



Probing New Physics with Heavy Hadron decays

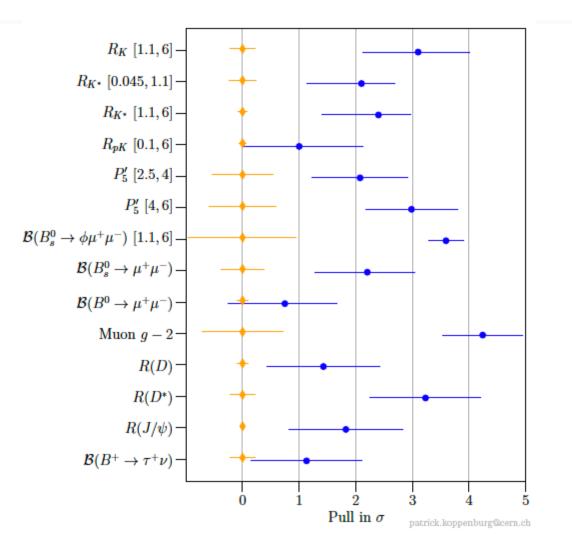
Fulvia De Fazio INFN Bari

EPS 2021 July 26-30 Hamburg

 $\begin{array}{c} \mbox{based on:} \\ \mbox{Inclusive semileptonic } \Lambda_{\rm b} \mbox{ decays in the Standard Model and beyond} \\ \mbox{P. Colangelo, F. Loparco, FDF} \\ \mbox{JHEP 11 (2020) 032 , arXiv:2006.13759} \end{array}$ 



# New & Old Anomalies



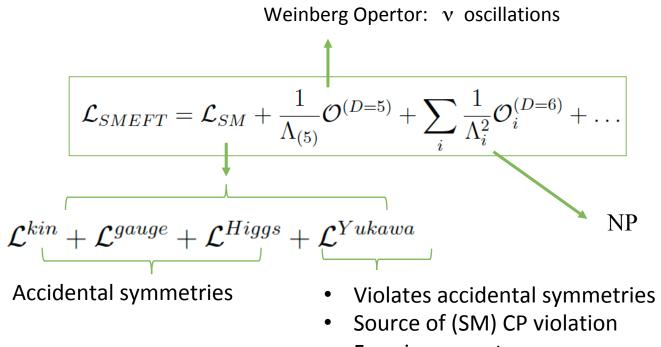
1) SM allowed processes: deviations from expectations  $\rightarrow$  NP

2) SM forbidden processes: observation  $\rightarrow$  NP

- many hints of LFU violation → relation between 1) and 2) expected
- Common origin of the anomalies?
   ex: Problems with V<sub>cb</sub> and V<sub>ub</sub> determinations might be correlated with observed anomalies in tree level modes
   P. Colangelo, FDF

PRD 95 (17) 011701

- tree level decays ( $R(D^{(*)})$  & co.)
- loop (rare) decays ( $R(K^{(*)}), P'_5, ...$ )
- puzzling quantities (V<sub>cb</sub>, V<sub>ub</sub>,  $\epsilon'/\epsilon$ , (g-2)<sub>µ</sub>...).
- o LFV decays  $\tau \rightarrow 3\mu, \mu \rightarrow e \gamma \dots$



• Fermion mass terms

### Exclusive b $\rightarrow$ c,u modes

- Identifications of suitable observables
- Issue of FF uncertainties
- b  $\rightarrow$  c unsolved debate: role of the parametrization: BGL vs CLN in heavy-to-heavy FF Proposed to reconcile inclusive vs exclusive V<sub>cb</sub> determinations

🦻 what about V<sub>ub</sub>?

# Inclusive b $\rightarrow$ c,u modes (exploit HQE)

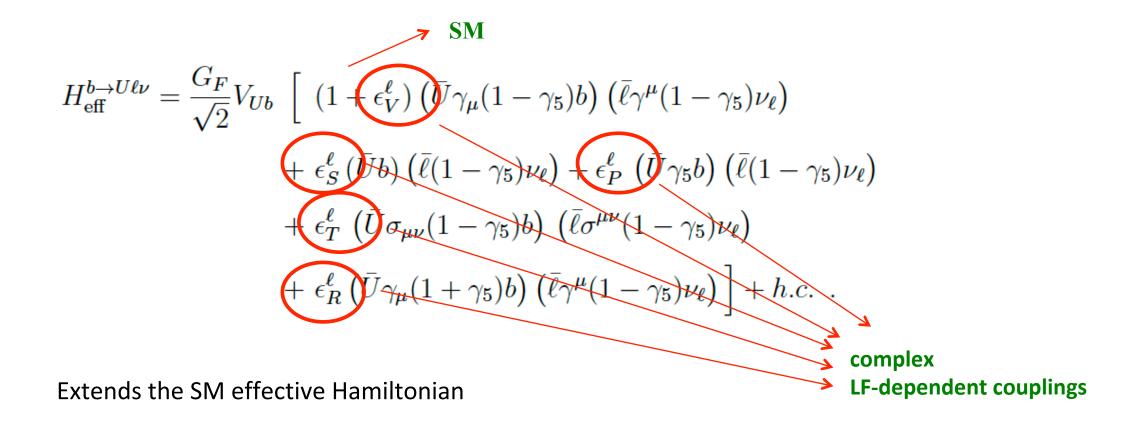
- Identifications of suitable observables
- Higher orders in 1/m  $_{\text{Q}}$  and  $\alpha_{\text{s}}$
- role of shape function

# **Common starting point (U=c,u)**

$$\begin{split} H^{b\to U\ell\nu}_{\text{eff}} &= \frac{G_F}{\sqrt{2}} V_{Ub} \left[ \left( 1 + \epsilon_V^\ell \right) \left( \bar{U} \gamma_\mu (1 - \gamma_5) b \right) \left( \bar{\ell} \gamma^\mu (1 - \gamma_5) \nu_\ell \right) \right. \\ &+ \epsilon_S^\ell \left( \bar{U} b \right) \left( \bar{\ell} (1 - \gamma_5) \nu_\ell \right) + \epsilon_P^\ell \left( \bar{U} \gamma_5 b \right) \left( \bar{\ell} (1 - \gamma_5) \nu_\ell \right) \\ &+ \epsilon_T^\ell \left( \bar{U} \sigma_{\mu\nu} (1 - \gamma_5) b \right) \left( \bar{\ell} \sigma^{\mu\nu} (1 - \gamma_5) \nu_\ell \right) \\ &+ \epsilon_R^\ell \left( \bar{U} \gamma_\mu (1 + \gamma_5) b \right) \left( \bar{\ell} \gamma^\mu (1 - \gamma_5) \nu_\ell \right) \right] + h.c. \; . \end{split}$$

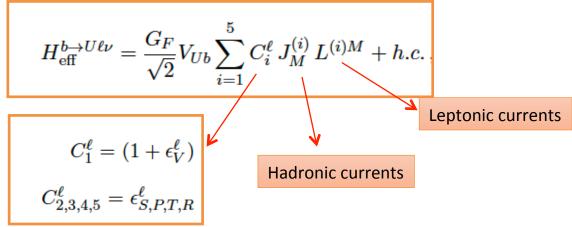
Extends the SM effective Hamiltonian

#### Common starting point (U=c,u)

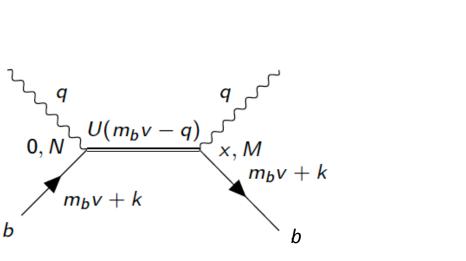


- Investigate correlations to similar processes in meson (B<sub>s</sub>, B<sub>c</sub>) decays and in b-baryon ( $\Lambda_{b_r} \Xi_{b_r} \Omega_b$ ) decays
- inclusive widths : use Optical theorem
   Heavy Quark expansion (HQE)

Pioneering works: J. Chay, H. Georgi and B. Grinstein, PLB 247 (1990) 399 I.I.Y. Bigi, M.A. Shifman, N.G. Uraltsev and A.I. Vainshtein, PRL 71 (1993) 496



SM: 
$$\epsilon_{V,S,P,T,R}^{\ell} = 0$$
  
 $J_{\mu}^{(1)} = \overline{U}\gamma_{\mu}(1-\gamma_5)b$   
 $L^{\mu(1)} = \overline{\ell}\gamma_{\mu}(1-\gamma_5)\nu_{\ell}$ 



$$d\Gamma = d\Sigma \frac{G_F^2 |V_{Ub}|^2}{4m_H} \sum_{i,j} C_i^* C_j (W^{ij})_{MN} (L^{ij})^{MN}$$

$$(W^{ij})_{MN} = \frac{1}{\pi} \text{Im}(T^{ij})_{MN}$$

$$(T^{ij})_{MN} = i \int d^4x \, e^{i \, (m_b v - q) \cdot x} \langle H_b(v, s) | T[\hat{J}_M^{(i)\dagger}(x) \, \hat{J}_N^{(j)}(0)] | H_b(v, s) \rangle$$

$$= \langle H_b(v, s) | \bar{b}_v(0) \Gamma_M^{(i)\dagger} S_U(p_X) \Gamma_N^{(j)} b_v(0) | H_b(v, s) \rangle$$
Intermediate U quark propagator

Expansion:

$$S_U(p_X) = S_U^{(0)} - S_U^{(0)}(i \not D) S_U^{(0)} + S_U^{(0)}(i \not D) S_U^{(0)}(i \not D) S_U^{(0)} + \dots$$

$$\frac{1}{m_b v / -q / -m_U}$$

$$\begin{split} \frac{1}{\pi} \mathrm{Im}(T^{ij})_{MN} &= \frac{1}{\pi} \mathrm{Im} \frac{1}{\Delta_0} \langle H_b(v,s) | \bar{b}_v[\Gamma_M^{(i)\dagger} \mathcal{P} \Gamma_N^{(j)}] b_v | H_b(v,s) \rangle \\ &- \frac{1}{\pi} \mathrm{Im} \frac{1}{\Delta_0^2} \langle H_b(v,s) | \bar{b}_v[\Gamma_M^{(i)\dagger} \mathcal{P} \gamma^{\mu_1} \mathcal{P} \Gamma_N^{(j)}] (iD_{\mu_1}) b_v | H_b(v,s) \rangle \\ &+ \frac{1}{\pi} \mathrm{Im} \frac{1}{\Delta_0^3} \langle H_b(v,s) | \bar{b}_v[\Gamma_M^{(i)\dagger} \mathcal{P} \gamma^{\mu_1} \mathcal{P} \gamma^{\mu_2} \mathcal{P} \Gamma_N^{(j)}] (iD_{\mu_1}) (iD_{\mu_2}) b_v | H_b(v,s) \rangle \\ &- \frac{1}{\pi} \mathrm{Im} \frac{1}{\Delta_0^4} \langle H_b(v,s) | \bar{b}_v[\Gamma_M^{(i)\dagger} \mathcal{P} \gamma^{\mu_1} \mathcal{P} \gamma^{\mu_2} \mathcal{P} \Gamma_N^{(j)}] (iD_{\mu_1}) (iD_{\mu_2}) (iD_{\mu_3}) b_v | H_b(v,s) \rangle \,. \end{split}$$

 $\Delta_0 = p_U^2 - m_U^2$  $p_U = m_b v - q$ HQE

Requires hadronic matrix elements with increasing number of derivatives:

$$\mathcal{M}_{\mu_1\dots\mu_n} = \langle H_b(v,s) | (\bar{b}_v)_a(iD_{\mu_1})\dots(iD_{\mu_n})(b_v)_b | H_b(v,s) \rangle$$

can be expressed in terms of non perturbative parameters

.

$$\mathcal{O}\left(\frac{1}{m_b^n}\right)\cdots \begin{cases} \mathcal{O}\left(\frac{1}{m_b^3}\right) \begin{cases} \mathcal{O}\left(\frac{1}{m_b^2}\right) \begin{cases} -2M_H \hat{\mu}_{\pi}^2 = \langle H_b | \overline{b}_v \ iD^{\mu} \ iD_{\mu} \ b_v | H_b \rangle \\ 2M_H \hat{\mu}_G^2 = \langle H_b | \overline{b}_v \ (-i\sigma_{\mu\nu}) \ iD^{\mu} \ iD^{\nu} \ b_v | H_b \rangle \\ 2M_H \hat{\rho}_D^3 = \langle H_b | \overline{b}_v \ iD^{\mu} \ (iv \cdot D) \ iD_{\mu} \ b_v | H_b \rangle \\ 2M_H \hat{\rho}_{LS}^3 = \langle H_b | \overline{b}_v \ (-i\sigma_{\mu\nu}) \ iD^{\mu} \ (iv \cdot D) \ iD^{\nu} \ b_v | H_b \rangle \\ \dots \end{cases}$$

.

$$\mathcal{O}\left(\frac{1}{m_{b}^{n}}\right)\cdots\begin{cases} \mathcal{O}\left(\frac{1}{m_{b}^{3}}\right) \begin{cases} \mathcal{O}\left(\frac{1}{m_{b}^{2}}\right) \begin{cases} -2N_{H}\hat{\mu}_{\pi}^{2} \neq \langle H_{b}|\overline{b}_{v} \ iD^{\mu} \ iD_{\mu} \ b_{v}|H_{b}\rangle \\ 2M_{H}\hat{\mu}_{G}^{2} \neq \langle H_{b}|\overline{b}_{v} \ (-i\sigma_{\mu\nu}) \ iD^{\mu} \ iD^{\nu} \ b_{v}|H_{b}\rangle \\ 2M_{H}\hat{\rho}_{D}^{3} = \langle H_{b}|\overline{b}_{v} \ iD^{\mu} \ (iv \cdot D) \ iD_{\mu} \ b_{v}|H_{b}\rangle \\ 2M_{H}\hat{\rho}_{LS}^{3} = \langle H_{b}|\overline{b}_{v} \ (-i\sigma_{\mu\nu}) \ iD^{\mu} \ (iv \cdot D) \ iD^{\nu} \ b_{v}|H_{b}\rangle \\ \cdots$$

# $\hat{\mu}_{\pi}^2$ matrix element of the kinetic energy operator

is different for different hadrons (i.e. B and  $\Lambda_{\rm b})$ 

$$\mu_{\pi}^2(B) - \mu_{\pi}^2(\Lambda_b) = \frac{2m_b m_c}{m_b - m_c} \left[ (m_{\Lambda_b} - m_{\Lambda_c}) - (\overline{m}_B - \overline{m}_D) \right] \left( 1 + \mathcal{O}(1/m_{b,c}^2) \right)$$

$$\hat{\mu}_{\pi}^2(\Lambda_b) = (0.50 \pm 0.1) \,\mathrm{GeV}^2$$

.

$$\mathcal{O}\left(\frac{1}{m_b^n}\right)\cdots \begin{cases} \mathcal{O}\left(\frac{1}{m_b^3}\right) \\ \mathcal{O}\left(\frac{1}{m_b^3}\right)$$

 $\hat{\mu}_G^2$  matrix element of the chromomagnetic operator

depends on the spin of the hadron and can be fixed from data (mass splittings)

$$\hat{\mu}_G^2(\Lambda_b) = 0$$

.

$$\mathcal{O}\left(\frac{1}{m_{b}^{n}}\right) \dots \begin{cases} \mathcal{O}\left(\frac{1}{m_{b}^{2}}\right) \begin{cases} \mathcal{O}\left(\frac{1}{m_{c}^{2}}\right) \begin{cases} -2M_{H}\,\hat{\mu}_{\pi}^{2} = \langle H_{b}|\overline{b}_{v}\,iD^{\mu}\,iD_{\mu}\,b_{v}|H_{b}\rangle \\ 2M_{H}\,\hat{\mu}_{G}^{2} = \langle H_{b}|\overline{b}_{v}\,(-i\sigma_{\mu\nu})\,iD^{\mu}\,iD^{\nu}\,b_{v}|H_{b}\rangle \\ 2M_{H}\,\hat{\rho}_{D}^{3} = \langle H_{b}|\overline{b}_{v}\,iD^{\mu}\,(iv\cdot D)\,iD_{\mu}\,b_{v}|H_{b}\rangle \\ 2M_{h}\,\hat{\rho}_{LS}^{3} \neq \langle H_{b}|\overline{b}_{v}\,(-i\sigma_{\mu\nu})\,iD^{\mu}\,(iv\cdot D)\,iD^{\nu}\,b_{v}|H_{b}\rangle \\ \dots \end{cases}$$

$$\hat{\rho}_D^3 \quad \text{Darwin term approx:} \quad \rho_D^3(\Lambda_b) \simeq \rho_D^3(B) \qquad \qquad \rho_D^3(\Lambda_b) = (0.17 \pm 0.08) \,\text{GeV}^3$$

$$\hat{\rho}_{LS}^3 \quad \text{spin-orbit term} \qquad \qquad \hat{\rho}_{LS}^3(\Lambda_b) = 0$$

Results

 $\mathcal{M}_{\mu_1\dots\mu_n} = \langle H_b(v,s) | (\bar{b}_v)_a(iD_{\mu_1})\dots(iD_{\mu_n})(b_v)_b | H_b(v,s) \rangle$ 

General parametrization including **dependence on the spin** up to O(m<sub>b</sub><sup>-3</sup>) not known before Method derived for B mesons in B.M. Dassinger, T. Mannel and S. Turczyk, JHEP 03 (2007) 087

New terms depending on the spin appear for a **polarized baryon** 

- Analytic results
- Main outcome of our study
- Applies to all spin ½ baryons

Results at  $O(m_b^{-2})$ : A.V. Manohar and M.B. Wise, PRD 49 (1994) 1310 S. Balk, J.G. Korner and D. Pirjol, EPJC 1 (1998) 221 Results

$$\mathcal{M}^{\rho\sigma\lambda} = M_{H} \left[ \left( \frac{\hat{\rho}_{D}^{3}}{3} \Pi^{\rho\lambda} v^{\sigma} \mathsf{P}_{+} + \frac{\hat{\rho}_{LS}^{3}}{6} v^{\sigma} i \epsilon^{\rho\lambda\alpha\beta} v_{\alpha} \mathsf{S}_{\beta} \right) - \left( \frac{\hat{\rho}_{D}^{3}}{3} \Pi^{\rho\lambda} v^{\sigma} s^{\mu} \mathsf{S}_{\mu} - \frac{\hat{\rho}_{LS}^{3}}{2} v^{\sigma} i \epsilon^{\rho\lambda\alpha\beta} v_{\alpha} s_{\beta} \mathsf{P}_{+} \right) \right]$$

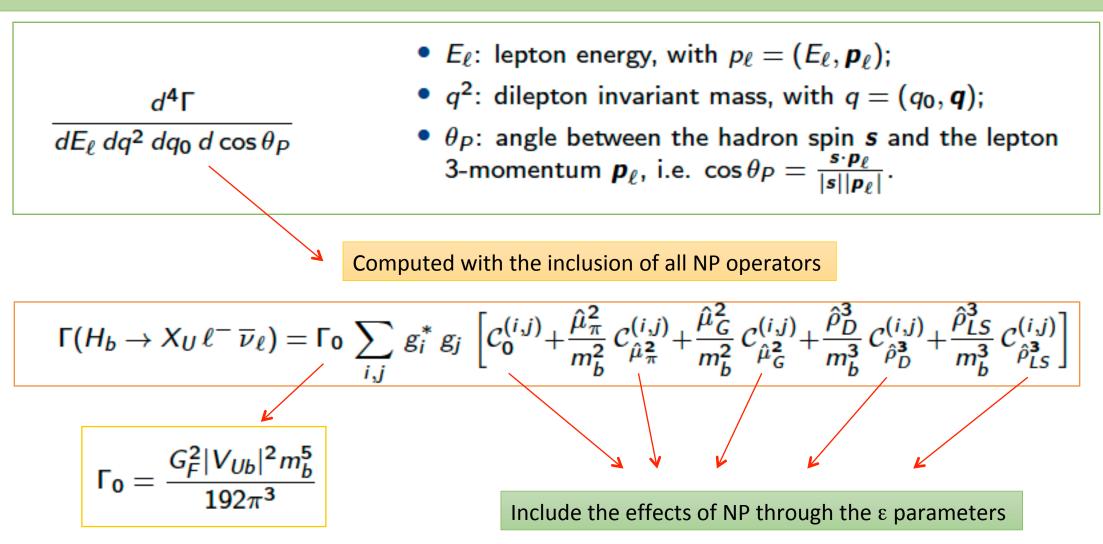
$$\begin{split} \mathcal{M}^{\rho\sigma} &= \mathcal{M}_{H} \left[ \left( \frac{\hat{\mu}_{\pi}^{2}}{3} \prod^{\rho\sigma} \mathsf{P}_{+} + \frac{\hat{\mu}_{G}^{2}}{6} i \epsilon^{\rho\sigma\alpha\beta} \mathsf{v}_{\alpha} \mathsf{S}_{\beta} + \right. \\ &+ \frac{\hat{\rho}_{D}^{3} + \hat{\rho}_{LS}^{3}}{24m_{b}} \left( 4 \left( i \epsilon^{\rho\sigma\alpha\beta} \mathsf{v}_{\alpha} \mathsf{S}_{\beta} - \mathsf{v}^{\rho} \mathsf{v}^{\sigma} \mathsf{y} \right) + \right. \\ &+ \mathsf{v}^{\rho} \left( 2 \gamma^{\sigma} + \mathbf{y} \gamma^{\sigma} - \gamma^{\sigma} \mathsf{y} \right) + \mathsf{v}^{\sigma} \left( 2 \gamma^{\rho} + \mathbf{y} \gamma^{\rho} - \gamma^{\rho} \mathsf{y} \right) \right) \right) + \\ &+ \left( - \frac{\hat{\mu}_{\pi}^{2}}{3} \prod^{\rho\sigma} \mathsf{P}_{+} \$ \gamma_{5} + \frac{\hat{\mu}_{G}^{2}}{2} i \epsilon^{\rho\sigma\alpha\beta} \mathsf{v}_{\alpha} \mathsf{s}_{\beta} \mathsf{P}_{+} + \right. \\ &+ \frac{\hat{\rho}_{D}^{3}}{12m_{b}} \left( 6 i \epsilon^{\rho\sigma\alpha\beta} \mathsf{v}_{\alpha} \mathsf{s}_{\beta} + i \left( \mathsf{v}^{\rho} \epsilon^{\sigma\mu\alpha\beta} - \mathsf{v}^{\sigma} \epsilon^{\rho\mu\alpha\beta} \right) \mathsf{v}_{\alpha} \mathsf{s}_{\beta} \gamma_{\mu} + \right. \\ &+ \left. s^{\rho} \mathsf{v}^{\sigma} \mathsf{y} \gamma_{5} + \mathsf{v}^{\rho} \mathsf{s}^{\sigma} \left( 2\gamma_{5} + \mathsf{y} \gamma_{5} \right) + \left( 2 \mathsf{v}^{\rho} \mathsf{v}^{\sigma} + \mathsf{v}^{\rho} \gamma^{\sigma} - \mathsf{v}^{\sigma} \gamma^{\rho} \right) \$ \gamma_{5} \right) + \\ &+ \left. \left. \frac{\hat{\rho}_{LS}^{3}}{8m_{b}} \left( 4 i \epsilon^{\rho\sigma\alpha\beta} \mathsf{v}_{\alpha} \mathsf{s}_{\beta} + i \left( \mathsf{v}^{\rho} \epsilon^{\sigma\mu\alpha\beta} - \mathsf{v}^{\sigma} \epsilon^{\rho\mu\alpha\beta} \right) \mathsf{v}_{\alpha} \mathsf{s}_{\beta} \gamma_{\mu} + \right. \\ &+ \left. \left. \left( s^{\rho} \mathsf{v}^{\sigma} + \mathsf{v}^{\rho} \mathsf{s}^{\sigma} \right) \gamma_{5} + \left( 2 \mathsf{v}^{\rho} \mathsf{v}^{\sigma} - \mathsf{v}^{\sigma} \gamma^{\rho} \right) \$ \gamma_{5} \right) \right) \right] \end{split}$$

P. Colangelo, F. Loparco, FDF JHEP 11 (2020) 032

## Results

$$\begin{split} \mathcal{M}^{\rho} &= M_{H} \left[ \left( \frac{\hat{\mu}_{\pi}^{2} - \hat{\mu}_{G}^{2}}{12m_{b}} \left( v^{\rho} \left( 3 + 5 \psi \right) - 2\gamma^{\rho} \right) - \frac{\hat{\rho}_{D}^{3} + \hat{\rho}_{LS}^{3}}{12m_{b}^{2}} \left( 4 v^{\rho} \psi - \gamma^{\rho} \right) \right) + \\ &+ \left( - \frac{\hat{\mu}_{\pi}^{2}}{12m_{b}} \left( \left( v^{\rho} \left( 3 + 5 \psi \right) - 2\gamma^{\rho} \right) \not s \gamma_{5} + 4s^{\rho} P_{+} \gamma_{5} \right) + \\ &+ \frac{\hat{\mu}_{G}^{2}}{4m_{b}} \left( \left( v^{\rho} \left( 1 + 2\psi \right) - \gamma^{\rho} \right) \not s \gamma_{5} + s^{\rho} \gamma_{5} \right) + \\ &+ \frac{\hat{\rho}_{D}^{3}}{12m_{b}^{2}} \left( \left( v^{\rho} \left( 1 + 4\psi \right) - 2\gamma^{\rho} \right) \not s \gamma_{5} + s^{\rho} \left( 2 - \psi \right) \gamma_{5} \right) + \\ &+ \frac{\hat{\rho}_{LS}^{3}}{8m_{b}^{2}} \left( \left( 3v^{\rho} \psi - \gamma^{\rho} \right) \not s \gamma_{5} + s^{\rho} \gamma_{5} \right) \right) \end{split}$$

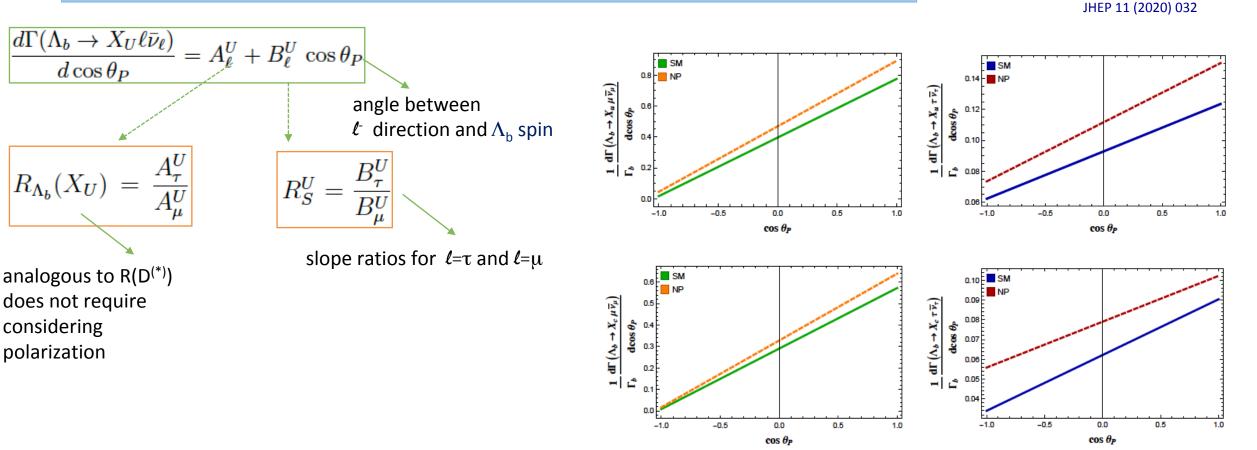
P. Colangelo, F. Loparco, FDF JHEP 11 (2020) 032 Fully differential decay width



Complete expression at  $O(1/m_b^3)$  in SM, including all NP operators and for non vanishing lepton mass Rather lengthy P. Colangelo, F. Loparco, FDF JHEP 11 (2020) 032, arXiv:2006.13759

### **Numerical Results**

Identification of observables sensitive to  $\Lambda_b$  polarization and to BSM effects (Longitudinal polarization expected for  $\Lambda_b$  resulting from b quark produced in top or Z<sup>0</sup> decays)



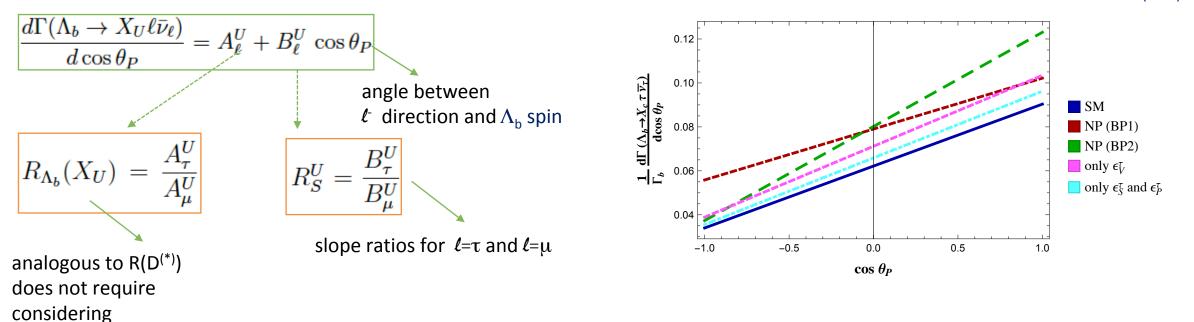
NP: benchmark points b ->u P. Colangelo, F. Loparco, FDF, PRD 100 (19) 075037

b ->c P. Colangelo, FDF, JHEP 06 (18) 082 (BP1) R.X. Shi, L.S. Geng, B. Grinstein, S. Jager, J.M. Camalich JHEP 12 (19) 065. (BP2) P. Colangelo, F. Loparco, FDF

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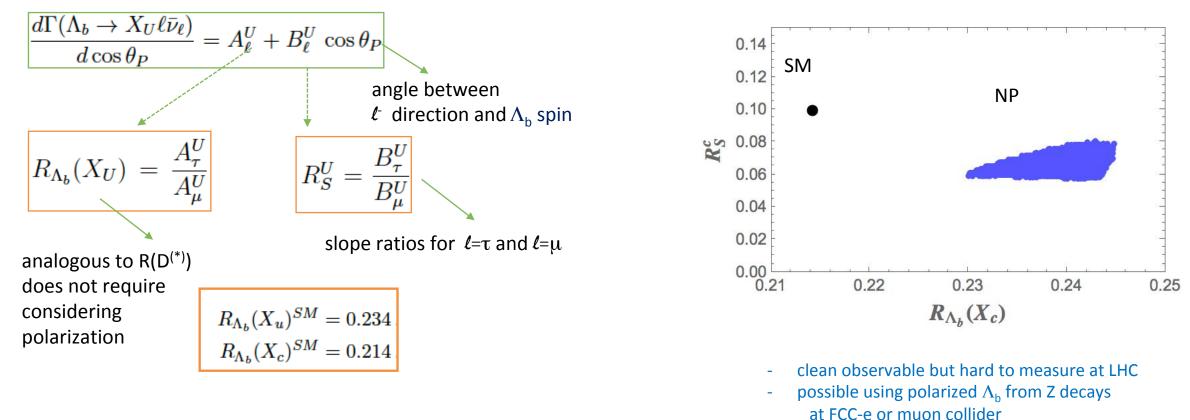
polarization

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### Conclusions

Inclusive heavy hadron decays

- Further testing ground for NP
- Essential to understand the inclusive/exclusive discrepancy in the  $V_{cb}$  and  $V_{ub}$  determinations

Theoretical improvement:

calculation of the necessary hadronic matrix elements in the case of a polarized baryon at  $O(1/m_b^3)$  and including all possible NP operators

Results: distributions in cos ( $\theta_{P}$ ) sensitive to NP

- Ratio  $\mathsf{R}(\Lambda_{\mathsf{b}})$  can deviate from SM
- Ratio of slope parameter to be considered together with  $R(\Lambda_b)$
- correlation between the two ratio shows the predicted pattern of deviation from SM
- measurable at FCC