

Introduction

There are a large number of experiments investigating both neutrino oscillations and their interactions. In both cases, it is important to theoretically investigate neutrino scattering on various targets [2,3], since scattering processes are either a tool for detecting neutrino fluxes: the processes of neutrino scattering on a nucleon or a nucleus studied in this work contribute to the signals of such experiments as MiniBooNE [10], COHERENT [4,5] and registration of supernova neutrinos in JUNO [11]; or a tool for studying fundamental interactions of neutrinos: in this work, the contribution of the electromagnetic properties of neutrinos is studied. The latter neutrino properties emerge in different extensions of the Standard Model, and they include [1]: millicharges and charge radii, electric, magnetic and anapole moments.

2 Cross sections of elastic neutrino scattering on nucleons and nuclei

We consider the process where an ultrarelativistic neutrino with energy E_{ν} originates from a source (reactor, accelerator, the Sun, etc.) and elastically scatters on a nucleon(nuclei) in a detector at energy-momentum transfer $q = (T, \mathbf{q})$. If the neutrino is born in the source in the flavor state $|\nu_{\ell}\rangle$, then its state in the detector is $|\nu_{\ell}(L)\rangle = \sum_{k=1}^{3} U_{\ell k}^* \exp(-i \frac{m_k^2}{2E_{\nu}} \mathcal{L}) |\nu_k\rangle$, where \mathcal{L} is the source-detector distance. We assume the target nucleon (nucleus) to be free and at rest in the lab frame. The matrix element of the transition $\nu_{\ell}(L) + X \rightarrow \nu_{j} + X$, where X is either a proton, a neutron or a nucleus, due to weak interaction is given by

$$\mathcal{M}_{j}^{(w)} = \frac{G_{F}}{\sqrt{2}} U_{\ell j}^{*} e^{-i \frac{m_{j}^{2}}{2E_{\nu}} \mathcal{L}} \bar{u}_{j,\lambda'}^{(\nu)}(k') \gamma^{\mu} (1-\gamma^{5}) u_{j,\lambda}^{(\nu)}(k) J_{\mu}^{(NC)}, \qquad (1)$$

here $J_{\lambda}^{(NC)}$ is a weak neutral current of a nucleon (nucleus). $\bar{u}_{j,\lambda'}^{(\nu)}(k') =$ $u_{i,\lambda'}^{(\nu)\dagger}(k')\gamma^0$, where $u_{i,\lambda}^{(\nu)}(k)$ is the bispinor amplitude of the massive neutrino state $|\nu_i\rangle$ with 4-momentum k and spin state λ . The matrix element due to electromagnetic interaction is

$$\mathcal{M}_{j}^{(\gamma)} = -\frac{4\pi\alpha}{q^{2}} \sum_{k=1}^{3} U_{\ell k}^{*} e^{-i\frac{m_{k}^{2}}{2E_{\nu}}\mathcal{L}} \bar{u}_{j,\lambda'}^{(\nu)}(k') \Lambda_{jk}^{(\mathrm{EM};\nu)\mu}(q) u_{k,\lambda}^{(\nu)}(k) J_{\mu}^{(EM)}, \tag{2}$$

where $J_{\mu}^{(EM)}$ is the electromagnetic current of the nucleon (nucleus). Assuming the target to be a free nucleon, these currents can be expanded as follows:

$$J_{\lambda}^{(NC)}(q) = \bar{u}_{s'}^{(N)}(p')\Lambda_{\lambda}^{(NC;N)}(-q)u_{s}^{(N)}(p,s), J_{\lambda}^{(EM)}(q) = \bar{u}_{s'}^{(N)}(p')\Lambda_{\lambda}^{(EM;N)}(-q)u_{s}^{(N)}(p,s),$$
(3)

where $\Lambda_{\lambda}^{(\mathrm{NC};N)}(q)$ and $\Lambda_{\lambda}^{(\mathrm{EM};N)}(-q)$ are nucleon neutral weak and electromagnetic vertexes, respectively. $\Lambda_{ik}^{(\text{EM};\nu)\mu}(q)$ is the electromagnetic neutrino vertex. We consider the following vertexes:

Assuming the target to be a free nucleus, the nuclear currents can be expanded as follows:

$$J_{\lambda}^{(NC)}(q) = 2M[\delta_0^{\mu} \mathcal{F}_1(\vec{q}) - \delta_i^{\mu} \mathcal{G}_A^i(\vec{q})],$$

$$J_{\lambda}^{(EM)}(q) = 2M\delta_0^{\mu} \mathcal{F}_Q(\vec{q}),$$
(5)

where M is the nuclear mass, and

$$\mathcal{F}_{1}(\vec{q}) = \frac{1}{(2\pi)^{3}} \int d^{3}r e^{i\vec{q}\cdot\vec{r}} \langle n, J, M'_{J} | \sum_{k=0}^{Z+N} g_{V}^{N(k)} \delta^{3}(\vec{r} - \vec{r}_{k}) | n, J, M_{J} \rangle,$$

$$\mathcal{G}_{A}^{i}(\vec{q}) = \frac{1}{(2\pi)^{3}} \int d^{3}r e^{i\vec{q}\cdot\vec{r}} \langle n, J, M'_{J} | \sum_{k=0}^{Z+N} g_{A}^{N(k)} \sigma_{(k)}^{i} \delta^{3}(\vec{r} - \vec{r}_{k}) | n, J, M_{J} \rangle, \qquad (6)$$

$$\mathcal{F}_{Q}(\vec{q}) = \frac{1}{(2\pi)^{3}} \int d^{3}r e^{i\vec{q}\cdot\vec{r}} \langle n, J, M'_{J} | \sum_{k=0}^{Z} \delta^{3}(\vec{r} - \vec{r}_{k}) | n, J, M_{J} \rangle.$$

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When evaluating the cross section, we neglect the neutrino masses. Since the final massive state of the neutrino is not resolved in the detector, the differential cross section measured in the scattering experiment is given by

$$\frac{d\sigma}{dT} = \frac{|\mathcal{M}|^2}{32\pi E_{\nu}^2 m_N},\tag{7}$$

with the following absolute matrix element squared:

$$|\mathcal{M}|^{2} = \sum_{j=1}^{3} \left| \mathcal{M}_{j}^{(w)} + \mathcal{M}_{j}^{(\gamma)} \right|^{2}, \qquad (8)$$

where averaging over initial and summing over final spin polarizations is assumed. The differential cross section can be presented as a sum of the helicity-preserving (hp) and helicity-flipping (hf) parts: $\frac{d\sigma}{dT} = \frac{d\sigma_{\rm hp}}{dT} + \frac{d\sigma_{\rm hf}}{dT}$. The cross section for neutrino-nucleon scattering is

$$\begin{aligned} \frac{d\sigma_{hp}^{L}}{dT} &= \frac{G_{F}^{2}m_{N}}{2\pi} \left[\left(C_{V}^{L} - 2ReC_{V\&A}^{L} + C_{A}^{L} \right) + \left(C_{V}^{L} + 2ReC_{V\&A}^{L} + C_{A}^{L} \right) \left(1 - \frac{T}{E_{\nu}} \right)^{2} \right. \\ &+ \left(C_{A}^{L} - C_{V}^{L} \right) \frac{m_{N}T}{E_{\nu}^{2}} + C_{M}^{L} \frac{T}{2m_{N}} \left(2 + \frac{m_{N}T}{E_{\nu}^{2}} - \frac{2T}{E_{\nu}} \right) - C_{E}^{L} \frac{T}{2m_{N}} \left(2 - \frac{m_{N}T}{E_{\nu}^{2}} - \frac{2T}{E_{\nu}} \right) \right. \\ &+ 2\frac{T}{E_{\nu}} ReC_{A\&M}^{L} \left(2 - \frac{T}{E_{\nu}} \right) - 2ReC_{V\&M}^{L} \frac{T^{2}}{E_{\nu}^{2}} \right], \\ \frac{d\sigma_{hf}^{L}}{dT} &= \frac{\pi\alpha^{2}}{m_{e}^{2}} |\mu_{\nu}^{L}(\mathcal{L}, E_{\nu})|^{2} \left[\left(\frac{1}{T} - \frac{1}{E_{\nu}} \right) F_{Q}^{2} + \left(\frac{1}{T} - \frac{1}{E_{\nu}} - \frac{m_{N}}{2E_{\nu}^{2}} \right) \frac{T^{2}}{4m_{N}^{2}} F_{A}^{2} \right. \\ &- \frac{T}{2E_{\nu}^{2}} F_{Q}F_{M} + \frac{\left(2 - \frac{T}{E_{\nu}} \right)^{2} - \frac{2m_{N}T}{E_{\nu}^{2}}}{8m_{N}} F_{M}^{2} - \frac{\left(2 - \frac{T}{E_{\nu}} \right)^{2}}{8m_{N}} F_{E}^{2} + \frac{\left(2 - \frac{T}{E_{\nu}} \right)T}{4E_{\nu}m_{N}} F_{A}(F_{M} - F_{Q}) \right] \end{aligned}$$

where [2]

$$C_{V}^{L} = \sum_{j} \left| \sum_{k} U_{\ell k}^{*} e^{-i\frac{m_{k}^{2}}{2E_{\nu}}\mathcal{L}}} (\delta_{jk}F_{1} - F_{Q}Q_{jk}^{L}) \right|^{2}, \quad Q_{jk}^{L} = \frac{2\sqrt{2}\pi\alpha}{G_{F}q^{2}} \left(f_{jk}^{Q} - q^{2}f_{jk}^{A} \right),$$

$$C_{VkA}^{L} = \sum_{j} \left(\sum_{k} U_{\ell k}^{*} e^{-i\frac{m_{k}^{2}}{2E_{\nu}}\mathcal{L}}} (\delta_{jk}F_{1} - F_{Q}Q_{jk}^{L}) \right) \left(\sum_{n} U_{\ell n} e^{i\frac{m_{n}^{2}}{2E_{\nu}}\mathcal{L}}} (-\delta_{jn}G_{A} + \frac{q^{2}F_{A}Q_{jn}^{L}}{4m_{N}^{2}}) \right),$$

$$C_{A}^{L} = \sum_{j} \left| \sum_{k} U_{\ell k}^{*} e^{-i\frac{m_{k}^{2}}{2E_{\nu}}\mathcal{L}}} (G_{A}\delta_{jk} - \frac{q^{2}F_{A}Q_{jk}^{L}}{4m_{N}^{2}}) \right|^{2},$$

$$C_{M}^{L} = \sum_{j} \left| \sum_{k} U_{\ell k}^{*} e^{-i\frac{m_{k}^{2}}{2E_{\nu}}\mathcal{L}}} (F_{2}\delta_{jk} - F_{M}Q_{jk}^{L}) \right|^{2},$$

$$C_{AkM}^{L} = \sum_{j} \left(\sum_{k} U_{\ell k}^{*} e^{-i\frac{m_{k}^{2}}{2E_{\nu}}\mathcal{L}}} (\delta_{jk}G_{A} - \frac{q^{2}F_{A}Q_{jk}^{L}}{4m_{N}^{2}}) \right) \left(\sum_{n} U_{\ell n} e^{i\frac{m_{n}^{2}}{2E_{\nu}}\mathcal{L}}} (F_{2}\delta_{jn} - F_{M}Q_{jn}^{L}) \right),$$

$$C_{VkM}^{L} = \sum_{j} \left(\sum_{k} U_{\ell k}^{*} e^{-i\frac{m_{k}^{2}}{2E_{\nu}}\mathcal{L}}} (-\delta_{jk}F_{1} + F_{Q}Q_{jk}^{L}) \right) \left(\sum_{n} U_{\ell n} e^{i\frac{m_{n}^{2}}{2E_{\nu}}\mathcal{L}}} (F_{2}\delta_{jn} - F_{M}Q_{jn}^{L}) \right),$$

$$C_{E}^{L} = \sum_{j} \left| \sum_{k} U_{\ell k}^{*} e^{-i\frac{m_{k}^{2}}{2E_{\nu}}\mathcal{L}}} F_{E}Q_{jk}^{L} \right|^{2}, |\mu^{L}(\mathcal{L}, E_{\nu})|^{2} = \sum_{j} \left| \sum_{k} U_{\ell k}^{*} e^{-i\frac{m_{k}^{2}}{2E_{\nu}}\mathcal{L}}} 2m_{e}(f_{jk}^{M} - if_{jk}^{E}) \right|$$
(10)

The cross section for neutrino-nucleus scattering is

$$\frac{d\sigma_L}{dT} = \frac{G_F^2 M}{2\pi} \left[\mathcal{C}_V^L \left(2 - \frac{MT}{E_\nu^2} \right) + \frac{1}{2J+1} \sum_{M_J M_{J'}} |\mathcal{G}_A^z|^2 \left(2 + \frac{MT}{E_\nu^2} \right) \right] + \frac{\pi \alpha}{m_e^2} \frac{|\mathcal{F}_Q|^2}{T} |\mu^L(\mathcal{L}, E_\nu)| \\ \mathcal{C}_V^L = \sum_j \left| \sum_k U_{\ell k}^* e^{-i\frac{m_k^2}{2E_\nu} \mathcal{L}} (\delta_{jk} \mathcal{F}_1 - \mathcal{F}_Q Q_{jk}^L) \right|^2, \quad Q_{jk}^L = \frac{2\sqrt{2\pi\alpha}}{G_F q^2} \left(f_{jk}^Q - q^2 f_{jk}^A \right).$$
(11)

3 Numerical results

Here we present numerical calculations for neutrino-nucleon and neutrinonucleus scattering. We restrict ourselves to the case of charge and magnetic electromagnetic form factors of a nucleon, accounting for the relation between the nucleon neutral weak and electromagnetic form factors

$$F_{1,2}^{p}(q^{2}) = \left(\frac{1}{2} - 2\sin^{2}\theta_{W}\right)F_{Q,M}^{p}(q^{2}) - 1\frac{1}{2}F_{Q,M}^{n}(q^{2}) - \frac{1}{2}F_{1,2}^{S}(q^{2}),$$

$$F_{1,2}^{n}(q^{2}) = \left(\frac{1}{2} - 2\sin^{2}\theta_{W}\right)F_{Q,M}^{n}(q^{2}) - 1\frac{1}{2}F_{Q,M}^{p}(q^{2}) - \frac{1}{2}F_{1,2}^{S}(q^{2}),$$

$$G_{A,P}^{N}(q^{2}) = \frac{\tau_{3}}{2}G_{A,P}^{a}(q^{2}) - \frac{1}{2}G_{A,P}^{S}(q^{2}),$$
(12)







Figure 3: The differential cross sections of neutrino scattering on (a) a proton and (b) a neutron at small energy transfer values, accounting for diagonal neutrino magnetic moments.

For the neutrino-nucleus case we chose ${}^{40}\!\text{Ar}$ as a target [6] with parametrization of nuclear form factors that can be found in [12] (and references therein). We present our results for a zero source-detector distance, with or without transition neutrino charge radii (Fig. 4), with or without diagonal neutrino magnetic moments (Fig. 5)

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where $F_{1,2}^S$, $G_{A,P}^S$ are strange form factors of the nucleon. We use the parametrization that can be found in [8] (and references therein). We present the numerical results for a zero source-detector distance, with and without strange form-factor contribution, with and without neutrino charge radii (Fig. 1), (Fig. 2), with and without diagonal neutrino magnetic moments (Fig. 3)





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Figure 5: The dif diagonal neutrino
4 Summa Elastic scatter been considered interactions of have two chant both cases, the In addition, ne into account. The formulas electromagneti feature allows are neutrino en neutrino intera from supernov [11], the study electric dipole characteristics for neutrino en (Fig.4,5) exper The results of approach to stu- on complex tar
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ifferential cross sections of neutrino scattering on ⁴⁰Ar, accounting for ino charge radii, at E_{ν} values of (a) 10 MeV, (b) 30 MeV, and (c) 50



ifferential cross section of neutrino scattering on $^{40}\!\mathrm{Ar}$ with account for o magnetic moments.

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ering of neutrinos by a nucleon and a nucleus has red theoretically, taking into account the electromagnetic E massive neutrinos. Thus, the processes under consideration nnels: through the exchange of a Z boson and a photon. In ne nucleon and nuclear form factors are taken into account. eutrino oscillations based on the source-detector are taken

obtained contain information about both neutrino tic form factors and nucleon and nuclear form factors. This the formulas to be used in various studies. Among them experiments with short and long baselines, the study of actions and oscillations in matter, registration of neutrinos va explosions using elastic neutrino scattering on protons of the anapole moment of the nucleon, the search for the moment of the neutron, the search for the electromagnetic of neutrinos. We have performed numerical calculations nergies relevant for MiniBooNE (Fig.1,3) and COHERENT riments

this work contribute to the development of a systematic udying the properties of neutrinos in their elastic scattering rgets (nuclei, atoms, condensed matter).

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