

Explaining the Cabibbo Angle Anomaly

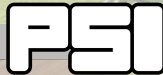
Claudio Andrea Manzari
UNIVERSITY OF ZÜRICH

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University of
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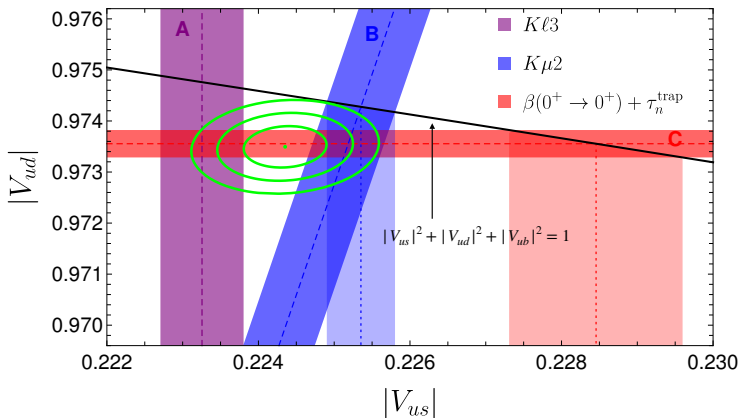
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Outline

- The Cabibbo Angle Anomaly
- SMEFT analysis
- Simplified Models
- Conclusions and prospects

The Cabibbo Angle Anomaly I



$$|V_{ud}|^2 + |V_{us}|^2 + |V_{ub}|^2 = 0.9985(5)$$

$$\frac{|V_{ud}|^2}{|V_{us}|^2} \approx 20$$

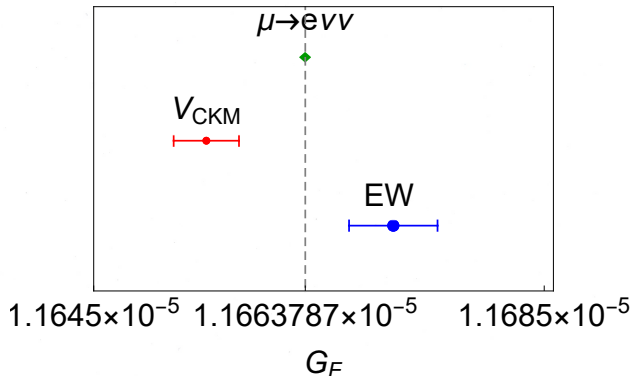
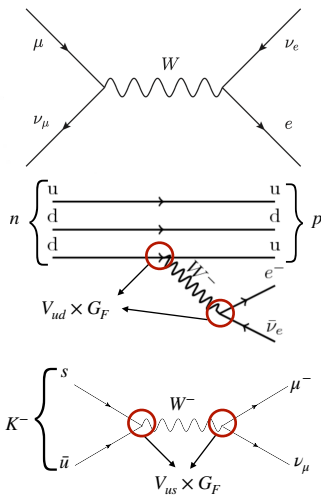


$$|V_{ud}|^2(1 - \epsilon)^2 + |V_{us}|^2 + |V_{ub}|^2$$

Note that a deviation from unitarity is also observed in the first column of the CKM matrix

$$|V_{ud}|^2 + |V_{cd}|^2 + |V_{td}|^2 = 0.9970(18), \text{ strengthening the idea of NP related to } V_{ud}$$

The Cabibbo Angle Anomaly II



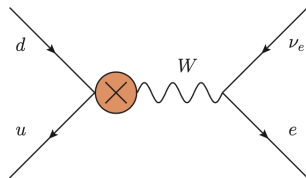
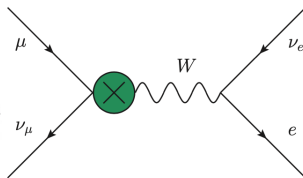
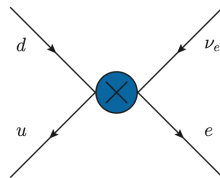
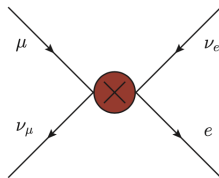
$$G_F^\mu = 1.1663787(6) \times 10^{-5} \text{ GeV}^{-2}$$

$$G_F^{CKM} = 1.16550(29) \times 10^{-5} \text{ GeV}^{-2}$$

SMEFT analysis

BSM explanations can be grouped into 4 classes using an EFT approach with gauge-invariant dimension 6 operators ([2102.02825](#) Crivellin, Hoferichter, C.A.M.)

- ▶ four-fermion operators in $\mu \rightarrow e\nu\nu$;
- ▶ four-fermion operators in $u \rightarrow d e \nu$;
- ▶ modified W - u - d couplings;
- ▶ modified W - ℓ - ν couplings.



4-fermion operators in $\mu \rightarrow e\nu\nu$

The only viable mechanism to modify the extraction of G_F proceeds via a modification of the SM operator

$$Q_{\ell\ell}^{2112} = (\bar{\ell}_2 \gamma^\mu \ell_1) (\bar{\ell}_1 \gamma^\mu \ell_2)$$

To bring data into agreement within 1σ we need

$$C_{\ell\ell}^{2112} = -1.4 \times 10^{-3} G_F$$

Constraints: G_F enters in the computation of EW precision observables
Within the reach of future e^+e^- colliders

4-fermion operators in $u \rightarrow dev$

We need constructive interference with the SM in β decays. The only possibility is

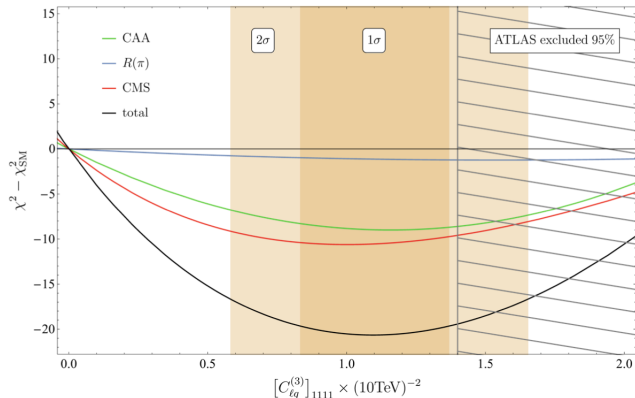
$$Q_{\ell q}^{(3)1111} = (\bar{\ell}_1 \gamma^\mu \tau^I \ell_1) (\bar{q}_1 \gamma^\mu \tau^I q_1)$$

The CAA at 1σ prefers

$$C_{\ell q}^{(3)1111} = \frac{1.22(4)}{(10\text{TeV})^2}$$

CMS $\equiv R_{\frac{e+e^-}{\mu+\mu^-}}$ di-lepton searches

$$R_\pi \equiv \frac{\pi \rightarrow \mu\nu}{\pi \rightarrow e\nu}$$



W - u - d couplings

Here the goal is to modify the extraction of V_{us} and V_{ud} on the quark side. Two solutions are possible

$$Q_{\phi ud}^{ij} = \tilde{\phi} i D_{\mu} \phi \bar{u}_i \gamma^{\mu} d_j$$

Generates right-handed W -quark couplings. In addition, a right-handed $W - u - s$ coupling could also account for the difference between $K_{\ell 2}$ and $K_{\ell 3}$ decays

$$Q_{\phi q}^{(3)ij} = \phi^{\dagger} i \overleftrightarrow{D}_{\mu} \phi \bar{q}_i \gamma^{\mu} \tau^I q_j$$

Due to $SU(2)_L$ invariance, in general effects in $\Delta F = 2$ processes as well as in Z decays are generated.

W - l - ν couplings

Only one operator generates W - l - ν couplings at tree level

$$Q_{\phi l}^{(3)ij} = \phi^\dagger \overleftrightarrow{D}_\mu^I \phi \bar{l}_i \gamma^\mu \tau^I l_j.$$

$C_{\phi l}^{(3)11}$ affects β decays and the G_F in the same way \implies no effect on CAA!

$C_{\phi l}^{(3)22}$ only enters in muon decay. CAA points to $C_{\phi l}^{(3)22} > 0$.

Constraints: EW precision Observables, Tests of Lepton Flavour Universality

Model Building

2 Mechanisms to solve the Cabibbo Angle Anomaly:

- ▶ new physics in G_F :
 - **Singly Charged Scalar Singlet** ([2010.14504](#) Crivellin, M., Algueró, Matias)
 - **Vector-like Leptons** ([2008.01113](#) Crivellin, Kirk, C.A.M., Montull)
 - **Vector Boson Triplet** ([2005.13542](#) Capdevila, Crivellin, C.A.M., Montull)

- ▶ new physics in β decay:
 - **Vector Boson Singlet** ([2104.07680](#) Buras, Crivellin, Kirk, C.A.M., Montull)
 - **Vector-like Quarks** ([2001.02853](#) Cheung, Keung, Lu, Tseng)
 - **Vector-like Leptons** ([2008.01113](#) Crivellin, Kirk, C.A.M., Montull)
 - **Vector Boson Triplet** ([2005.13542](#) Capdevila, Crivellin, C.A.M., Montull)

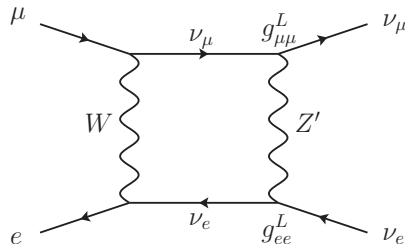
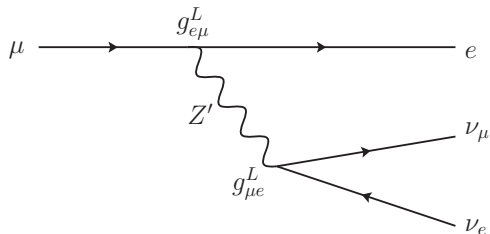
Vector Boson Singlet: Z'

- Constraints: $\mu \rightarrow e\gamma$, $\mu \rightarrow e$ conversion, EW data, LEP 4-electron bounds



LFU scenario ✗

LFUV scenario \implies can alleviate CAA ([2104.07680](#))



Vector-like Quarks I

- 7 possible Vector-like Quarks representations under $SU(3)_C \times SU(2)_L \times U(1)_Y$

Only 3 of them can generate

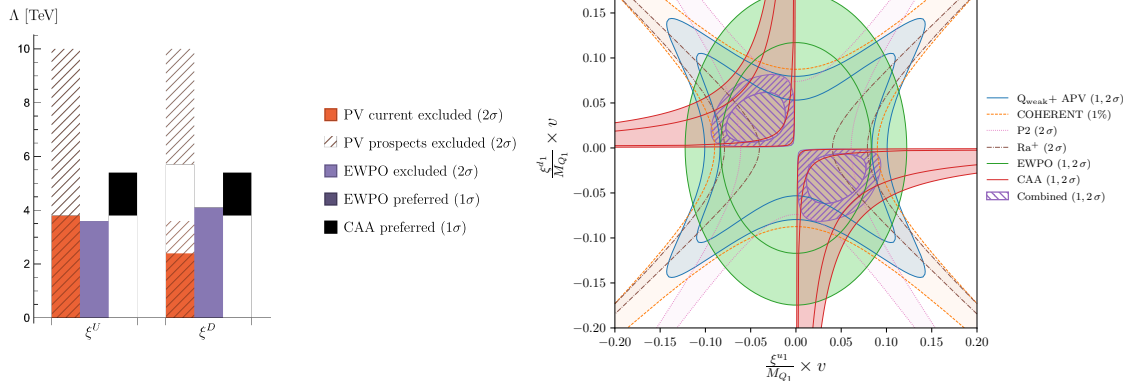
$$C_{\phi q}^{(3)11} < 0 \quad \text{or} \quad C_{\phi ud}^{11} < 0$$



U , D and Q_1 coupling to up- and down-quarks

	$SU(3)$	$SU(2)_L$	$U(1)_Y$
U	3	1	2/3
D	3	1	-1/3
Q_1	3	2	1/6
Q_5	3	2	-5/6
Q_7	3	2	7/6
T_1	3	3	-1/3
T_2	3	3	2/3

Vector-like Quarks II



Regions preferred by the CAA and excluded by EWPO and PV experiments (for couplings fixed to unity on the left).

Vector-like Leptons

There are 6 possible representations under $U(1)_Y \times SU(2)_L$ generating different patterns of $Q_{\phi\ell}^3$ and $Q_{\phi\ell}^1$.

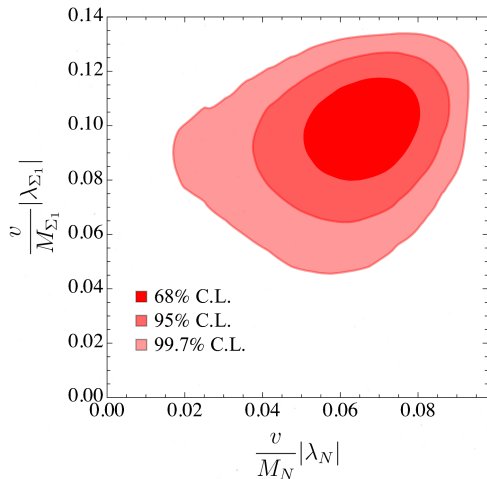
These operators modify W and Z boson couplings



EW precision observables and tests of LFU (π , K , τ decays) have to be considered.

	$SU(3)_c$	$SU(2)_L$	$U(1)_Y$
ℓ	1	2	-1/2
e	1	1	-1
ϕ	1	2	1/2
N	1	1	0
E	1	1	-1
$\Delta_1 = (\Delta_1^0, \Delta_1^-)$	1	2	-1/2
$\Delta_3 = (\Delta_3^-, \Delta_3^{--})$	1	2	-3/2
$\Sigma_0 = (\Sigma_0^+, \Sigma_0^0, \Sigma_0^-)$	1	3	0
$\Sigma_1 = (\Sigma_1^0, \Sigma_1^-, \Sigma_1^{--})$	1	3	-1

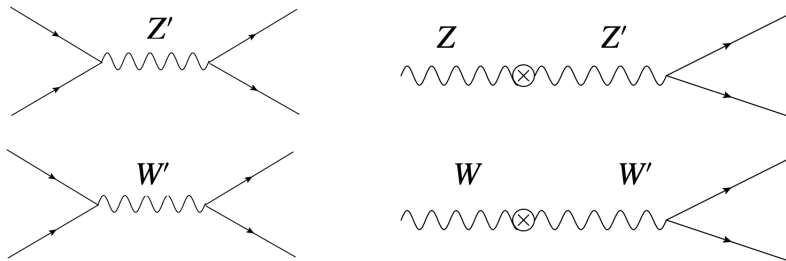
Vector-like Leptons



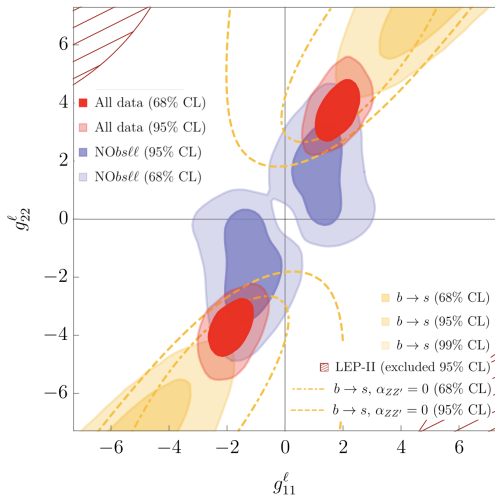
- ▶ each representation alone does not improve the fit w.r.t the SM
- ▶ there is a **minimal model strongly improving the agreement with data** made of a singlet N coupling with electrons and a triplet Σ_1 coupling with muons! ([2008.01113](#))

Vector Boson Triplet

- ▶ $SU(2)_L$ triplet of heavy vector bosons with zero hypercharge: W' , Z'
- ▶ the W' generates $Q_{\ell\ell}^{2112}$ at tree level and $Q_{\phi\ell}^{(3)}$, $Q_{\phi\ell}^{(1)}$ via $W - W'$ mixing
- ▶ The Z' allows for interesting connections with $b \rightarrow s\ell\ell$



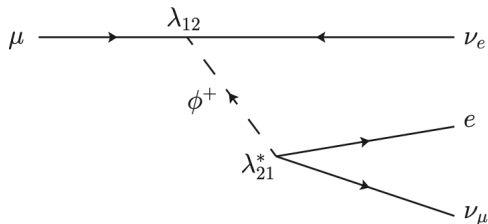
Vector Boson Triplet



- ▶ several observables need to be included: CAA, EW data, LFU tests, LHC bounds, parity violation experiments, $b \rightarrow sll$ and $B_s - \bar{B}_s$
- ▶ The global fit improves the agreement with $b \rightarrow sll$ data by $\approx 5\sigma$ compared to the SM, and solve the CAA. ([2005.13542](#))

The Singly Charged Scalar Singlet

- ▶ $SU(2)_L \times SU(3)_C$ singlet with hypercharge +1
- ▶ can only couple off-diagonally to leptons \implies generates $Q_{\ell\ell}^{2112}$



$$C_{\phi\ell}^{2112} \propto \frac{|\lambda_{12}|^2}{M^2} \stackrel{!}{>} 0$$

EW Fit + CAA



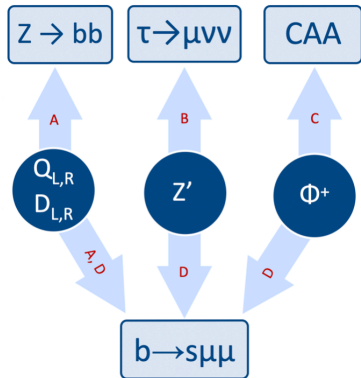
$$|\lambda_{12}|^2 = (0.043 \pm 0.010) \frac{m_{\phi^+}^2}{\text{TeV}^2}$$

The Singly Charged Scalar Singlet

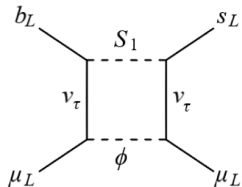
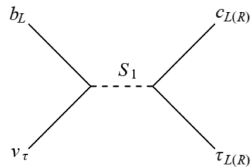
- ▶ it allows very interesting correlations with other observables

$$b \rightarrow sll + Z \rightarrow \bar{b}b + \tau \rightarrow \mu\nu\nu$$

(2010.14504)



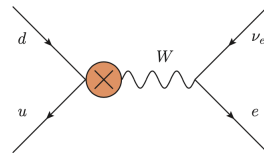
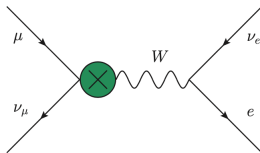
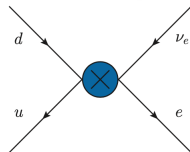
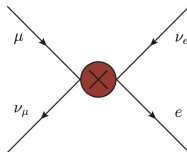
$$b \rightarrow sll + (g - 2)_\mu \text{ (2104.05730)}$$



Conclusions

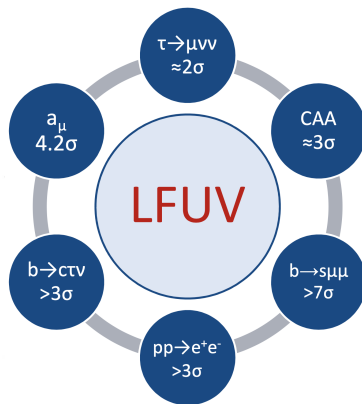
- ▶ The Cabibbo Angle Anomaly is a deviation from unitarity observed in the 1st row and column of the CKM matrix at the 3σ level

- ▶ If this tension is due to NP, there are only 4 SMEFT operators at the dim-6 level which can explain it



- ▶ The NP simplified models able to appropriately generate these operators are: VLQs, VLLs, a Z' , a Vector Boson Triplet and a Singly Charged Scalar Singlet
- ▶ Interesting model-dependent correlations with other anomalies arise!

- ▶ It is worth to look at the CAA as a hint of LFUV!



Backup

Future Prospects

- ▶ Improvements in the determination of CKM unitarity:
 - a. advances in nuclear-structure and EW radiative corrections treatment
 - b. experimental developments in the determination from neutron decay, $K_{\ell 3}$ and complementary constraint on $|V_{ud}|/|V_{us}|$ via pion β decay
 - c. improved measurements of $|V_{cd}|$ from D decays to bring the precision of the first column CKM unitarity competitive

- ▶ Improvement in a second G_F determination from the EW fit: Belle-II, FCC-ee, ILC, CEPC, or CLIC (m_t and m_W)