

TECHNISCHE  
UNIVERSITÄT  
DRESDEN



# Reconstructing Exceptional New Physics from LHC data

Peter Athron

# Contents

❖ Title is a little aspirational – Not there yet!

- $E_6$ SSM model
- $cE_6$ SSM
- Mass Spectra
- Phenomenology
- Improved Precision

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Road map

■  $E_6$ SSM model

■  $cE_6$ SSM

■ Mass Spectra

■ Phenomenology

■ Improved Precision

Understand the  
model

What does it look like?

Signatures

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Signatures

parameters ↔ masses

precision low energy observables

Incorporate within a fitting  
package, e.g. Fittino

# Exceptional Supersymmetric Standard Model

[Phys.Rev. D73 (2006) 035009 , Phys.Lett. B634 (2006) 278-284 S.F.King, S.Moretti & R. Nevzorov]

- $E_6$  inspired model with an extra gauged  $U(1)$  symmetry

$$SU(3) \times SU(2) \times U(1)_Y \times U(1)_N \quad \tan \theta = \sqrt{15}$$

$$U(1)_N = \cos \theta U(1)_\chi + \sin \theta U(1)_\psi$$

Solves the  $\mu$ -problem!

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“Inspired” by:

Solves the  $\mu$ -problem!

$$E_6 \rightarrow SO(10) \times U(1)_\psi$$

$$\quad \quad \quad \downarrow \rightarrow SU(5) \times U(1)_\chi$$

$$\quad \quad \quad \quad \quad \downarrow \rightarrow SU(3)_C \times SU(2)_W \times U(1)_Y$$

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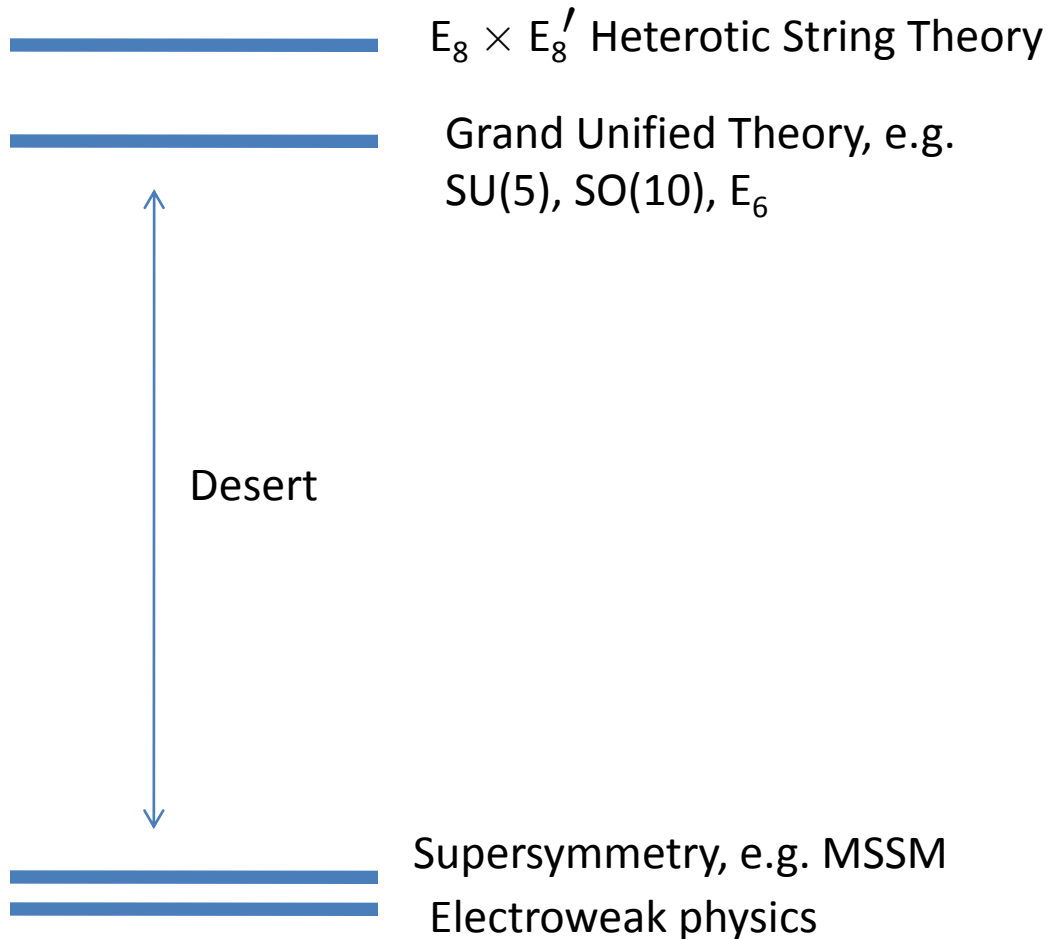
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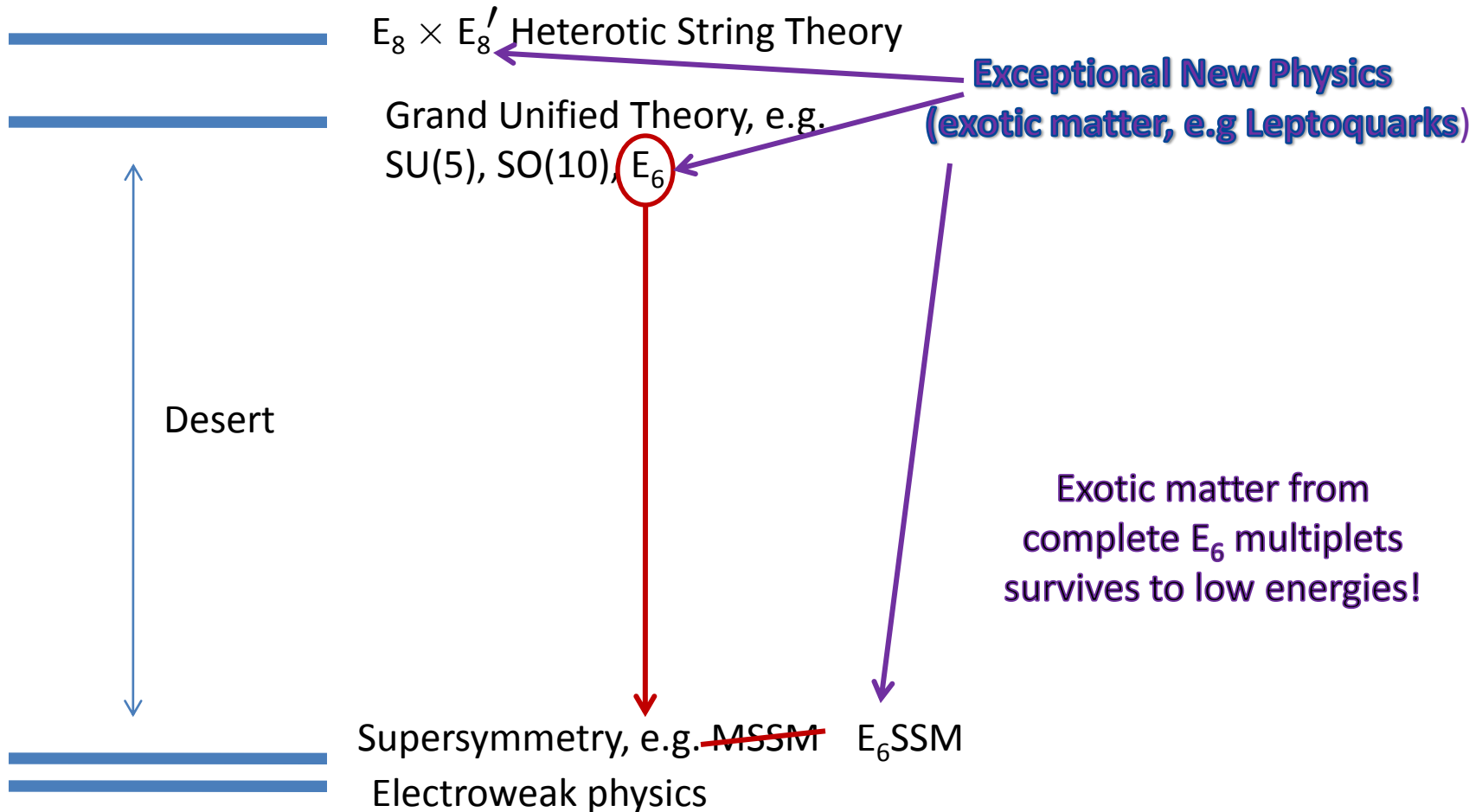
$$\quad \quad \quad \quad \quad \downarrow \rightarrow SU(3)_C \times SU(2)_W \times U(1)_Y$$

- Matter from 3 complete generations of  $E_6$   
 $\Rightarrow$  automatic cancellation of gauge anomalies

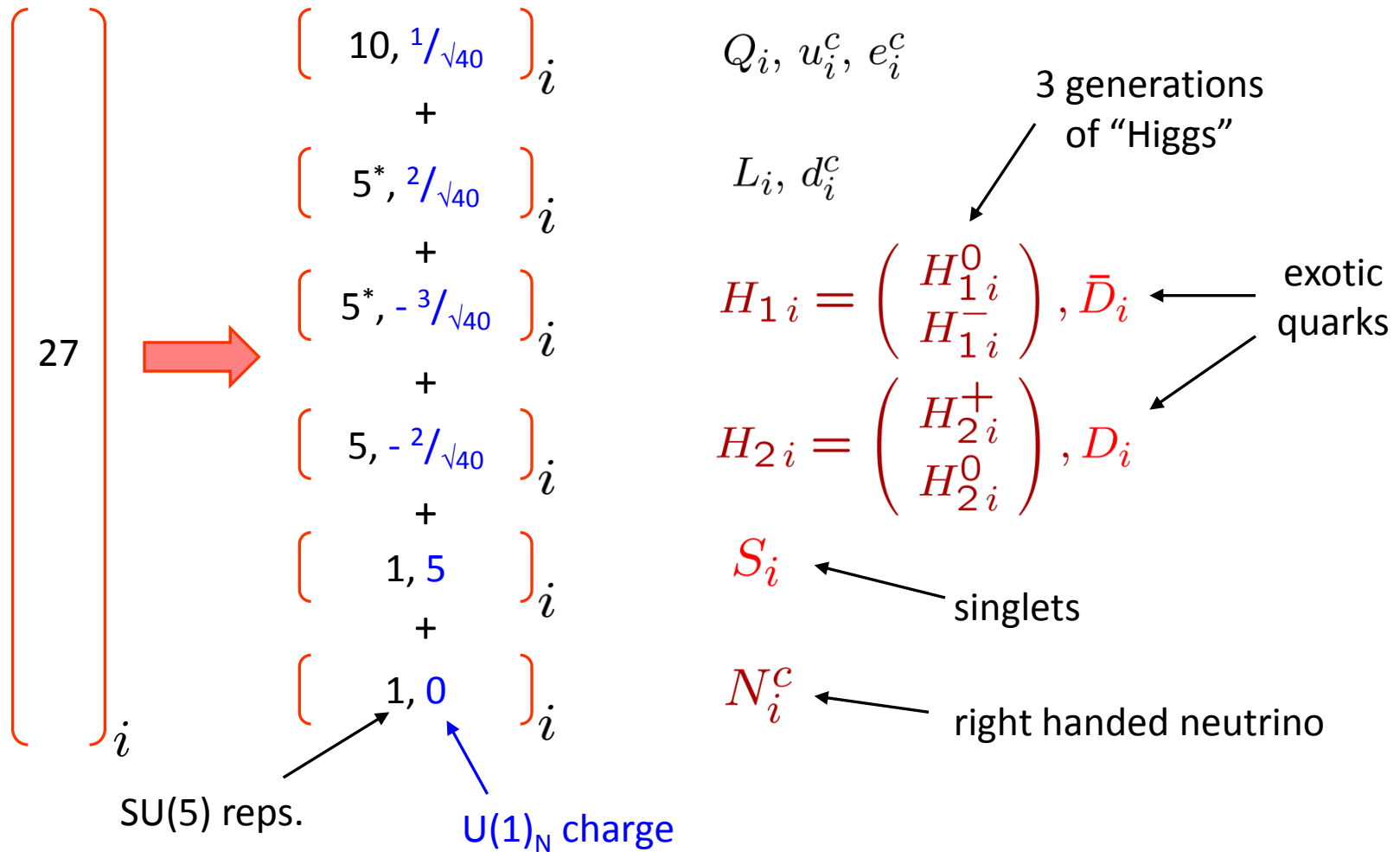
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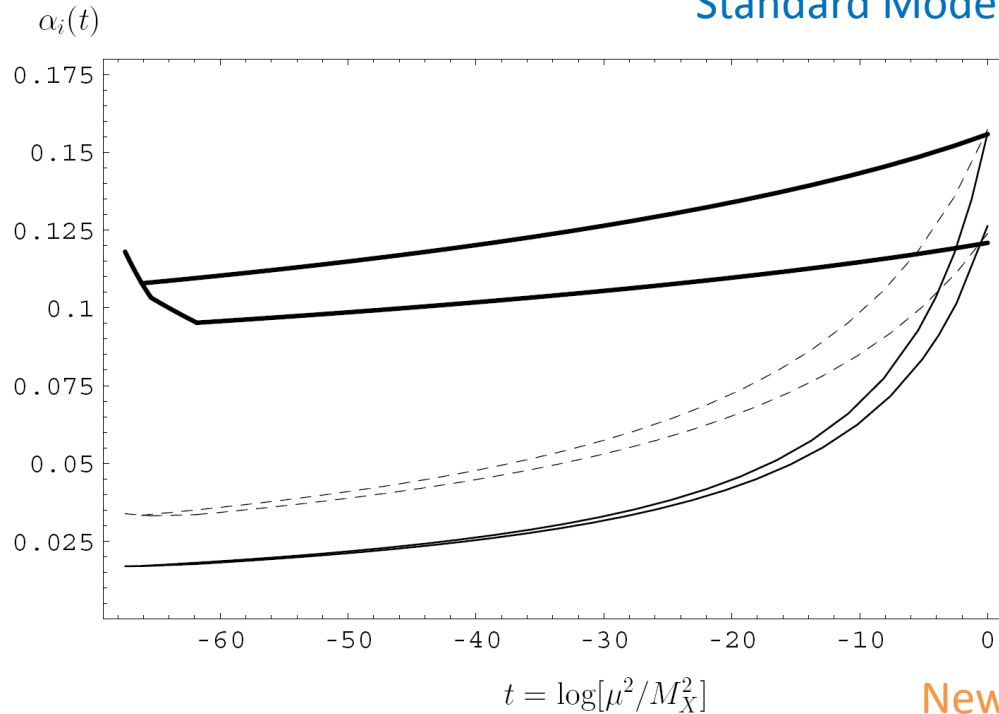


All the SM matter fields are contained in one 27-plet of  $E_6$  per generation.



# Gauge Coupling Unification

## Exceptional Supersymmetric Standard Model



- Higgs  $\in E_6$  27plets  $\Rightarrow$  relics of  $27'$  and  $\overline{27}'$ , ( $H'$  and  $\bar{H}'$ ).
- ( for 2step unification without relics see R.Howl, S.F. King PLB 652, 331, JHEP 0801:030)
- Evolution changed dramatically!
- $\beta_s = 0$  at one loop!
- 2-loop and threshold effects important !

SU(N) gauge theory

$$b_N = \frac{11}{3}N - \frac{2}{3}N$$

Gauginos

$$- \frac{1}{3}n_f - \frac{1}{6}n_s$$

New exotic  
matter!

U(1) gauge

$$b_1 = -\frac{1}{3} \sum_i Y_i^2$$

Number of  
fermions

Number of  
scalars

(matter particles in  
fundamental  
representation )

# Discrete Symmetries

- **Problem:** proton decay    ➤ **Solution:** impose  $Z_2^B$  or  $Z_2^L$  symmetry.  
Like R-parity but  $\bar{D}$  is odd,  $\tilde{D}$  is even.  
 $Z_2^B \Rightarrow$  **leptoquarks** ;     $Z_2^L \Rightarrow$  **diquarks**.
- **Problem:** large Flavour Changing Neutral Currents,    ➤ **Solution:** Approximate  $Z_2^H$   
3<sup>rd</sup> gen Higgs ( $H_{1,3}$ ,  $H_{2,3}$  and  $S_3$ ) : **even**,  
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Dropping suppressed term etc. ..

## Superpotential

$$W_{E_6SSM} \approx \lambda_i S H_{1,i} H_{2,i} + \kappa_i S D_i \bar{D}_i \\ + h_t H_u Q t^c + h_b H_d Q b^c + h_\tau H_d L \tau^c$$

# The Constrained $E_6$ SSM

[PA, S.F.King, D.J.Miller, S.Moretti, R.Nevzorov, PRD 80, 035009 (2009), PLB 681, 448-456, (2009)]

- At  $M_x \approx 10^{15}$  GeV
  - $M_{1/2}$  Universal Gaugino Mass
  - $A$  Universal trilinear soft mass
  - $m_0$  Universal scalar mass

Parameters:  $\lambda_i, \kappa_i, m_0, M_{1/2}, A$

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- Use EWSB Replace soft parameters with  $\langle S \rangle = \frac{s}{\sqrt{2}}, M_Z, \tan \beta$

Free Parameters:  $\lambda_i, \kappa_i, s$

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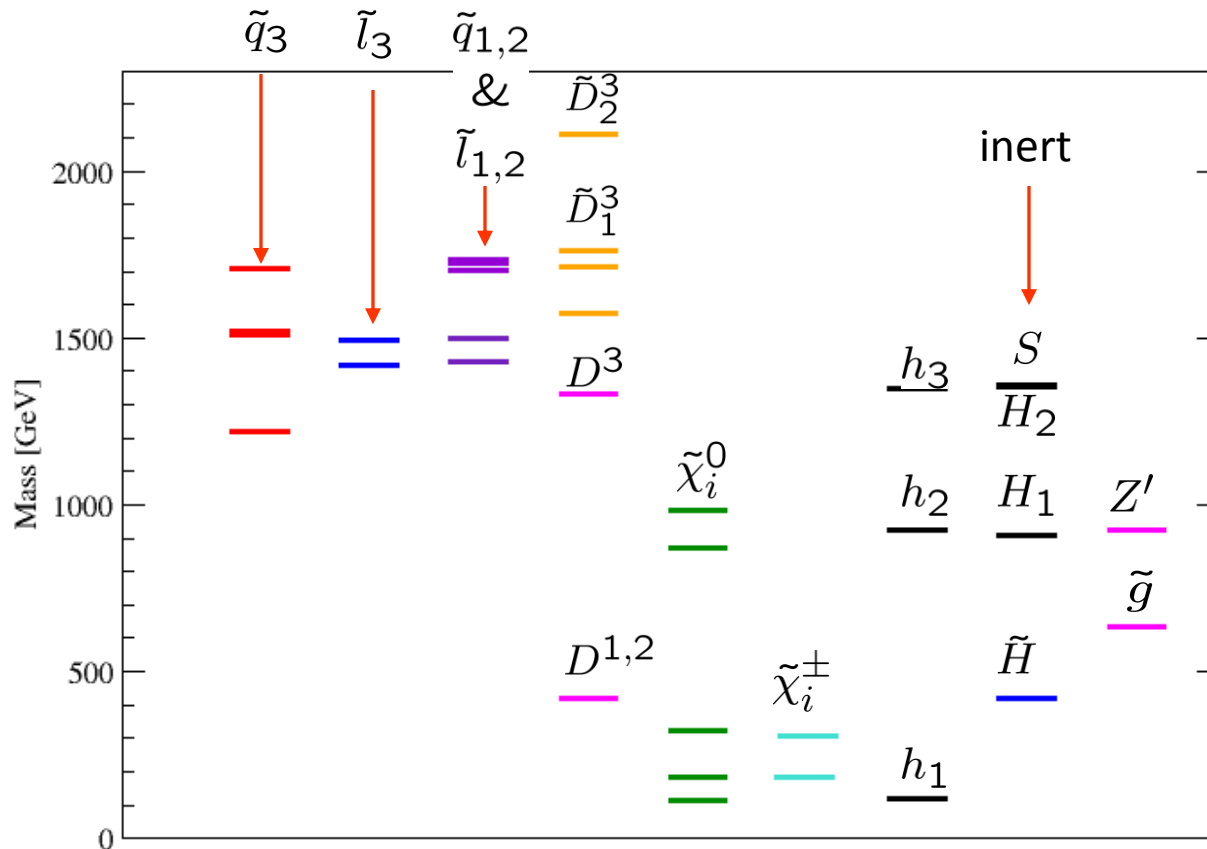
- Use EWSB Replace soft parameters with  $\langle S \rangle = \frac{s}{\sqrt{2}}, M_Z, \tan \beta$   
Free Parameters:  $\lambda_i, \kappa_i, s$

## Renormalisation Group Equations (RGEs)

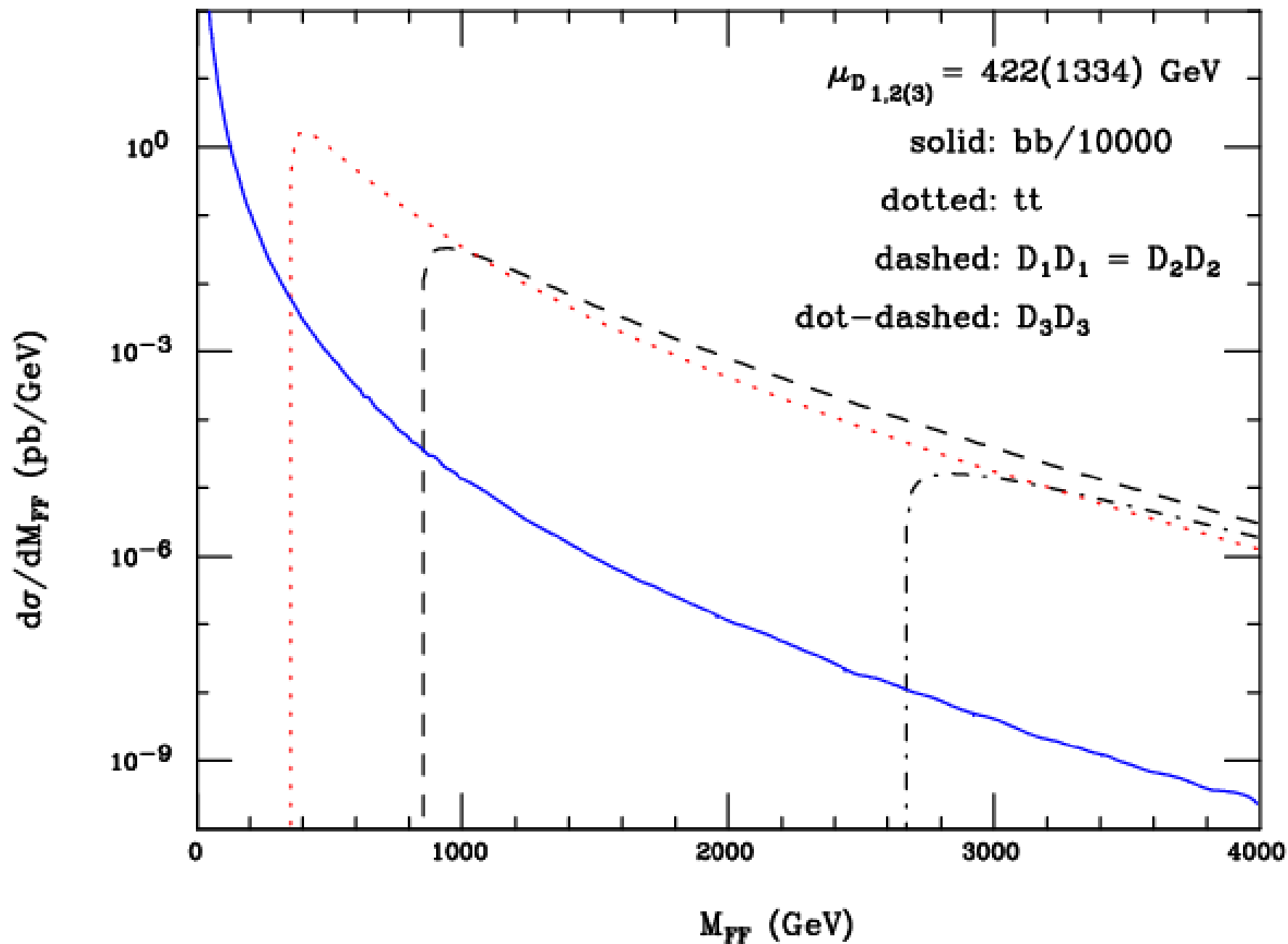
- To connect these high scale conditions with low energies we use RGEs for:
  - Gauge and Yukawa couplings (2 loop).
  - Soft breaking gaugino and trilinear masses (2 loop).
  - Soft scalar masses (1 loop).

## Light $Z'$ Scenario

- Scenario with a sub TeV  $Z'$  (926 GeV)
- Heavy sfermions and light gluino (general prediction)
- Light exotic quarks

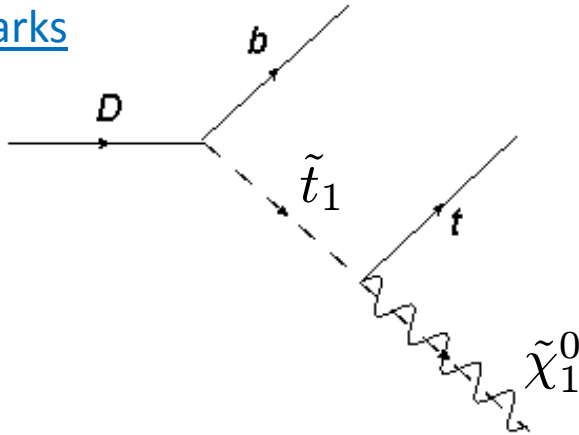


$$\begin{aligned}
 \tan \beta &= 10, \\
 s &= 2.5 \text{ TeV}, \\
 M_{1/2} &= 728 \text{ GeV}, \\
 m_0 &= 1387 \text{ GeV}, \\
 A &= -908 \text{ GeV} \\
 \lambda(M_X) &= -0.15, \\
 \lambda_{1,2}(M_X) &= 0.1 \\
 \kappa_{1,2}(M_X) &= 0.08, \\
 \kappa_3(M_X) &= 0.28
 \end{aligned}$$



## Exotic Signatures

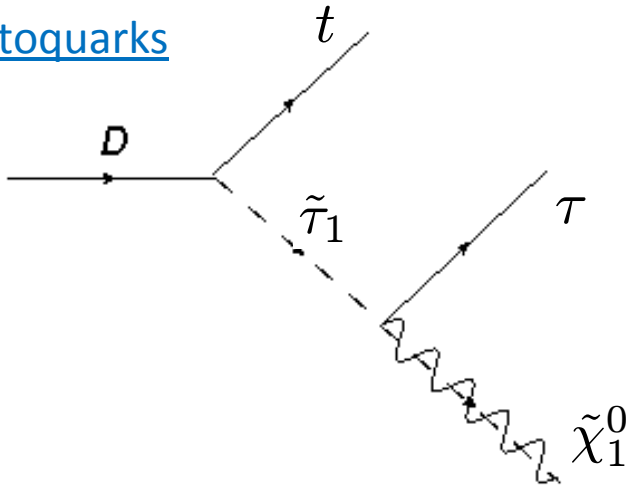
### Diquarks



Enhancement of

$$pp \rightarrow t\bar{t}b\bar{b} + E_T^{miss} + X$$

### Leptoquarks



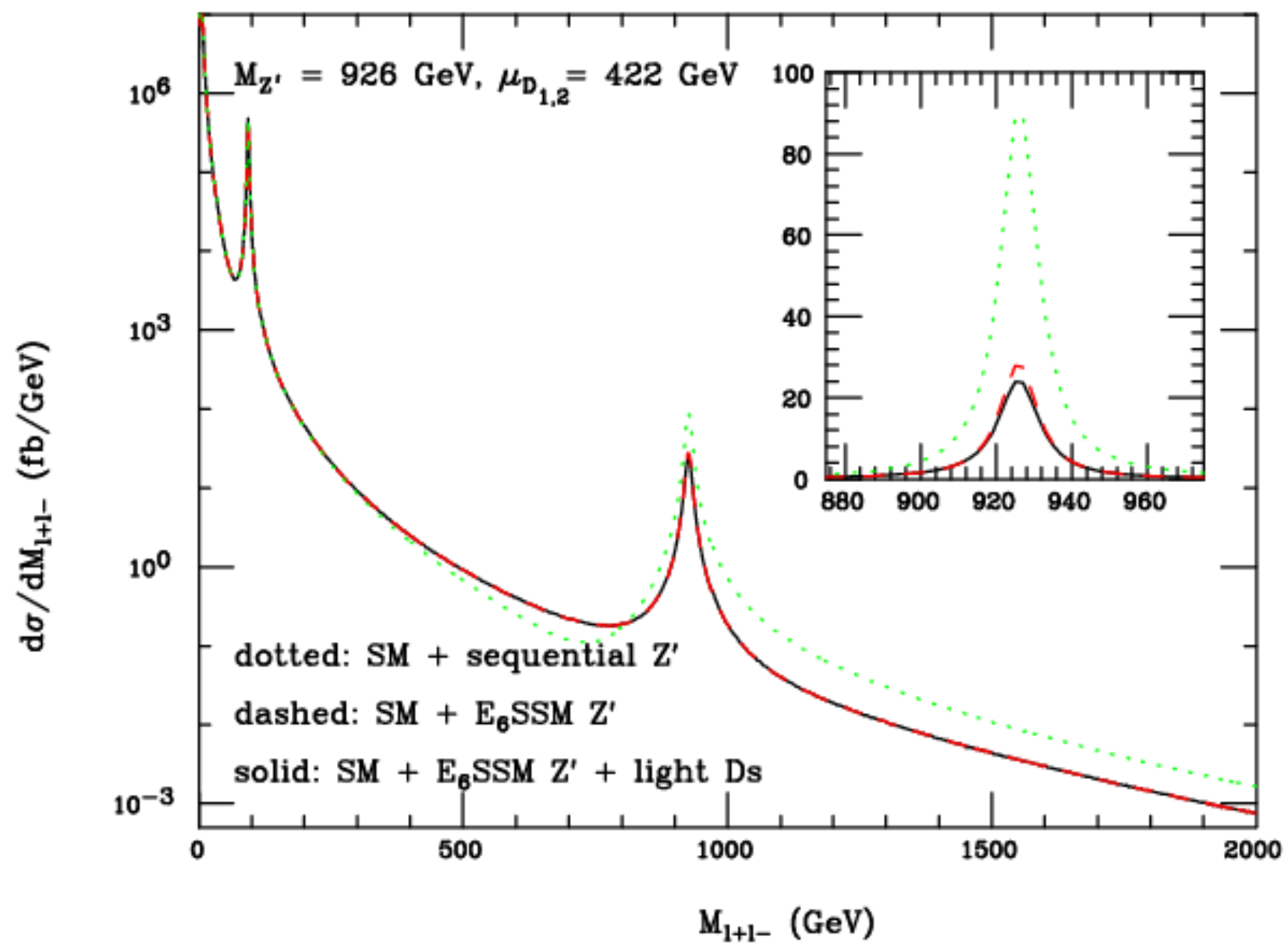
$$pp \rightarrow t\bar{t}\tau\bar{\tau} + E_T^{miss} + X$$

$$pp \rightarrow b\bar{b} + E_T^{miss} + X$$

### Scalar partners

Scalar  $\tilde{D}$  similar, but without missing energy from  $\tilde{\chi}_1^0$

e.g.  $pp \rightarrow t\bar{t}\tau\bar{\tau} + X$



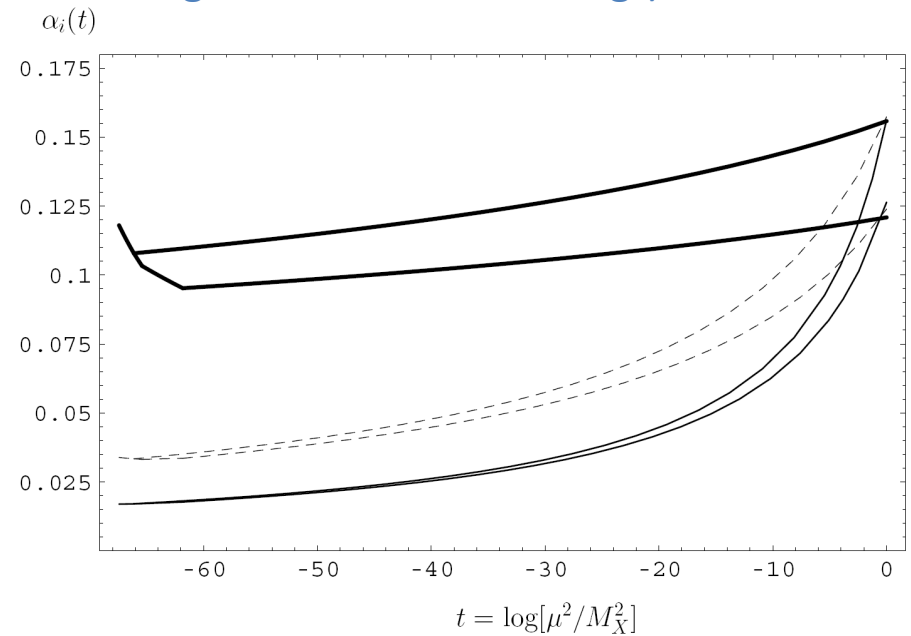
# Exotic Phenomenology

- Sub-TeV  $Z'$  not (yet!) ruled out in  $e_6$ SSM.
  - Sfermions heavy in such scenarios
  - Light Exotics - Diquarks/Leptoquarks, singlinos and higgsinos - possible
  - Observation from Drell-yan production.
  - Exotic matter could make a detectable contribution here
- Exotic quark production comparable with  $t\bar{t}$ 
  - Could give striking signature
  - More phenomenological studies important

# Threshold Corrections

(In collaboration with Dominik Stockinger and Alexander Voigt)

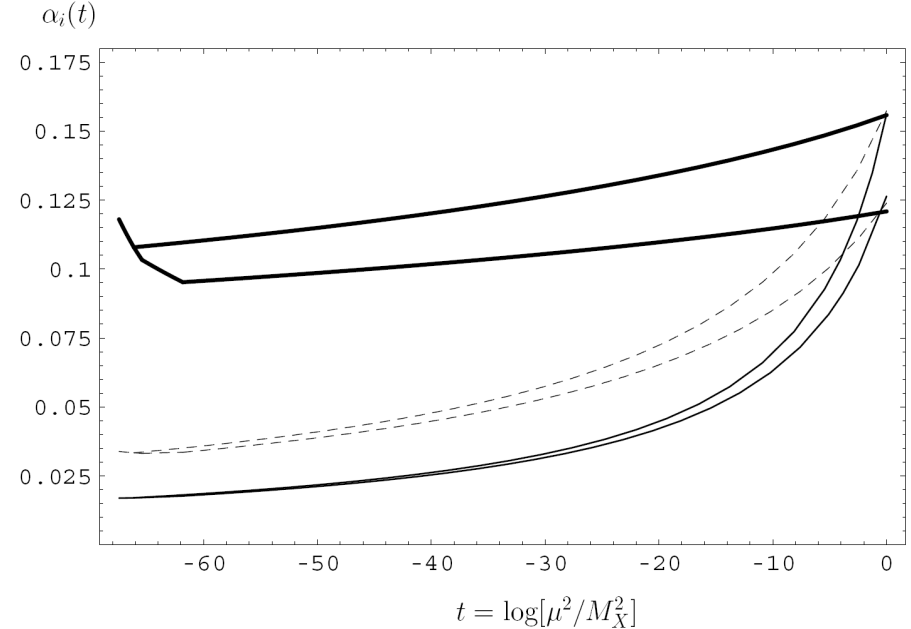
- Varying  $T_{\text{ESSM}} \Rightarrow$  10 -15% effect



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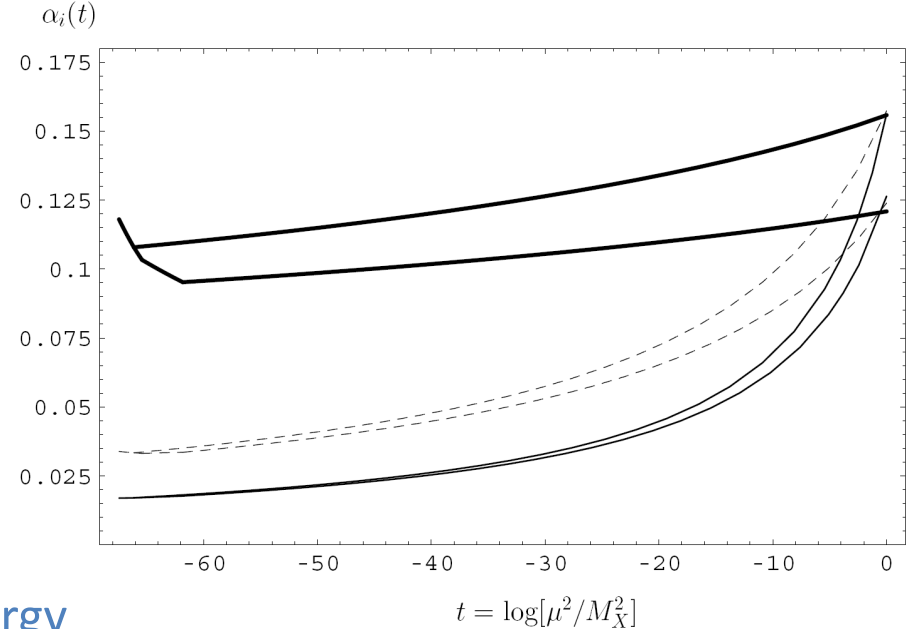
- Varying  $T_{\text{ESSM}} \Rightarrow$  10 -15% effect
- Obstacle for precision calculations
- Solution: include individual sparticle thresholds iteratively.



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## Full theory

Particles: Heavy, masses  $M_i$

Couplings:  $g''_{ij} M_i M_j$   $g'_{ij} m_i M_j$

$$T_M \leq M_i$$

## Energy

Light, masses  $m_i$

$$g_{ij}^F m_i m_j$$

$$g_{ij}^F = g_{ij}^E + \zeta_{ij}$$

Matching scale

Matching scale

## Effective theory

Particles: Light only, masses  $m_i$

Couplings:  $g_{ij}^E m_i m_j$

## Energy

Equate Green's  
Functions

$$\frac{1}{g_i^2} - \frac{1}{\hat{g}_i^2} = C_i - \sum_f \frac{1}{24\pi^2} \ln \frac{m_f}{T} - \sum_s \frac{1}{48\pi^2} \ln \frac{m_s}{T} - \frac{2N}{24\pi^2} \ln \frac{m_{\tilde{g}}}{T}$$

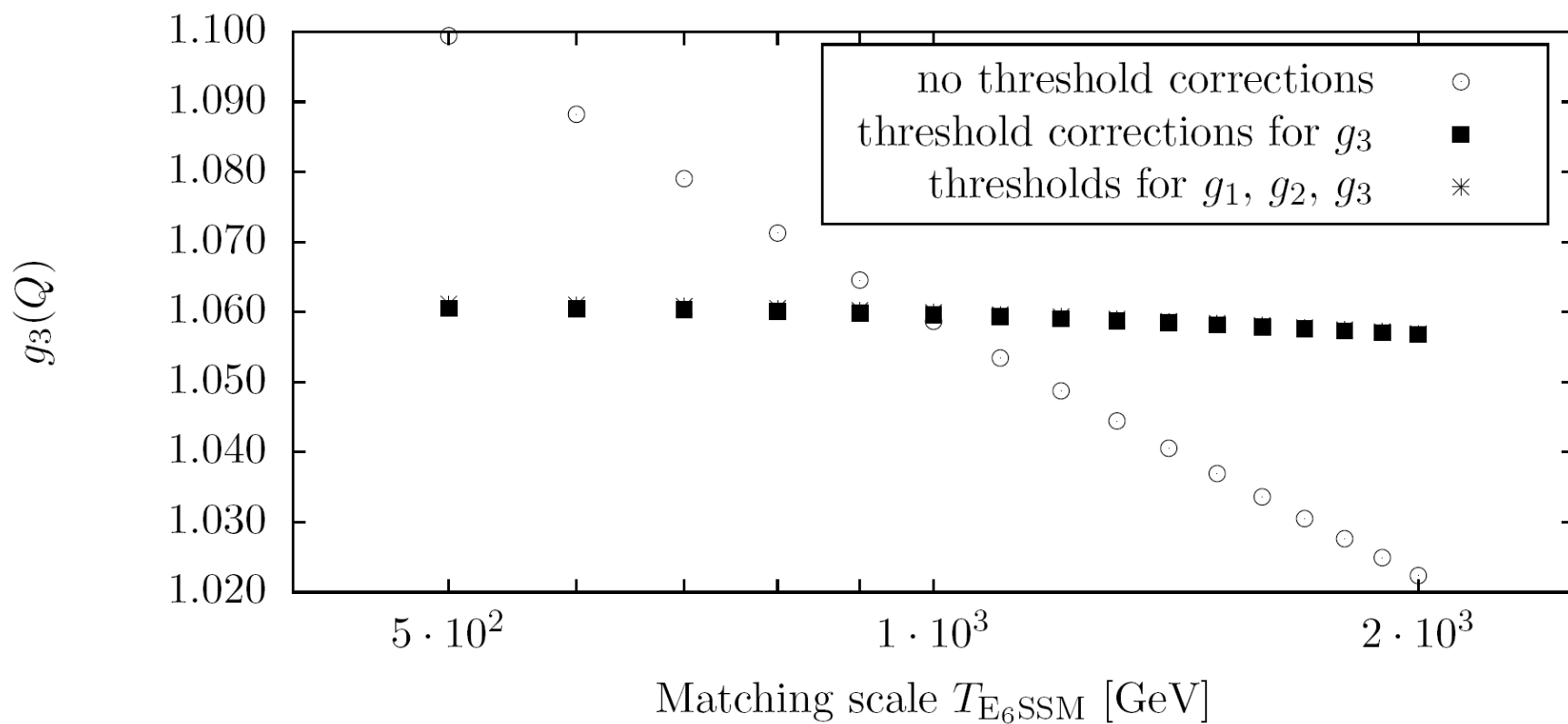
Effective coupling

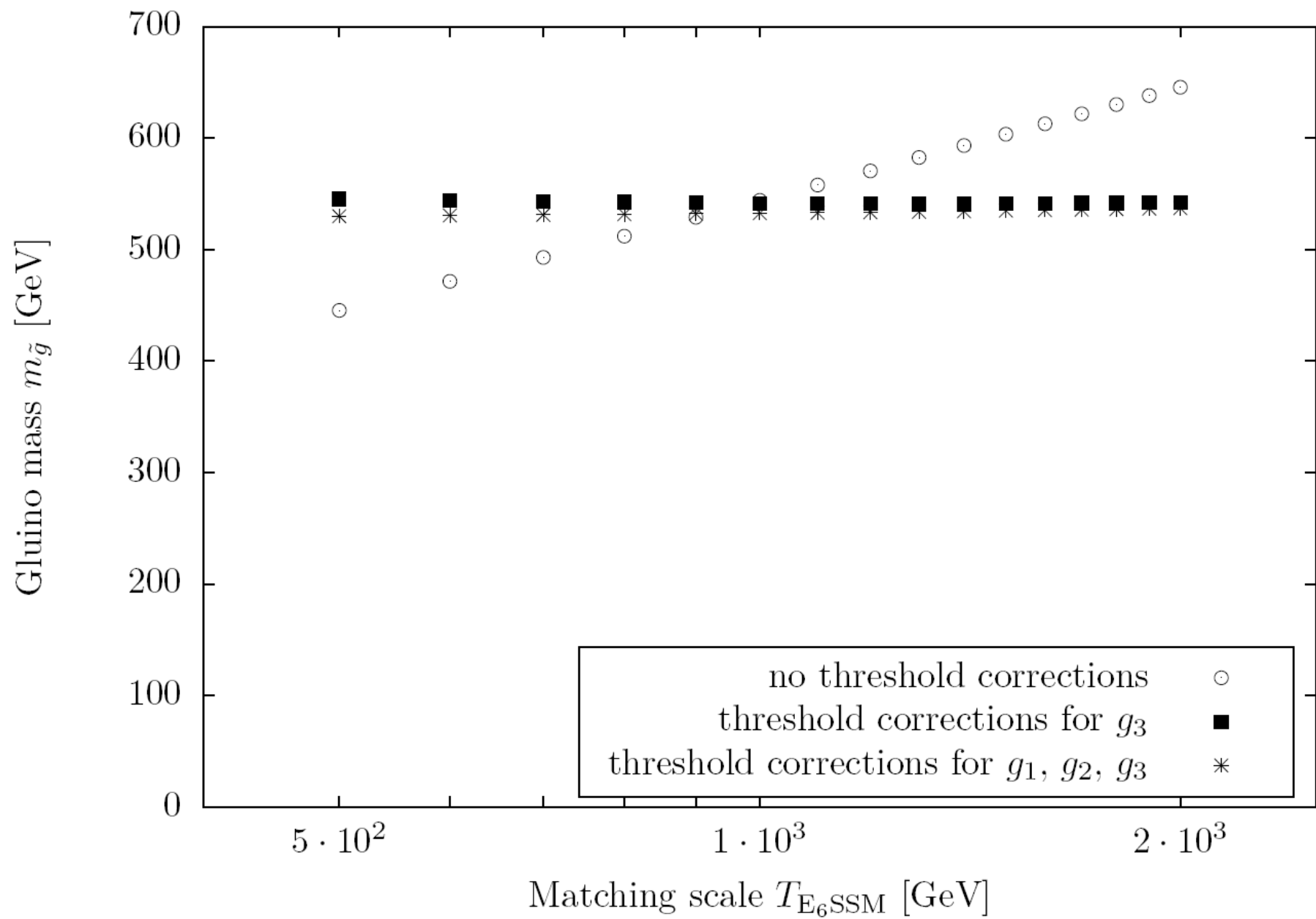
Vanishes for DR-bar couplings

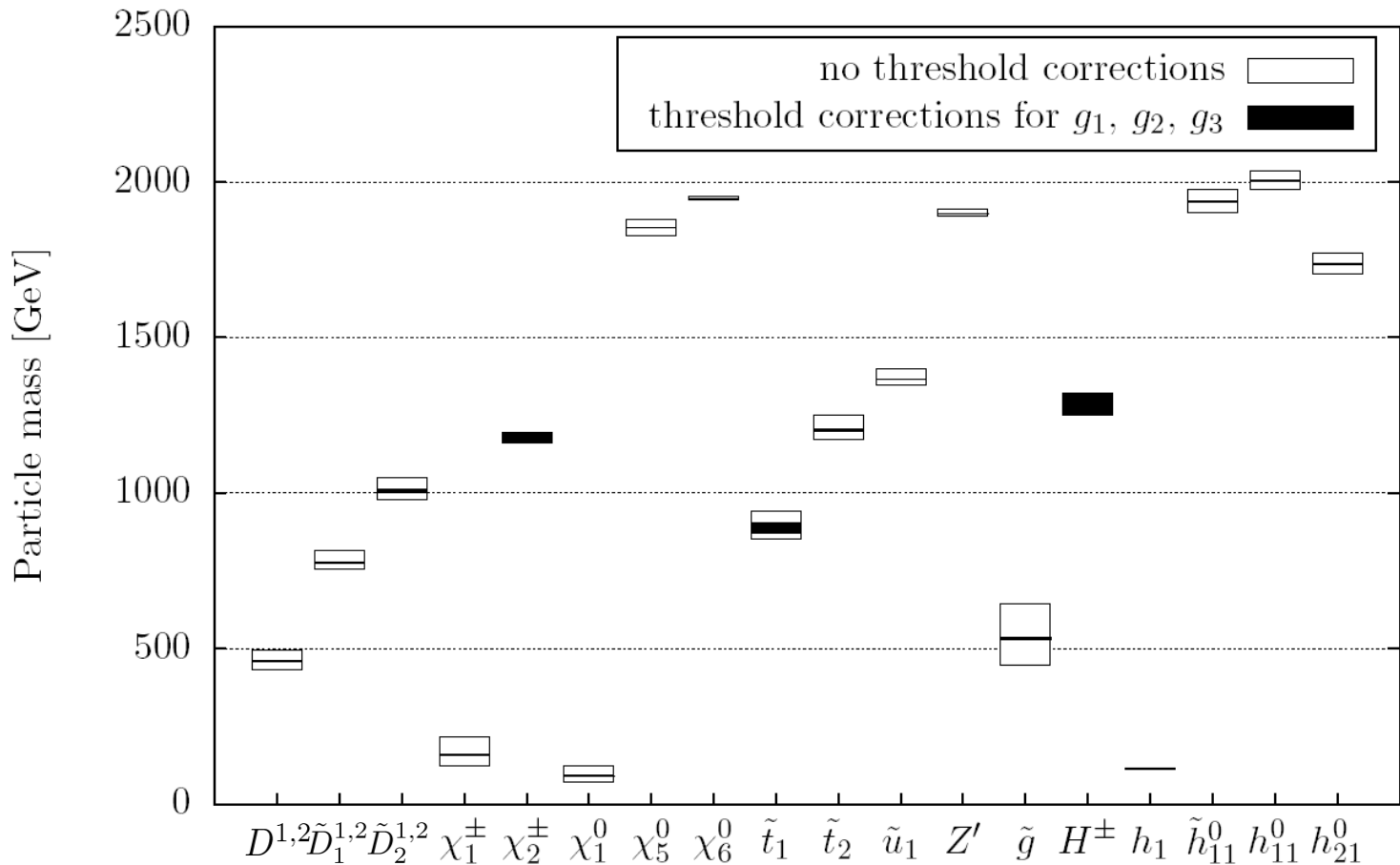
Integrated out fermions

Integrated out scalars

Integrated out gauginos







- Threshold Corrections important for precision.
  - Individual sparticle thresholds included for gauge couplings.
  - Large reduction in threshold scale dependence.
  - Residual dependence from Yukawa thresholds (coming soon)

# Conclusions

- $E_6$  / extra U(1) SUSY models, (e.g.  $cE_6$ SSM) well motivated
  - $cE_6$ SSM investigated ,parameter space explored.
  - General prediction of heavy sfermions and light gluino
- Phenomenology of the  $cE_6$ SSM:
  - If light exotics can be copiously produced, viable scenarios shown .
  - $Z'$  can give rise to striking signatures. Impact of the exotics could be visible. Sfermions contribution low in considered point.

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  - Many other corrections, e.g. shifts to pole, two loop scalar mass RGEs...

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- Extracting  $cE_6$ SSM from data:
  - Extremely important if  $E_6$ SSM like signatures are observed.

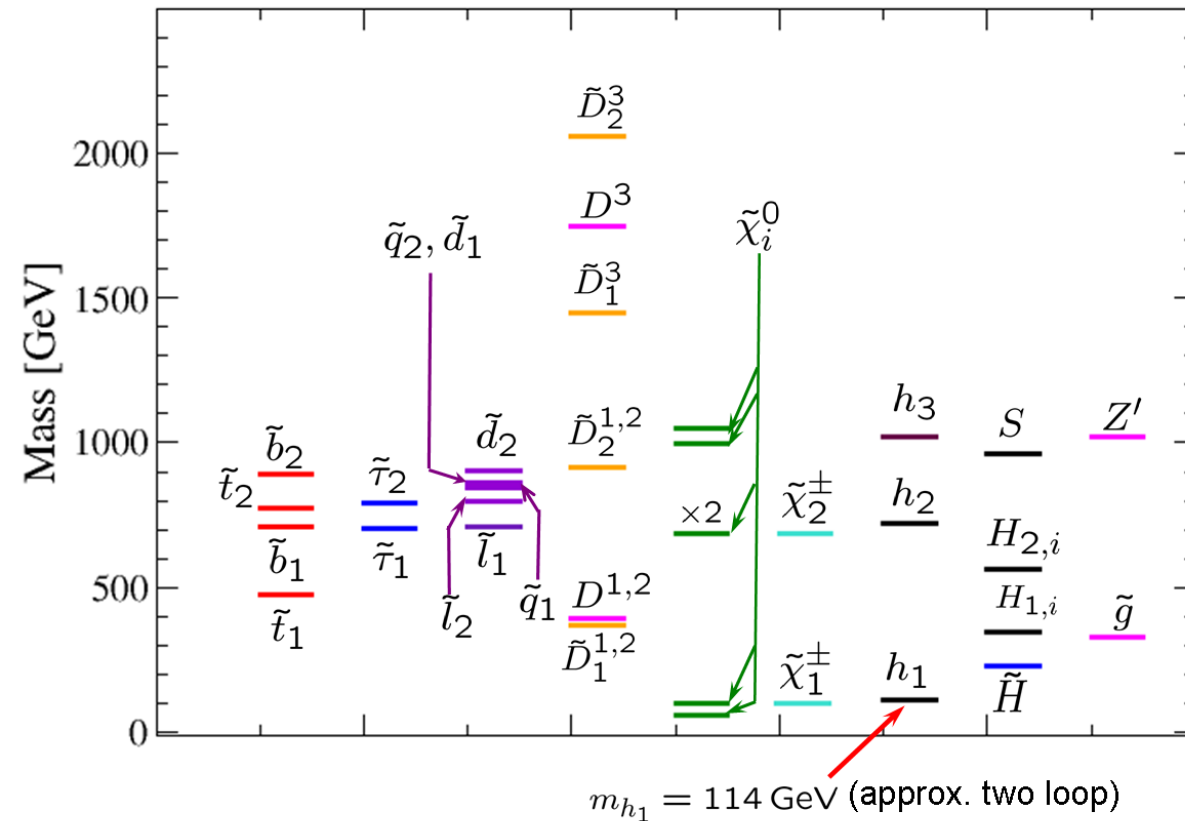
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  - Lots to do...work in progress...

**BACK UP SLIDES**

## Scenario (Light exotic fermions and scalars)

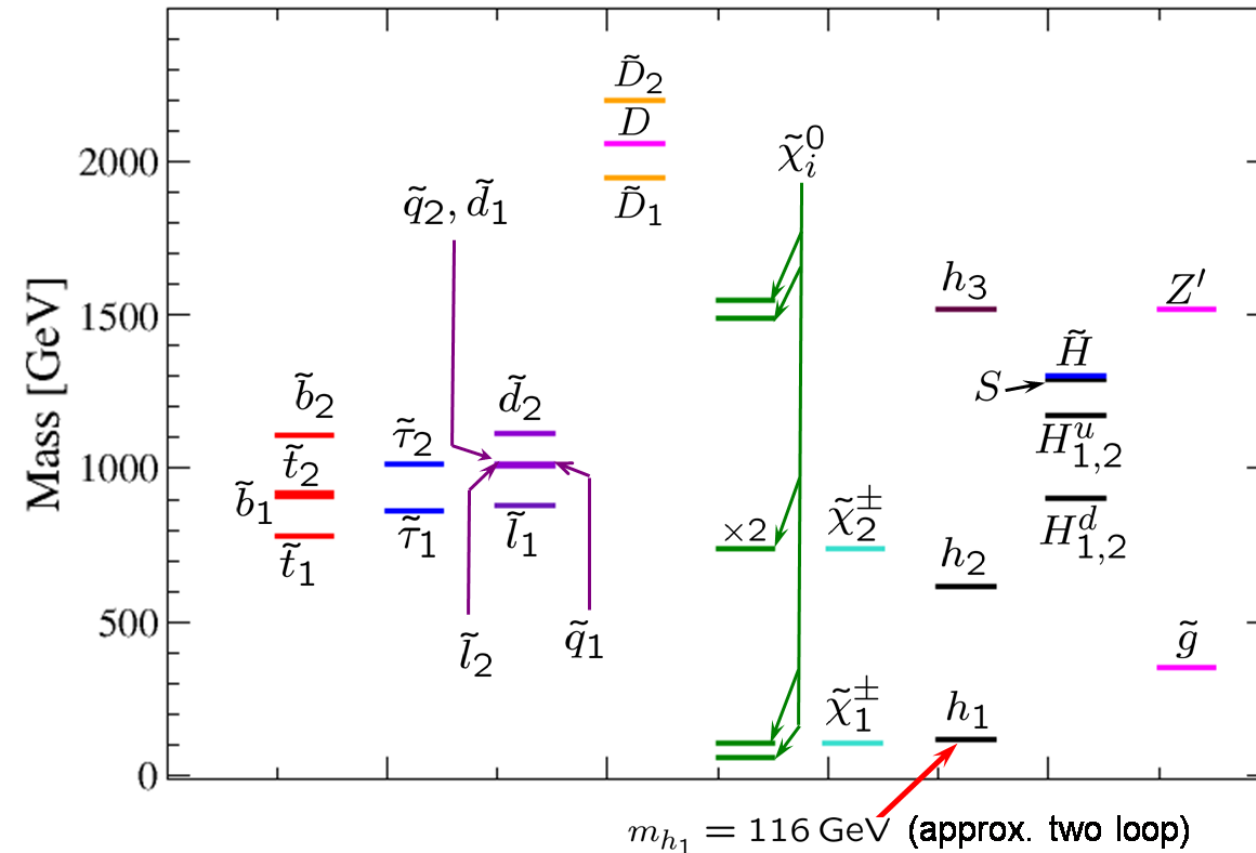
- Large  $\kappa$  drives electroweak symmetry breaking
- With a universal exotic coupling  $\kappa$  at the GUT scale  
 $\Rightarrow$  exotic quarks are always heavy ( $\mu_D = \frac{\kappa_i(M_S)}{\sqrt{2}} s$ )
- Break  $\kappa$  universality and exotic quarks can be light



$$\begin{aligned}
 \tan \beta &= 10, \\
 s &= 2.7 \text{ TeV}, \\
 M_{1/2} &= 358 \text{ GeV}, \\
 m_0 &= 623 \text{ GeV}, \\
 A &= 757 \text{ GeV} \\
 \lambda(M_X) &= -0.40, \\
 \lambda_{1,2}(M_X) &= 0.1 \\
 \kappa_{1,2}(M_X) &= 0.08, \\
 \kappa_3(M_X) &= 0.43
 \end{aligned}$$

**Caution:** It is possible all the exotics are heavy and challenging to detect, e.g.

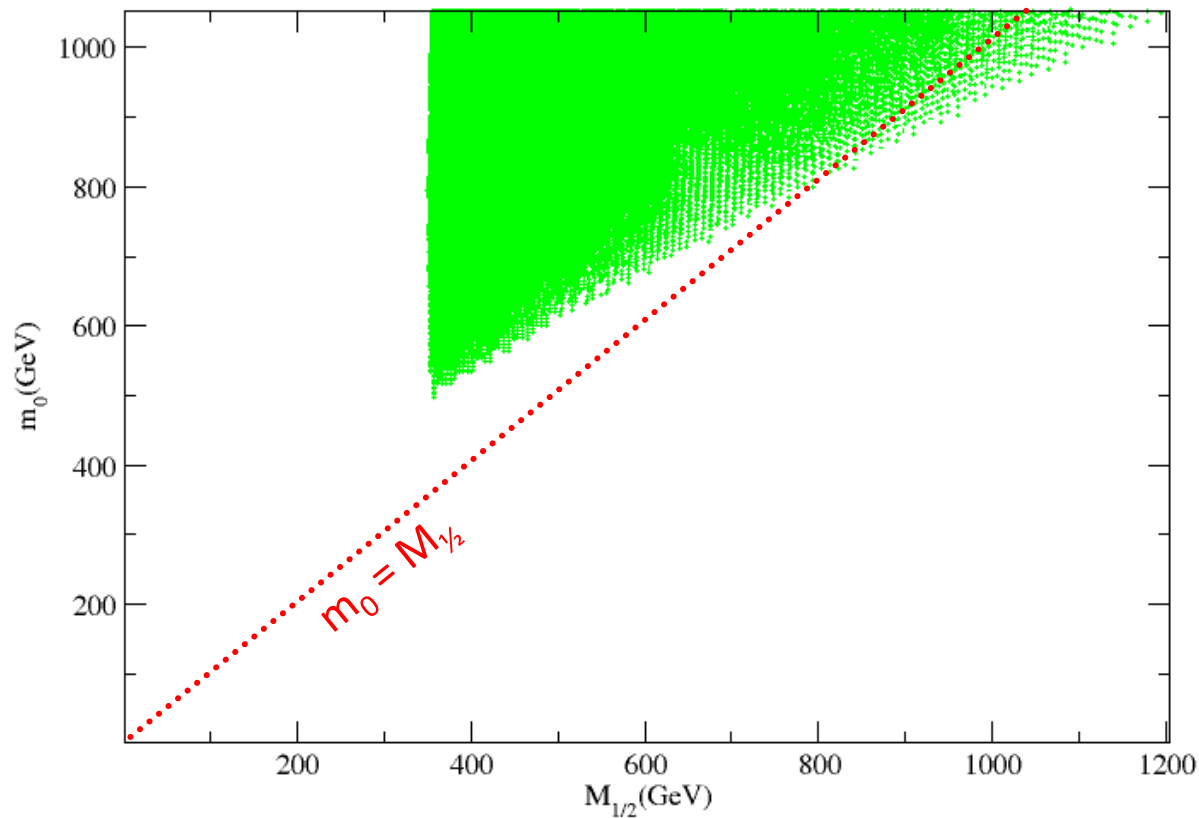
**Scenario B** (Pessimistic)



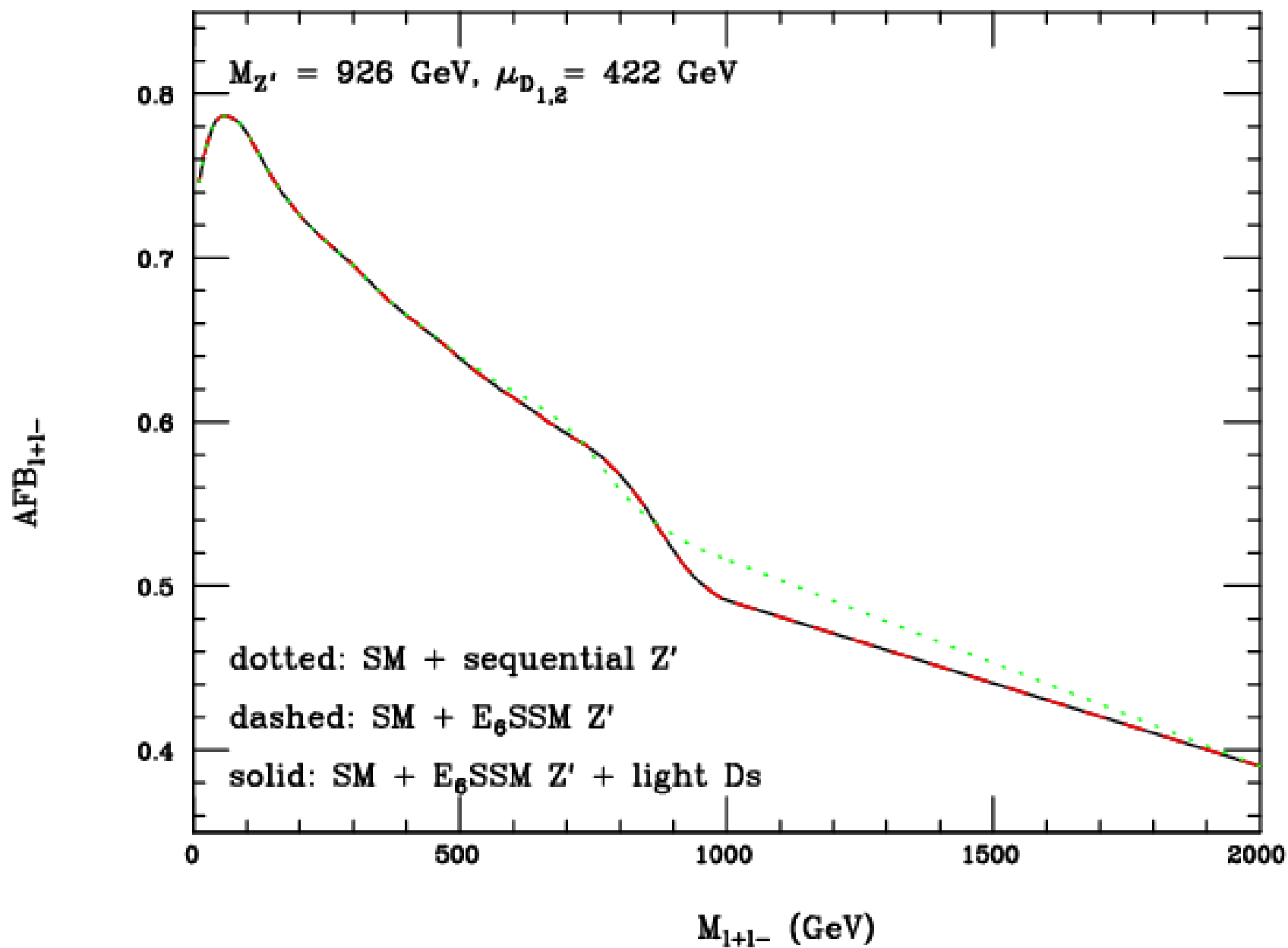
$$\begin{aligned}
 \tan \beta &= 10, \\
 s &= 4.0 \text{ TeV} \\
 M_{1/2} &= 389 \text{ GeV}, \\
 m_0 &= 725 \text{ GeV}, \\
 A &= -1528 \text{ GeV} \\
 \lambda(M_X) &= -2.0, \\
 \lambda_{1,2}(M_X) &= 2.6 \\
 \kappa_{1,2,3}(M_X) &= 2.5,
 \end{aligned}$$

## Allowed regions in the $m_0 - M_{1/2}$ plane

Fix  $\tan \beta = 10$ ,  $\lambda_{1,2} = 0.1$ , vary  $\lambda_3$  and  $\mu = \mu_{1,2,3}$  and  $s$ :



**Note:** since  $m_0$ ,  $M_{1/2}$  are derived, some possible regions are sparsely populated



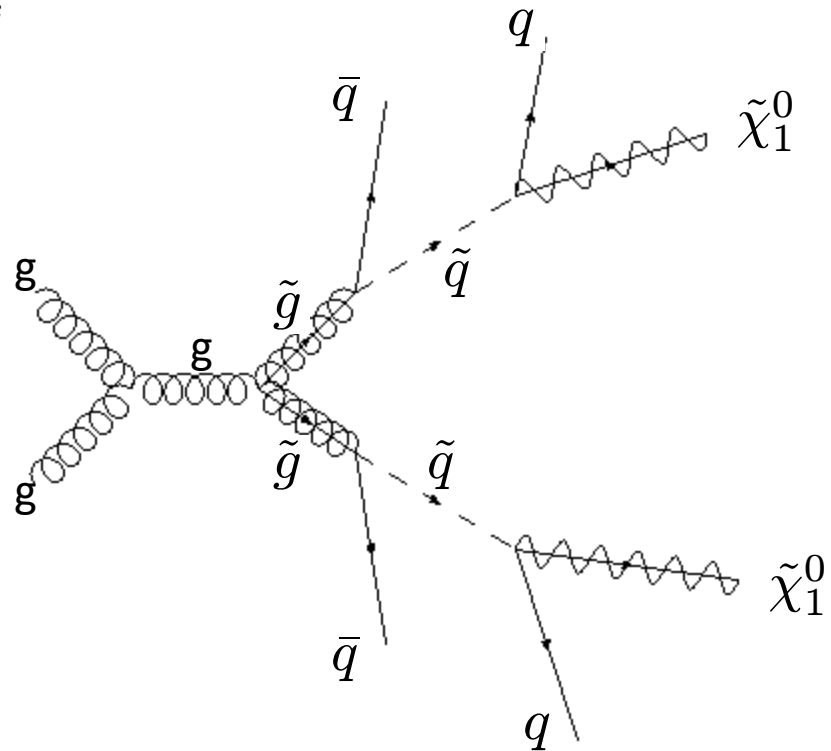
- It is possible all the exotics are heavy and challenging to detect
- Even in such a scenario there is still a striking prediction, which is a general result of the cE<sub>6</sub>SSM.

- All spectra have a clear hierarchy
- Gluino is lighter than all sfermions of ordinary matter
- Strong contrast with typical MSSM scenario
- Result of the RGE evolution

➤ Decay  $\tilde{g} \rightarrow \bar{q}\tilde{q}^* \rightarrow q\bar{q} + E_T^{Miss}$

➤  $\Rightarrow$  Appreciable enhancement of:

$$pp \rightarrow q\bar{q}q\bar{q} + E_T^{Miss} + X$$



# E<sub>6</sub>SSM Superpotential

- Imposing  $Z_2^{B/L}$  and  $Z_2^H$

$$\begin{aligned}
 W_{E_6SSM} \rightarrow & \lambda_i \hat{S}(\hat{H}_{1i} \hat{H}_{2i}) + \kappa_i \hat{S}(\hat{D}_i \hat{\bar{D}}_i) + f_{\alpha\beta} \hat{S}_\alpha(\hat{H}_d \hat{H}_{2\beta}) \\
 & + \tilde{f}_{\alpha\beta} \hat{S}_\alpha(\hat{H}_{1\beta} \hat{H}_u) + \frac{1}{2} M_{ij} \hat{N}_i^c \hat{N}_j^c + \mu'(\hat{H}' \hat{\bar{H}}') \\
 & + h_{4j}^E(\hat{H}_d \hat{H}') \hat{e}_j^c + h_{4j}^N(\hat{H}_u \hat{H}') \hat{N}_j^c + W_{MSSM}(\mu = 0)
 \end{aligned}$$

- To ensure only 3<sup>rd</sup> gen. gets vevs, we choose:

$$\kappa_i \sim \lambda_3 \geq \lambda_{1,2} \gg f_{\alpha\beta}, \tilde{f}_{\alpha\beta}, h_{4j}^E, h_{4j}^N.$$

- Further integrating out super heavy, right handed neutrinos, and dropping  $\mu'$  which decouples, leaves:

$$\begin{aligned}
 W_{E_6SSM} \approx & \lambda_i S H_{1,i} H_{2,i} + \kappa_i S D_i \bar{D}_i \\
 & + h_t H_u Q t^c + h_b H_d Q b^c + h_\tau H_d L \tau^c
 \end{aligned}$$