

# Large Triple Higgs Couplings in the 2HDM

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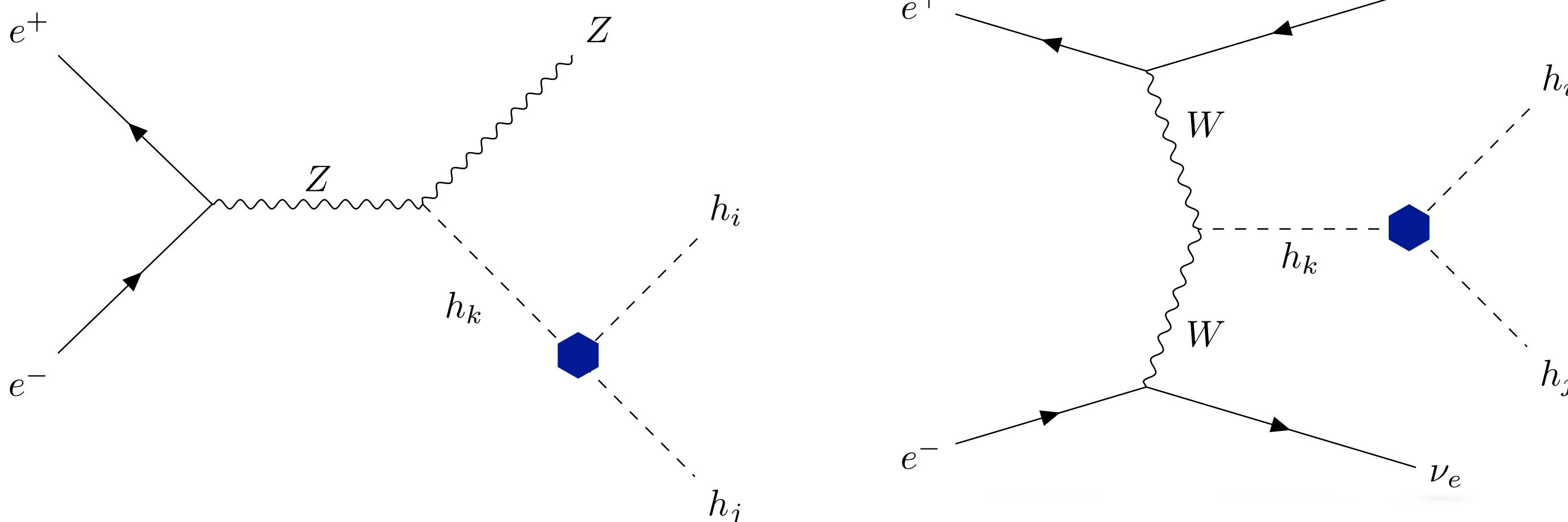
# Motivation

In the context of the 2HDM (type I and II), triple Higgs couplings  $\lambda_{h_i h_j h_k}$ , can be large while respecting all the relevant constraints (*Eur.Phys.J.C 80 (2020) 9, 884, [arXiv2005.10576]*)



$\lambda_{h_i h_j h_k}$  can affect the di-Higgs production at tree level

Two channels of interest:  $e^+ e^- \rightarrow h_i h_j Z$  and  $e^+ e^- \rightarrow h_i h_j \nu \bar{\nu}$  with  $h_i h_j = hh, hH, HH, AA$



# The Two Higgs Doublet Model (2HMD)

Adding a second Higgs doublet to the SM  $\implies$  5 physical Higgs bosons:  $h$ ,  $H$ ,  $A$  and  $H^\pm$

Potential: 
$$V = m_{11}^2(\Phi_1^\dagger \Phi_1) + m_{22}^2(\Phi_2^\dagger \Phi_2) - m_{12}^2(\Phi_1^\dagger \Phi_2 + \Phi_2^\dagger \Phi_1) + \frac{\lambda_1}{2}(\Phi_1^\dagger \Phi_1)^2 + \frac{\lambda_2}{2}(\Phi_2^\dagger \Phi_2)^2$$
$$+ \lambda_3(\Phi_1^\dagger \Phi_1)(\Phi_2^\dagger \Phi_2) + \lambda_4(\Phi_1^\dagger \Phi_2)(\Phi_2^\dagger \Phi_1) + \frac{\lambda_5}{2}[(\Phi_1^\dagger \Phi_2)^2 + (\Phi_2^\dagger \Phi_1)^2]$$

*Considerations:*

- $CP$  conservation: all parameters are real
- $Z_2$  symmetry to avoid FCNC: softly broken by  $m_{12}^2$ 
  - 4 possible Yukawa structures: we only consider 2HDM type I and type II

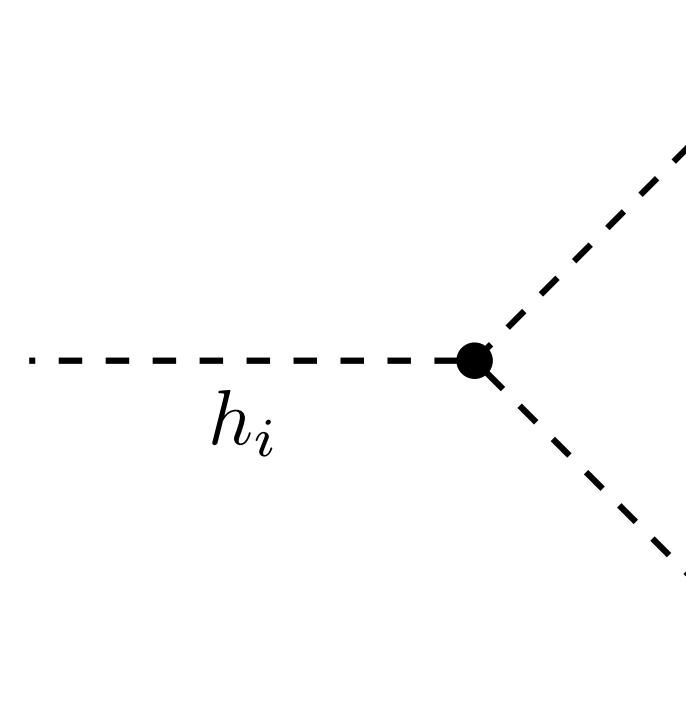
Input parameters:

$m_h$  ( $= 125$  GeV),  $m_H$ ,  $m_A$ ,  $m_{H^\pm}$ ,  $\tan \beta := v_2/v_1$ ,  $\cos(\beta - \alpha) \equiv c_{\beta-\alpha}$  and  $m_{12}^2$

ALIGNMENT LIMIT:  $c_{\beta-\alpha} \rightarrow 0$ , the SM interactions for  $h$  are recovered

# Triple Higgs Couplings (THC)

## Coupling definition:


$$= - i v n! \lambda_{h_i h_j h_k}$$

and

$$\kappa_\lambda := \lambda_{hhh} / \lambda_{hhh}^{\text{SM}}$$

## Final allowed ranges:

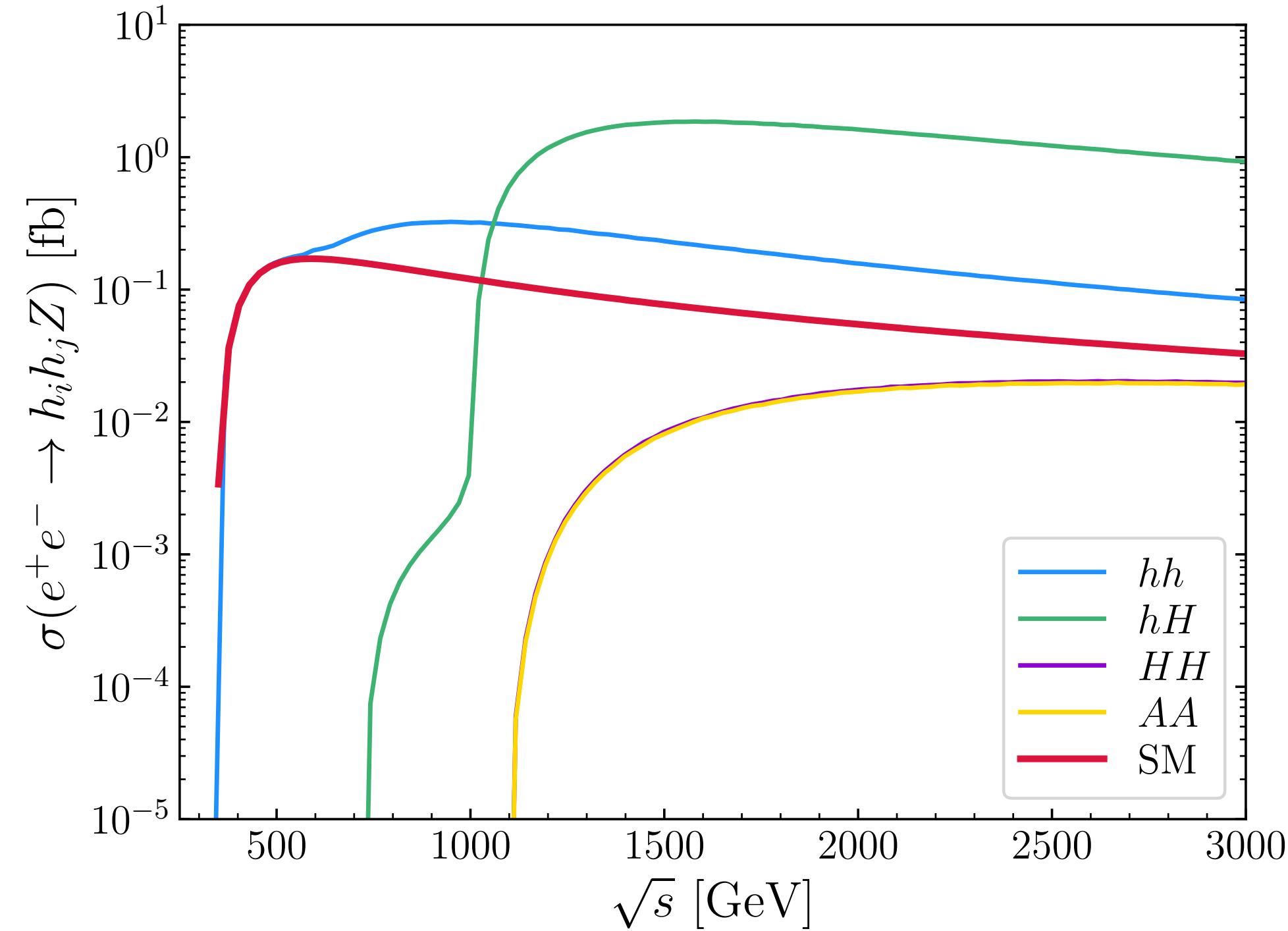
Type I	Type II
$\kappa_\lambda \in [-0.5, 1.5]$	$\kappa_\lambda \in [0.0, 1.0]$
$\lambda_{hhH} \in [-1.4, 1.5]$	$\lambda_{hhH} \in [-1.6, 1.8]$
$\lambda_{hHH} \in [0, 15]$	$\lambda_{hHH} \in [0, 15]$
$\lambda_{hAA} \in [0, 16]$	$\lambda_{hAA} \in [0, 16]$

## Constraints

- Electroweak precision data,  $T$  parameter:  
motivates scenarios with degenerate masses
    - ▶ For us  $m_H = m_A = m_{H^\pm} \equiv m$
  - Tree level unitarity and potential stability:  
 $m_{12}^2 = m_H^2 \cos^2 \alpha / \tan \beta$  helps reach large masses
  - Collider measurements of the 125 GeV Higgs
    - Close to  $\cos(\beta - \alpha) = 0$ , specially for type II
  - BSM Higgs searches in LEP, TeVatron and LHC
  - Flavor observables:  $\text{BR}(B \rightarrow X_s \gamma)$  and  $\text{BR}(B_s \rightarrow \mu\mu)$
- 2HDMC, HiggsBounds, HiggsSignals and superISO were used

(More detailed discussion to all these constraints in [\[arXiv2005.10576\]](#))

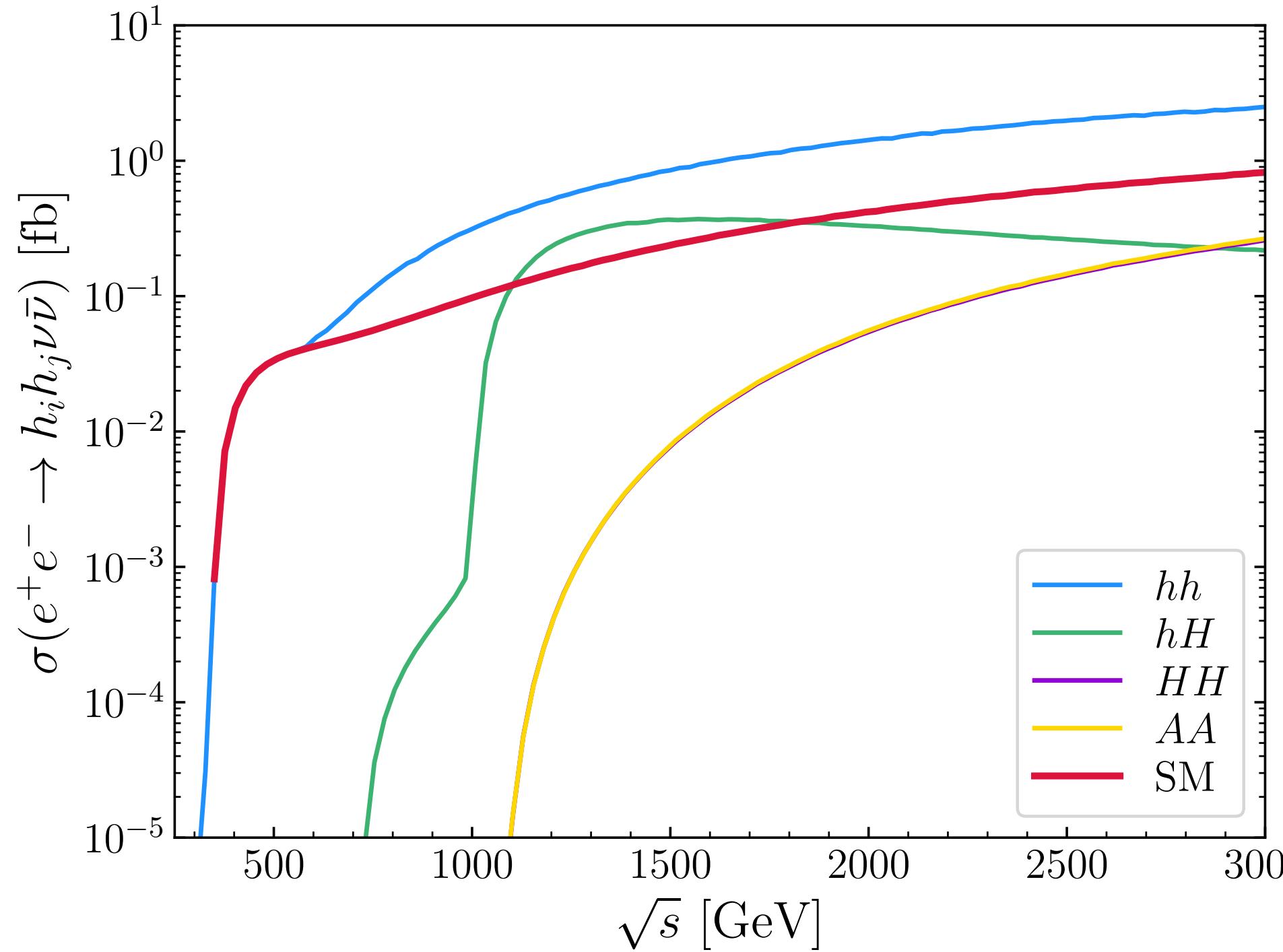
# Dependence with energy



$Z$  channel  $\rightarrow$  decreases  
with the energy

$\nu\bar{\nu}$  channel  $\rightarrow$  increases  
with the energy (VBF  
topologies!)

- $hhZ$  and  $hh\nu\bar{\nu}$ :  $\sim 3$  times the SM due to resonant diagrams mediated by  $H$  (contains  $\lambda_{hhH}$ ) and  $A$  (without THC)
- $hHZ$  and  $hH\nu\bar{\nu}$ :  $A$  mediated diagrams are the dominant contribution but we can still have THC sensitivity at large energies
- $HH\nu\bar{\nu} \sim AA\nu\bar{\nu}$ : dominated at large energies by  $\lambda_{hHH}$  ( $\lambda_{hAA}$ ) if it is large enough (because  $m_H = m_A$ )



Type I  
 $m = 500$  GeV  
 $\tan\beta = 10$   
 $c_{\beta-\alpha} = 0.2$   
 $m_{12}^2 = 24000$  GeV $^2$

$\kappa_\lambda := \lambda_{hhh}/\lambda_{hhh}^{SM} \simeq 1$   
 $\lambda_{hhH} = -0.5$   
 $\lambda_{hHH} = \lambda_{hAA} = 6$   
 $\lambda_{hH^+H^-} = 12$

# $hh$ production, ILC 500GeV (type I)

Production cross sections wrt the SM at ILC 500 GeV for  $hhZ$  (left) and  $hh\nu\bar{\nu}$  (right)

- Here  $hhZ$  is the most important channel

1.  $\kappa_\lambda$ : positive interference in the  $Z$  channel and negative interference in the  $\nu\bar{\nu}$  channel

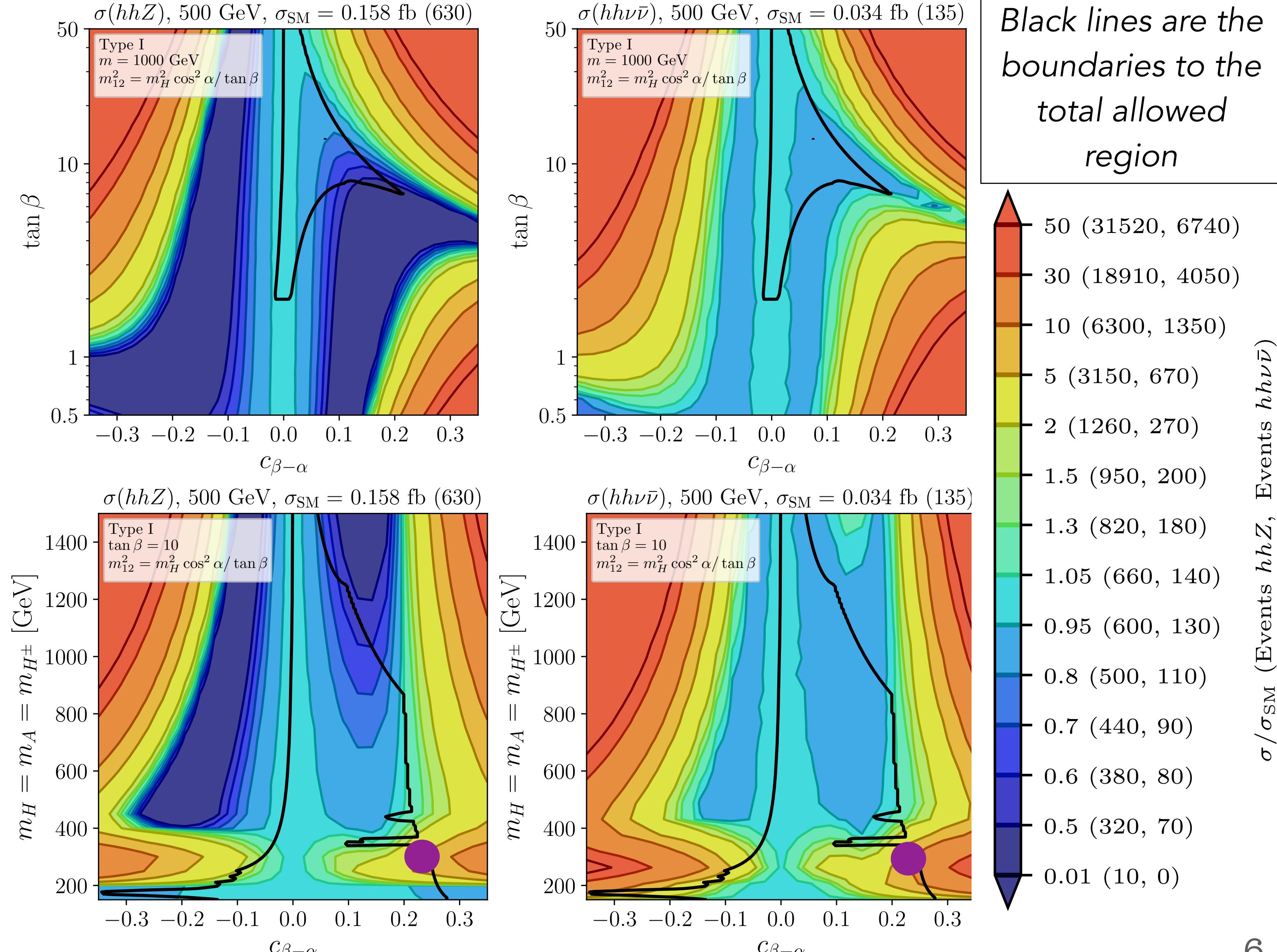
Larger distortion wrt the SM at the “tip”  
( $\kappa_\lambda = -0.4$ )

2.  $\lambda_{hhH}$ : through resonant diagrams mediated by  $H$

For low masses away from the alignment limit

3. Extra contribution from resonant diagrams mediated by  $A$ , but no information about THC :(

It is essential to look to the invariant mass of the final Higgs pair  $m_{hh}$  to see the effects of THC

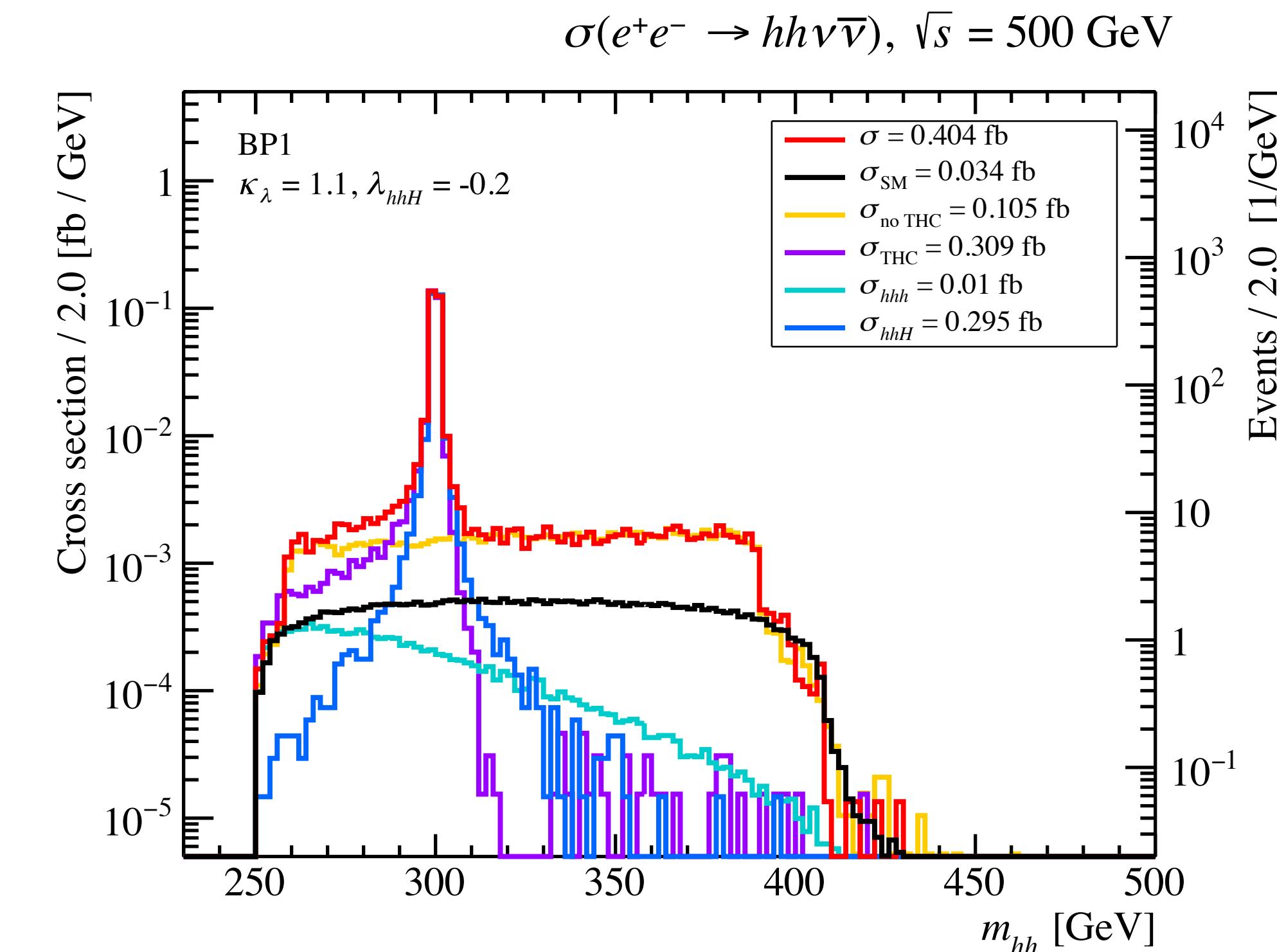
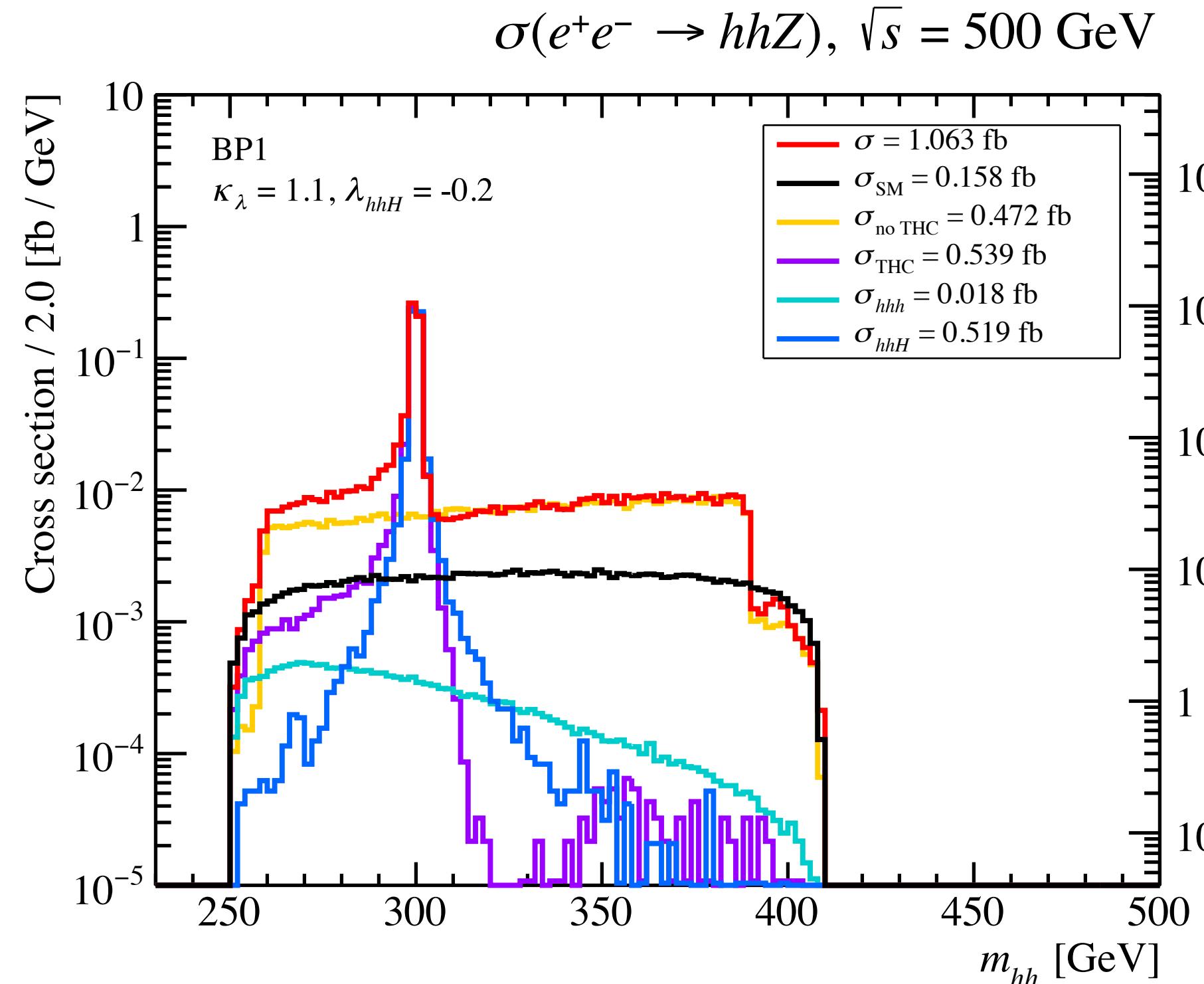


Black lines are the boundaries to the total allowed region

$\sigma / \sigma_{\text{SM}}$  (Events  $hhZ$ , Events  $hh\nu\bar{\nu}$ )

# $hh$ production, ILC 500GeV, THC dependence (type I)

Cross section distribution on the invariant mass of  $hh$ , contribution from different diagrams:



Type I  
 $m = 300 \text{ GeV}$   
 $\tan \beta = 10$   
 $c_{\beta-\alpha} = 0.25$   
 $m_{12}^2 = \frac{m_H^2 \cos^2 \alpha}{\tan \beta}$

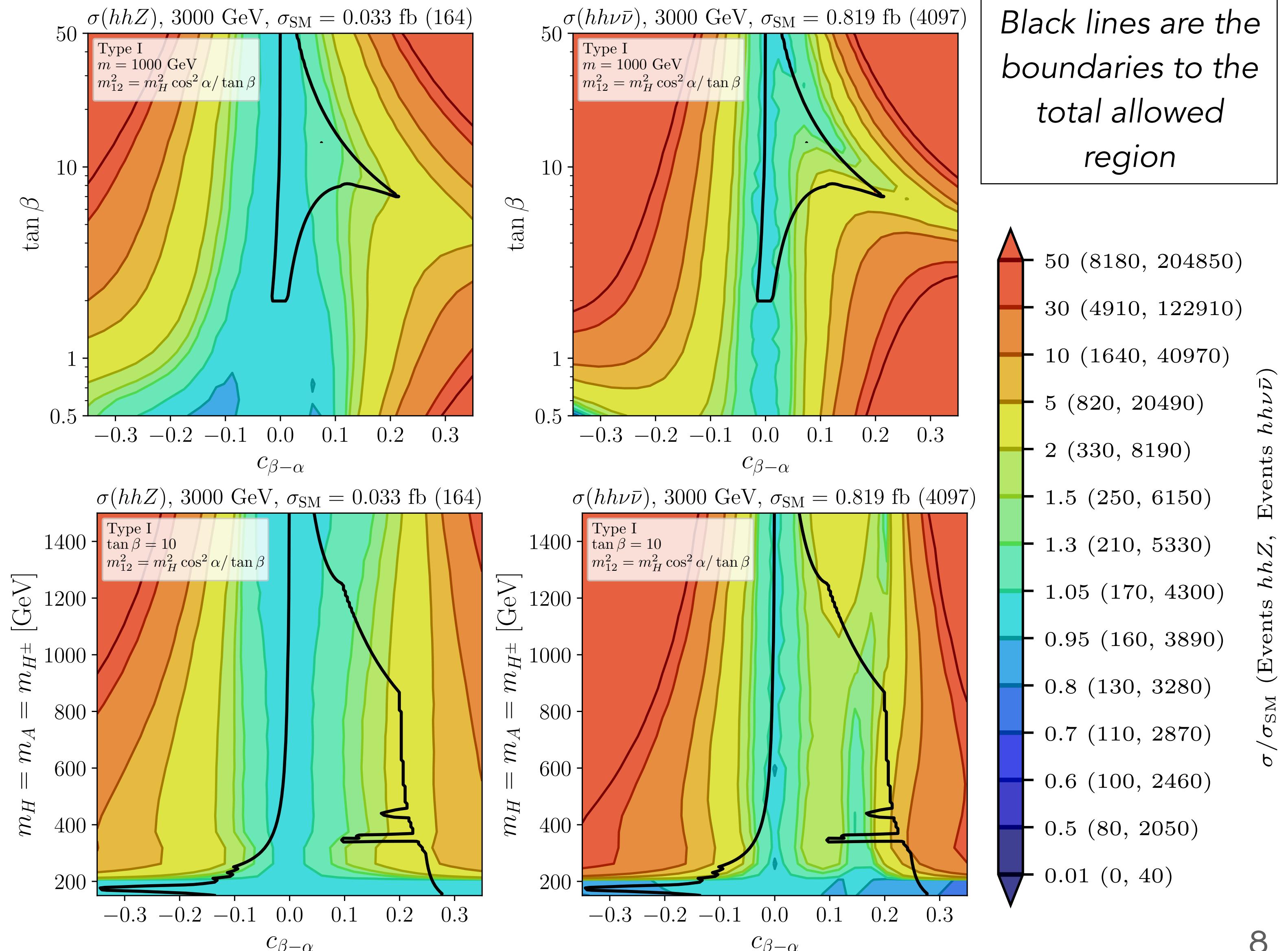
- Larger influence of  $\kappa_\lambda$  appears at the threshold of  $m_{hh}$  (light blue line)
- $H$  resonance (dark blue line): around  $m_{hh} = m_H \rightarrow$  information from  $\lambda_{hhH}$
- Plateau in the diagrams without THC (yellow line) wrt the SM (black line) due to the  $A$  resonant diagrams

The effect from  $\kappa_\lambda$  and  $\lambda_{hhH}$  can be “mixed” if  $m_H$  is small

# $hh$ production, CLIC 3TeV (type I)

Production cross sections wrt the SM at CLIC 3 TeV for  $hhZ$  (left) and  $hh\nu\bar{\nu}$  (right)

- At this energy,  $hh\nu\bar{\nu}$  channel is the most important channel
- $hhZ$  is very dominated by the  $A$  mediated diagrams, while in  $hh\nu\bar{\nu}$  the  $H$  mediated diagrams are more important
- In the neutrino channel we can find very large XS:  $\sim 10\sigma_{\text{SM}} = 9 \text{ fb}$  at low masses and  $\sim 3\sigma_{\text{SM}}$  for a wide range of masses



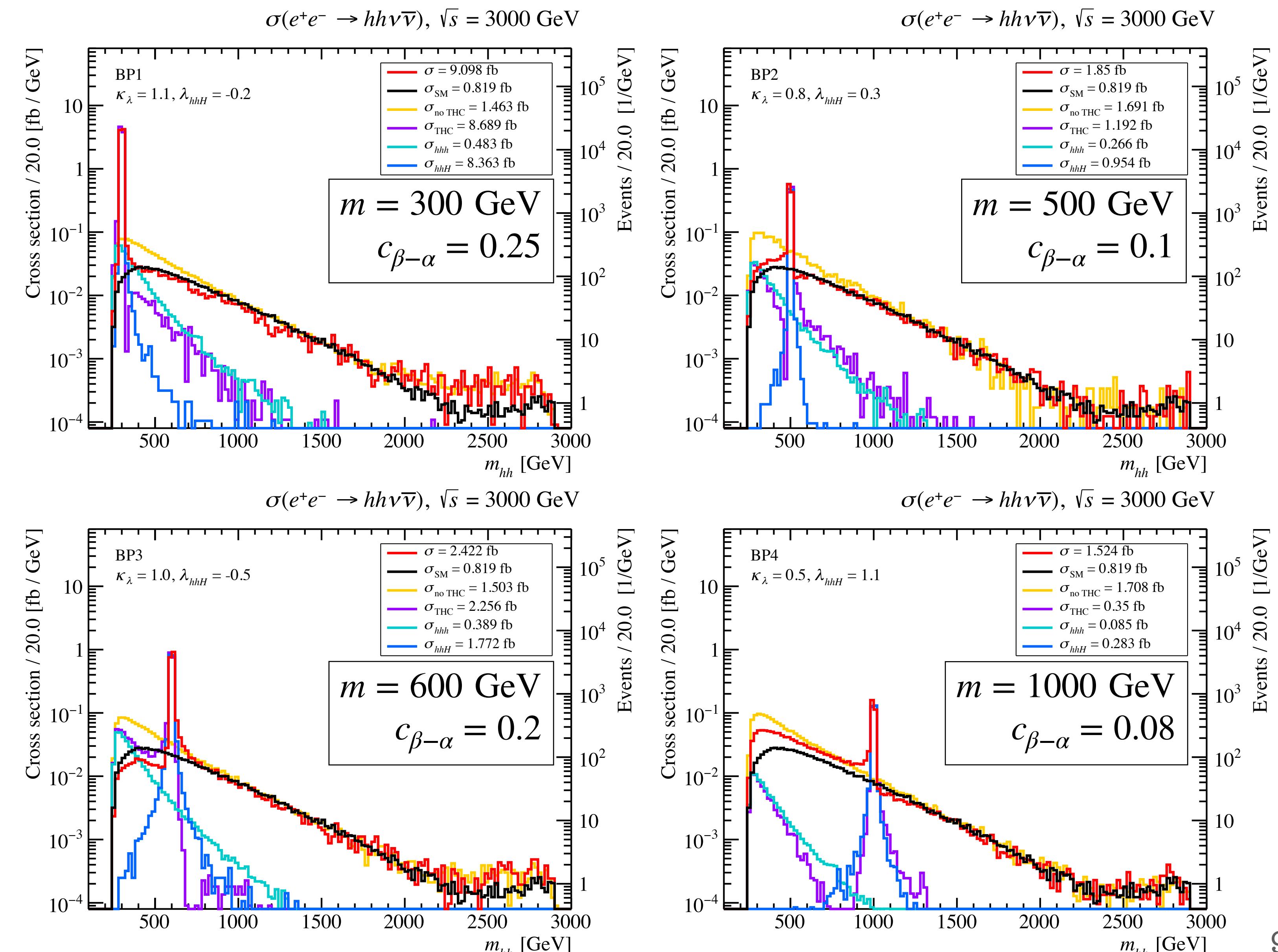
# $hh$ production, CLIC 3TeV, THC dependence (type I)

Cross section distribution on the invariant mass of  $hh$ , contribution from different diagrams:

- The effect of  $\kappa_\lambda$  appear at the region of low invariant mass
- The neutrino channel can access to the  $H$  resonant peak (i.e. to  $\lambda_{hhH}$ ) for a wide range of  $m_H$  and  $c_{\beta-\alpha}$

- Sign of  $\lambda_{hhH}$ : asymmetry around the  $H$  peak

⇒ which collider and channel are best suited to access to  $\lambda_{hhH}$ ?



# $hh$ production, “sensitivity” to $\lambda_{hhH}$ (type I)

We define our theoretical sensitivity as:

$$R = \frac{\bar{N}^R - \bar{N}^C}{\sqrt{\bar{N}^C}}$$

$R$  estimates the sensitivity to  $\lambda_{hhH}$  via 4  $b$ -jets events in the  $m_{hh}$  region close to the  $H$  resonance

$hhZ$	$\sqrt{s}$ [GeV]	$\sigma_{2\text{HDM}} / \sigma_{\text{SM}}$ [fb]	$\bar{N}_{4bZ}^R / \bar{N}_{4bZ}^C / \bar{N}_{4bZ}^{\text{SM}}$	$R_{4bZ}$
BP1	500	1.063 / 0.158	193 / 10 / 3	58
	1000	0.913 / 0.120	206 / 1 / 4	205
	1500	0.493 / 0.077	22 / < 1 / 1	-
	3000	0.147 / 0.033	1 / < 1 / < 1	-
BP2	1000	0.156 / 0.120	20 / 1 / 1	19
	1500	0.106 / 0.077	4 / < 1 / < 1	-
	3000	0.042 / 0.033	< 1 / < 1 / < 1	-
BP3	1000	0.254 / 0.120	29 / 5 / 2	11
	1500	0.218 / 0.077	8 / 1 / < 1	7
	3000	0.086 / 0.033	1 / < 1 / < 1	-
BP4	1500	0.075 / 0.077	1 / < 1 / < 1	-
	3000	0.038 / 0.033	< 1 / < 1 / < 1	-

$\bar{N}^{R/C}$  are the expected realistic events from the  $H$  resonance and from diagrams without THC, considering the  $b$ -tagging efficiency and detection acceptance at the collider with the following cuts:  
 $p_T^b > 20$  GeV,  $|\eta^b| < 2$ ,  $\Delta R_{bb} > 0.4$ ,  $p_T^Z > 20$  GeV,  $E_T > 20$  GeV

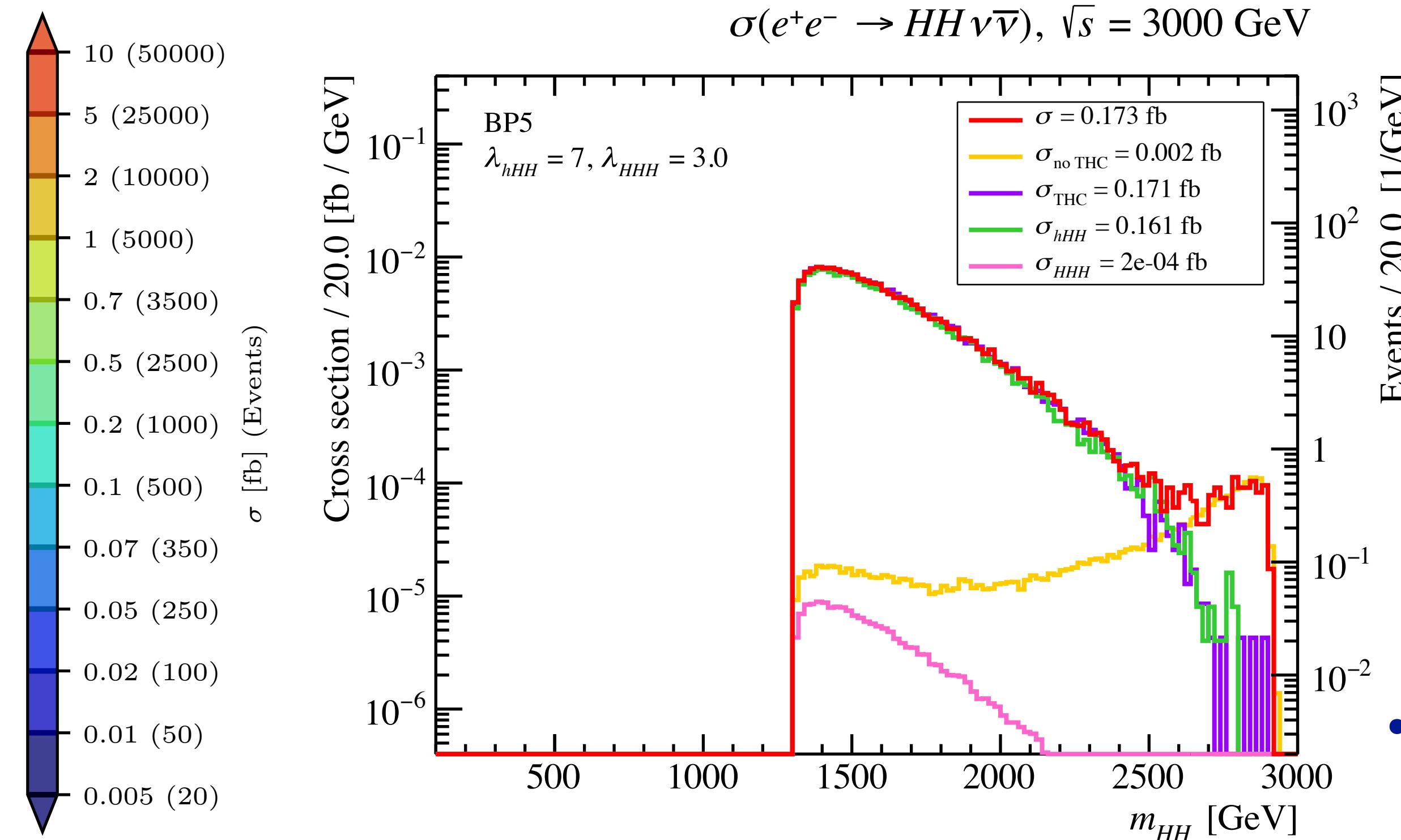
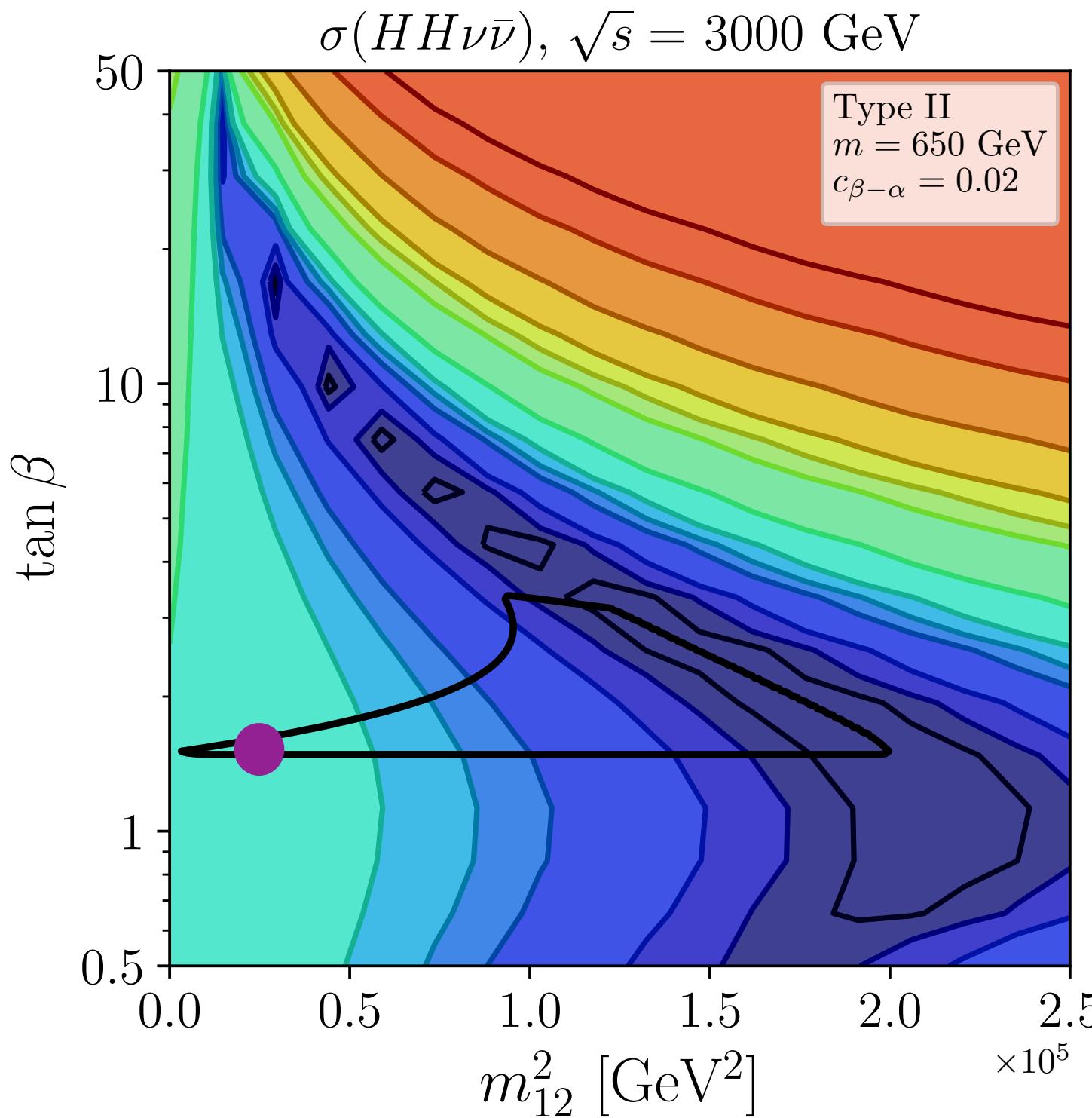
$hh\nu\bar{\nu}$	$\sqrt{s}$ [GeV]	$\sigma_{2\text{HDM}} / \sigma_{\text{SM}}$ [fb]	$\bar{N}_{4bE_T}^R / \bar{N}_{4bE_T}^C / \bar{N}_{4bE_T}^{\text{SM}}$	$R_{4bE_T}$
BP1	500	0.404 / 0.034	119 / 4 / 1	58
	1000	2.391 / 0.097	1510 / 24 / 0	303
	1500	4.423 / 0.239	794 / 13 / 2	217
	3000	9.098 / 0.819	2425 / 46 / 6	351
BP2	1000	0.234 / 0.097	79 / 3 / 1	44
	1500	0.625 / 0.239	70 / 3 / 1	39
	3000	1.850 / 0.819	282 / 28 / 9	48
BP3	1000	0.208 / 0.097	85 / 5 / 3	36
	1500	0.709 / 0.239	111 / 5 / 3	47
	3000	2.422 / 0.819	577 / 30 / 11	100
BP4	1500	0.428 / 0.239	4 / < 1 / < 1	-
	3000	1.523 / 0.819	72 / 4 / 3	34

More sensitivity to  $\lambda_{hhH}$  (i.e. larger  $R$ ) in the neutrino channel at all studied points, specially at CLIC 3 TeV

more details in [\[arxiv:2106.11105\]](https://arxiv.org/abs/2106.11105)

# $HH \sim AA$ production, CLIC 3TeV, THC dependence (type II)

In type II, due to the collider constraints, only  $HH\nu\bar{\nu} \sim AA\nu\bar{\nu}$  production is relevant



Type II  
 $m = 650 \text{ GeV}$   
 $\tan \beta = 1.5$   
 $c_{\beta-\alpha} = 0.02$   
 $m_{12}^2 = 10000 \text{ GeV}^2$

- XS is larger at low  $m_{12}^2$ , that is the region where  $\lambda_{hHH}$  is larger
- The dominant effect in  $HH\nu\bar{\nu}$  comes from  $\lambda_{hHH}$  (green line) and it is responsible for almost all the cross section
- In both type I and type II, we will see a sizable XS in  $HH\nu\bar{\nu}$  where  $\lambda_{hHH}$  can be large (if  $m_H$  is light enough)

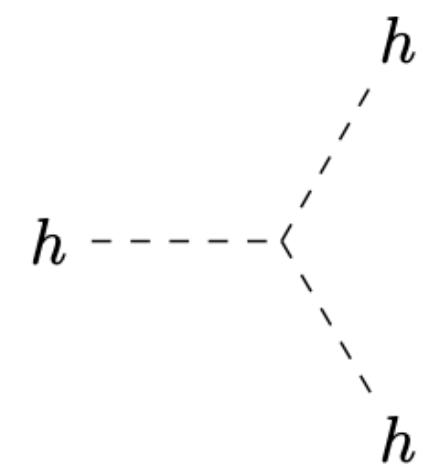
# Summary & Conclusions

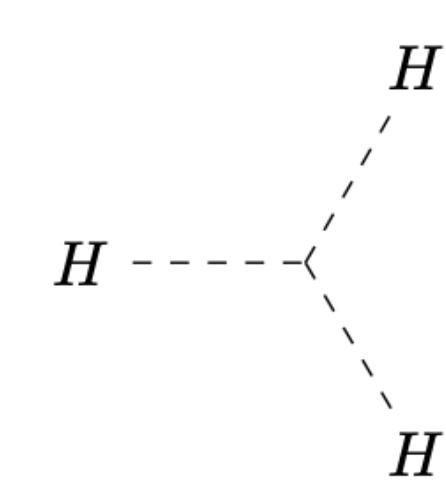
- The di-Higgs production of neutral Higgs bosons is studied at ILC and CLIC ( $e^+e^-$  colliders) in the 2HDM, with the aim to find effects coming from triple Higgs couplings (THC)
  - ▶ Two production channels were studied:  $e^+e^- \rightarrow h_i h_j Z$  and  $e^+e^- \rightarrow h_i h_j \nu\bar{\nu}$
- In  $hh$  production: only sizable distortions at type I (type II is very constrained)
  - ▶ From  $\kappa_\lambda$ , at low invariant mass of the  $hh$  pair, similar to what happens in the SM (extensively studied in the literature)
  - ▶ From  $\lambda_{hhH}$ , through a resonant peak due to the  $H$  boson: a “realistic” study shows that the neutrino channel is better to access this coupling at all center-of-mass energies (specially at CLIC 3TeV)
- The  $HH\nu\bar{\nu} \sim AA\nu\bar{\nu}$  production can have sizable cross sections (around 0.2 fb), in both 2HDM type I and II, mainly because the effects from  $\lambda_{hHH}$  ( $\lambda_{hAA}$ ) (and if the  $H$  boson is light enough to produce two of them)
  - ▶ What about a “future”  $\mu^+\mu^-$  collider???

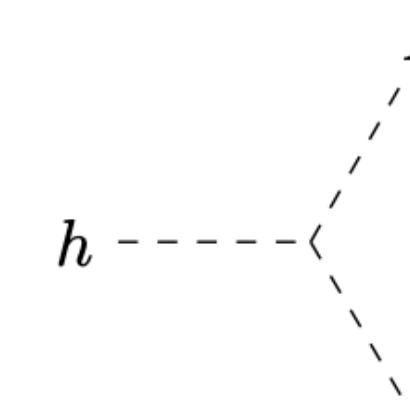
Thanks for your attention :)

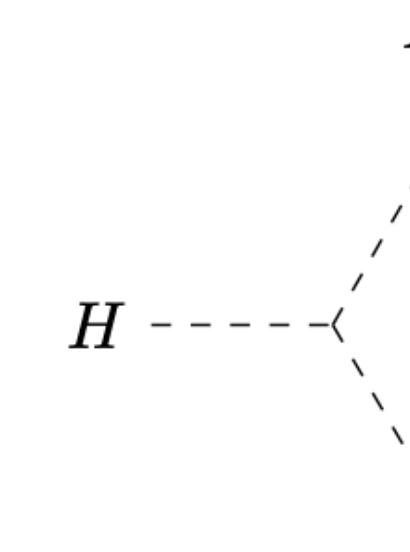
*Questions??*

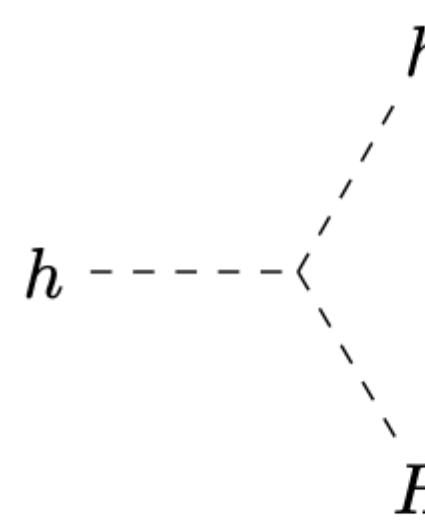
# Back-up, Feynman Rules with THC

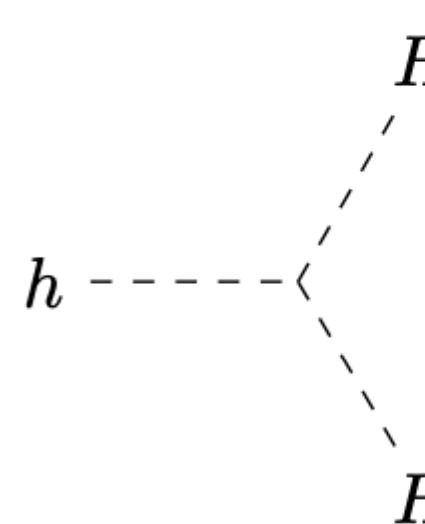
  $= -\frac{3i}{v} \left( 2 \cot 2\beta (m_h^2 - \bar{m}^2) c_{\beta-\alpha}^3 + (3m_h^2 - 2\bar{m}^2) c_{\beta-\alpha}^2 s_{\beta-\alpha} + m_h^2 s_{\beta-\alpha}^3 \right)$

  $= -\frac{3i}{v} \left( (3m_H^2 - 2\bar{m}^2) c_{\beta-\alpha} s_{\beta-\alpha}^2 + 2 \cot 2\beta (\bar{m}^2 - m_H^2) s_{\beta-\alpha}^3 + m_H^2 c_{\beta-\alpha}^3 \right)$

  $= -\frac{i}{v} (s_{\beta-\alpha} (-2\bar{m}^2 + 2m_A^2 + m_h^2) + 2 \cot 2\beta (m_h^2 - \bar{m}^2) c_{\beta-\alpha})$

  $= \frac{i}{v} (2 \cot 2\beta (m_H^2 - \bar{m}^2) s_{\beta-\alpha} - c_{\beta-\alpha} (-2\bar{m}^2 + 2m_A^2 + m_H^2))$

  $= \frac{ic_{\beta-\alpha}}{v} \left( 2\bar{m}^2 (c_{\beta-\alpha}^2 - 3 \cot 2\beta c_{\beta-\alpha} s_{\beta-\alpha} - 2s_{\beta-\alpha}^2) + (2m_h^2 + m_H^2) (-c_{\beta-\alpha}^2 + 2 \cot 2\beta c_{\beta-\alpha} s_{\beta-\alpha} + s_{\beta-\alpha}^2) \right)$

  $= -\frac{is_{\beta-\alpha}}{v} \left( (m_h^2 + 2m_H^2) (-c_{\beta-\alpha}^2 + 2 \cot 2\beta c_{\beta-\alpha} s_{\beta-\alpha} + s_{\beta-\alpha}^2) - 2\bar{m}^2 (-2c_{\beta-\alpha}^2 + 3 \cot 2\beta c_{\beta-\alpha} s_{\beta-\alpha} + s_{\beta-\alpha}^2) \right)$

# Methodology

- Model implemented with FeynRules and computation of the cross section with MadGraph and obtain the Higgs widths with 2HDMC
  - ▶ We do NOT use the Narrow Width Approximation
- Cross sections presented in some benchmark planes that present large THC within the allowed region (based on [\[arXiv2005.10576\]](#)):
  - ▶ Plane  $c_{\beta-\alpha} - \tan \beta$ : Type I with  $m = 1$  TeV and  $m_{12}^2 = m_H^2 \cos^2 \alpha / \tan \beta$
  - ▶ Plane  $c_{\beta-\alpha} - m$ : Type I with  $\tan \beta = 10$  and  $m_{12}^2 = m_H^2 \cos^2 \alpha / \tan \beta$
  - ▶ Plane  $m_{12}^2 - \tan \beta$ : Type II with  $m = 650$  GeV and  $c_{\beta-\alpha} = 0.02$
  - ▶ Plane  $m_{12}^2 - m$ : Type II with  $\tan \beta = 1.5$  and  $c_{\beta-\alpha} = 0.02$
- Access to THC with the XS distributions on the invariant mass of the final  $h_i h_j$  (with ROOT) of some Benchmark Points (BP)

We use the projected luminosities and center-of-mass for ILC and CLIC:

Collider	$\sqrt{s}$ [GeV]	$\mathcal{L}_{\text{int}}$ [ $\text{ab}^{-1}$ ]
ILC	500	4
ILC	1000	8
CLIC	1500	2.5
CLIC	3000	5

Point	Type	$m$	$\tan \beta$	$c_{\beta-\alpha}$	$m_{12}^2$
BP1	I	300	10	0.25	<a href="#">Eq. (8)</a>
BP2	I	500	7.5	0.1	32000
BP3	I	600	10	0.2	<a href="#">Eq. (8)</a>
BP4	I	1000	8.5	0.08	<a href="#">Eq. (8)</a>
BP5	II	650	1.5	0.02	10000

$$(\text{Eq. (8)} \rightarrow m_{12}^2 = m_H^2 \cos^2 \alpha / \tan \beta)$$

# back-up, $hh$ production: $\lambda_{hhH}$ “sensitivity”

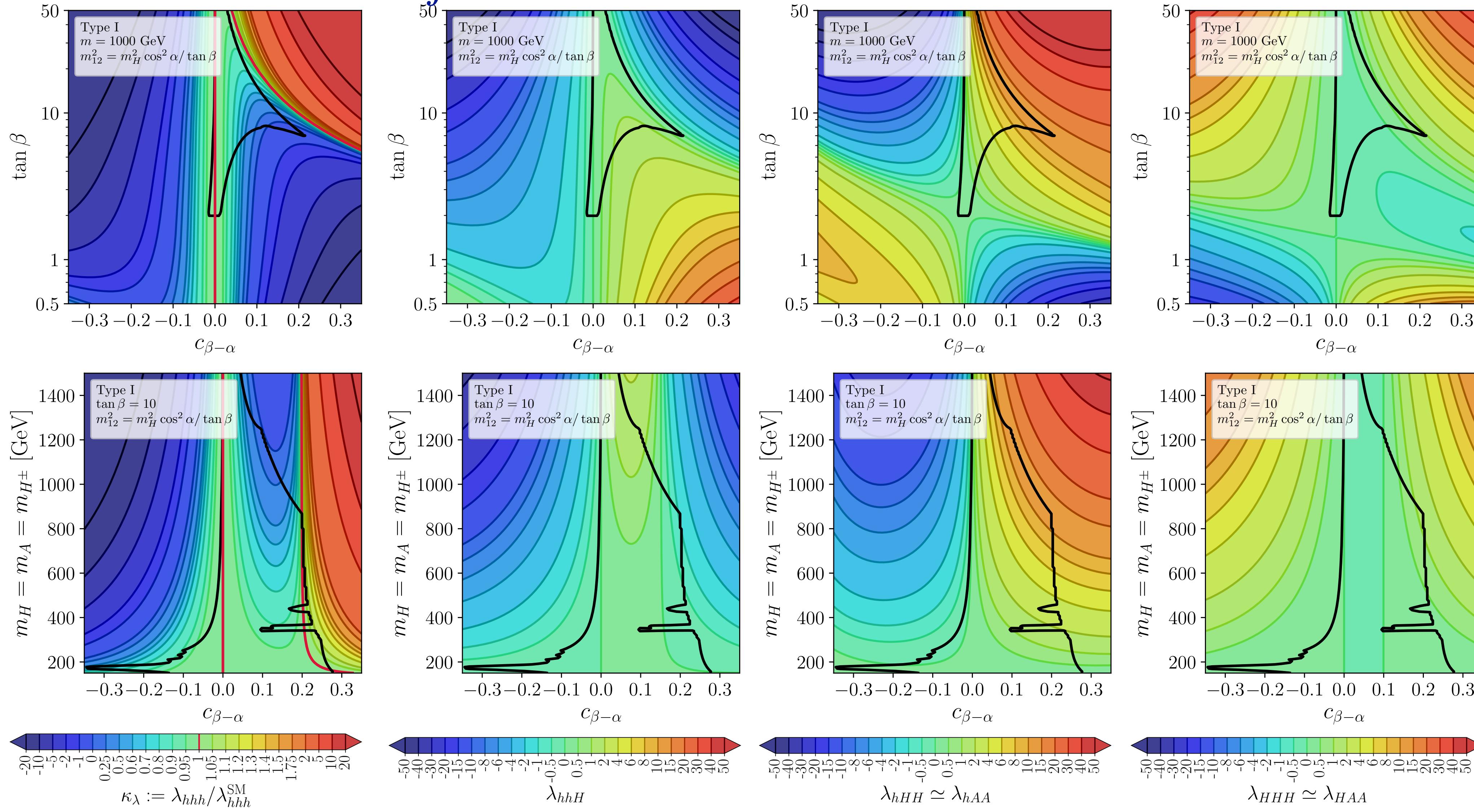
- We propose a estimator to try to determine when the effect of  $\lambda_{hhH}$  will be more prominent
  - Considering a realistic collider situation to reconstruct the experimental signal
  - We consider the events in the range where the XS distribution of the  $H$  mediated diagrams (dark blue lines) is larger than the XS distribution of the diagrams without THC (yellow lines)

$$R = \frac{\bar{N}^R - \bar{N}^C}{\sqrt{\bar{N}^C}}$$

$\bar{N}^R$  refers to the resonance  
and  $\bar{N}^C$  to the “continuum”

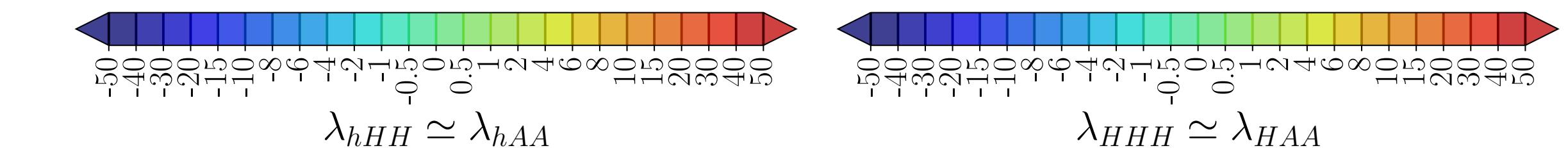
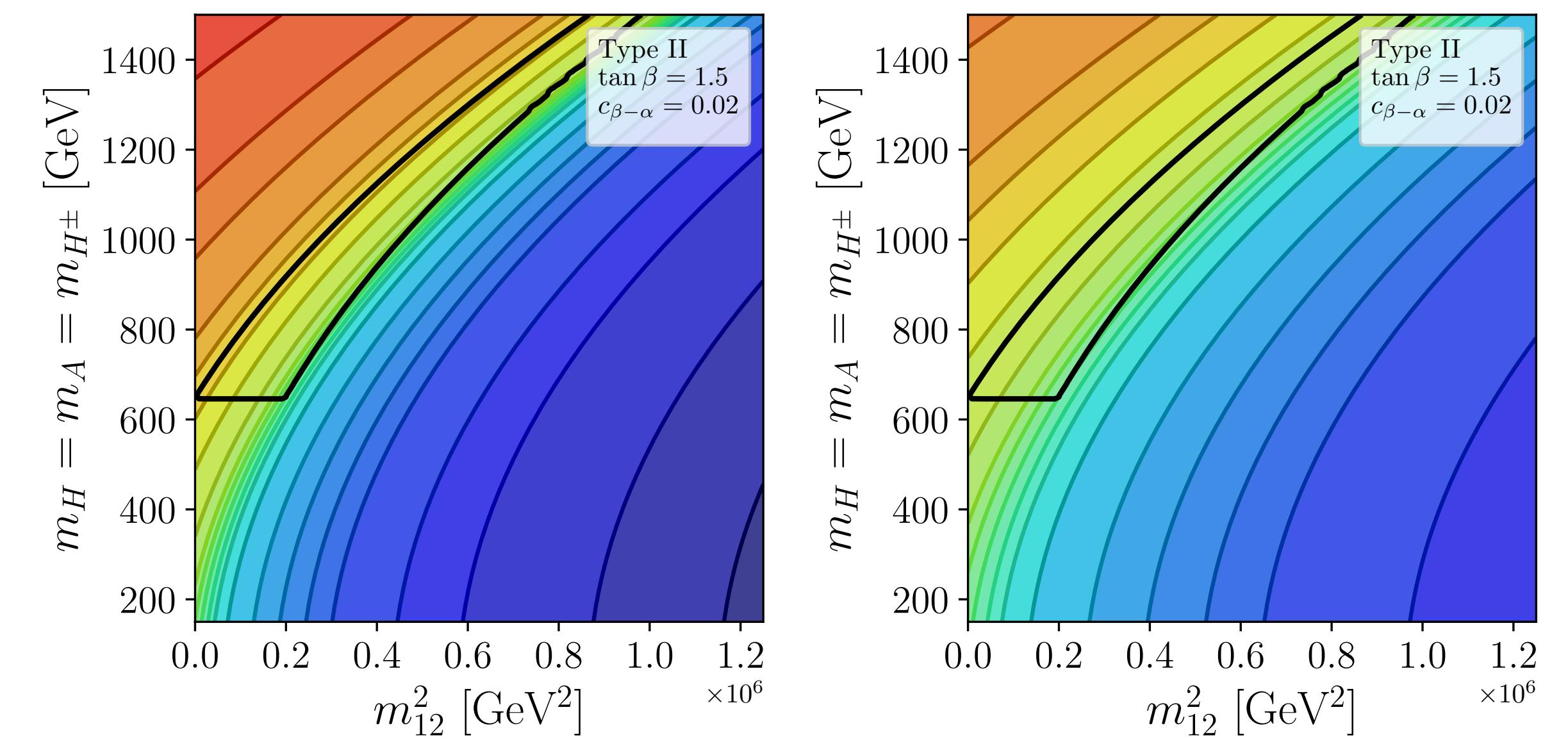
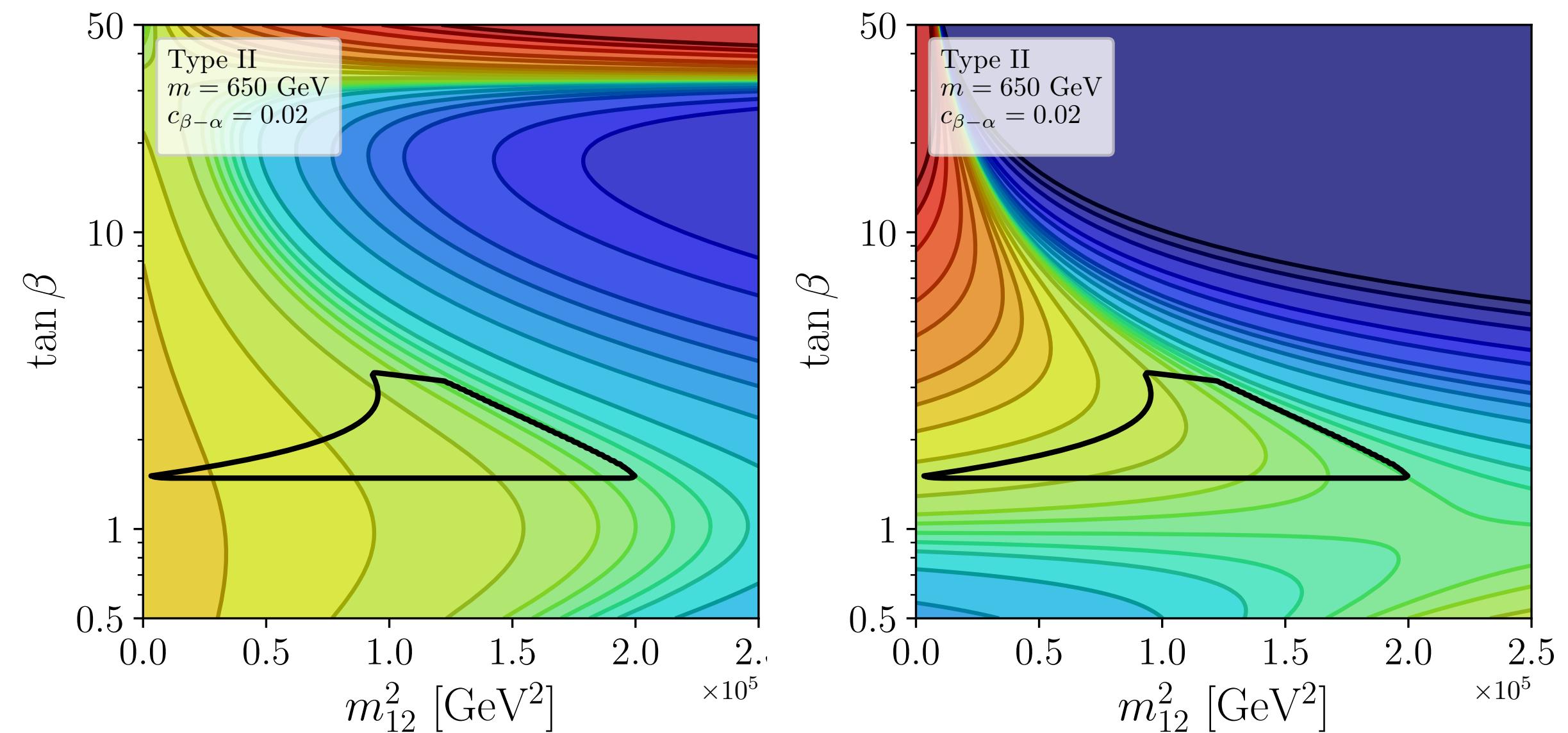
- where  $\bar{N} = N \times \mathcal{A} \times \epsilon_b^4$  with  $N$  the number of total events,  $\mathcal{A} = N_{\text{cuts}}/N_{\text{no cuts}}$  is the acceptance of the collider and  $\epsilon_b \sim 0.8$  the  $b$ -tagging efficiency
- **Cuts:**  $p_T^b > 20 \text{ GeV}$ ,  $|\eta^b| < 2$ ,  $\Delta R_{bb} > 0.4$ ,  $p_T^Z > 20 \text{ GeV}$ ,  $E_T > 20 \text{ GeV}$

# Back-up, $\lambda_{h_i h_j h_k}$



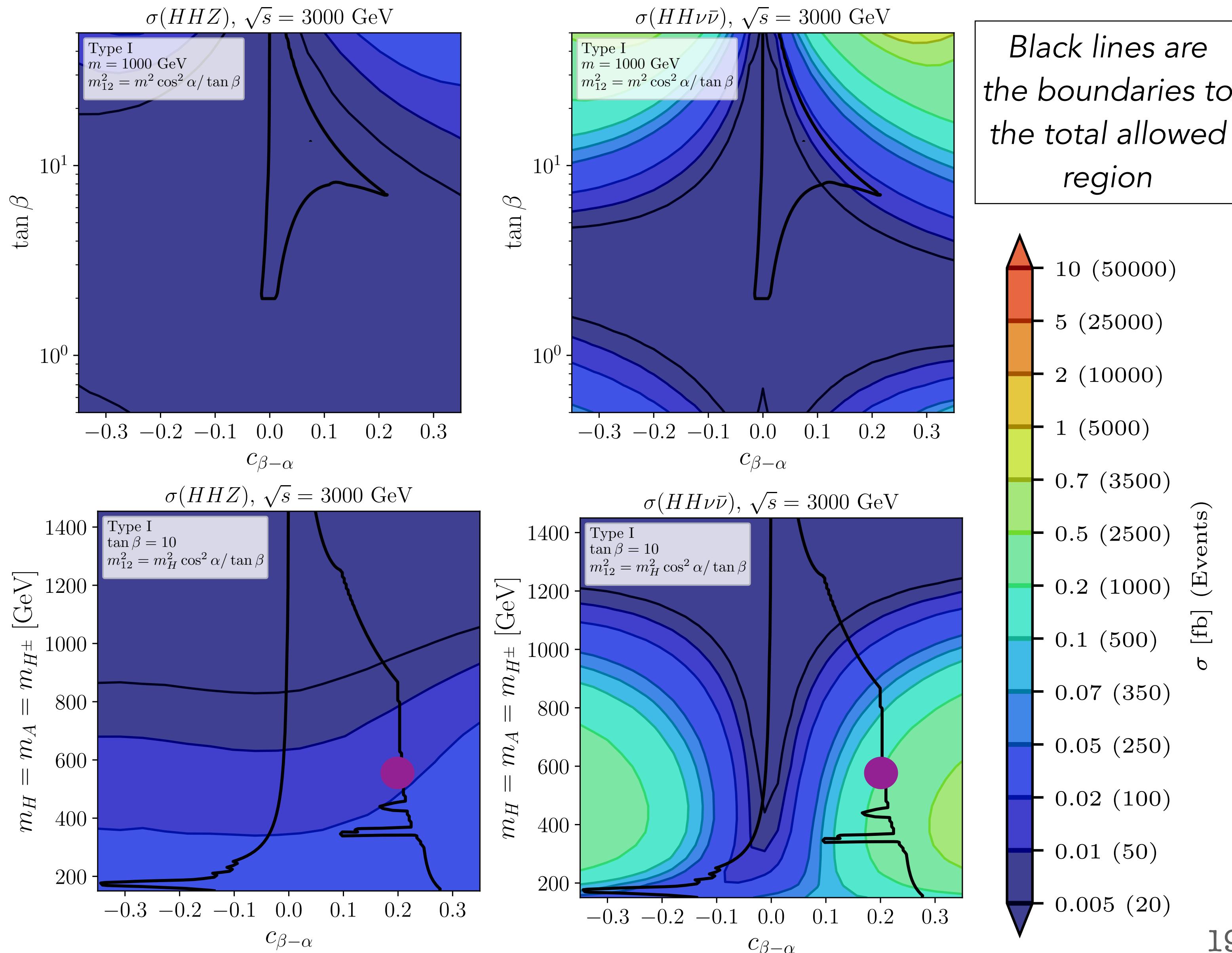
# Back-up,

$\lambda_{h_i h_j h_k}$



# $HH \sim AA$ production, CLIC 3TeV

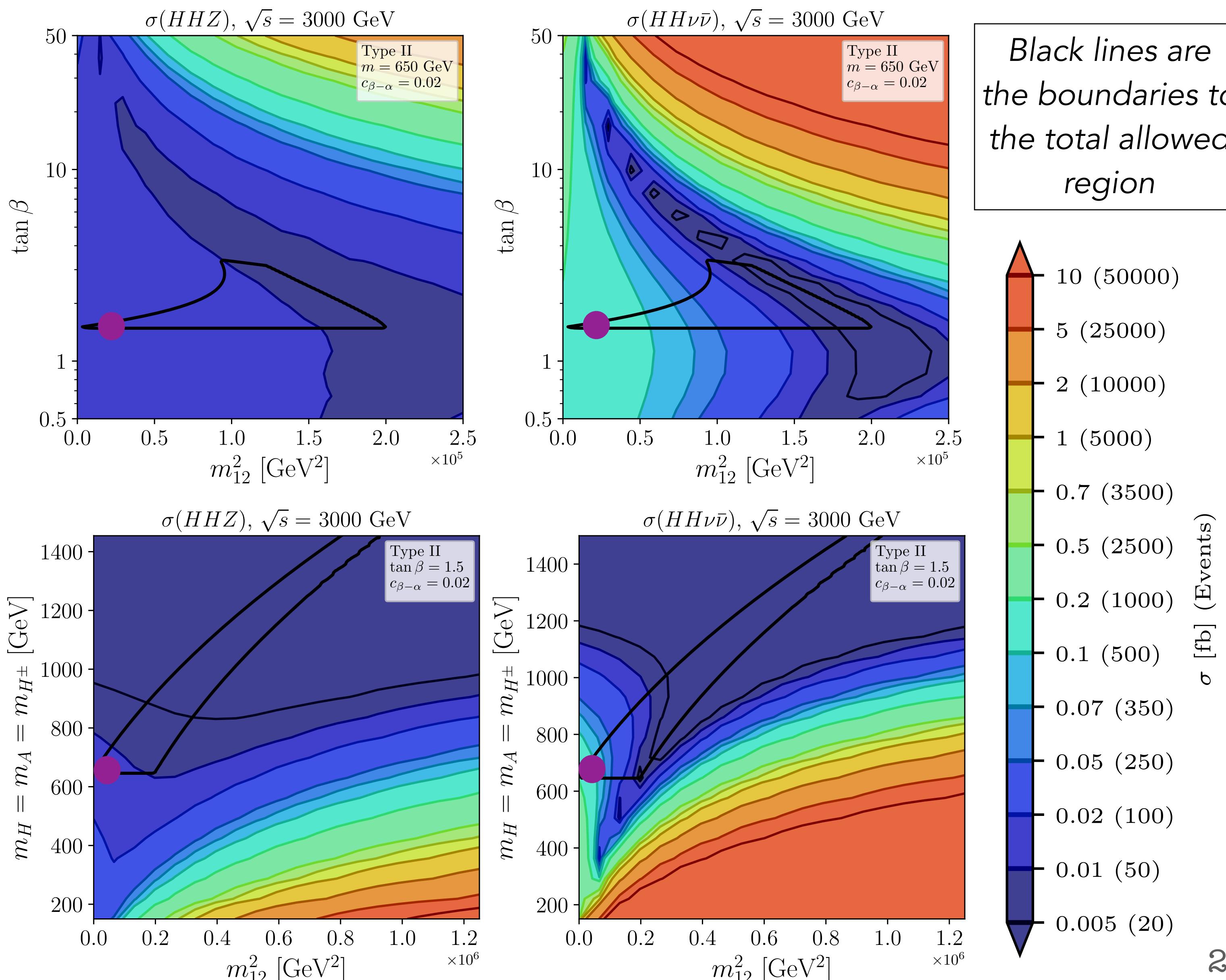
- The  $HH \sim AA$  production can be non-zero even in the alignment limit ( $c_{\beta-\alpha} \rightarrow 0$ )
- Only sizable cross sections inside the allowed region for the neutrino channel
  - Not larger than 0.5 fb
- The sizable cross sections comes from the effect of  $\lambda_{hHH}$  ( $\lambda_{hAA}$ )
  - Effects from  $\lambda_{HHH}$  ( $\lambda_{HAA}$ ) could be important only for larger values of  $c_{\beta-\alpha}$



# $HH \sim AA$ production, CLIC 3TeV (type II)

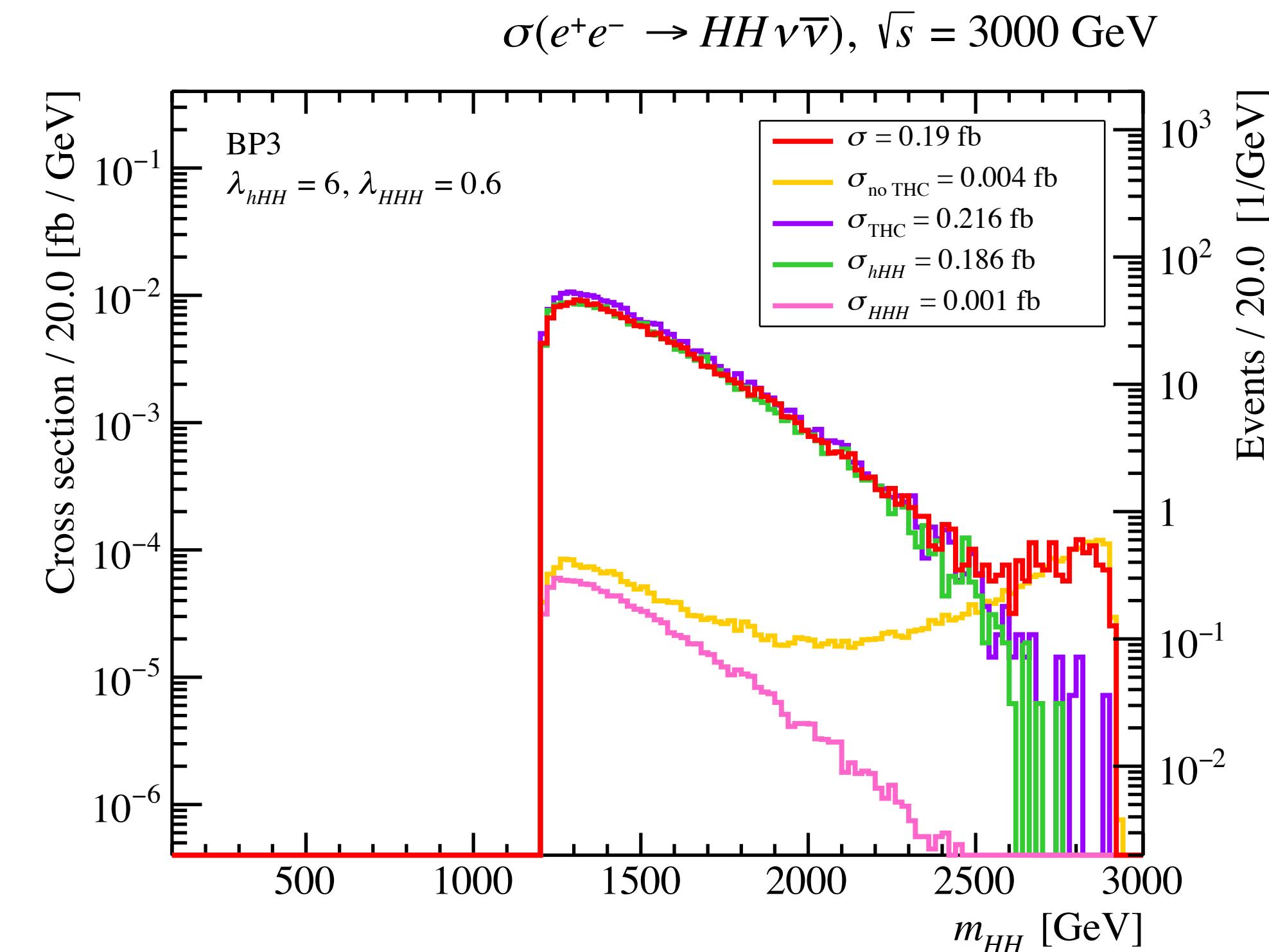
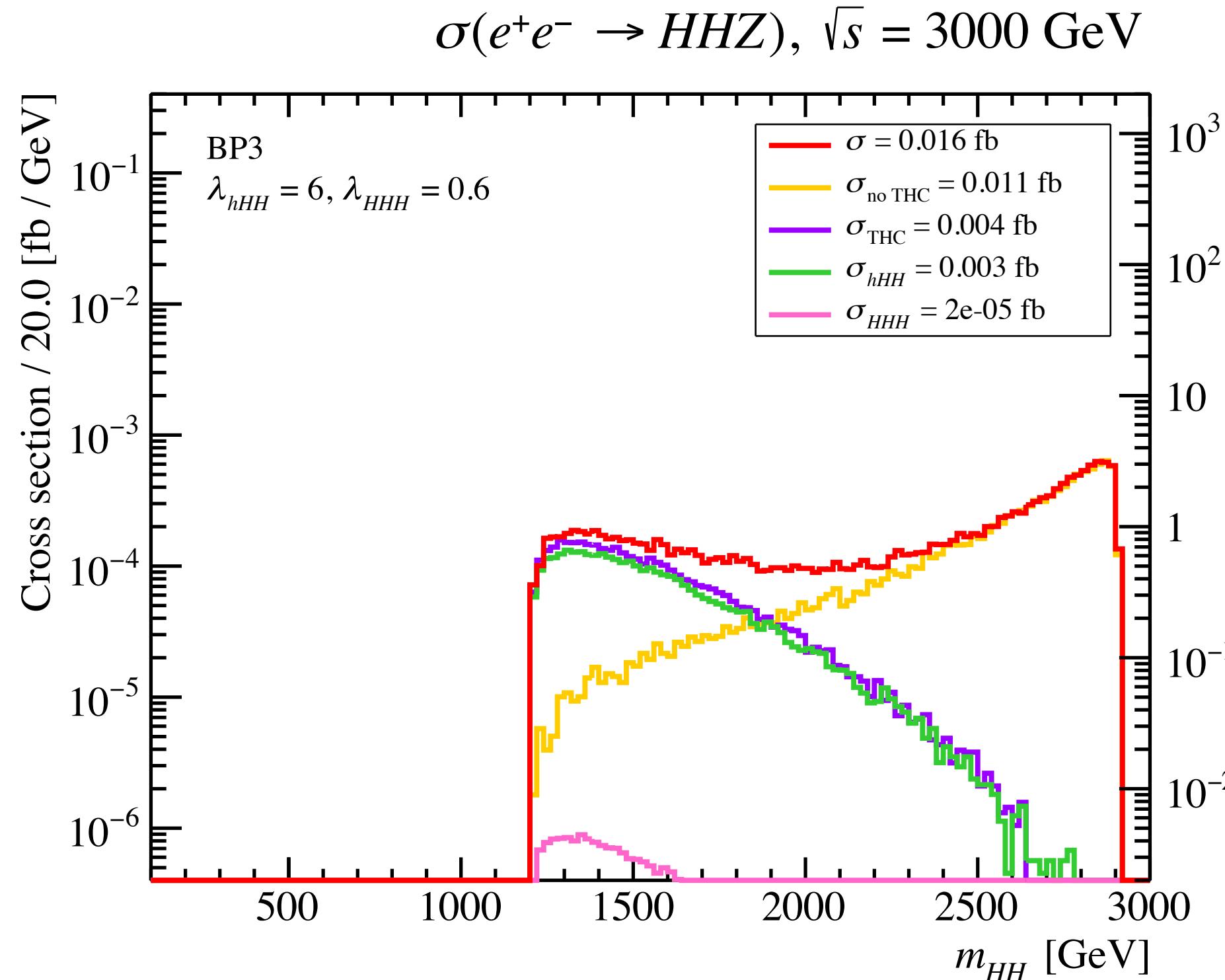
Production cross sections wrt the SM at ILC 500 GeV for  $HHZ$  (left) and  $HH\nu\bar{\nu}$  (right)

- In type II, due to the collider constraints, only  $HH \sim AA$  production is relevant
- Only sizable XS, not larger than 0.5 fb, inside the allowed region for the neutrino channel
- Sizable XS comes from the effect of  $\lambda_{hHH}$  ( $\lambda_{hAA}$ )
  - XS is larger at low  $m_{12}^2$ , that is the region where  $\lambda_{hHH}$  is larger!
- In type I we can obtain similar XS (in other regions of the parameter space)



# $HH \sim AA$ production, CLIC 3TeV, THC dependence

Cross section distribution on the invariant mass of  $HH$ :



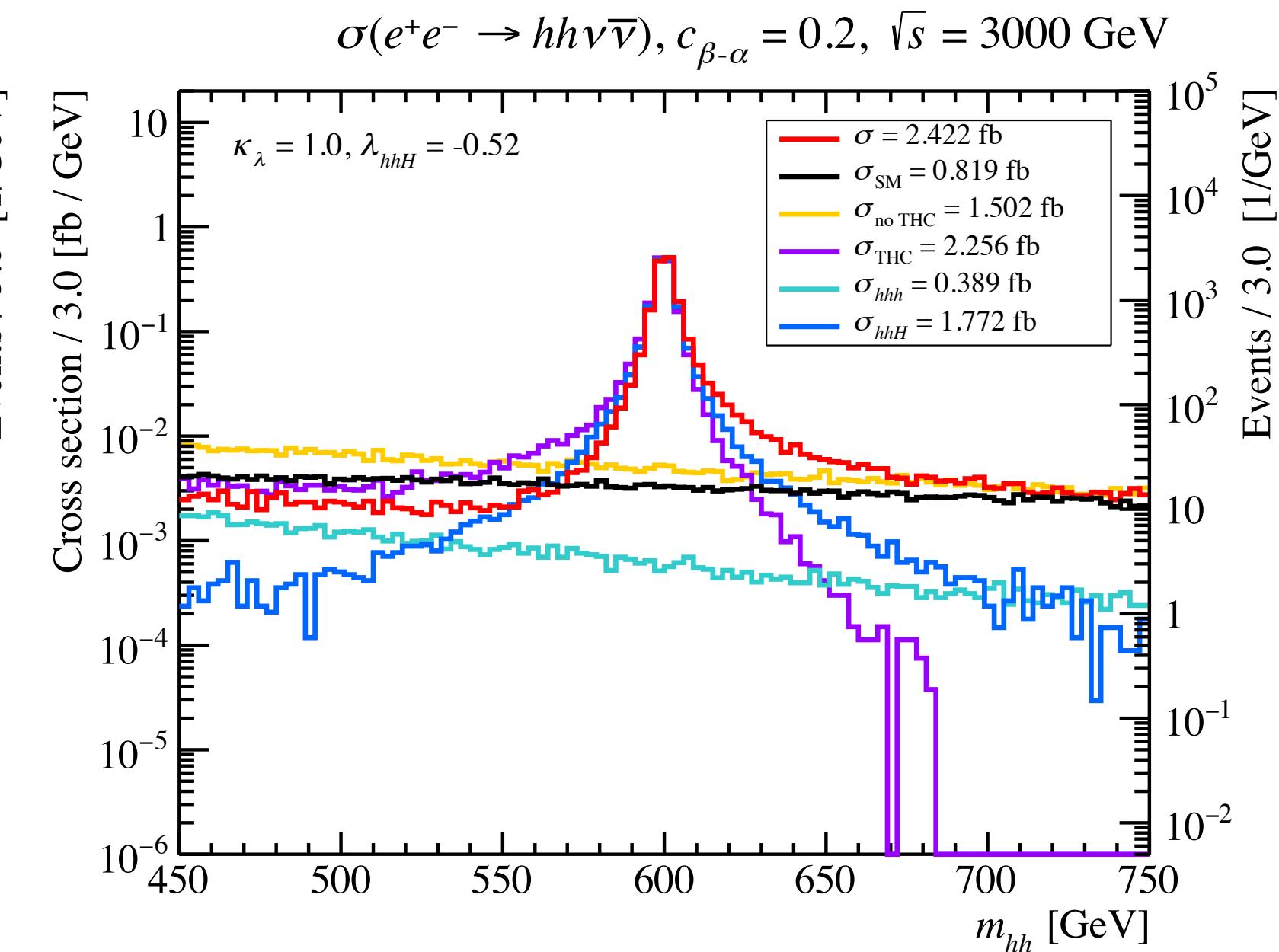
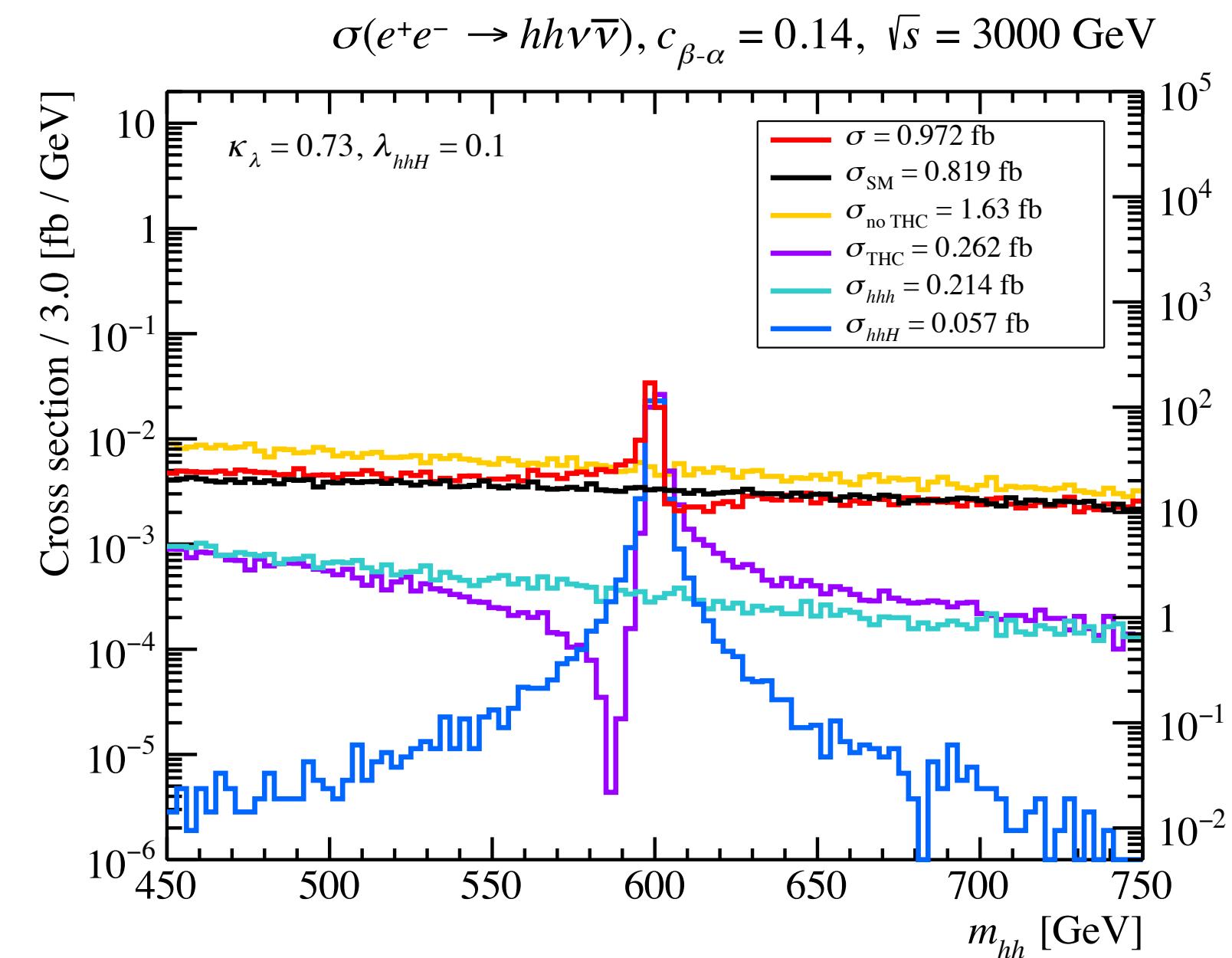
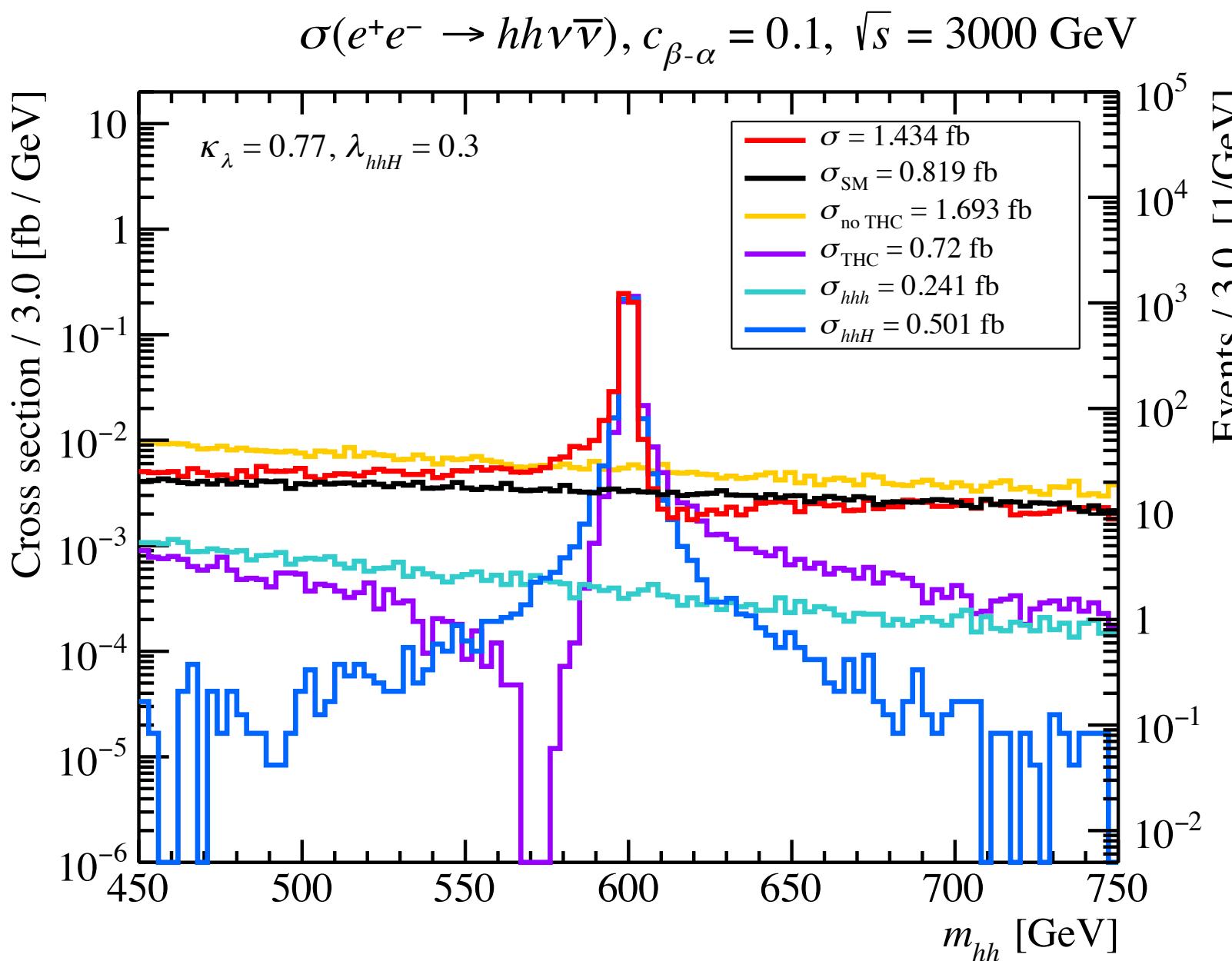
Type I  
 $m = 600 \text{ GeV}$   
 $\tan \beta = 10$   
 $c_{\beta-\alpha} = 0.2$   
 $m_{12}^2 = m_H^2 \cos^2 \alpha / \tan \beta$

- Very small XS and number of events in the  $HHZ$  channel
- Dominant effect in  $HH\nu\bar{\nu}$  comes from  $\lambda_{hHH}$  and it is responsible for almost all the cross section

# $hh$ production, CLIC 3TeV, THC dependence (type I)

Evolution of the  $H$  resonance with  $c_{\beta-\alpha}$  (and indirectly with  $\lambda_{hhH}$ )

Type I,  $m = 600$  GeV,  
 $\tan \beta = 10, m_{12}^2 = m_H^2 \cos^2 \alpha / \tan \beta$



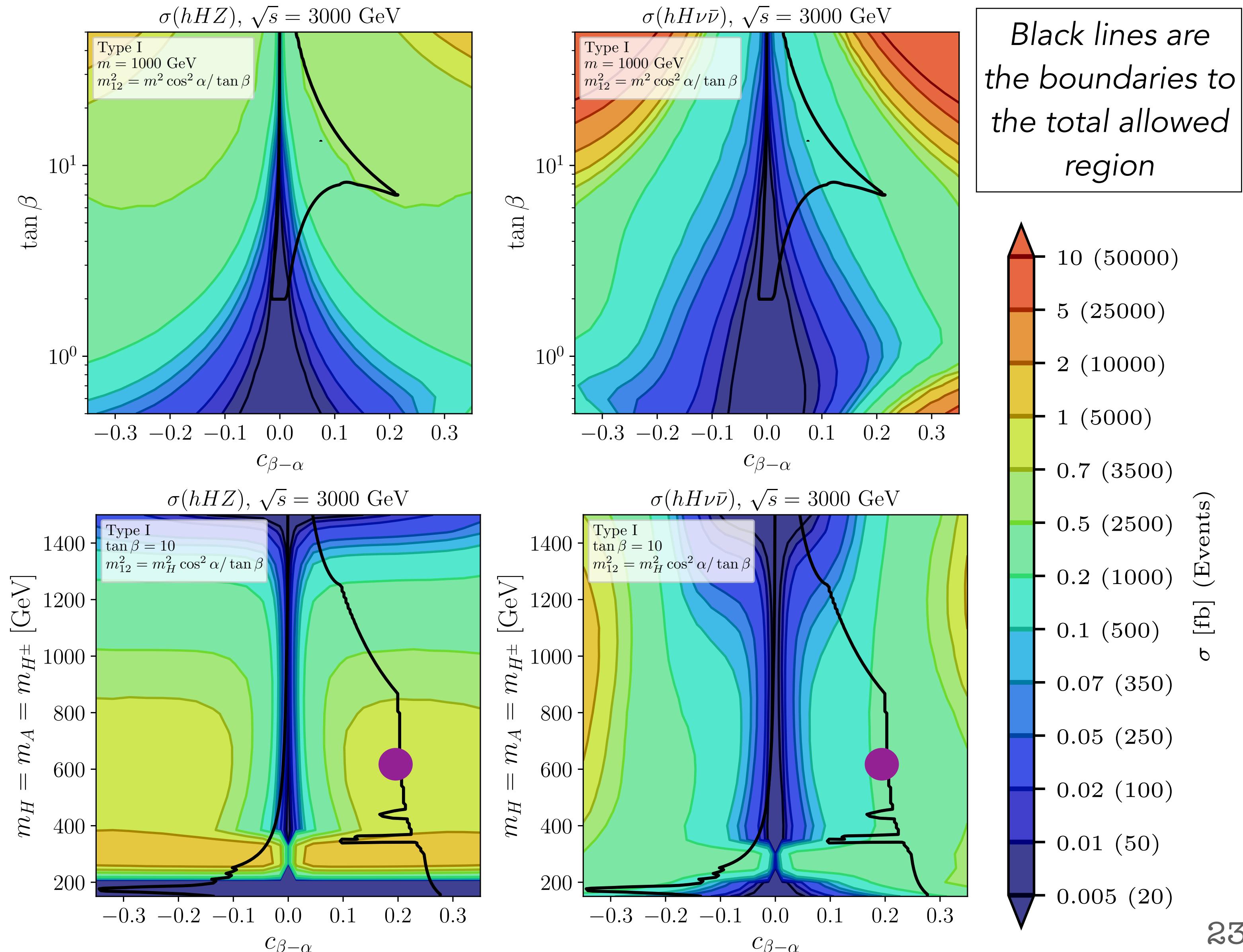
- Height of the resonance depends on  $\lambda_{hhH}$
- For large  $c_{\beta-\alpha}$  the resonance is wider because  $\Gamma_H$  is larger

$\lambda_{hhH} > 0$ :  
 More events at the left of the peak than at the right

$\lambda_{hhH} < 0$ :  
 More events at the right of the peak than at the left

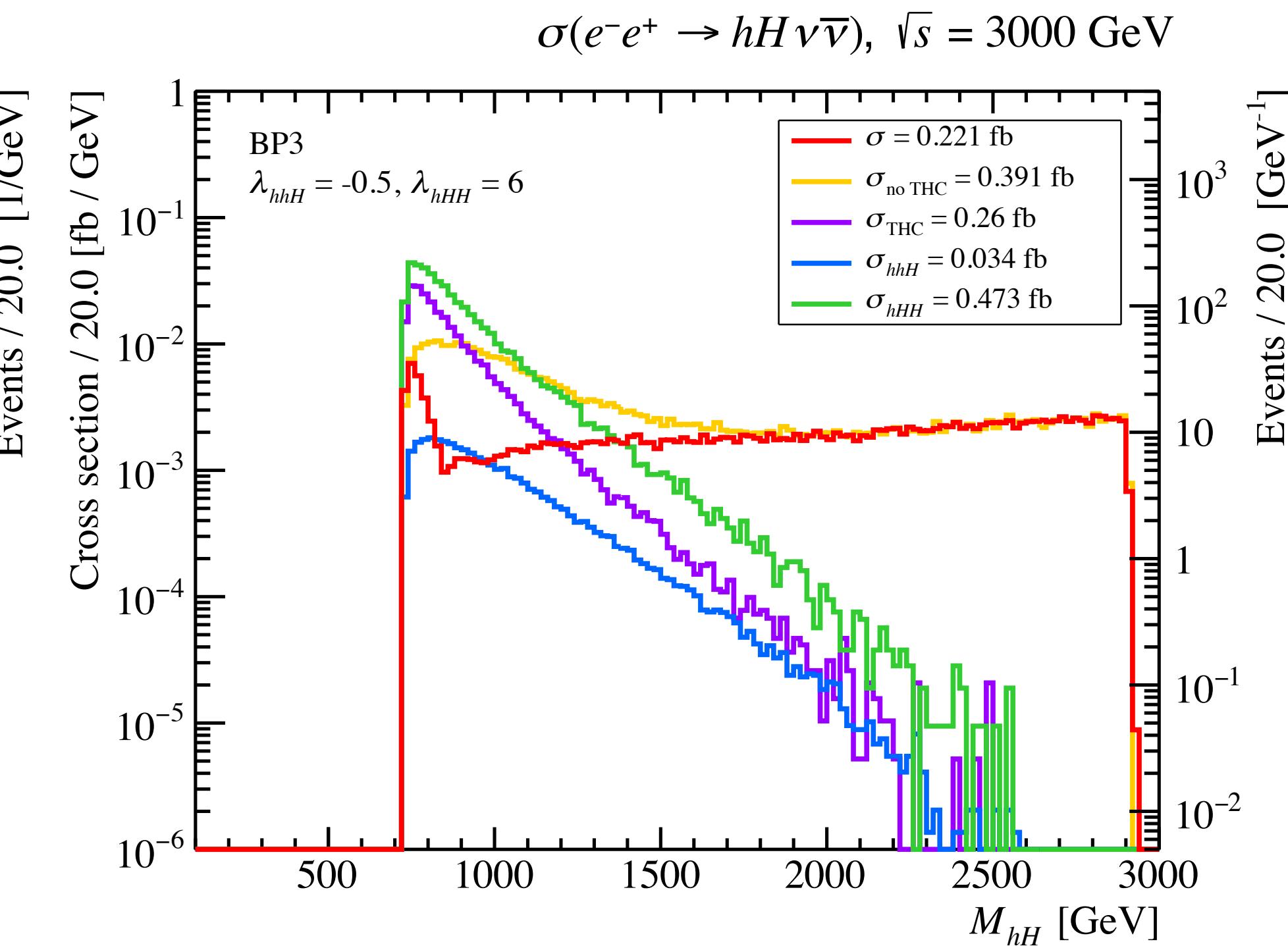
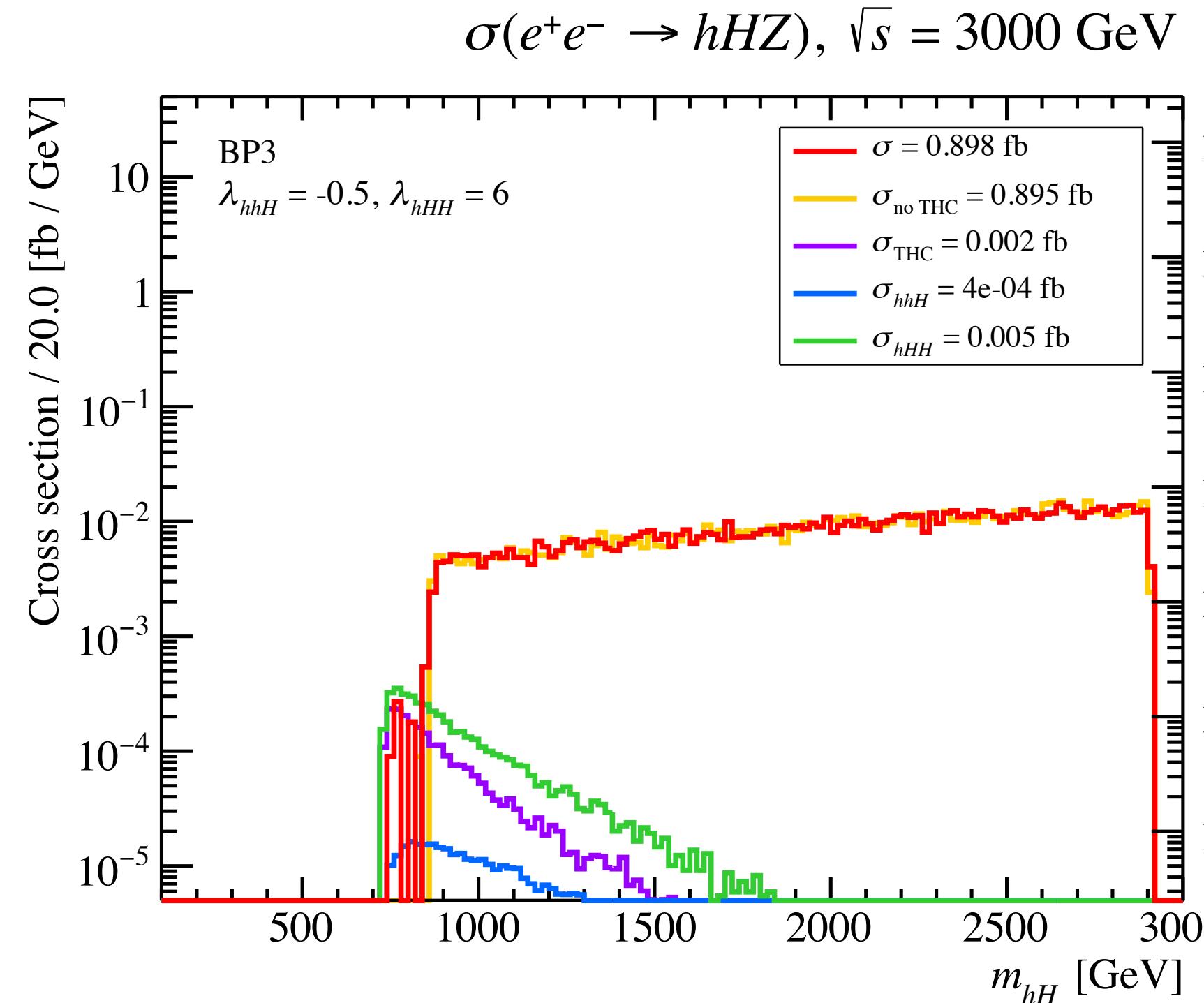
# $hH$ production, CLIC 3TeV (type I)

- The  $hH$  production channels disappear in the alignment limit
- Very strong contribution from resonant  $A$  diagrams in the  $hHZ$  channel
- In the neutrino channel, the effects from  $A$  mediated diagrams mixes with the effects coming from the THC (for this process:  $\lambda_{hhH}$  and  $\lambda_{hHH}$ )



# $hH$ production, CLIC 3TeV, THC dependence (type I)

Cross section distribution on the invariant mass of  $hH$ :



Type I  
 $m = 600 \text{ GeV}$   
 $\tan \beta = 10$   
 $c_{\beta-\alpha} = 0.2$   
 $m_{12}^2 = m_H^2 \cos^2 \alpha / \tan \beta$

- Large “steps” in both channels coming from  $A$  resonant diagrams
- Large effects from  $\lambda_{hhH}$  (dark blue line) and  $\lambda_{hHH}$  (green line) at low  $m_{hH}$  only in the neutrino channel at the  $m_{hH}$  threshold
- The combined effect of both THC (purple line) depends on their relative sign

# Triple Higgs Couplings (THC), Type I

- Two benchmark planes:
  - ▶ Plane  $c_{\beta-\alpha} - \tan \beta$ : Type I with  $m = 1$  TeV and  $m_{12}^2 = m_H^2 \cos^2 \alpha / \tan \beta$
  - ▶ Plane  $c_{\beta-\alpha} - m$ : Type I with  $\tan \beta = 10$  and  $m_{12}^2 = m_H^2 \cos^2 \alpha / \tan \beta$
- $\kappa_\lambda := \lambda_{hhh} / \lambda_{hhh}^{\text{SM}}$

Lowest value  $\kappa_\lambda = 1$  at the “tip” of  $c_{\beta-\alpha} - \tan \beta$  plane

$$\lambda_{hhH}$$

Larger positive values around  $c_{\beta-\alpha} \simeq 0.05$  and large negative values at large  $c_{\beta-\alpha}$  in  $c_{\beta-\alpha} - m$  plane

⇒ Explore the production cross section of  $hhZ$  and  $hh\nu\bar{\nu}$  in these planes

