

Isolated photon production in the Parton Reggeization Approach with real NLO corrections

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15-19 November 2021
DESY, Hamburg, Germany

**Talk at International Workshop on Resummation, Evolution,
Factorization - REF2021**

Outline

- 1 Introduction
- 2 Parton Reggeization Approach
- 3 UnPDFs with exact normalization
- 4 ReggeQCD and KaTie
- 5 Isolated photon production at the LHC
- 6 On double counting between LO and real NLO contributions
- 7 Conclusions

Introduction

Isolated single-photon production in CPM of QCD

- $K(\text{exp}/LO) \simeq 3$
- $K(\text{exp}/NLO) \simeq 1.5$ [*M. Fontannaz, J. P. Guillet and G. Heinrich, Isolated prompt photon photoproduction at NLO// Eur. Phys. J. C* **21** (2001), 303-312]
- $K(\text{exp}/NNLO) \simeq 1.0$ [*X. Chen, T. Gehrmann, N. Glover, M. Höfer and A. Huss, Isolated photon and photon+jet production at NNLO QCD accuracy // JHEP* **04** (2020), 166]

Parton Reggeization Approach (PRA)

Details of the LO PRA are presented in Refs.

- *Nefedov M.A., Saleev V.A., Shipilova A.V. Dijet azimuthal decorrelations at the LHC in the parton Reggeization approach. Phys. Rev. D. 2013. V. 87. P. 094030.*
- *Karpishkov A.V., Nefedov M.A. and Saleev V.A., $B B\bar{B}$ angular correlations at the LHC in parton Reggeization approach merged with higher-order matrix elements// Phys. Rev. D. 2017. V. 96. P. 096019.*
- *M. A. Nefedov and V. A. Saleev, High-Energy Factorization for Drell-Yan process in pp and $p\bar{p}$ collisions with new Unintegrated PDFs, Phys. Rev. D **102** (2020), 114018*

Developments of PRA in NLO can be found here

- M. A. Nefedov, Towards stability of NLO corrections in High-Energy Factorization via Modified Multi-Regge Kinematics approximation, JHEP **08** (2020), 055
- M. A. Nefedov, Computing one-loop corrections to effective vertices with two scales in the EFT for Multi-Regge processes in QCD,” Nucl. Phys. B **946** (2019), 114715
- M. Nefedov and V. Saleev, On the one-loop calculations with Reggeized quarks,” Mod. Phys. Lett. A **32** (2017) no.40, 1750207

Parton Reggeization Approach (PRA)

I. High-energy factorization

$$d\sigma = \sum_{i,j} \int_0^1 \frac{dx_1}{x_1} \int \frac{d^2\mathbf{q}_{T1}}{\pi} \Phi_i(x_1, t_1, \mu^2) \int_0^1 \frac{dx_2}{x_2} \int \frac{d^2\mathbf{q}_{T2}}{\pi} \Phi_j(x_2, t_2, \mu^2) \cdot d\hat{\sigma}_{ij}^{\text{PRA}},$$

where $t_{1,2} = -\mathbf{q}_{T1,2}^2$, $i, j = R, Q, \bar{Q}$

$\Phi_{R/Q}(x, t, \mu^2)$ are gluon/quark unintegrated parton distribution functions (uPDFs)

$d\hat{\sigma}_{ij}^{\text{PRA}}$ is partonic cross section which is written via off-shell squared matrix elements $\overline{|M^{\text{PRA}}|^2}$ of PRA, and

$$\lim_{t_1, t_2 \rightarrow 0} \int \frac{d\phi_1}{2\pi} \int \frac{d\phi_2}{2\pi} \overline{|M^{\text{PRA}}|^2} = \overline{|M^{\text{CPM}}|^2}$$

Parton Reggeization Approach

II. Off-shell amplitudes as multi-Regge limit of auxiliary $(n + 2)$ QCD amplitudes

The PRA hard-scattering amplitude is *gauge-invariant* because the initial-state off-shell partons are treated as Reggeized partons (R, Q, \bar{Q}) in a sense of gauge-invariant EFT for QCD processes in Multi-Regge Kinematics(MRK), introduced by L.N. Lipatov.

Feynman's rules of EFT:

- L. N. Lipatov, Gauge invariant effective action for high-energy processes in QCD, Nucl. Phys. B **452**, 369 (1995).
- L. N. Lipatov and M. I. Vyazovsky, QuasimultiRegge processes with a quark exchange in the t channel, Nucl. Phys. B **597**, 399 (2001).
- M. A. Nefedov, ReggeQCD model-file for FeynArts.

Parton Reggeization Approach

III. Modified KMR unintegrated PDFs with exact normalization at arbitrary x

$$\Phi_i(x, t, \mu^2) = \frac{d}{dt} [T_i(t, \mu^2, \mathbf{x}) F_i(x, t)],$$

where $T_i(t, \mu^2, \mathbf{x})$ is usually referred to as *Sudakov formfactor*, satisfying the boundary conditions $T_i(t = 0, \mu^2, \mathbf{x}) = 0$ and $T_i(t = \mu^2, \mu^2, \mathbf{x}) = 1$.

$$\Phi_i(x, t, \mu_Y^2) = \frac{\alpha_s(t)}{2\pi} \frac{T_i(t, \mu^2, \mathbf{x})}{t} \sum_{j=q, \bar{q}, g} \int_x^1 dz P_{ij}(z) F_j\left(\frac{x}{z}, t\right) \theta(\Delta(t, \mu_Y^2) - z).$$

Parton Reggeization Approach

Modified KMR unintegrated PDFs with exact normalization at arbitrary x

$$T_i(t, \mu^2, \mathbf{x}) = \exp \left[- \int_t^{\mu^2} \frac{dt'}{t'} \frac{\alpha_s(t')}{2\pi} (\tau_i(t', \mu^2) + \Delta\tau_i(t', \mu^2, \mathbf{x})) \right]$$

$$\tau_i(t, \mu^2) = \sum_j \int_0^1 dz z P_{ji}(z) \theta(\Delta(t, \mu^2) - z),$$

$$\Delta\tau_i(t, \mu^2, \mathbf{x}) = \sum_j \int_0^1 dz \theta(z - \Delta(t, \mu^2)) \left[z P_{ji}(z) - \frac{F_j(\frac{x}{z}, t)}{F_i(x, t)} P_{ij}(z) \theta(z - x) \right].$$

For details, see Ref.

- *M. A. Nefedov and V. A. Saleev, High-Energy Factorization for Drell-Yan process in pp and $p\bar{p}$ collisions with new Unintegrated PDFs, Phys. Rev. D **102** (2020), 114018*

Parton Reggeization Approach

Self agreement of the PRA is based on multi-Regge limit of the relevant QCD amplitudes and proved CPM formalism

- Factorization formula is obtained from relevant ones of CPM
- Reggeized amplitudes are gauge invariant
- Unintegrated PDFs are normalized on collinear PDFs

Single-photon production in the PRA

LO and most important real NLO correction to single-photon production in the PRA

- LO: $Q + \bar{Q} \rightarrow \gamma$
- NLO: $Q(\bar{Q}) + R \rightarrow \gamma + q(\bar{q})$

Negligible contributions to single-photon production in the PRA (see (*))

- NLO: $Q + \bar{Q} \rightarrow \gamma + g$
- NNLO: $R + R \rightarrow \gamma + q + \bar{q}$ and $R + R \rightarrow \gamma + g$ (*quark box*)

(*) [M. Nefedov and V. Saleev, *Diphoton production at the Tevatron and the LHC in the NLO approximation of the parton Reggeization approach*, *Phys. Rev. D* **92** (2015) no.9, 094033]

MC event generator KaTie

As it has been shown in Refs.

- *Nefedov M.A., Saleev V.A., Shipilova A.V. Dijet azimuthal decorrelations at the LHC in the parton Reggeization approach. Phys. Rev. D. 2013. V. 87. P. 094030.*
- *Karpishkov A.V., Nefedov M.A. and Saleev V.A., $B B\bar{B}$ angular correlations at the LHC in parton Reggeization approach merged with higher-order matrix elements// Phys. Rev. D. 2017. V. 96. P. 096019.*
- *Kutak K., Maciula R., Serino M., Szczurek A. and van Hameren A., Four-jet production in single- and double-parton scattering within high-energy factorization// JHEP. 2016. V. 1604. P. 175,*

at the level of tree diagrams, analytical formalism based on Lipatov's EFT fully coincide with numerically generated off-shell amplitudes using MC event generator KaTie

- *van Hameren A., KaTie: For parton-level event generation with kT -dependent initial states. Comput.Phys.Commun. 2018. V. 224. P. 371.*

Single-photon production at the LHC

Setup of ATLAS measurements at 13 TeV

- For photons transverse momenta: $p_{T1} > 125$ GeV,
- For pseudorapidity all photons: $|\eta_\gamma| < 2.37$, excluding the range $1.37 < |\eta_\gamma| < 1.56$,
- For photon-jet separation conditions:

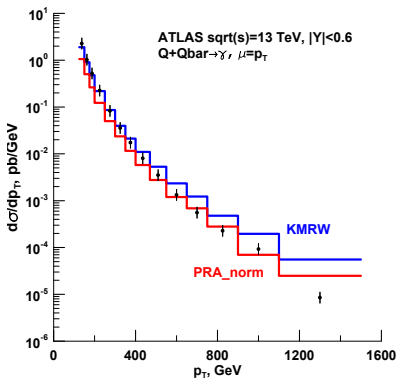
$$\Delta R_{\gamma j} = \sqrt{(\eta_\gamma - \eta_j)^2 + (\phi_\gamma - \phi_j)^2} > R_0 = 0.40$$

Fragmentation contribution is included using the Frixione condition for $QR \rightarrow q\gamma$ subprocesses

$$E_T^{iso}(\Delta R_{q\gamma}) = p_{Tq} < E_T^{max} \frac{1 - \cos(\Delta R_{q\gamma})}{1 - \cos(R_0)}, \text{ where } E_T^{max} = 10 \text{ GeV}$$

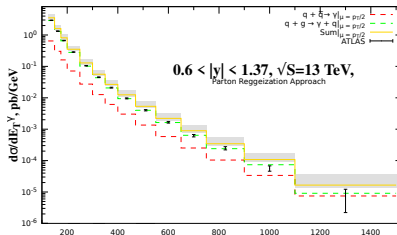
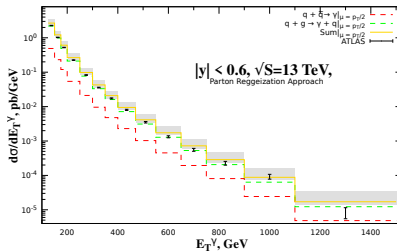
Single-photon production at the LHC

Comparison between KMRW and PRA PDFs. Only LO contributions are shown.



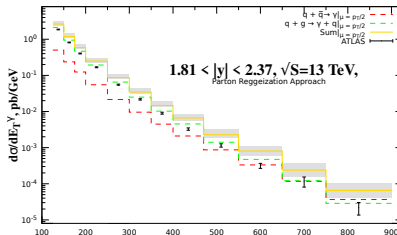
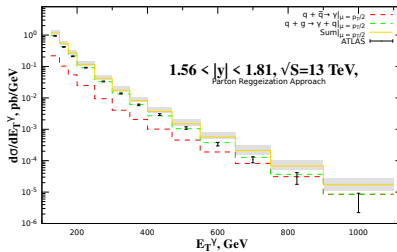
Single-photon production at the LHC

The differential cross sections for the production of one isolated photon as functions p_T . The hard scale in PRA calculations is taken as $\mu = p_T/2$.



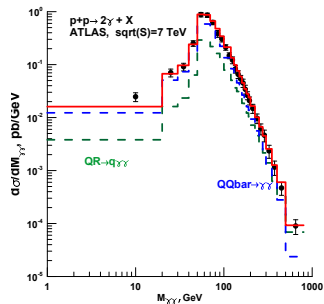
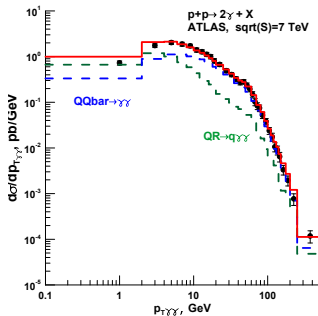
Single-photon production at the LHC

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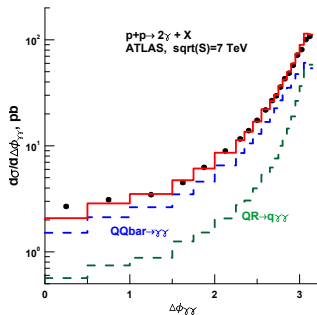
Two-photon production at the LHC

The differential cross sections for the production of two isolated photon as functions $p_{T\gamma\gamma}$ and $M_{\gamma\gamma}$.



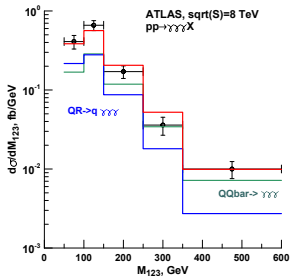
Two-photon production at the LHC

The differential cross sections for the production of one isolated photon as functions $\Delta\phi_{\gamma\gamma}$.



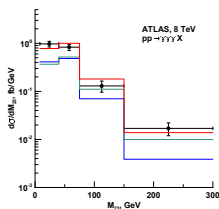
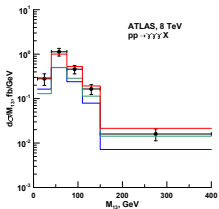
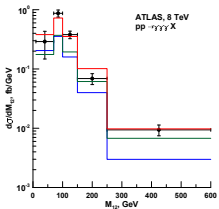
Three-photon production at the LHC

The differential cross sections for the production of three isolated photons as functions M_{123} . The hard scale in PRA calculations are taken as invariant mass of photons, $\mu = M_{3\gamma}$. The green histogram corresponds LO contribution from $Q\bar{Q} \rightarrow \gamma\gamma\gamma$ subprocess. The blue histogram corresponds NLO contribution from $QR \rightarrow q\gamma\gamma\gamma$ subprocess. The red histogram is their sum.



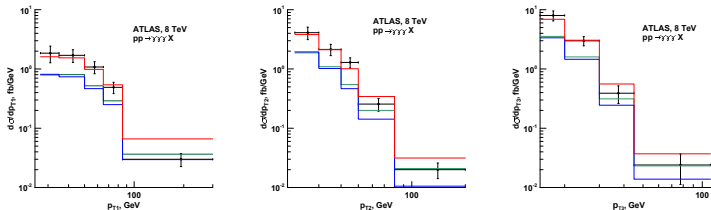
Three-photon production at the LHC

The differential cross sections for the production of three isolated photons as functions of M_{12} (left panel), M_{13} (central panel), and M_{23} (right panel).



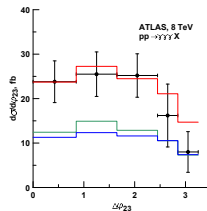
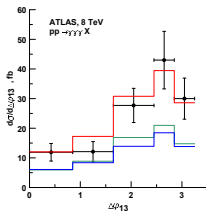
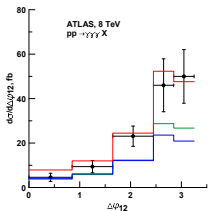
Three-photon production at the LHC

The differential cross sections for the production of three isolated photons as functions of p_{T1} (left panel), p_{T2} (central panel) and p_{T3} (right panel).



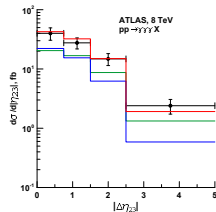
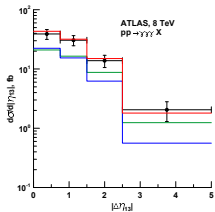
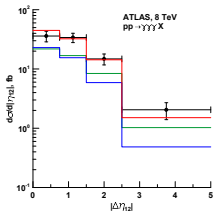
Three-photon production at the LHC

The differential cross sections for the production of three isolated photons as functions of $|\Delta\phi_{12}|$ (left panel), $|\Delta\phi_{13}|$ (central panel) and $\Delta\phi_{23}$ (right panel).



Three-photon production at the LHC

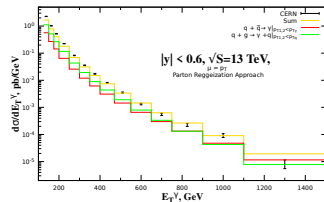
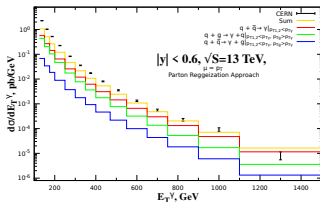
The differential cross sections for the production of three isolated photons as functions of $|\Delta y_{12}|$ (left panel), $|\Delta y_{13}|$ (central panel) and $|\Delta y_{23}|$ (right panel).



On double counting between LO and real NLO contributions

Subtraction scheme based on k_T -ordering

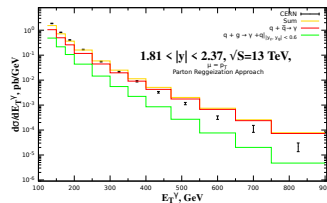
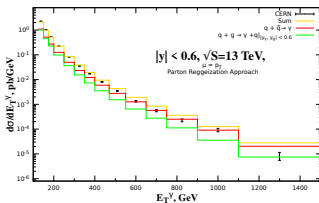
- *Karpishkov A.V., Nefedov M.A. and Saleev V.A., $B B\bar{B}$ angular correlations at the LHC in parton Reggeization approach merged with higher-order matrix elements// Phys. Rev. D. 2017. V. 96. P. 096019.*
- *A. Karpishkov, V. Saleev and A. Shipilova, Angular decorrelations in $\gamma + 2\text{jet}$ events at high energies in the parton Reggeization approach, Mod. Phys. Lett. A **34** (2019) no.32, 1950266*
- *R. Maciula and A. Szczurek, Consistent treatment of charm production in higher-orders at tree-level within k_T -factorization approach, Phys. Rev. D **100** (2019) no.5, 054001*



On double counting between LO and real NLO contributions

Subtraction scheme based on rapidity-ordering

- [M. Nefedov and V. Saleev, *Diphoton production at the Tevatron and the LHC in the NLO approximation of the parton Reggeization approach*, *Phys. Rev. D* **92** (2015) no.9, 094033]



Conclusions

- We describe cross sections and spectra for 1-2-3-photon production in LO PRA with real NLO corrections
- We demonstrate advantages of normalized PRA uPDFs instead of KMRW PDFs, especially for quarks uPDFs
- PRA results in LO+NLO approximation are roughly coincide with full NNLO predictions of CPM
- Double counting between LO and real NLO contributions in k_T -factorization should be small.

Thank you for your attention!