

Testing the neutrino mass generation mechanism at the future colliders

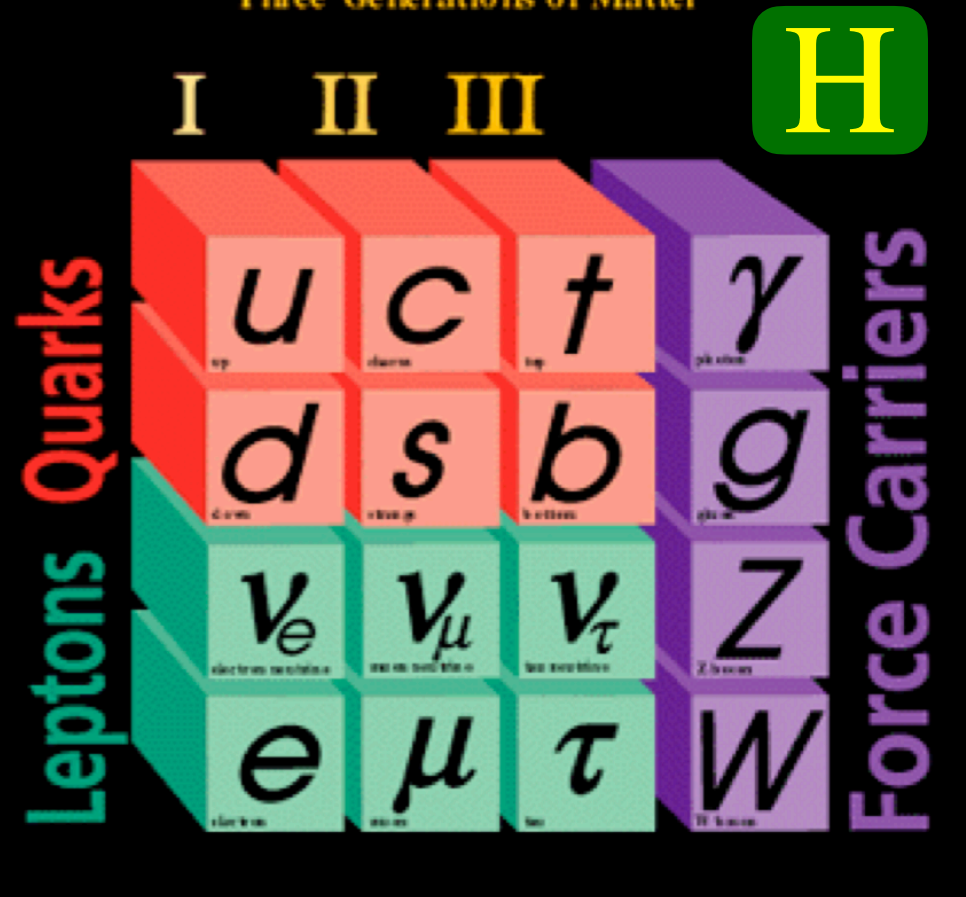


EPS – HEP Conference 2021 July 26 – 30, 2021



The Standard Model of Particle Interactions

Three Generations of Matter



Over the decades experiments have found each and every missing pieces

Verified the facts that they belong to this family

Finally at the Large Hadron collider Higgs has been observed
→ Its properties must be verified

Strongly established with interesting shortcomings
Few of the very interesting anomalies :

Tiny neutrino mass and flavor mixings
Relic abundance of dark matter...

SM can not explain them

Models of Neutrino mass

There is a wide variety of neutrino mass models

The predicted models extend the SM minimally

At the tree level SM can be extended by Singlet fermions

→ Right handed neutrinos seesaw mechanism
inverse seesaw mechanism

Minkowski, Ramond, Slansky, Yanagida, Gell – Mann, Glashow, Mohapatra, Senjanovic, Schechter, Valle,
Linear, Hybrid

Alternative ideas extending the Standard Model

→ SU(2) triplet scalar : type – II seesaw

Schechter, Valle, Lazarides, Shafi, Wetterich, Mohapatra, Senjanovic

→ SU(2) triplet fermion : type – III seesaw

Foot, Lew, He, Joshi, Ma

→ One – loop and even at 2/3 – loop models also exist

For example : Ma – model, Zee – Model, Zee – Babu model, BNT, KNT, etc .
Babu, Leung, Hirsch, King, Nasri, Volkas Dev, Pilaftsis AD, Nomura, Okada, Roy

→ Discrete symmetry, Effective operator approaches

Petcov, Tanimoto, et . al; Volkas, et . al

→ Light neutrino induced model : ν SM

Asaka, Gorbunov, Shaposhnikov

→ Gauge extended : U(1) and Left – Right

Pati, Salam; Mohapatra, Pati; Senjanovic, Mohapatra Buchmuller, Greub; FileviezPerez, Han, Li; Heeck, Teresi;
Kang, Ko, Li; Keung, Senjanovic; Ferrari et . al . ; Nemevsek, Nesti, Senjanovic, Zhang; AD, Dev, Okada, Raut
Chen, Dev, Mohapatra; Dev, Mohapatra, Zhang; AD, Dev, Mohapatra; Deppisch, Desai, Kulkarni, Valle; Gluza

Particle content

Dobrescu, Fox; Cox, Han, Yanagida; AD, Okada, Raut;
Chiang, Cottin, AD, Mandal; AD, Takahashi, Oda, Okada AD, Dev, Okada

	$SU(3)_c$	$SU(2)_L$	$U(1)_Y$		$U(1)_X$
q_L^i	3	2	$+1/6$	$x_q =$	$\frac{1}{6}x_H + \frac{1}{3}x_\Phi$
u_R^i	3	1	$+2/3$	$x_u =$	$\frac{2}{3}x_H + \frac{1}{3}x_\Phi$
d_R^i	3	1	$-1/3$	$x_d =$	$-\frac{1}{3}x_H + \frac{1}{3}x_\Phi$
ℓ_L^i	1	2	$-1/2$	$x_\ell =$	$-\frac{1}{2}x_H - x_\Phi$
e_R^i	1	1	-1	$x_e =$	$-x_H - x_\Phi$
H	1	2	$+1/2$	$x'_H =$	$\frac{1}{2}x_H$
N_R^i	1	1	0	$x_\nu =$	$-x_\Phi$
Φ	1	1	0	$x'_\Phi =$	$2x_\Phi$

$m_{Z'} = 2 g_X v_\Phi$
 x_H, x_Φ will appear
the coupling with Z'

B - L case
 $x_H = 0, x_\Phi = 1$

3 generations of
SM singlet right handed
neutrinos (anomaly free)

Charges **before**
the anomaly cancellations

Charges **after**
Imposing the
anomaly
cancellations

$U(1)_X$ breaking

$$\mathcal{L}_Y \supset - \sum_{i,j=1}^3 Y_D^{ij} \bar{\ell}_L^i H N_R^j - \frac{1}{2} \sum_{i=k}^3 Y_N^k \Phi \overline{N_R^k}^c N_R^k + \text{h.c.},$$

$$m_D^{ij} = \frac{Y_D^{ij}}{\sqrt{2}} v_h$$

$$m_{N^i} = \frac{Y_N^i}{\sqrt{2}} v_\Phi$$

$$m_\nu = \begin{pmatrix} 0 & M_D \\ M_D^T & M_N \end{pmatrix} \quad m_\nu \simeq -M_D M_N^{-1} M_D^T$$

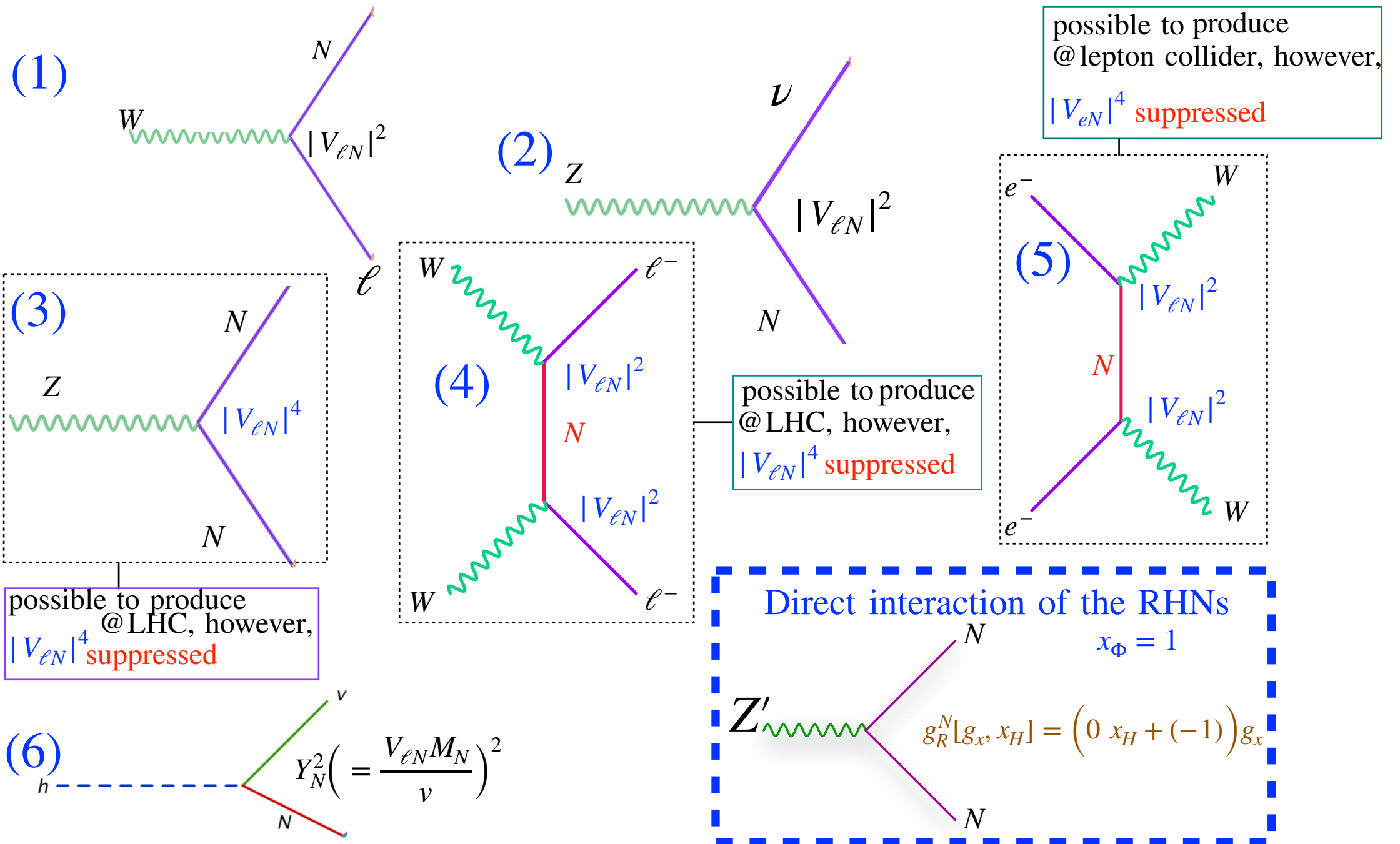
Seesaw mechanism

Production modes of the RHNs at the colliders : pp, e^-e^+, e^-p

Flavor eigenstate can be expressed in terms of the mass eigenstate

$$\nu_\ell \simeq U_{\ell m} \nu_m + V_{\ell n} N_n$$

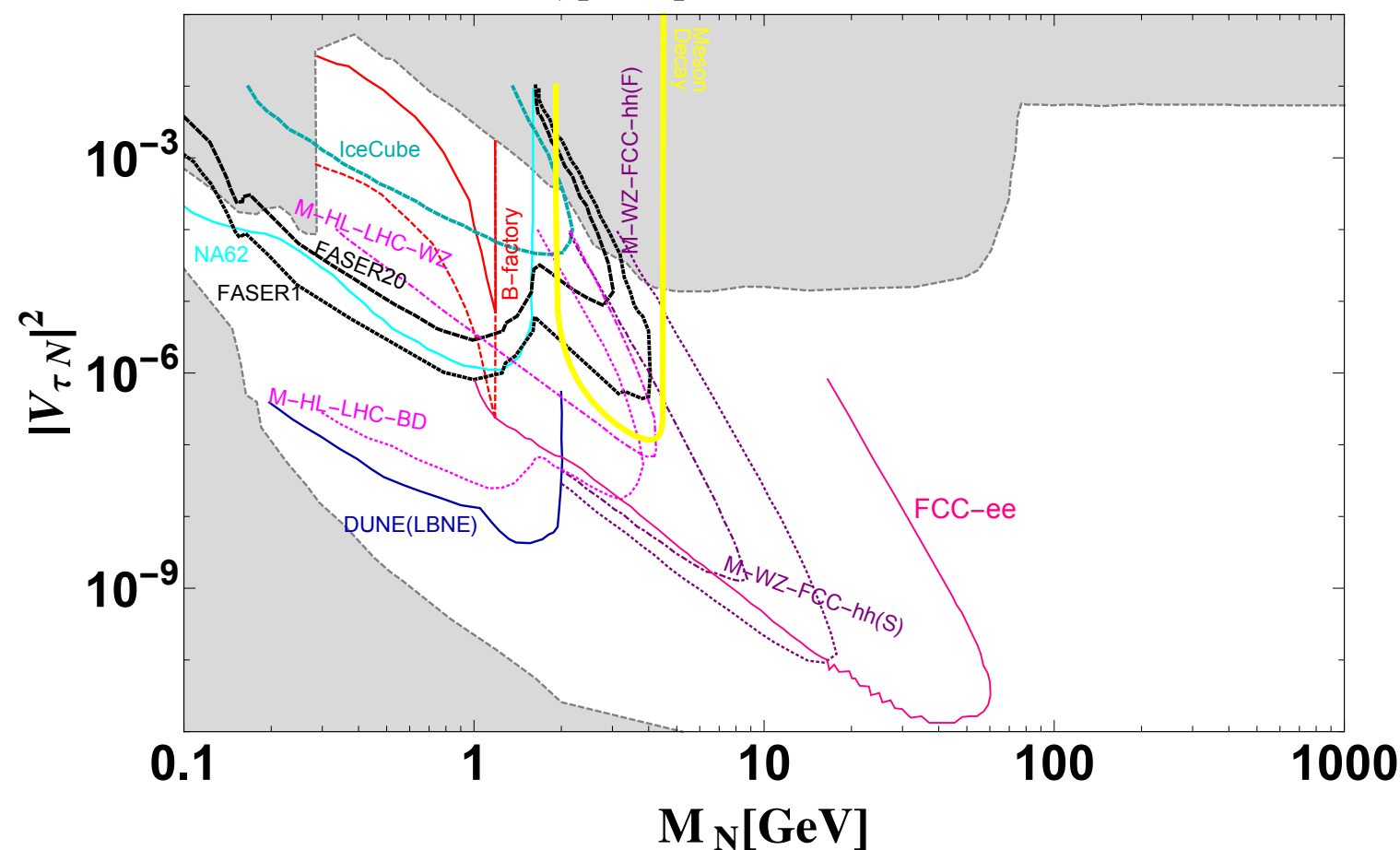
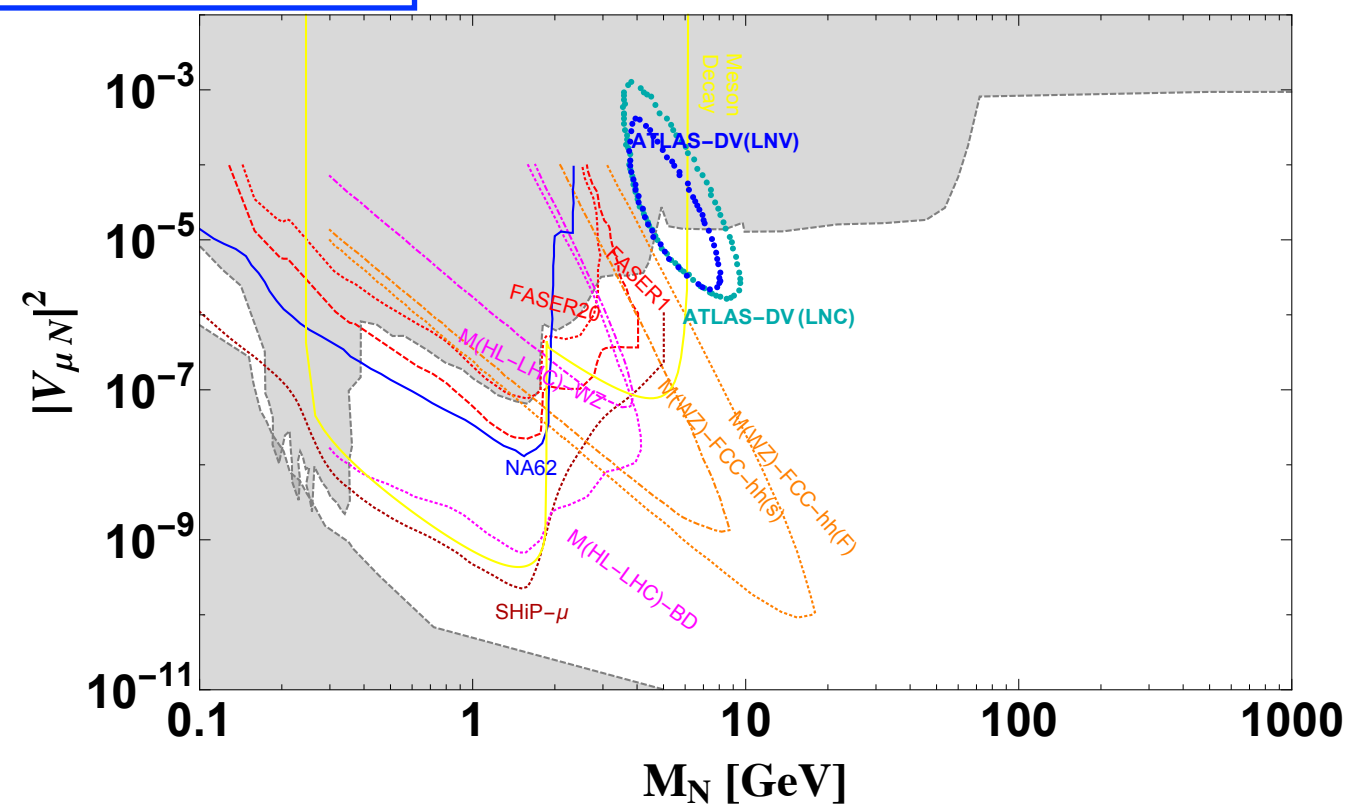
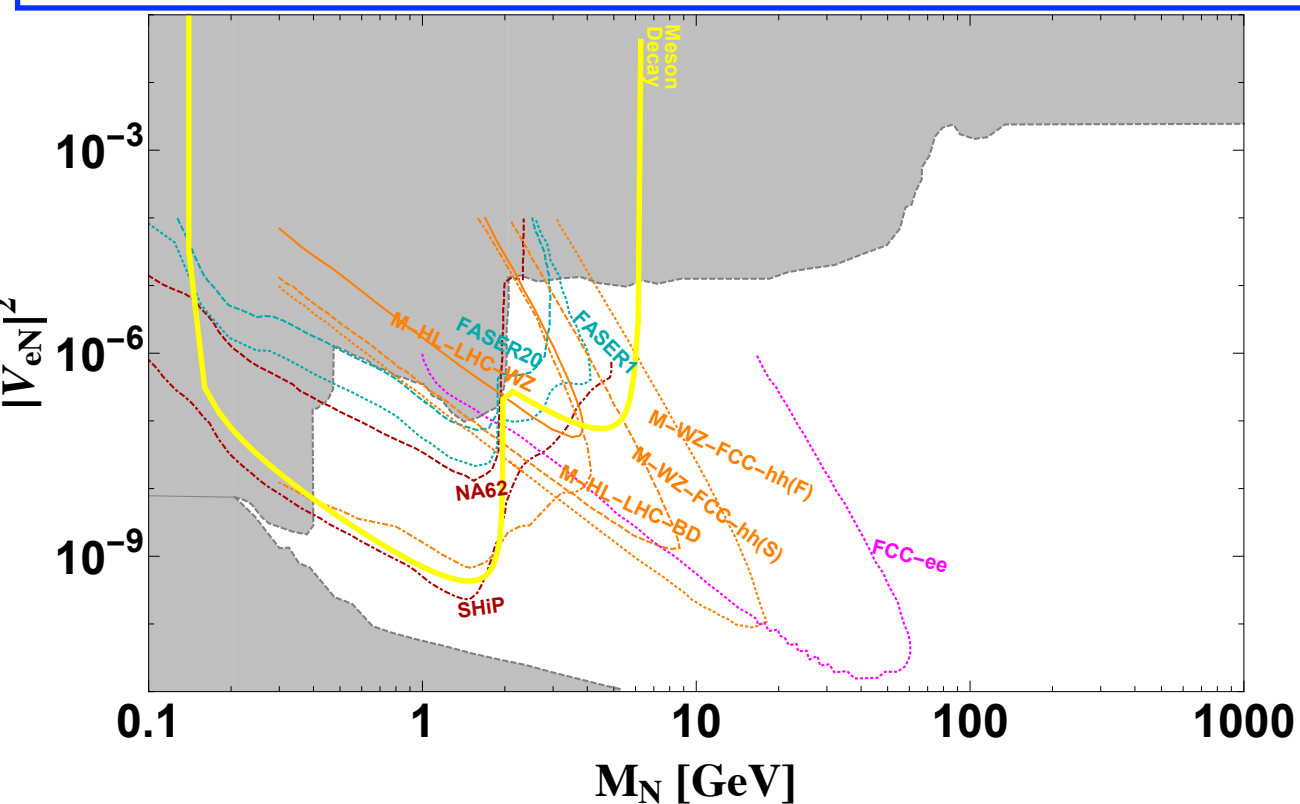
\swarrow PMNS matrix $\searrow M_D M_N^{-1}$



We consider $x_\Phi = 1$

$Z \rightarrow N \nu$, see Andre de Gouvea's talk : Dirac – Majorana nature

Existing and prospective bounds on the mixings



In back – up slides

CMS $\ell^\pm \ell^\pm + \text{jets}$

1806.10905 13 TeV, 35.9 fb $^{-1}$

CMS $3\ell + \text{MET}$

1802.02965 13 TeV, 35.9 fb $^{-1}$

ATLAS $3\ell + \text{MET}$

1905.09787, 36.1 fb $^{-1}$

General Yukawa structure : 1702.04668

Also : Meson decay : Julia Harz's talk

Limits on sterile neutrinos from DUNE : Kevin Kelly's talk

FASER ν : Tomoko Ariga's talk

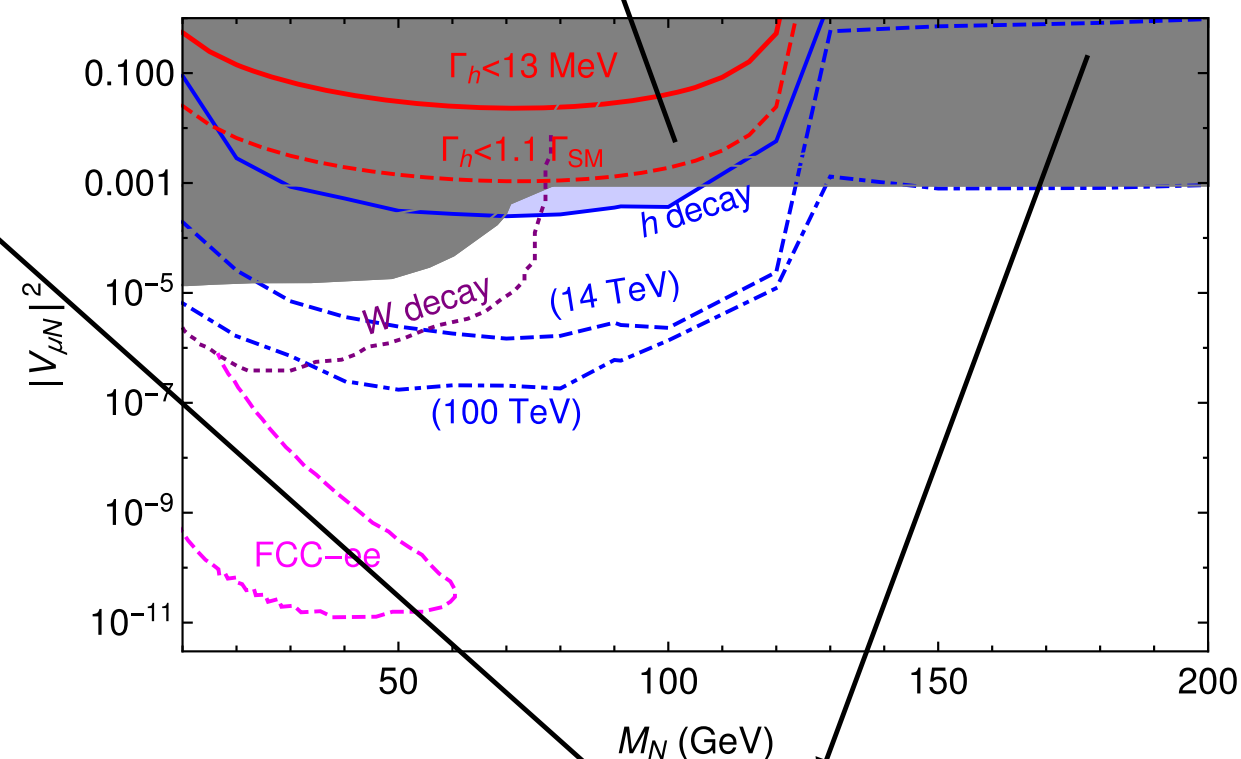
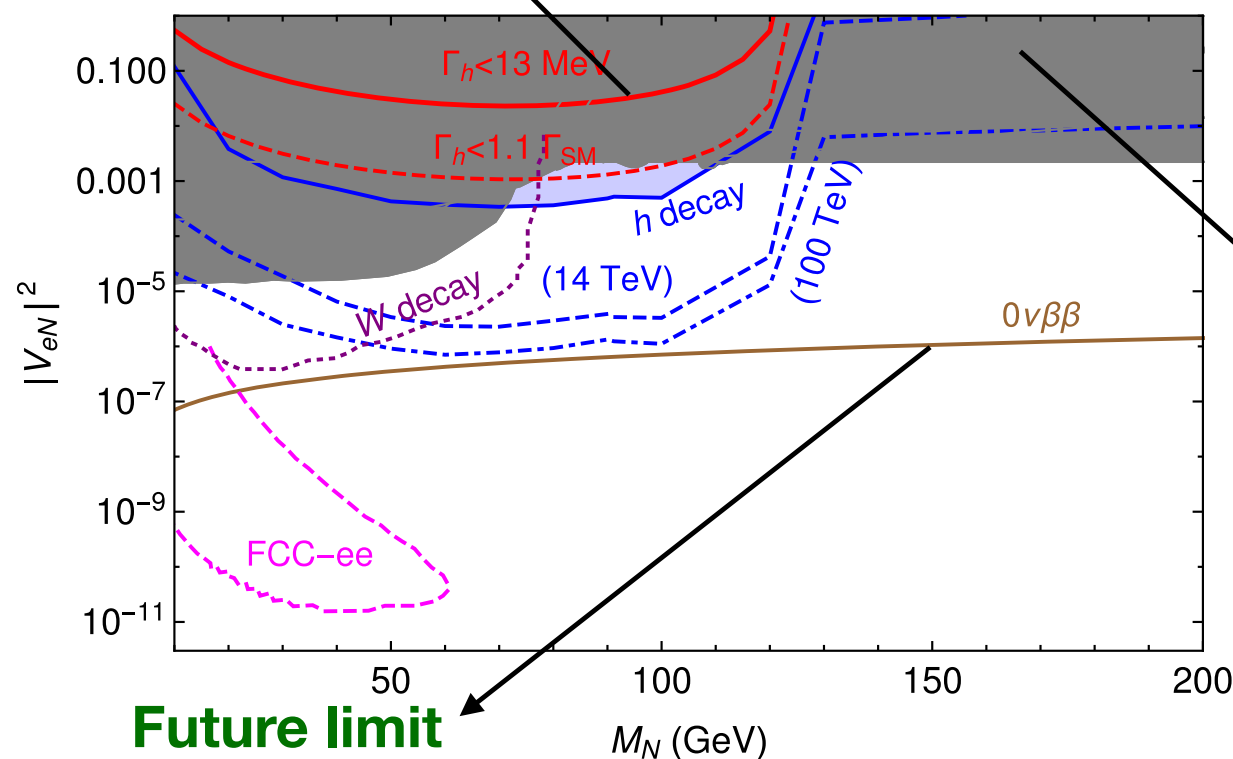
μ BooNE : Pawel Guzowski's talk

$2\ell + p_T^{\text{miss}}$: bounds from the Higgs decay ($h \rightarrow N\nu, N \rightarrow 2\ell\nu$)

**CMS, JHEP 09 (2016) 051: 7&8 TeV combined
H \rightarrow W W*, upper limit on Yukawa as
well as mixing**

**Future sensitivity can go down to
10% precise result at pp collider:
arXiv:1606.09408**

1704.00880
1704.00881

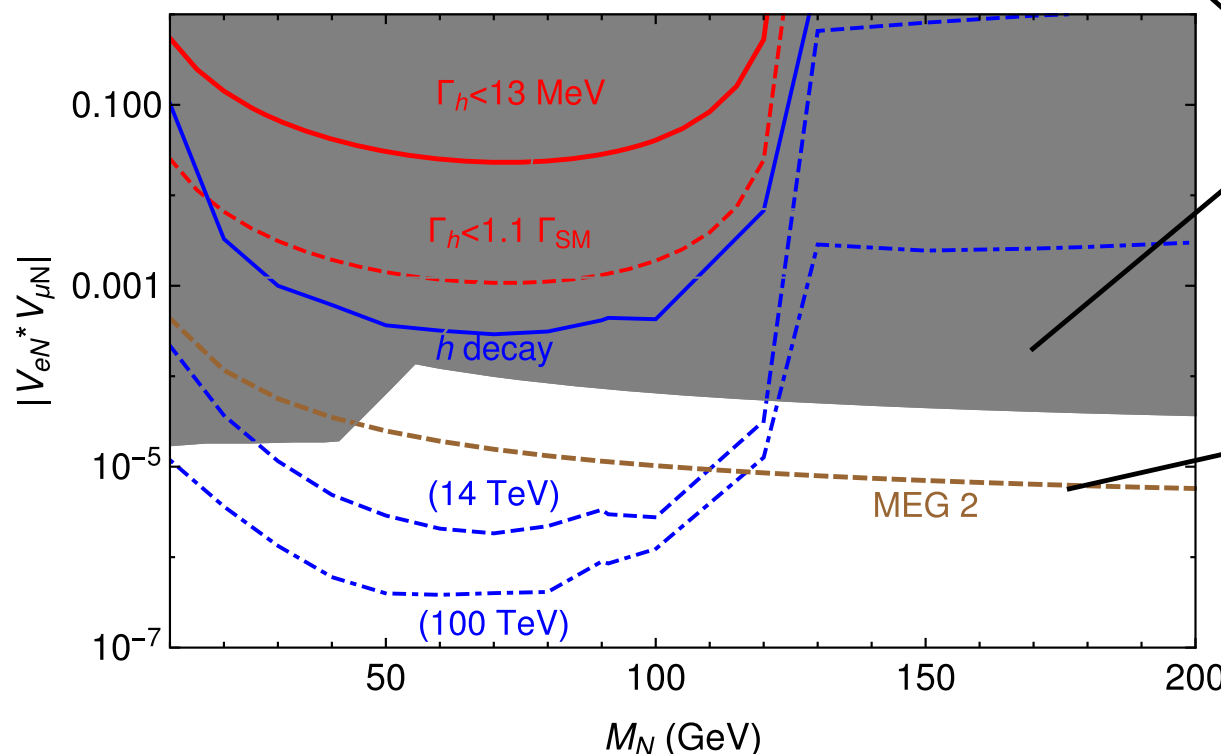


**Future limit
considering
Majorana heavy
neutrinos only**

**Excluded by LEP
LHC, EEPD,
LFV limits from CMS
is also included in the
lower panel**

**FCC-ee : Limits from
Z decay
W-decay @LHC**

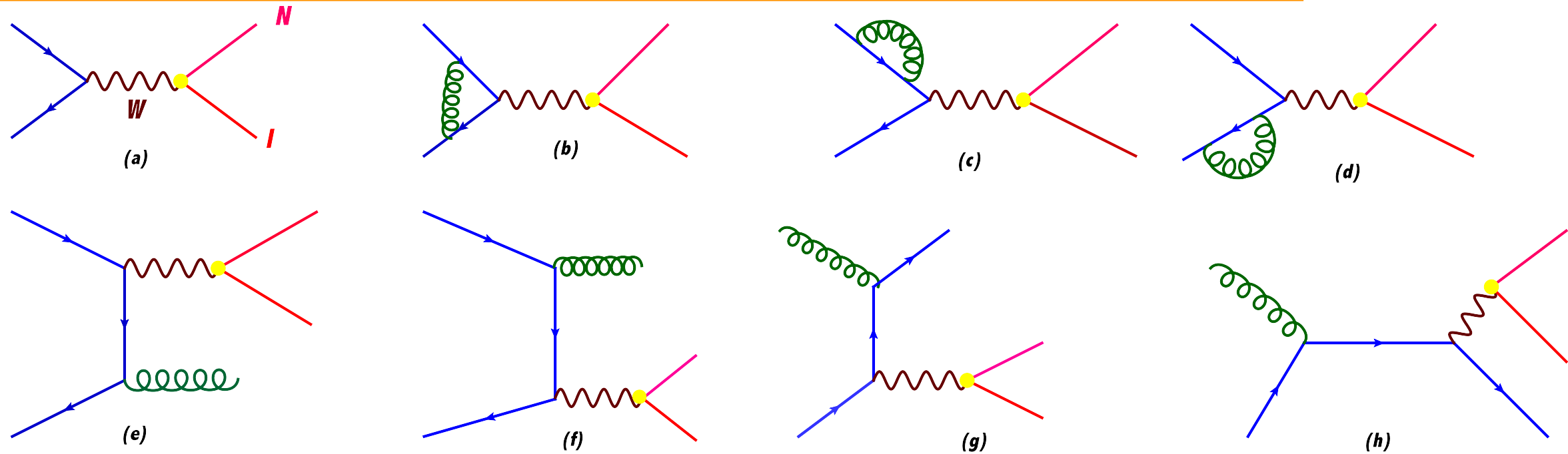
Future limits



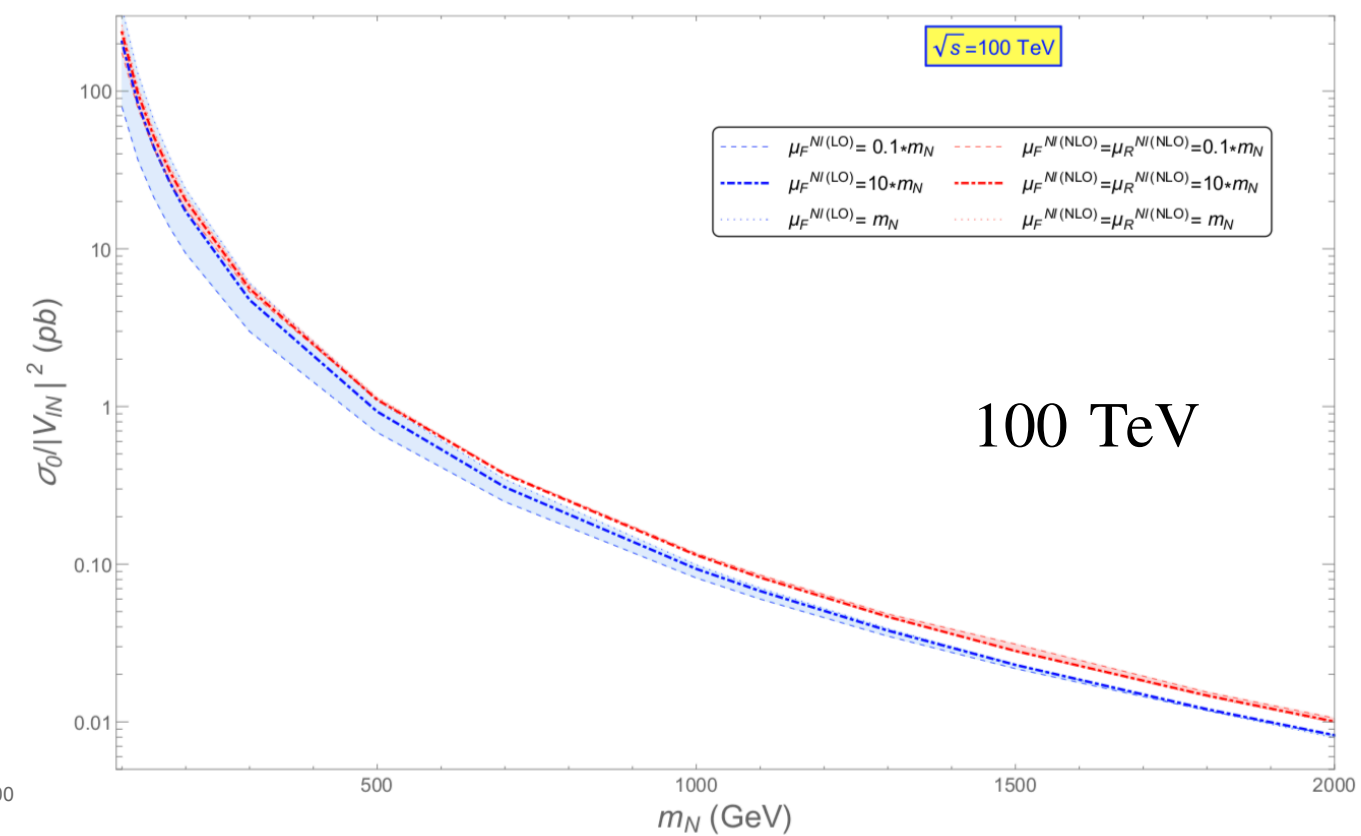
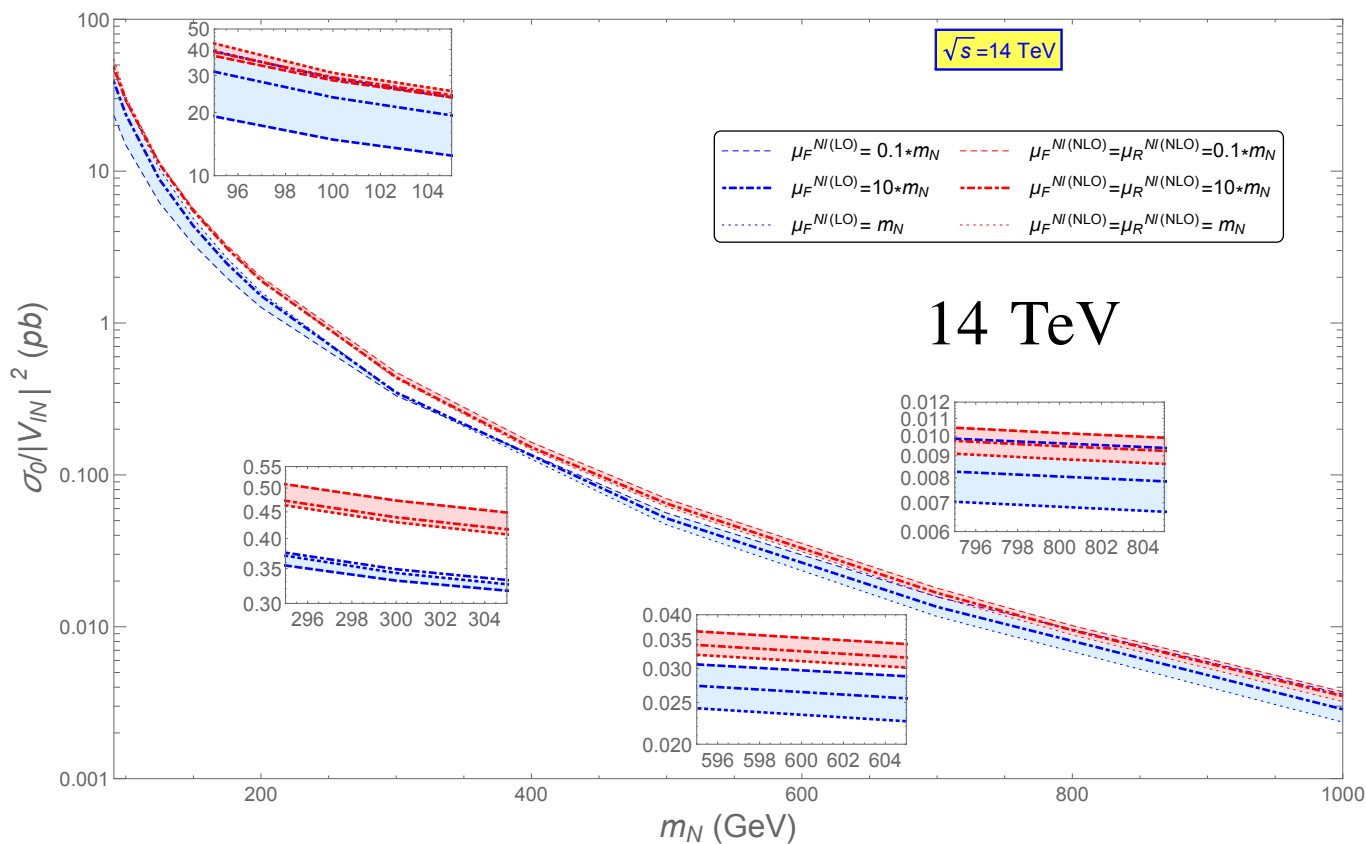
$\mu \rightarrow e\gamma$
~ future branching
ratio $O(10^{-15})$

NLO – QCD production of the heavy neutrinos

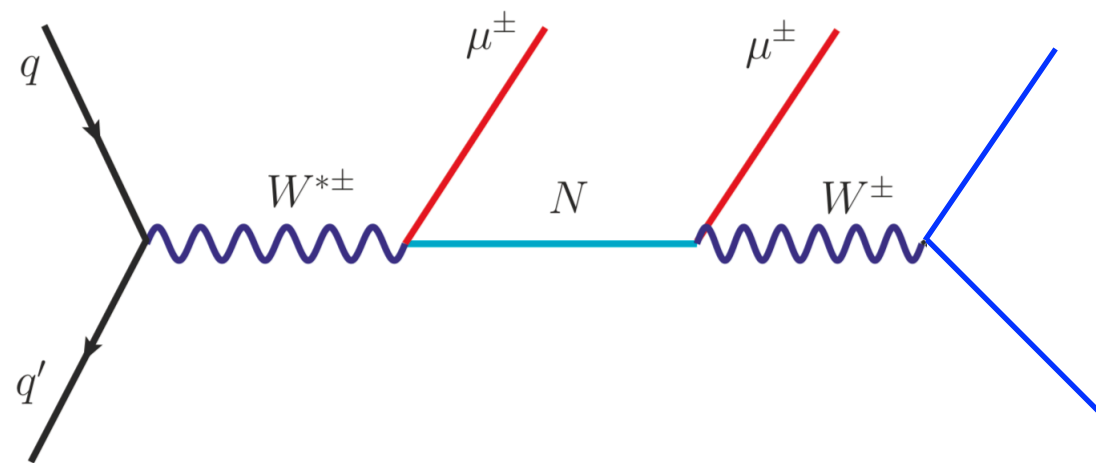
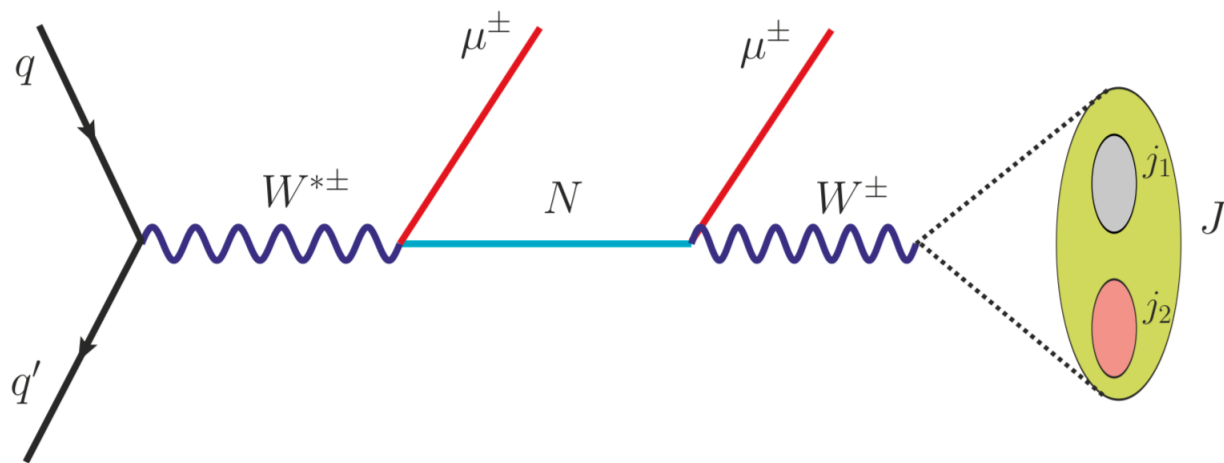
1602.06957



$$\mu_F^{\text{NLO}} = \mu_R^{\text{NLO}} = \xi * m_N \quad \mu_F^{\text{NLO}} = m_N, \mu_R^{\text{NLO}} = \xi * m_N \quad \mu_F^{\text{NLO}} = \xi * m_N, \mu_R^{\text{NLO}} = \xi * m_N \quad 0.1 \leq \xi \leq 10$$



Normalized by $|V_{\ell N}|^2$

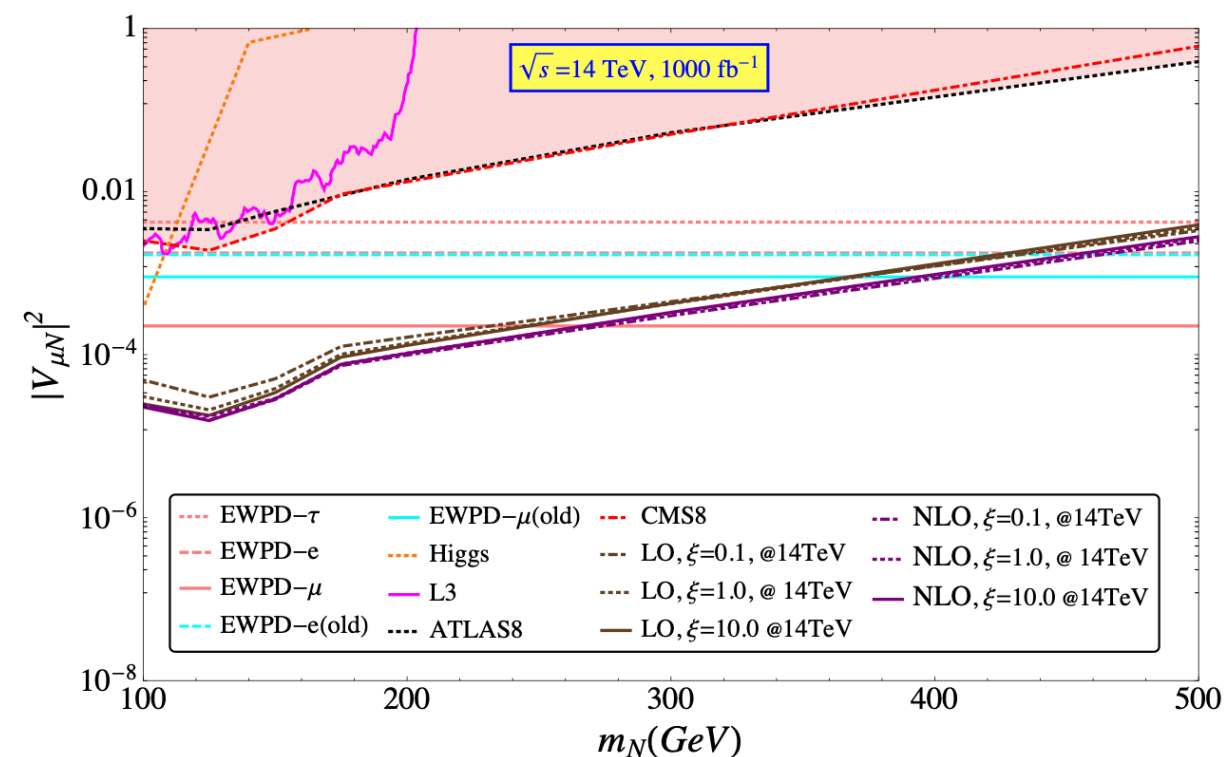
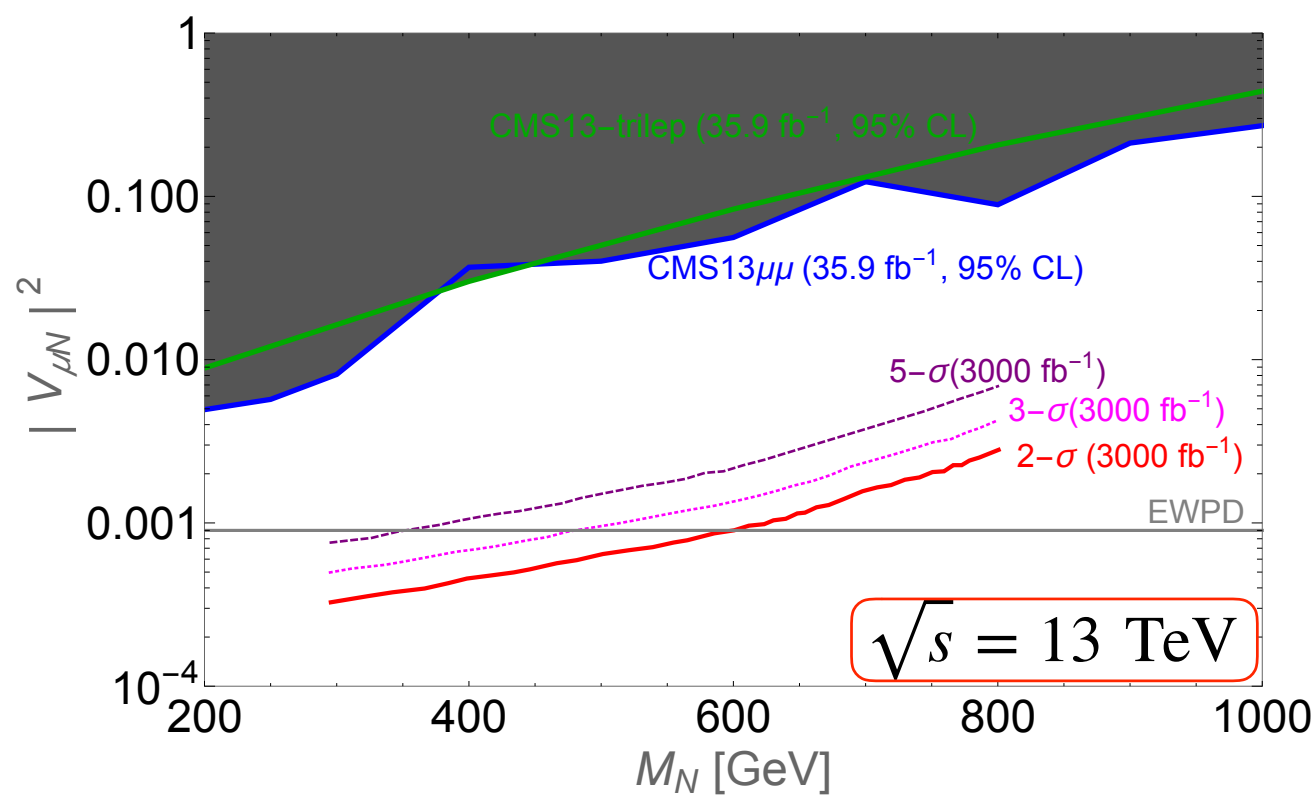


$$R = 0.8, p_T^J > 150 \text{ GeV}, \tau_{21}^J < 0.5, E_T^{\text{miss}} < 35 \text{ GeV}, M^J > 50 \text{ GeV}$$

SSDL + 1 – Fat jet

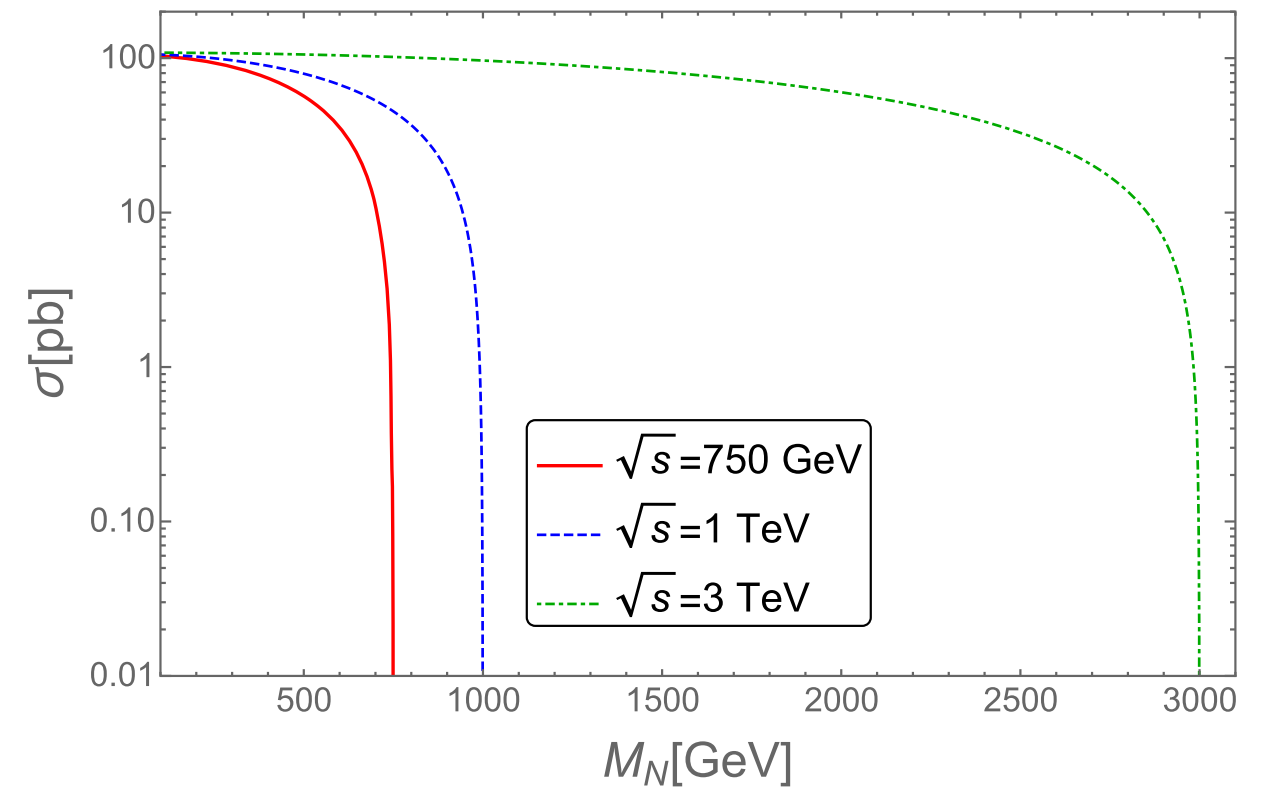
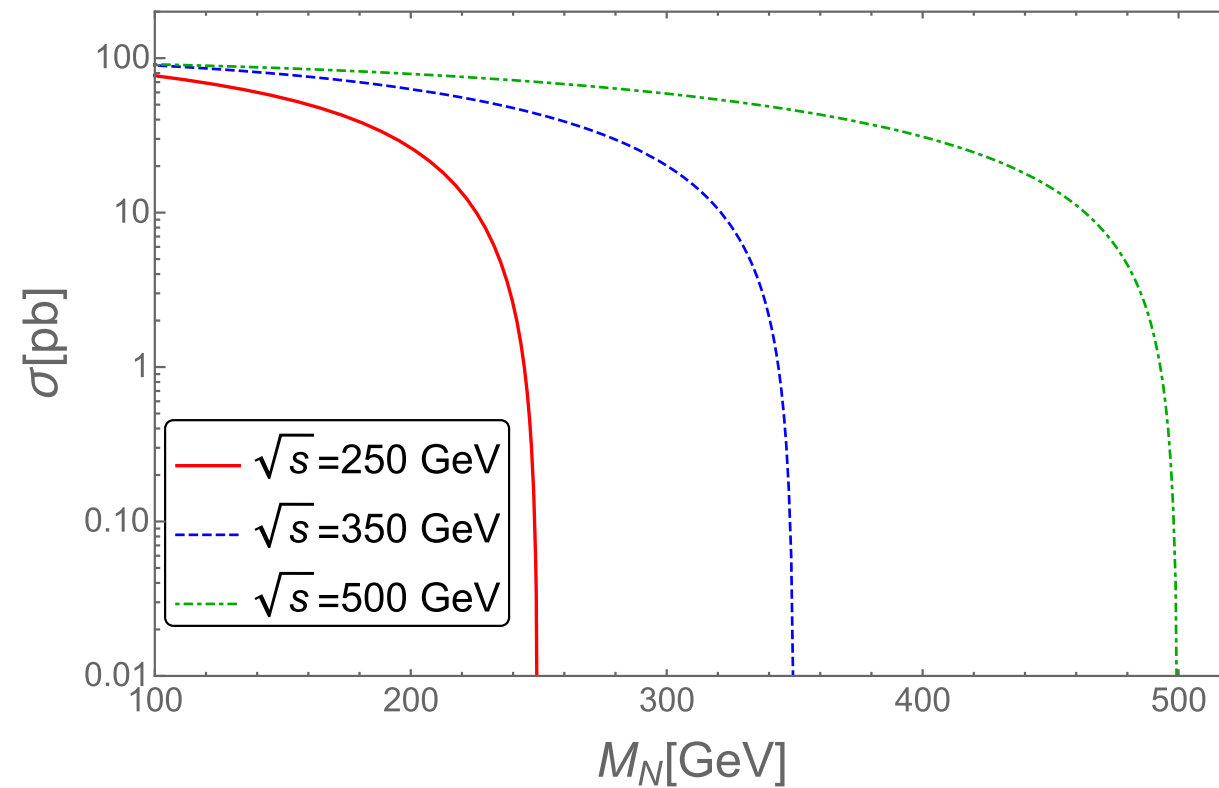
SSDL + 2 – jet

Mass versus mixing plot and comparison to the current bounds

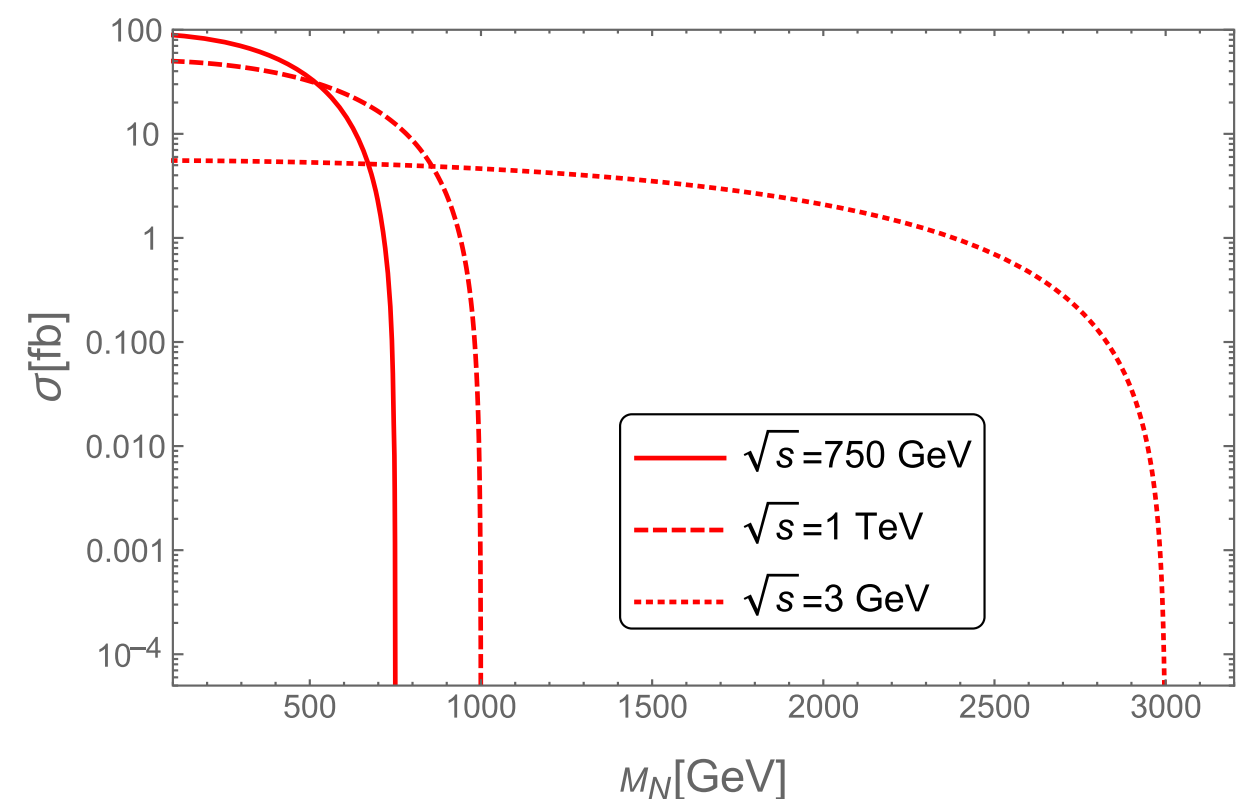
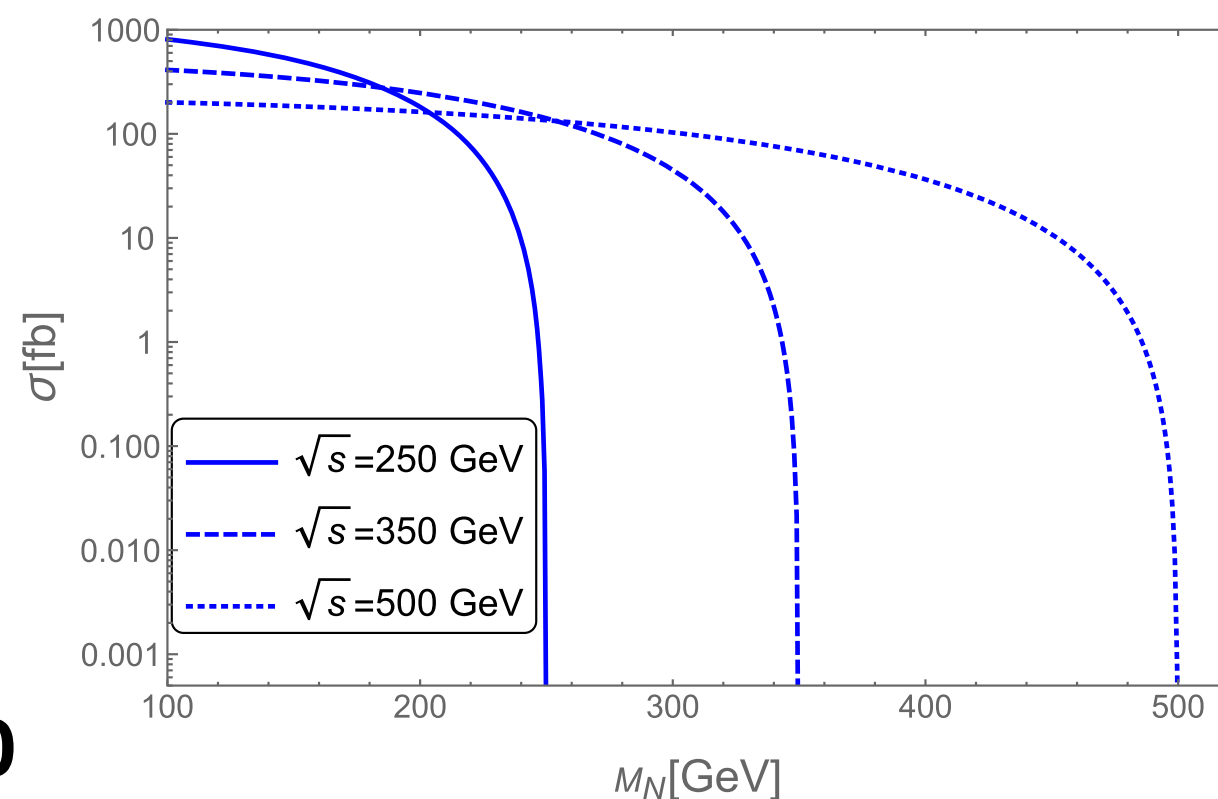


14 TeV, 1000 fb⁻¹

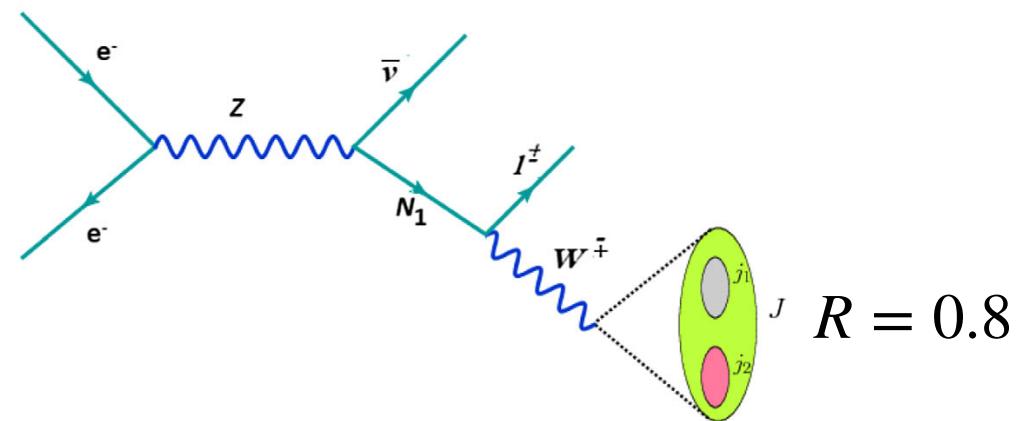
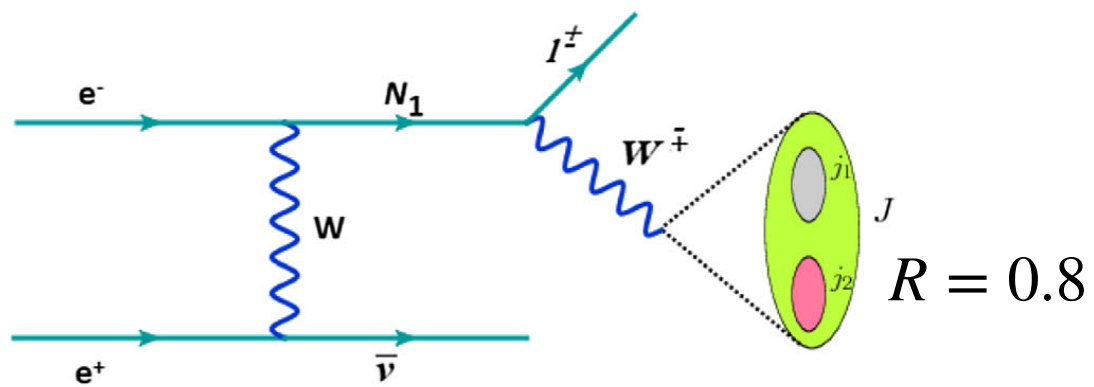
$e^+e^- \rightarrow \nu_1 N_1$ Includes s – channel and t – channel processes



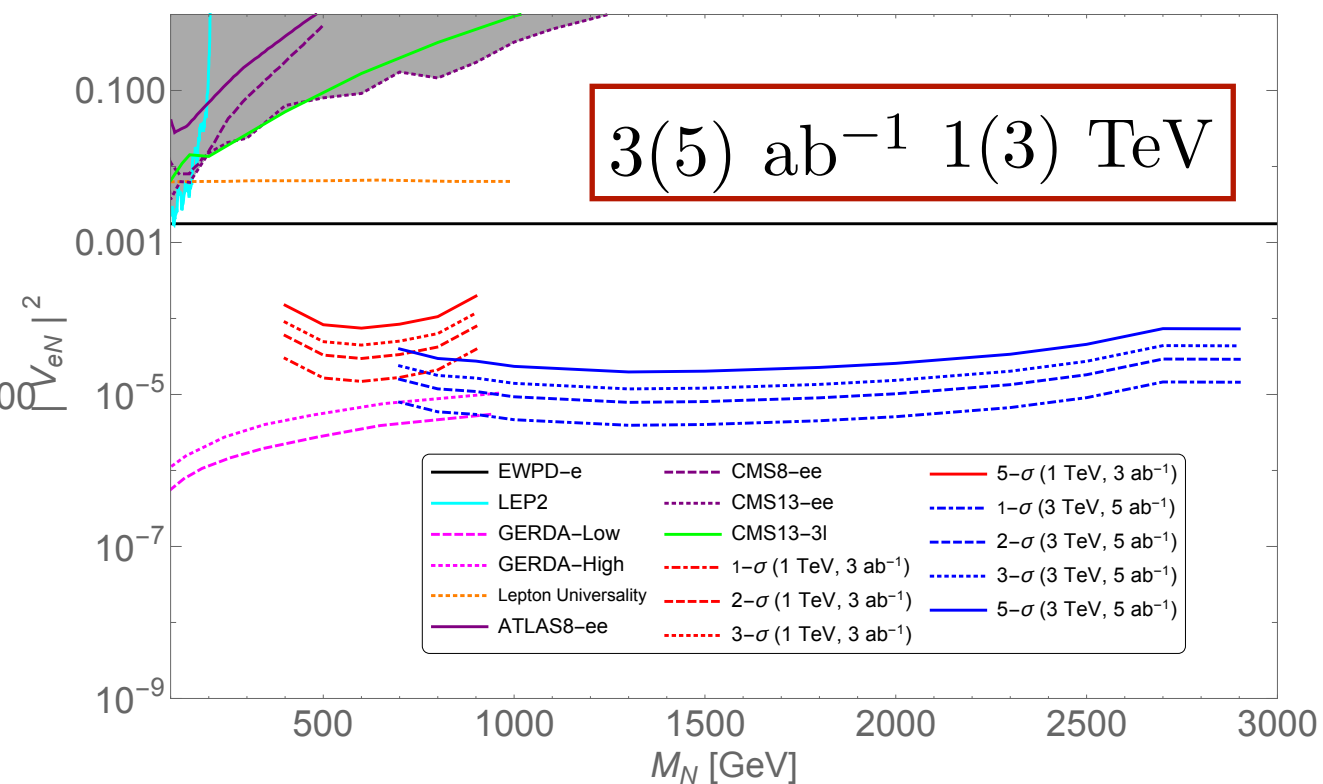
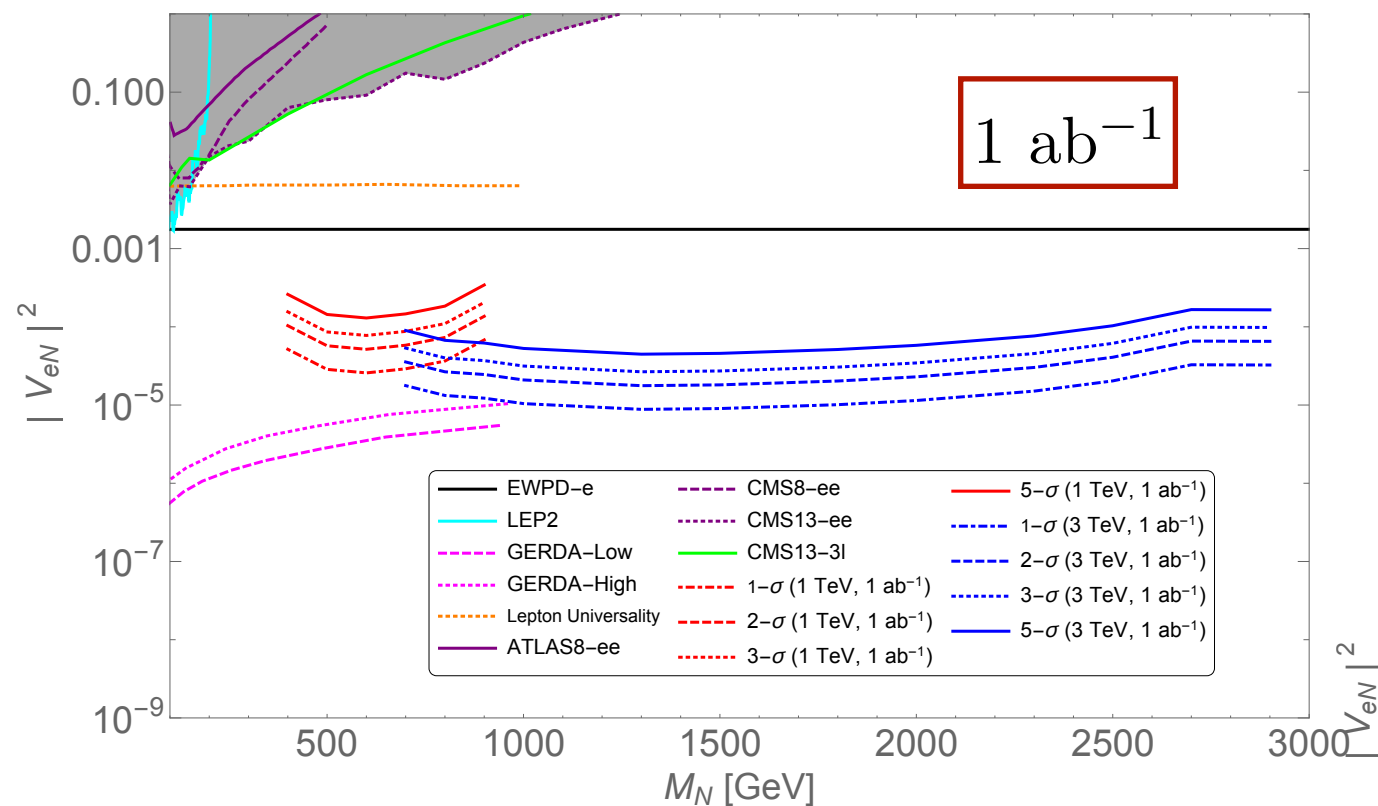
$e^+e^- \rightarrow \nu_2 N_2 / \nu_3 N_3$ Includes s – channel process, t – channel suppressed by off – diagonal Yukawa, away from the Z pole



$e + J + p_T^{\text{miss}}$ final states at the linear colliders



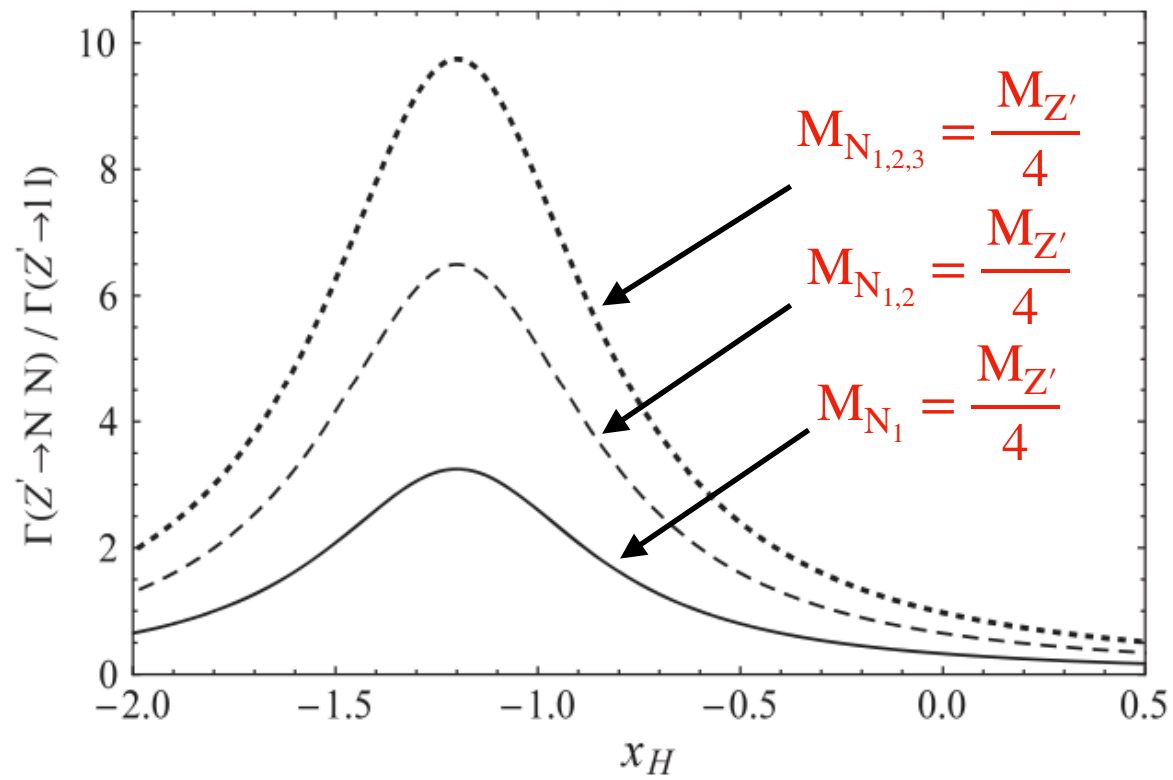
1 TeV (red band) and 3 TeV (blue band)



Decay length of RHNs neutrinos as a function of lightest active neutrino mass

$pp \rightarrow Z' \rightarrow NN$, under $U(1)_X$ scenario

1906.04132 1908.09838



$$\mathcal{L}^q = -g'(\bar{q}\gamma_\mu q_{x_L}^q P_L q + \bar{q}\gamma_\mu q_{x_R}^q P_R q)Z'_\mu \quad Z' - \text{quarks}$$

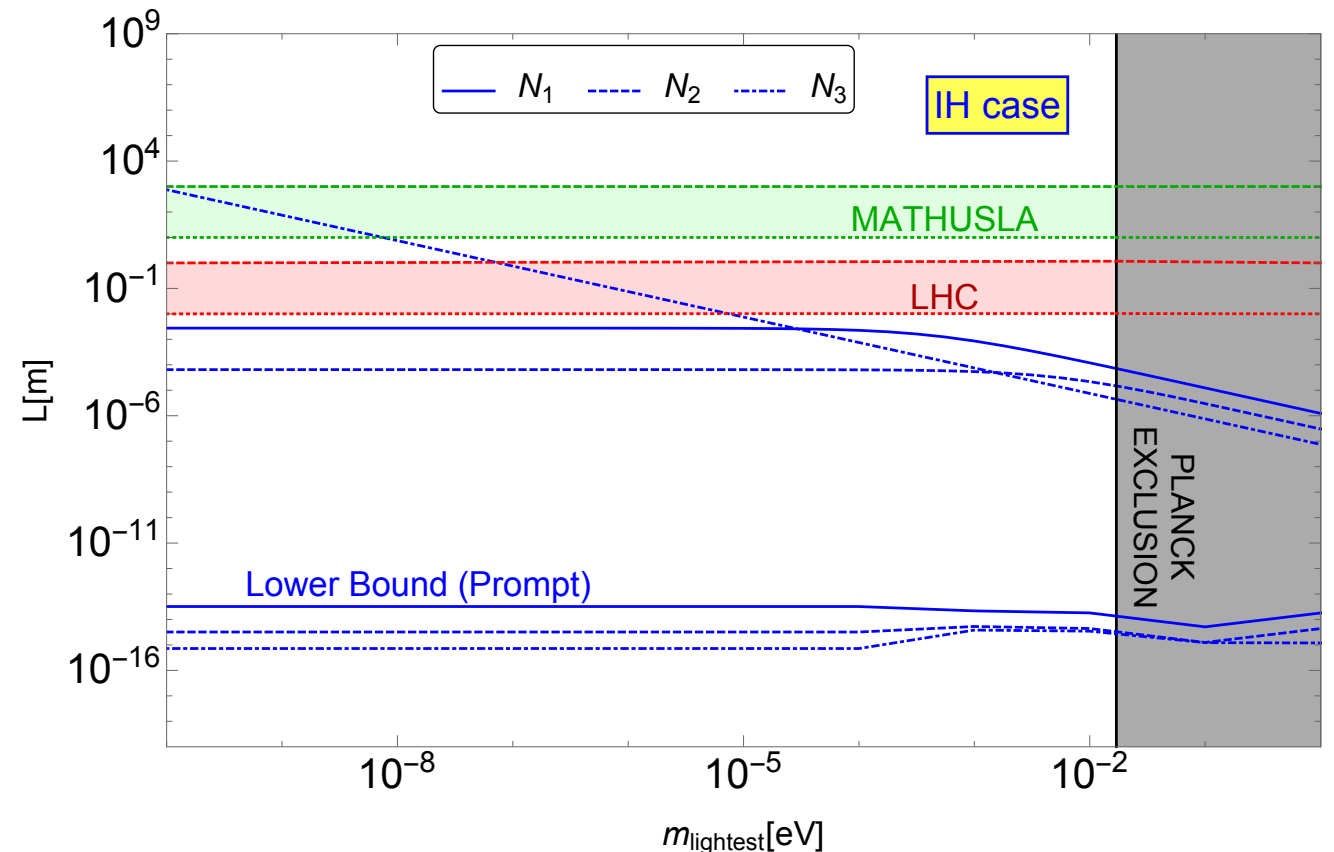
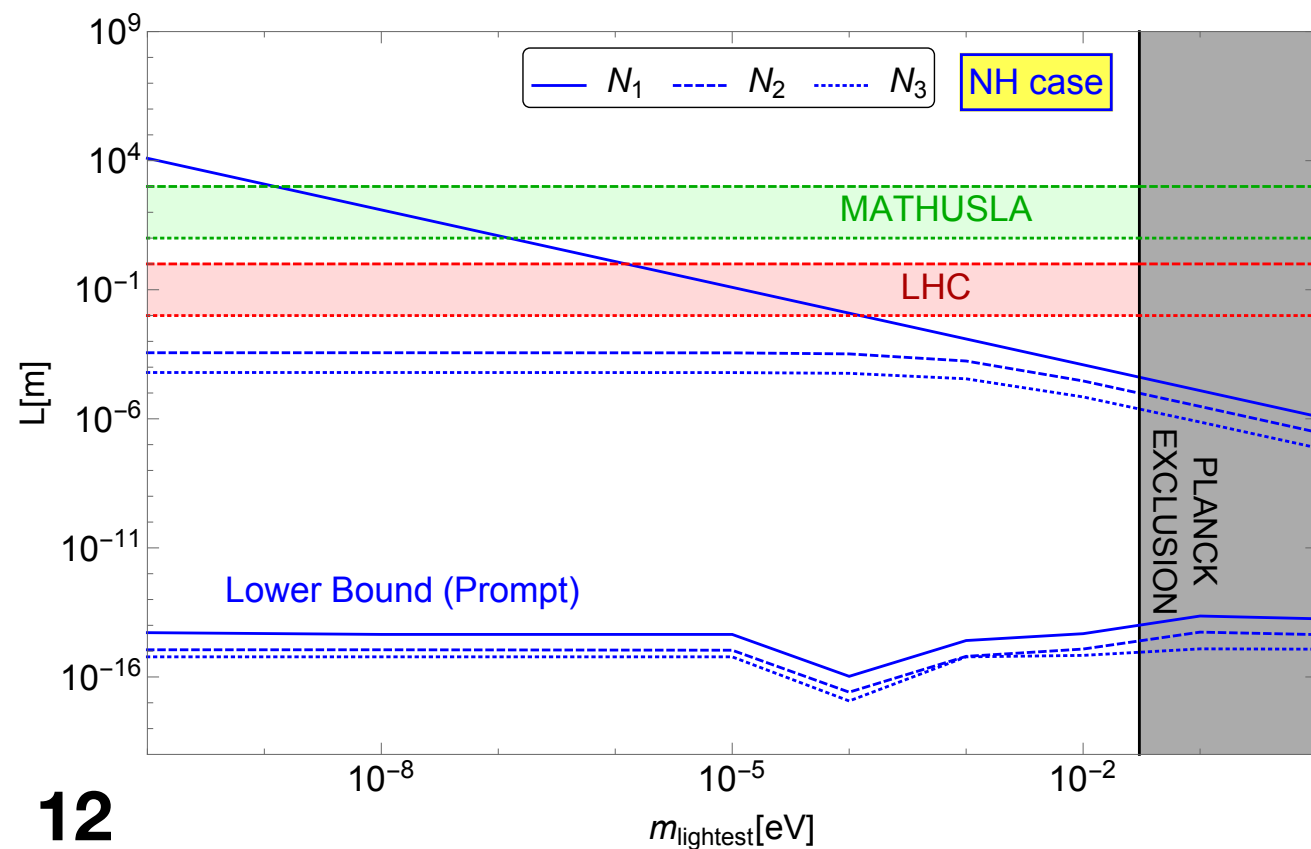
$$\mathcal{L}^\ell = -g'(\bar{\ell}\gamma_\mu q_{x_L}^\ell P_L \ell + \bar{\ell}\gamma_\mu q_{x_R}^\ell P_R \ell)Z'_\mu \quad Z' - \text{charged leptons}$$

$$\Gamma(Z' \rightarrow 2f) = N_c \frac{M_{Z'}}{24\pi} \left(g_L^f [g', x_H, x_\Phi]^2 + g_R^f [g', x_H, x_\Phi]^2 \right)$$

$$\Gamma(Z' \rightarrow 2\nu) = \frac{M_{Z'}}{24\pi} g_L^\nu [g', x_H, x_\Phi]^2 \quad \Gamma(Z' \rightarrow N^i N^i) = \frac{g^2}{24\pi} m_{Z'} \left(1 - \frac{4m_{N^i}^2}{m_{Z'}^2} \right)^{3/2},$$

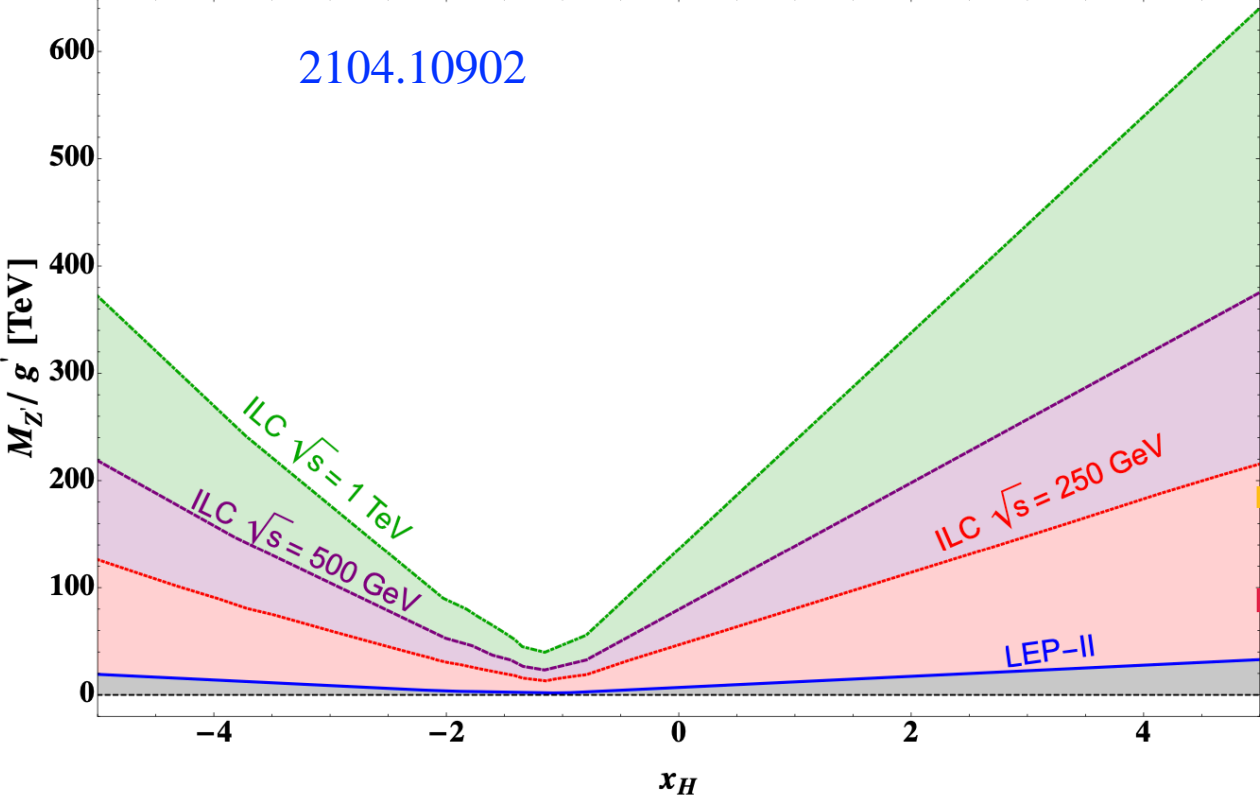
$$\frac{\Gamma(Z' \rightarrow NN)}{\Gamma(Z' \rightarrow \ell^+ \ell^-)} = \frac{4}{8 + 12x_H + 5x_H^2} \left(1 - \frac{4m_N^2}{m_{Z'}^2} \right)^{\frac{3}{2}}.$$

$$M_{N_1} = 500 \text{ GeV} \quad M_{N_3} = 2 \text{ TeV} \quad M_{N_2} = 1 \text{ TeV}$$



Limits on the model parameters

Considering the limit $M_{Z'} > > \sqrt{s}$ and applying effective theory we find the limits on $\frac{M_{Z'}}{g'}$ using **LEP – II (1302.3415) and (prospective) ILC (1908.11299) :**



$$\frac{\pm 4\pi}{(1 + \delta_{ef})(\Lambda_{AB}^{f\pm})^2}(\bar{e}\gamma_\mu P_A e)(\bar{f}\gamma_\mu P_B f)$$

Z' exchange matrix element for our process

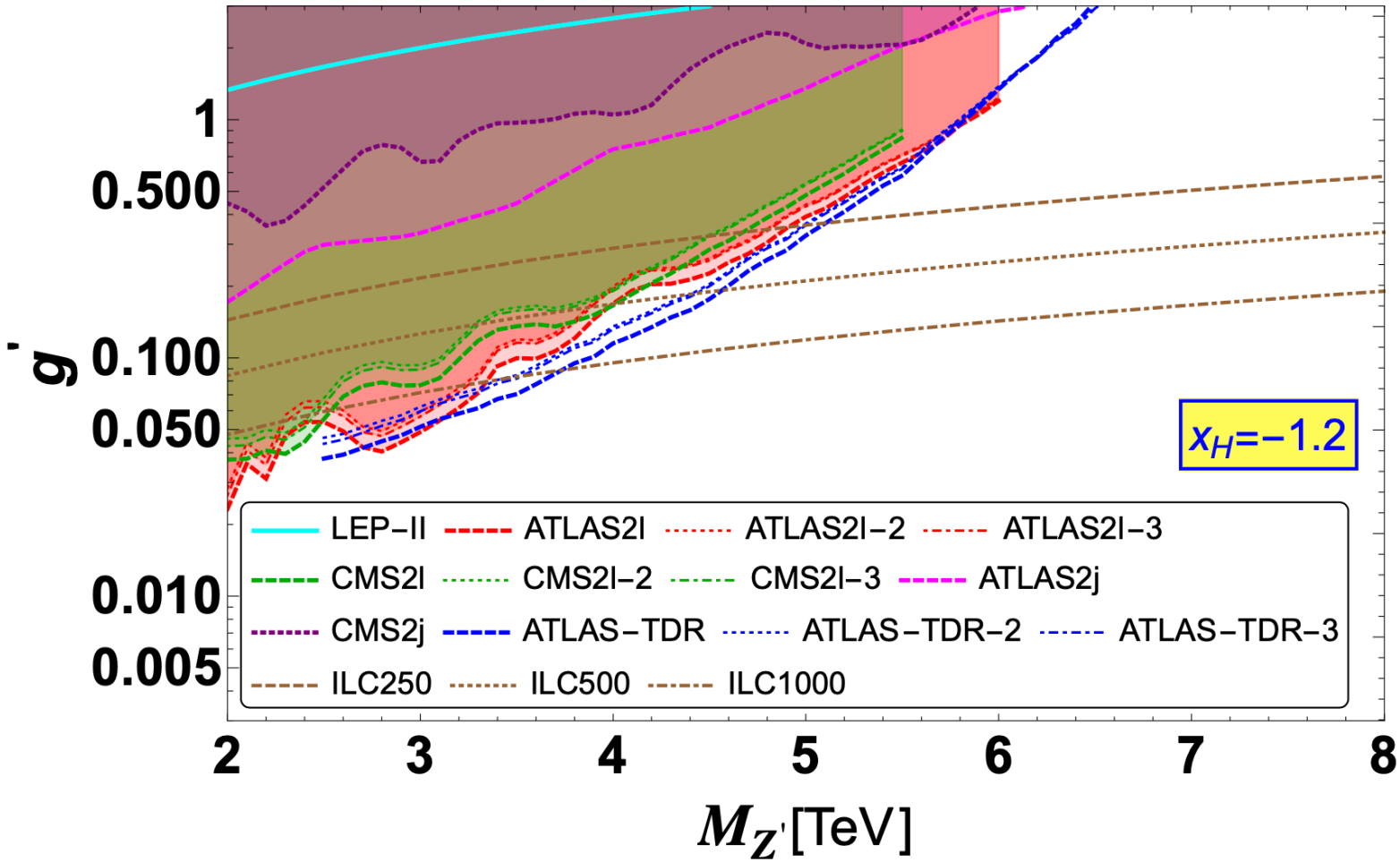
$$\frac{(g')^2}{M_{Z'}^2 - s}[\bar{e}\gamma_\mu(x_{\ell'}P_L + x_e'P_R)e][\bar{f}\gamma_\mu(x_{fL}P_L + x_{fR}P_R)f]$$

Matching the above equations :

$$M_{Z'}^2 - s \geq \frac{g'^2}{4\pi}|x_{e_A}x_{f_B}|(\Lambda_{AB}^{f\pm})^2$$

Indicates a large VEV scale can be probed from LEP – II to ILC1000 via ILC250 and ILC500
Shows limits on $M_{Z'}$ vs g' for **LEP – II, ILC250, ILC500 and ILC1000**

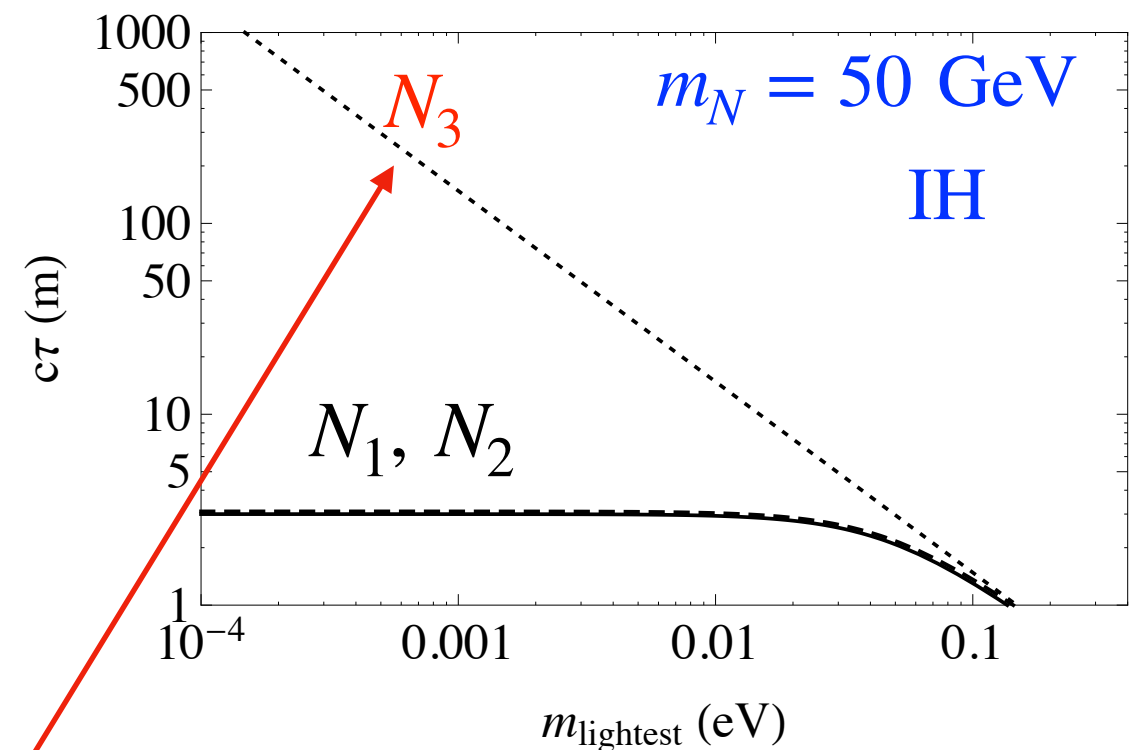
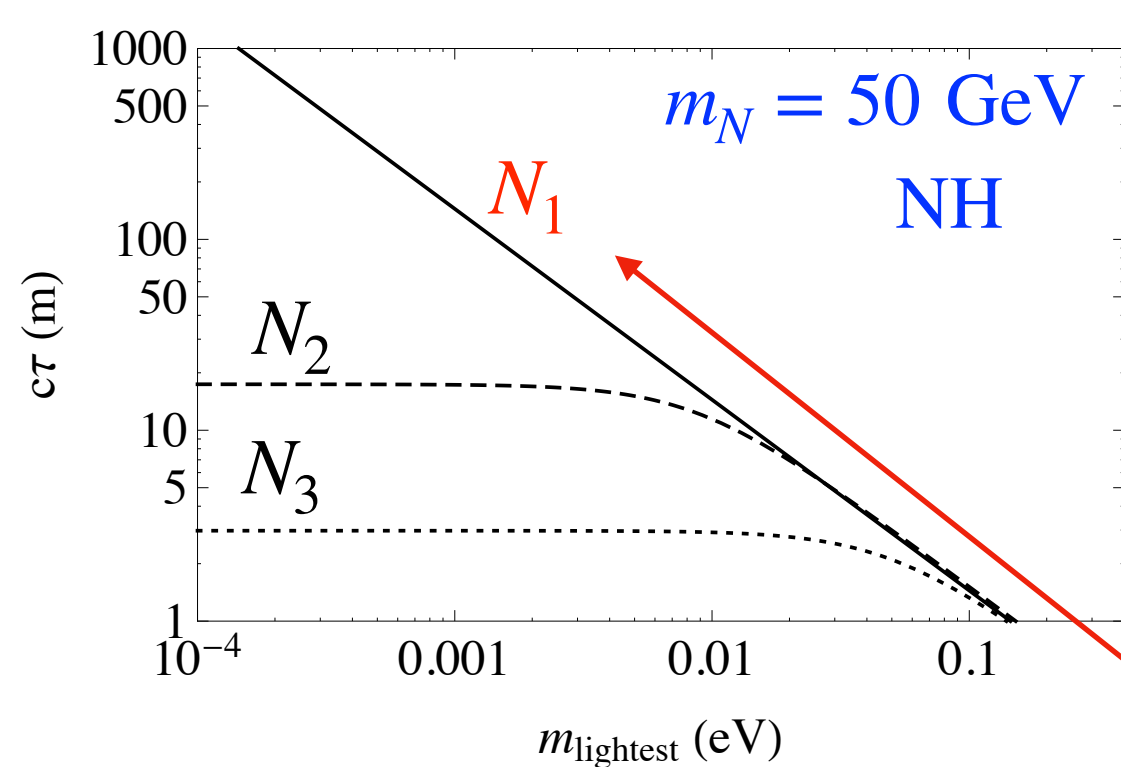
Limits on $M_{Z'}$ and g' can also be obtained from dilepton and dijet searches at the LHC $g' = \sqrt{g_{\text{Model}}^2 \left(\frac{\sigma_{\text{ATLAS}}^{\text{Obs.}}}{\sigma_{\text{Model}}} \right)}$



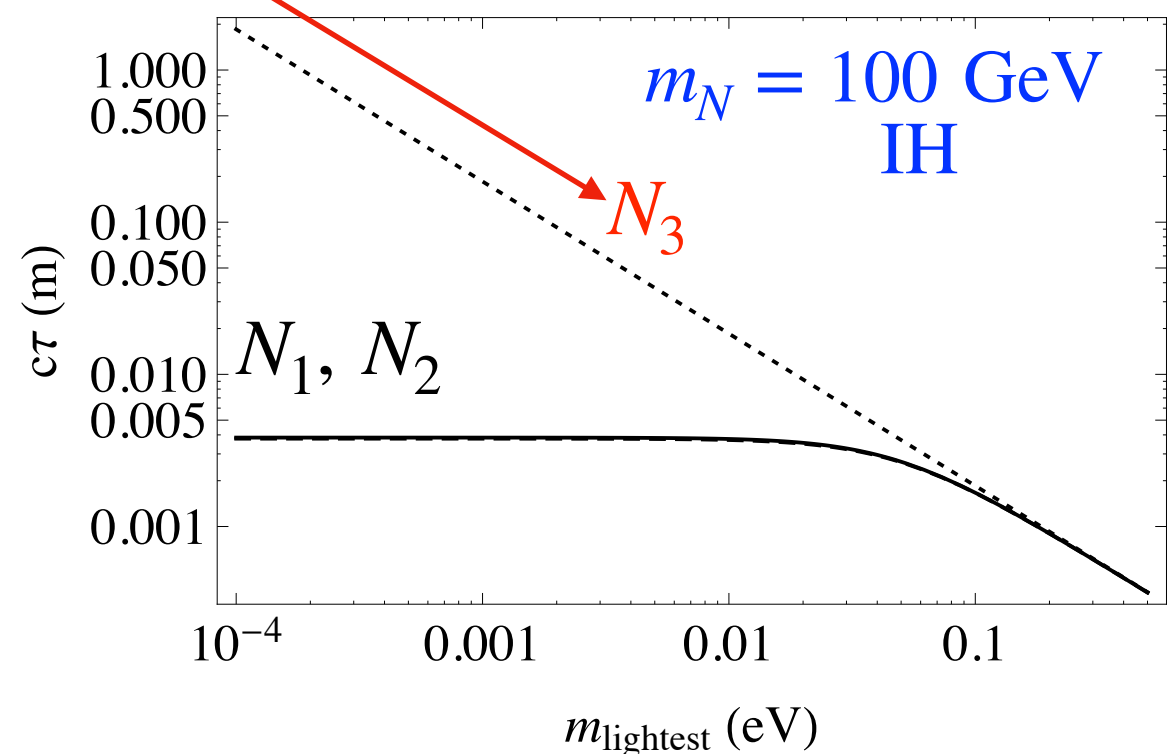
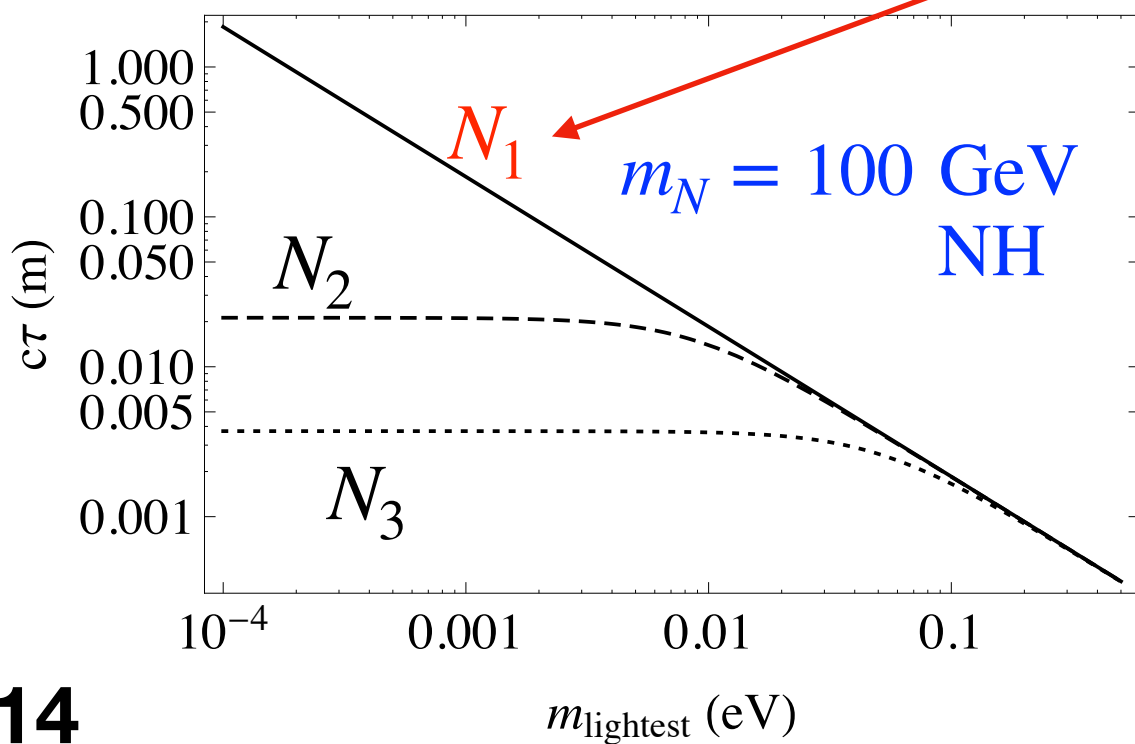
ATLAS2l/CMS2l/ATLAS – TDR : $M_N > \frac{M_{Z'}}{2}$
 ATLAS2l – 1/CMS2l – 1/ATLAS – TDR – 1 : $M_N = 500\text{GeV}$
 ATLAS2l – 2/CMS2l – 2/ATLAS – TDR – 2 : $M_N = 1000\text{GeV}$

Long lived RHNs

B – L case, $x_H = 0$



Longest lived RHN life time is inversely proportional to m_{lightest}
 $m_{\text{lightest}} \rightarrow 0$ leads to the long lived species as a potential DM candiadte



Type – III seesaw

SM + SU(2)_L triplet fermion

Franceschini, Hambye, Strumia Biggio, Bonnet
 Biggio, Fernandez Martinez, Hernandez Garcia, Lopez Pavon
 AD, Mandal, Modak 2005.02267 AD, Mandal 2006.04123

$$\mathcal{L} = \mathcal{L}_{\text{SM}} + \text{Tr}(\bar{\Psi} i \gamma^\mu D_\mu \Psi) - \frac{1}{2} M \text{Tr}(\bar{\Psi} \Psi^c + \bar{\Psi}^c \Psi) - \sqrt{2}(\bar{\ell}_L Y_D^\dagger \Psi H + H^\dagger \bar{\Psi} Y_D \ell_L)$$

$$\Psi = \begin{pmatrix} \Sigma^0/\sqrt{2} & \Sigma^+ \\ \Sigma^- & -\Sigma^0/\sqrt{2} \end{pmatrix} \text{ and } \Psi^c = \begin{pmatrix} \Sigma^{0c}/\sqrt{2} & \Sigma^{-c} \\ \Sigma^{+c} & -\Sigma^{0c}/\sqrt{2} \end{pmatrix}$$

$$-\mathcal{L}_{\text{mass}} = (\bar{e}_L \ \bar{\Sigma}_L) \begin{pmatrix} m_\ell & Y_D^\dagger v \\ 0 & M \end{pmatrix} \begin{pmatrix} e_R \\ \Sigma_R \end{pmatrix} + \frac{1}{2} (\bar{\nu}_L^c \ \bar{\Sigma}_R^0) \begin{pmatrix} 0 & Y_D^T \frac{v}{\sqrt{2}} \\ Y_D \frac{v}{\sqrt{2}} & M \end{pmatrix} \begin{pmatrix} \nu_L \\ \Sigma_R^{0c} \end{pmatrix} + h.c. \quad \boxed{m_\nu \simeq -\frac{v^2}{2} Y_D^T M^{-1} Y_D = M_D M^{-1} M_D^T}$$

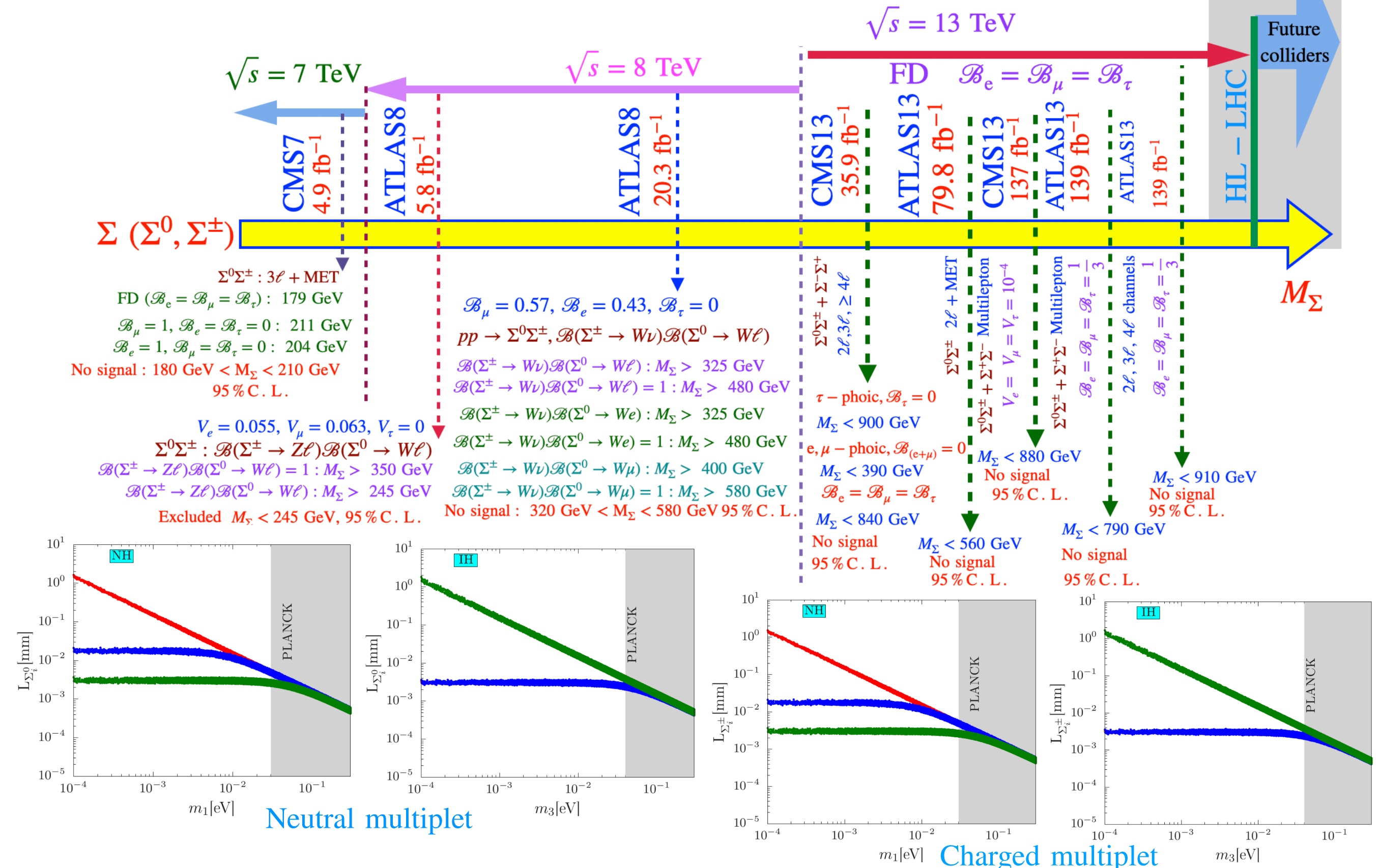
$$\begin{aligned} \Gamma(\Sigma^\pm \rightarrow \nu W) &= \frac{g^2 |V_{\ell\Sigma}|^2}{32\pi} \left(\frac{M^3}{M_W^2} \right) \left(1 - \frac{M_W^2}{M^2} \right)^2 \left(1 + 2 \frac{M_W^2}{M^2} \right) \\ \Gamma(\Sigma^\pm \rightarrow \ell Z) &= \frac{g^2 |V_{\ell\Sigma}|^2}{64\pi \cos^2 \theta_W} \left(\frac{M^3}{M_Z^2} \right) \left(1 - \frac{M_Z^2}{M^2} \right)^2 \left(1 + 2 \frac{M_Z^2}{M^2} \right) \\ \Gamma(\Sigma^\pm \rightarrow \ell h) &= \frac{g^2 |V_{\ell\Sigma}|^2}{64\pi} \left(\frac{M^3}{M_W^2} \right) \left(1 - \frac{M_h^2}{M^2} \right)^2, \end{aligned}$$

$$\begin{aligned} \Gamma(\Sigma^\pm \rightarrow \Sigma^0 \pi^\pm) &= \frac{2G_F^2 V_{ud}^2 \Delta M^3 f_\pi^2}{\pi} \sqrt{1 - \frac{m_\pi^2}{\Delta M^2}} \\ \Gamma(\Sigma^\pm \rightarrow \Sigma^0 e \nu_e) &= \frac{2G_F^2 \Delta M^5}{15\pi} \\ \Gamma(\Sigma^\pm \rightarrow \Sigma^0 \mu \nu_\mu) &= 0.12 \Gamma(\Sigma^\pm \rightarrow \Sigma^0 e \nu_e) \end{aligned}$$

$$\begin{aligned} \Gamma(\Sigma^0 \rightarrow \ell^+ W) &= \Gamma(\Sigma^0 \rightarrow \ell^- W) = \frac{g^2 |V_{\ell\Sigma}|^2}{64\pi} \left(\frac{M^3}{M_W^2} \right) \left(1 - \frac{M_W^2}{M^2} \right)^2 \left(1 + 2 \frac{M_W^2}{M^2} \right) \\ \Gamma(\Sigma^0 \rightarrow \nu Z) &= \Gamma(\Sigma^0 \rightarrow \bar{\nu} Z) = \frac{g^2 |V_{\ell\Sigma}|^2}{128\pi \cos^2 \theta_W} \left(\frac{M^3}{M_Z^2} \right) \left(1 - \frac{M_Z^2}{M^2} \right)^2 \left(1 + 2 \frac{M_Z^2}{M^2} \right) \\ \Gamma(\Sigma^0 \rightarrow \nu h) &= \Gamma(\Sigma^0 \rightarrow \bar{\nu} h) = \frac{g^2 |V_{\ell\Sigma}|^2}{128\pi} \left(\frac{M^3}{M_W^2} \right) \left(1 - \frac{M_h^2}{M^2} \right)^2, \end{aligned}$$

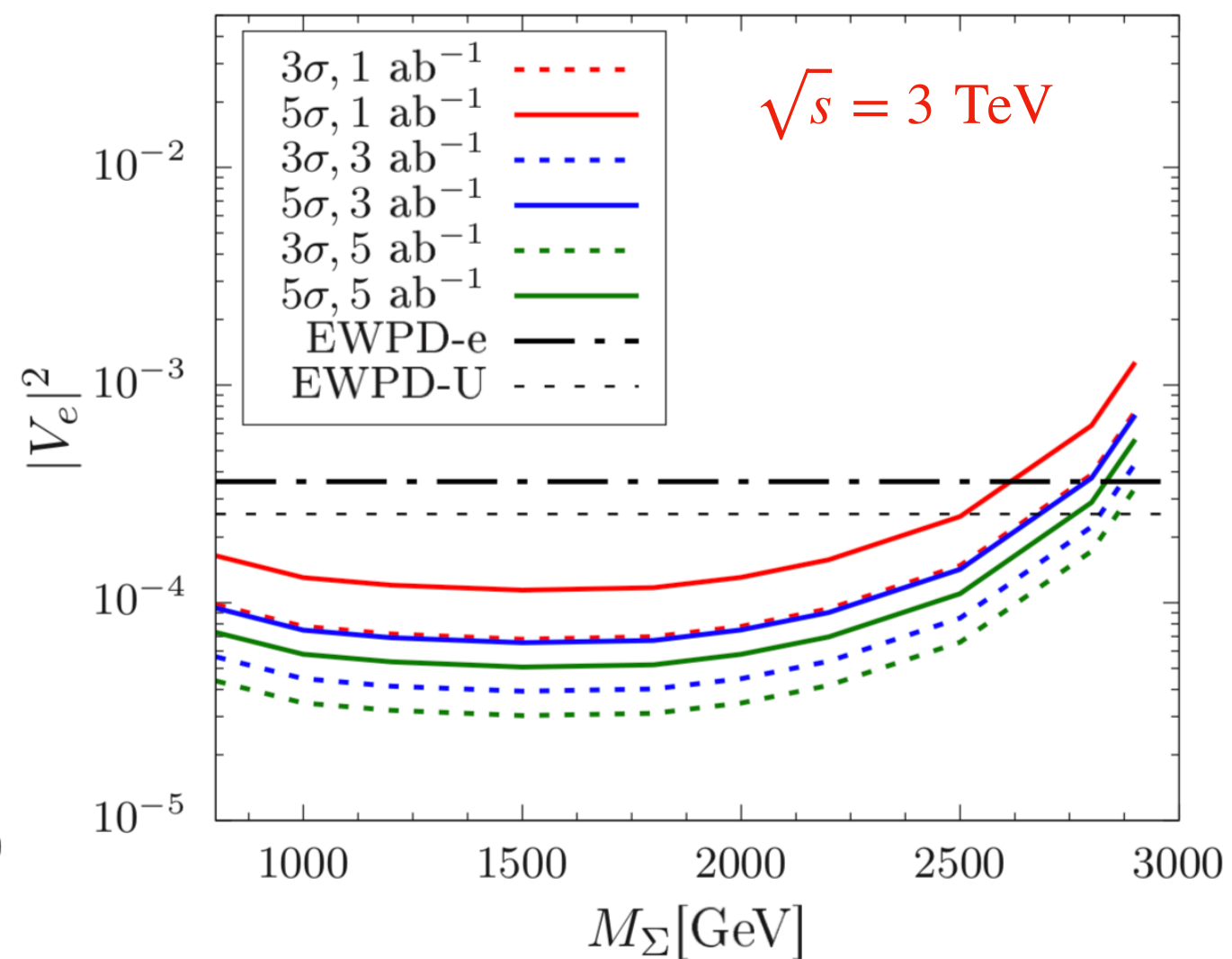
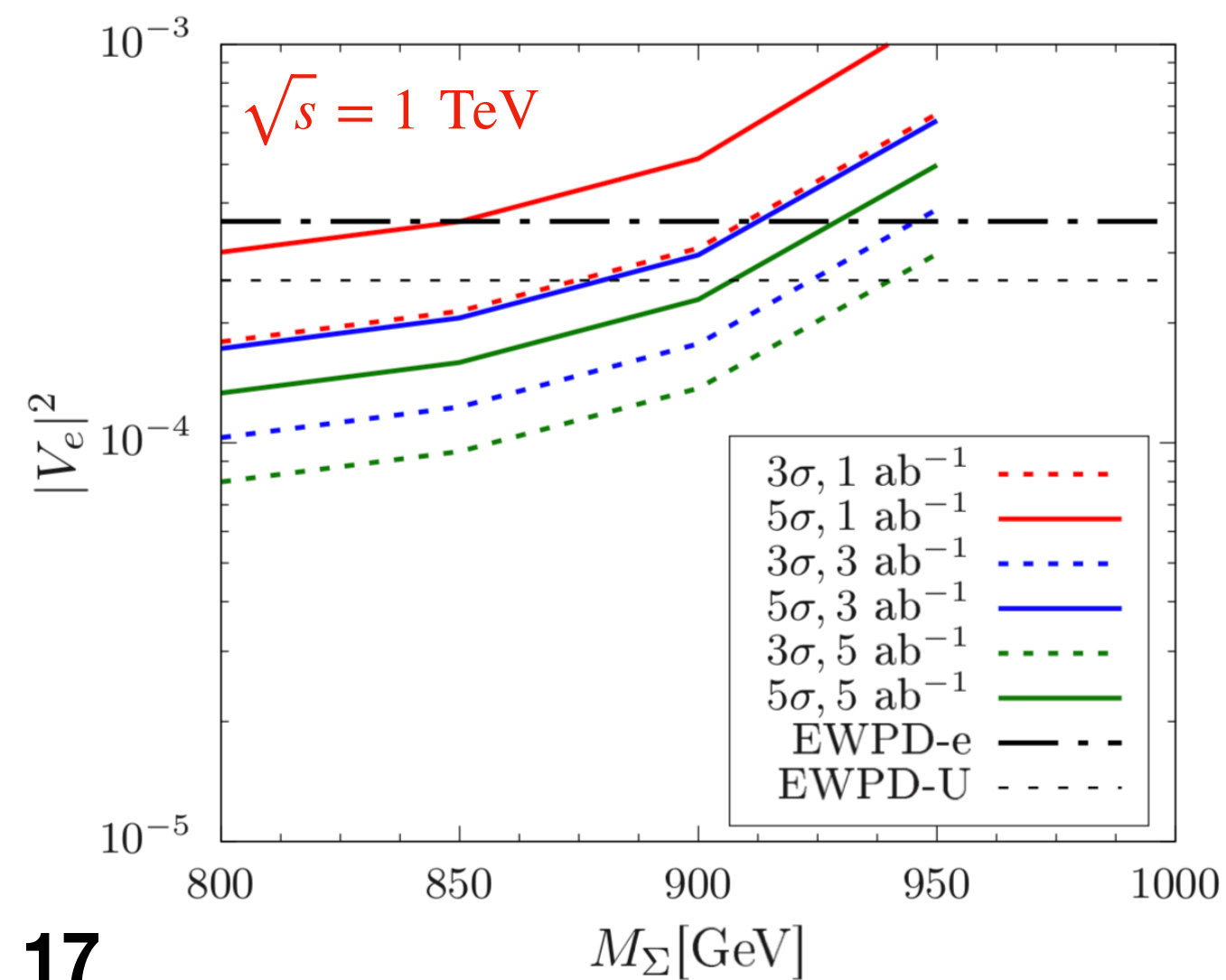
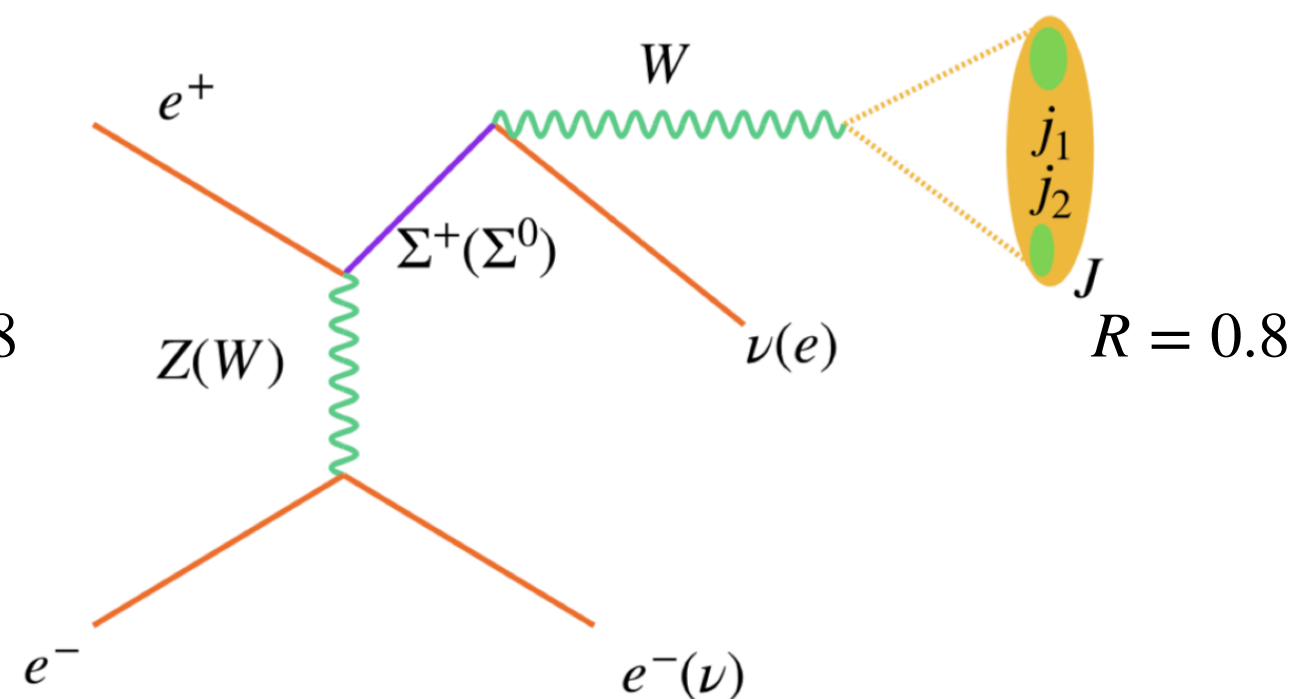
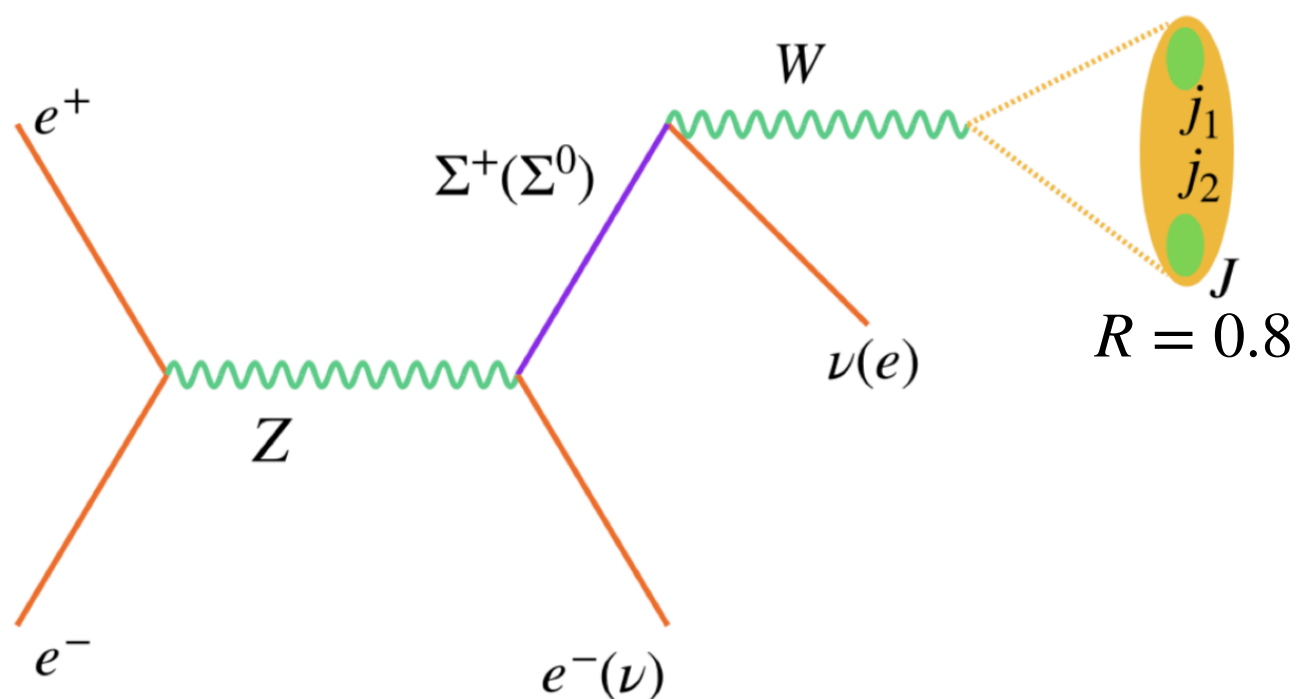
Experimental limits from ATLAS and CMS on type – III seesaw

2006.04123



Mass-mixing limit plots

2005.02267



Summary

We study the models with the heavy fermions under the simple extensions of the SM where the neutrino mass is generated by the seesaw mechanism at the tree level to reproduce the neutrino oscillation data.

Stay tuned . . .

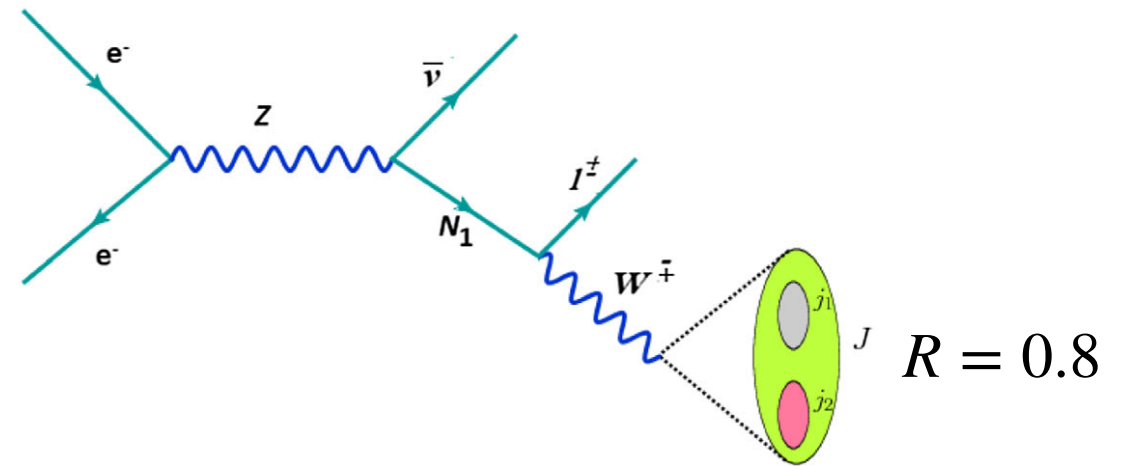
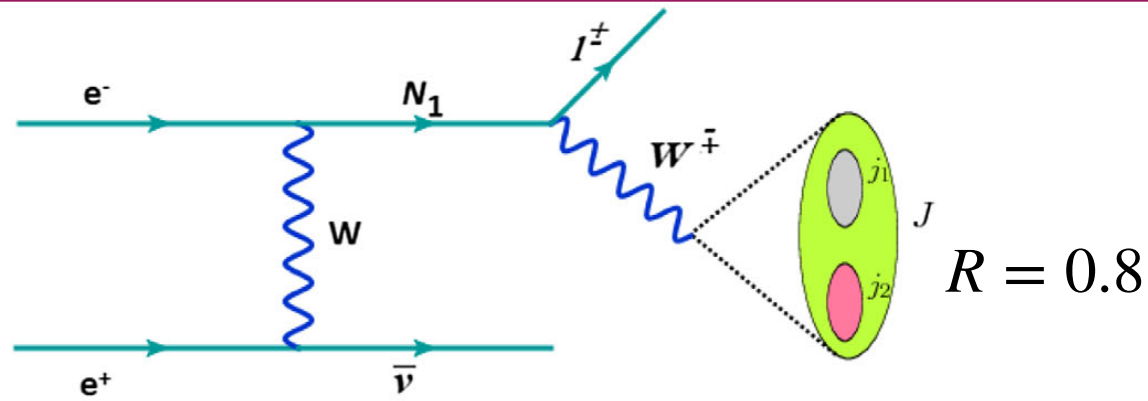


Thank You

We find that such heavy fermions can be tested at the underground experiments- at the proton-proton, electron-positron and electron-proton colliders in the near future. We have calculated the bounds on the light-heavy mixings for the electron-positron collider which could be probed in the near future.

Back – up slides

$e + J + p_T^{\text{miss}}$ final states at the linear colliders.



- Transverse momentum for fat-jet $p_T^J > 150$ GeV for M_N mass range 400 GeV-600 GeV and $p_T^J > 250$ GeV for M_N mass range 700 GeV-900 GeV.
- Transverse momentum for leading lepton $p_T^{e^\pm} > 100$ GeV for M_N mass range 400 GeV-600 GeV and $p_T^{e^\pm} > 200$ GeV for M_N mass range 700 GeV-900 GeV.
- Polar angle of lepton and fat-jet $|\cos \theta_e| < 0.85$, $|\cos \theta_J| < 0.85$.
- Fat-jet mass $M_J > 70$ GeV.

1 TeV e^-e^+ collider

- Transverse momentum for fat-jet $p_T^J > 250$ GeV for the M_N mass range 700 GeV-900 GeV and $p_T^J > 400$ GeV for M_N mass range 1 – 2.9 TeV.
- Transverse momentum for leading lepton $p_T^{e^\pm} > 200$ GeV for M_N mass range 700 – 900 GeV and $p_T^{e^\pm} > 250$ GeV for M_N mass range 1 – 2.9 TeV.
- Polar angle of lepton and fat-jet $|\cos \theta_e| < 0.85$, $|\cos \theta_J| < 0.85$.
- Fat-jet mass $M_J > 70$ GeV.

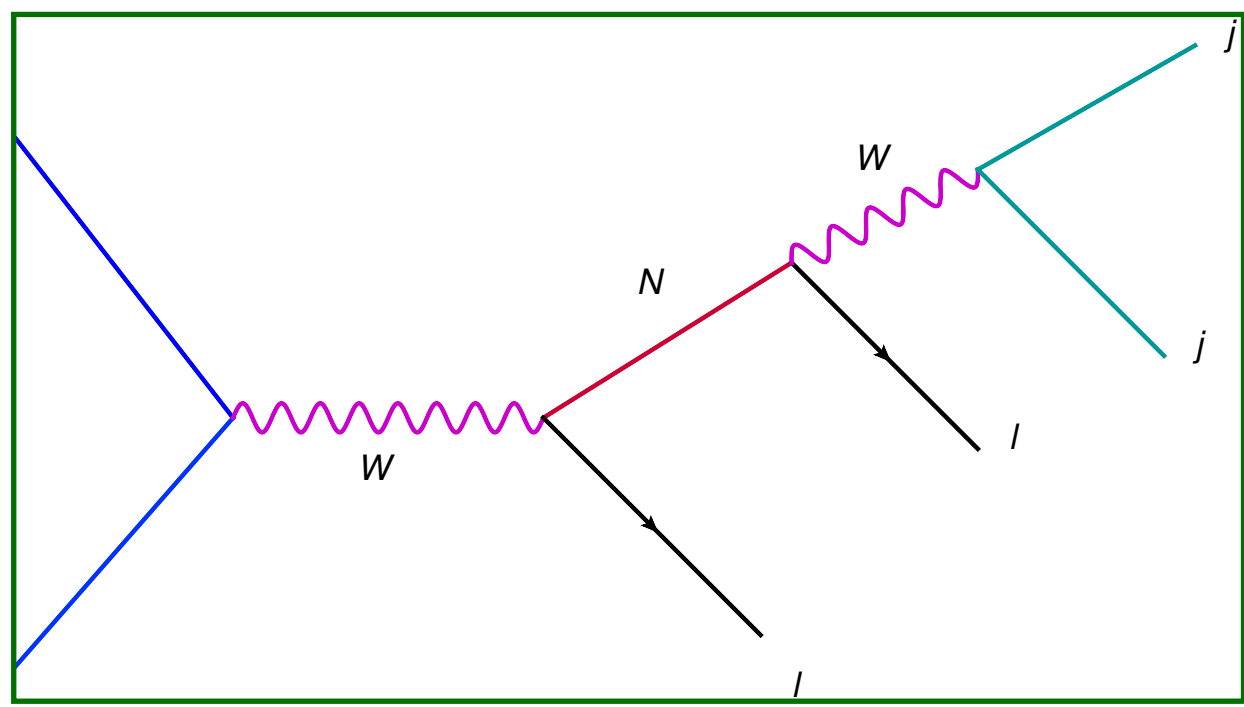
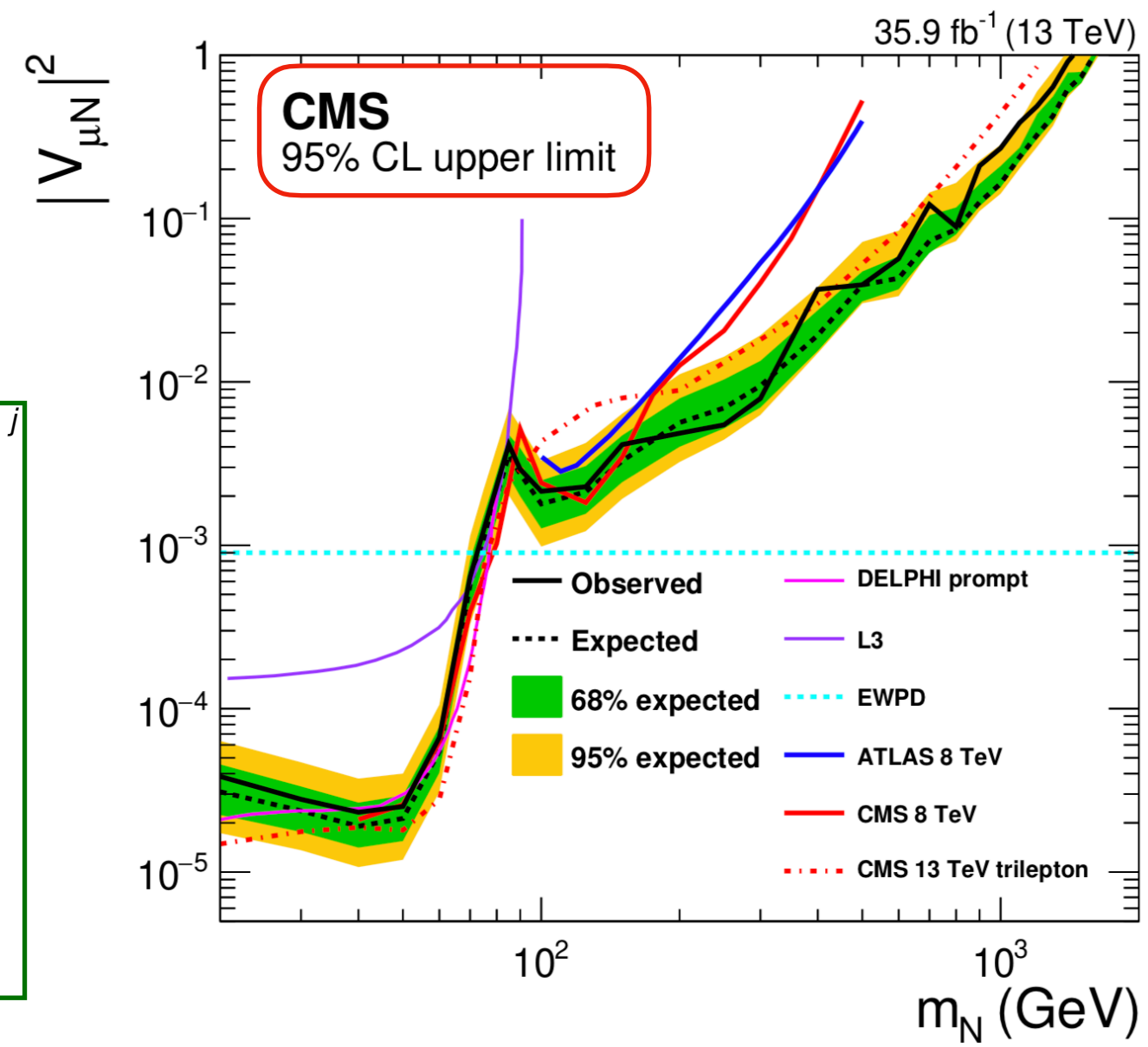
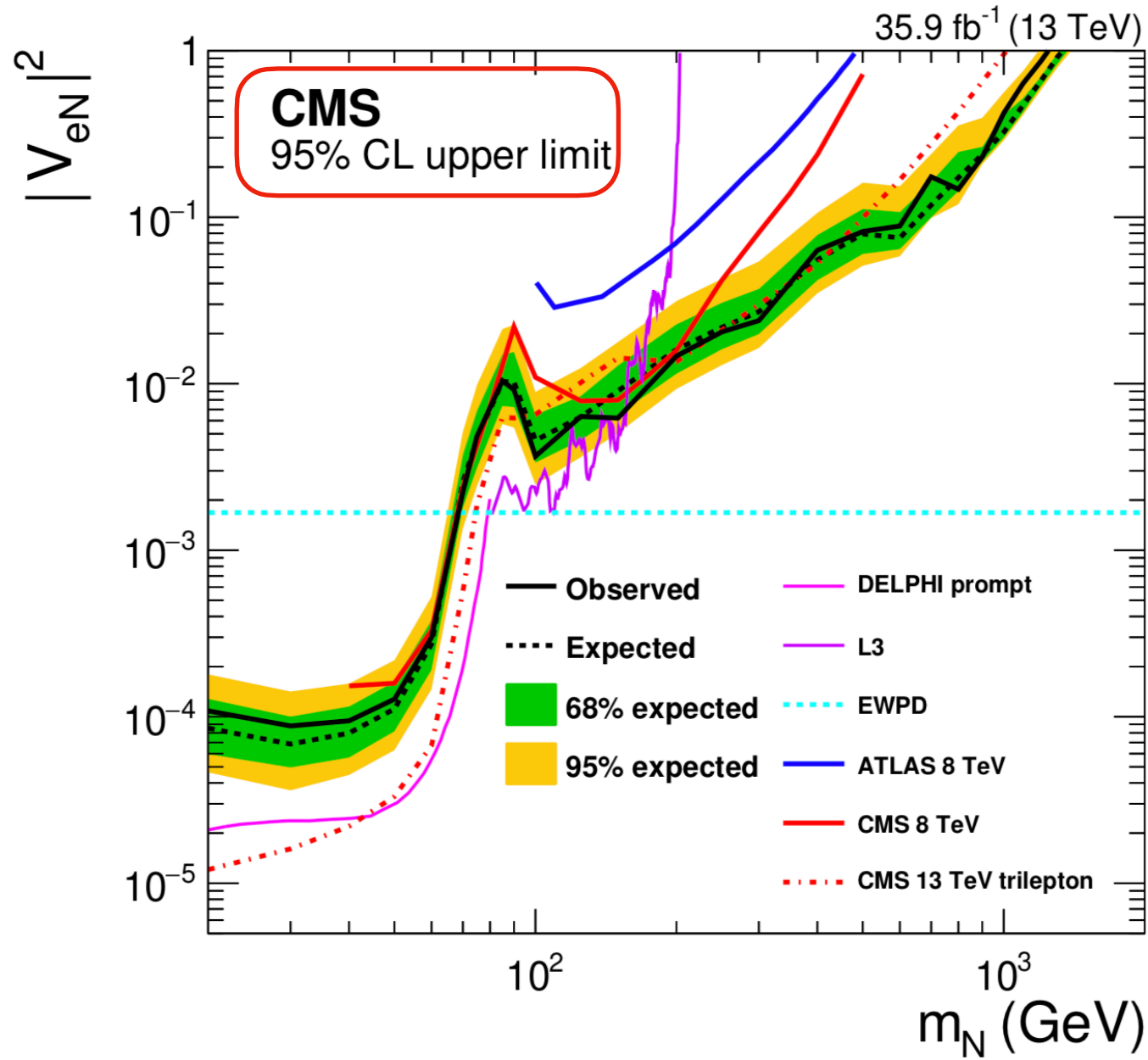
3 TeV e^-e^+ collider

Experimental limits

$\ell^\pm \ell^\pm + \text{jets}$

CMS

1806.10905 13 TeV, 35.9 fb⁻¹



22


$$|V_{\mu N}|^2$$

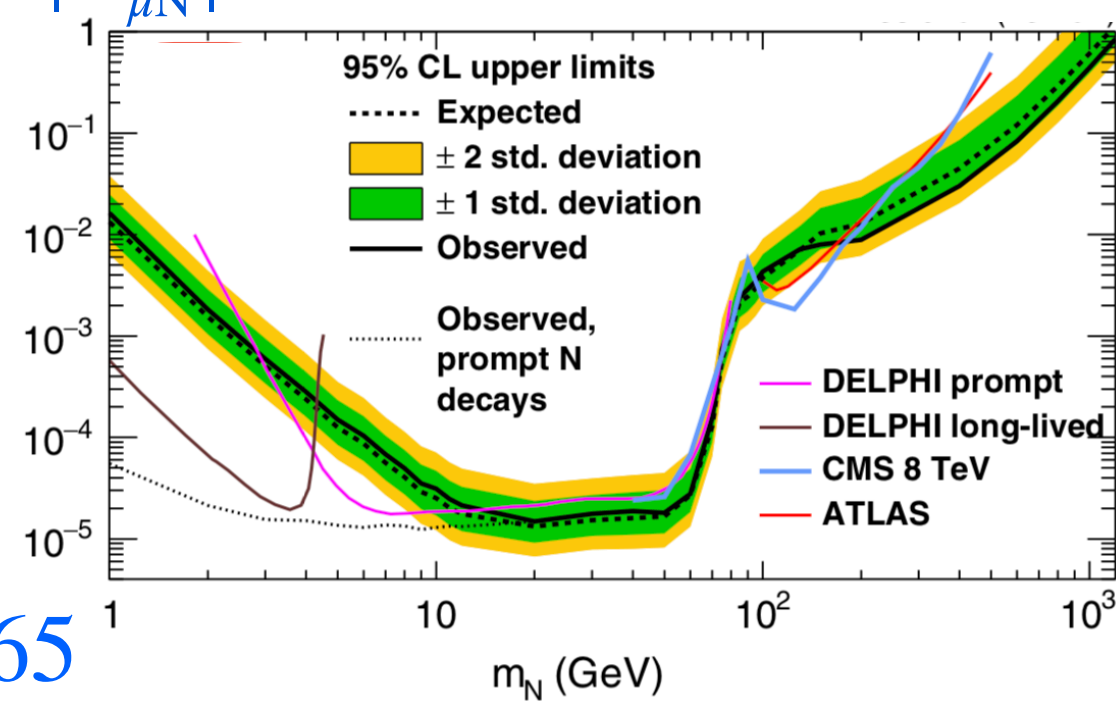

1905.09787



CMS

 35.9 fb^{-1}

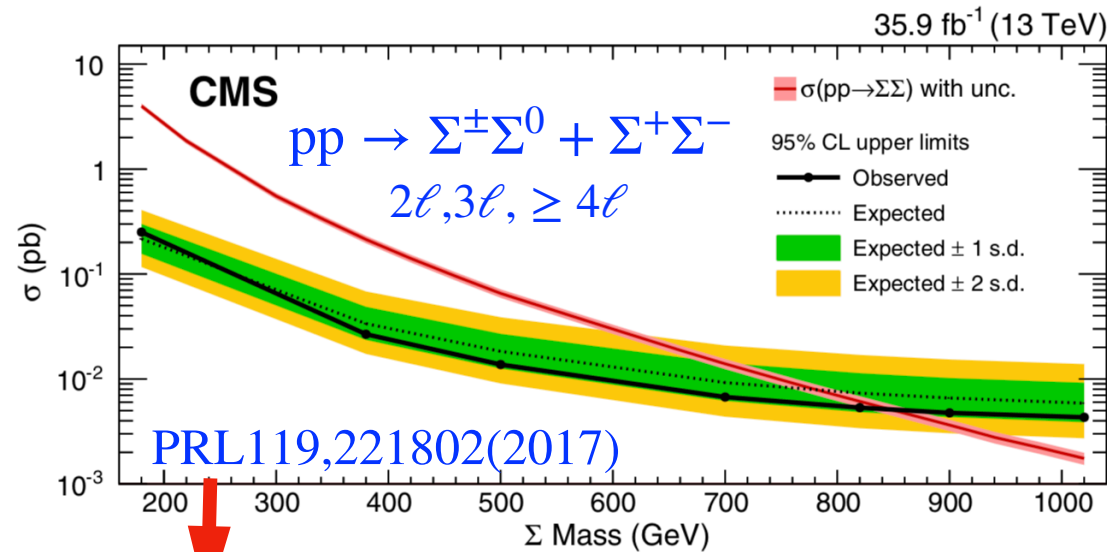
1802.02965³



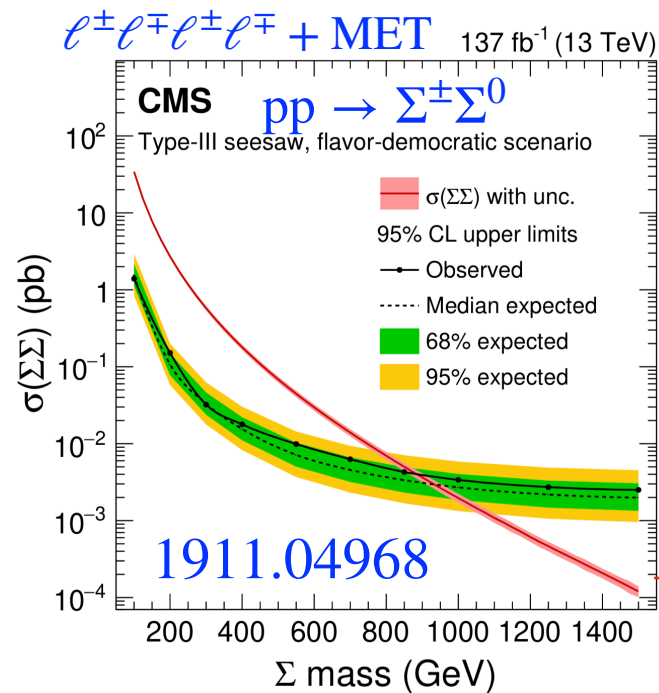
LHC limits

$$\text{BR} = B_\ell \propto \frac{|V_\ell|^2}{|V_e|^2 + |V_\mu|^2 + |V_\tau|^2}$$

$B_e = B_\mu = B_\tau$
Flavor – democratic scenario



τ – phoic, $B_\tau = 0, M_\Sigma = 900$ GeV, 90 % CL
(e, μ) – phoic, $B_{e+\mu} = 0, M_\Sigma = 390$ GeV, 90 % CL



$M_\Sigma \leq 800$ GeV
 $M_\Sigma \leq 900$ GeV

