# Impact of generation mixing on the search for squarks at the LHC

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## Outline

- I. Flavour violation in the MSSM
- 2. Fermionic squark decays
- 3. Bosonic squark decays
- 4. Conclusion and Outlook

In the Standard Model, quark flavour violation interactions are parametrized through CKM-matrix

$$V_{\rm CKM} = V_u^{\dagger} V_d$$

## Flavour violation in the MSSM

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Beyond the Standard Model, e.g. Minimal Supersymmetric Standard Model (MSSM)

#### Minimal flavour-violation (MFV)

- no new sources of flavour violation
- in super-CKM basis squarks undergo same rotations as quarks
- all flavour-violating entries related to CKM-matrix
- Example:  $\tilde{\chi}_i^{\pm} \tilde{q}_j q_k$  interaction proportional to  $V_{q_j q'_k}$

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- e.g. gravity-mediation, messengermatter mixing, ...
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Flavour-violating terms incorporated in the mass matrices at the electroweak scale

$$\mathcal{M}_{\tilde{u}}^2 = \begin{pmatrix} \mathcal{M}_{LL}^2 & \left(\mathcal{M}_{RL}^2\right)^{\dagger} \\ \mathcal{M}_{RL}^2 & \mathcal{M}_{RR}^2 \end{pmatrix}$$

Focus here on flavour violation in the squark sector (slepton sector analogously with PMNS-matrix)

# Squark sector with flavour violation

Soft-breaking matrices may include off-diagonal, i.e. flavour-violating, entries

$$\mathcal{M}_{LL,\alpha\beta}^{2} = M_{Q,\alpha\beta}^{2} + \frac{1}{2} \left[ m_{u,\alpha}^{2} + \left(\frac{1}{2} - \frac{2}{3}s_{W}^{2}\right) m_{Z}^{2}c_{2\beta} \right] \delta_{\alpha\beta}$$
$$\mathcal{M}_{RR,\alpha\beta}^{2} = M_{U,\alpha\beta}^{2} + \frac{1}{2} \left[ m_{u,\alpha}^{2} + \frac{2}{3}s_{W}^{2}m_{Z}^{2}c_{2\beta} \right] \delta_{\alpha\beta}$$
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Introduce dimensionless parametrization through normalization w.r.t. diagonal elements

$$\delta^{u\{LL,RR\}}_{\alpha\beta} = M^2_{\{Q,U\},\alpha\beta} / \sqrt{M^2_{\{Q,U\},\alpha\alpha}} M^2_{\{Q,U\},\beta\beta}$$
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Diagonalization through 6x6 rotation matrices leads to mass eigenstates ( $m_{\tilde{u}_1} < ... < m_{\tilde{u}_6}$ )

$$\mathcal{R}_{\tilde{u}}\mathcal{M}_{\tilde{u}}^{2}\mathcal{R}_{\tilde{u}}^{\dagger} = \operatorname{diag}\left(m_{\tilde{u}_{1}}^{2}, m_{\tilde{u}_{2}}^{2}, m_{\tilde{u}_{3}}^{2}, m_{\tilde{u}_{4}}^{2}, m_{\tilde{u}_{5}}^{2}, m_{\tilde{u}_{6}}^{2}\right)$$

Mass limits from collider searches [PDG 2008-2010]

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Electroweak precision and low-energy measurements [PDG 2008-2010; HFAG 2008-2010]

$$BR(b \to s\gamma) = (3.57 \pm 0.65) \cdot 10^{-4}$$
$$\Delta M_{B_s} = (17.77 \pm 3.31) \text{ ps}^{-1}$$
$$BR(b \to s\mu^+\mu^-) = (1.60 \pm 1.00) \cdot 10^{-6}$$
$$BR(B_s \to \mu^+\mu^-) < 4.3 \cdot 10^{-8}$$
$$\Delta a_\mu = a_\mu^{SM} - a_\mu^{exp} = (29.0 \pm 8.6) \cdot 10^{-10}$$

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Cosmological constraints due to cold dark matter [WMAP 2010]

$$0.1018 < \Omega_{\rm CDM} h^2 < 0.1228$$

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[e.g. Bozzi, Fuks, Herrmann, Klasen 2007; Fuks, Herrmann, Klasen 2008; Bartl, Hidaka, Hohenwarter-Sodek, Kernreiter, Majerotto, Porod 2009; Hurth, Porod 2009; Bruhnke, Herrmann, Porod 2010; Bartl, Eberl, Herrmann, Hidaka, Majerotto, Porod 2010]

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[Bruhnke, Herrmann, Porod (2010)]

Reference scenario for following studies: SPSIa' [Aguilar-Saavedra et al. 2006]

$$m_0 = 70 \text{ GeV}, m_{1/2} = 250 \text{ GeV}, A_0 = -300 \text{ GeV}, \tan \beta = 10, \mu > 0$$

Numerical evaluation of RGE, mass spectrum, and observables using SPheno 3.0 [Porod 2003-2010]

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Rather wide regions for QFV elements remain allowed w.r.t. precision measurements, in particular no stringent constraints on flavour mixing in right-right sector

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Couplings of squarks to scalars and fermions governed by flavour contents (i.e. rotation matrices)

$$\Gamma_{\tilde{u}_{i}\tilde{u}_{j}A^{0}} = \frac{g_{2}}{2m_{W}} \left[ \mu^{*} \left( \mathcal{R}_{\tilde{u}} \right)_{i(k+3)} m_{u_{i}} \left( \mathcal{R}_{\tilde{u}}^{\dagger} \right)_{kj} + \frac{v_{u}}{\sqrt{2}\tan\beta} \left( \mathcal{R}_{\tilde{u}} \right)_{i(k+3)} \left( T_{U} \right)_{kl} \left( \mathcal{R}_{\tilde{u}}^{\dagger} \right)_{lj} \right] + \text{h.c.}$$

[see e.g. Bozzi, Fuks, Herrmann, Klasen (2007); Fuks, Herrmann, Klasen (2008); Bruhnke, Herrmann, Porod (2010)]

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# Fermionic squark decays

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Potentially large branching ratios lead to interesting production signatures at colliders

$$pp \rightarrow \tilde{u}_{1,2} \tilde{u}_{1,2}^* \rightarrow c \bar{t} \tilde{\chi}_1^0 \tilde{\chi}_1^0$$
$$pp \rightarrow \tilde{u}_{1,2} \tilde{u}_{1,2} \rightarrow t t \tilde{\chi}_1^0 \tilde{\chi}_1^0$$

Numerical evaluation of cross-sections using Whizard/O'Mega 1.93 [Kilian, Reuter, Ohl 2001-2010], FeynArts/FormCalc [Hahn 2000-2010] and CTEQ6L parton density functions [Pumplin et al. 2002]

#### Production cross-sections and LHC signatures

[Bartl, Eberl, Herrmann, Hidaka, Majerotto, Porod (2010)]

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Expect up to 10<sup>4</sup> events for "jet + top +  $E_T^{miss}$ " production at  $E_{cm}$ =14 TeV and  $L_{int}$ =100 fb<sup>-1</sup> Event rate for top-top production found to be rather small ( $\sigma \leq 0.1$  fb at  $E_{cm}$ =14 TeV)

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Event rate for top-top production found to be rather small ( $\sigma \leq 0.1$  fb at  $E_{cm}=14$  TeV)

Loop corrections for dominant (flavour-conserving) channels increase cross-section by about 30% [Beenakker, Höpker, Spira, Zerwas 1997]

#### **Discrimination and background**

[Bartl, Eberl, Herrmann, Hidaka, Majerotto, Porod (2010)]

Identification of top-quarks crucial:  $t \to bW^+ \to b \ q\bar{q}$  [Hisano et al. (2002+2003)] Efficient charm-tagging useful, otherwise search for  $p \ p \to \tilde{u}_{1,2} \ \tilde{u}_{1,2}^* \to q \ \bar{t} \ (t \ \bar{q}) \ \tilde{\chi}_1^0 \ \tilde{\chi}_1^0$ 

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Descrimination between top and anti-top necessary:

$$: t \to bW^+ \to b \ l^+ \nu$$
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Standard Model top quark production can be distinguished through jets and/or missing energy

[Bruhnke, Herrmann, Porod (2010)]

Within MFV, only one (two) squark(s) can decay into a given squark plus a neutral (charged) boson

$$\tilde{u}_1 = \tilde{t}_1 \qquad \tilde{u}_6 = \tilde{t}_2$$
$$\tilde{d}_1 = \tilde{b}_1 \qquad \tilde{d}_2 = \tilde{b}_2$$

$$\begin{array}{cccc} \tilde{u}_6 & \to & \tilde{u}_1 Z^0 / h^0 \\ \tilde{d}_1 & \to & \tilde{u}_1 W^- \\ \tilde{d}_2 & \to & \tilde{u}_1 W^- \end{array}$$

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Considering NMFV, additional decay channels with the same final state can be opened due to the modified phase space and squark flavour contents



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Characteristical signatures found in wide ranges of NMFV-MSSM parameter space  $\tilde{q}_i \rightarrow \tilde{q}_j Z^0 / H^0$  for given i and (at least) two different values of j (or vice-versa)  $\tilde{q}_i \rightarrow \tilde{q}'_j W^{\pm}(H^{\pm})$  for given i and (at least) three different values of j (or vice-versa)

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If squarks are observed at LHC, bosonic modes can provide complementary information w.r.t. fermionic decays (which will be helpful for reconstruction of couplings and mass parameters)

# Variation of two QFV parameters

[Bruhnke, Herrmann, Porod (2010)]

Simultaneous variation of more than one QFV-parameters extends or amplifies signal patterns

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Studies of other scenarios (e.g. SPSIb, ...) show qualitatively similar signatures However, differences in the mass spectrum lead to quantitatively different results

# **Conclusion and Outlook**

Flavour-violating terms can a priori be present in soft-breaking terms at the weak scale Possibly not related to CKM-matrix (non-minimal flavour violation) Important impact on phenomenology (e.g. masses, flavour contents, ....)

Observation of characteristic signatures at colliders might rule out hypothesis of MFV

New decay channels of squarks are possible in NMFV

Fermionic decays may lead to sizeable event rates at the LHC [Bruhnke, Herrmann, Porod (2010)]

$$p p \rightarrow \tilde{u}_{1,2} \, \tilde{u}_{1,2}^* \rightarrow c \, \bar{t} \, \tilde{\chi}_1^0 \, \tilde{\chi}_1^0$$

Bosonic decays may give additional information (once squarks are observed) [Bartl, Eberl, Herrmann, Hidaka, Majerotto, Porod (2010)]

$$\tilde{q}_i \to \tilde{q}_j Z^0 / H^0 \qquad \tilde{q}_i \to \tilde{q}'_j W^\pm / H^\pm$$

#### The obtained results are a clear call for a detailed Monte Carlo study

Explore feasibility in current collider experiments Determine regions of parameter space where signals would be observable ("5-sigma-discovery-region")