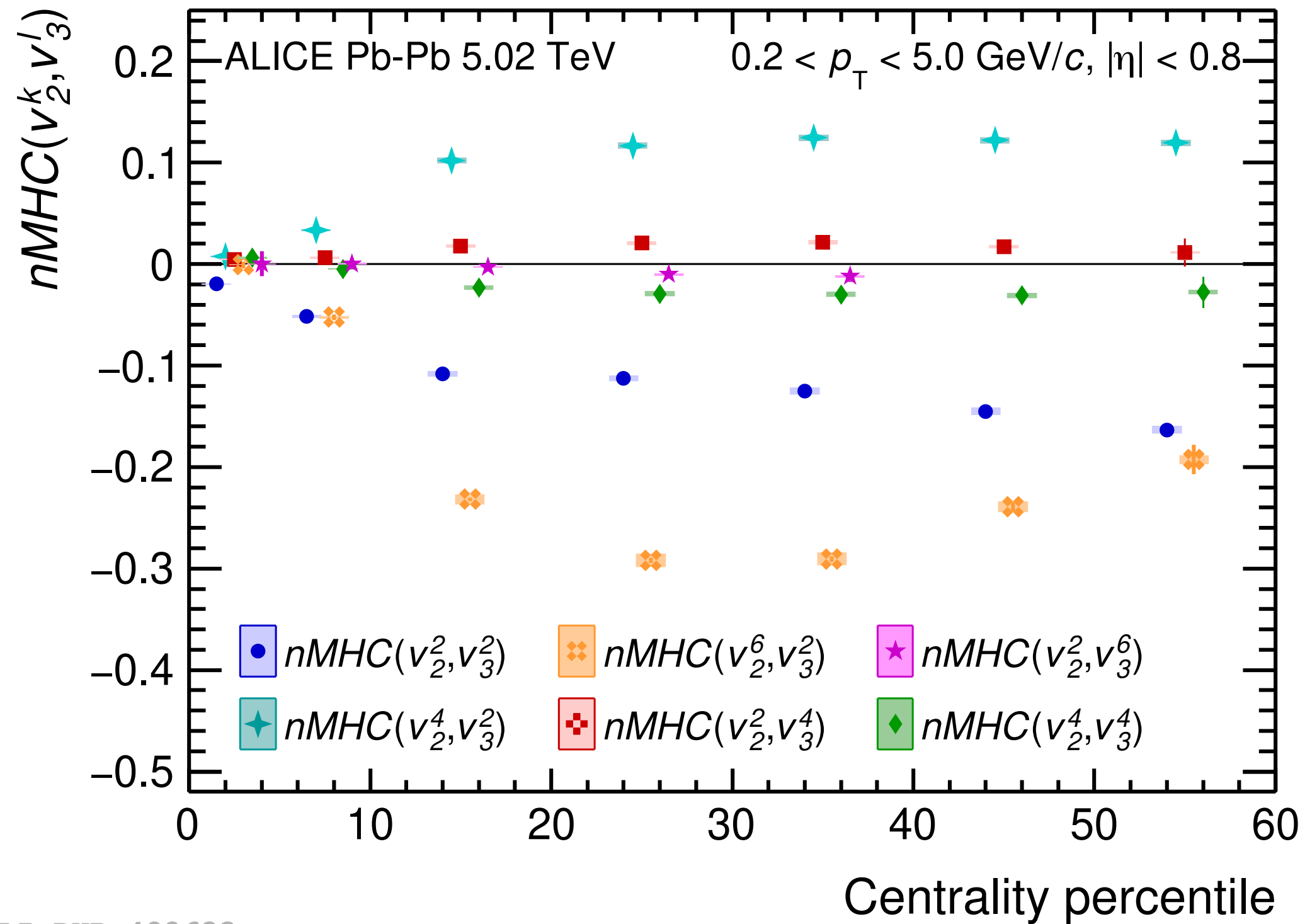
- ❖ First measurement of correlations between higher order moments of  $v_2$  and  $v_3$ 
  - ▶ characteristic -, +, - signs observed for 4-, 6- and 8-particle cumulants of *mixed harmonics*



# First measurement of $v_m^k$ and $v_n^l$ correlations

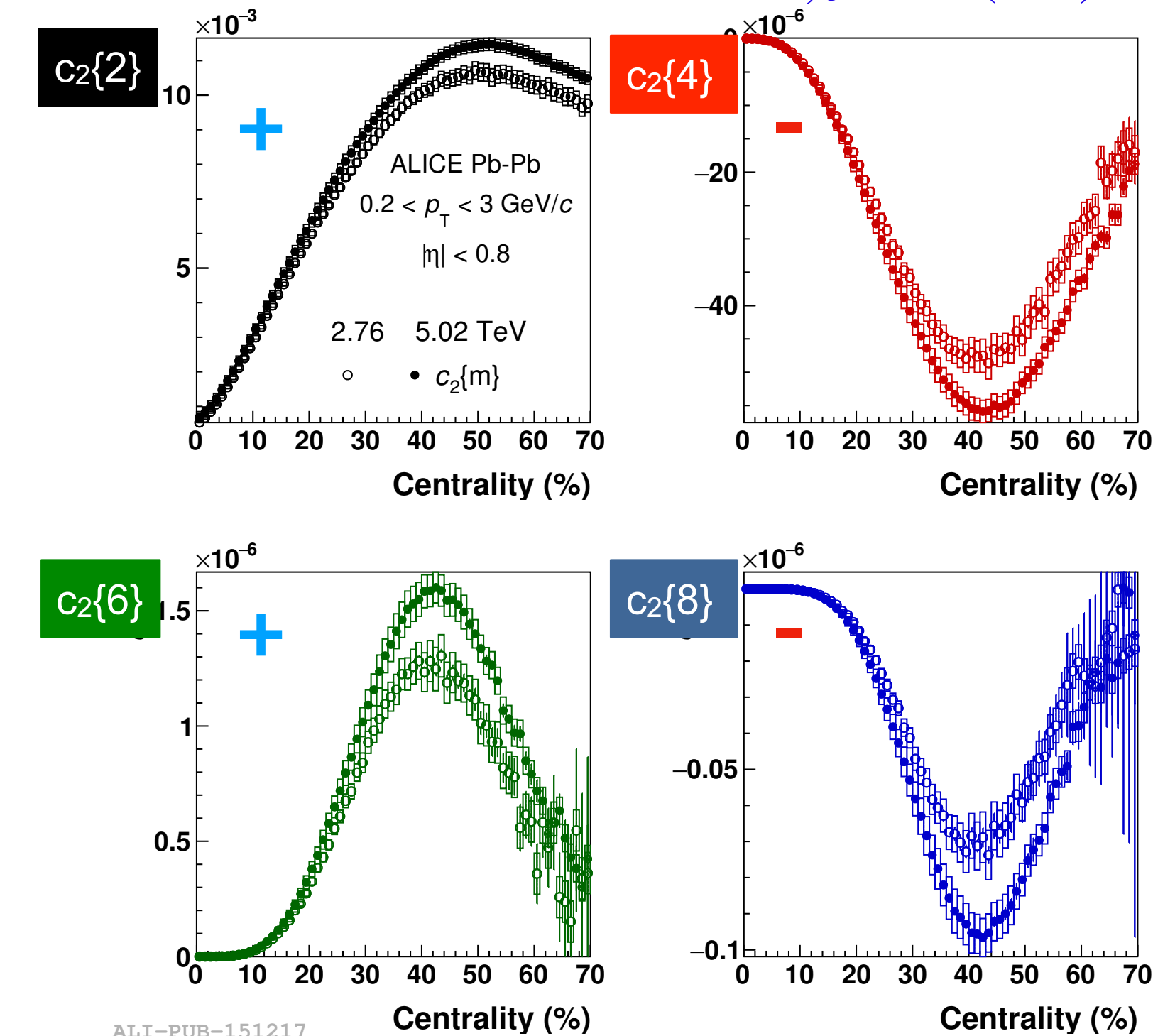
ALICE, PLB818 (2021) 136354

NEW



ALI-PUB-482633

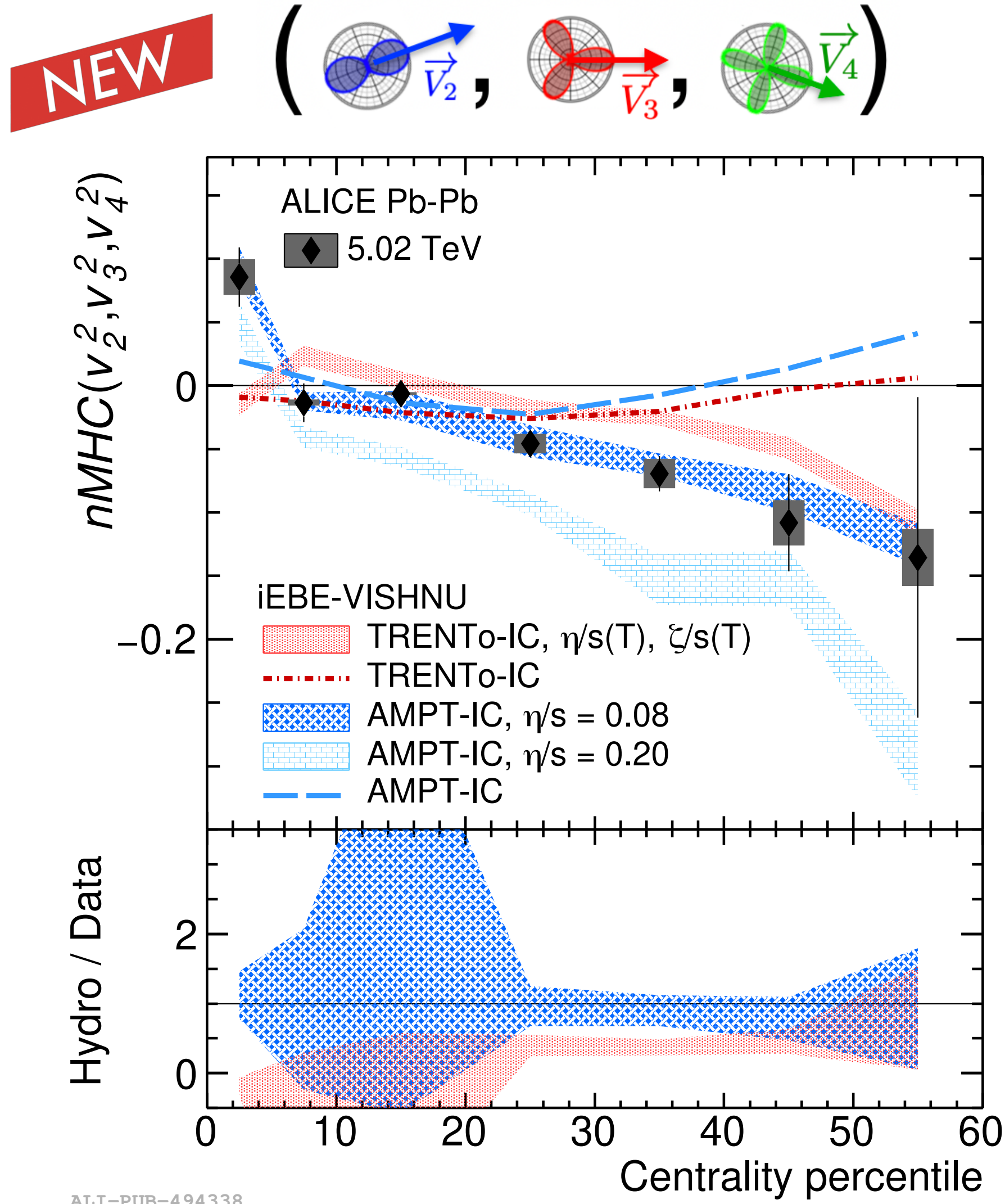
ALICE, JHEP07 (2018) 103



- ❖ First measurement of correlations between higher order moments of  $v_2$  and  $v_3$ 
  - ▶ characteristic -, +, - signs observed for 4-, 6- and 8-particle cumulants of *mixed harmonic*
  - ▶ Similar to +, -, +, - signs seen in 2-, 4-, 6- and 8-particle cumulants of *single harmonic*
  - ▶ A *potential probe of collectivity in small systems*



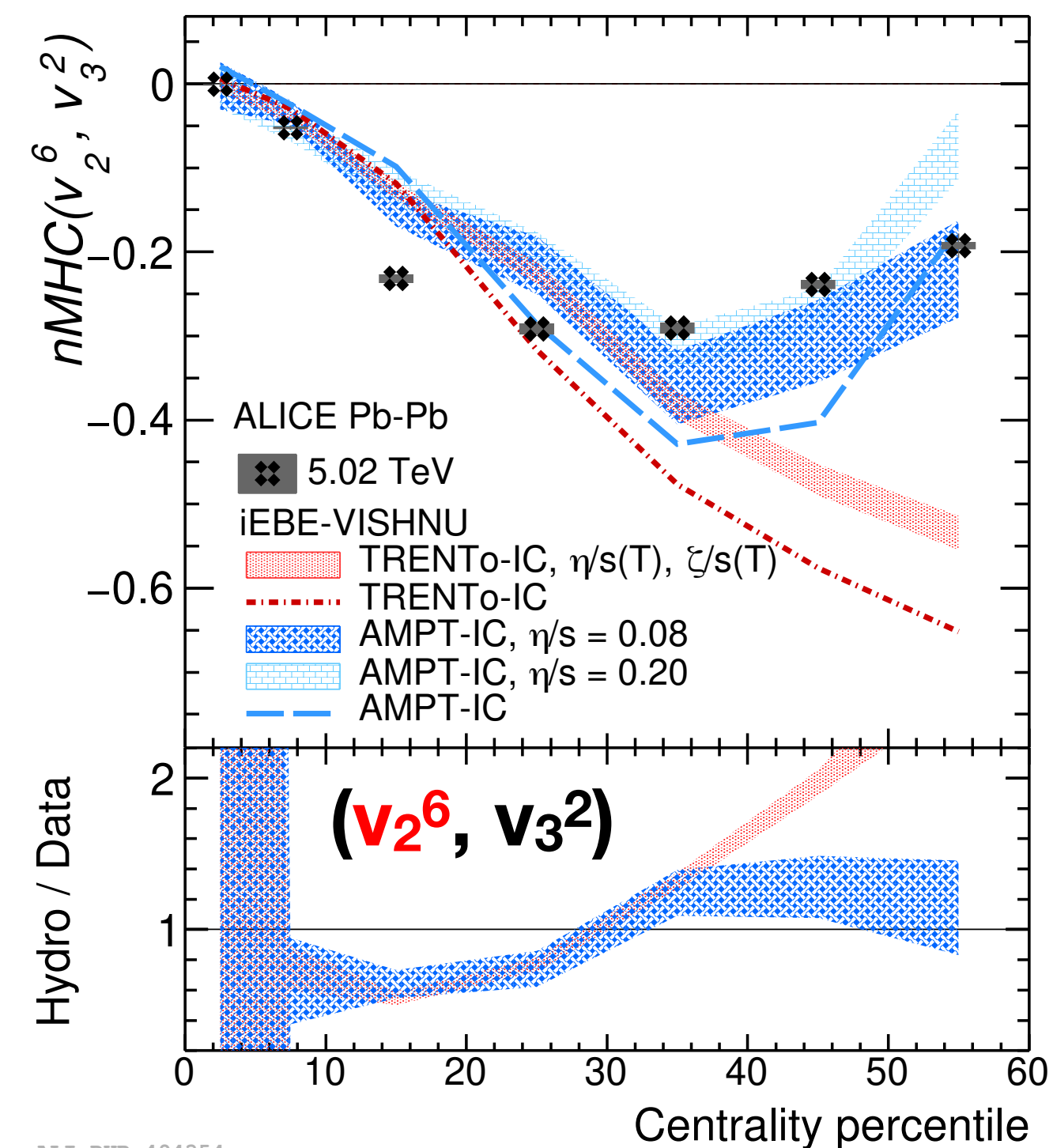
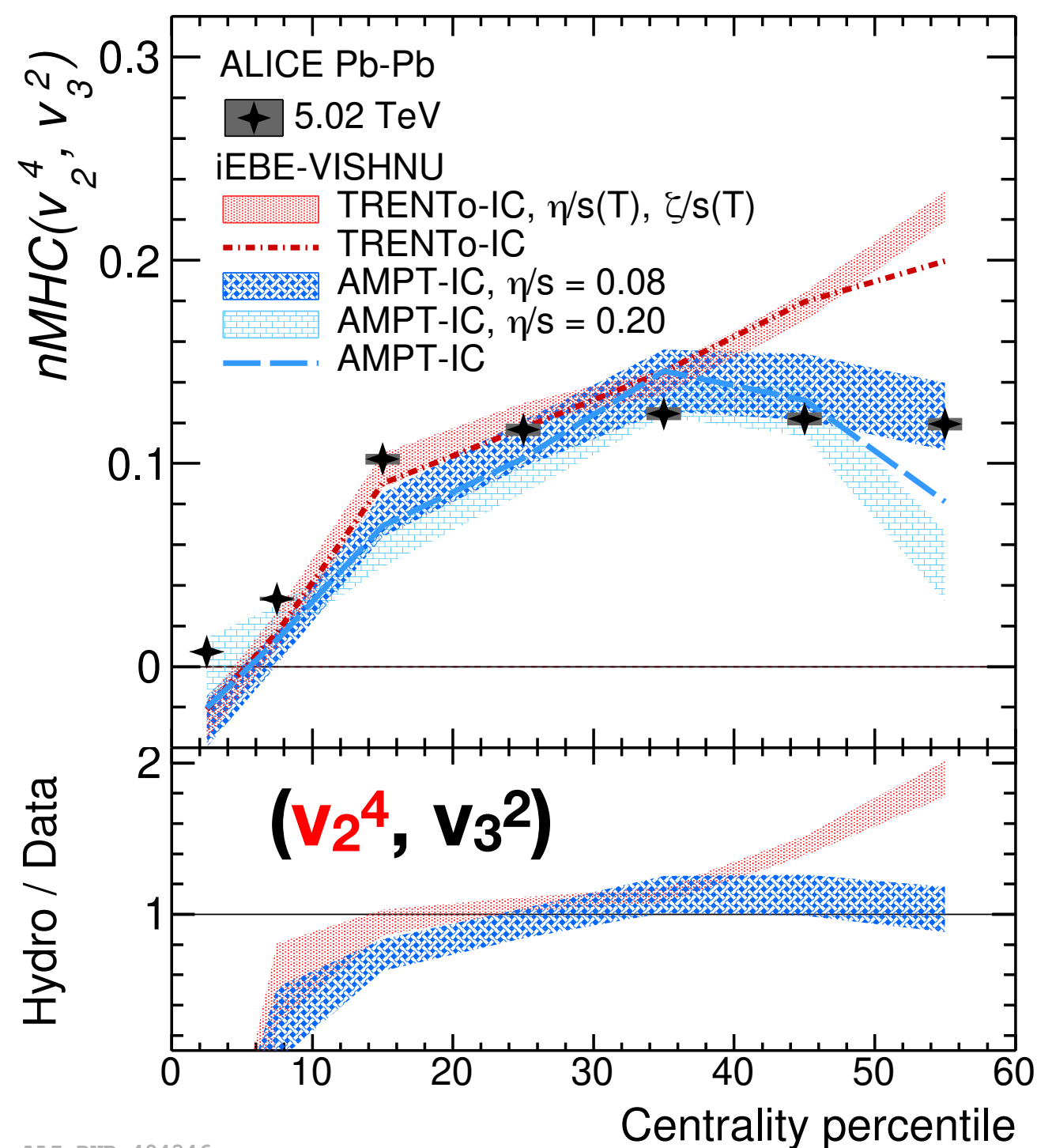
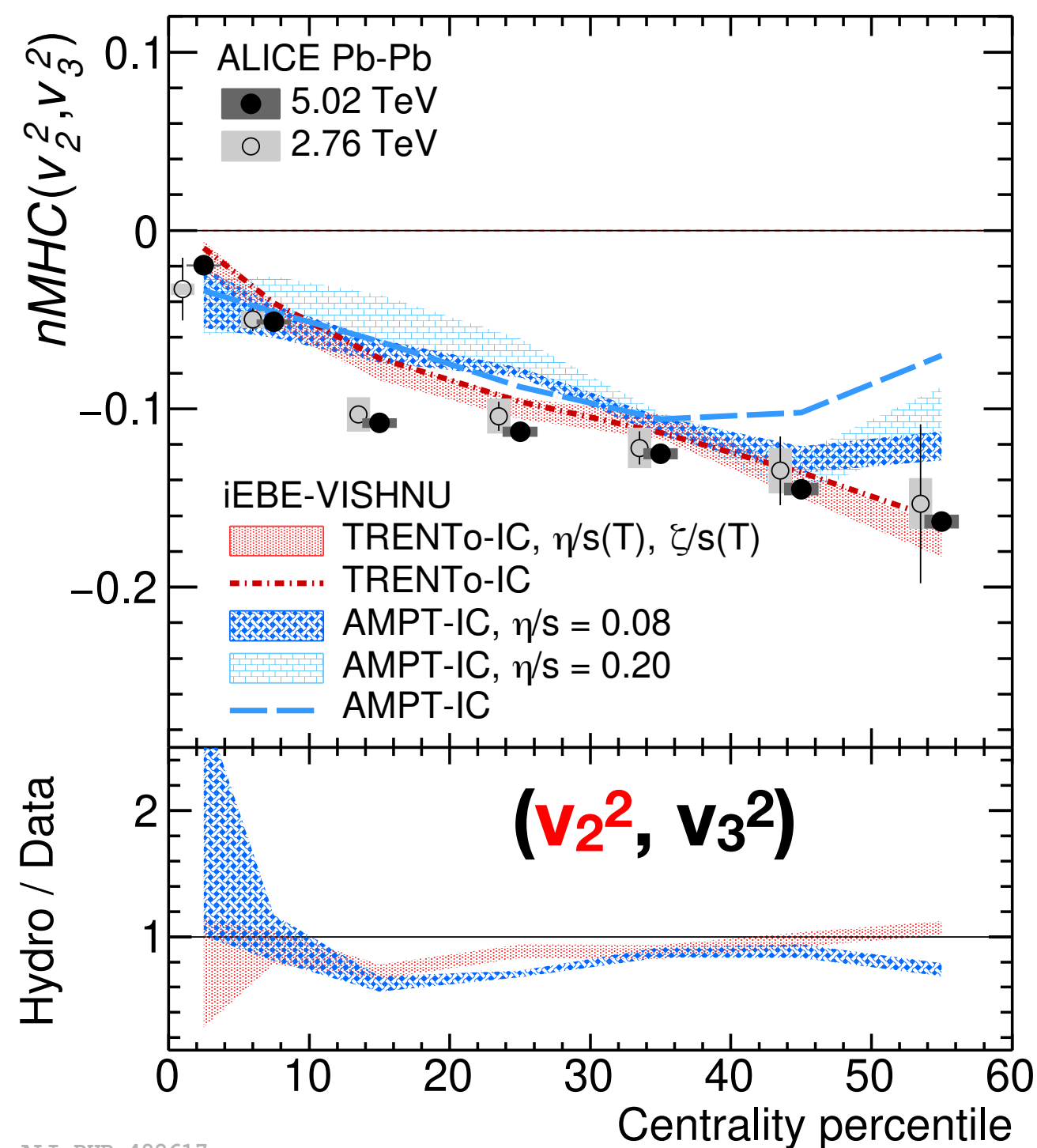
# Data vs hydro: $v_m^2$ , $v_n^2$ and $v_p^2$ correlations



- ❖  $nMHC(v_2^2, v_3^2, v_4^2) \neq nMHC(\epsilon_2^2, \epsilon_3^2, \epsilon_4^2)$ 
  - ▶ Non-linear response
  - ▶  $nMHC(v_2^2, v_3^2, v_4^2)$  is sensitive to  $\eta/s$  of QGP
- ❖ AMPT+iEBE-VISHNU calculations quantitatively agree with the ALICE data
- ❖ TRENTo+iEBE-VISHNU calculations underestimate the data by 50%
- ❖ A new challenge for the current understanding of initial conditions and QGP properties from Bayesian analysis (TRENTo+iEBE-VISHNU) with the presented  $nMHC(v_m^2, v_n^2, v_p^2)$  data

# $v_2^k$ and $v_3^2$ correlations

NEW

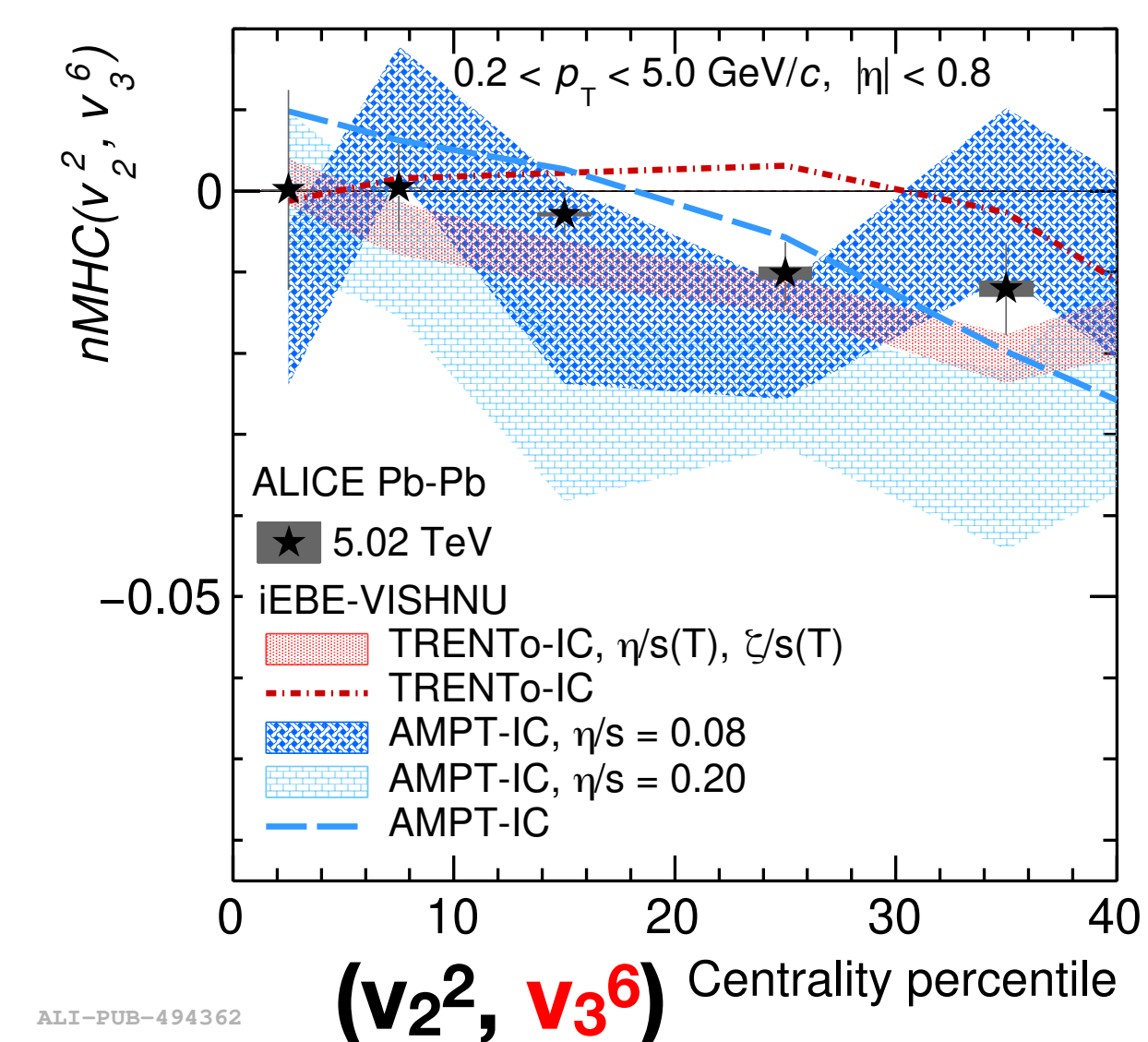
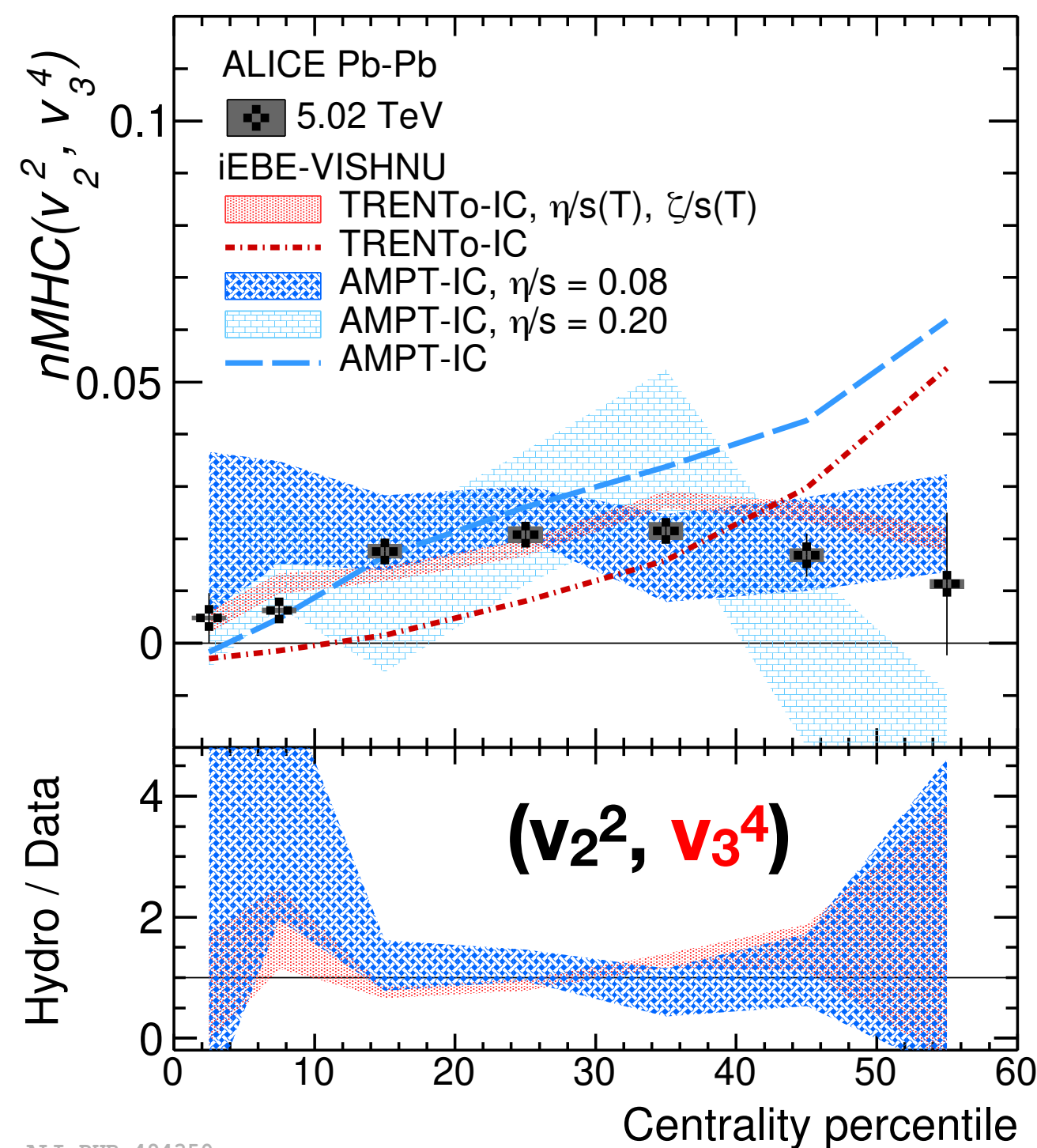
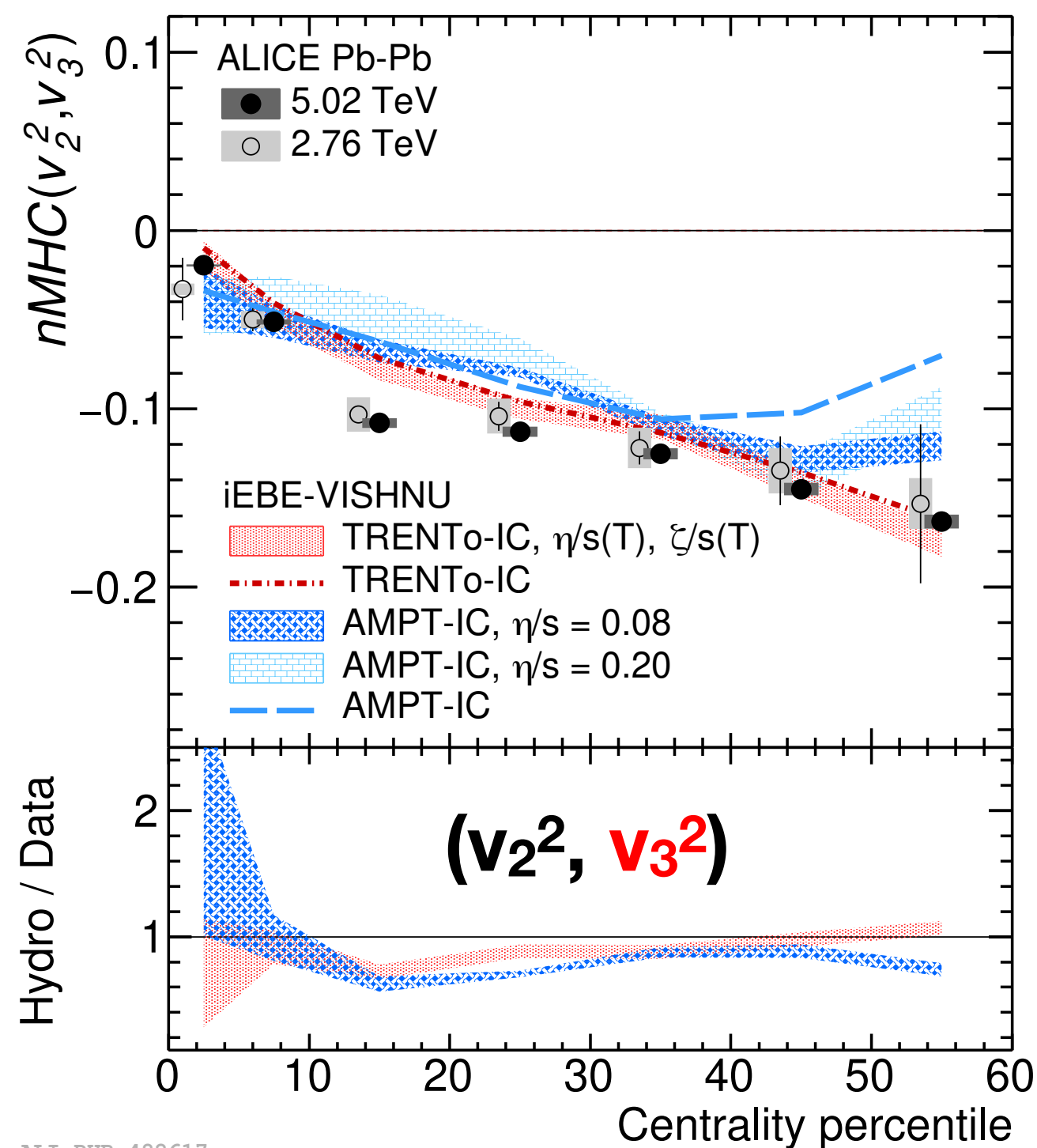


ALICE, PLB818 (2021) 136354  
 M. Li etc, arXiv:2104.10422

- ❖ Good agreement between initial eccentricity estimations and final  $nMHC(v_2^k, v_3^2)$  in central collisions
- ❖ Deviations are getting larger in more peripheral collisions and/or for higher order moments of  $v_2$ 
  - ▶ Non-linear response of  $v_2$  in non-central Pb-Pb collisions
- ❖ AMPT+iEBE-VISHNU calculations work better in peripheral collisions

# $v_2^2$ and $v_3^\ell$ correlations

NEW



ALICE, PLB818 (2021) 136354  
 M. Li etc, arXiv:2104.10422

- ❖ Deviations between initial eccentricity estimations and final  $nMHC(v_2^2, v_3^\ell)$  already in central collisions
  - ▶ Stronger nonlinear response of  $v_3$  than  $v_2$  in Pb-Pb collisions
    - > more sensitive to  $\eta/s(T)$  of QGP
- ❖ Both hydro calculations are compatible with data within large uncertainties

# Summary

- ❖ General correlations between flow coefficients are studied using mixed harmonic cumulants
  - ▶ Non-zero  $nMHC(v_2^2, v_3^2, v_4^2)$  is observed, results are sensitive to the initial conditions and shear and bulk viscosities of the QGP
  - ▶ *Negative, positive and negative* signs of 4-, 6- and 8-particle cumulants with mixed harmonics have been observed
  - ▶ The results involving higher-order moments could significantly enhance the contributions that arise from nonlinearities of  $v_2$  and  $v_3$  to  $\epsilon_2$  and  $\epsilon_3$
- ❖ Further information on the initial conditions and tighter constraints on the evolution of the QGP

*Thanks for your attention!*



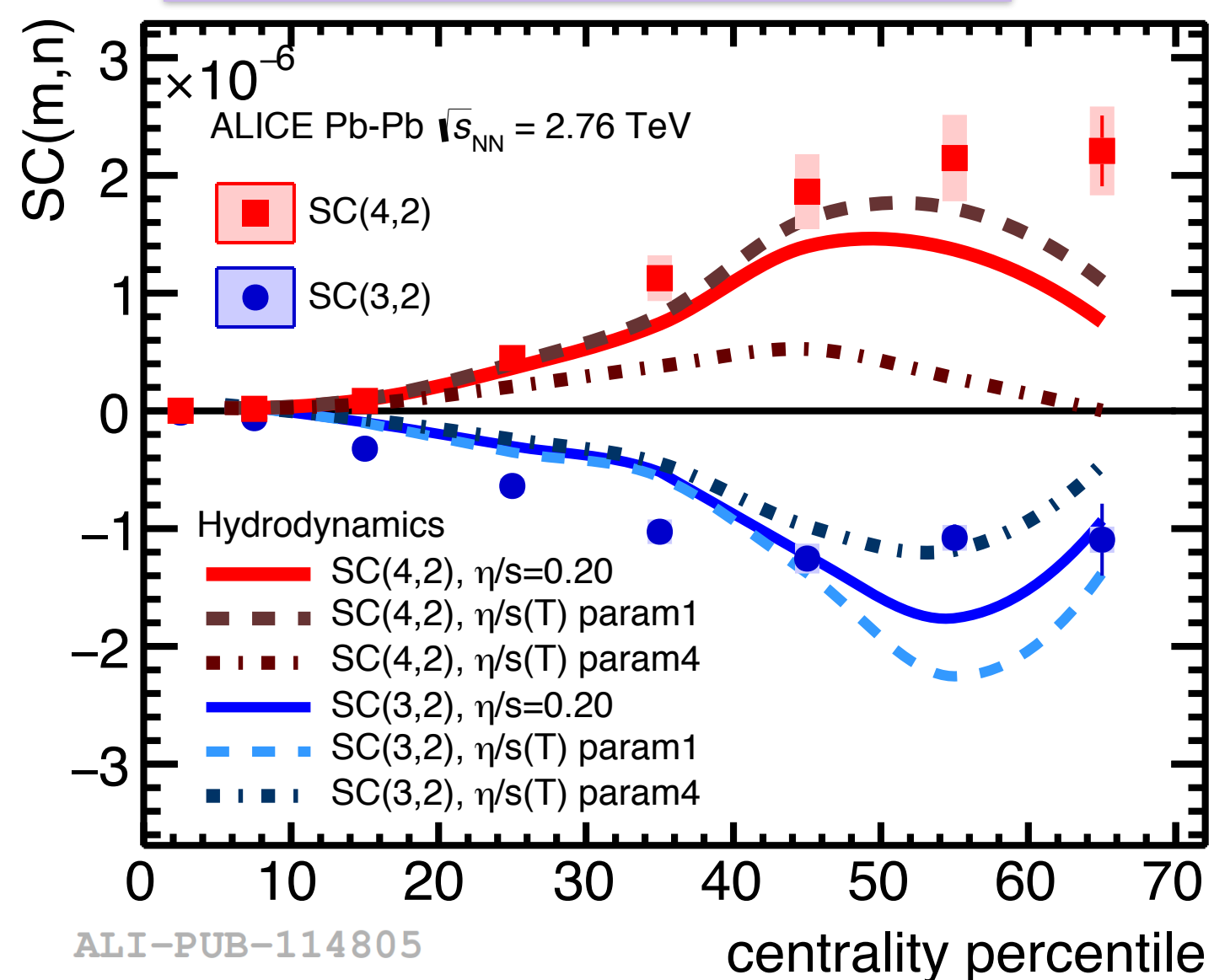
# Backup



# Correlations between $v_m$ and $v_n$

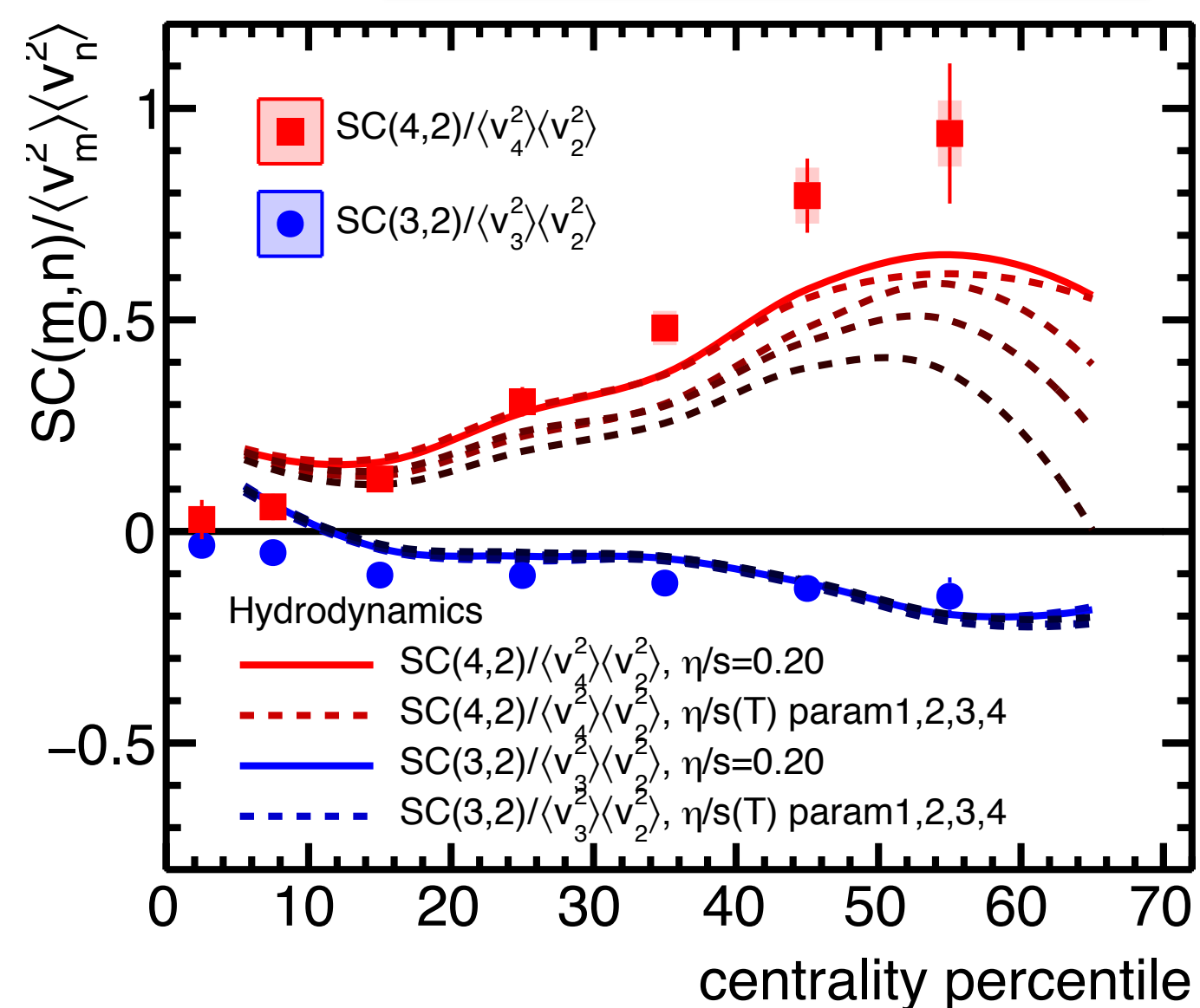
## Symmetric cumulants:

$$SC(m, n) = \langle v_m^2 v_n^2 \rangle - \langle v_m^2 \rangle \langle v_n^2 \rangle$$



## Normalized Symmetric cumulants:

$$NSC(m, n) = \frac{SC(m, n)}{\langle v_m^2 \rangle \langle v_n^2 \rangle}$$

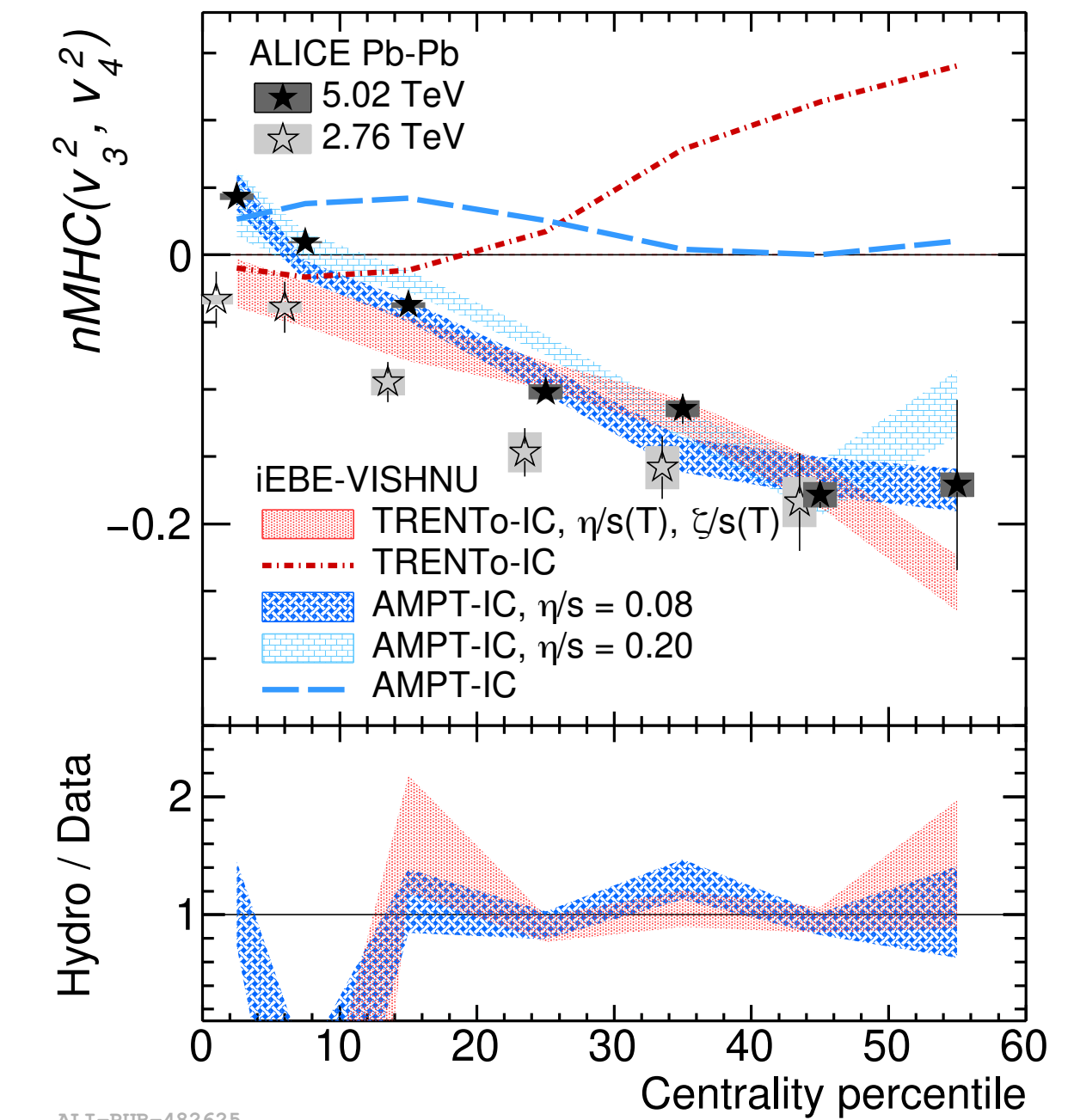
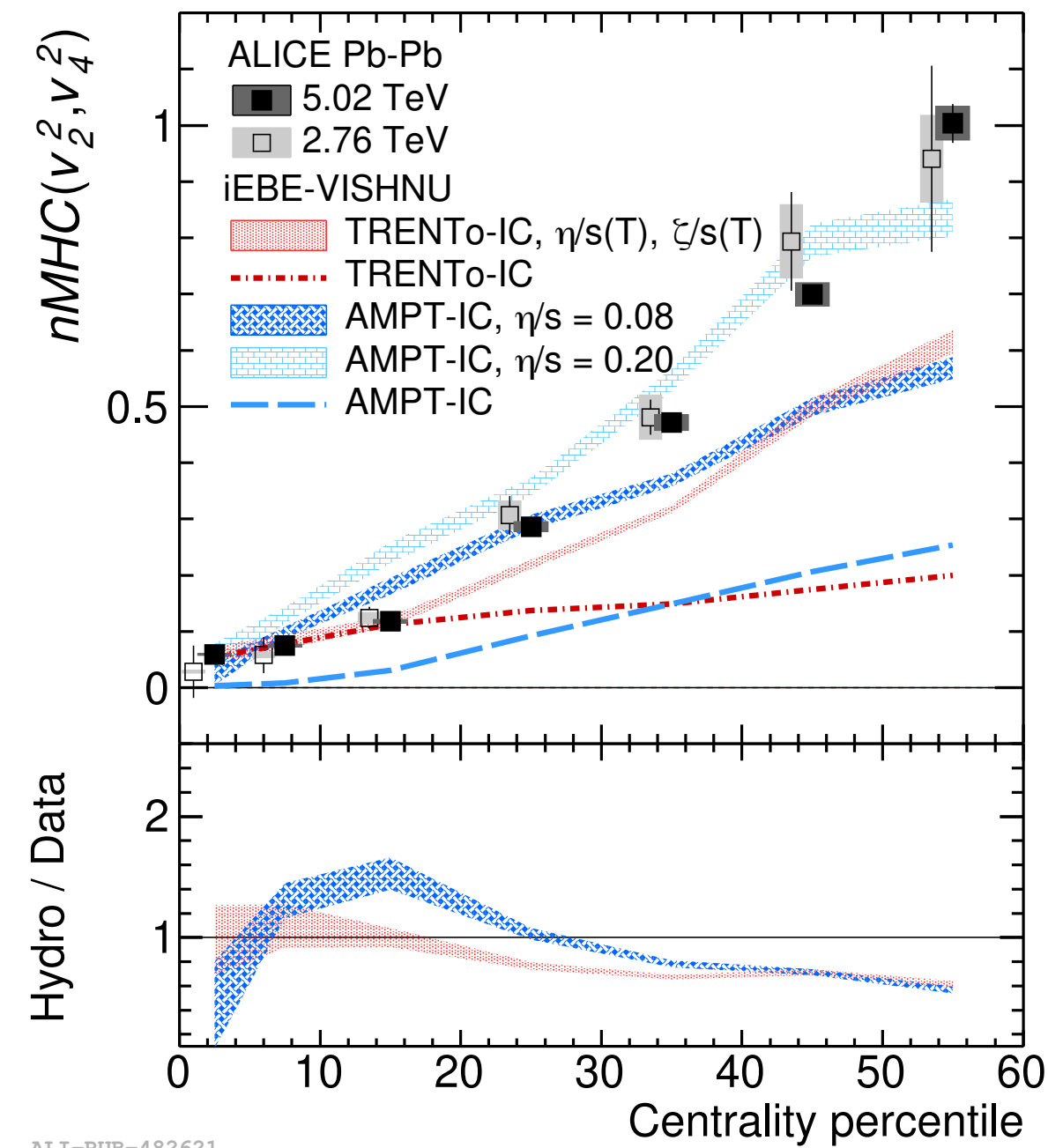
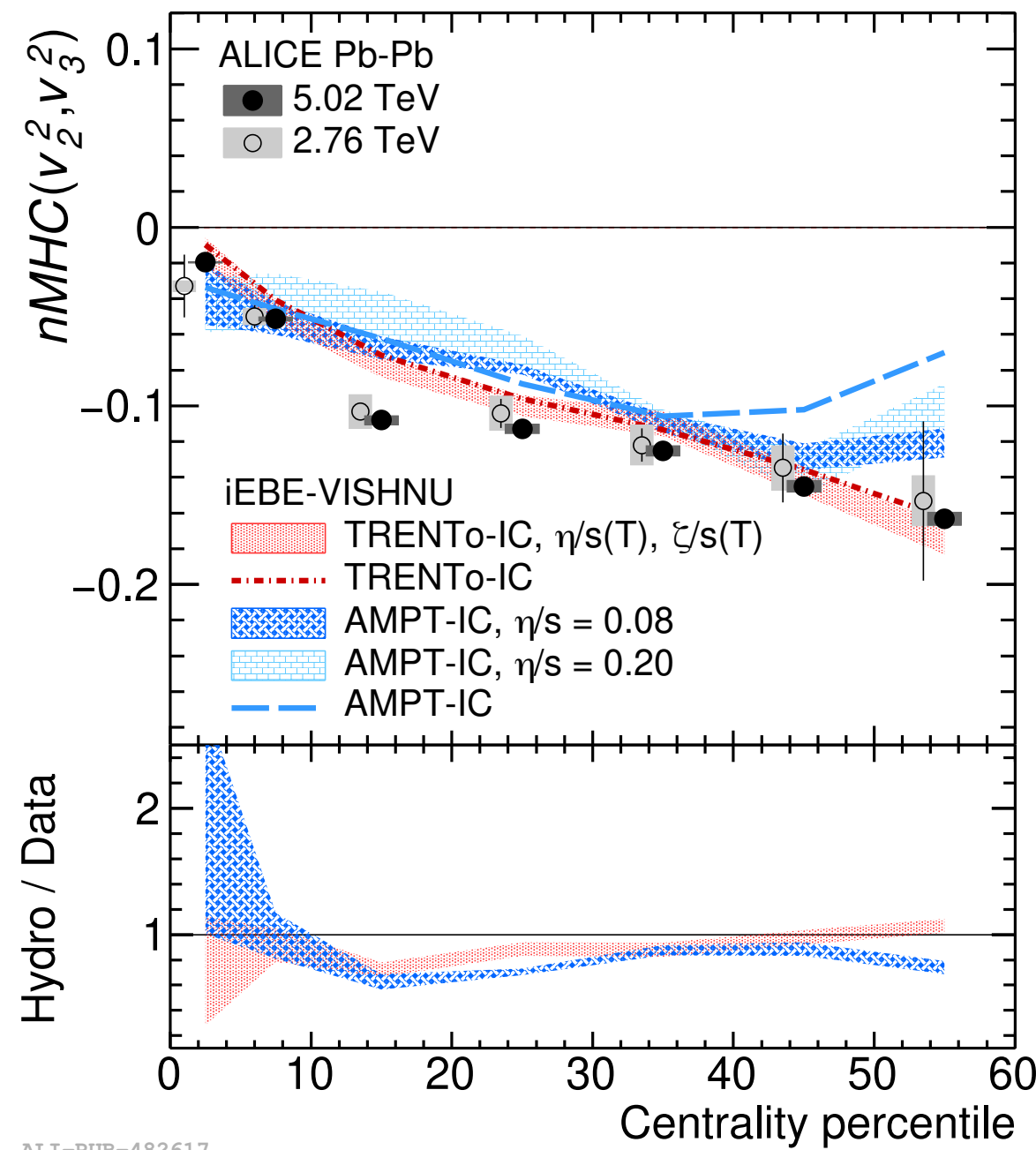
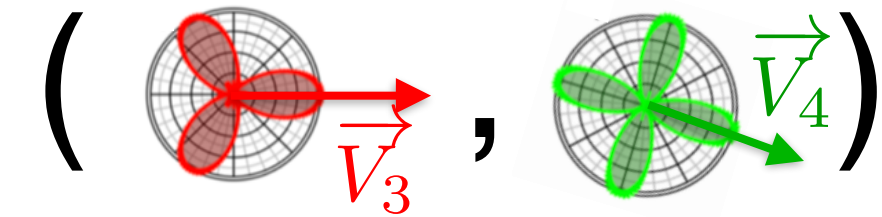
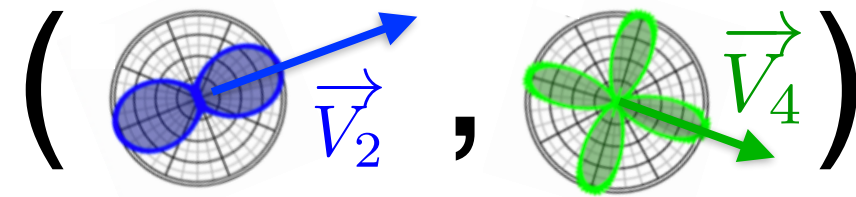
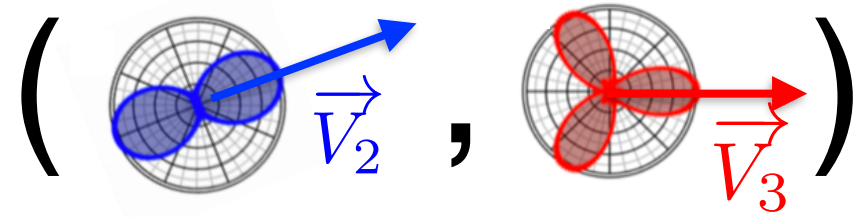


Symmetric Cumulant,  
PRC89, 064904 (2014)

ALICE,  
PRL117, 182301 (2016)

- ❖ Comparison of SC and Normalized SC (NSC) to hydrodynamic calculations
  - ▶ Although hydrodynamic calculations describes  $v_n$  fairly well, do not describe SC and NSC
    - > tighter constraints!
  - ▶ NSC(3,2) measurements provide direct access into the initial conditions
  - ▶ NSC(4,2) is sensitive to both initial conditions and  $\eta/s(T)$

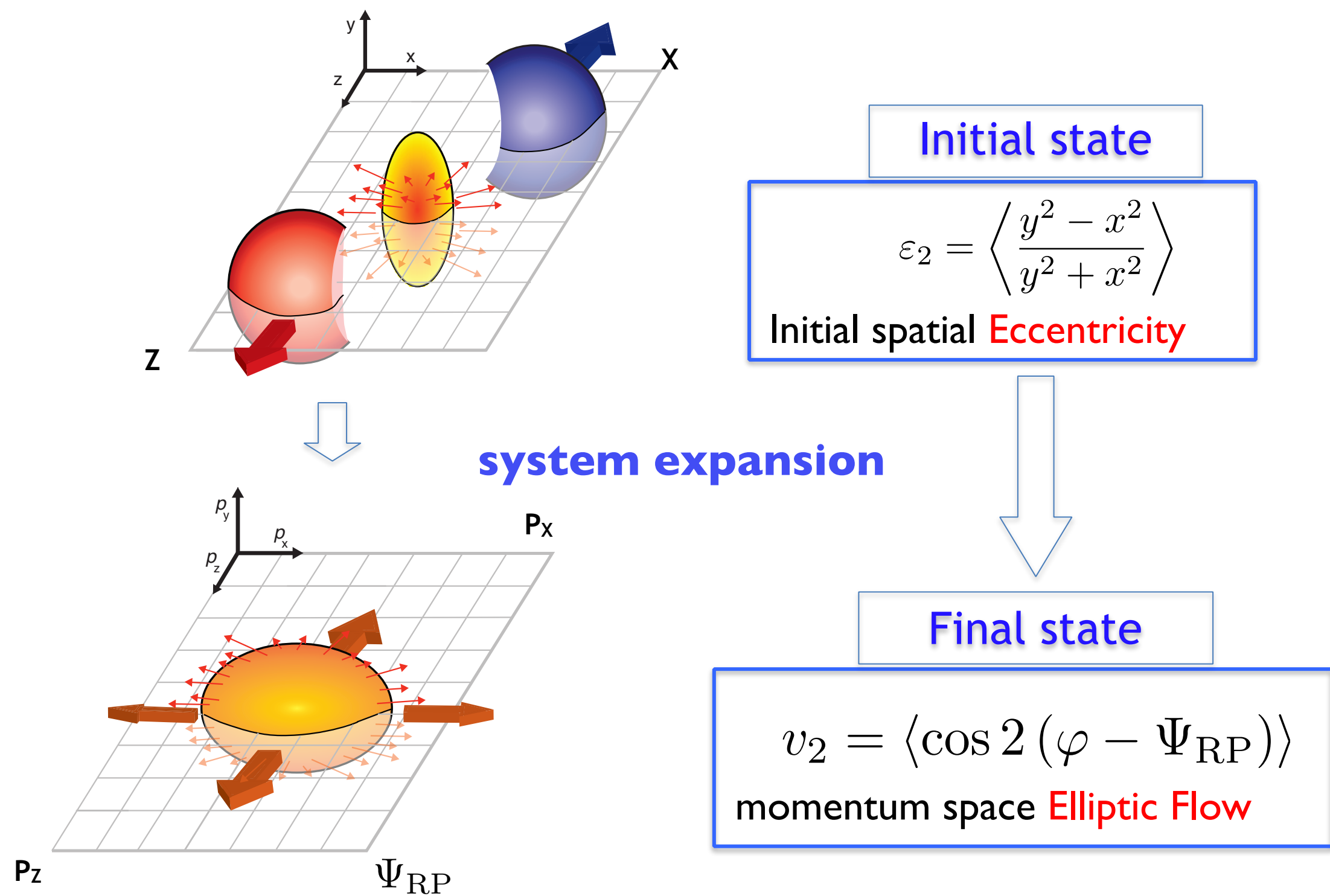
# Data vs hydro: $v_m^k$ and $v_n^l$ correlations



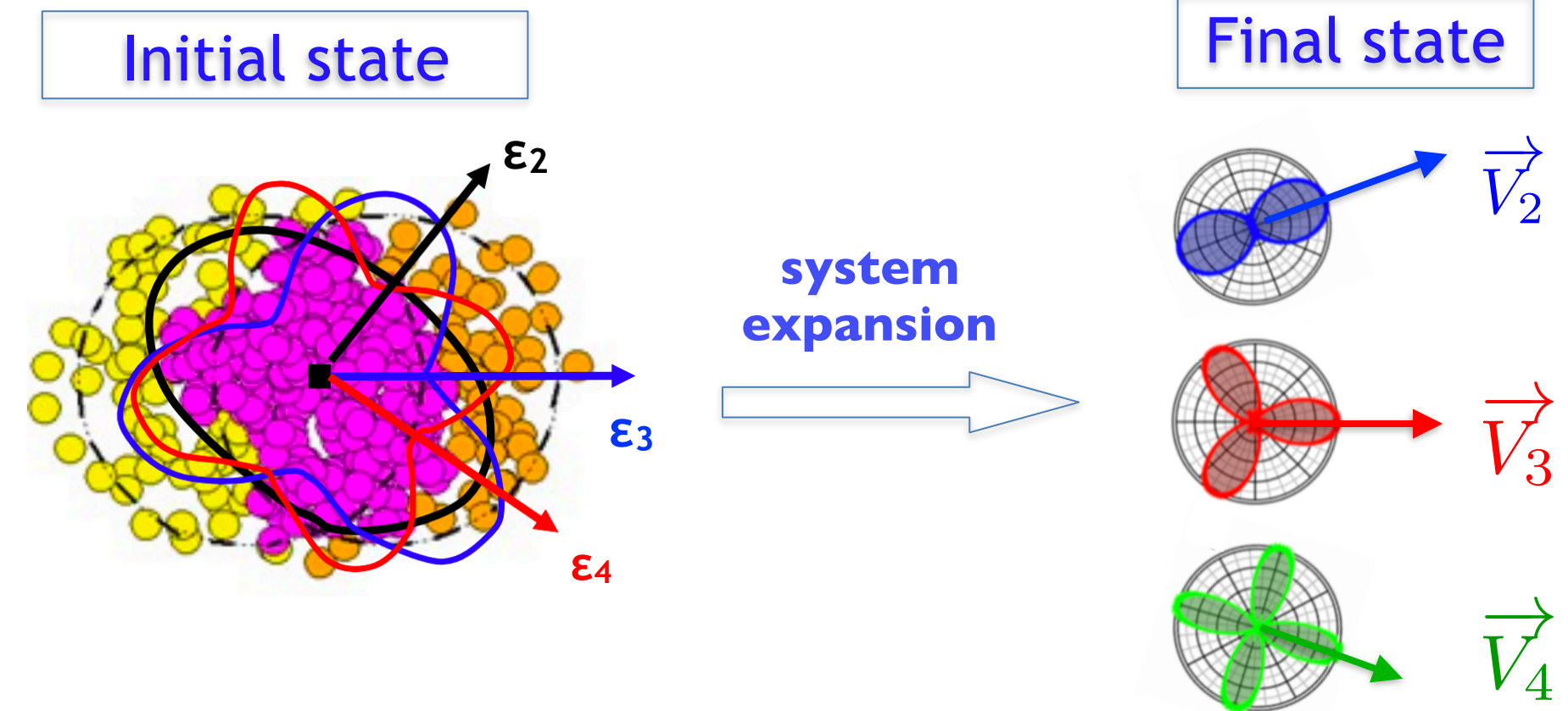
ALICE, PLB818 (2021) 136354

- ❖  $nMHC(v_2^2, v_3^2)$  is insensitive to  $\eta/s$ , reflects information from the initial conditions
- ❖  $nMHC(v_2^2, v_4^2)$  and  $nMHC(v_3^2, v_4^2)$  are very different from  $nMHC(\epsilon_m^k, \epsilon_n^l)$ 
  - ▶ Significant contributions from nonlinear hydrodynamic response
- ❖ Deviation of  $nMHC(v_3^2, v_4^2)$  from two energies  $\rightarrow$  larger centrality fluctuations at 5.02 TeV

# Studying QGP with flow



- ❖ Spatial eccentricity in the initial state converted to momentum anisotropic particle distributions
  - ▶ known as **elliptic flow**
  - ▶ reflect initial **eccentricity** and **transport properties** of QGP



$$\vec{V}_n = v_n e^{-in\Psi_n}$$

- $v_n$  : Anisotropic flow
- $\Psi_n$  : Flow symmetry plane

## ❖ General questions:

- ▶ how does  $v_n$  fluctuate
- ▶ how does  $\psi_n$  fluctuate
- ▶ correlations between  $\psi_m$  and  $\psi_n$
- ▶ **correlations between  $v_m$  and  $v_n$**
- ▶ new information on initial conditions and/or  $\eta/s(T)$ ?

ALICE, [JHEP 07 \(2018\) 103](#)  
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[JHEP06 \(2020\) 147](#)  
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[PLB818 \(2021\) 136354](#)