The future of high-energy astrophysical neutrino flavor measurements

Mauricio Bustamante

Niels Bohr Institute, University of Copenhagen

Based on:

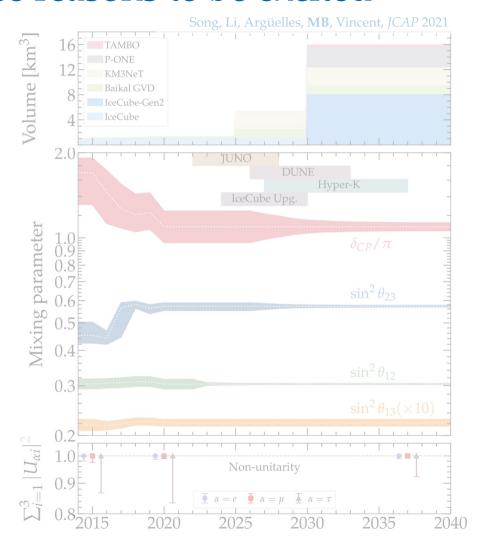
Ningqiang Song, Shirley Li, Carlos Argüelles, MB, Aaron Vincent JCAP 04, 054 (2021) [2012.12893]

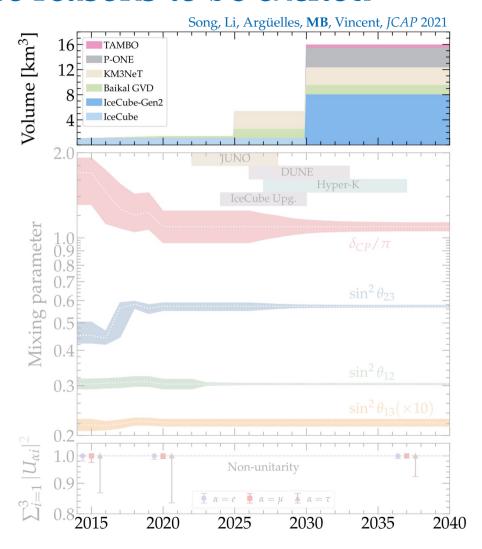
EPS-HEP July 29, 2021



VILLUM FONDEN

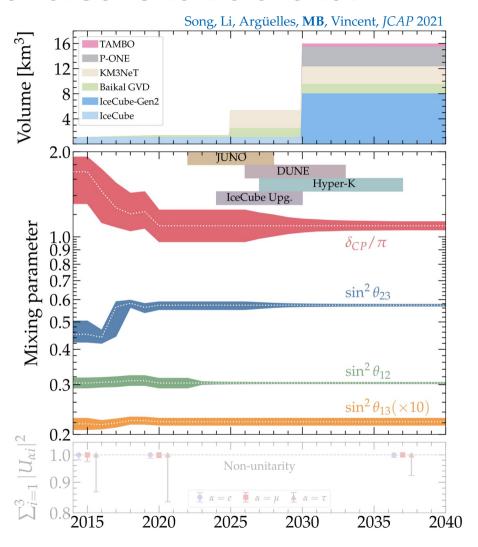






Flavor measurements:

New neutrino telescopes = more events, better flavor measurement

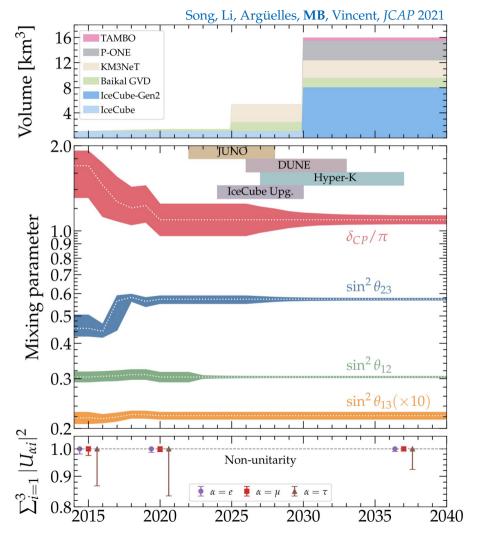


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Oscillation physics:

We will know the mixing parameters better (JUNO, DUNE, Hyper-K, IceCube Upgrade)



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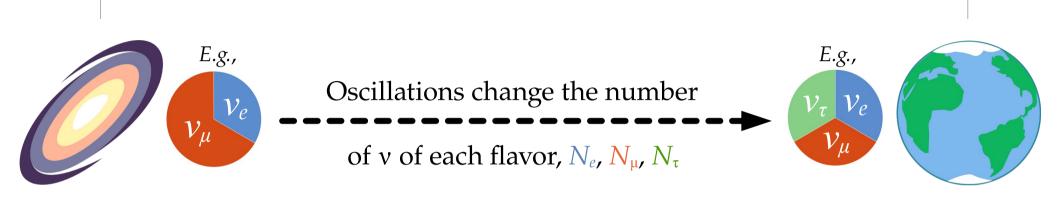
Oscillation physics:

We will know the mixing parameters better (JUNO, DUNE, Hyper-K, IceCube Upgrade)

Test of the oscillation framework:

We will be able to do what we want even if oscillations are non-unitary

Up to a few Gpc



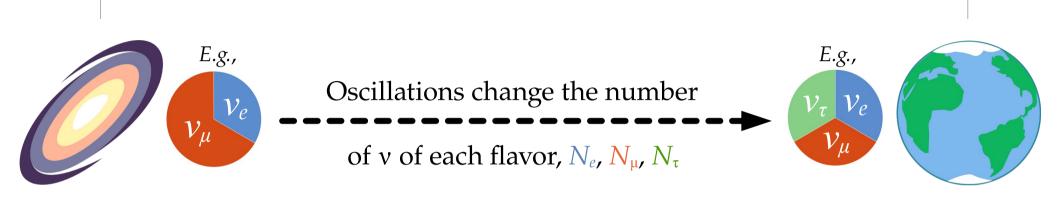
Different production mechanisms yield different flavor ratios:

$$(f_{e,S}, f_{\mu,S}, f_{\tau,S}) \equiv (N_{e,S}, N_{\mu,S}, N_{\tau,S})/N_{\text{tot}}$$

Flavor ratios at Earth ($\alpha = e, \mu, \tau$):

$$f_{\alpha,\oplus} = \sum_{\beta=e,\mu,\tau} P_{\nu_{\beta}\to\nu_{\alpha}} f_{\beta,S}$$

Up to a few Gpc



Different production mechanisms yield different flavor ratios:

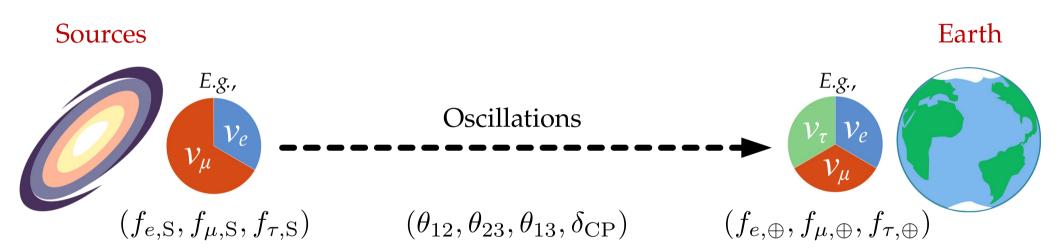
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Flavor ratios at Earth
$$(\alpha = e, \mu, \tau)$$
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$$f_{\alpha, \oplus} = \sum P_{\nu_{\beta} \to \nu_{\alpha}} f_{\beta, S}$$

$$f_{\alpha,\oplus} = \sum_{\beta=e,\mu,\tau} P_{\nu_{\beta} \to \nu_{\alpha}} f_{\beta,\beta}$$

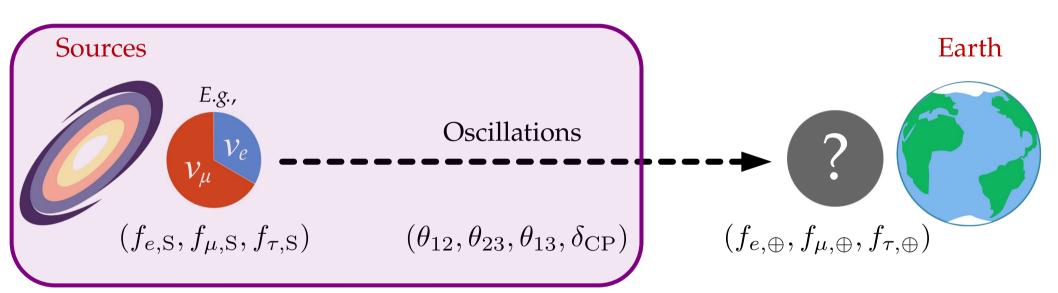
Standard oscillations or new physics

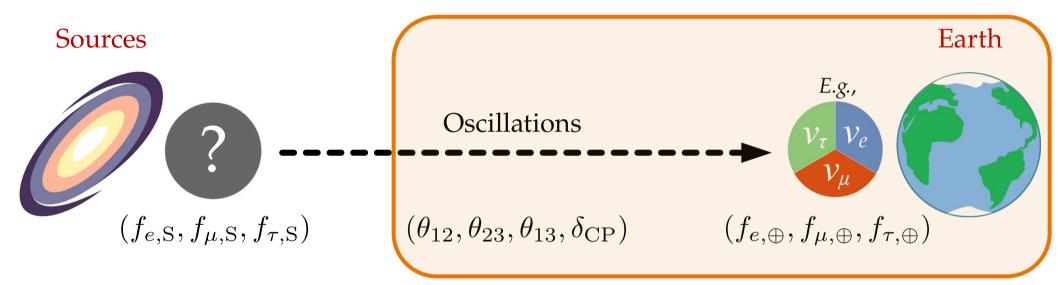
From sources to Earth: we learn what to expect when measuring $f_{\alpha,\oplus}$



From Earth to sources: we let the data teach us about $f_{\alpha,S}$

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From Earth to sources: we let the data teach us about $f_{\alpha,S}$

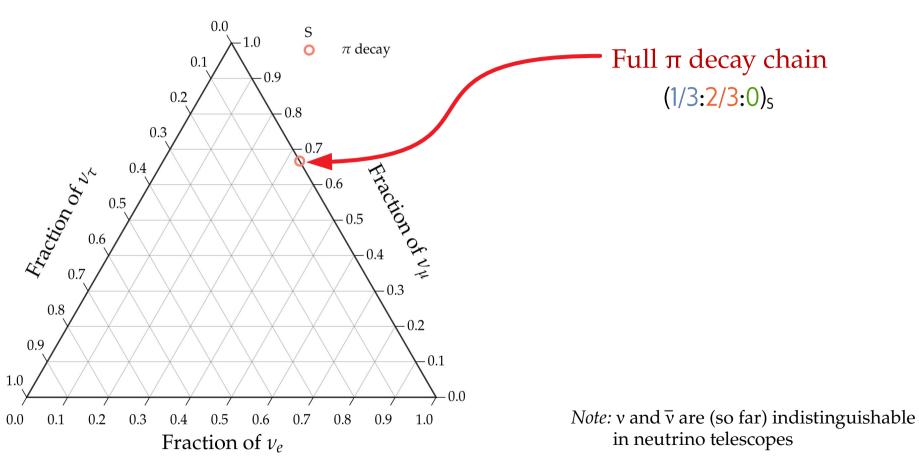
One likely TeV–PeV v production scenario: $p + \gamma \rightarrow \pi^+ \rightarrow \mu^+ + \nu_{\mu}$ followed by $\mu^+ \rightarrow e^+ + \nu_e + \overline{\nu}_{\mu}$

Full π decay chain (1/3:2/3:0)₅

Note: v and \overline{v} are (so far) indistinguishable in neutrino telescopes

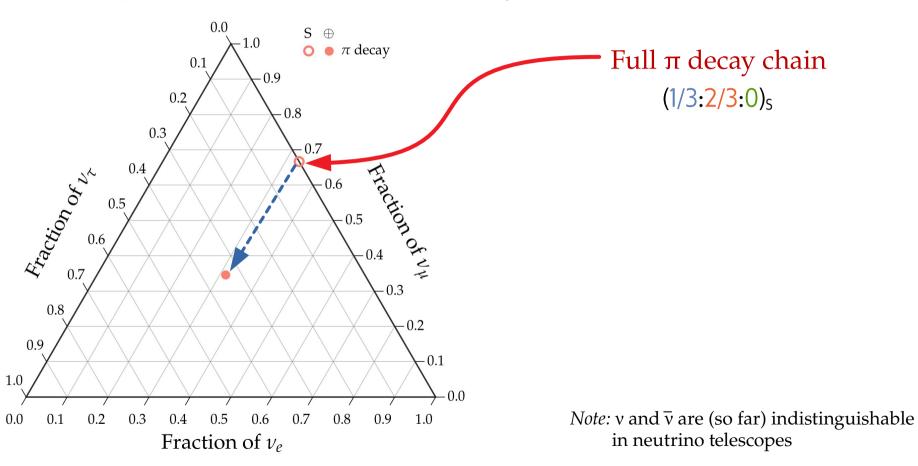
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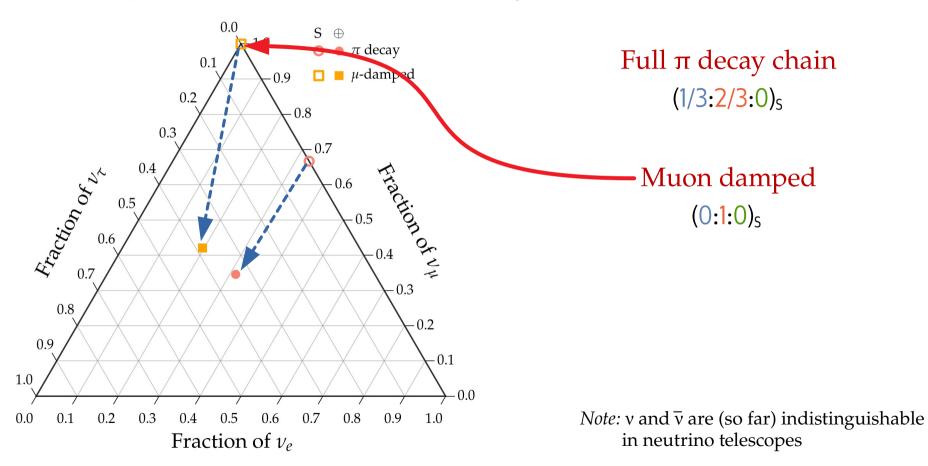
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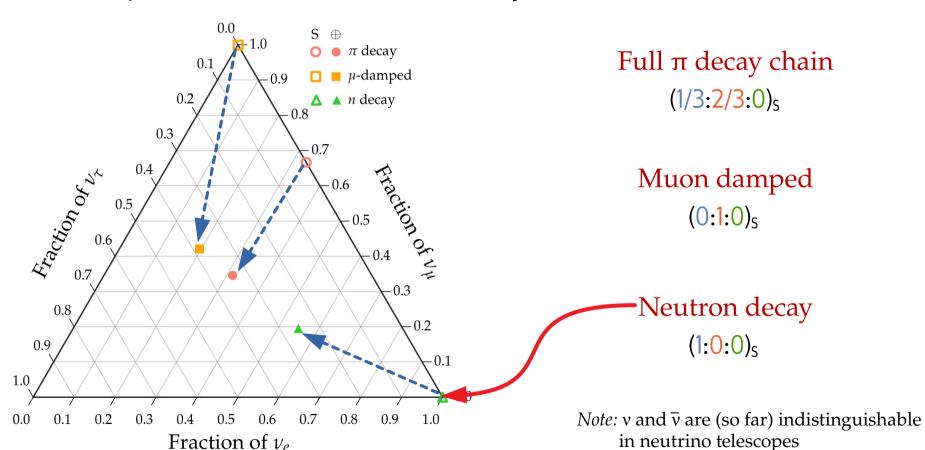
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How does IceCube see TeV-PeV neutrinos?

Deep inelastic neutrino-nucleon scattering

Neutral current (NC)

Charged current (CC)

$$v_x + N \rightarrow v_x + X$$

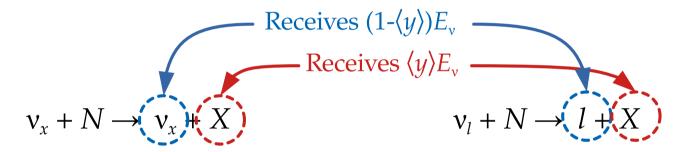
$$v_l + N \rightarrow l + X$$

How does IceCube see TeV-PeV neutrinos?

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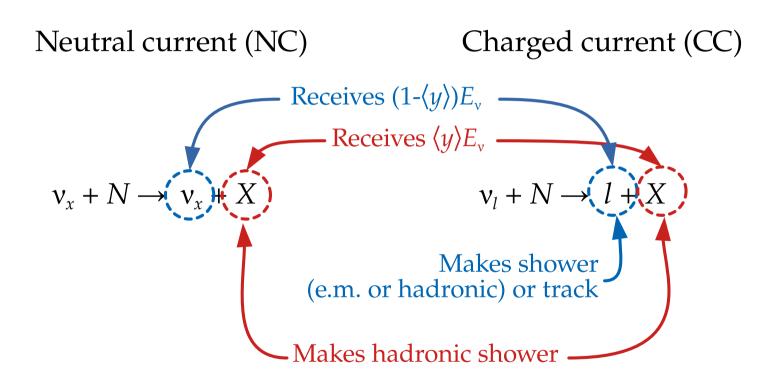
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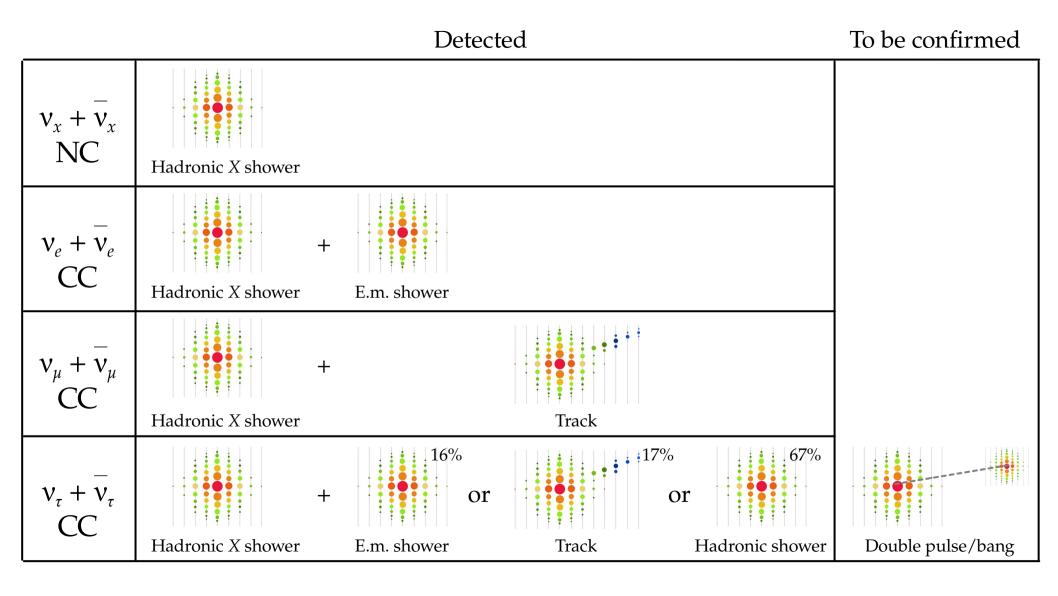
At TeV–PeV, the average inelasticity $\langle y \rangle = 0.25-0.30$

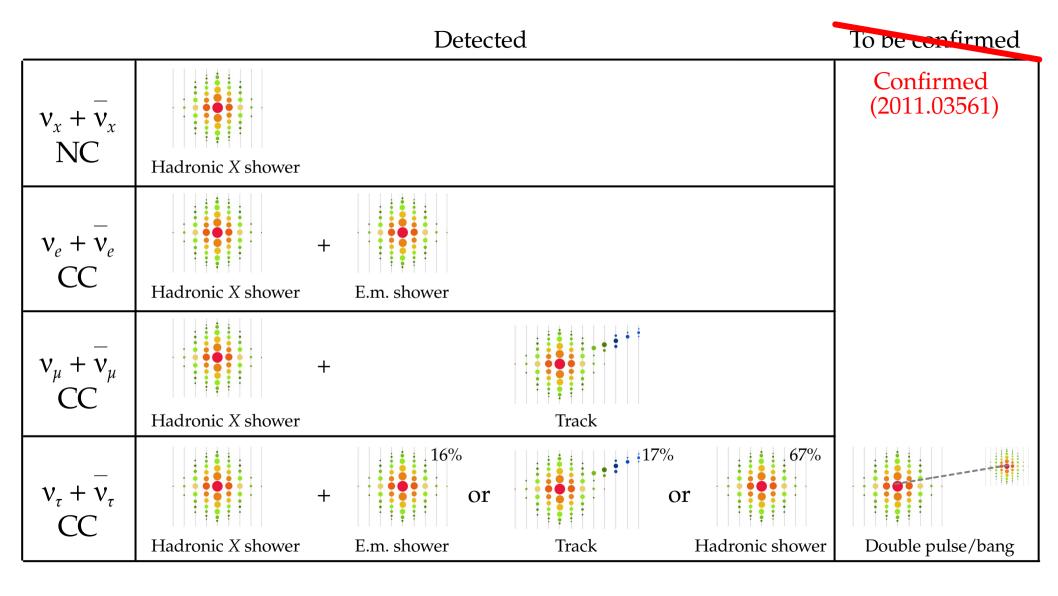
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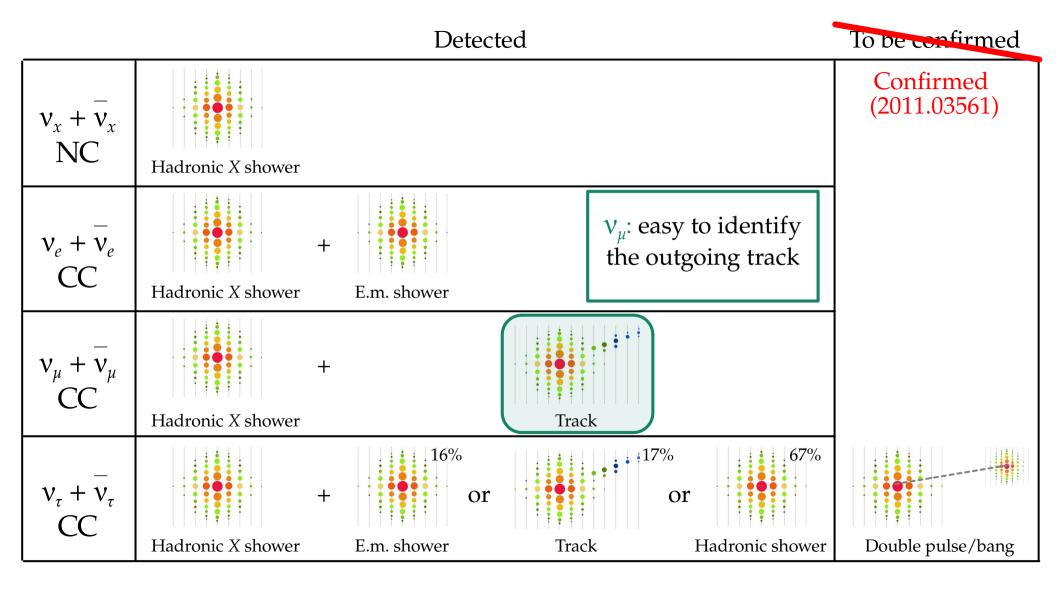
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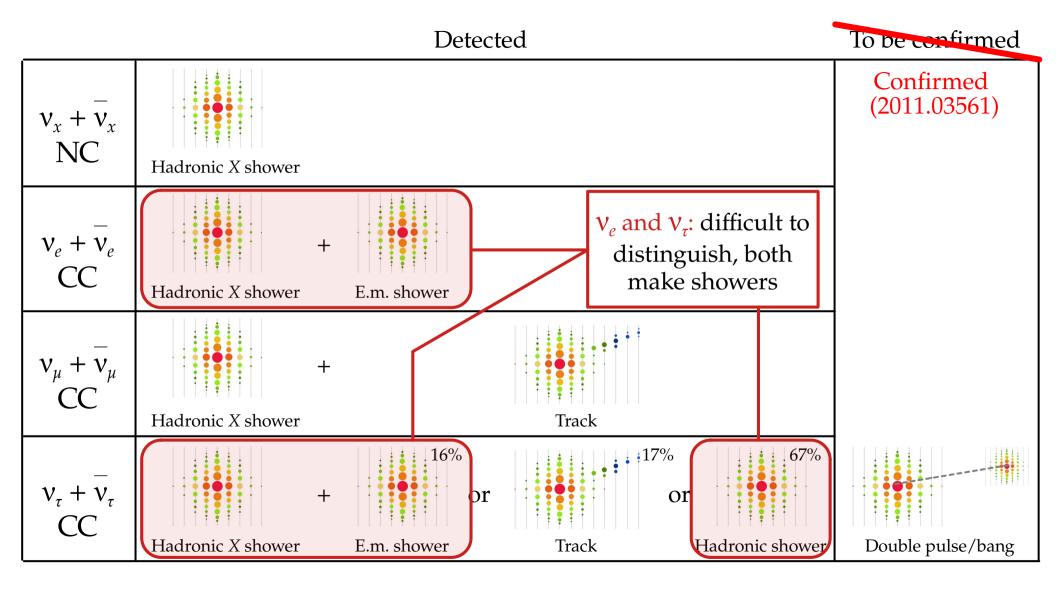


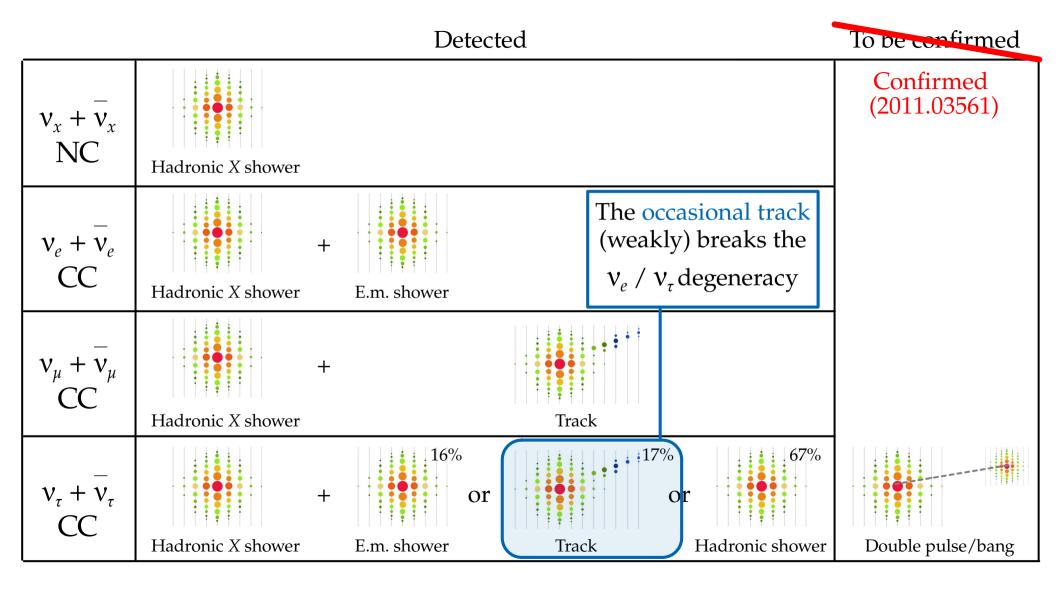
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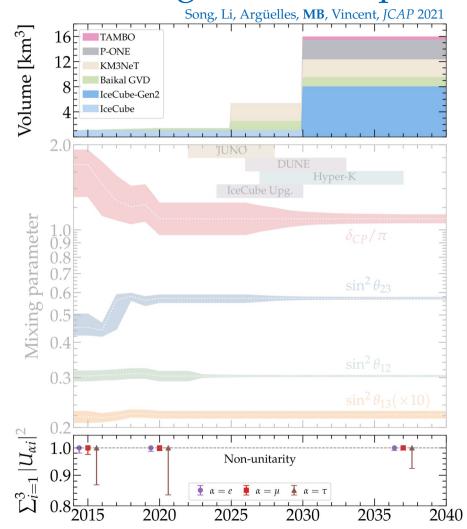


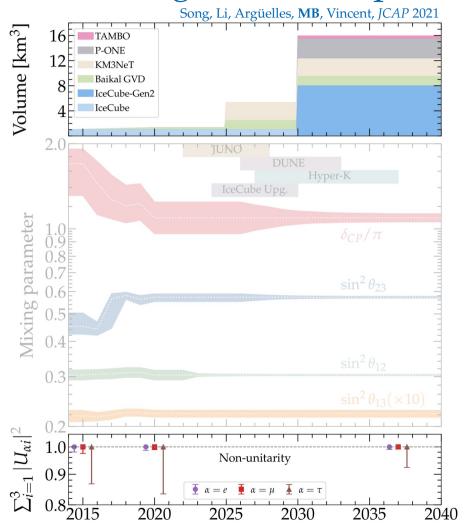


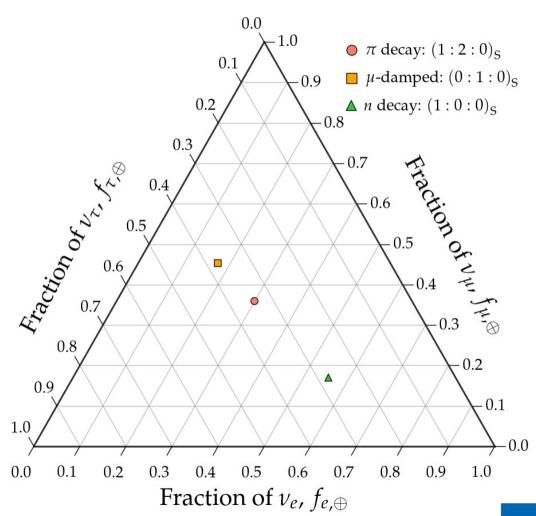


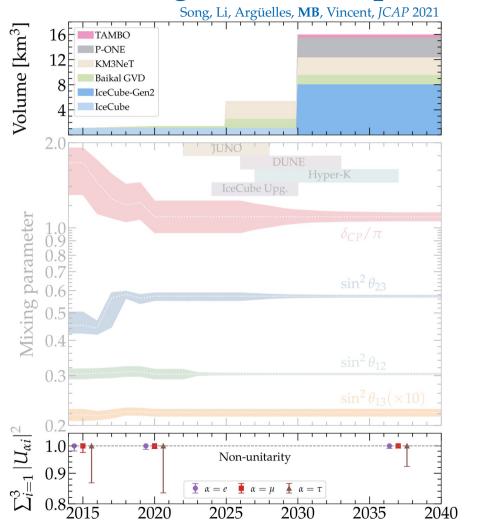


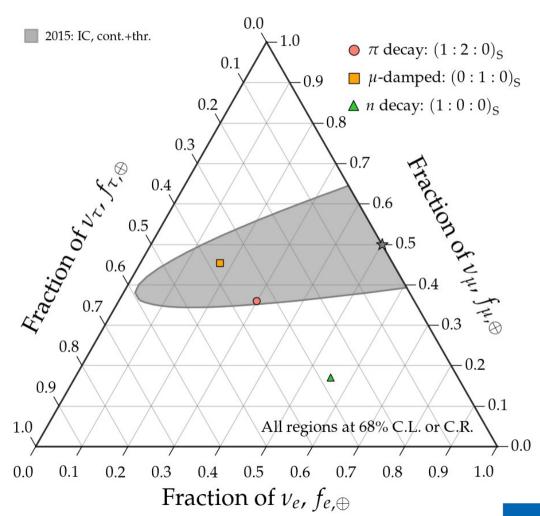


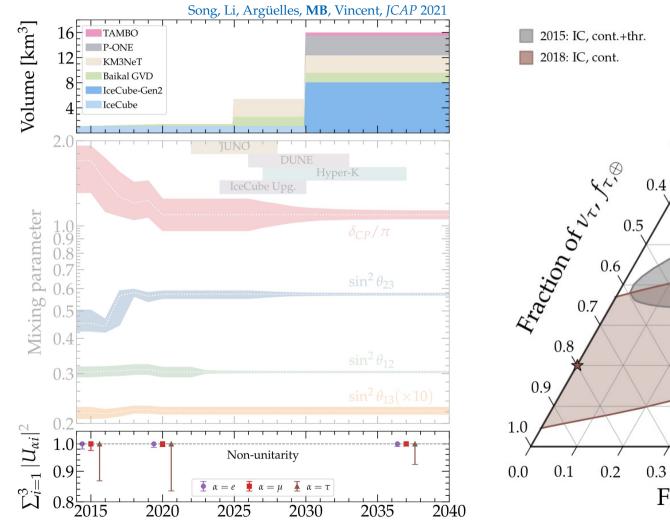


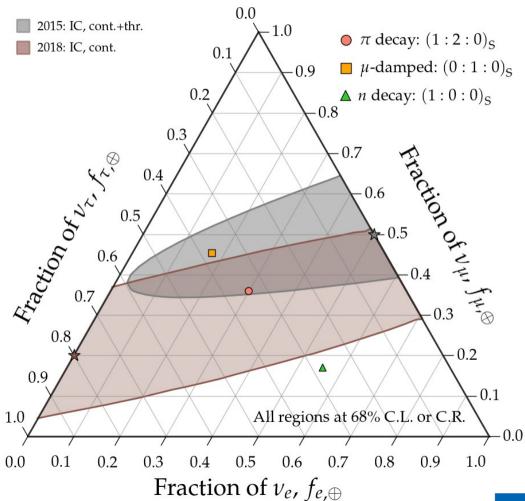


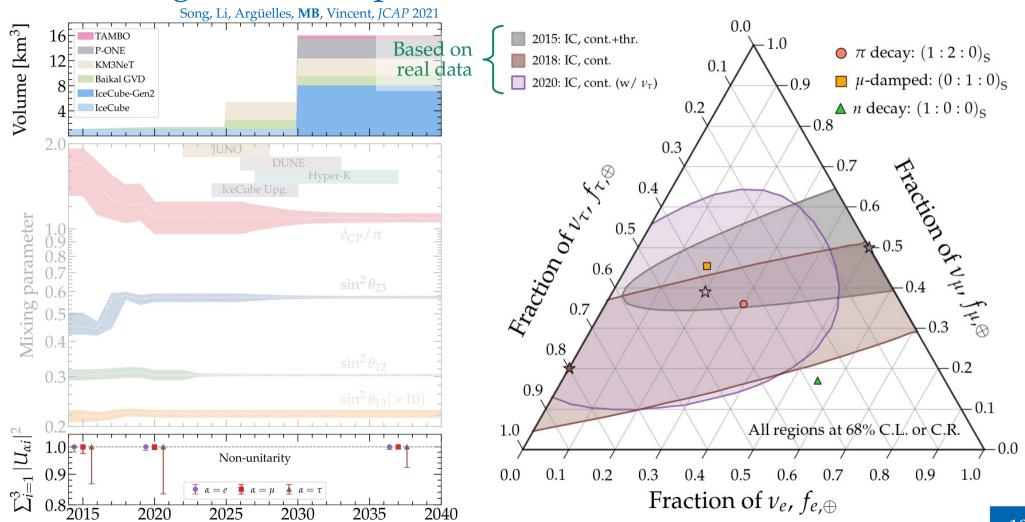


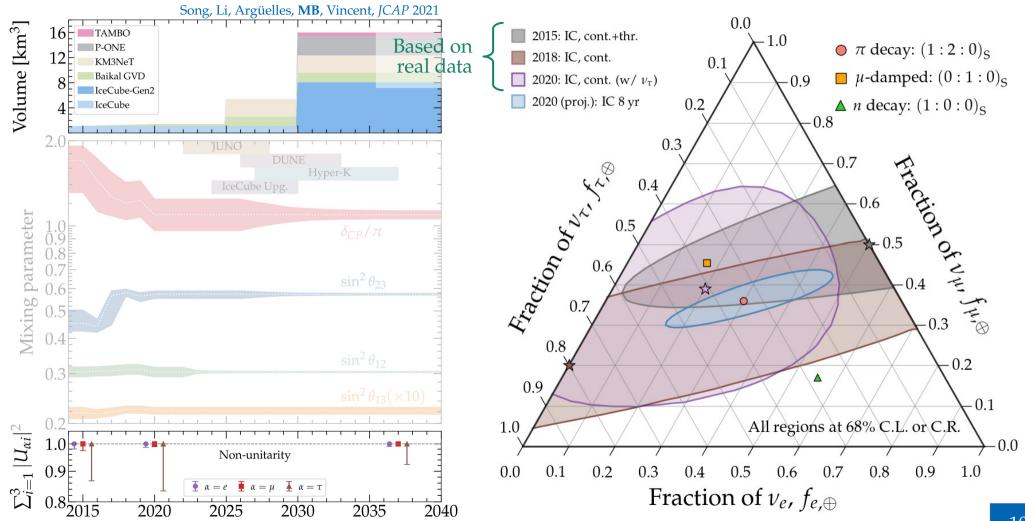


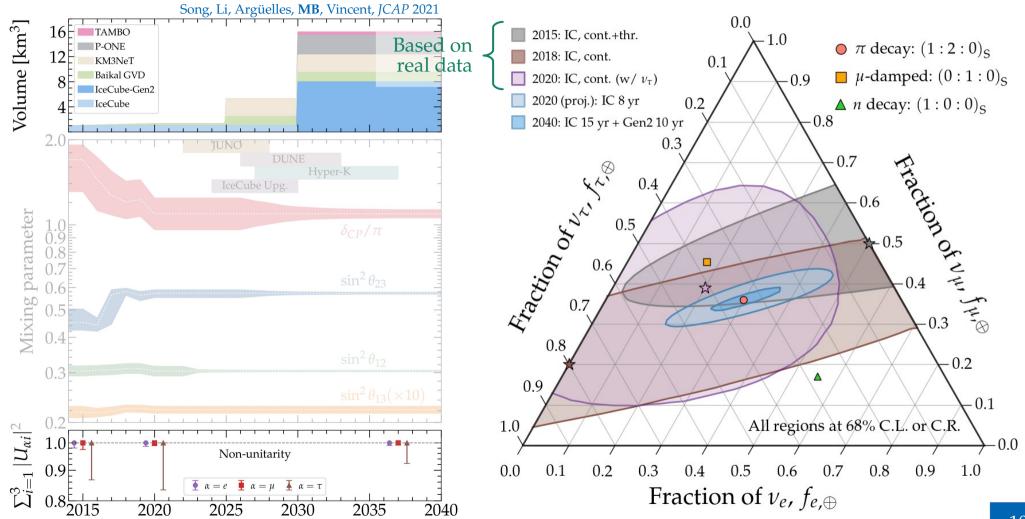


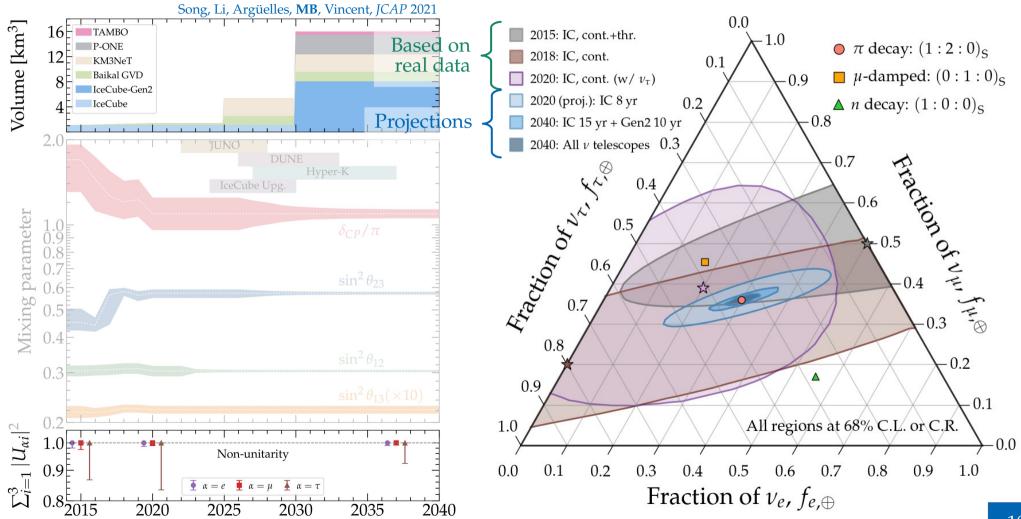




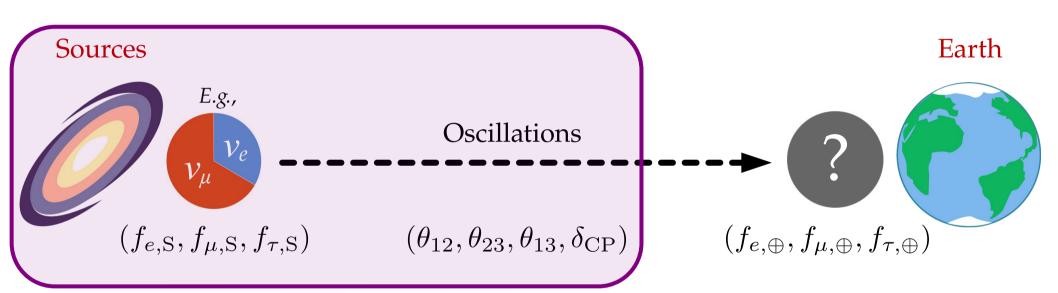








From sources to Earth: we learn what to expect when measuring $f_{\alpha,\oplus}$



Theoretically palatable flavor regions

=

MB, Beacom, Winter, PRL 2015

Allowed regions of flavor ratios at Earth derived from oscillations

Note:

The original palatable regions were frequentist [MB, Beacom, Winter, PRL 2015]; the new ones are Bayesian

Theoretically palatable flavor regions

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Ingredient #1:

Flavor ratios at the source,

 $(f_{e,S},f_{\mu,S},f_{\tau,S})$

Fix at one of the benchmarks (pion decay, muon-damped, neutron decay)

or

Explore all possible combinations

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Ingredient #2:

Theoretically palatable flavor regions

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Flavor ratios at the source, $(f_{e,S}, f_{\mu,S}, f_{\tau,S})$

Ingredient #2:

Probability density of mixing parameters (θ_{12} , θ_{23} , θ_{13} , δ_{CP})

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Flavor at the Earth: theoretically palatable regions

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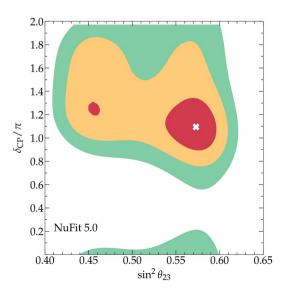
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Ingredient #2: Probability density of mixing parameters (θ_{12} , θ_{23} , θ_{13} , δ_{CP})

2020: Use χ² profiles from the NuFit 5.0 global fit (solar + atmospheric + reactor + accelerator) Esteban et al., JHEP 2020 www.nu-fit.org



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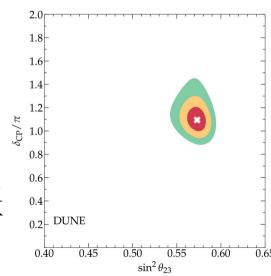
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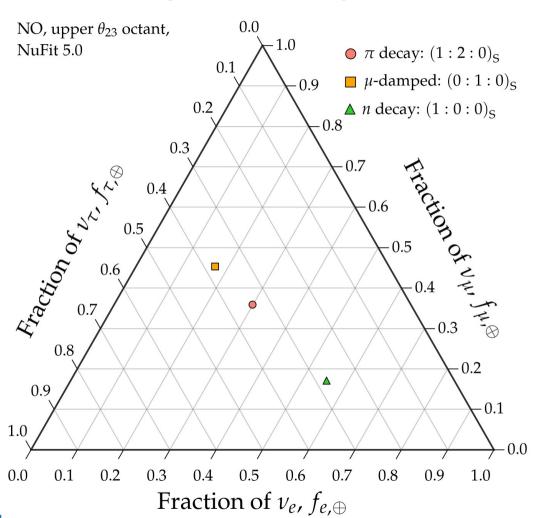
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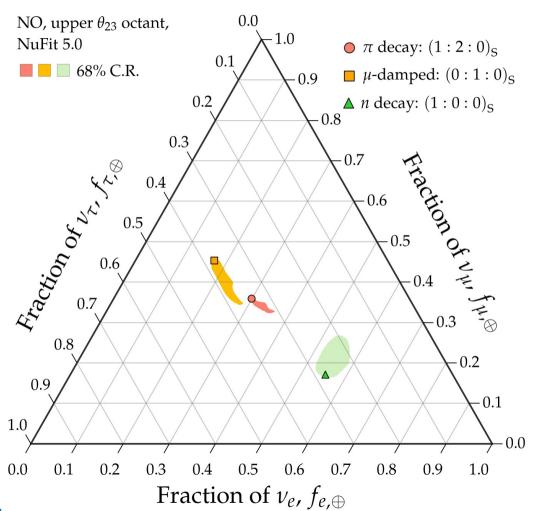
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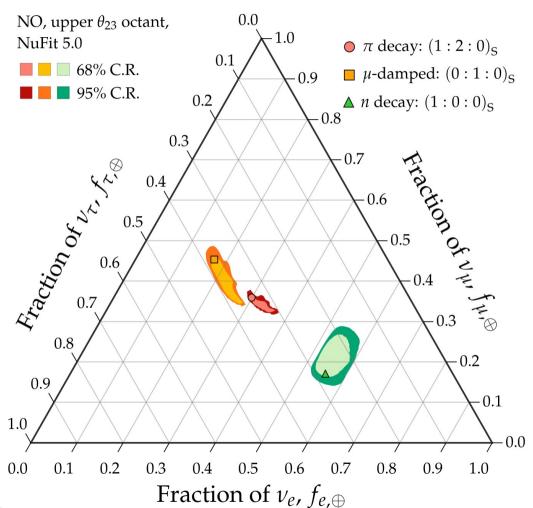
Post-2020: Build our own profiles using simulations of JUNO, DUNE, Hyper-K

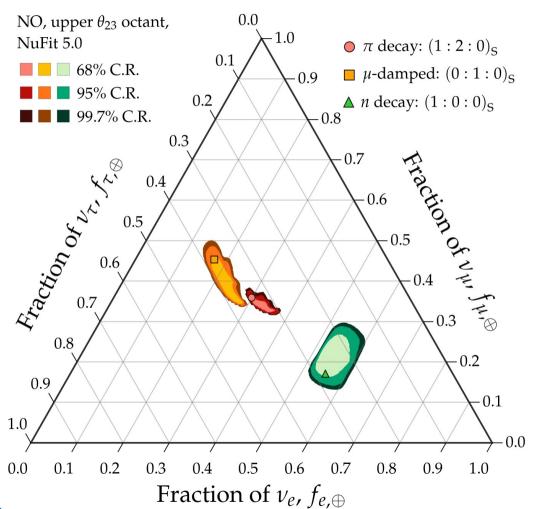
An et al., J. Phys. G 2016 DUNE, 2002.03005 Huber, Lindner, Winter, Nucl. Phys. B 2002



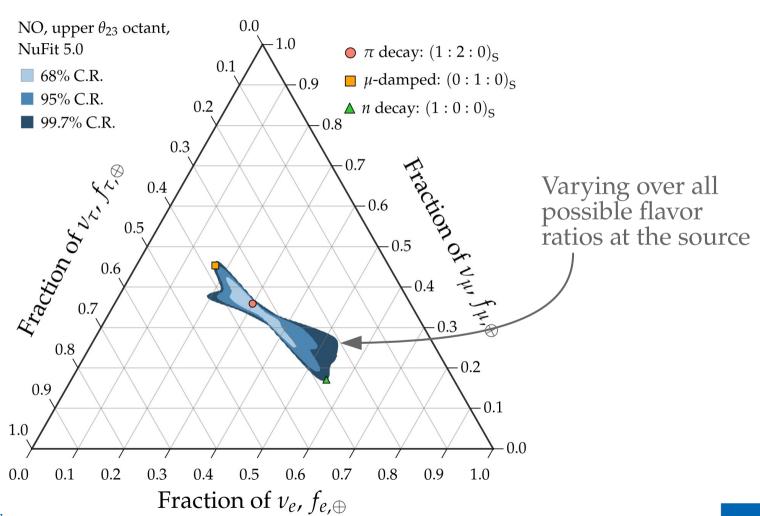


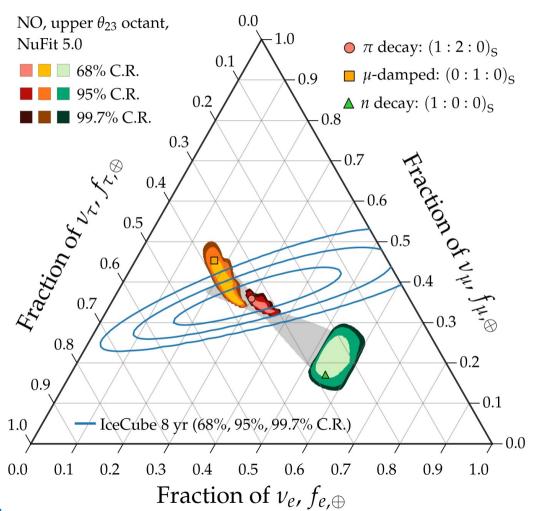


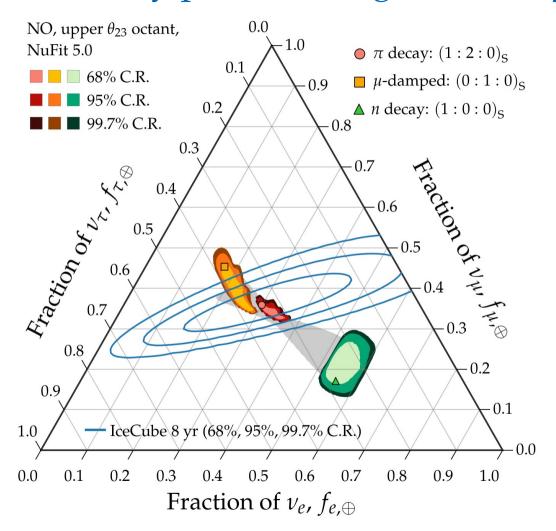




Note:



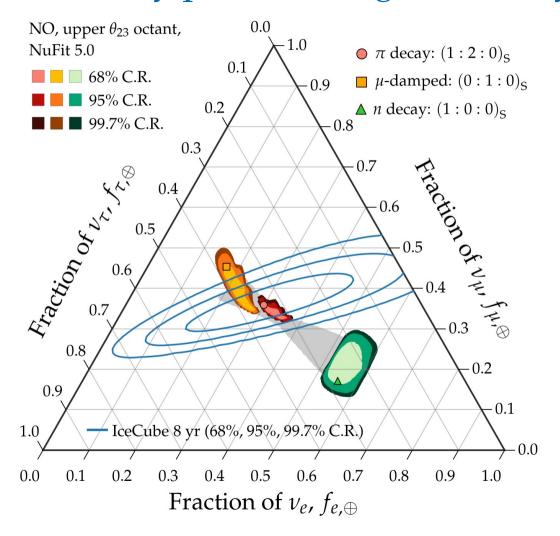




Two limitations:

Allowed flavor regions overlap – Insufficient precision in the mixing parameters

Measurement of flavor ratios – Cannot distinguish between pion-decay and muon-damped benchmarks even at 68% C.R. (1σ)

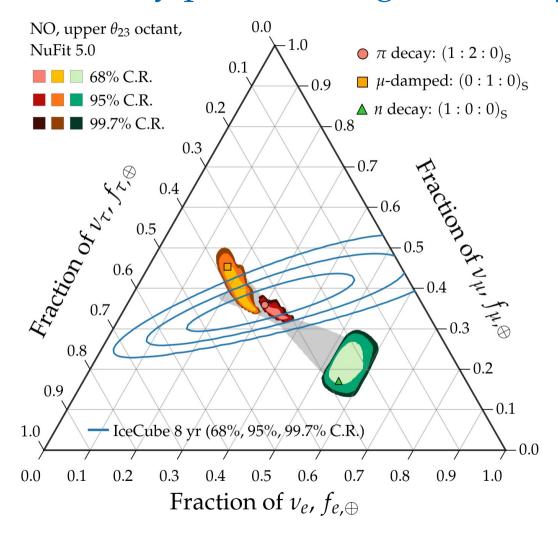


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Will be overcome by 2030

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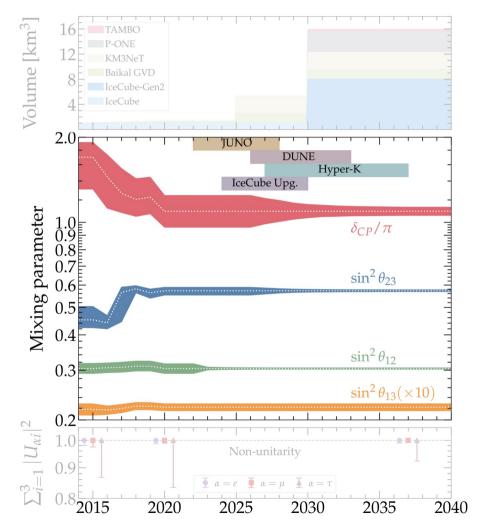
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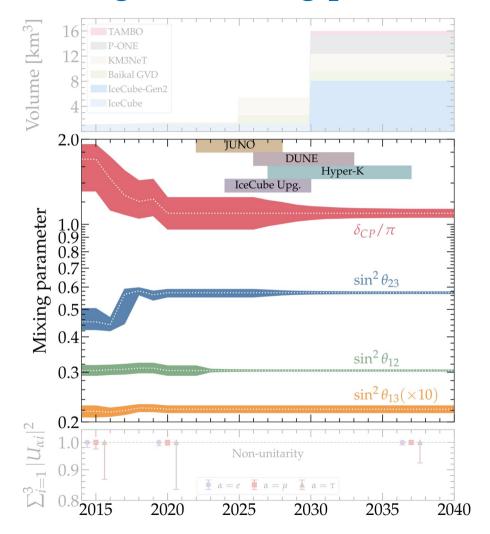
Will be overcome by 2040



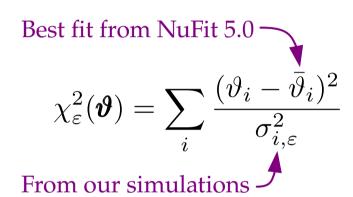
We can compute the oscillation probability more precisely:

$$f_{\alpha,\oplus} = \sum_{\beta=e,\mu,\tau} P_{\beta\alpha} f_{\beta,S}$$

So we can convert back and forth between source and Earth more precisely

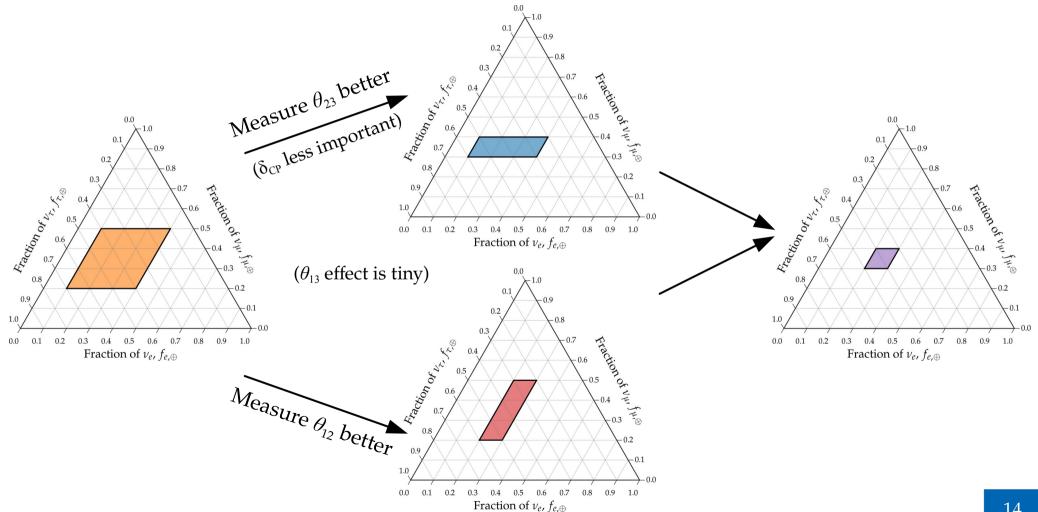


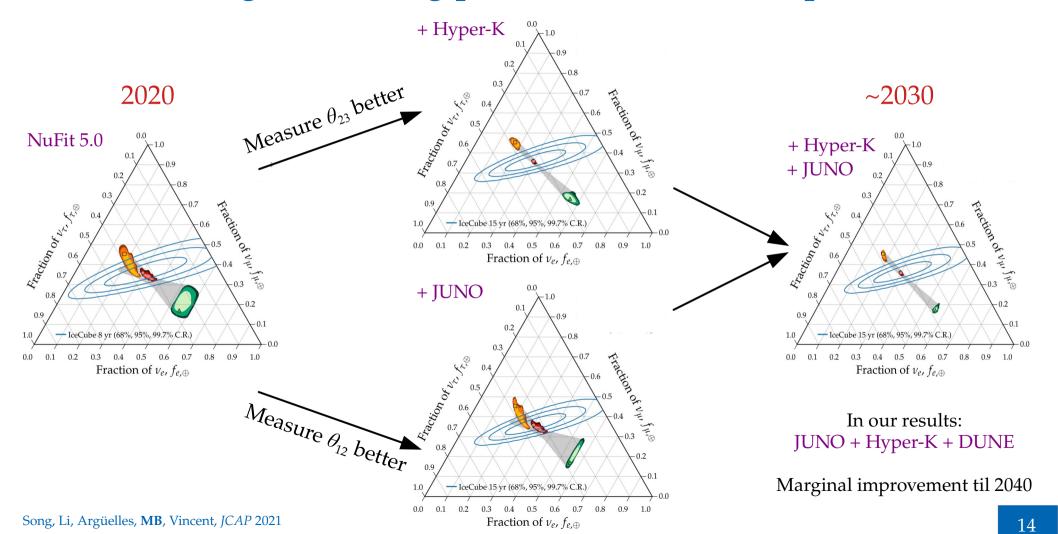
For a future experiment $\varepsilon = JUNO$, DUNE, Hyper-K:



We combine experiments in a likelihood:

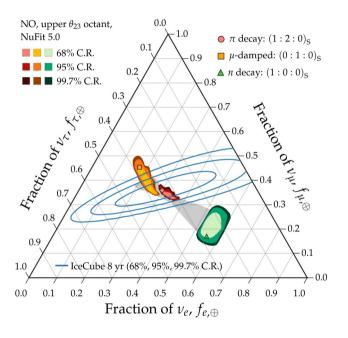
$$-2\log \mathcal{L}(\boldsymbol{\theta}) = \sum_{\varepsilon} \chi_{\varepsilon}^{2}(\boldsymbol{\vartheta})$$





Song, Li, Argüelles, MB, Vincent, JCAP 2021

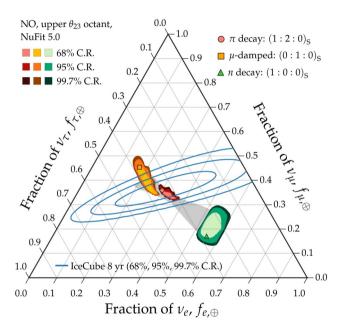
2020



Allowed regions: overlapping

Measurement: imprecise

2020

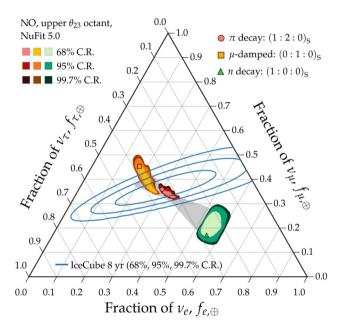


Allowed regions: overlapping

Measurement: imprecise

Not ideal

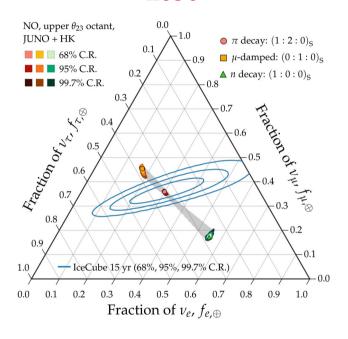




Allowed regions: overlapping Measurement: imprecise

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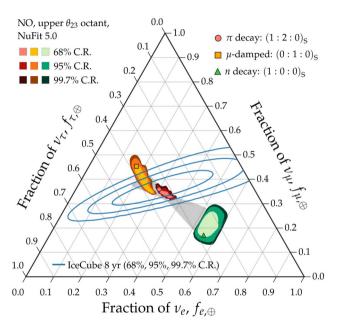
2030



Allowed regions: well separated

Measurement: improving

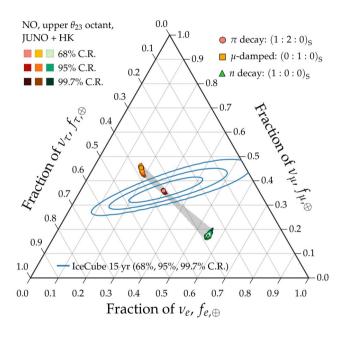




Allowed regions: overlapping Measurement: imprecise

Not ideal

2030

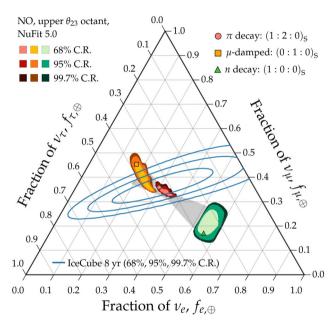


Allowed regions: well separated

Measurement: improving

Nice

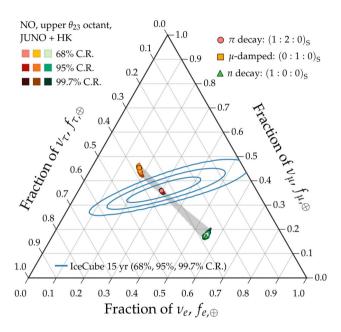




Allowed regions: overlapping Measurement: imprecise

Not ideal

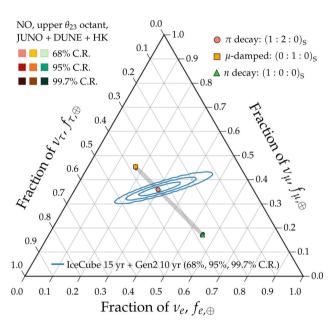
2030



Allowed regions: well separated Measurement: improving

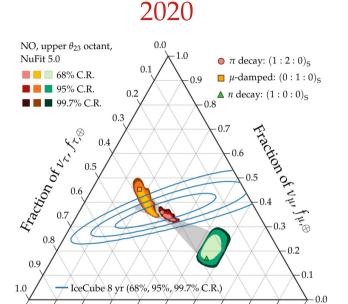
Nice

2040



Allowed regions: well separated

Measurement: precise

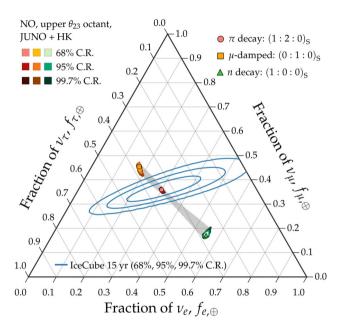


Allowed regions: overlapping Measurement: imprecise

Fraction of ν_e , $f_{e,\oplus}$

Not ideal

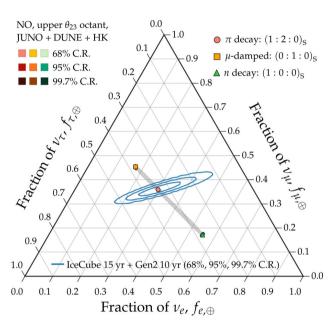
2030



Allowed regions: well separated Measurement: improving

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2040

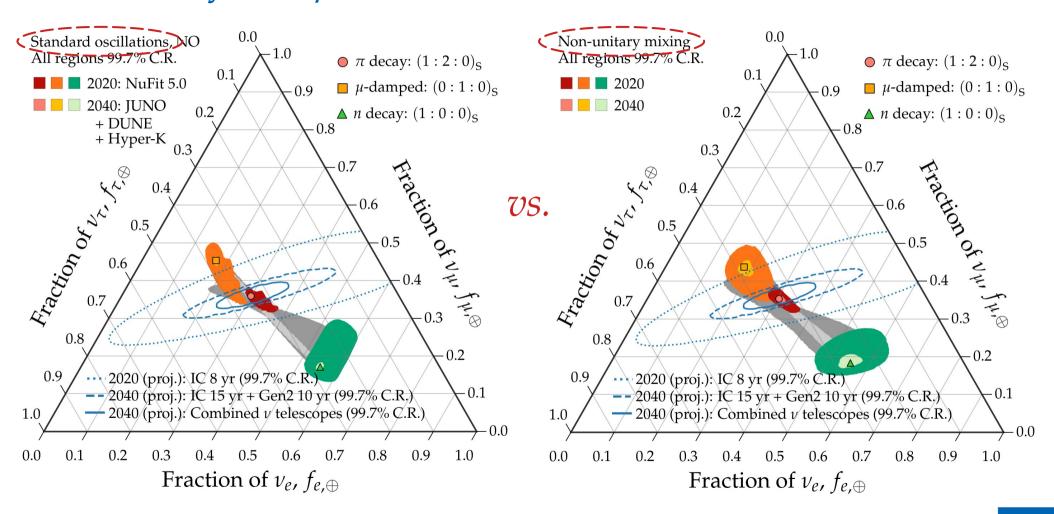


Allowed regions: well separated

Measurement: precise

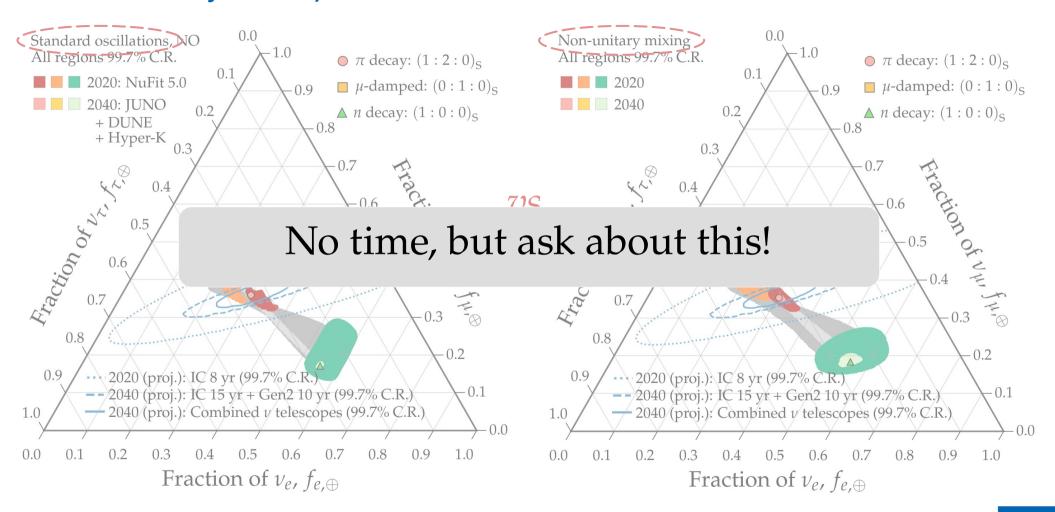
Success

No unitarity? *No problem*

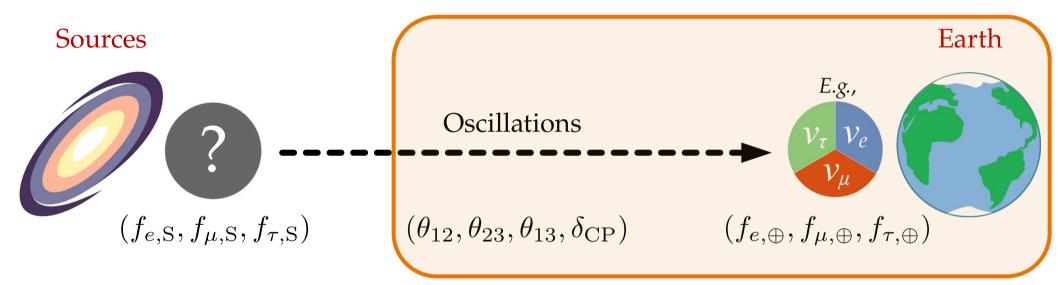


Song, Li, Argüelles, MB, Vincent, JCAP 2021

No unitarity? No problem



Song, Li, Argüelles, MB, Vincent, JCAP 2021

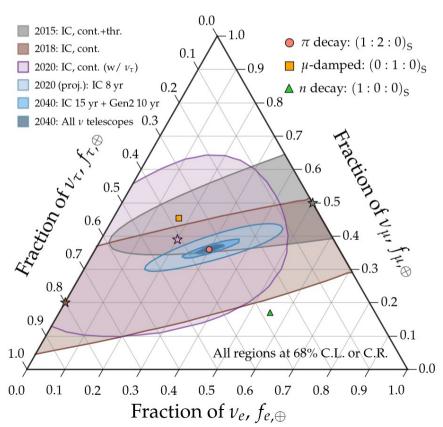


From Earth to sources: we let the data teach us about $f_{\alpha,S}$

Ingredient #1:

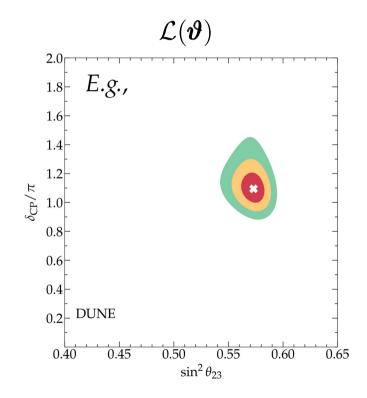
Flavor ratios measured at Earth,

$$(f_{e,\oplus},f_{\mu,\oplus},f_{\tau,\oplus})$$



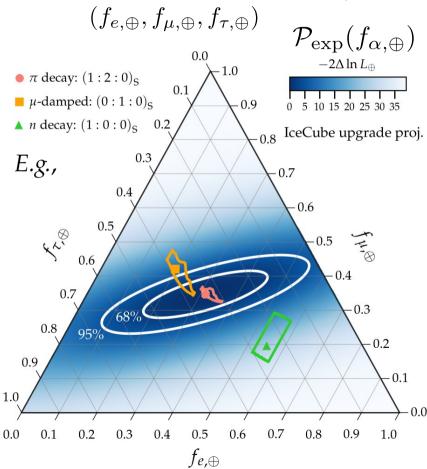
Ingredient #2:

Probability density of mixing parameters (θ_{12} , θ_{23} , θ_{13} , δ_{CP})



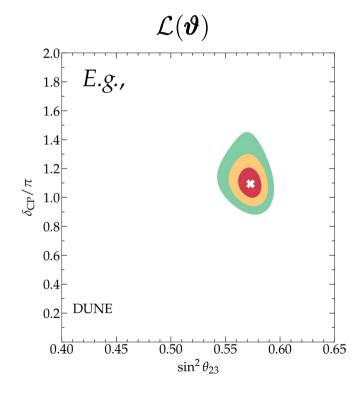
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Flavor ratios measured at Earth,



Ingredient #2:

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Ingredient #1:

Flavor ratios measured at Earth, $(f_{e,\oplus},f_{\mu,\oplus},f_{ au,\oplus})$

Ingredient #2:

Probability density of mixing parameters (θ_{12} , θ_{23} , θ_{13} , δ_{CP})

Posterior probability of $f_{\alpha,S}$ [MB & Ahlers, PRL 2019]:

$$\mathcal{P}(m{f}_s) = \int dm{artheta} \mathcal{L}(m{artheta}) \mathcal{P}_{
m exp}(m{f}_{\oplus}(m{f}_{
m S},m{artheta}))$$

Ingredient #1:

Flavor ratios measured at Earth, $(f_{e,\oplus},f_{\mu,\oplus},f_{ au,\oplus})$

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Posterior probability of $f_{\alpha,S}$ [MB & Ahlers, PRL 2019]:

$$\mathcal{P}(\boldsymbol{f}_s) = \int d\boldsymbol{\vartheta} \mathcal{L}(\boldsymbol{\vartheta}) \mathcal{P}_{\mathrm{exp}}(\boldsymbol{f}_{\oplus}(\boldsymbol{f}_{\mathrm{S}}, \boldsymbol{\vartheta}))$$

Oscillation experiments Neutrino telescopes

Ingredient #1:

Flavor ratios measured at Earth. $(f_{e,\oplus},f_{\mu,\oplus},f_{\tau,\oplus})$

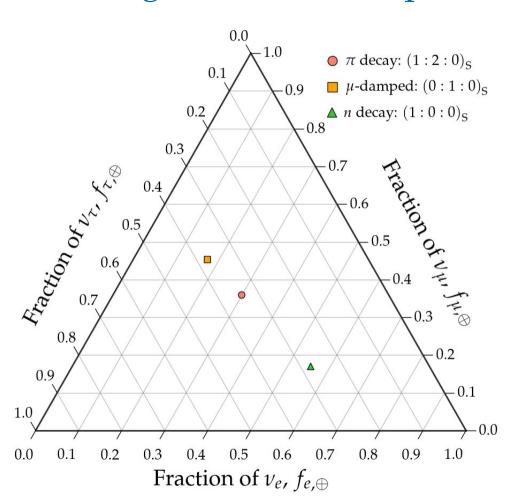
Ingredient #2:

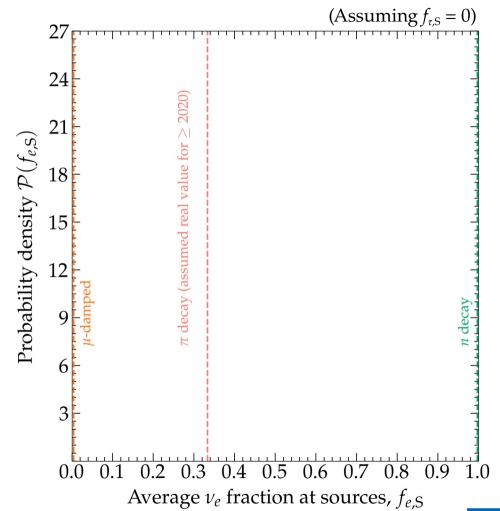
Probability density of mixing parameters $(\theta_{12}, \theta_{23}, \theta_{13}, \delta_{CP})$

Posterior probability of $f_{\alpha,S}$ [MB & Ahlers, PRL 2019]:

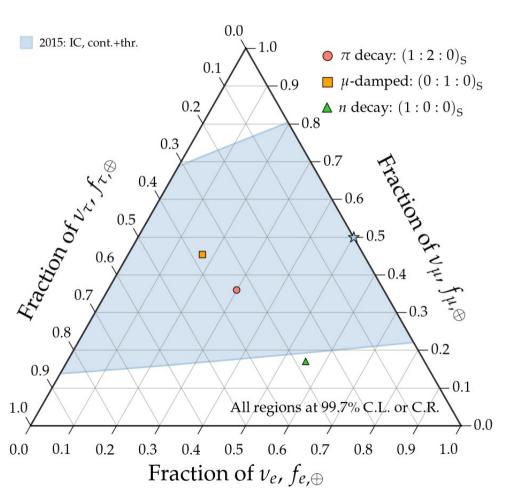
$$f_{lpha,\oplus} = \sum_{eta=e,\mu, au} P_{eta olpha} f_{eta,\mathrm{S}}$$
 $\mathcal{P}(oldsymbol{f}_s) = \int doldsymbol{artheta} \mathcal{L}(oldsymbol{artheta}) \mathcal{P}_{\mathrm{exp}}(oldsymbol{f}_\oplus(oldsymbol{f}_\mathrm{S},oldsymbol{artheta}))$

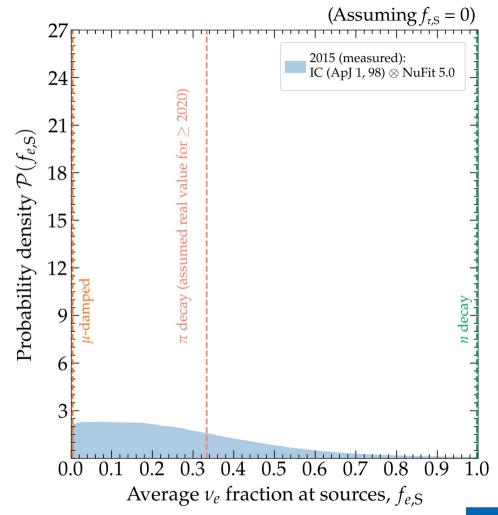
Oscillation experiments Neutrino telescopes

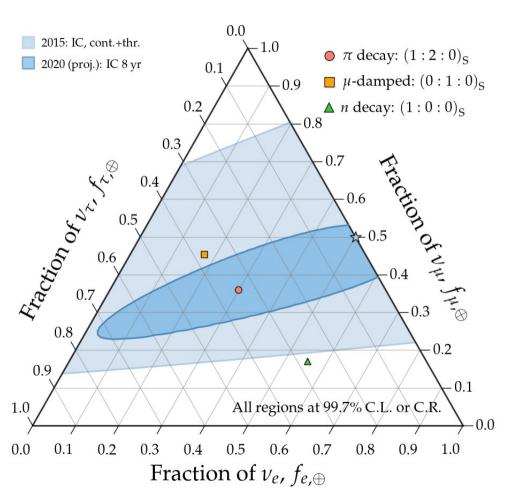


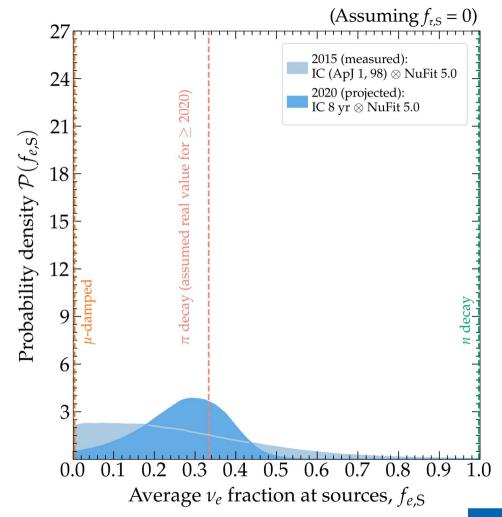


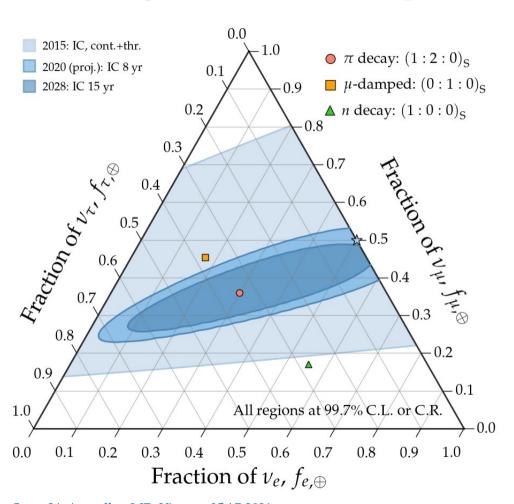
Song, Li, Argüelles, **MB**, Vincent, *JCAP* 2021 **MB** & Ahlers, *PRL* 2019

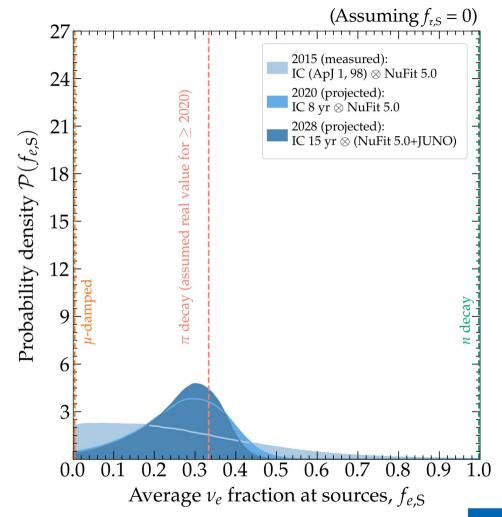


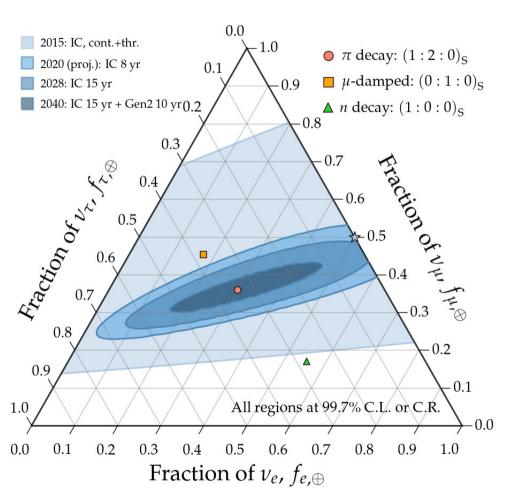


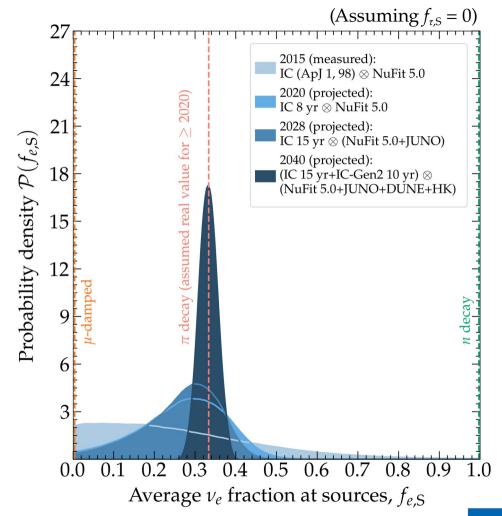




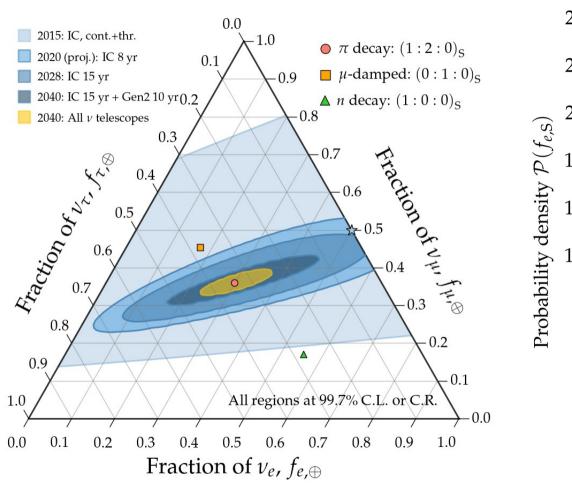


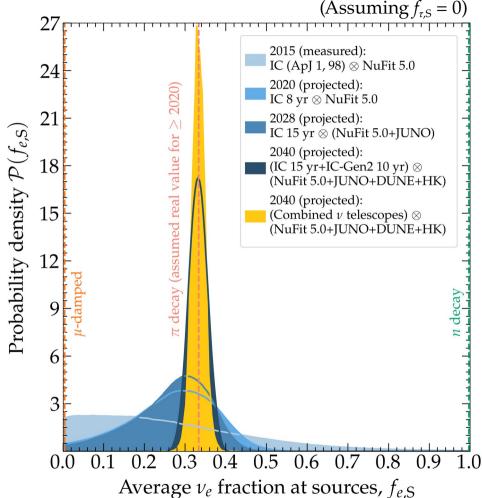






Inferring the flavor composition at the sources



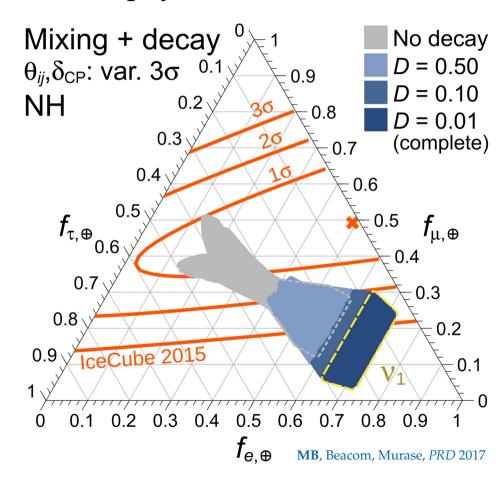


Repurpose the flavor sensitivity to test new physics:

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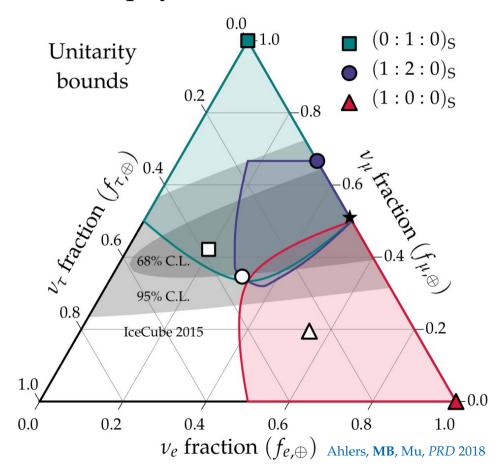


Reviews:

Mehta & Winter, JCAP 2011; Rasmussen et al., PRD 2017

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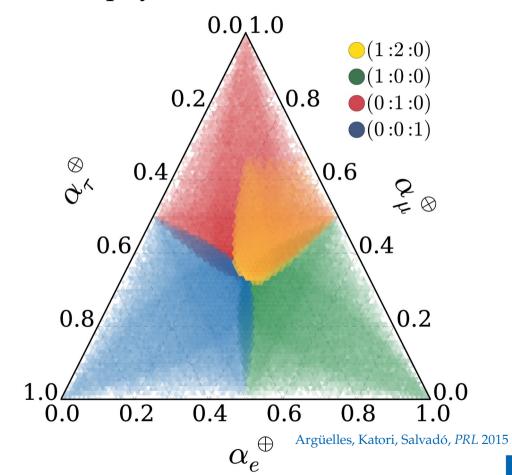


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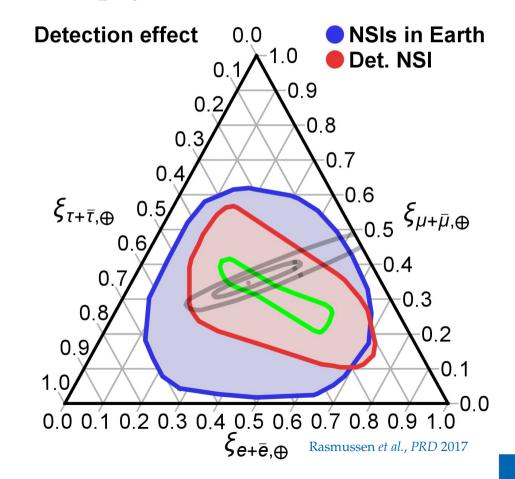
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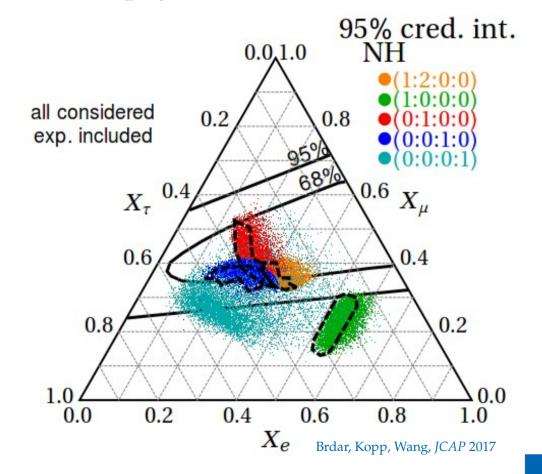
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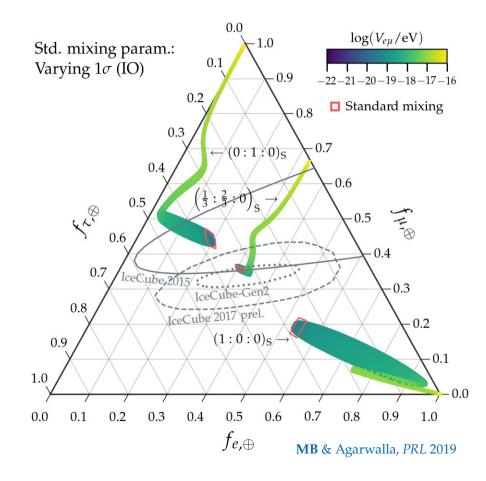
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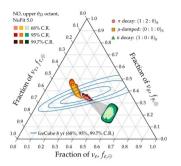
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► Long-range *ev* interactions [MB & Agarwalla, *PRL* 2019]

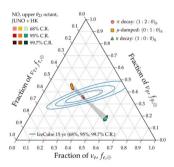
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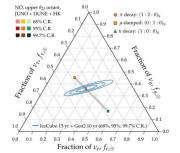
The high-energy flavor charter



Today: Allowed flavor regions at Earth large, imprecise flavor measurements



2030: Allowed flavor regions shrunk, thanks to JUNO + Hyper-K + DUNE

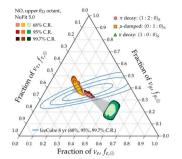


2040: Allowed flavor regions shrunk + precise flavor measurements

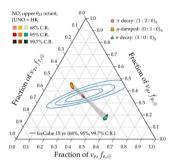
Opportunities for astrophysics and particle physics exist throughout!

The high-energy flavor charter

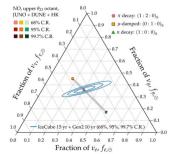
See PLEvM for what we can do for other observables by combining future detectors: 2107.13534



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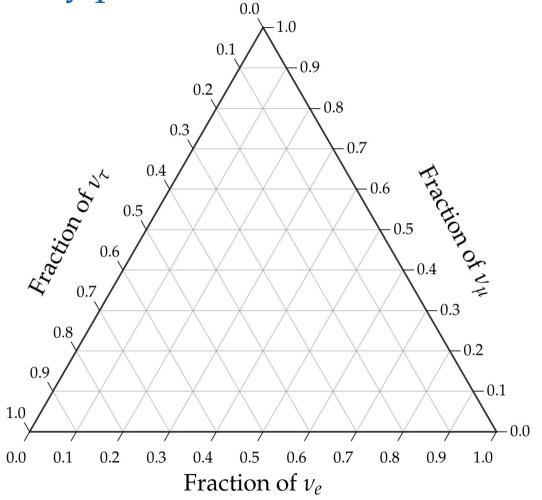
Opportunities for astrophysics and particle physics exist throughout!

Backup slides

Assumes underlying unitarity – sum of projections on each axis is 1

How to read it:

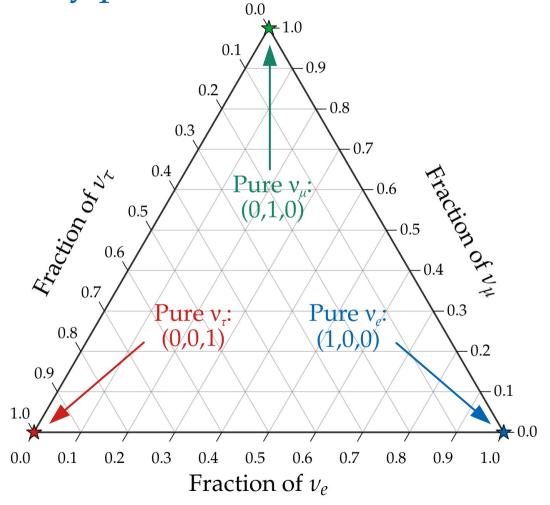
Follow the tilt of the tick marks



Assumes underlying unitarity – sum of projections on each axis is 1

How to read it:

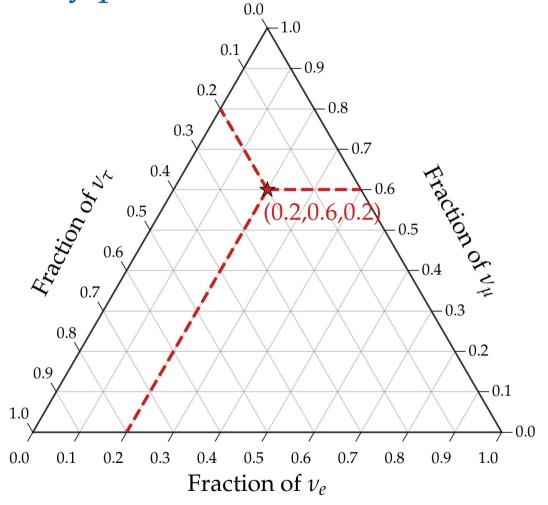
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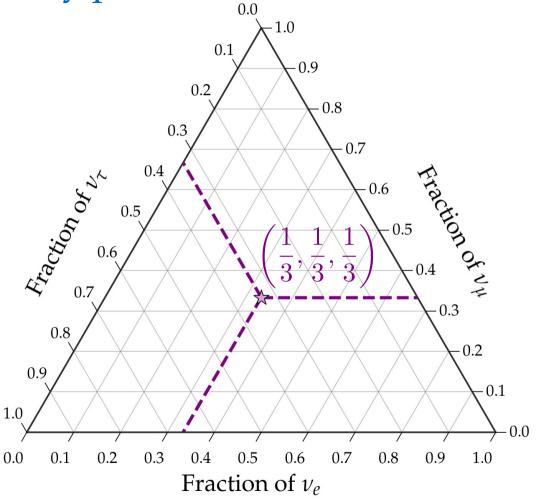
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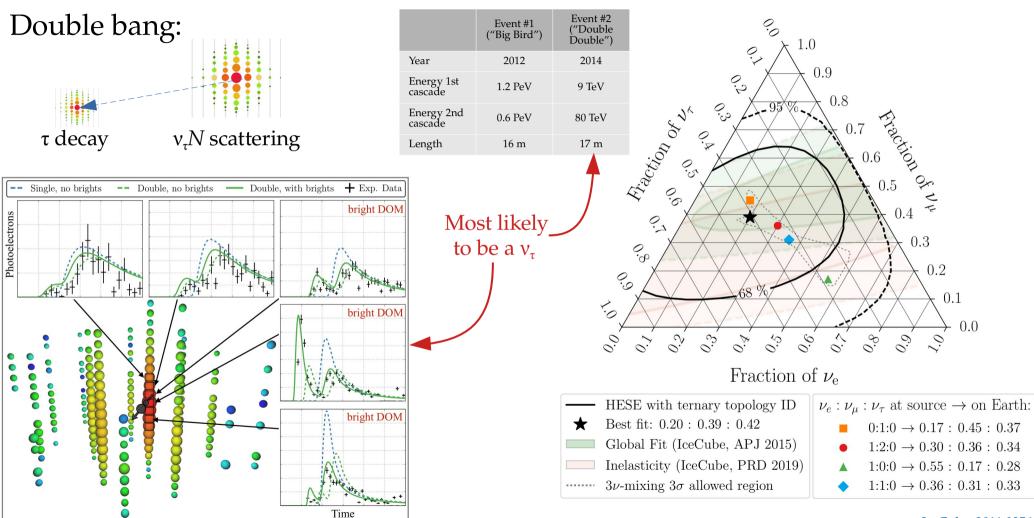
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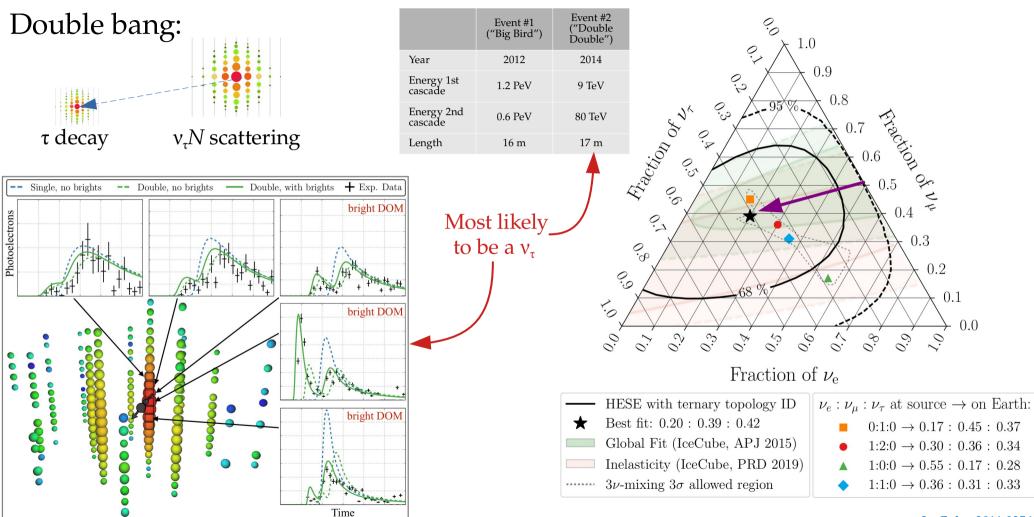
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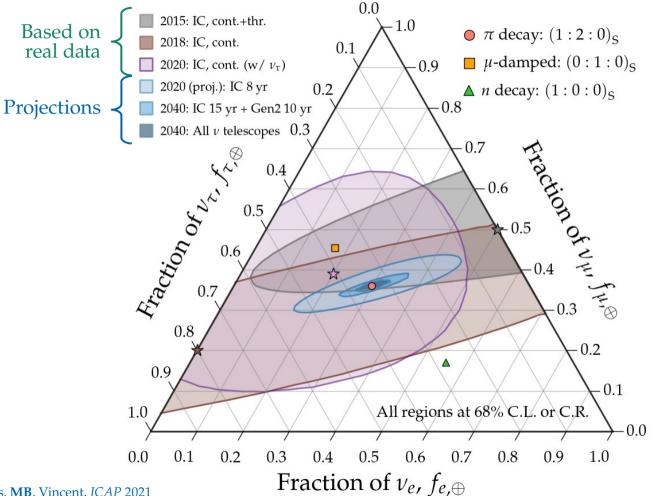
New (IC 7.5 yr): First identified high-energy astrophysical v_{τ}



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Measuring flavor composition: 2015–2040



Status today:

Measurements are compatible with standard expectations (but errors are large!)

Projections:

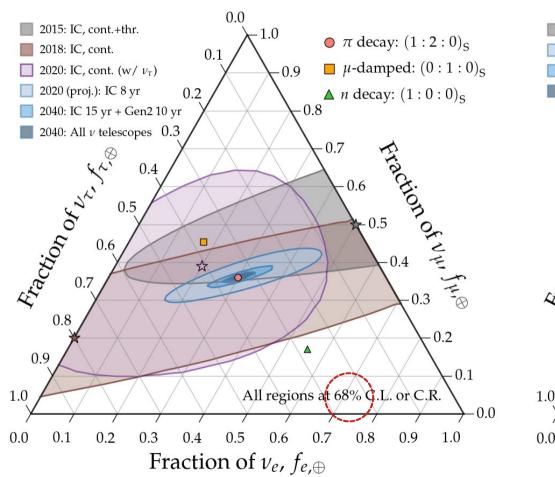
Near future (~2020):

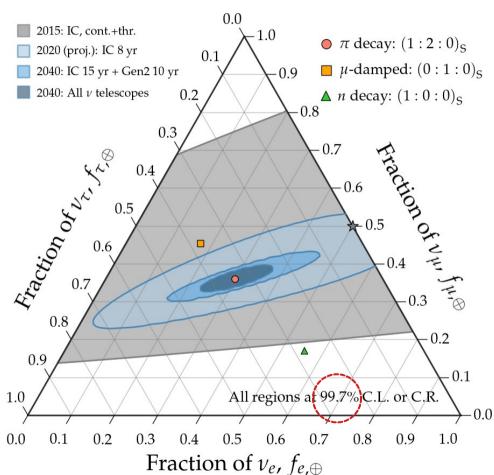
× 5 reduction using 8 yr of IC contained + thru.

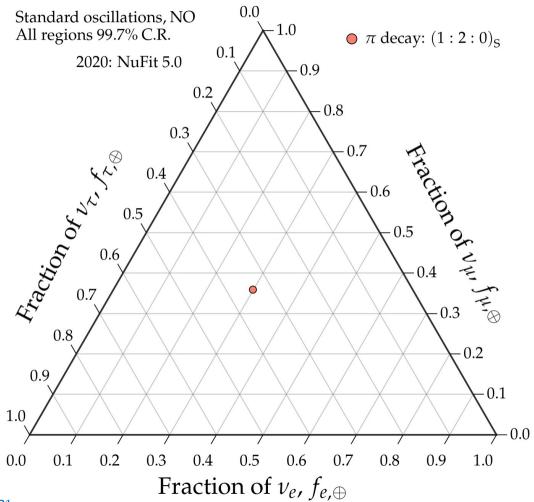
Coming up (~2040):

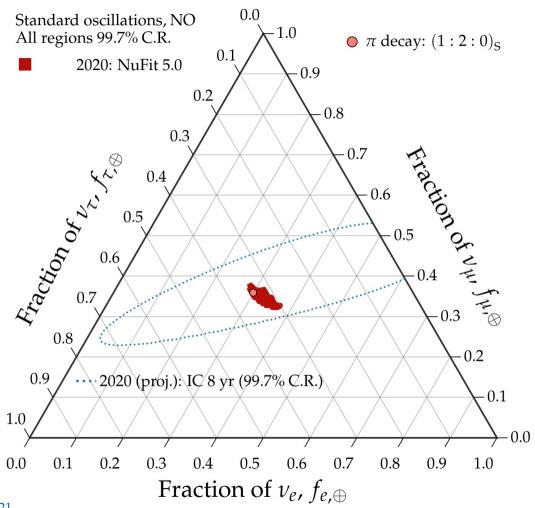
× 10 reduction using Gen2 and all v telescopes

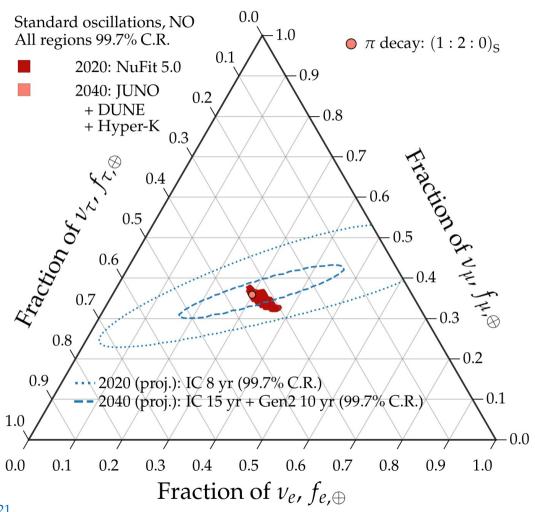
Measuring flavor composition: 2015–2040



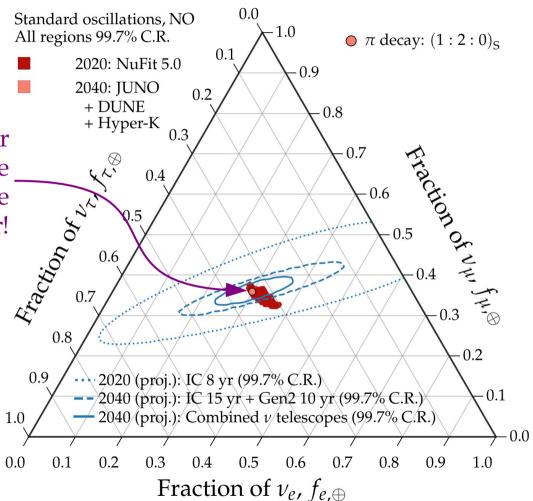


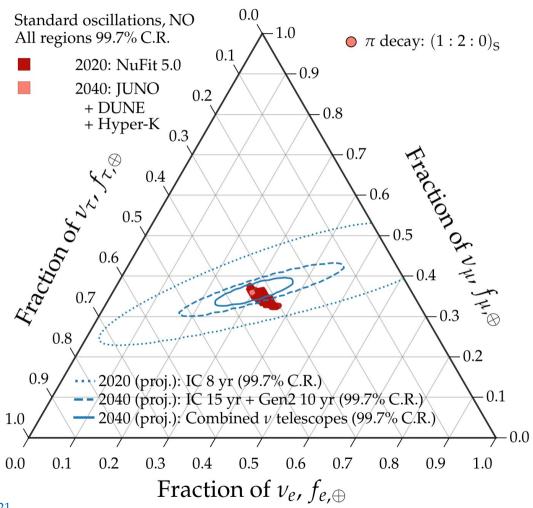


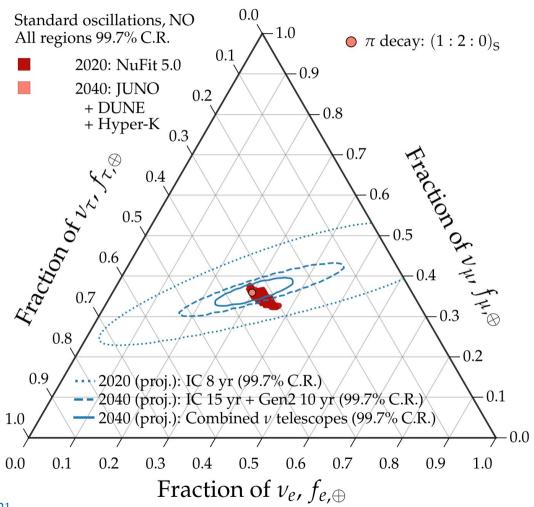


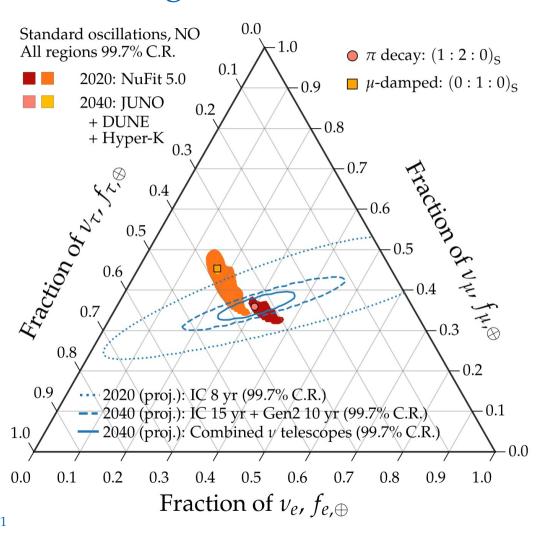


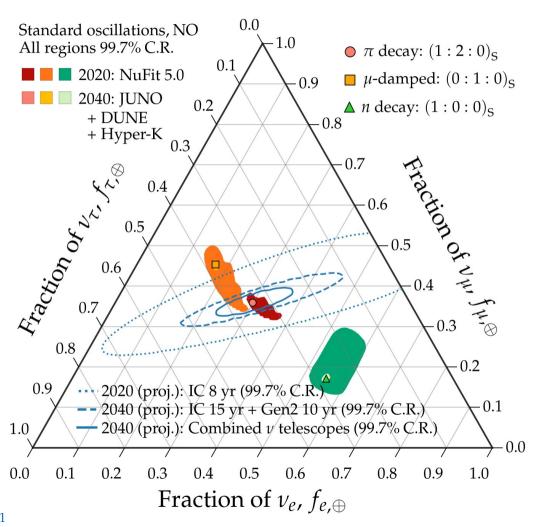
The allowed flavor region in 2040 is the same size as the best-fit point marker!

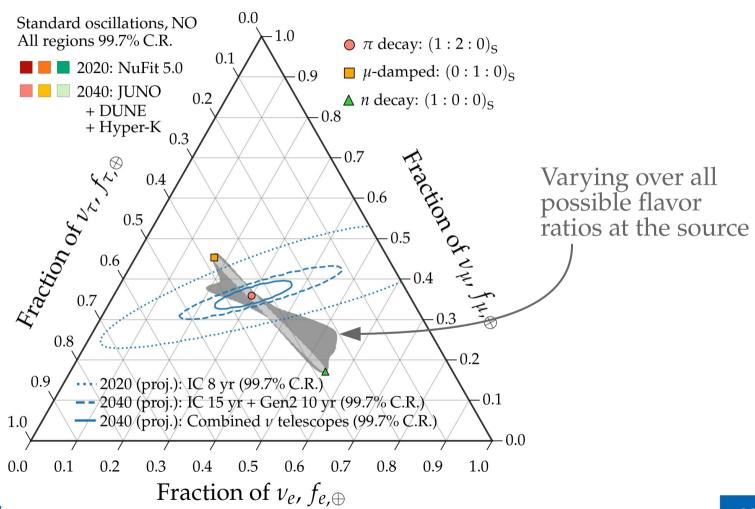


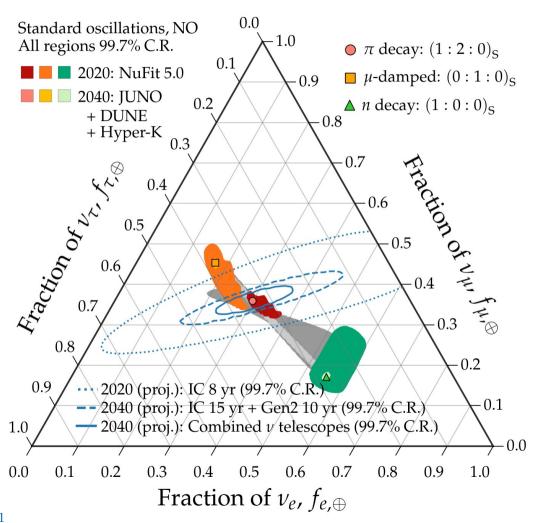


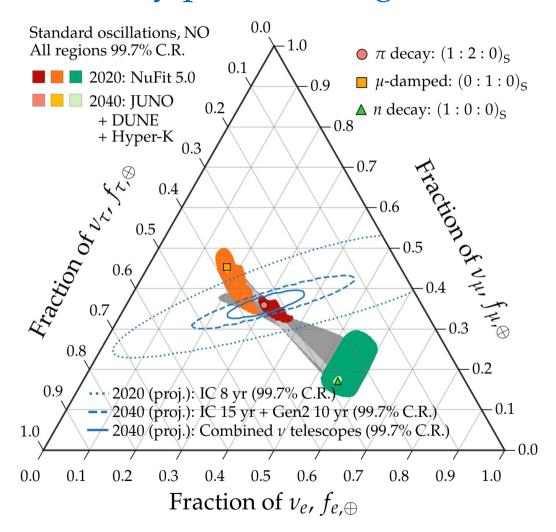












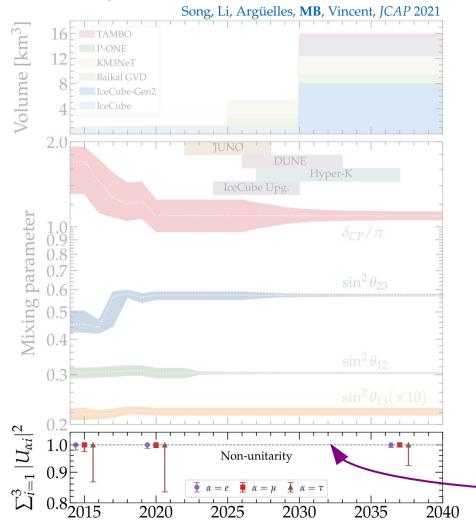
By 2040:

Theory –

Mixing parameters known precisely: allowed flavor regions are *almost* points (already by 2030)

Measurement of flavor ratios – Can distinguish between similar predictions at 99.7% C.R. (3σ)

Can finally use the full power of flavor composition for astrophysics and neutrino physics



The 3×3 active mixing matrix is a non-unitary sub-matrix of a bigger one:

Active flavors

$$U = \begin{pmatrix} U_{e1} & U_{e2} & U_{e3} & \cdots \\ U_{\mu 1} & U_{\mu 2} & U_{\mu 3} & \cdots \\ U_{\tau 1} & U_{\tau 2} & U_{\tau 3} & \cdots \\ & & \ddots & & \ddots \end{pmatrix}$$

Additional sterile flavors

The elements $|U_{\alpha i}|^2$ for active flavors can be measured *without* assuming unitarity

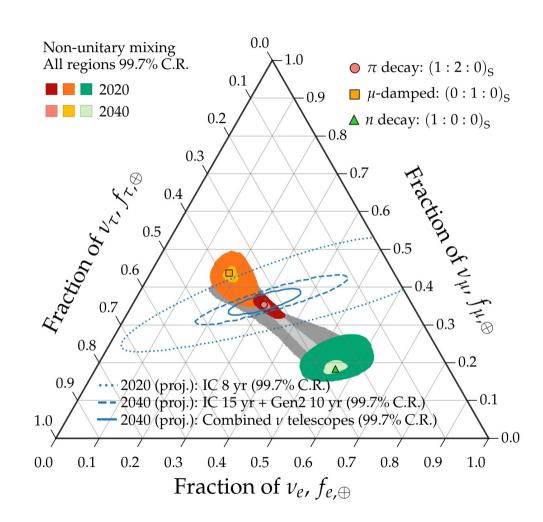
Because the sub-matrix is not-unitary $(U_{3\nu}^{\dagger}U_{3\nu}\neq 1)$, the "row sum" may be ≤ 1

Flavor ratios at Earth:

$$f_{\alpha,\oplus} = \sum_{\beta=e,\mu,\tau} P_{\beta\alpha} f_{\beta,S}$$

Same as for standard oscillations...

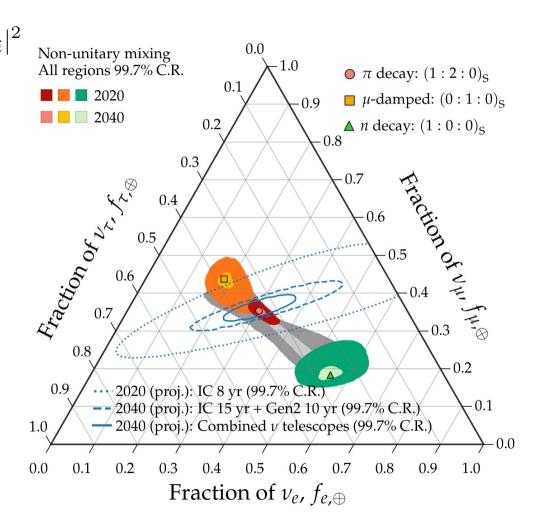
... but the probability is computed directly using the values of the $|U_{\alpha i}|^2$ (instead of the mixing angles)



Flavor ratios at Earth:
$$P_{\beta\alpha} = \sum_{i=1,2,3} |U_{\alpha i}|^2 |U_{\beta i}|^2$$
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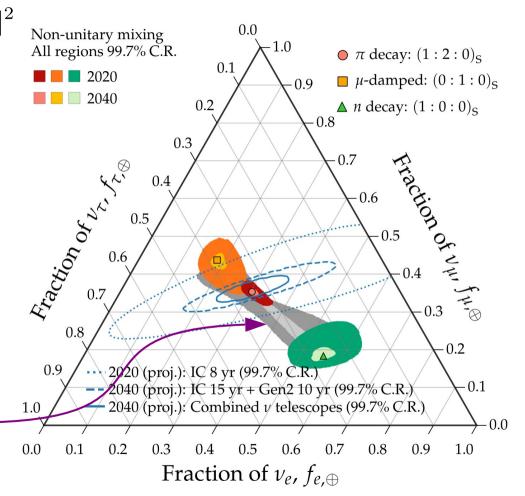


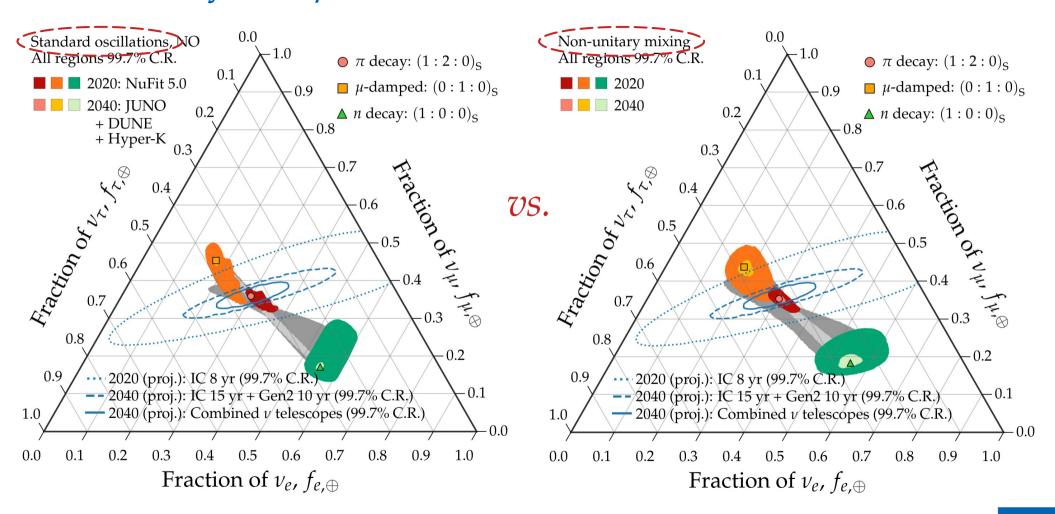
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The allowed flavor regions are bigger, but *not much bigger*!





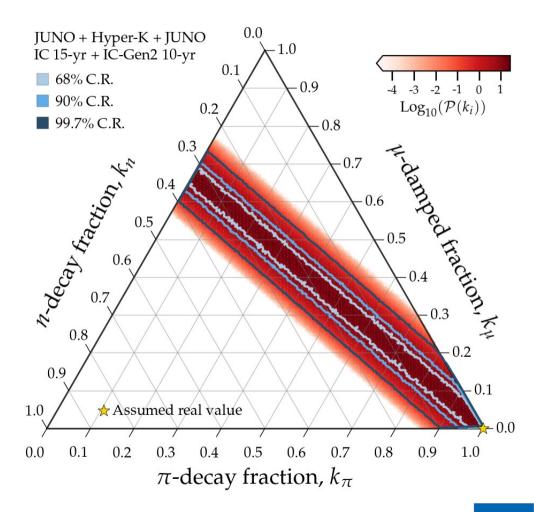
27

Song, Li, Argüelles, MB, Vincent, JCAP 2021

Can we detect the contribution of multiple v production mechanisms?

$$m{f}_{
m S}=k_{\pi}m{f}_{
m S}^{\pi}+k_{\mu}m{f}_{
m S}^{\mu}+k_{n}m{f}_{
m S}^{n}$$
 π decay: μ damped: n decay: $(1/3,2/3,0)$ $(0,1,0)$ $(1,0,0)$ Propagate to Earth $m{f}_{\oplus}$

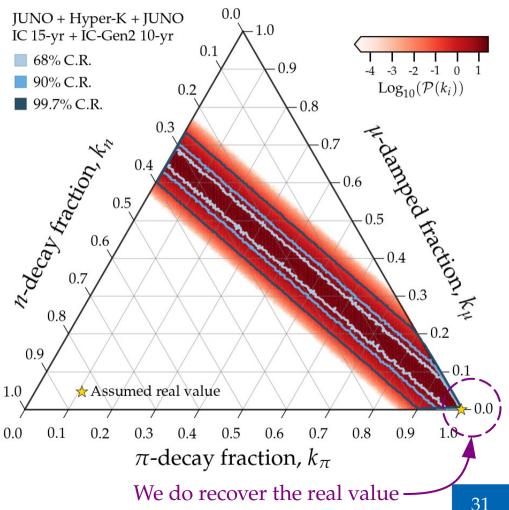
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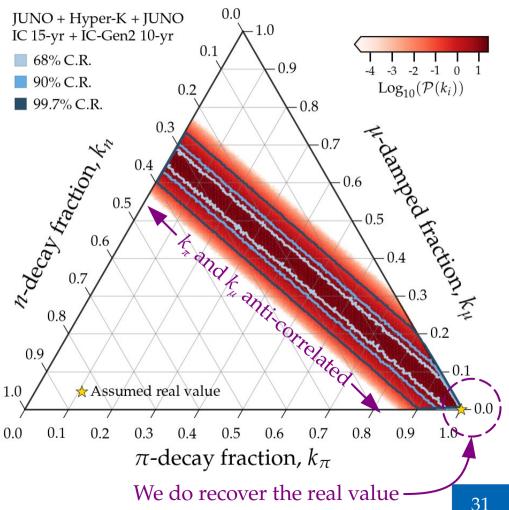
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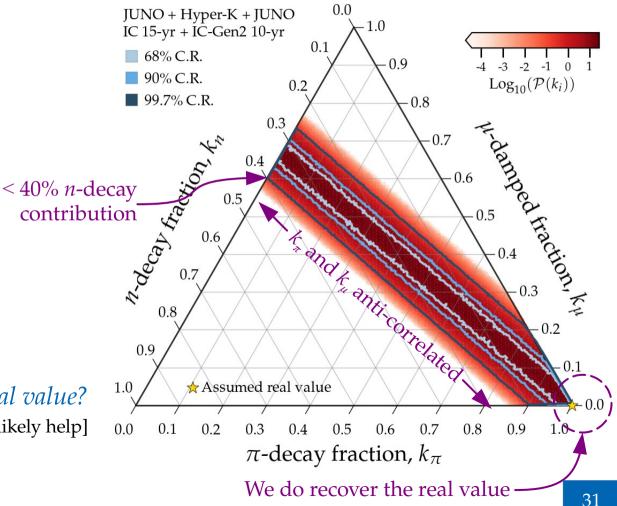
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Propagate to Earth $m{f}_{\oplus}$

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By 2040, how well will we recover the real value?

[Adding spectrum information (not shown) will likely help]



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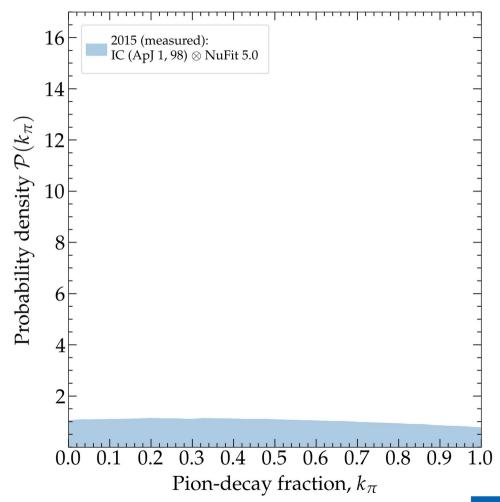
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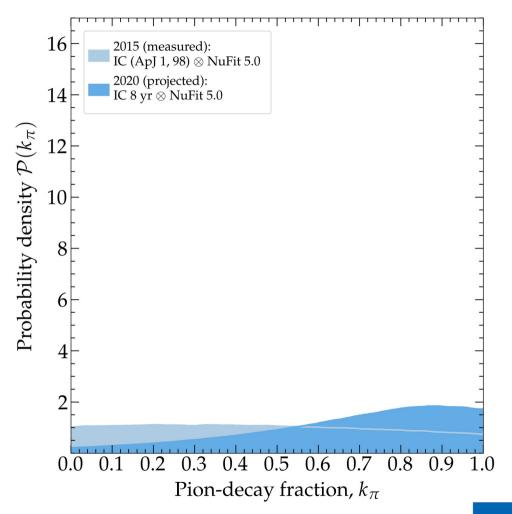
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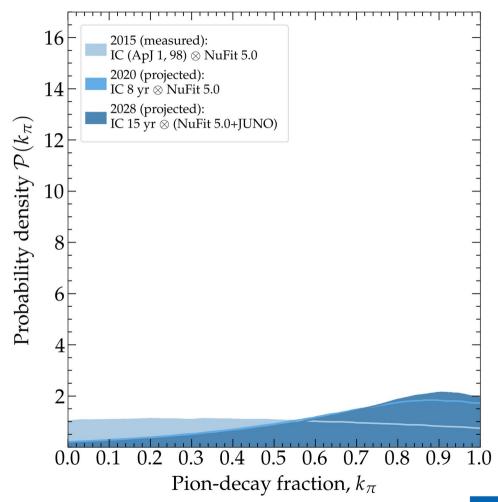
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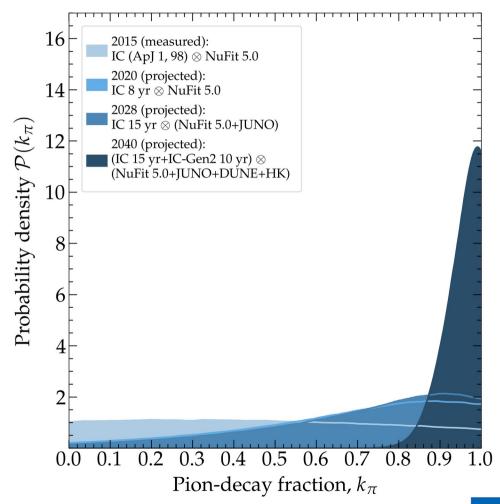
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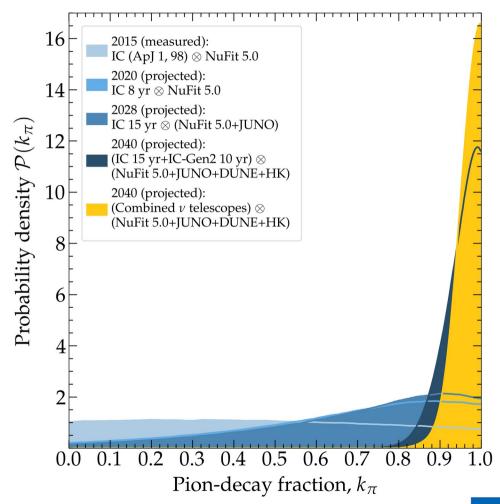
Assume real value $k_{\pi} = 1$ ($k_{\mu} = k_{n} = 0$)



Can we detect the contribution of multiple v production mechanisms?

$$m{f}_{
m S}=k_{\pi}m{f}_{
m S}^{\pi}+k_{\mu}m{f}_{
m S}^{\mu}+k_{n}m{f}_{
m S}^{n}$$
 π decay: μ damped: n decay: $(1/3,2/3,0)$ $(0,1,0)$ $(1,0,0)$ Propagate to Earth

Assume real value $k_{\pi} = 1$ ($k_{\mu} = k_{n} = 0$)



If sources have strong magnetic fields, charged particles cool via synchrotron:

$$p + \gamma(p) \to \pi^+ \to \mu^+ + \nu_{\mu}$$

$$\downarrow \bar{\nu}_{\mu} + e^+ + \nu_{e}$$

If sources have strong magnetic fields, charged particles cool via synchrotron:

Proton cooling

Induce a high-energy cut-off in the emitted v spectrum:

$$E_{\nu}^{\prime 2} \frac{dN_{\nu}}{dE_{\nu}^{\prime}} \propto E_{\nu}^{\prime 2 - \alpha_{\nu}} e^{-E_{\nu}^{\prime}/E_{\nu}^{\prime \max}}$$

$$E_{\nu}^{\max} \approx \frac{10^{10} \Gamma \text{ GeV}}{\sqrt{B^{\prime}/G}} \qquad (p + \gamma(p) \rightarrow \pi^{+} \rightarrow \mu^{+} + \nu_{\mu} \rightarrow \bar{\nu}_{\mu} + e^{+} + \nu_{e}$$

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Muon cooling

Change flavor composition:

$$(f_{e,S}, f_{\mu,S}, f_{\tau,S}) = \begin{cases} (\frac{1}{3}, \frac{2}{3}, 0), & \text{if } E_{\nu} < E_{\nu,\mu}^{\text{sync}} \\ (0, 1, 0), & \text{if } E_{\nu} \ge E_{\nu,\mu}^{\text{sync}} \end{cases}$$

$$E_{\nu,\mu}^{\text{sync}} \approx 10^{9} \Gamma \frac{G}{B'} \text{ GeV}$$

$$\downarrow \bar{\nu}_{\mu} + e^{+} + \nu_{e}$$

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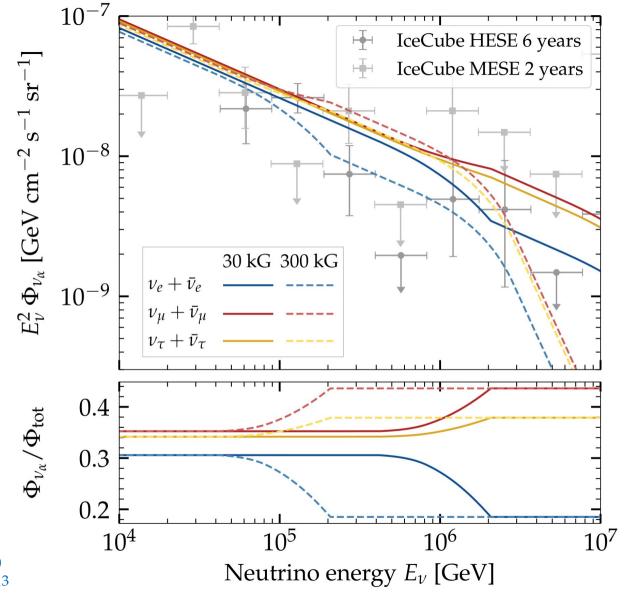
$$E_{\nu,\mu}^{\rm sync} \approx 10^9 \Gamma \frac{\rm G}{B'} \,\, {\rm GeV}$$

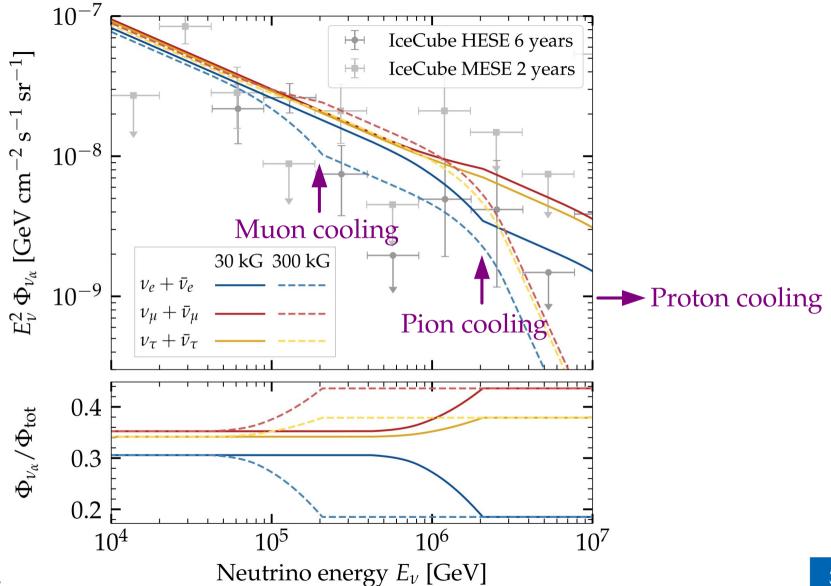
$$(p + \gamma(p) \rightarrow (\pi^{+}) \rightarrow (\mu^{+}) + \nu_{\mu}$$

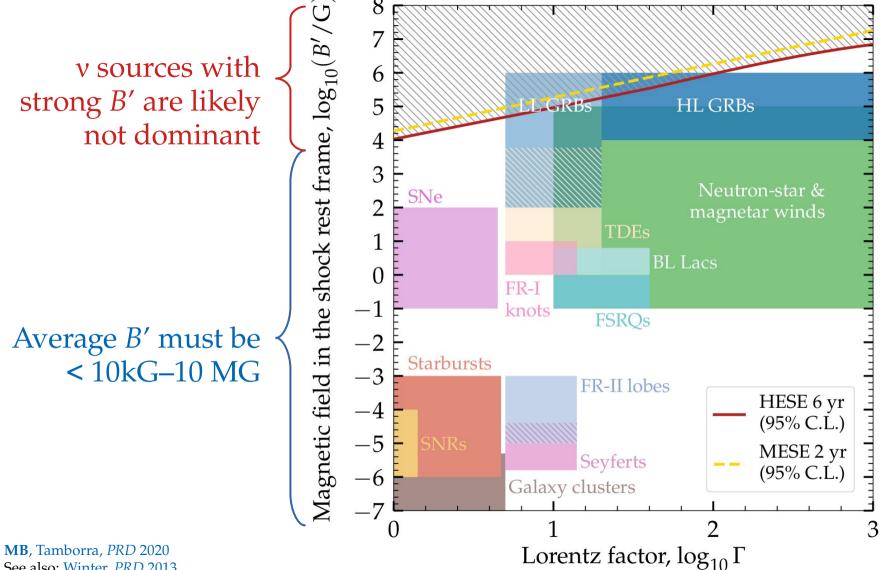
$$\downarrow \bar{\nu}_{\mu} + e^{+} + \nu_{e}$$

$$\begin{array}{l} \textbf{Pion cooling} \\ \textbf{Steepen the v spectrum:} \ \alpha_{\nu} = \left\{ \begin{matrix} \gamma, & \text{if} \ E_{\nu} < E_{\nu,\pi}^{\mathrm{sync}} \\ \gamma+2, & \text{if} \ E_{\nu} \geq E_{\nu,\pi}^{\mathrm{sync}} \end{matrix} \right. \end{array}$$

$$E_{\nu,\pi}^{\rm sync} \approx 10^{10} \Gamma \frac{\rm G}{B'} \, {\rm GeV}$$

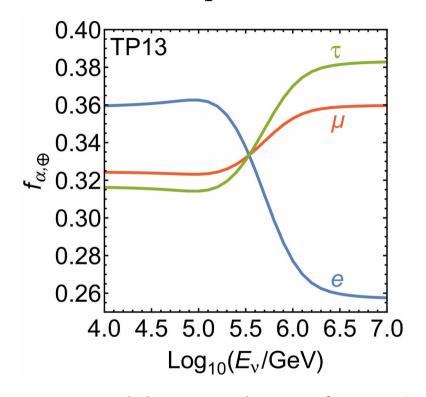


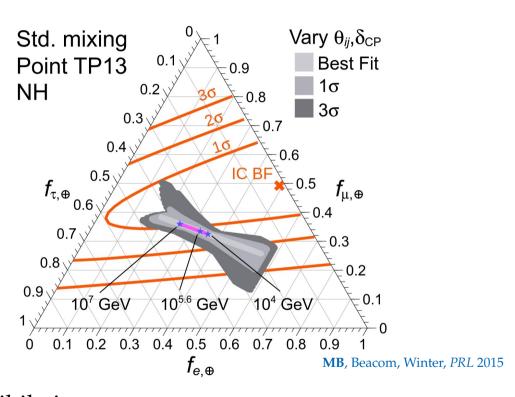




Energy dependence of the flavor composition?

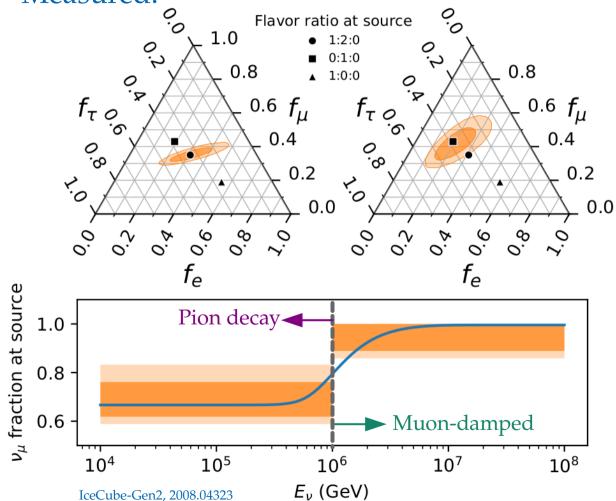
Different neutrino production channels accessible at different energies –

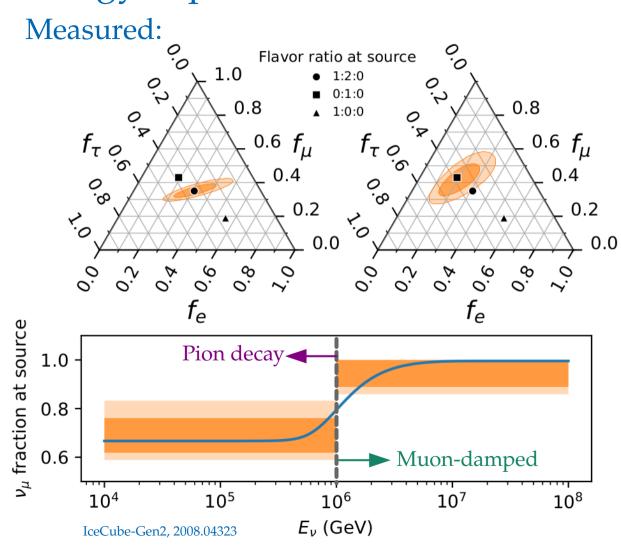




- ► TP13: p_Y model, target photons from e^-e^+ annihilation [Hümmer+, Astropart. Phys. 2010]
- ► Will be difficult to resolve [Kashti, Waxman, PRL 2005; Lipari, Lusignoli, Meloni, PRD 2007]

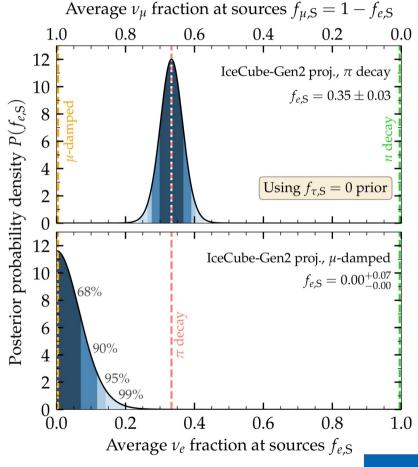
Measured:

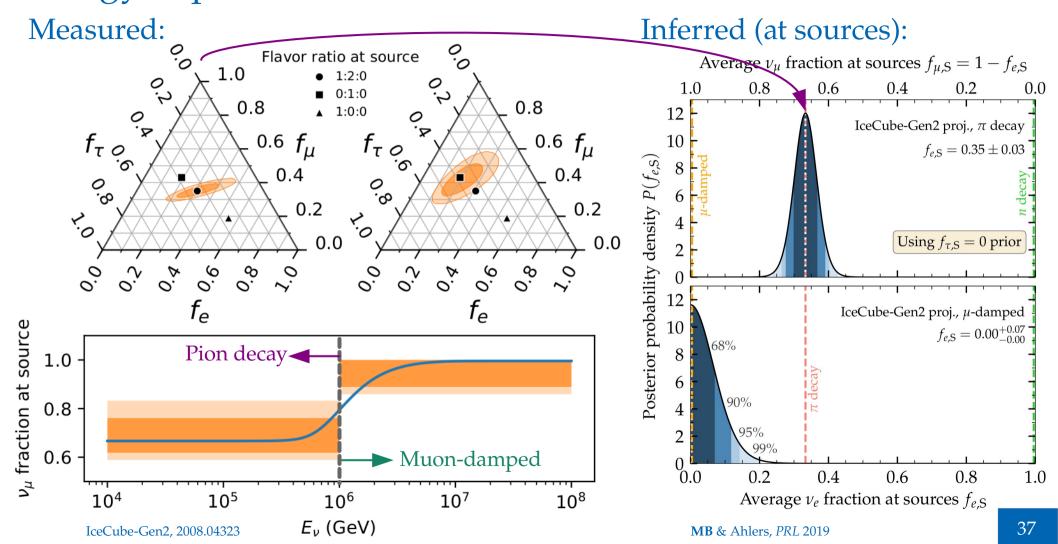


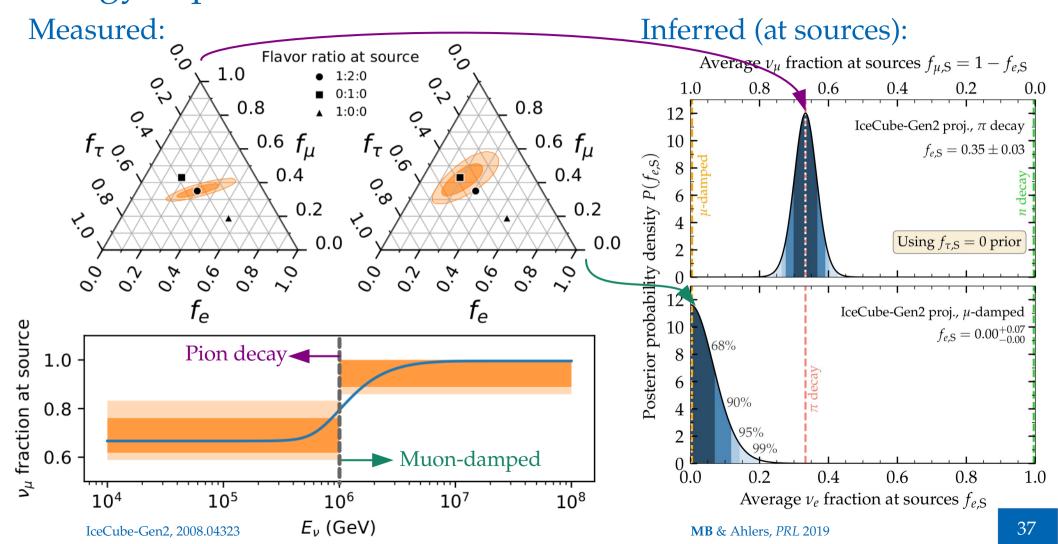


Inferred (at sources):

MB & Ahlers, PRL 2019

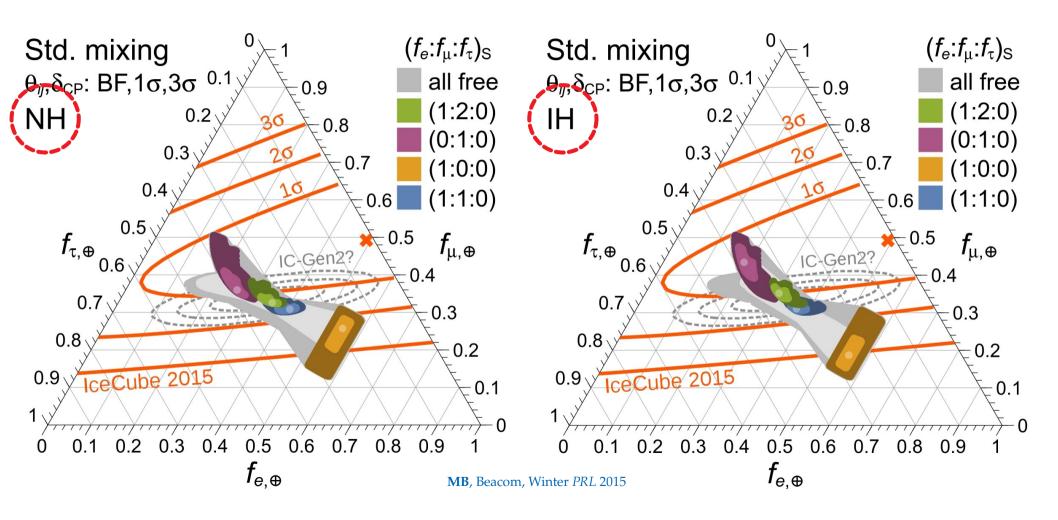


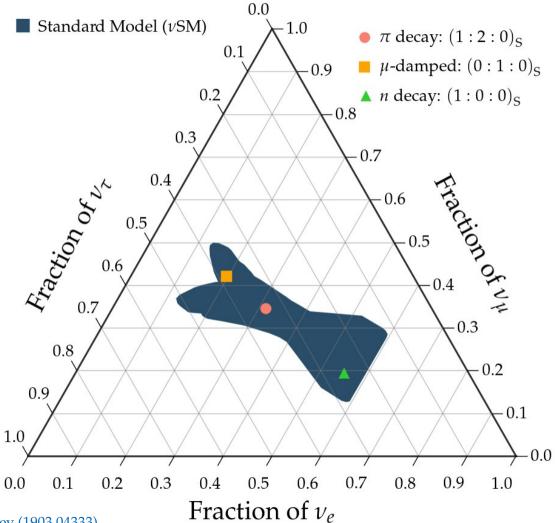


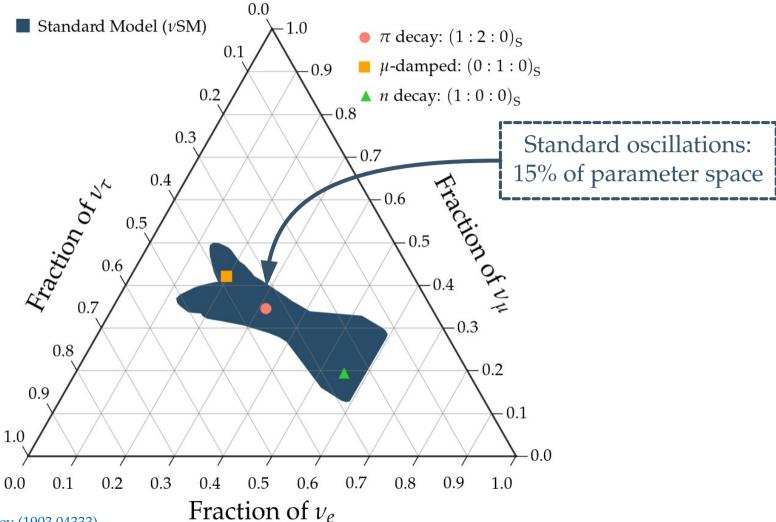


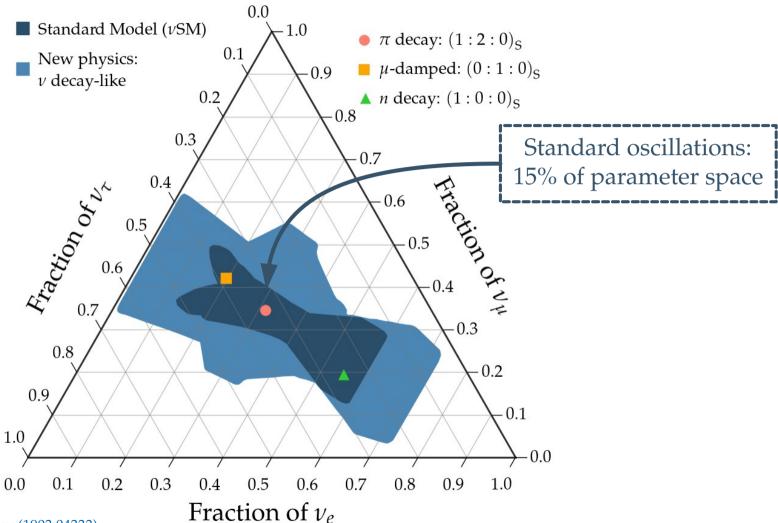
Flavor composition – a few source choices

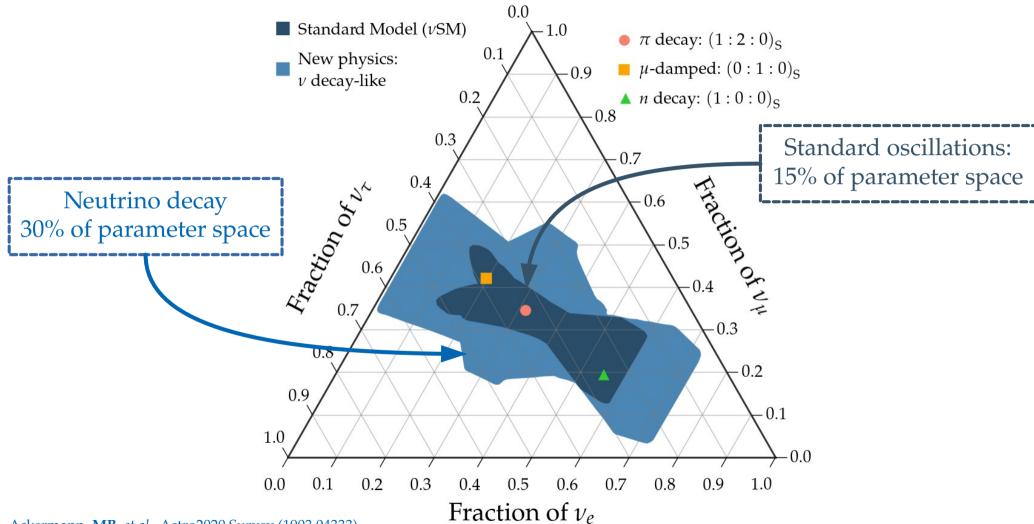
Flavor composition – a few source choices

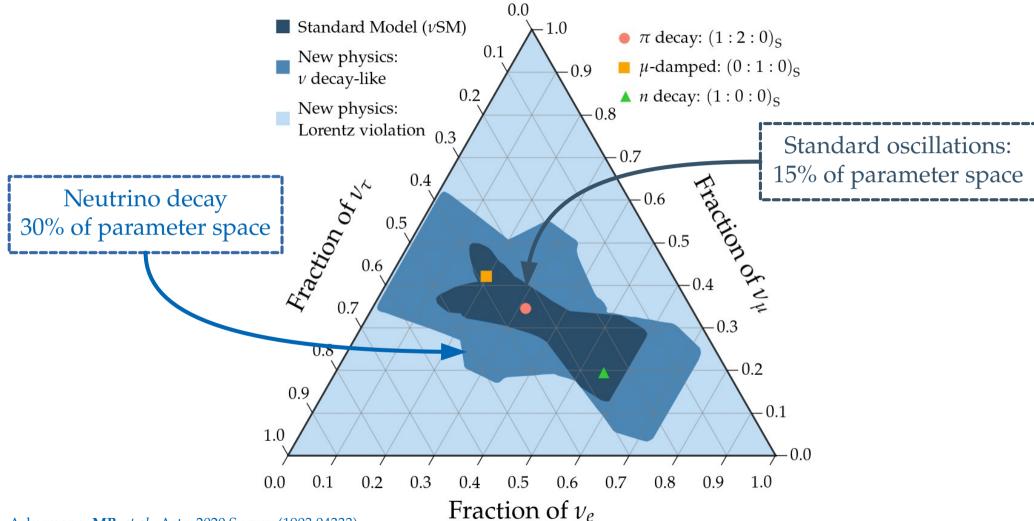


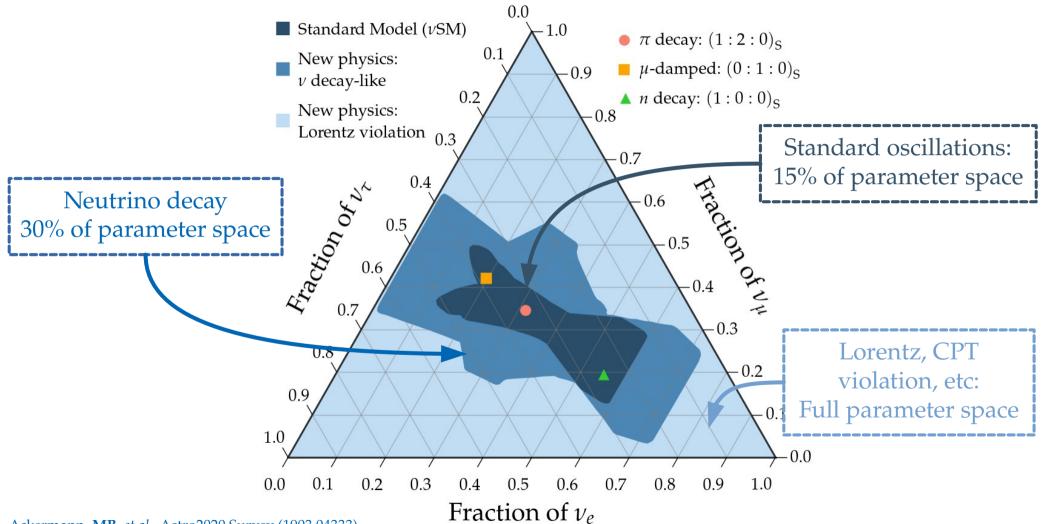


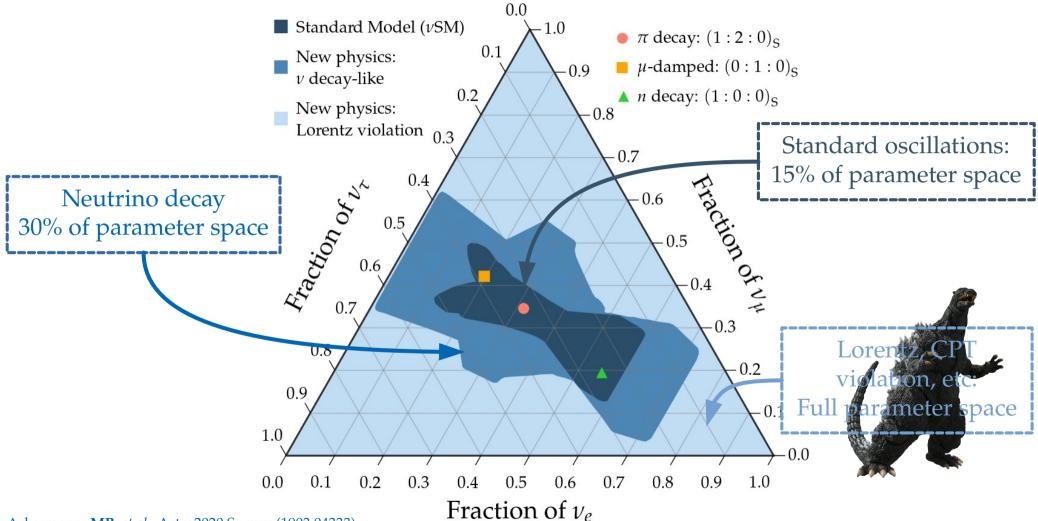






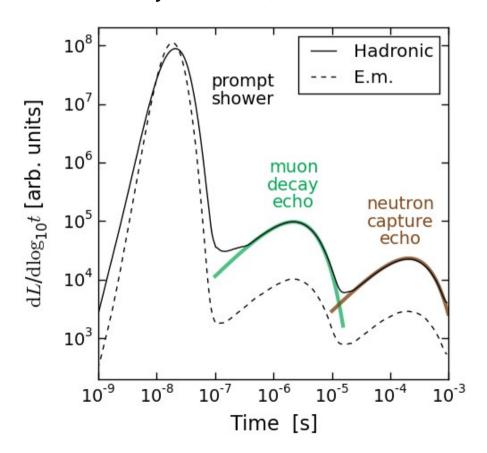


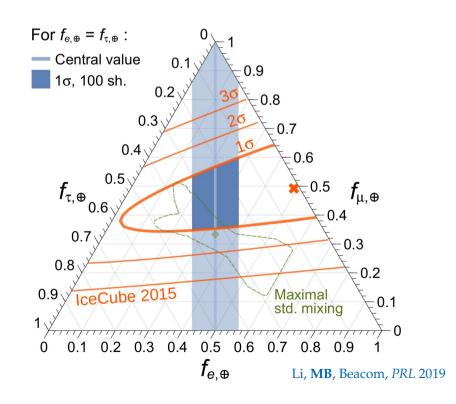




Side note: Improving flavor-tagging using echoes

Late-time light (*echoes*) from muon decays and neutron captures can separate showers made by v_e and v_τ –

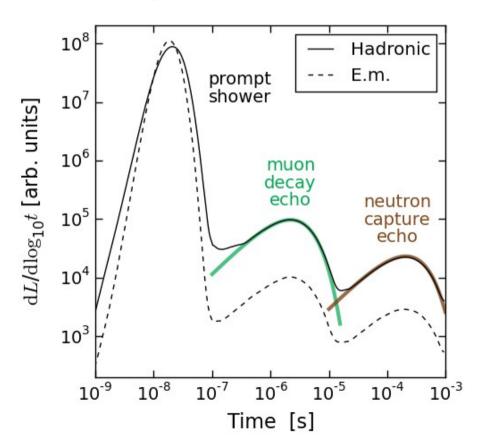


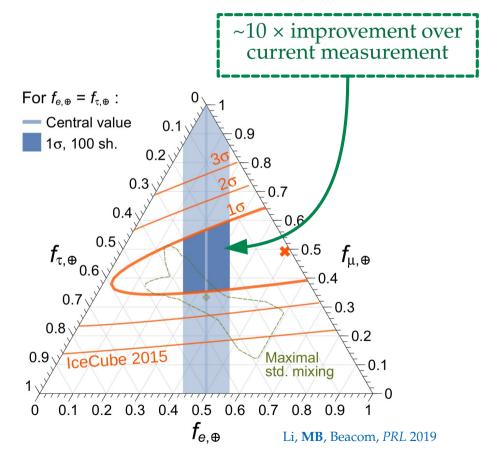


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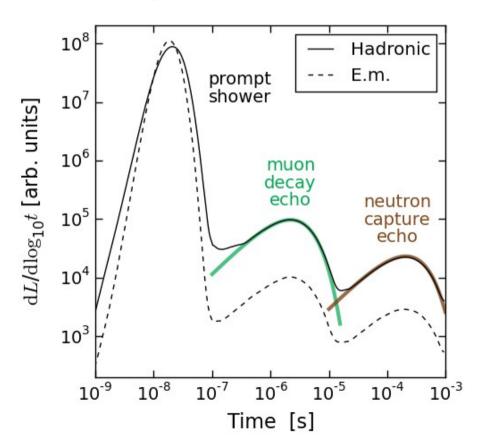


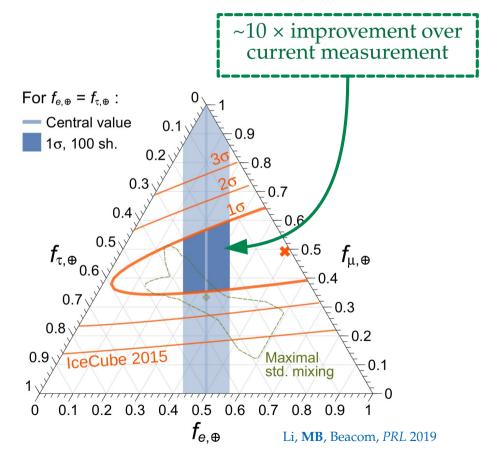


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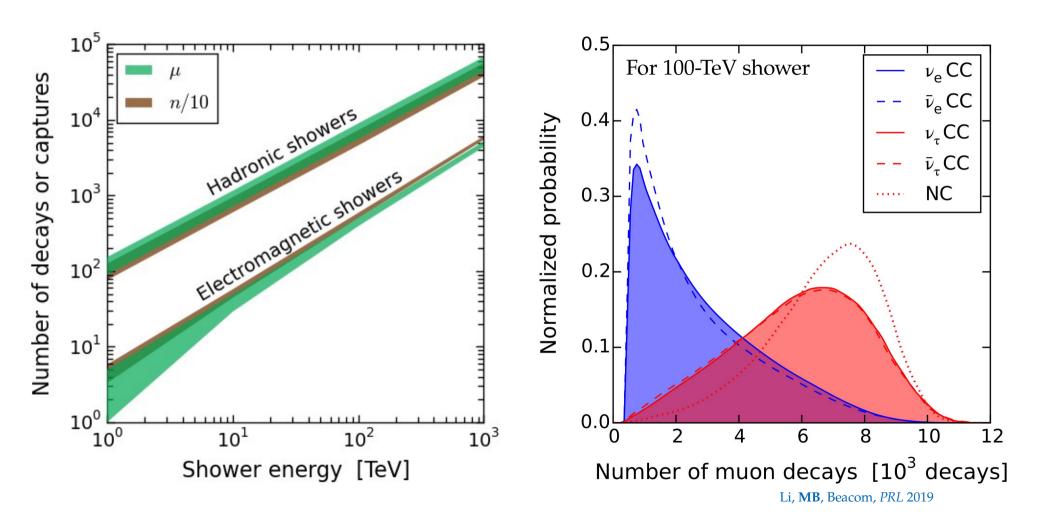
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Hadronic vs. electromagnetic showers

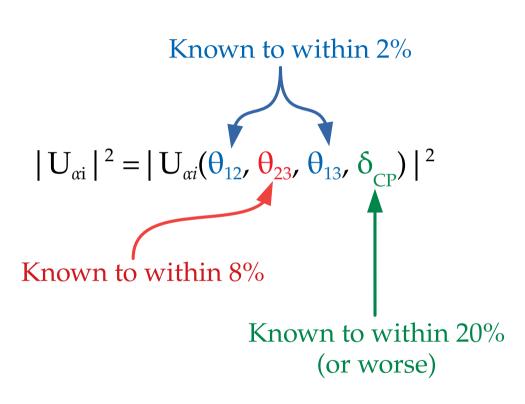


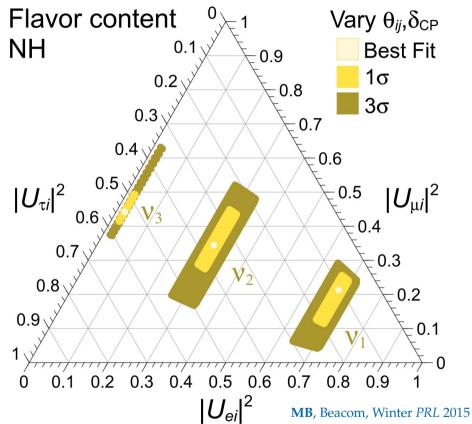
Are neutrinos forever?

- ▶ In the Standard Model (vSM), neutrinos are essentially stable ($\tau > 10^{36}$ yr):
 - ► One-photon decay $(v_i \rightarrow v_j + \gamma)$: $\tau > 10^{36} (m_i/\text{eV})^{-5} \text{ yr}$
 - Two-photon decay $(v_i \rightarrow v_j + \gamma)$: $\tau > 10^{-57} (m_i/\text{eV})^{-9} \text{ yr}$
 - ► Three-neutrino decay $(v_i \rightarrow v_j + v_k + \overline{v_k})$: $\tau > 10^{55} (m_i/\text{eV})^{-5} \text{ yr}$
- » Age of Universe (~ 14.5 Gyr)
- ► BSM decays may have significantly higher rates: $v_i \rightarrow v_j + \varphi$
- φ: Nambu-Goldstone boson of a broken symmetry (*e.g.*, Majoron)

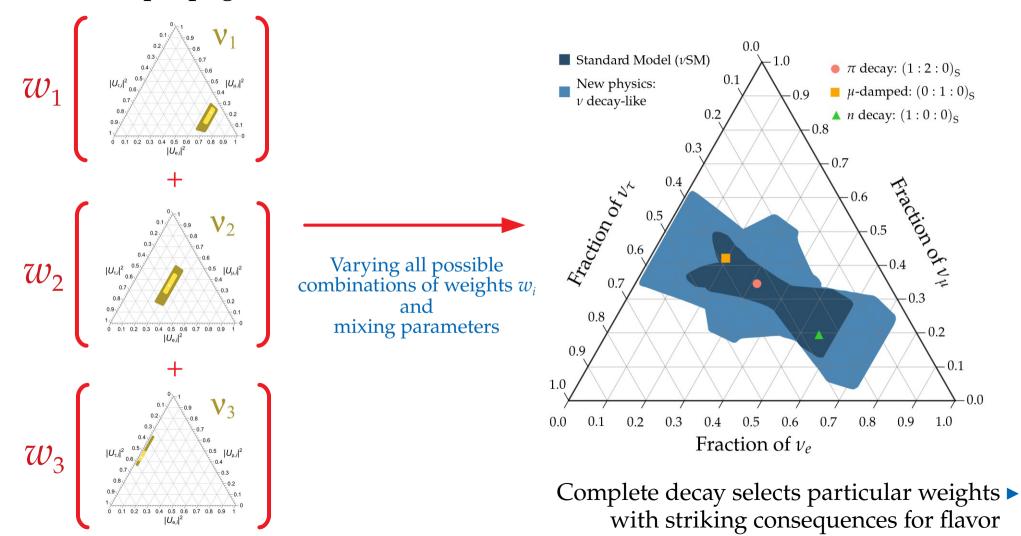
▶ We work in a model-independent way: the nature of φ is unimportant if it is invisible to neutrino detectors

Flavor content of neutrino mass eigenstates





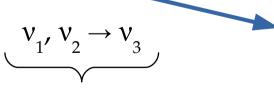
Neutrinos propagate as an incoherent mix of v_1 , v_2 , v_3 —



Measuring the neutrino lifetime $v_{2'}$ $v_3 \rightarrow v_1$ Sources v₁ lightest and stable (normal mass ordering)

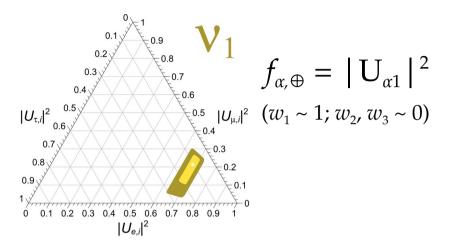
0.2 0.3 0.4 0.5 $f_{ au,S}$ 0.7 0.8 0.2 0.9 0.1 0.1 0.2 0.3 0.4 0.5 0.6 0.7 0.8 0.9 $f_{ m e.S}$

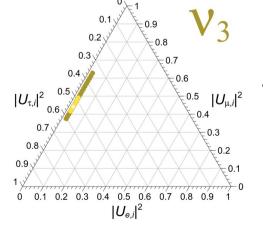
If all unstable neutrinos decay



v₃ lightest and stable (inverted mass ordering)

Earth

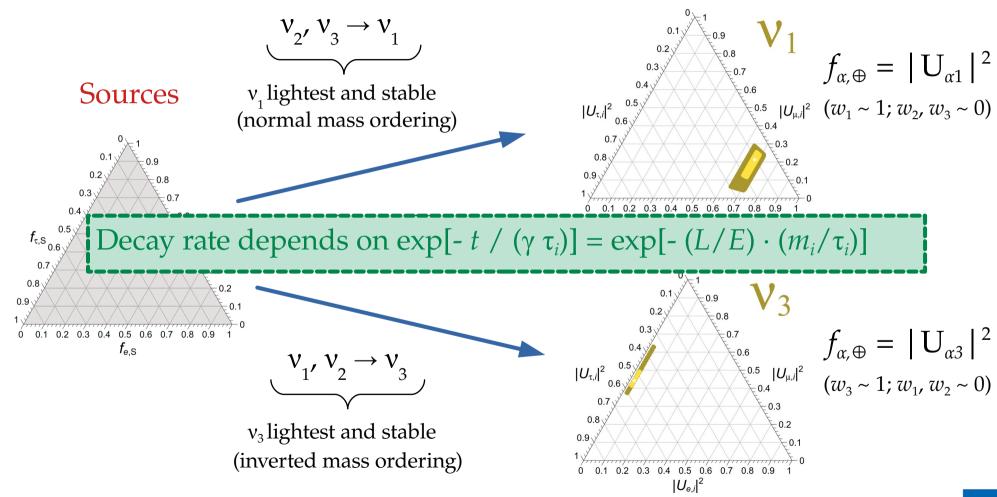


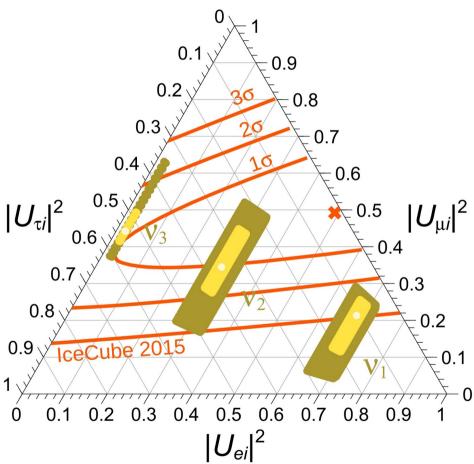


$$f_{\alpha,\oplus} = |\mathbf{U}_{\alpha 3}|^2$$
$$(w_3 \sim 1; w_1, w_2 \sim 0)$$

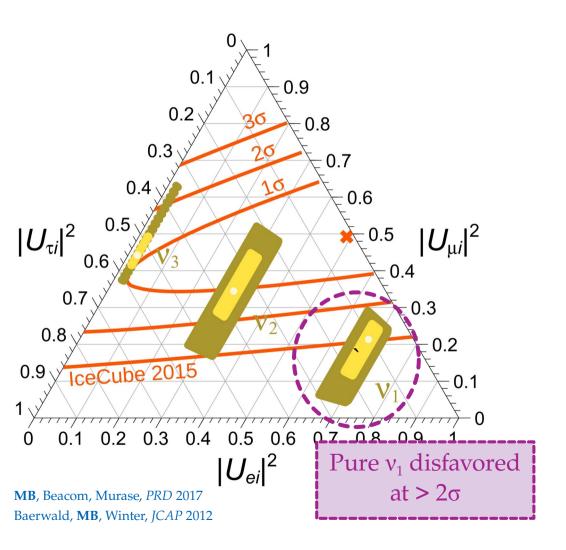
Measuring the neutrino lifetime

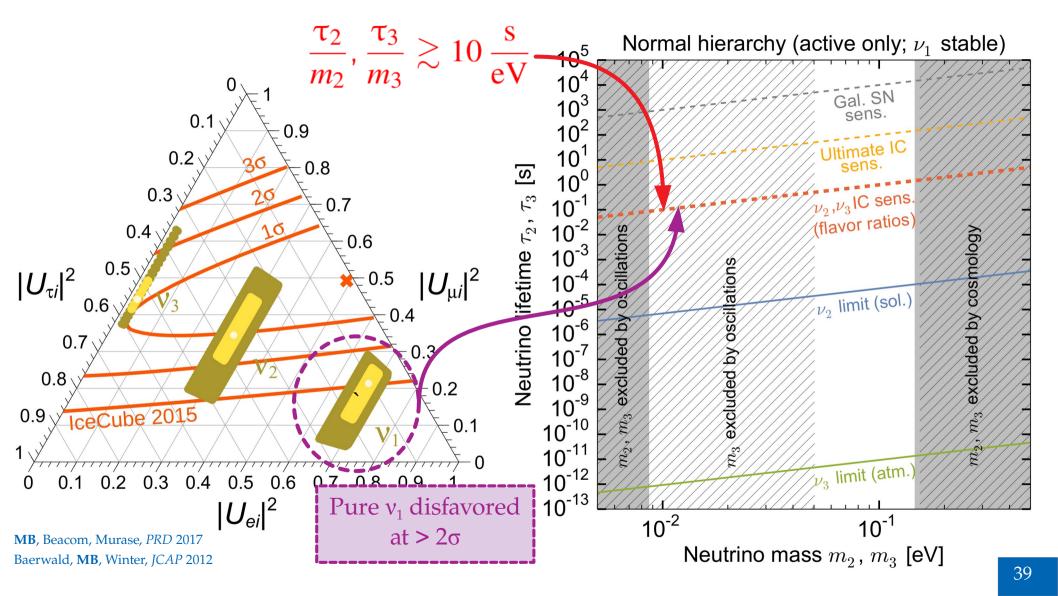
Earth





MB, Beacom, Murase, *PRD* 2017 Baerwald, **MB**, Winter, *JCAP* 2012

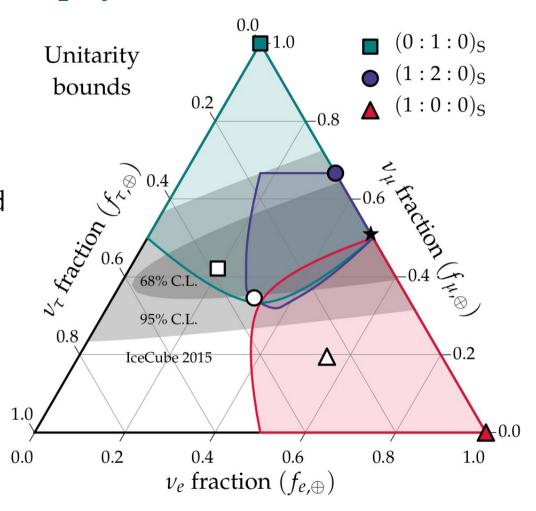




Using unitarity to constrain new physics

$$H_{tot} = H_{std} + H_{NP}$$

- ▶ New mixing angles unconstrained
- ► Use unitarity $(U_{NP}U_{NP}^{\dagger} = 1)$ to bound all possible flavor ratios at Earth
- Can be used as prior in new-physics searches in IceCube



Ahlers, **MB**, Mu, *PRD* 2018 See also: Xu, He, Rodejohann, *JCAP* 2014

How to fill out the flavor triangle?

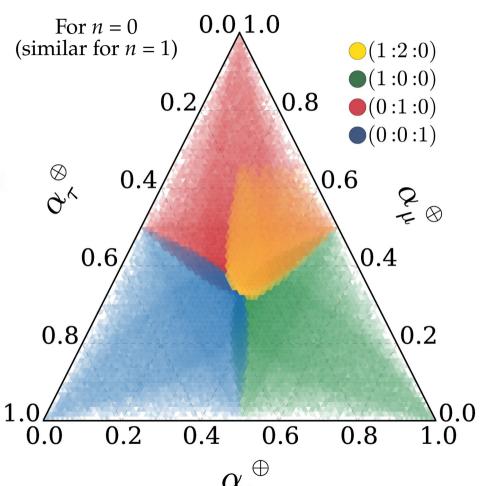
$$H_{\mathsf{tot}} = H_{\mathsf{std}} + H_{\mathsf{NP}}$$

$$H_{\mathsf{std}} = rac{1}{2E} U_{\mathsf{PMNS}}^{\dagger} \, \mathsf{diag} \left(0, \Delta m_{21}^2, \Delta m_{31}^2 \right) \, U_{\mathsf{PMNS}}$$

$$H_{\mathsf{NP}} = \sum_{n} \left(\frac{E}{\Lambda_n}\right)^n U_n^{\dagger} \operatorname{diag}\left(O_{n,1}, O_{n,2}, O_{n,3}\right) U_n$$

This can populate *all* of the triangle –

- ► Use current atmospheric bounds on $O_{n,i}$: $O_0 < 10^{-23}$ GeV, $O_1/\Lambda_1 < 10^{-27}$ GeV
- ► Sample the unknown new mixing angles



See also: Ahlers, **MB**, Mu, *PRD* 2018; Rasmusen *et al.*, *PRD* 2017; **MB**, Beacom, Winter *PRL* 2015; **MB**, Gago, Peña-Garay *JCAP* 2010; Bazo, **MB**, Gago, Miranda *IJMPA* 2009; + many others

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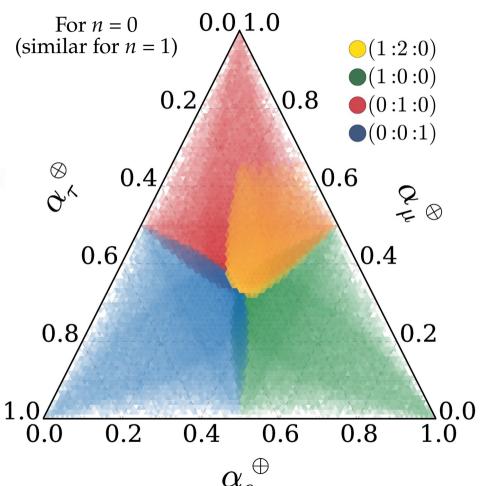
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